# QoT-Aware Optical Amplifier Placement in Filterless Metro Networks

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Abstract-Filterless Optical Networks (FONs) represent a novel cost-effective solution for metro optical networks, that allows to achieve equipment-cost savings by removing expensive optical-switching components from network nodes. In this study, we investigate how to further reduce equipment cost in FONs by minimizing amplifiers' cost. We propose a Genetic Algorithm (GA) for placing boosters, inline amplifiers and pre-amplifiers in FONs with the objective of minimizing amplifiers cost. We provide two versions of the GA and compare their performance against a baseline amplifier placement in terms of amplifiers cost and quality-of-transmission (QoT), i.e., lightpaths OSNR and received power. Moreover, we provide a comparison between filterless and wavelength-switched architectures. Simulative results achieved over realistic network topologies show significant amplifier cost savings, up to 60% compared to baseline approaches. Index Terms—Filterless Optical Networks, Optical Amplifiers,

Cross-layer Design

## I. INTRODUCTION

Filterless Optical Networks (FONs) are emerging as a promising technological direction to reduce cost in optical networks. In FONs, Reconfigurable Optical Add/Drop Multiplexers (ROADM), based on costly Wavelength Selective Switches (WSS), are replaced by broadcast-and-select switching architectures composed by passive splitters and combiners, which interconnect add/drop nodes via fiber trees [1]. However, due to channels' broadcast on unnecessary fiber links, FONs suffer a reduced spectral efficiency. Moreover, when amplifiers are deployed in FONs, the absence of WSSs causes propagation of Amplified Spontaneous Emission (ASE) noise beyond lightpath termination, and accumulation of ASE generated before a lightpath is initiated. Hence, FON architectures may become more sensitive to lightpaths degradation due to higher ASE noise compared to ROADM-based architectures (note that ROADMs contain WSSs, i.e., filters, that block unintended ASE accumulation). FONs have been already standardized and deployed as shown in [2]. In particular, FON deployment has attracted particular interest for metro networks [3] based on ring/horseshoe topologies. In metro, network operators, in the attempt to minimize network cost, are more prone to consider node architectures without WSSs, especially taking into account the high number of nodes in a metro network. Moreover, taking advantage of relatively short metro distances, operators have the opportunity to optimize also the number (and location) of Optical Amplifiers (OAs) needed to guarantee lightpaths Quality-of-Transmission (QoT). Hence, an optimized deployment of amplifiers is crucial to reduce

network cost and maintain lightpaths feasibility in FONs. An optimized deployment must consider different amplifier types, i.e., boosters, pre-amplifiers and in-line amplifiers (ILAs), considering their different characteristics in terms of gain and noise figure.

In this letter, we investigate how to minimize the cost of OAs in FONs, while maintaining lightpath feasibility, expressed as a minimum requirement in terms of end-toend OSNR and optical power at the receiver. We propose a Genetic Algorithm (GA) to perform OSNR-aware OA placement which considers the differences between boosters, preamplifiers and ILAs. Although the problem of OA placement has received attention for ROADM-based networks [4], [5], to the best of our knowledge, no study has been done in the context of filterless metro networks, where the presence of ASE accumulation makes solutions for OA cost minimization (as the one in [4], [5]) not applicable.







Fig. 2. a) Filterless node architecture and b) Example of channel broadcast and ASE accumulation in a filterless horseshoe topology

