### MEAN-SHIFT ANALYSIS FOR IMAGE AND VIDEO APPLICATIONS

A THESIS SUBMITTED TO THE DEPARTMENT OF ELECTRICAL AND ELECTRONICS ENGINEERING AND THE INSTITUTE OF ENGINEERING AND SCIENCE OF BILKENT UNIVERSITY IN PARTIAL FULFILLMENT OF THE REQUIREMENTS FOR THE DEGREE OF MASTER OF SCIENCE

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#### ABSTRACT

#### MEAN-SHIFT ANALYSIS FOR IMAGE AND VIDEO APPLICATIONS

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In this thesis, image and video analysis algorithms are developed. Tracking moving objects in video have important applications ranging from CCTV (Closed Circuit Television Systems) to infrared cameras. In current CCTV systems, 80% of the time, it is impossible to recognize suspects from the recorded scenes. Therefore, it is very important to get a close shot of a person so that his or her face is recognizable. To take high-resolution pictures of moving objects, a pan-tiltzoom camera should automatically follow moving objects and record them. In this thesis, a mean-shift based moving object tracking algorithm is developed. In ordinary mean-shift tracking algorithm a color histogram or a probability density function (pdf) estimated from image pixels is used to represent the moving object. In our case, a joint-probability density function is used to represent the object. The joint-pdf is estimated from the object pixels and their wavelet transform coefficients. In this way, relations between neighboring pixels, edge and texture information of the moving object are also represented because wavelet coefficients are obtained after high-pass filtering. Due to this reason the new tracking algorithm is more robust than ordinary mean-shift tracking using only color information.

A new content based image retrieval (CBIR) system is also developed in this thesis. The CBIR system is based on mean-shift analysis using a joint-pdf. In this system, the user selects a window in an image or an entire image and queries similar images stored in a database. The selected region is represented using a joint-pdf estimated from image pixels and their wavelet transform coefficients. The retrieval algorithm is more reliable compared to other CBIR systems using only color information or only edge or texture information because the jointpdf based approach represents both texture, edge and color information. The proposed method is also computationally efficient compared to sliding-window based retrieval systems because the joint-pdfs are compared in non-overlapping windows. Whenever there is a reasonable amount of match between the queried window and the original image window then a mean-shift analysis is started.

*Keywords:* Mean-shift tracking, FLIR imagery, saliency detection, color histogram, content-based image retrieval.

### ÖZET

### RESİM VE VİDEO UYGULAMALARI İÇİN ORTALAMA DEĞER KAYMASI ANALİZİ

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Bu tezde imge ve video uygulamaları için analiz yazılımları geliştirilmiştir. Videoda hareketli nesnelerin takibi ve izlenmesi önemli uygulamaları olan bir problemdir. Örneğin, kapalı devre televizyon sistemi kullanan güvenlik uygulamalarında izleme yapan kameranın hareketli nesneye otomatik olarak odaklanması çok önemlidir. Çünkü olay çıkabilecek yerlere yerleştirilen her kamerayı izleyen bir güvenlik görevlisi yoktur. Hırsızlık olaylarında yapılan kayıtların %80'inde suç işleyenler tanınacak düzeyde değildir. Bu kayıtlardaki kişilerin yüzleri 20-30 oluşmakta ve bu suçluları tanımak mümkün olmamaktadır. Ayrıca enfraruj kameralarda da otomatik takip özelliği faydalı bir özelliktir. Bu tezde hareketli nesneleri otomatik olarak takip edebilecek bir algoritma geliştirilmiştir. Geliştirilen algoritma ve yazılım ortalama değer kayması metoduna dayalıdır. Ancak literatürde belirtilen metodlardan farklı olarak imgecikler arasındaki ilişkiler de göz önüne alınmıştır ve standart metodlardan daha üstün bir izleme yazılımı oluşturulmuştur. Hareket eden nesnenin komşu imgecikleri, kenar ve doku bilgisi arasında ki ilişkiler, yüksek-bant süzgeç işlemi sonucu elde edilen dalgacık katsayılarının kullanılması nedeniyle göz önüne alınmıştır. Dalgacık dönüşümü katsayıları kenar bilgilerini de içerdiğinden algoritma sadece renk histogramı kullanan algoritmalara göre daha dayanıklıdır.

Bu tez çerçevesinde ortalama değer kaymasına dayalı bir içerik tabanlı imge sorgulama metodu da geliştirilmiştir. Böyle bir sistemle sayısal video ya da imge kaydı yapılan bir ortamdan sorgulama yapmak mümkün olacaktır. Kullanıcı sorgulama yapacağı türden bir resmi ya da resim parçasını sisteme girecek sistem de sorgulanan resime benzer ya da onu içeren resimleri veri tabanından getirecektir. Sorgulama penceresinin içindeki resim parçasından ortakolasılık yoğunluk fonksiyonu dalgacık dönüşümü ve gerçek imgecikler kullanılarak oluşturulmaktadır. Hem renk, hem de kenar yoğunluğu bilgisi kullanıldığından sorgulama işlemi sadece renk bilgisi kullanan sorgulamalara göre daha güvenlidir. Arama işlemi veritabanındaki resimlerin üzerinden kayan bir pencere üzerinden değil de ortalama değer kayması kullanılacağından normalden hızlı olmaktadır.

*Anahtar sözcükler*: Ortalama değer kayması takibi, FLIR resim galerisi, belirginlik bulma, renk histogramı, içeriğe dayalı resim arama.

### Acknowledgement

I would like to express my gratitude to my supervisor Prof. Dr. Ahmet Enis Çetin for his instructive comments in the supervision of the thesis.

I would like to express my special thanks and gratitude to Assoc. Prof. Dr. Ezhan Karaşan and Asst. Prof. Uğur Güdükbay for showing keen interest to the subject matter and accepting to read and review the thesis.

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## Chapter 1

# Introduction

In this thesis, image and video analysis algorithms based on mean-shift analysis [1] is developed. Mean-shift analysis was applied to moving object tracking in video [2], image segmentation [2], image filtering [1], and Content Based Image Retrieval (CBIR) [23]. In above applications moving objects or image windows, or images are characterized by a probability density function (pdf) estimated from image pixel values. The estimated pdf is basically a normalized and smoothed version of the color histogram in color images, and gray level histogram in gray level images including infrared images.

Obviously, a color histogram of an object does not uniquely represent a given image object or a region. However, it is an efficient way of representing a given object because it is a one-dimensional function. In addition, it allows a given object change its shape over time in video. For example, a walking person changes its shape in video. On the other hand, his or her clothes and their colors do not change. Therefore, the color histogram can be used to characterize a walking person in video and many tracking algorithms using the color histogram were developed in the literature. On the other hand, color or gray level histogram (gray-level histogram) will not be an effective way of representing the object when the background has the same colors or similar colors (gray levels) as the moving object. This causes problems in tracking and the object can be lost by the tracking algorithm. Similarly, unrelated images having the same colors as the image to be queried can be retrieved by the content based image retrieval system.

In this thesis, a joint-pdf estimated from image pixels and their wavelet transform coefficients are used for object tracking and content based image retrieval. Since wavelet transform coefficients are obtained using a high pass filter wavelet coefficients capture the texture and edges in a given object or an image region. Additional information coming from the wavelet domain is essential to distinguish a moving object from the background. A special emphasis is given to gray-level Forward Looking Infrared (FLIR) images.

Similarly, a given query image is better described by using both the actual pixel values and corresponding wavelet coefficients representing the highfrequency content of the queried image. This leads to better results in CBIR applications.

In the next section we review the current object tracking methods. In Section 1.2, image processing algorithms used in content based image retrieval systems are reviewed

#### 1.1 Review of Object Tracking Methods

The object tracking problem in video is defined as finding the location of a given blob in the current frame. Usually, the blob is specified in the previous frame or in an initial image frame. The object is tracked in the video by keeping track of the locations of the blob over the video consisting of image frames.

The most straightforward approach of finding a given object in the current frame is based on correlating the pixels of the blob with the current image:

$$g(n,m) = \sum_{k,l} I_t(k,l) * I_{t-1}(n+k,m+l)$$
(1.1)

where  $I_t(k, l)$  represent the current image pixels,  $I_{t-1}$  are the pixels of the blob in the previous frame and the summation is carried out over the object pixels. The correlation function produces a maximum when the two objects overlap. Mean absolute deviation can be also used instead of correlation providing a computationally more efficient version of the correlation tracker. One of the main problems with this approach is that the object may change its shape while moving due to rotation, arm and leg movements, and/or bending etc. Another problem is that it is a brute force approach. The correlation function has to be estimated in a window and its maximum has to be determined in the window. The direction of the moving object cannot be estimated until the last step of maximum detection.

In mean-shift tracking the blob to be tracked is placed on the current image and a weight for each pixel is computed. The weights are simply the ratio of the probabilities of estimated histogram etc. For example, if the current pixel is not a part of the blob then its probability is zero and the corresponding weight is zero. If the current pixel is part of the original blob then the corresponding weight is a nonzero value. The first iteration of the mean shift procedure is completed by computing the center of mass of weights. The next iteration starts by placing the blob on the center of mass. It is proven by Comaniciu and Meer that this process converges. As described above the contribution of this thesis is the use of multi-dimensional joint-pdf instead of the color only based pdf estimated from the color histogram.

Recently, particle filtering [6] based moving object trackers are developed. However, particle filtering is computationally more expensive then mean shift tracking procedure. Particle filtering based approach also uses the probability density function to describe an object. It should be pointed out that the jointpdf approach proposed in this thesis can be also used in particle filtering based tracker as well.

#### 1.2 Mean Shift Tracking in CBIR

Content based image retrieval may find applications in video surveillance systems, medical image retrieval, and image-similarity based Internet browsing, etc. In CBIR systems, the user selects a portion of a given image or the entire image and tries to retrieve similar images from an image database [13]-[21]. In some systems the user sketches or paints an image of the object that he wants to retrieve [22]. In this thesis, we focus on image retrieving for image based queries.

The brute force approach is based on correlating the query image with images in the database to find similar images. If image sizes are different then the smaller image is correlated with other images in sliding windows. The mean-shift method was also used in content based image retrieval by Koubaroulis, Matas and Kittler [23]. Each image in the database is divided into non-overlapping windows and whenever there is some partial match the mean shift process is started and if the amount of match increases after mean-shift iterations then the image is accepted as a match. This approach is computationally more efficient than the brute force approach because the search windows do not overlap as in sliding window based approaches. As in standard mean-shift tracking the queried image is modelled using a color histogram or its smoothed versions estimated from the image pixels.

