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## ABSTRACT

In this paper, we report the theoretical and experimental possibility of achieving a quarter-wave plate regime by using high-contrast gratings, which are binary, vertical, periodic, near-wavelength, and two-dimensional high refractive index gratings. Here, we investigate the characteristics of two distinct designs, the first one being composed of silicon-dioxide and silicon, and the second one being composed of silicon and sapphire. The suggested quarter-wave plate regime is achieved by the simultaneous optimization of the transverse electric and transverse magnetic transmission coefficients,  $T_{TE}$  and  $T_{TM}$ , respectively, and the phase difference between these transmission coefficients, such that  $|T_{TM}| \simeq |T_{TE}|$  and  $\angle T_{TM} - \angle T_{TE} \simeq \pi/2$ . As a result, a unity circular polarization conversion efficiency is achieved at  $\lambda_0 = 1.55 \mu\text{m}$  for both designs. For the first design, we show the obtaining of unity conversion efficiency by using a theoretical approach, which is inspired by the periodic waveguide interpretation, and rigorous coupled-wave analysis (RCWA). For the second design, we demonstrate the unity conversion efficiency by using the results of finite-difference time-domain (FDTD) simulations. Furthermore, the FDTD simulations, where material dispersion is taken into account, suggest that an operation percent bandwidth of 51% can be achieved for the first design, where the experimental results for the second design yield a bandwidth of 33%. In this context, we define the operation regime as the wavelength band for which the circular conversion efficiency is larger than 0.9.

**Keywords:** Polarization, periodic slab waveguide, high-contrast grating, quarter-wave plate

## 1. INTRODUCTION

High-contrast gratings (HCGs), which are composed of high refractive index gratings with subwavelength periodicities enclosed by low refractive index materials,<sup>1</sup> have been notably studied since the numerical<sup>2</sup> and experimental<sup>3</sup> revelation of their diffraction-free and broadband high-reflectivity regimes. The most notable and intriguing properties of HCGs include large fabrication tolerance, geometrical simplicity and design flexibility.<sup>4</sup> In addition, their well-established theoretical descriptions also contribute to the enabling of benefiting from HCGs for the purpose of designing various optical devices, i.e., polarization-independent broadband reflectors,<sup>5</sup> polarizing beam splitters,<sup>6</sup> saturable and cavity-enhanced absorbers,<sup>7,8</sup> monolithic high-reflectivity cavity mirrors,<sup>9</sup> planar lenses and reflectors with high focusing abilities,<sup>10,11</sup> high quality-factor Fabry–Perot resonators,<sup>12</sup> vertical-cavity surface emitting and nanoelectromechanical lasers,<sup>13,14</sup> slow light waveguides,<sup>15</sup> and one-, two- and three- dimensional hollow-core low-loss optical waveguides.<sup>16–18</sup>

In this study, we benefit from the unique properties of HCGs for the purpose of achieving the desired transmission characteristics of a broadband and highly efficient quarter-wave plate, which operates in the near-infrared regime. It has recently been shown that transmission characteristics of binary and vertical HCGs can be obtained by the implementation of the periodic dielectric slab waveguide interpretation.<sup>19</sup> In one of our recent studies, we propose a two-dimensional HCG structure with optimized geometrical parameters<sup>20</sup> by

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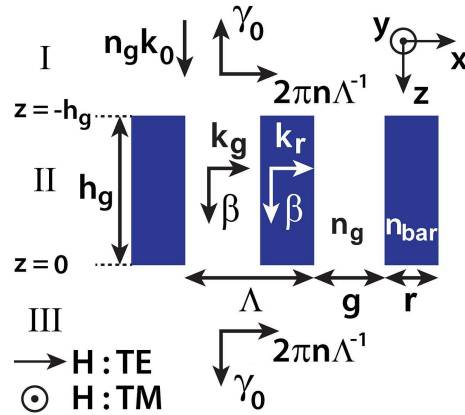