Note that while in [5] the OA placement is done through an iterative greedy-approach; the GA ensures a dynamic exploration of teh search-space. Moreover, considering FON nodes implies adapting the physical layer modeling to account for the ASE noise propagation beyond lightpath termination. We consider a practical case of a metro network composed by several interconnected filterless branches, where each branch is constituted by a horseshoe as shown in Fig. 1. These horseshoe topologies are becoming popular in metro aggregation networks [6] and typically contain two types of nodes: Terminal nodes (T-nodes) and Filterless nodes (F-nodes). T-nodes are interconnected to the rest of the metro network and equipped with filters that impede ASE noise propagation beyond them, and thus avoid creating laser loop effects due to the continuous propagation and amplification of the optical signal [7]. F-nodes that are placed along the optical line are equipped with passive splitters, combiners and Variable Optical Attenuators (VOAs)<sup>1</sup>. Fig. 2a shows the architecture of the filterless nodes considered in our study. To show the impact of ASE accumulation in a filterless horseshoe, consider the example in Fig. 2b. Two lightpaths are established on two different wavelengths, i.e., L1 between nodes T1 and F1 on  $\lambda_1$ , and L2 between nodes F1 and F2 on  $\lambda_2$ . The OA placed between nodes T1 and F1 (i.e., OA-A) introduces an ASE noise contribution (ASE-A), which propagates also beyond the filterless node F1 (dotted line) and accumulates with ASE-B generated by OA-B. Therefore, the overall ASE noise contribution (ASE-A and ASE-B) will propagate up to node T2 and, in particular, will affect the OSNR of lightpath L2.

## II. OPTICAL AMPLIFIER PLACEMENT IN FILTERLESS

# NETWORKS

# A. Problem statement

The problem of OA placement in filterless metro networks can be stated as follows: **Given** a horseshoe FON, a set of traffic demands (each characterized by source/destination nodes) and a set of candidate locations to place OAs, **decide** the OA placement (location ,i.e., booster, pre-amplifier and ILA) and decide the route and spectrum allocation (RSA) for each traffic demand, **constrained by** a required QoT for each lightpath (OSNR and received power thresholds), spectrum continuity and contiguity constraint, network capacity constraint, with the **objective** of minimizing the overall cost, constituted by the deployed OAs.

### B. Genetic Algorithm for OA placement

Due to high combinatorial complexity of the problem (considering x OA candidate locations, there are  $2^x$  combinations of OA placement) and, its non-linear nature which requires to consider several cross-layer design parameters, we have developed a Genetic Algorithm (GA) to solve this problem. The evolutionary process of the GA is driven by competition among members (solutions) of the population and genetic operations, such as mutation and crossover. Each solution of the population is encoded as a string of binary values, i.e., the genes, which represent the candidate locations for OA placement, and assume value "1" if an OA is placed and "0" if the OA is not placed. In Fig.3a, we show an example of encoding the placement of OAs for two members of the



Fig. 3. a) Encoding of OA placement in a string of 1s and 0s; b) crossover and mutation operations and c) flowchart of the proposed solution for optimized OA placement population, noted as I) and II). We show the two members

population, noted as 1) and 11). We show the two members (*chromosomes*) as strings of 1s and 0s in Fig.3b (*selection*). A crossover point (dashed line) is randomly selected and the latter parts of the two members are swapped (*crossover*). A gene for each member is randomly selected and its value is inverted (*mutation*). Note that a cost value is reported for each member and the cost change due to crossover and mutation is reflected in each step. Each solution is characterized by its fitness value and feasibility status. Let us now define the fitness and feasibility of a solution: The fitness of a member of the population is determined by a cost function accounting for the type (set T) and location (set L) of the placed OAs. We define the fitness of a solution as the sum of costs of placed OAs:

$$fitness = \sum_{l \in L} \sum_{t \in T} (OA_l * C_{l,t}) \tag{1}$$

where  $OA_l$  is a binary variable equal to 1 if an OA is placed in location l and 0 otherwise, while  $C_{l,t}$  is the cost of an OA of type t placed in location l (OA costs are reported in Sec.III). A lower fitness value is desirable as we minimize the total cost of OAs. Feasibility represents the extent to which a solution satisfies the constraints and is a real number between 0 and 1. We define feasibility f as the ratio between the total number

<sup>&</sup>lt;sup>1</sup>The VOAs match/attenuate the channel powers according to the channel with the lower power level, thus regulate the power of optical channels.

of lightpaths (LP) that are feasible (set J) to the total number of lightpaths routed (set I):

$$f = \sum_{j \in J} LP_j / \sum_{i \in I} LP_i \tag{2}$$

A lighthpath *i* is feasible if it meets the QoT requirements, i.e., the total OSNR (which also comprises the non-linear noise from the GN-model [8]) and received power ( $P_{rec}$ ) constraints ( $OSNR_i > threshold$  and  $P_{rec,i} > threshold$ , as defined in Eq. (5) and (6) in [5]). A solution is feasible if all lightpaths meet QoT requirements (thus f = I), whereas a solution is unfeasible if there is at least one lightpath in set *I* which does not meet the OSNR and/or  $P_{rec}$  constraint (f < I).