In this thesis, we use not only the color histogram but also the joint-pdf estimated from the image pixels and their wavelet coefficients. This approach produces more reliable retrieval results because both color, texture and edges are taken into account by the joint-pdf. The computational cost increases due to the use of a multi-dimensional pdf instead of a marginal color based pdf estimates. However the increase is not high because the dynamic range of wavelet coefficients is not high, e.g., wavelet coefficients corresponding to flat regions are zero due to high pass filtering.

### 1.3 Organization of the Thesis

The thesis is organized as follows: Chapter 2 includes mean-shift tracking of moving objects using multi-dimensional histogram in FLIR imagery and gives simulation examples. In Chapter 3, the methods used in content-based image retrieval systems are discussed. A CBIR method based on the color histogram and the corresponding image wavelet coefficients by using the mean-shift analysis is proposed and experimental results are presented. Finally, the thesis is concluded in Chapter 4.

### Chapter 2

# Mean-Shift Object Tracking in FLIR Imagery

Moving object tracking in video is a critical task in many applications including surveliance in CCTV systems, vision based human-computer interaction, and infrared imaging [2, 4, 3, 7, 8, 9]. Recently tracking the mean shift method became popular (see e.g., in [5]) and Yilmaz et al. [7] combined kernel tracking with global motion compensation for forward-looking infrared (FLIR) imagery.

The mean shift algorithm tracks objects in image sequences by using probability distributions describing the object. This means that the image data has to be represented as a probability distribution. In regular video, pdfs are estimated from color histograms to characterize the object. In FLIR videos, the ordinary mean shift method relies on the intensity distributions or smoothed histograms of the target region. It then estimates the location of the target in an iterative manner in the next image frame by comparing the intensity distributions. Since the original mean-shift method [2] is based only on the one-dimensional histograms constructed from the image intensity values it completely misses the texture information of the object. One-dimensional histograms approximating probability density functions (pdf) do not incorporate spatial relation of the image intensity values. This produces problems especially in small targets in FLIR sequences [7, 8] because the number of target intensity values are relatively small compared to large targets. In order to achieve a more realistic target modelling two-dimensional histograms or estimates of the two-dimensional probability density functions (pdf) are used to model targets in [7, 8]. In addition, the authors used an estimate of the pdf of the local standard deviation of the target region to highlight the low contrast between the target and the background in FLIR images. In [11], edges of the object are highligted by including an additional bit in the histogram characterizing the object. If there is a significant change in consecutive pixels then the additional bit is set to 1.

In this this, the two-dimensional image data is processed using a highpass filter to capture object features including edges on the object [12]. Let the random vector [x, xh] represent the original and highpass filtered version of the original image x. In this article, the histogram or the pdf of this vector is estimated and the tracking is carried out using the composite histogram which characterizes the object not only from the image pixels but also from the pixels of the high-pass filtered image. The main advantage of this approach over the regular intensity value based tracking is that the first entry captures the intensity information of the target and the second entry captures (i) the pixel intensity variation information, and (ii) hightlights the contrast between the target and the background around the edges of the target.

#### 2.1 Forward Looking Infrared Systems

Forward Looking Infrared (FLIR) is a night vision system that is used in many applications. FLIR systems have superior feature over the conventional night vision systems. It was originally developed for military purposes but today several civil applications such as law enforcement, fire fighting, governmental and commercial operations use these systems. FLIR was first used by military forces to identify the opposite forces. FLIR units measure the amount of infrared energy emitted by objects. Human eye does not see infrared energy but FLIR system senses and interprets that energy and converts to an image in complete darkness.



Figure 2.1: A comparison between the night vision camera and FLIR image.

FLIR systems do not provide a perfect image like the traditional night vision systems. It produces sufficient image to distinguish objects. Conventional night vision systems improve image quality by processing visible night. Therefore they need a minimal amount of available light to produce acceptable images. At that point, FLIR systems become more important under the conditions of very low visibility and full darkness as seen in Figure 2.1. FLIR can be an effective system for surveillance aims without using special lighting equipments since it measures thermal energy. It is also significant system for military forces. It has been adopted to aircrafts, naval vessels and ground vehicles during the last decade. Recently, its handheld versions have been manufactured.

FLIR systems are widely used in many areas as mentioned above. Therefore, motion detection and object tracking in FLIR system became a challenging task for researchers in recent years.

#### 2.2 Mean-Shift Object Tracking

Mean-shift tracking algorithm is an iterative scheme based on comparing the histogram of the original object in the current image frame and histogram of candidate regions in the next image frame. The aim is to maximize the correlation between two histograms.

Let x represent an image  $x : Z^2 - > \{0, 1, 2, ..., N-1\}$  where N is the dynamic range of the pixel values. Let O represent the support of an object. Let  $y_o$  be the center of mass of the support O which is a subset of  $Z^2$ . The histogram of the object O in image frame n is defined as follows

$$h_O(\ell) = \sum_{(n_1, n_2) \in O} \left( \delta(x(n_1, n_2) - \ell) \right)$$
(2.1)

where  $x(n_1, n_2)$  is the value of the  $(n_1, n_2)$ -th pixel of the image x,  $\delta(.)$  is the discrete Dirac-delta function, and  $\ell = 0, 1, 2, ..., N-1$ . The histogram is smoothed and normalized in several ways in [2]. In our work, an ordinary low-pass FIR filter is used to smooth the histogram.

In mean-shift tracking algorithm, histograms of regions are compared to each other using the Bhattacharya coefficient:

$$\rho(h_O, h) = \sum_{\ell} \sqrt{h_O(\ell)h(\ell)}$$
(2.2)

In the next image frame, the histogram of the same region is estimated and the following weights  $w(n_1, n_2)$  for each pixel in the region O in the (n+1)st frame are computed.

$$w(n_1, n_2) = \sum_{\ell=0}^{N-1} \sqrt{\frac{h_O(\ell)}{h(\ell)}} \left(\delta(x(n_1, n_2) - \ell)\right)$$
(2.3)

where  $h(\ell)$  represents the histogram of the region O in (n+1)st image frame of of the video. After this step, the center of mass  $\mathbf{y}_t$  of the weights are determined by:

$$\mathbf{y}_{\mathbf{t}} = \frac{\sum_{n_1, n_2} x(n_1, n_2) w(n_1, n_2)}{\sum_{n_1, n_2} w(n_1, n_2)}.$$
(2.4)

The histogram of the region centered at  $\mathbf{y}_t$  is computed and compared it to the original histogram using the Bhattacharya coefficient. If

$$\rho(h_O, h_{y_o}) < \rho(h_O, h_{y_1}), \tag{2.5}$$

then the first candidate region for the object in the (n+1)-st image frame is determined as the region centered at  $(y_o+y_1)/2$ . The above procedure is repeated until a satisfactory convergence level is reached. In practice, the average number of iterations is 5.

If a background subtraction based moving object detection method is used to determine the moving blobs in the image then the initial starting point of the iterations can be the blob determined by the background subtraction algorithm [10]. Mean-shift tracking iterations improve the accuracy of the detected region obtained using background subtraction.

#### 2.3 Image Feature Selection

The efficiency of the mean-shift tracking algorithm depends on how representative the choice of random variables discriminating an object. The original algorithm is implemented in color image sequences and it uses color information. In infrared image sequences there is only the intensity information and the histogram constructed from the intensity information may not be satisfactory to distinguish objects. In a FLIR image there may be image regions with similar intensity histograms and this makes tracker to loose the moving object.

The ultimate goal is to find a sufficient statistic whose distribution chracterizes the moving object in a unique manner. Since ordinary and FLIR images have no underlying statistical random process, it is almost impossible to define a sufficient statistic.

By using a high-pass filtered version of the image together with the actual image pixels the aim is to increase the discriminating capability of the meanshift tracker. Pixels of the high-pass filtered image can capture structure on the



Figure 2.2: FLIR image of a plane.

moving object including the edges.

In Figure 2.2, FLIR image of a plane is shown. The image shown in Figure 2.3 is a high-pass filtered version of this image. A high-pass filter with cut-off frequency at  $\pi/2$  is used. This image does not clearly reflect the edges of the object. In Figure 2.4, another high-pass filter with cut-off  $\pi/4$  is used. This image clearly shows the edges. Therefore, it is necessary to use a high-pass filter with a lower cut-off frequency to extract the image structure.

High-pass information can be incorporated into the histogram. Since the dimension of the data is doubled compared to pixel-only histograms, the dynamic range of the new histogram is  $N^2$ . In order to reduce the range the highpass filtered image is quantized to 4 levels, and this leads to a 4xN size histograms.

As it can be seen from the above images high-pass filtering captures (i) the pixel intensity variation information, and (ii) hightlights the contrast between the target and the background around the edges of the target. This makes the tracking algorithm more robust. Otherwise the histogram of the object shown in Figure 2.2 essentially contains a single peak around the mean value of the object region and this is not enough to uniquely determine the object.



Figure 2.3: High-pass filtered version of the above plane image. The cut-off frequency of the filter is  $\pi/2$ .

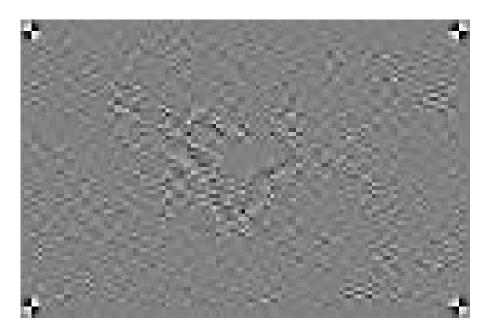


Figure 2.4: High-pass filtered version of the above plane image. The cut-off frequency of the high-pass filter is  $\pi/4$ .



Figure 2.5: A FLIR image from the web page: www.dii-llc.com.