Figure 1: Geometrical description of the proposed HCG based quarter-wave plate. The incident wave is impinged on the structure from region I, where the transmitted converted wave propagates in region III.

benefiting from this theoretical consideration, rigorous coupled-wave analysis<sup>21</sup> and finite-difference time domain simulations (FDTD Solutions, Lumerical Inc.). After presenting the detailed theoretical investigation of the HCG based quarter-wave plate, we have recently demonstrated the experimental realization of another HCG based quarter-wave plate by proposing a structure with a more feasible choice of materials.<sup>22</sup>

For the theoretical study (first design), the transmission results obtained from the RCWA and FDTD based simulations reveal that an operation bandwidth of 54% and 51% can be achieved, respectively, under the assumption that the structure is in the operation regime if the conversion efficiency is equal to or larger than 0.9. Likewise, an operation bandwidth of 42% and 33% is achieved from the FDTD simulations and measurements, respectively, in the experimental study (second design). Further, it should be noted that such designs are promising for the implementation of compact and electrically thin circular polarizers by combining the proposed quarter-wave structures with HCG based,<sup>6</sup> wire grid,<sup>23</sup> thin-film grating,<sup>24</sup> or plasmonic<sup>25</sup> linear polarizers.

## 2. ANALYSIS OF THE FIRST DESIGN

Firstly, we propose a HCG based structure, for which the aim is to maximize the operation bandwidth and total transmission with a reasonable design concerning the practical realization stage. The proposed design is depicted in Fig. 1. For the achievement of a realistic design, the material constituting region III is selected as silicon-dioxide ( $\text{SiO}_2$ ). Furthermore, as a result of aiming the maximization of the operation band and the transmission through the structure, the material constituting region I and the grooves in region II is selected as also  $\text{SiO}_2$ . Finally, we select the material for the ridges as silicon (Si) due to its high refractive index and low absorption coefficient at  $\lambda_0 = 1.55 \mu\text{m}$ .

Concerning the theoretical consideration and numerical simulations, regions I and III are assumed to be extending to infinity in  $-z$  and  $+z$  directions, respectively. In order to approximate this assumption in the experimental realization stage, one can use a substrate (in region III) and deposit a dielectric layer (in region I) that is much thicker than the coherence length of the incident light.

In the subsequent subsections, we will first consider the proposed HCG theoretically, and then present circular conversion coefficients and the circular conversion efficiency spectrum.

### 2.1 Theoretical Analysis

For the purpose of analyzing the proposed HCG structure theoretically, we adopt the analysis that is inspired by the periodic waveguide interpretation and performed by Karagodsky et al.<sup>19</sup> Accordingly, we obtain the

following condition for the *unity* transmission of a TM wave that is normally incident onto the structure:

$$\left| \sum_m (a_m^{\text{TM}} - a_m^{\rho, \text{TM}}) \Lambda^{-1} \int_0^\Lambda h_{y,m}^{\text{in, TM}}(x) dx \right| = 1, \quad (1)$$

where  $a_m^{\text{TM}}$  and  $a_m^{\rho, \text{TM}}$  represent the coefficients of the magnetic field components of the  $m^{\text{th}}$  TM waveguide mode propagating in the  $+z$  and  $-z$  directions inside region II, respectively.  $\Lambda$  is the period of the HCG structure, and  $h_{y,m}^{\text{in, TM}}$  is the lateral magnetic field distribution of the corresponding TM mode. By invoking the duality principle, the unity transmission condition for TE waves can be simply written as follows:

$$\left| \sum_m (a_m^{\text{TE}} - a_m^{\rho, \text{TE}}) \Lambda^{-1} \int_0^\Lambda h_{x,m}^{\text{in, TE}}(x) dx \right| = 1. \quad (2)$$