In Fig. 3c we show the flowchart of the proposed solution, which performs RSA of traffic demands first and then OA placement. In the following, we elaborate on the main building blocks of the GA (highlighted text in bold), namely the *Tournament selection policies, Tournament rules, "stuck" state* and *stopping condition.* 

The GA starts the search by generating an initial population as a random set of solutions while new populations are generated according to tournament selection policies. Tournament selection policies define the pairs of solutions to participate in the tournament. If no feasible solution has been found yet, the solution which provides the highest number of feasible demands is defined as the current best solution. Until no feasible solution has been found, members of the population are sorted in two groups: A) solutions close to current best solution and B) all other solutions. The set of solutions in group A depends on how close is the current best solution to reach feasibility of all lightpaths (i.e., f = 1). For example, if the current best solution has a f = 0.7, then 5% of the best solutions are sorted in group A or if f = 0.9, then 1% of the best solutions are sorted in group A. In principle, the closer to a feasible solution, i.e., f = 1, the lower is the % of best solutions sorted in group A. We consider solutions from group A to participate in the tournament 70% of the time, whereas solutions from group B, 30% of the time.

Once the GA starts finding feasible solutions, members of the population are sorted in three groups: A) feasible solutions with a low fitness value, B) feasible solutions with a high fitness value C) unfeasible solutions with a f > 0.95 and a low fitness value. We consider a solution to have a low (*high*) fitness value if it is not 5% (25%) higher than the best solution found so far. Solutions from group A participate in the tournament 70% of the time, solutions from group B, 20%, and solutions from group C, 10% of the time. We have fine-tuned the tournament selection policies based on the performance of the GA so that it converges quickly, i.e., in a few generations. Tournament rules are defined as follows: i) a feasible solution wins over an unfeasible solution; *ii*) if two feasible solutions compete, the solution with the lower fitness wins and iii) if two unfeasible solutions compete, the winner is chosen at random. New generations are created by performing genetic operations (crossover and mutation) on tournament winners. In case there is no improvement of the fitness function after a finite number of generations, we consider the GA to be in a "*stuck*" state. In this case, all feasible solutions which have a *low* fitness value are deleted in order to restart the search process and try to escape the local minimum. If there is no improvement of the fitness value for 15 generations, the GA reaches a local optimum, i.e., "stuck" state. The stopping condition for the GA is reached if there is no improvement for a number of generations equal to twice the number of genes. Therefore, if the GA has reached the "stuck" state and there is no improvement for twice the number of genes generations, then the GA stops the search. Note that the GA may find several best-cost solutions, however, in our results we show only the solution with the highest minimal OSNR (minOSNR).

We propose two versions of the GA, *minCostGA* and *ConstrainedGA*. Since the objective of *minCostGA* is to minimize cost, this may lead to a drawback on the OSNR performance. *ConstrainedGA* overcomes the drawbacks of *minCostGA* and aims at minimizing the OA cost while guaranteeing the OSNR performance provided by the benchmark approaches. While *minCostGA* is constrained to a minOSNR equal to 13 dB, *ConstrainedGA* is constrained by the minOSNR achieved by the benchmark approach, i.e., OSNR threshold is set equal to minOSNR of benchmark.