In Figure 2.5, another FLIR image is shown. This image sequence is downloaded from the web page: www.dii-llc.com/FLIR\_multimedia.html. In this image there are edges within the object as well. Therefore it is important to include these features in the histogram characterizing the object in a unique manner. The highpass histograms of the plane in Figure 2.2 and the moving car in Figure 2.5 are shown in Figure 2.6-a and 2.6-b, respectively. The dynamic range of the graph in Figure 2.6-b is higher than Figure 2.6-a. As it can be seen from these graphs high-pass information provides additional information about the moving object. A composite histogram describing both regular pixel values and pixel values of the high-pass filtered image can be constructed in several ways. The easiest approach is to concatenate the normalized histograms of two images. In this case, the dynamic range of the concatenated histogram is 2N. One can also create a two-dimensional data set by combining the pixels of the two images. In this case, the dimension of the data is doubled compared to a pixel-only histogram, therefore the dynamic range of the new histogram is theoretically  $N^2$ . However, actual dynamic range of the high-pass filtered image is much smaller than dynamic range of intensity pixels. Quantized version of the high-pass filtered image pixels can be used. It is experimentally observed that 4 to 8 levels are found satisfactory, and this leads to a 4xN to 8xN size histograms. The

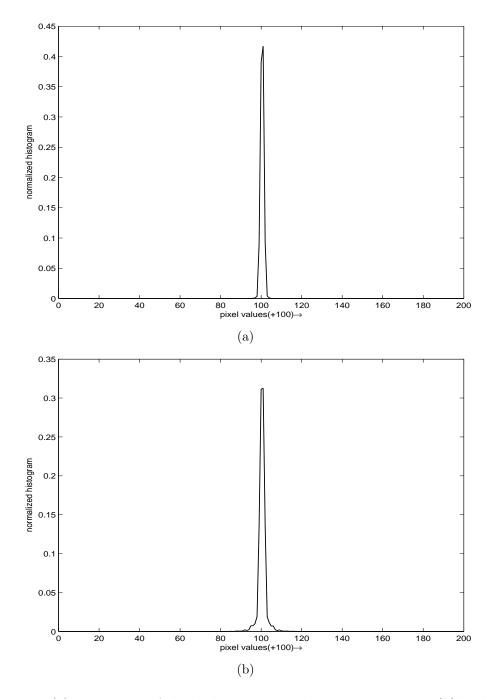


Figure 2.6: (a) Histogram of the highpass image shown in Figure 2.2, (b) highpass histogram of the moving car in Figure 2.5. Mean values of high-pass histograms are very close to zero. The variance of the histogram in part (b) is higher than the variance of the histogram in part (a). In the above plots, histograms are shifted by 100.

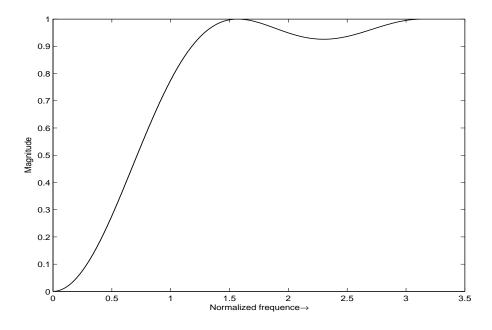


Figure 2.7: Frequency response of the high-pass filter at cut-off  $\pi/4$ .

second approach provides a more robust description of the object. This comes at the expense of additional computation. However, in both cases, the computational complexity does not increase drastically with the additional high-pass information in both approaches.

#### 2.4 Simulation Examples

The proposed tracking method was developed by MATLAB 6.5. It is tested for six FLIR image sequences downloaded from Internet. Due to military nature of FLIR imaging we could not get permission to use other image sequences in this thesis. The ordinary mean-shift tracking tracks the targets in four sequences successfully. Our method tracks them as well. But the ordinary mean-shift algorithm fails for the image sequences 1 and 2. Table 2.1 gives the number of frames tracked successfully by the ordinary mean-shift tracking and our method.

The car in the parking lot (Figure 2.5) from image sequence 4 can be also tracked very easily by both trackers using image pixels, and image and high-pass filtered image pixels because the background is not cluttered in this scene, either.

| Sequence | # of Frame | # of Frame Tracked | # of Frame Tracked |
|----------|------------|--------------------|--------------------|
|          |            | by Mean-Shift Alg. | by Our Method      |
| 1        | 25         | 11                 | 25                 |
| 2        | 57         | 6                  | 57                 |
| 4        | 29         | 29                 | 29                 |
| 4        | 10         | 10                 | 10                 |
| 5        | 49         | 49                 | 49                 |
| 6        | 35         | 35                 | 35                 |

Table 2.1: The number of frames tracked successfully by the ordinary mean-shift and the proposed scheme.

A couple of images showing the tracking is shown in Figure 2.10.

In Figure 2.11, the IR image of a walking man is shown. In this case, the ordinary mean-shift tracker fails to track the object as shown in Figure 2.11. It is clear that gray-scale pixel histogram is not enough to uniquely characterize the walking man in this case. On the other hand, the tracker using both the FLIR pixel and high-pass information successfully tracks the object as shown in Figure 2.12. The Bhattacharya coefficients are drawn in Figure 2.8 for both trackers in case of sequence 1 tracking. The Bhattacharya coefficient decreases (dotted) in Figure 2.8 when the ordinary mean-shift loses the tracking but the proposed method keeps the tracking.

The tracking of the plane in an airport (sequence 2) is the second example. In Figure 2.13, the ordinary mean-shift tracker fails to track the plane at frame 6. But the prosed mean-tracker continues to track the plane at frame 10 as seen in Figure 2.14.

In Figure 2.7 the frequency response of the FIR high-pass filter used in filtering the image is shown. This image is filtered both horizontally and vertically using the filter shown in Figure 2.7 to obtain the high-pass filtered image. The computational cost of filtering operation is low because the FIR filter has only 7 nonzero coefficients. To obtain the high-pass histogram there is no need to filter

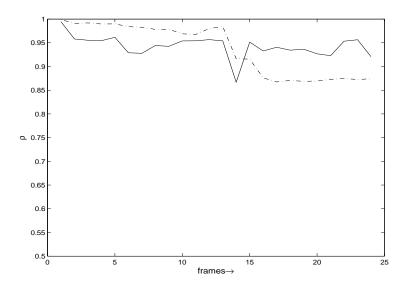


Figure 2.8: The Bhattacharya coefficients of the ordinary mean-shift (dotted) and the proposed method (solid) for image sequence 1.

the entire image frame. Only a window around the moving object is sufficient because means-shift tracker performs a local search to determine the next location of the object.

Another issue in the tracking based on mean-shift is the number of iterations. For example, iteration values per frame are depicted in Figure 2.9 for image sequence 1. The peak and average value is 7 and 2.95, respectively. These may be used to compute the required processing power in a real-time application.

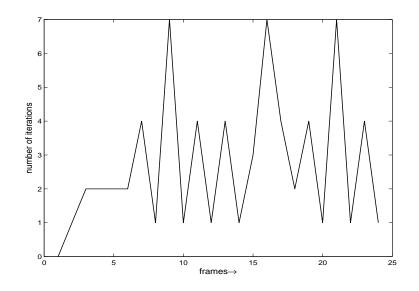


Figure 2.9: The iteration number of the proposed tracking method.

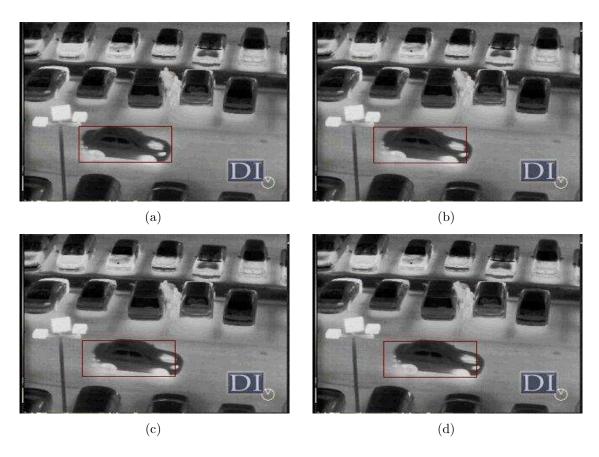


Figure 2.10: Tracking the car on the parking lot: (a) frame 1, (b) frame 3, (c) frame 5, and (d) frame 9.





(c)





Figure 2.11: Tracking the walking man with ordinary mean-shift: (a) frame 1, (b) frame 5, (c) frame 10, (d) frame 15, (e) frame 20, and (f) frame 25.







Figure 2.12: Tracking the walking man with the proposed mean-shift method using both image and high-pass filter information: (a) frame 1, (b) frame 5, (c) frame 10, (d) frame 15, (e) frame 20, and (f) frame 25.

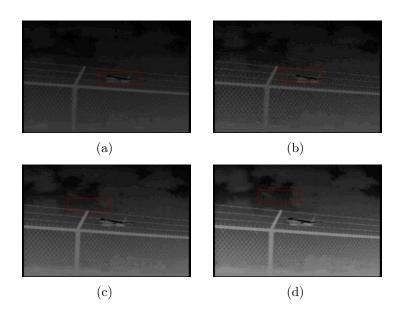


Figure 2.13: Tracking the plane in the airport. Ordinary mean-shift tracker fails: (a) frame 1, (b) frame 3, (c) frame 6, and (d) frame 10.

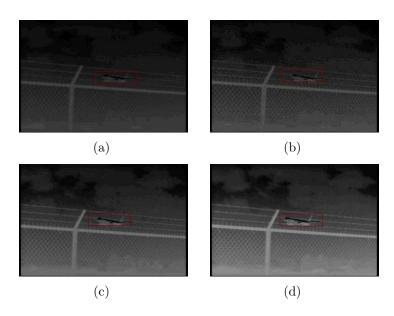


Figure 2.14: Tracking the plane in the airport with the proposed mean-shift method: (a) frame 1, (b) frame 3, (c) frame 6, and (d) frame 10.

### Chapter 3

## Mean-Shift Tracking in CBIR

Content-based image retrieval (CBIR) is a method to search images from a database of images according to the user's interest. It uses visual contents of image in searching. CBIR has been an active and challenging research area since 1990s. A significant progress has been made in both theoretical research and practical applications during the last decade.

Early methods were usually based on textual annotations of images. In other words, images were first annotated with text and then searched using text-based approach in database management systems. However, most text-based image retrieval systems require manual annotation of images since automatic generation of descriptive texts for a wide spectrum of images is not feasible. It is obvious that manual image annotation is expensive task for large databases and often subjective. As a result, CBIR by using traditional database management systems is not sufficient to support different queries.