For the achievement of the quarter-wave plate operation, i.e., transmission of a circularly polarized wave when the structure is illuminated by a linearly polarized wave with a polarization plane angle of  $\pi/4$  with respect to the  $x$ -axis on the  $xy$ -plane, it is necessary to also satisfy the following condition:

$$\angle T_{\text{TM}} - \angle T_{\text{TE}} \simeq \pi/2. \quad (3)$$

In Eq. 3, TM and TE can be interchanged and the choice is arbitrary. In this case, our choice leads to the transmission of a right hand circularly polarized wave when the polarization plane angle of the incident wave is  $\pi/4$ . The operation condition given in Eq. 3 corresponds to the following equation in the theoretical consideration:

$$\angle \left( \sum_m (a_m^{\text{TM}} - a_m^{\rho, \text{TM}}) \Lambda^{-1} \int_0^\Lambda h_{y,m}^{\text{in, TM}}(x) dx \right) - \angle \left( \sum_m (a_m^{\text{TE}} - a_m^{\rho, \text{TE}}) \Lambda^{-1} \int_0^\Lambda h_{x,m}^{\text{in, TE}}(x) dx \right) = \pm \pi/2. \quad (4)$$

Afterwards, the longitudinal wavenumber of the waveguide modes inside region II,  $\beta_m$ , can be written as a function of the incident wavelength and the lateral wavenumbers as follows:

$$\beta_m^2 = (2\pi n_g / \lambda_0)^2 - k_{g,m}^2 = (2\pi n_{\text{bar}} / \lambda_0)^2 - k_{r,m}^2, \quad (5)$$

where  $\lambda_0$  is the free-space wavelength, and  $k_{g,m}$  and  $k_{r,m}$  are the lateral wavenumbers inside  $\text{SiO}_2$  and Si, respectively. Subsequently, for TM modes, the dispersion equation, the relation between the lateral wavenumbers, is given as follows:

$$n_{\text{bar}}^{-2} k_{r,m} \tan(k_{r,m} r / 2) = -n_g^{-2} k_{g,m} \tan(k_{g,m} g / 2). \quad (6)$$

By invoking the duality principle, the dispersion relation for TE modes can be written as:

$$k_{r,m} \tan(k_{r,m} r / 2) = -k_{g,m} \tan(k_{g,m} g / 2). \quad (7)$$

The qualitative interpretation of Eqs. 6 and 7 is that the TM and TE waveguide modes can have different lateral wavenumbers, which, according to Eq. 5, results in different longitudinal wavenumbers. As a consequence, one can expect the TE and TM modes to accumulate different phases upon transmission through the HCG.

For the purpose of calculating the transmission coefficients of TE and TM waves, we invoke a two mode approximation at this point, i.e., introducing the restriction that  $m$  can be 0 and 1. Under this approximation, the longitudinal and lateral wavenumbers for TM and TE modes can be calculated using Eqs. 5 and 6, and Eqs. 5 and 7, respectively. In the calculations,  $n_{\text{bar}} = 3.48$  and  $n_g = 1.47$ , which correspond to the refractive indices of Si and  $\text{SiO}_2$ , respectively, at the frequency of interest,  $\lambda_0 = 1.55 \mu\text{m}$ . Afterwards, with the help of a custom parametric optimization code, we obtain the geometrical parameters, for which Eqs. 1, 2, and 4 are satisfied simultaneously, by using the following definitions for  $h_{y,m}^{\text{in, TM}}$  and  $h_{x,m}^{\text{in, TE}}$ :<sup>19</sup>

$$h_{y,m}^{\text{in, TM}} = h_{x,m}^{\text{in, TE}} = \begin{cases} \cos(k_{r,m} r / 2) \cos[k_{g,m} (x - g / 2)], & \text{inside the grooves} \\ \cos(k_{g,m} g / 2) \cos\{k_{r,m} [x - (g + \Lambda) / 2]\}, & \text{inside the ridges} \end{cases}. \quad (8)$$