#### **III. ILLUSTRATIVE NUMERICAL RESULTS**

In our numerical evaluation, we compare different technologies (FON vs WSON) considering horseshoe topologies of different lengths and with different number of nodes. As FON and WSON have different node architectures, T-nodes, considered in WSON are assumed to introduce a 17 dB loss whereas F-nodes, considered in FON introduce a 13 dB loss (additional 4 dB loss in T-nodes may lead to deploy more OAs in WSON compared to FON containing F-nodes). Note that the add/drop path introduces half of the node loss, e.g., 6.5 dB loss in FON. We model optical nodes loss as an equivalent fiber span loss generated in a fiber with length equal to 68 km and 52 km for T-nodes and F-nodes, respectively. Note that, we consider that no non-linear interference (NLI) is generated in the fiber span mimicking the node. We assume Standard Single-Mode Fiber (SSMF) with attenuation coefficient of 0.25 dB/km. We consider the placement of two types of OAs that differ in terms of gain<sup>2</sup> (G) and noise figure (NF). Booster OAs are characterized by a G range of (10-20) dB and a NF range of (6-12) dB, while pre-amp OAs by a G range of (18-32) dB and a NF range of (6.2-10.5) dB<sup>3</sup>. We consider the placement of OAs in three possible locations: i) at the ingress of the node (for pre-amplifiers), *ii*) at the egress of the node (for boosters) and *iii*) along the fiber (for inline amplifiers, which have the same characteristics of boosters). We assume the cost of a booster is 1 cu (cost unit) while the cost of a pre-amplifier is 1.2 cu. If deployed as an ILA, the cost of an OA assumes an additional 0.8 cu accounting for the deployment, maintenance and management of the cabinet/location (e.g., therefore, the cost of a booster type deployed as an ILA is  $1.8^4$ ). In all our

<sup>&</sup>lt;sup>2</sup>We assume a flat OA gain profile due to the use of gain flattening filters.

<sup>&</sup>lt;sup>3</sup>Note that a high NF corresponds to a low G and vice-versa.

<sup>&</sup>lt;sup>4</sup>SM-Optics, private communication

			MINIMUM (AVE	TABLE II           MINIMUM (AVERAGE) OSNR VALUES IN [DB] FOR THE 6-NODE HORSESHOE TOPOLOGY						
TABLE I Cost of GA vs BF [ <i>cu</i> ]		I 5 BF [ <i>cu</i> ]	Strategy	100 km	300 km	500 km	700 km	900 km		
CL	GAcost	BFcost	minCostGA-FON ConstrainedGA-FON	19.24 (25.89) 22.73 (28.32)	14.05 (18.02) 20.39 (23.70)	13.39 (16.13) 19.22 (22.50)	13.52 (15.73) 18 49 (21.54)	13.41 (15.46) 17.89 (20.83)		
24	18.0	18.0	minCostGA-WSON	16.15 (24.57)	13.99 (20.45)	13.54 (18.22)	13.36 (17.71)	13.44 (17.57)		
30	18.6	18.0	CostrainedGA-WSON	21.68 (27.03)	19.98 (24.47)	18.83 (23.32)	18.17 (22.68)	17.66 (22.01)		
36	18.6	18.0	Baseline-FON Baseline WSON	21.40 (23.59)	20.11 (22.34)	18.91 (21.15)	18.15 (20.39)	17.57 (19.83)		
			basenne-wson	21.15 (23.09)	19.74 (25.75)	18.04 (22.04)	17.95 (21.94)	17.39 (21.41)		



Fig. 4. OAs total cost for FON, WSON and Baseline as a function of total horseshoe length (km)

simulations we consider a full-mesh traffic matrix, 100 Gbps transceivers using DP-QPSK for each demand, occupying 37.5 GHz optical spectrum. To guarantee satisfactory signal reception (i.e., "lightpath feasibility"), a minimum 13 dB OSNR and a -18 dBm received power are required.

#### A. GA validation

To validate the effectiveness of the GA, given the strong non-linearity of the problem, we consider a truncated bruteforce (BF) approach on a small topology, exploring all possible OA placement solutions considering the solution provided by the GA as an upper-bound. In Tab. I we compare GA and BF performance in terms of cost for a 4-node horseshoe with 3 bidirectional links, varying the number of OA candidate locations (CL) for a total horseshoe length of 360 km. The BF achieves cost savings up to 3.2% compared to the GA, however it takes days to solve even for these limited cases.