In the 1990s, advances in the Internet and new digital image sensor technologies drastically increased the volume of digital images produced by scientific, educational, medical, industrial and other applications for users. Therefore the difficulties of text-based retrieval became more severe. An efficient management of quickly increasing visual information became an urgent problem. Several researchers from the different areas such as computer vision, database management, human-computer interaction etc. worked on the field [24]-[28]. Then research on CBIR has developed rapidly. The number of publications on the methods for visual infirmation extraction, organization, indexing and user query has increased. Similarly, a large number of CBIR system has been developed by universities, governments, companies and hospitals.

CBIR systems use the visual contents of an image such as *color*, *shape*, *texture* and *spatial layout* to describe and index the image. Next sections explain these image content descriptors.

#### **3.1** Image Content Descriptors

Image usually consists of both visual and semantic content. General image content includes color, texture, shape and spatial relationships etc. Semantic content is obtained by textual annotation or complex inference procedures based on visual content. This section focuses on general contents descriptions.

A successful visual content descriptor should be robust against the variances on image such as the variation of the illuminant of scene. However, there is a tradeoff between the robustness and the discriminative power of visual features. The discrimination of the essential differences is reduced while increasing robustness.

A visual content descriptor can be local or global. A local descriptor uses the visual features of regions and objects to describe the image where a global descriptor uses the visual features of the whole image. An image is often divided into parts in the local visual descriptors. The image is simply cut into tiles of equal size and shape. This simple partition does not guarantee perceptually meaning regions but gives the global features of the images at a lower resolution. More complex methods are used to obtain semantically meaningful objects such as bird, car, etc. Some methods widely used to extract color, texture, shape, and spatial information from are introduced briefly.

## 3.1.1 Color

Color is widely used for image retrieval systems. The three-dimensional values of color has obviously higher discriminator feature when compared to gray values of the image. Firstly, color space that will be used in CBIR systems should be determined before selecting an appropriate color descriptor. Therefore color space is introduced first before color descriptors.

*Color space:* Each pixel of the image is represented by a point in a 3D color space. RGB, Munsell, CIE L\*a\*b, CIE L\*u\*v and HSV are used commonly in CBIR systems.

RGB space is widely used as a color space to display and print image. It consists of three color components: red, green and blue. A color in RGB space is produced by adding them together. RGB space is device independent and perceptually non-uniform.

The CIE color space is device independent. It can be considered as perceptually uniform. They include a luminance or lightness component and two chromatic. The transformation of RGB space to CIE space is given in [29].

HSV space is widely used in computer graphics. It has the three color components: hue, saturation and value. The hue is invariant to the illumination changes and camera direction. So it is more suitable for object retrieval.

*Color moments:* Color moments are widely used in several CBIR systems. The mean (the first order) and variance (the second order) and skewness (third order) have been proven to be efficient and effective for the representation of color distributions of an image [30]. The color moment method has better performance when both CIE color spaces are used. The use of third moment besides the mean and variance improves the overall performance of image retrieval.

*Color histogram:* The color histogram is the effective way to represent the color content of an image, if all the processed data is unique. The extraction of the color histogram is simple and it is quite effective in characterizing of local and

global distribution of an image. It is also robust to changes in the view angle, occlusion and rotation.

The histogram is distribution of the number of pixels for each quantized bins, which can be defined separately or jointly for each component, since any pixel in the image has three components in certain color space such as red, green and blue in RGB space and hue, saturation and value in HVS. It is clear that it has more discriminative power if more bins is used in the color histogram. However, the use of large number of bins increases the computational cost. It also makes difficult to build efficient indexes for image database. A very fine bin quantization does not improve the retrieval performance in many applications. A way to reduce the number of bins is to use the clustering methods to determine the K best colors in a given space for a set of images. Each of these best colors are taken as a histogram bin. Another way is to use the bins which have the largest pixels numbers since a small number of histogram bins contain the majority of pixels in an image [31]. This reduction does not degrade the performance of histogram matching.

The histogram comparison saturates the discrimination when database has large number of image. The joint histogram method is proposed in [32]. In addition, color histogram does not take account into spatial information. Thus very different image may have similar the color histograms. Therefore several method to incorporate the color histogram with spatial information are proposed to increase the discrimination power. A simple approach is to divide an image into small areas and extract the histograms of these small areas. Increasing the number of areas increase the spatial information. but also it increases the computational cost and memory requirement.

Color coherence vectors: A proposed method is to use the spatial information in the histogram extraction [33]. Each histogram bins is divided into two types. It is coherent if it belongs to a large colored region or incoherent if it does not. Color coherence vectors method has better performance than color histograms for image retrieval especially when images have mostly uniform colors and mostly texture regions. *Color correlogram:* The color correlogram [34] is used to characterize both the color distribution of pixels and the spatial correlation of pairs of colors. The color histogram has three dimension. The first and second dimension are used for the colors of any pixel pairs. The third one is used for their spatial distance. The size of the color correlogram is very large when all possible combinations of color pairs. Its simple version called the color autocorrelogram is often used to reduce this large size.

Invariant color features: Color varies with change of illumination, the surface orientation and the view angle of camera. Therefore these changes may decrease the performance of image retrieval system and should be considered. However, these changes are not considered in the most of the color descriptors given above. Recently invariant color descriptions have been proposed in [35, 36]. The discrimination power is decreased when this method is applied to provide the independent color representation.

## 3.1.2 Texture

Texture is a significant property of images. There are many texture representations in pattern recognition and computer vision. The texture representation has basically two categories: structural and statistical. Structural methods include morphological operator and adjacency graph to describe texture by identifying structural primitives and their placement rules. Statistical methods include Fourier power spectra, co-occurrence matrices, shift invariant component analysis, Tamura feature, Wold decomposition, Markov random field, fractal model and multi-resolution filtering methods such as Gabor and wavelet transform. All of methods are used to characterize texture by the statistical distribution of the image intensity. The details of image retrieval by the texture are not given because they are out of scope of this thesis.

### 3.1.3 Shape

The shape features of objects or regions are used in many CBIR systems. The shape features are usually described after images have been segmented into regions or objects when it is compared to color and texture features. However, robust image segmentation is difficult. Therefore use of shape features has some limitations except some special applications. The shape descriptions method can be divided into two categories: boundary-based and region-based methods. The boundary-based methods includes rectilinear shapes, polygonal approximations, finite element models, Fourier-based shape descriptors . The region-based methods are statistical moments.

## 3.1.4 Spatial Information

Regions and objects with similar color and texture properties can be distinguished by using spatial constraints. For example, a region of sky and ocean may be blue and have same color distribution and texture. But their spatial locations on the image are different. Therefore spatial information of region or object can be used in CBIR systems. The most popular representation of spatial relationships is the 2D strings [37]. Besides the 2D strings, spatial quad-tree [38] and symbolic image [39] are also used to represent the spatial information.

# 3.2 Similarity Measures

Content-based image retrieval systems calculate visual similarities between a query image and images from database. The retrieval result consists of multiple image ranked from top to bottom according to their similarity measures with the query image. There are many similarity measures used in CBIR studies. Some of them are given below. D(I, J) donates the distance measure between the query image and I and the image J from the database.  $f_i(I)$  is number of the pixels in bin i of I.

*Minkowski-Form distance:* The Minkowski-Form distance is suitable to measure distance between two images if each dimension of feature vector is independent from others. The distance  $L_p$  is defined as:

$$D(I,J) = (\sum_{i} |f_i(I) - f_i(J)|^p)^{1/p}$$
(3.1)

The  $L_1, L_2$  is called Euclidean distance. The Minkowski-Form distance is widely used as a metric in CBIR systems.

*Quadratic form distance:* The Minkowski distance takes account into all bins of the color histogram completely independently and does not consider the certain pairs of bins corresponding to features. The Quadratic Form Distance is propsed to solve this problem:

$$D(I,J) = \sqrt{(\mathbf{F}_I - \mathbf{F}_J)^T \mathbf{A} (\mathbf{F}_I - \mathbf{F}_J)}$$
(3.2)

where  $A = [a_{ij}]$  is a similarity matrix and  $a_{ij}$  donates similarity between bin *i* and *j*.  $\mathbf{F}_I$  and  $\mathbf{F}_J$  are vectors which lists all entries of  $f_i(I)$  and  $f_i(J)$ . It is widely used in the histogram-based retrieval systems.

*Mahalanobis distance:* It can be used when each dimension of image feature vector is dependent on each other and has different importance. Its definition is:

$$D(I,J) = \sqrt{(\mathbf{F}_I - \mathbf{F}_J)^T C^{-1} (\mathbf{F}_I - \mathbf{F}_J)}$$
(3.3)

where C is the covariance matrix of the feature vectors.

# **3.3** Indexing Methods

Another critical issue in CBIR is effective indexing and fast searching of images based on visual features. Because the feature vectors are usually large sized with multiple dimensions. Therefore they are not appropriate for the well-known indexing schemes. In general, a size reduction is applied before implementing efficient indexing scheme. The size reduction methods and indexing schemes are not detailed since CBIR in this thesis is index free.

# 3.4 User Interaction

The user interaction with CBIR systems is important. The flexibility for user in CBIR systems can be obtained by involving the user to the retrieval procedure. The interface consists of two parts: query specification and a result presentation. Query specification can be done in many ways. These are category browsing, query by concept, query by sketch and query by sample.

- Category browsing is to browse in the database according to the category of the images. By this reason, images in the database are classified according to their semantic and visual contents.
- Query by concept is to retrieve images according to the conceptual description.
- Query by sketch allows the user to draw a sketch of an image with a tool (graphical editing).
- Query by example allows the user to define a query on an example image. The CBIR system converts this query into its feature representation internally.