Accordingly, the optimal geometric parameters for quarter-wave plate operation at  $\lambda_0 = 1.55 \mu\text{m}$  are obtained as  $r = 160 \text{ nm}$ ,  $g = 220 \text{ nm}$ , and  $h_g = 550 \text{ nm}$ . The lateral wavenumbers of TM modes for these geometric parameters are calculated as  $k_{g,0}^2 = -4.2/\Lambda^2$ ,  $k_{r,0}^2 = 19.43/\Lambda^2$  and  $k_{g,1}^2 = 31.3/\Lambda^2$ ,  $k_{r,1}^2 = 54.9/\Lambda^2$ . Similarly, for TE modes, we obtain  $k_{g,0}^2 = -13.1/\Lambda^2$ ,  $k_{r,0}^2 = 10.48/\Lambda^2$  and  $k_{g,1}^2 = 30.2/\Lambda^2$ ,  $k_{r,1}^2 = 53.8/\Lambda^2$ . Recalling that, in such a waveguide, the cutoff condition is given by  $k_r^2 = (n_{bar}/n_g)^2 k_g^2$  and thus, it is seen that only the first modes in the TM and TE cases are propagating modes with  $\beta_m^2 > 0$ . The second modes in both cases correspond to exponentially decaying modes with  $\beta_m^2 < 0$ . In addition, the longitudinal wavenumbers of the diffraction orders is given by  $\gamma_n^2 = (2\pi n_g)^2 (\lambda_0^{-2} - n^2 \Lambda^{-2})$ , where  $n$  denotes the diffraction order. Since  $\lambda_0/\Lambda = 4.1$  in the proposed design, it follows that  $\gamma_0^2 > 0$ , where  $\gamma_n^2 < 0$  for  $\forall n, n \neq 0$ . In other words, only  $0^{th}$  reflection and transmission orders are propagating, which results in the fact that, if a planewave propagating in the  $+z$  direction is impinged on the structure, the reflected and transmitted waves are planewaves propagating in the  $-z$  and  $+z$  directions, respectively.

Finally, we calculate the complex transmission coefficients,  $T_{\text{TM}}$  and  $T_{\text{TE}}$ , theoretically. We obtain  $|T_{\text{TM}}| = 0.988$  and  $|T_{\text{TE}}| = 0.936$ , where  $\angle T_{\text{TM}} - \angle T_{\text{TE}} = 92^\circ$ . The resulting transmission coefficients for the aforementioned geometrical parameters suggest that the desired quarter-wave operation regime is achieved theoretically. For detailed information regarding the calculation of the transmission coefficients, we suggest the readers to refer to Ref. 19.

## 2.2 Numerical Validation

For the purpose of validating our theoretical predictions, we employ numerical simulations based on RCWA and FDTD method. Using these methods,  $T_{\text{TM}}$  and  $T_{\text{TE}}$  are calculated. In RCWA, we neglect the material dispersion, whereas we take the material dispersion into account properly in the FDTD method. Subsequently, the circular conversion coefficients,  $C_+$  (for right-hand circularly polarized waves) and  $C_-$  (for left hand circularly polarized waves), which indicate the amplitudes and phases of the circularly polarized waves at the output interface for an incident plane wave with a polarization plane angle of  $\pi/4$ , can be directly calculated by a simple transformation of the basis vectors as  $C_\pm = 0.5 (T_{\text{TM}} \mp iT_{\text{TE}})$ .<sup>26</sup>

For being able to measure the degree of conversion from the linear polarization to the circular one, we define the conversion efficiency parameter,  $C_{\text{eff}}$ , as follows:

$$C_{\text{eff}} = \frac{|C_+|^2 - |C_-|^2}{|C_+|^2 + |C_-|^2}. \quad (9)$$

It is noteworthy that the ellipticity parameter,  $\eta$ , can be directly calculated from the  $C_{\text{eff}}$  spectrum as follows:

$$\eta = \arctan \left( \frac{\sqrt{(1 + C_{\text{eff}})/(1 - C_{\text{eff}})} - 1}{\sqrt{(1 + C_{\text{eff}})/(1 - C_{\text{eff}})} + 1} \right). \quad (10)$$

Using the relation given in Eq. 10, it can be shown that  $C_{\text{eff}} = 0.9$  corresponds to  $\eta = 32^\circ$ . Due to the one-to-one correspondence between  $C_{\text{eff}}$  and  $\eta$ , we only provide  $C_{\text{eff}}$  in this paper.