## B. Numerical results and discussion

We now evaluate our GA in larger and more realistic network scenarios. We consider two horseshoe topologies, consisting of 6 and 11 nodes, which correspond to 5 and 10 bidirectional fiber links, respectively. We consider a candidate OA location every 10 km of fiber and booster and pre-amplifier candidate locations at each node. The number of OA CLs varies with the horseshoe length. The length of the horseshoe is varied, simulating small metro (100 km) and regional metro (900 km) networks. Results are averaged for each horseshoe length by considering 20 topologies with random link lengths with a variability of +/-50% from the average length of a link. For example, a horseshoe of length 300 km with 5 links, the average link length is 60 km so each link's length is equal to a random value between 30 km and 90 km. For these two network case studies, we compare five approaches: the minCostGA (i.e., minCostGA-FON and minCostGA-WSON in the figure) and ConstrainedGA (i.e., ConstrainedGA-FON and ConstrainedGA-WSON in the figure) against the Baseline OA placement. Recapping: minCostGA, finds the minimum-cost solution and represents a lower-bound in terms of the cost of OAs while ensuring that the minOSNR of the lightpaths meets the required threshold. ConstrainedGA, aims at minimizing OA cost while guaranteeing minimal OSNR values for all lightpaths which are higher or equal to the values provided by the Baseline strategy.

As a benchmark strategy, we consider a baseline OA placement (intended to represent current OA placement strategy) working as follows: i) all nodes are equipped with preamplifiers and boosters (booster OA gain is set to compensate for the node loss and pre-amp gain set to compensate for the span it terminates), and ii) inline amplifiers are placed every 60 km (considering OA gain set to compensate span losses, this corresponds to gain of 15 dB in all ILAs). In Fig. 4 we report the results obtained for the two topologies, showing the OA cost (in *cu*) for the cases of filterless network (FON) and WSS-based wavelength-switched optical network (WSON).

**minCostGA vs Baseline**: Results show significant savings in total OA cost achieved by GA in comparison to the baseline approach<sup>5</sup>. Specifically, the savings range between 45% and 60% for the 6-node topology and between 45%and 59% for the 11-node topology for the filterless horseshoe scenario (*minCostGA-FON* vs Baseline). Similarly, savings for *minCostGA-WSON* compared to Baseline between 42%to 52% for the 6-node topology and between 35% and 55%for the 11-node topology are achieved. These results confirm that relevant OA cost savings can be achieved in metro filterless networks. Even though *minCostGA* provides significant savings in total OA cost, OSNR performance of *minCostGA* 

Tab. II shows the minimal and average OSNR of lightpaths for the 6-node topology considering minCostGA-FON, minCostGA-WSON and the Baseline-FON and Baseline-

<sup>&</sup>lt;sup>5</sup>Note that Baseline deployment is the same for FON and WSON

WSON. We observe that Baseline-FON provides a better OSNR performance with a minOSNR (avgOSNR) up to 6.06 (5.02) dB higher compared to *minCostGA-FON*. Similarly, Baseline-WSON provides a higher minOSNR (avgOSNR) up to 5.76 (4.42) dB compared to *minCostGA-WSON*.

1) <u>ConstrainedGA vs Baseline</u>: We now observe the performance of *ConstrainedGA* that still targets OA cost savings, but constraining the GA in such a way that OSNR is guaranteed to be at least as in the Baseline case.

Fig. 4 shows that *ConstrainedGA-FON* achieves cost savings ranging between 31% and 56% for the 6-node topology and between 32% and 59% for the 11-node topology compared to *Baseline-FON*. Similarly, *ConstrainedGA-WSON* achieves cost savings between 26% and 41% for the 6-node topology and between 19% and 54% for the 11-node topology, compared to *Baseline-WSON*. *The minimal and average OSNR* values for *ConstrainedGA* shown in Tab. II are now higher compared to Baseline achieving higher values up to 1.33 (4.73) dB in terms of minOSNR (avgOSNR) in FON and 0.53 (1.94) dB in WSON. In conclusion, *ConstrainedGA* is capable of achieving significant OA cost savings while ensuring higher OSNR compared to baseline OA deployment.