# 3.5 Mean-Shift Analysis in CBIR

The proposed CBIR system is based on the color histogram for the local region. In fact the mean-shift tracking uses the color histograms. Therefore it is efficiently used to localize the candidate region for an image in database. The region specified by the user (target region) is searched on the database images by comparing the color histograms. The color histogram involving background effect reduction and edge information is first computed to extract the features of user interest. A search method is applied to the images in database. The search method can be divided into two categories. The first one is processes which are performed to localize the candidate region similar to the target region for an image from

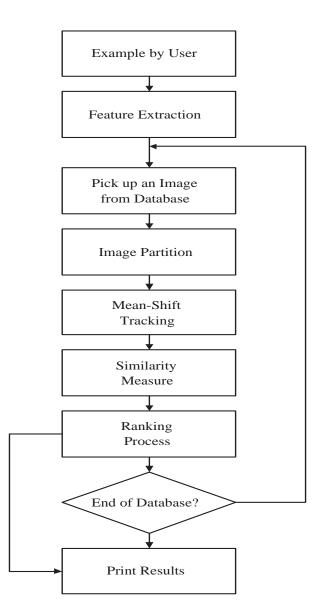


Figure 3.1: Flow diagram of the proposed CBIR system.

database. These processes are image partition, the histogram computation for sub-blocks in the image partition, evaluation of similarity measure and the meanshift tracking algorithm. Their details can be found in the following sections. A similarity measure is assigned to the image after all these processes in the first category are performed. That similarity measure is input to the second category that handles the ranking of the database images. At the end of search, the best similar five images are given to user as searching result. The flow chart of retrieval system is shown in Figure 3.1.

## 3.5.1 Modelling of User interest

A user interest (target) region is chosen before modelling the target. The model of the target is represented by the joint-color histogram. Background reduction and use of edge information are considered in the construction of the histogram. The edge information of the target region is extracted by using wavelet coefficients and represented in the histogram with color distribution. The details of the histogram computation are given in the following sections.

#### 3.5.1.1 Histogram or Kernel Density Estimation

Statisticians developed many ways of estimating the probability density function of a random variable from observed data [40]. The easiest way is to construct the histogram H of the data and normalize the area under the histogram to one. The paper by Dorin Comaniciu and Peter Meer [2] followed the approach studied by statisticians. This approach is called the kernel density estimation. The kernel density estimate at the observation  $x_i$  is defined by

$$f(x) = \frac{1}{n} \sum_{i=1}^{n} K_W(x - x_i)$$
(3.4)

where n is the observed data points or the number of pixel values in an image or an image region, and  $x_i$  represent a sample from some unknown density f, or in the case of gray scale images or video, the pixels themselves. The function  $K_W$  is defined as follows:

$$K_W(x) = \frac{1}{\sqrt{|W|}} K(W^{-0.5}x)$$
(3.5)

where K(z) is the d-variate kernel function with compact support satisfying the regularity constraints as described in [40], and W is a symmetric positive definite d d bandwidth matrix. For the radially symmetric kernel, the function K(z)becomes

$$K(z) = ck(||z||^2)$$
(3.6)

where c is a normalization constant. If one assumes a single global spherical bandwidth,  $W = h^2 I$ , the kernel density estimator becomes

$$f(x) = \frac{1}{n(h)^d} \sum_{x_i=1}^n K(\frac{x - x_i}{h})$$
(3.7)

A widely used choice for the function K is Gaussian function.

The aim of using a d-variate kernel function is to smooth the histogram. This is especially useful when the number of observed data n is small or, equivalently, image region is a small region. Obviously the histogram may be very jagged if the observed image region is small. For example,  $x_i = 200$  and  $x_j = 202$  may be observed in a 20 by 20 image region but  $x_i = 201$  may not have observed and the value of histogram for  $x_i = 201$  will be h(201) = 0. However, if a Gaussian smoothing function is used then f(201) will be nonzero. The parameter h defined above controls the variance of the function K. By changing the value of h a smoother or sharper pdf is estimated. In the extreme case, the function K becomes an impulse and the pdf estimate is simply the normalized histogram H(x). This approach is fine but it is computationally expensive. Because the pdf estimate is iteratively updated for each observed data point.

We do not follow this approach in our work. We cannot assume a specific underlying probability density for images. Therefore, the aim is simply to smooth the histogram so that the value of the estimate for 201 becomes nonzero in the above example.

There are more computationally efficient ways of smoothing data in electrical engineering: namely low-pass filtering. We can smooth the histogram by simply using a discrete low-pass filter. The narrower the bandwidth of the low-pass filter or smaller the cut-off frequency of the low-pass filter the smoother the estimated pdf. At the other extreme, when the impulse response of the filter is a Dirac-delta function then the probability density estimate is simply the histogram.

The computational cost of this approach is a one-dimensional discrete convolution whose cost is determined by the impulse response of the low-pass filter. As a rule of thumb, the narrower the bandwidth of the low-pass filter the longer the impulse response. Hence the computational cost increases. But this cost is negligible compared to the kernel density smoothing process used by statisticians and [2].

In our work, Finite-extent Impulse Response (FIR) filters are used. Example low-pass filters are presented in Section 3.5.1.4. Recursive Infinite-extent Impulse Response (IIR) filters have non-symmetric impulse responses therefore they are not used in smoothing

#### 3.5.1.2 Color Histogram Construction

Figure 3.2 shows a region of interest in an image selected by the user. The region of interest is called the target region from now. The RGB color space is used to extract the color feature of the selected target region. Because a color conversion from the RGB to another color space does not drastically improve the retrieval performance [41]. Another reason is that the developed CBIR system combines the color histogram and the mean-shift tracking algorithm. Since the original the mean-shift algorithm uses the RGB space, the fusion of the retrieval based on the color histogram and mean-shift tracking algorithm is simplified. The color histogram is not constructed separately for each color components in this thesis. The joint-color histogram is used to characterize the target region. The color components in the RGB space vary between 0 and 255 in an image. The dimension of the color histogram is  $255^3$  when the original color component values are taken account during the histogram computation. This is not an efficient method by the reason of the computational cost and large memory requirement. It also decreases

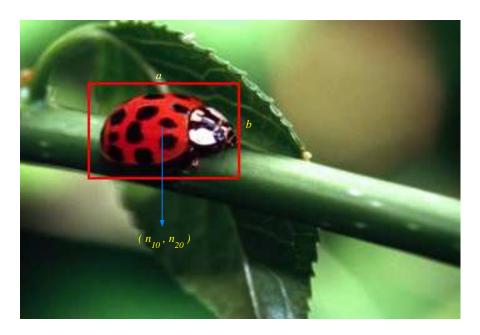


Figure 3.2: User interest in a query image.

the discriminative power of retrieval system for similar images that have different illumination, viewing angles and compression loss, etc. Therefore most of the CBIR systems use the quantized values of color components. In this thesis, the color component values are quantized by a fixed constant Q. As a result, the dimension of the color histogram reduces to  $(255/Q)^3 = N^3$ . For instance, it is 4096 when Q equals to 16. A method using the quantized color component values in the color histogram extraction is mostly known as N-bin histogram extraction [2].

The position  $(n_{10}, n_{20})$  is the center of the target region with width a and height b. Let  $\mathbf{h}_t$  be the color histogram of the target region. The size of the histogram is  $N^3$  since the joint-color histogram is used. Equation 3.8 is used to construct the N-bins joint-color histogram.

$$h_t[k] = \frac{1}{C} \sum_{n_2 = n_{20} - \frac{b}{2}}^{n_{20} + \frac{b}{2}} \sum_{n_1 = n_{10} - \frac{a}{2}}^{n_{10} + \frac{a}{2}} \delta[\Delta(n_1, n_2) - k] \quad \text{for} \quad k = 1, 2, .., N^3 \quad (3.8)$$

where  $\delta$  is the discrete Dirac-delta function and C is the normalization constant and equals to *ab*. The index  $\Delta(n_1, n_2)$  is derived from the quantized color values by using the following formula.

$$\Delta(n_1, n_2) = R_q(n_1, n_2) + NG_q(n_1, n_2) + N^2 B_q(n_1, n_2)$$
(3.9)

where  $R_q(n_1, n_2)$ ,  $G_q(n_1, n_2)$  and  $B_q(n_1, n_2)$  are the quantized values of R, G and B at the pixel location  $(n_1, n_2)$ , respectively. The quantization is performed by Equation 3.10.

$$R_q(n_1, n_2) = \left\lfloor \frac{R(n_1, n_2)}{Q} \right\rfloor$$

$$G_q(n_1, n_2) = \left\lfloor \frac{G(n_1, n_2)}{Q} \right\rfloor$$

$$B_q(n_1, n_2) = \left\lfloor \frac{B(n_1, n_2)}{Q} \right\rfloor$$
(3.10)

where  $\lfloor \bullet \rfloor$  is called the largest integer less than  $\bullet$ . After this step, the  $\mathbf{h}_t$  is smoothed by using a FIR low-pass filter defined in Section 3.5.1.1.

#### 3.5.1.3 Reduction of Background Effect on Histogram

The background information is automatically captured while selecting the target region or especially the object using rectangular window as seen Figure in 3.2. The background information is important for two reasons. First, the performance of the mean-shift tracking is decreased due to the background colors in the color histogram of the target region. Second, it is very difficult to model an object at its boundary. However, the effect of the background on the color histogram can be reduced and this improves the discriminative power of retrieving and the tracking performance of the mean-shift algorithm.

An easy way to reduce weight of the background information in the color histogram is to estimate the color histogram of background and modify the target histogram. In Figure 3.2, a rectangular block is chosen by user. The color histogram for this block obviously contains the object and background information. A new extended block is virtually defined to estimate the color histogram of background. The size of the extended block is 10% larger than the size of the block originally selected by the user. Then the color histogram  $\mathbf{h}_{\mathbf{b}}$  is computed



Figure 3.3: Pixels whose histograms entries are larger than 0.005 are colored in blue to show the effect of background reduction.

for the region between two blocks by using exactly same method for the target region. Then target color histogram is updated according to  $\mathbf{h}_{\mathbf{b}}$ . A set weights to modify the target color histogram  $\mathbf{h}_{\mathbf{t}}$  is defined as follows:

$$\alpha_k = \min(\frac{\hat{h}_b}{h_b[k]}, 1) \tag{3.11}$$

where  $\hat{h}_b$  is the smallest nonzero entry of the  $\mathbf{h}_b$ . Then each entry of  $\mathbf{h}_t$  is multiplied by the weight corresponding to this entry:

$$\hat{h}_t[k] = \alpha_k h_t[k]$$
 for  $k = 1, 2, ..., N^3$  (3.12)

where  $\hat{\mathbf{h}}_t$  is updated the target histogram. The weight reduction makes the target histogram  $\hat{\mathbf{h}}_t$  non-normalized. Thus re-normalization is performed:

$$C = \sum_{k=0}^{N^3} \hat{h}_t[k]$$
 (3.13)

$$\tilde{h}_t[k] = \frac{1}{C} \hat{h}_t[k] \quad \text{for} \quad k = 1, 2, .., N^3$$
(3.14)

where  $\tilde{\mathbf{h}}_t$  is the normalized histogram in which the effect of the background is reduced. For example, Figure 3.3 shows the effect of the background reduction.