The circular conversion coefficients obtained from RCWA and the conversion efficiency spectrum obtained from RCWA and FDTD simulations are shown in Fig. 2. The presented results obtained from RCWA suggest that a conversion efficiency that is larger than 0.9 is achieved between  $1.36 \mu\text{m}$  and  $2.36 \mu\text{m}$ . The FDTD results suggest a narrower wavelength band,  $1.4 \mu\text{m} - 2.36 \mu\text{m}$ , as a consequence of the dependence of the refractive index of Si on the wavelength. For the calculation of the percent bandwidth of operation, we use the following classical definition:<sup>27</sup>

$$\text{BW}\% = 200\% \frac{\lambda_H/\lambda_L - 1}{\lambda_H/\lambda_L + 1}, \quad (11)$$

where  $\lambda_H$  and  $\lambda_L$  are the higher and lower corner wavelengths of the operation band, respectively. Using the definition given in Eq. 11, we obtain  $\text{BW}\% = 54\%$  and  $\text{BW}\% = 51\%$  from the RCWA and FDTD results, respectively.

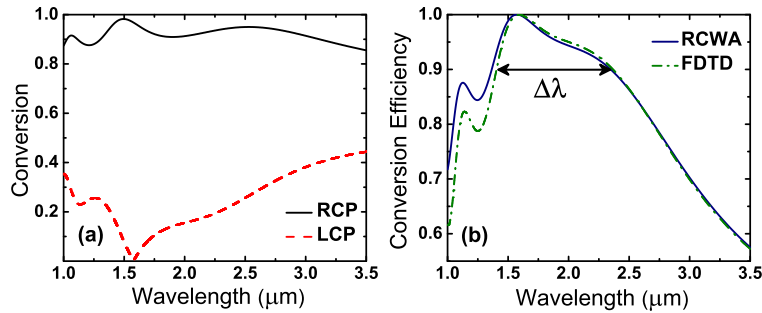


Figure 2: (a) Circular conversion coefficients obtained using the RCWA and (b) the conversion efficiencies obtained from the RCWA and FDTD. The wavelength range for the FDTD result satisfying the 0.9 efficiency threshold is denoted by  $\Delta\lambda$ .

### 3. ANALYSIS OF THE SECOND DESIGN

After demonstrating the possibility of a HCG based quarter-wave plate in Section 2, we modify the design depicted in Fig. 1 such that the choice of materials is more feasible for fabrication. In this design, the material filling region III is sapphire, whereas region I and the grooves in region II are filled with free-space.

For the present design, a theoretical interpretation is not provided since it is largely similar to the one shown in Section 2.1. However, one major difference arises from the choice of different materials for region I and III. In the present case, the longitudinal wavenumber of the zeroth reflection order is given by  $\gamma_{0,I} = 2\pi\lambda_0^{-1}$ , where, for the zeroth transmission order, we have  $\gamma_{0,III} = 2\pi n_s \lambda_0^{-1}$ . This characteristic conduces to discrepant lateral magnetic field distributions in regions I and III. Thus, one should pay attention to the utilization of correct distributions while matching the tangential electric and tangential magnetic fields at  $z = 0$  and  $z = -h_g$ .

#### 3.1 Numerical Results

The geometrical parameters of the HCG structure for optimal operation, i.e., *unity* conversion efficiency at  $\lambda_0 = 1.55 \mu\text{m}$ , are obtained by utilizing the theoretical model and RCWA simulations as  $r = 220 \text{ nm}$ ,  $g = 350 \text{ nm}$ , and  $h_g = 320 \text{ nm}$ . Subsequently, FDTD simulations are run in order to characterize the transmission of the