2) <u>FON vs WSON</u>: Let us now observe the different deployment of OAs for FON vs WSON. In terms of total cost of OAs, *minCostGA-FON* ensures savings between 6% and 21% compared to *minCostGA-WSON* for the 6-node topology and between 10% and 21% for the 11-node topology. *ConstrainedGA-FON* ensures savings between 7% and 25% compared to *ConstrainedGA-WSON* for the 6-node topology and between 10% and 30% for the 11-node topology. These results confirm that FON leads to a significant reduction in total OA cost in metro networks.

Regarding the minimal and average OSNR of lightpaths for the 6-node topology, results for FON vs WSON are shown in Tab. II. We observe that: i) minOSNR is lower in WSON compared to FON and *ii*) avgOSNR is lower in FON compared to WSON. AvgOSNR is lower in FON compared to WSON because ASE noise accumulation has a higher impact in FON, i.e., more lightpaths are affected by the propagated ASE noise beyond lightpath termination. Instead, minOSNR is lower in WSON because minOSNR is experienced on the longest path, i.e., the path between the two furthest nodes in the case of a horseshoe, for this path, the ASE noise and NLI contributions are the same along the fiber spans (if the OA placement is the same, e.g., Baseline). However, the higher node loss in WSON leads to a higher ASE noise generated by the OA following the node, e.g., booster OA, therefore, the higher node loss in WSON is the decisive factor why minOSNR is lower in WSON compared to FON.

Finally, we confirm that, due to the channel broadcast feature, FONs has a higher spectrum occupation in comparison to WSONs. Specifically, FONs occupy 36% (43%) more spectrum compared to WSONs for the 6-node (11-node) topology. *C. Sensitivity analysis: OA Gain Ripple* 

We perform a sensitivity analysis on the robustness of solutions provided by GA, accounting for the unpredictable

TABLE III PROBABILITY (p) OF MINOSNR BEING BELOW 13 DB DUE TO OA GAIN RIPPLE: P(MINOSNR <13DB) FOR 6-NODE 900 KM AND 500 KM TOPOLOGIES CONSIDERING MINCOSTGA, CONSTRAINEDGA AND BASELINE STRATEGIES

Strategy (horseshoe km)	Cost [cu]	minOSNR [dB]	р
minCostGA (900)	38	13.12	0.68
constrainedGA (900)	50.8	17.76	0.00
Baseline (900)	68.8	17.36	0.00
minCostGA (500)	22.6	13.71	0.26
constrainedGA (500)	31.2	18.81	0.00
Baseline (500)	43.6	18.78	0.00

variation due to OA gain ripple. We assume a uniform statistical variation in the OA gain with a variance of 1.5 dB and 1 dB for pre-amp and booster type, respectively. Provided the solution by the GA, we consider the variance of the OA gain a posteriori and repeat this simulation 1000 times in order to achieve a statistical confidence. For each GA solution we determine the probability that a solution is unfeasible due to OA gain variation. In Tab. III we report the probability (p) that minOSNR is below the OSNR threshold (13 dB) for the 6-node 500 km and 900 km topology for minCostGA, constrainedGA and Baseline solutions. While p is equal to 0.26 and 0.68 for 500 km and 900 km for minCostGA, constrainedGA and Baseline have a p equal to zero for both cases. The constrainedGA solutions not only achieve significant cost savings and meet the OSNR performance of the Baseline but also ensure that random fluctuations of OSNR due to gain ripple do not lead to unfeasible solutions. Due to page limitation, we do not report the analysis for other horseshoe lengths, however, we note that for 100 km and 300 km also minCostGA achieves p equal to zero.

In conclusion, we propose two versions of a Genetic Algorithm (i.e., *minCostGA* and *ConstrainedGA*) for OA placement in FON and WSON metro topologies and compare their performance against a Baseline OA deployment. We show that *minCostGA* can achieve up to 60% (55%) OA cost savings compared to Baseline for FON (WSON). Moreover, we show that *ConstrainedGA* achieves up to 59% (54%) OA cost savings for FON (WSON) while guaranteeing better OSNR performance compared to Baseline.

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