Pixels whose histogram entries are larger than 0.005 are colored in blue. As seen in Figure 3.3, the background information around the beetle image within the user's rectangle is reduced. The color histogram mostly contains the color information of the beetle.

This approach may have some disadvantages in some cases. For example, if there are similar colors on the background around the target region, this meaningful information will be reduced by the method discussed above in the histogram. As a result, the retrieval performance of the CBIR system is reduced.

#### 3.5.1.4 Incorporation of Edge Information to Color Histogram

In this section, we describe how a joint-pdf including edge information is estimated from a given image region  $x(n_1, n_2)$ . Edge information can be extracted by using wavelet coefficients. In order to obtain the wavelet coefficients the image is processed by a filterbank with following low-pass and high-pass filters:

$$h_l[n] = \{0.25, 0.5, 0.25\} \tag{3.15}$$

and the impulse response of the high-pass filter is

$$h_h[n] = \{-0.25, 0.5, -0.25\}.$$
(3.16)

The filters are complementary with cut-off frequencies at  $\pi/2$ . Or,

$$h_l[n] = \{-1/32, 0, 9/32, 1/2, 9/32, 0, -1/32\}$$
(3.17)

and the corresponding high-pass filter is given by

$$h_h[n] = \{1/32, 0, -9/32, 1/2, -9/32, 0, 1/32\}$$
(3.18)

Both filters are related with Lagrange family of wavelets [42]. The image is processed in a separable manner by the filterbank and four wavelet sub-images  $x_{ll}(n_1, n_2), x_{lh}(n_1, n_2), x_{hl}(n_1, n_2)$ , and  $x_{hh}(n_1, n_2)$  are obtained as shown in Figure 3.4. Due to decimation by a factor of two after each filtering operation the wavelet subimages are quarter size versions of the original image.



Figure 3.4: Wavelet sub-images of the beetle image.

If the pixel  $x(n_1, n_2)$  is part of a horizontal edge then coefficients near  $|x_{lh}(n_1/2, n_2/2)|$  and  $|x_{hh}(n_1/2, n_2/2)|$  take high values compared to flat areas in which wavelet coefficients are close to zero. Similarly, when the pixel  $x(n_1, n_2)$  is part of a vertical edge then wavelet coefficients  $x_{hl}(n_1/2, n_2/2)$  and  $x_{hh}(n_1/2, n_2/2)$  take high values compared to flat areas in which wavelet coefficients are close to zero. We construct a sub-image from the high-band wavelet subimages as follows:

$$x_a(n_1, n_2) = |x_{lh}(n_1, n_2)| + |x_{hl}(n_1, n_2)| + |x_{hh}(n_1, n_2)|$$
(3.19)

The subimage  $x_a(n_1, n_2)$  covers both horizontal and vertical edges, i.e., when the pixel  $x(n_1, n_2)$  is part of an edge then the subimage pixels around  $x_a(n_1/2, n_2/2)$  take high values compared to flat areas because the subimage  $x_a$  is constructed from the wavelet coefficients.

A joint-pdf representing a given image region can be estimated from the image  $x(n_1, n_2)$  and the corresponding subimage  $x_a$  by adding an extra dimension. This joint-pdf will represent not only the gray scale information but also the high-frequency content of the region because the subimage  $x_a$  is obtained by using the high-pass filters of the wavelet filterbank.

The additional dimension for the subimage increases the size of the joint color histogram depending on the quantization level of the subimage. Another way to add edge information into the joint color histogram is to determine the state of a pixel. In other words, the edge pixels are separated from non-edge pixels while constructing the color histogram. This method doubles the dimension of the histogram. Let  $E(n_1, n_2)$  be the edge binary state of pixel at  $(n_1, n_2)$ . The construction of the joint-histogram is modified as follows:

$$h_t[k] = \frac{1}{C} \sum_{n_2} \sum_{n_1} \delta[E(n_1, n_2)N^3 + \Delta(n_1, n_2) - k] \quad \text{for} \quad k = 1, 2, .., 2N^3 \quad (3.20)$$

and  $E(n_1, n_2)$  is found by:

$$E(n_1, n_2) = \begin{cases} 1 & , & x_a(n_1/2, n_2/2) > T \\ 0 & , & \text{otherwise} \end{cases}$$
(3.21)

where T is a treshold used to determine the status of the pixel at  $(n_1, n_2)$  to be on edge or not. In this case, the wavelet domain information is inherently quantized to a single bit (or two levels). Higher quantization levels leading to longer  $\mathbf{h}_t$  functions can be used. The joint-histogram defined in Equation 3.20 can be smoothed by using a low-pass filter.

### 3.5.2 Similarity Measure

Similarity measures used in CBIR systems are discussed in Section 3.2. In this thesis, the Bhattacharya coefficient is used to measure the similarity between the target and candidate histogram. The Bhattacharya coefficient is a divergence type measure and has a simple geometric interpretation and used in mean-shift track method by converting to distance to determine the convergence state. It is simply the cosine of the angle between two unit vectors. The sample estimate of the Bhattacharya coefficient between two histograms  $\mathbf{h_t}$  and  $\mathbf{h_c}$  is defined as

$$\rho = \sum_{k=1}^{N_h} \sqrt{h_t[k] h_c[k]}$$
(3.22)

where  $N_h$  is the size of histograms instead of  $N^3$  or  $2N^3$ . Because the size of the histogram varies according to the use of the edge information. The maximum of

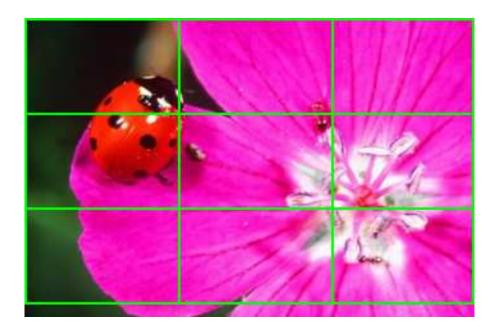


Figure 3.5: Image partition.

 $\rho$  is 1.0 when  $\mathbf{h_t}$  and  $\mathbf{h_c}$  are equal to each other. Its minimum is 0 if there is no intersection between both histograms. It gives a value between 0 and 1 in other cases.

## 3.5.3 Image Partition

The candidate region in an image from database, which is the most similar to the target region, is initially unknown. Before performing the mean-shift tracking algorithm, the approximate location of candidate regions is determined by a method based on sub-block technique where image is divided into sub-blocks as shown in Figure 3.5. The size of sub-blocks is equal to the size of user's block. Let W and H are width and height of an image respectively. The number of sub-blocks  $N_s$ :

$$N_s = \frac{W.H}{a.b}.\tag{3.23}$$

After this step, the color histogram or joint-histogram of each sub-block (from left to right, from top to bottom) is evaluated according to the methods expressed in Sections 3.5.1.2-4. Then similarity measures between the target region and the sub-blocks are computed. The sub-block with the largest similarity measure

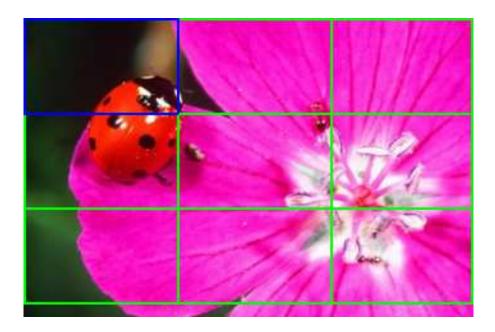


Figure 3.6: The sub-block with the highest similarity measure (blue rectangle).

as seen in Figure 3.6 is assumed as the approximate position of the candidate region. The center coordinate  $(n_{1b}, n_{2b})$  of this sub-block is passed to the mean-shift tracking as an initial position.

## 3.5.4 Mean-Shift Tracking

The image partition generally gives the approximate location of candidate region as depicted in Figure 3.6. However, its correct location is necessary to obtain the similarity measure of correct region for database images. At this point, the mean-shift tracking algorithm is an efficient and effective method to localize the candidate region. The key point of the algorithm is to maximize the Bhattacharya coefficient by using the color histograms in a iterative manner. In the proposed CBIR method aims to maximize the similarity measure (the Bhattacharya coefficient) for the candidate region as well. This is obviously achieved by iterating the mean-shift method after the image partition.

The initial position for mean-shift tracking  $(n_{1b}, n_{2b})$  is obtained by image partition. The  $\mathbf{h}_{\mathbf{t}}$  is already available from modelling of user interest. The following

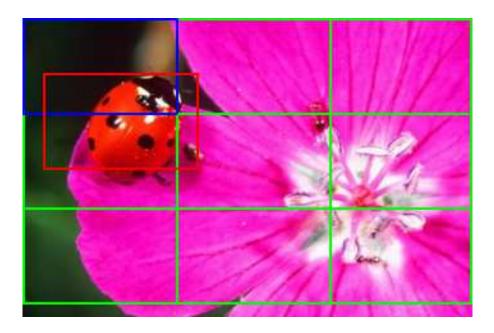


Figure 3.7: The localization of candidate region by mean-shift tracking algorithm after image partition (red rectangle).

algorithm is iteratively processed to maximize the similarity measure:

- 1. Compute histogram for the location  $(n_{1b}, n_{2b})$  using Equation 3.8 or 3.20.
- 2. Compute weights.

$$w[k] = \sqrt{\frac{h_t[k]}{h_c[k]}}$$
 for  $k = 1, 2, ..., N_h.$  (3.24)

3. Derive new location of the candidate region.

$$n_{1n} = \frac{\sum_{n_2} \sum_{n_1} w[\Delta(n_1, n_2)] . n_1}{\sum_{n_2} \sum_{n_1} w[\Delta(n_1, n_2)]}, \text{ and}$$

$$n_{2n} = \frac{\sum_{n_2} \sum_{n_1} w[\Delta(n_1, n_2)] . n_2}{\sum_{n_2} \sum_{n_1} w[\Delta(n_1, n_2)]}$$
(3.25)

where  $\Delta(n_1, n_2)$  is defined in Equation 3.9.