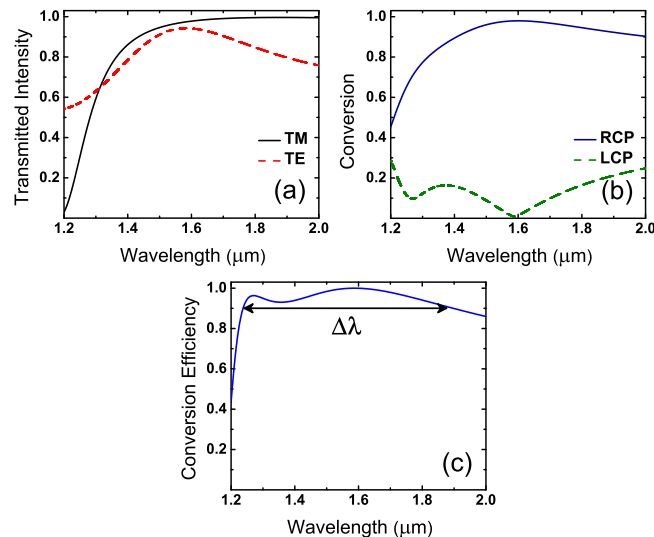


Figure 3: (a) Circular conversion coefficients obtained using the RCWA and (b) the conversion efficiencies obtained from the RCWA and FDTD. The wavelength range for the FDTD result satisfying the 0.9 efficiency threshold is denoted by  $\Delta\lambda$ .

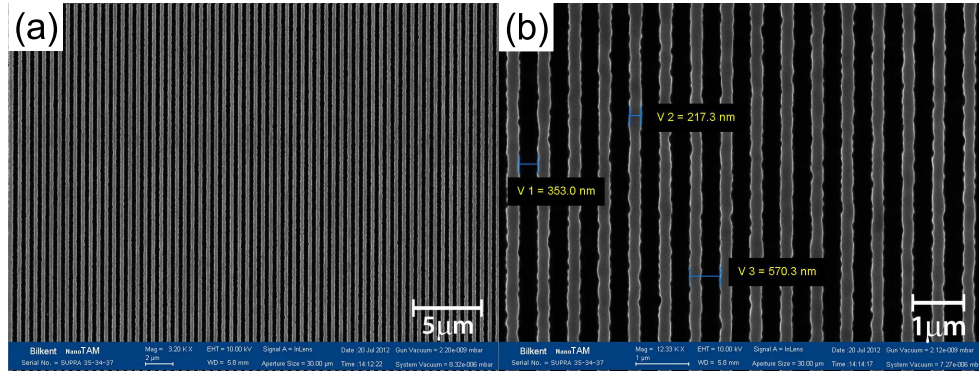


Figure 4: (a) Zoomed out and (b) zoomed in top view SEM micrographs of the fabricated HCG structure. In (b), the legends V1, V2, and V3 denote the geometrical parameters  $g$ ,  $r$ , and  $\lambda$ , respectively.

proposed structure. The numerically obtained normalized transmitted intensities ( $|T_{TM}|^2$  and  $|T_{TE}|^2$ ) are shown in Fig. 3(a).

In the close neighborhood of  $\lambda_0 = 1.55 \mu\text{m}$ , the conditions given in Eqs. 1, 2, and 4 are satisfied simultaneously, which result in the transmission of a right hand circularly polarized wave assuming that a planewave with a polarization plane angle of  $\pi/4$  is impinged on the structure. The conversion coefficients are calculated using the same formulation given in Sec. 2.2 and the results are shown in Fig. 3(b). Finally, the conversion efficiency spectrum is calculated using Eq. 9 and shown in Fig. 3. The numerical results suggest that the condition  $C_{\text{eff}} > 0.9$  is satisfied in the wavelength interval  $1.24 \mu\text{m} - 1.40 \mu\text{m}$ . By using Eq. 11, it is calculated that this wavelength interval corresponds to a percent bandwidth of 42%.