4. Stop if  $|n_{1b} - n_{1n}| = 0$  and  $|n_{2b} - n_{2n}| = 0$ , else  $n_{n1} \to n_{1b}$  and  $n_{2n} \to n_{2b}$ , go to step 1.

| Process         | Similarity |  |
|-----------------|------------|--|
|                 | Measure    |  |
| Image Partition | 0.43       |  |
| MS Iteration 1  | 0.46       |  |
| MS Iteration 2  | 0.47       |  |
| MS Iteration 3  | 0.48       |  |
| MS Iteration 4  | 0.48       |  |
| MS Iteration 5  | 0.48       |  |

Table 3.1: Similarity measures for the most similar sub-block after image partition and iterations of the mean-shift tracking algorithm.

The mean-shift tracking algorithm correctly localizes the candidate region as seen Figure 3.7. From the practical experiences, the five iterations are sufficient for the converge of the algorithm. The maximization process of the algorithm can be seen in Table 3.1 in terms of similarity measure for the image partition and five iterations of the algorithm. The location obtained by the mean-shift tracking algorithm is used in the computation of similarity measure for the image from database. Final similarity measure is input to rank the images in the database. Top five images are always held in the ranking queue.

# **3.6** Experimental Results

In this section, experimental results of proposed retrieval system are given. A software tool is developed in order to try the proposed system by using VC++ 6.0 as shown Figure 3.8. The system is based on query by example image. Therefore it allows user to open an example image and select a region. The use of background effect reduction and edge information is optional. It is also possible to filter images having lower similarity measures by entering a treshold before searching. Then a search in the database is started. The resultant images (top 5) matching to the example image are displayed on the screen together with their similarity measures as seen in Figure 3.8. Five image categories are tried to see the retrieving performance of the proposed system in the database. The database includes



Figure 3.8: The developed software to test image retrieving.

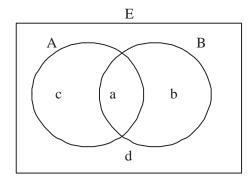


Figure 3.9: Set representation of retrieving process.

images more than 200 images. The goal of the proposed method is not fast retrieval so that the computational cost is not considered. The aim is to show that the proposed method works properly.

In the CBIR systems, two metrics are used to evaluate the performance of retrieval. *Recall* expresses the relevant images in the database which are retrieved in the response to a user query. *Precision* is defined as the fraction of the retrieved images that are indeed relevant to the query [43]. In Figure 3.9, a is the number of retrieved relevant images, b is the number of retrieved irrelevant images, c is the number of unretrieved relevant images and d is the number of unretrieved

| Category | Recall | Precision |
|----------|--------|-----------|
| Beetle   | 1      | 1         |
| Flower   | 1      | 1         |
| Face     | 1      | 1         |
| Flag     | 0.4    | 0.4       |
| Bird     | 0.8    | 0.8       |

Table 3.2: Recall and Precision values for the example image categories.

Table 3.3: The number of the relevant and irrelevant images in top five for the example image categories.

| Category | Additional | # of total | # of retrieved | # of retrieved |
|----------|------------|------------|----------------|----------------|
|          | histogram  | relevant   | relevant       | irrelevant     |
|          | feature    | image      | image          | image          |
| Beetle   | None       | 5          | 5              | 0              |
| Flower   | None       | 5          | 5              | 0              |
| Face     | None       | 5          | 5              | 0              |
| Flag     | None       | 5          | 2              | 3              |
| Flag     | Background | 5          | 4              | 1              |
| Bird     | None       | 5          | 4              | 1              |
| Bird     | Egde       | 5          | 5              | 0              |

irrelevant images. Recall and precision ratios are computed by:

$$Recall = \frac{a}{a+c},\tag{3.26}$$

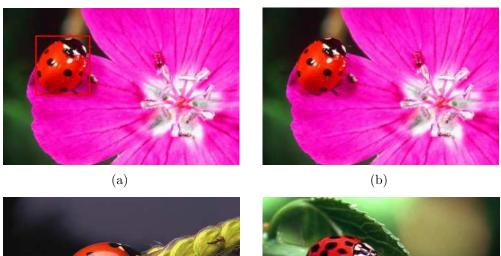
and

$$Precision = \frac{a}{a+b}.$$
(3.27)

The image retrieval is said to be effective if the precision values are higher at the same recall values. However, recall and precision are only rough expression of the performance of the retrieval system. Recall and precision values for the example image categories without using additional feature in histogram are given in Table 3.2. Table 3.3 gives the number of relevant and irrelevant images in top five corresponding to each image category. In the first example image, a group of beetle images is used to test the retrieval performance. All beetle images in the database are successfully retrieved with the the straightforward color histogram for the target region as shown in Figure 3.10. The same performance is obtained for flower and human face images as seen in Figures 3.11 and 3.12, respectively.

In the fourth example, the images included the Turkish flag are searched in database. The CBIR system using only histogram extraction shows low performance. As seen in Figure 3.13, there are only two relevant flag images. The other three ones are birds images and completely irrelevant images. The dominant colors on flag is red and white. But, user's rectangle in Figure 3.13-a contains a significant amount of the background information. When the background reduction method is applied, the number of relevant image becomes 4 as shown in Figure 3.14. As a result, an improvement for this category is provided by the background reduction method described in Section 3.5.1.3.

The images in the database include the birds and they are searched in the last example. The query region in this example is the head of a bird. Four images in top 5 in Figure 3.15 are relevant and the last one is irrelevant. The color distribution of the bird head and the last retrieved image (especially walls) is close to each other. The background reduction is not appropriate here since the weight of colors characterizing the bird head is reduced because of its body. Therefore the use of edge information in the color histogram is applied. Figure 3.16 demonstrates the elimination of the irrelevant image by use of the edge information.







(d)



Figure 3.10: (a) Beetle example image with user interest. (b) Hit 1 with 0.99 similarity measure. (b) Hit 2 with 0.40 of similarity measure. (c)-(f) Other hits with 0.39, 0.30 and 0.29 respectively.







Figure 3.11: (a) Flower example image with user interest. (b) Hit 1 with 0.74 similarity measure. (b) Hit 2 with 0.74 of similarity measure. (c)-(f) Other hits with 0.54, 0.48 and 0.46 respectively.

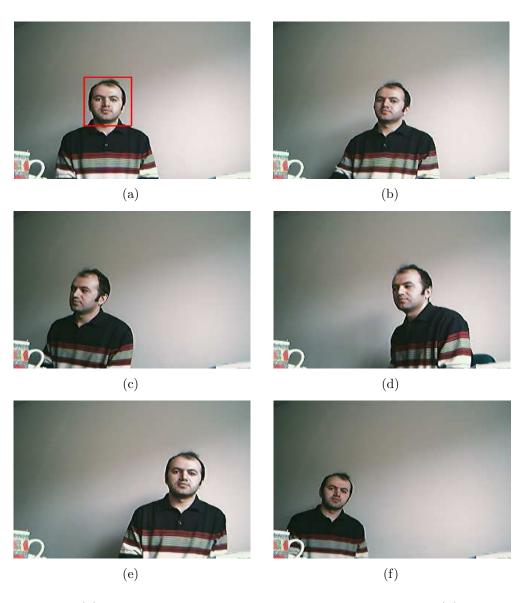


Figure 3.12: (a) Human face example image with user interest. (b) Hit 1 with 0.91 similarity measure. (b) Hit 2 with 0.90 of similarity measure. (c)-(f) Other hits with 0.89, 0.88 and 0.79 respectively.







(b)







Figure 3.13: (a) Turkish flag example image with user interest. (b) Hit 1 with 0.99 similarity measure. (b) Hit 2 with 0.40 of similarity measure. (c)-(f) Other hits with 0.39, 0.30 and 0.29 respectively.



Figure 3.14: (a) Turkish flag example image with user interest. User interest is modelled by background reduction. (b) Hit 1 with 0.67 similarity measure. (b) Hit 2 with 0.40 of similarity measure. (c)-(f) Other hits with 0.32, 0.31 and 0.31 respectively.

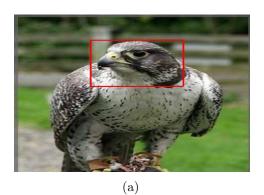
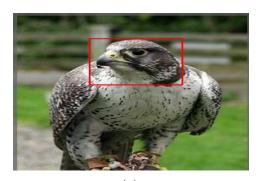








Figure 3.15: (a) Bird example image with user interest. (b) Hit 1 with 0.94 similarity measure. (b) Hit 2 with 0.93 of similarity measure. (c)-(f) Other hits with 0.92, 0.87 and 0.77 respectively.







(b)





Figure 3.16: (a) Bird example image with user interest. User interest includes edge information .(b) Hit 1 with 0.90 similarity measure (b) Hit 2 with 0.87 of similarity measure. (c)-(f) Other hits with 0.86, 0.83 and 0.70 respectively.

# Chapter 4

# Conclusions

In this thesis, mean-shift method is applied to tracking of moving objects in FLIR imagery and CBIR using multi-dimensional histograms. The first dimension of the histogram is estimated from actual pixel values of image. The second dimension is extracted by using the high-pass filtered version of the image which is related with wavelet transform of the image.

Experimental results clearly show the superior quality of the proposed tracker using both the pixel information and the high-frequency information over the ordinary mean-shift tracker using only pixel information. The same behavior is observed in all the examples tried. Whenever the background is cluttered the ordinary mean-shift tracker fails to track the moving object due to the lack of information in gray scale histogram. In general, the histogram constructed from the gray-level information of FLIR images is not sufficient to uniquely characterize the object.

By including high-pass information to tracking process the robustness of the tracker is improved against noise and cluttered background. Additional high-pass information leads to a good characterization of the moving object by the histogram in all the examples tried.

The computational cost of the proposed scheme is low. It consists of only

an additional high-pass filtering operation and an increased size in histogram construction. High-pass filtering operation may not be carried out over the entire image. It is enough to perform high-pass filtering only around the moving object.

The second contribution of the thesis is a content-based image retrieval method developed for queries based on especially region and object. The joint color histogram is used to describe the region selected by user. In order to increase the discriminative power of retrieving, the reduction of background information and use of edge information in the histogram are considered. While searching candidate region similar to the target region within an image from database, the mean-shift tracking algorithm is used to localize that candidate region. A demonstration software is developed to test the proposed CBIR method. The software gives top five images matching to the query image.