### 3.2 Fabrication

The proposed HCG based quarter-wave plate is fabricated using a silicon-on-sapphire wafer (Valley Design Corporation). The thickness of the sapphire (R-plane) substrate is specified as  $0.52 \pm 0.05 \text{ mm}$ . The  $\langle 100 \rangle$  Si layer is grown epitaxially on the substrate and its thickness is  $600 \pm 60 \text{ nm}$ . The fabrication of the structure starts with the reduction of the thickness of the Si layer to 320 nm by using sulfur hexafluoride chemistry based reactive ion etching (RIE). Afterwards, an electron beam sensitive photoresist, poly(methyl methacrylate), is deposited on the wafer by means of spinning. After photoresist deposition, the desired regions are exposed by the e-beam lithography technique. The e-beam step is followed by the development of the photoresist. Finally, the unexposed Si regions are etched with the aid of the RIE system. The scanning electron microscope micrographs of the fabricated HCG structure are shown in Fig. 4.

### 3.3 Experimental Setup

The detailed outlines of the two experimental setups are depicted in Fig. 5. The first setup, see Fig. 5(a), is utilized for measuring the intensity transmission coefficients,  $|T_{TM}|^2$  and  $|T_{TE}|^2$ . In this measurement, the sample is illuminated by a broadband near-infrared light source (Spectral Products, ASBN-W100-F-L) and the polarization of the incident wave is set to either TM or TE polarization by the usage of an adjustable linear polarizer (Thorlabs, DGL10). The spot size of the incident light on the sample is set to  $50 \mu\text{m}$  with the aid of standard commercial objectives. The transmitted light is collimated by the objectives at the output interface and coupled into the fiber. Finally, the spectrum of the transmitted wave is analyzed by the spectrometer (Ocean Optics, NIR256-2.5).

The second setup, see Fig. 5(b), is utilized for the measurement of the circular conversion coefficients,  $C_+$  and  $C_-$ . Considering that the linear polarizer at the input interface makes an angle of  $45^\circ$  with the  $x$ -axis on the  $xy$ -plane and the quarter-wave plate (Thorlabs, WPQ05M-1550) is oriented such that its fast axis is along the  $x$  direction, the HCG is illuminated by a right hand circularly polarized wave. Using Jones calculus, the

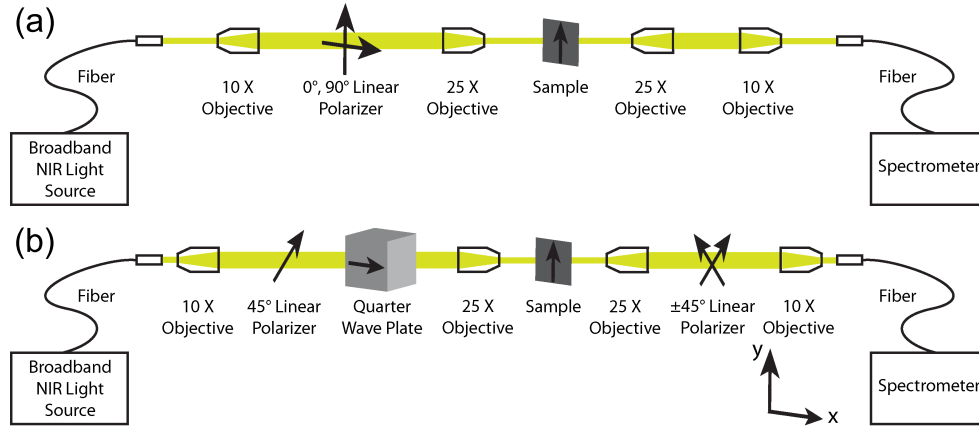


Figure 5: Visual illustrations of the experimental setups that are utilized for the measurement of (a) linear transmission and (b) circular conversion coefficients.

transmission characteristics of the HCG can be described as follows:

$$\begin{pmatrix} E_x^t \\ E_y^t \end{pmatrix} = \begin{pmatrix} T_{TM} & 0 \\ 0 & T_{TE} \end{pmatrix} \begin{pmatrix} E_x^i \\ E_y^i \end{pmatrix}, \quad (12)$$

where  $E^i$  and  $E^t$  denote the incident and transmitted fields, respectively. Therefore, by aligning the linear polarizer transmission axis at  $-45^\circ$  and  $45^\circ$ , we measure  $|C_+|^2$  and  $|C_-|^2$ , respectively. For instance, it is seen that, if the structure is illuminated by a right hand circularly polarized wave with unity amplitude at  $\lambda_0 = 1.55 \mu\text{m}$ , the transmitted wave will be represented as  $(1/\sqrt{2}; -1/\sqrt{2})$  and passed by a polarizer with its transmission axis aligned at  $-45^\circ$ . Similarly, at  $\lambda_0 = 1.55 \mu\text{m}$ , a linear polarizer oriented at  $45^\circ$  passes the transmitted wave,  $(1/\sqrt{2}; 1/\sqrt{2})$ , when the structure is illuminated by a left hand circularly polarized wave with unity amplitude.

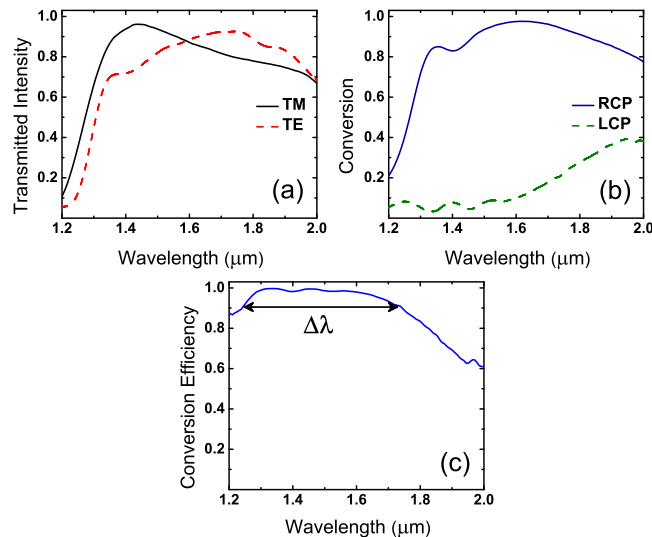


Figure 6: Experimentally obtained (a) TM and TE transmitted intensities, (b) circular conversion coefficients, and (c) conversion efficiency spectrum. The wavelength interval of operation is denoted by  $\Delta\lambda$ . The experimental conversion efficiency spectrum yields a percent bandwidth of 33%.



### 3.4 Experimental Results

The linear intensity transmission coefficients,  $|T_{\text{TM}}|^2$  and  $|T_{\text{TE}}|^2$ , measured using the setup shown in Fig. 5(a) are shown in Fig. 6(a). The circular conversion coefficients measured using the setup shown in Fig. 5(b) are shown in Fig. 6(b). Finally, the conversion efficiency spectrum,  $C_{\text{eff}}$ , is calculated from the circular conversion coefficients by using Eq. 9 and plotted in Fig. 6(c). The experimental  $C_{\text{eff}}$  spectrum suggests that the lower and higher corner wavelengths are  $\lambda_L = 1.25 \mu\text{m}$  and  $\lambda_H = 1.75 \mu\text{m}$ , respectively, which result in a percent bandwidth of 33%. Although the experimental bandwidth is smaller compared to the numerical one, 42%, the experimental results are in good agreement with the numerical ones.

## 4. CONCLUSIONS

In conclusion, we have shown the theoretical realization and the experimental characterization of broad-band quarter-wave plates that are composed of two-dimensional HCGs. While the material chosen for the ridges remain same both in theoretical and experimental studies, the material used for the substrate is changed to Sapphire from  $\text{SiO}_2$  for the purpose of achieving a more fabricable design. For the first design, it is shown that a conversion efficiency that is higher than 0.9 can be achieved in theoretical and numerical percent bandwidth of 54% and 51%, respectively. Similarly, a percent bandwidth of 42% and 33% is achieved numerically and experimentally for the second design. The possible application areas of the proposed quarter-wave plates can include liquid crystal displays, laser applications and remote sensors.

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