The proposed CBIR method is tested for five category images in the database. The three categories of them are successfully retrieved. The proposed system shows low performance for other two categories. However, by reducing the background information on the joint color histogram and forcing the edge information into the joint color histogram, the retrieval performance of the system is increased.

There are two observed reasons affecting the retrieval performance of a CBIR system from the experiments. The first one is the quality of the example image. Therefore, it is useful to use query images that have good visual quality and view angle in order to obtain an effective model of the selected region. The second one is the size of the region specified by user. Since the query of the proposed method is based on region or object, it may fail to retrieve the images including the similar regions or objects whose sizes are much smaller or larger than the size of the region drawn by the user. Although the mean-shift has the ability to update the search window size adaptively, there are practical implementation problems.

In fact the computational cost of the proposed scheme is not considered during this study. However, use of the mean-shift tracking in localization of the candidate region increases the retrieving speed when compared to the traditional methods. Therefore, the computational bottleneck of the proposed method is histogram extraction. A fast histogram computation technique drastically speeds up the retrieval process. The background reduction method from the color histogram does not increase the retrieval time as it is applied to only query image while modelling the target region. But use of the edge information consumes the processing power because of extracting wavelet coefficients for each image in the database. The demonstration system is not computationally optimized. Implementation issues are left as a future work.

# Bibliography

- D. Comaniciu, P. Meer, "Mean Shift Analysis and Applications," *IEEE Int'l Conf. Comp. Vis.*, Kerkyra, Greece, pp. 1197-1203, 1999.
- [2] D. Comaniciu, V. Ramesh, and P. Meer, "Real-Time Tracking of Non-Rigid Objects Using Mean Shift," *Proc. IEEE Conf. Computer Vision and Pattern Recognition*, Vol. II, pp. 142-149, June 2000.
- [3] D. Comanicu, P. Meer, "Mean shift: A robust approach toward feature space analysis," *IEEE Trans. Pattern Anal. Machine Intell.*, Vol. 24, pp. 603-619, May 2002.
- [4] D. Comaniciu, et al., "Real-Time Tracking of Non-Rigid Objects Using Mean Shift", US patent pending, 2000.
- [5] Dorin Comaniciu, Visvanathan Ramesh, and Peter Meer, "Kernel-Based Object Tracking," *IEEE Trans. on Pattern Anal. and Machine Intelligence*, Vol. 25, No. 5, pp. 564-579, May 2003.
- [6] M. Isard and A. Blake, "Condensation-Conditional density propagation for visual tracking," Intl. J. of Computer Vision, Vol. 28(1), No. 1, pp. 5-28, 1998.
- [7] A. Yilmaz, K. Shafique, N. Lobo, X. Li, T. Olson, and M. Shah, "Target Tracking in FLIR Imagery Using Mean Shift and Global Motion Compensation," *IEEE Workshop on Computer Vision Beyond Visible Spectrum*, 2001.

- [8] A.Yilmaz, K .Shafique, and Mubarak Shah, "Target Tracking in Airborne Forward Looking Infrared Imagery," *Journal of Image and Vision Computing*, Vol. 21, No. 7, pp. 623-635, 2003.
- [9] Murat Bagci, Yasemin Yardimci, A. Enis Cetin, "Moving object detection using adaptive subband decomposition and fractional lower order statistics in video sequences," *Signal Processing, Elsevier*, Vol. 82, pp. 1941-1947, 2002.
- [10] F.M. Porikli, O. Tuzel, "Fast Object Tracking by Adaptive Background Models and Mean-Shift Analysis", International Conference On Computer Vision Systems (ICVS), April 2003.
- [11] M.D. Flickner, I. Haritaoglu, "Method of detecting and tracking groups of people", US Patent application, No. 0107649 June 12, 2003.
- [12] Halil I. Cuce and A. Enis Cetin, "Mean-shift tracking of moving objects using multidimensional histograms," *Proc. SPIE Int. Soc. Opt. Eng.*, Vol. 5428, pp. 70-77, 2004.
- [13] Selim Aksoy, Robert M. Haralick, "Textural Features for Image Database Retrieval," *IEEE Workshop on Content-Based Access of Image and Video Libraries*, pp. 45-49, Santa Barbara, CA, June 21, 1998.
- [14] Selim Aksoy, Robert M. Haralick, "Content-Based Image Database Retrieval Using Variances of Gray Level Spatial Dependencies," *IAPR International* Workshop on Multimedia Information Analysis and Retrieval, pp. 3-19, Hong Kong, August 13-14, 1998.
- [15] Ediz Saykol, Ugur Gudukbay, Ozgur Ulusoy, "Integrated Querying of Images by Color, Shape, and Texture Content of Salient Objects," *Lecture Notes in Computer Science (LNCS)*, Vol. 3261, pp. 363-371, 2004.
- [16] Y. Rubner, C. Tomasi, and L. Guibas, "A Metric for Distributions with Applications to Image Databases," *IEEE Proceedings of the International Conference On Computer Vision*, pp. 59-66, 1998.

- [17] B. Funt and G. Finlayson, "Color Constant Color Indexing," *IEEE Trans*actions on Pattern Analysis and Machine Intelligence, 17(5), pp. 522-529, 1995.
- [18] T. Gevers and W. M. Smeulders, "Color-based Object Recognition," Pattern Recognition, 32(3), pp. 453-464, 1999.
- [19] R. J. Smith and S.-F. Chang, "Integrated Spatial and Feature Image Query," *Multimedia Systems*, 7(2), pp. 129-140, 1999.
- [20] K. Nagao and W. Grimson, "Using Photometric Invariants for 3D Object Recognition," Computer Vision and Image Understanding, 71(1) pp. 74-93, July 1998.
- [21] S. Nayar and R. Bolle, "Reflectance Based Object Recognition," International Journal of Computer Vision, 17(3), pp. 219-240, 1996.
- [22] Charles E. Jacobs, Adam Finkelstein, David H. Salesin, "Fast Multiresolution Image Querying," Proceedings of SIGGRAPH 95, in Computer Graphics Proceedings, Annual Conference Series, pp. 277-286, August 1995.
- [23] D. Koubaroulis, J. Matas, and J. Kitler, "Colour-based Image Retrevial from Video Sequences," *Challenge of Image Retrevial*, Brighton, 2000.
- [24] A. E. Cawkill, "The British Library's Picture Research Projects: Image, Word, and Retrieval," *Advanced Imaging*, Vol. 8, No. 10, pp. 38-40, October 1993.
- [25] J. Dowe, "Content-based retrieval in multimedia imaging," In Proc. SPIE Storage and Retrieval for Image and Video Database, 1993.
- [26] C. Faloutsos et al, "Efficient and effective querying by image content," Journal of intelligent information systems, Vol. 3, pp. 231-262, 1994.
- [27] Y. Gong, H. J. Zhang, and T. C. Chua, "An image database system with content capturing and fast image indexing abilities," *Proc. IEEE International Conference on Multimedia Computing and Systems*, Boston, pp. 121-130, 1994.

- [28] H. J. Zhang, and D. Zhong, "A scheme for visual feature-based image indexing," Proc. of SPIE conf. on Storage and Retrieval for Image and Video Databases III, pp. 36-46, San Jose, 1995.
- [29] A. K. Jain, Fundamental of Digital Image Processing, Englewood Cliffs, Prentice Hall, 1989.
- [30] M. Stricker, and M. Orengo, "Similarity of color images," SPIE Storage and Retrieval for Image and Video Databases III, vol. 2185, pp.381-392, Feb. 1995.
- [31] Y. Gong, H. J. Zhang, and T. C. Chua, "An image database system with content capturing and fast image indexing abilities", Proc. IEEE International Conference on Multimedia Computing and Systems, Boston, pp.121-130, 1994.
- [32] G.Pass, and R. Zabith, "Comparing images using joint histograms," Multimedia Systems, Vol .7, pp. 234-240, 1999.
- [33] G. Pass, and R. Zabith, "Histogram refinement for content-based image retrieval," *IEEE Workshop on Applications of Computer Vision*, pp. 96-102, 1996.
- [34] J. Huang, et al., "Image indexing using color correlogram," *IEEE Int. Conf.* on Computer Vision and Pattern Recognition, pp. 762-768, Puerto Rico, June 1997.
- [35] J. E. Gary, and R. Mehrotra, "Shape similarity-based retrieval in image database systems," Proc. of SPIE, Image Storage and Retrieval Systemes, Vol. 1662 pp. 2-8, 1992
- [36] G. D. Finlayson, "Color in perspective," *IEEE Trans on Pattern Analysis and Machine Intelligence*, Vol.8, No. 10, pp.1034-1038, Oct. 1996.
- [37] S. K. Chang, Q. Y. Shi, and C. Y. Yan, "Iconic indexing by 2-D strings," *IEEE Trans. on Pattern Anal. Machine Intell.*, Vol. 9, No. 3, pp. 413-428, May 1987.
- [38] H. Samet, "The quadtree and related hierarchical data structures," ACM Computing Surveys, Vol. 16, No. 2, pp. 187-260, 1984.

- [39] V. N. Gudivada, and V. V. Raghavan, "Design and evaluation of algorithms for image retrieval by spatial similarity," ACM Trans. on Information Systems, Vol. 13, No. 2, pp. 115-144, April 1995.
- [40] M. Wand, and M. Jones, Kernel Smoothing, Chapman & Hall, 1995.
- [41] B.G. Prasad, K.K. Biswas, and S.K. Gupta, "Region-based image retrieval using integrated color, shape, and location index," *ELSEVIER Computer Vision and Image Understanding*, Vol. 94, pp. 193-233, 2004.
- [42] C. W. Kim, R. Ansari and A. E. Cetin, "A class of linear-phase regular biorthogonal wavelets," *IEEE International Conference on Acoust., Speech,* and Signal Processing (ICASSP'92), Vol. 4, pp. 673-676, San Francisco, USA, March 1992.
- [43] A. M. W. Smeulders, M. Worring, S. Santini, A. Gupta, and R. Jain, "Content-based image retrieval at the end of the early years," *IEEE Trans.* on Pattern Analysis and Machine Intelligence, Vol. 22, No. 12, pp. 1349-1380, 2000.