# DESIGN OF AN S-BAND POWER COMBINER SYSTEM WITH TWO PARALLEL POWER AMPLIFIERS AND PHASE SHIFTERS 

A THESIS<br>SUBMITTED TO THE DEPARTMENT OF ELECTRICAL AND<br>ELECTRONICS ENGINEERING<br>AND THE GRADUATE SCHOOL OF ENGINEERING AND SCIENCE OF BILKENT UNIVERSITY<br>IN PARTIAL FULFILLMENT OF THE REQUIREMENTS<br>FOR THE DEGREE OF<br>MASTER OF SCIENCE

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August 2011

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## ABSTRACT

# DESIGN OF AN S-BAND POWER COMBINER SYSTEM WITH TWO PARALLEL POWER AMPLIFIERS AND PHASE SHIFTERS 

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RF power amplifiers are important blocks in a wireless communication system that play a vital role in determining the level of overall performance. In some situations, more power than a single power amplifier can alone provide is required in applications such as a radar or a space communication system. In such cases, power combiners that can surpass the maximum output power level of a single power amplifier should be used. In this thesis, we study the performance of a power combiner built in classical binary structure. The combiner operates at 3 GHz (S-band) and comprises two power amplifiers which can supply up to 38 dBm of saturated power. Wilkinson power dividers/combiners are utilized at the input/output respectively in order to divide and combine the input and output signals. While building a power combiner, one should also note that the phases of the amplified signals should be matched at the output or else the level of combining loss can reach significant levels. At a phase difference of $180^{\circ}$, the signals will be completely out of phase and will combine destructively at the output. Therefore, in our study, in order to be able to control the phases at each arm of the power combiner, two tunable microwave phase shifters are
placed before the active devices. The phase shift generated by these shifters are controlled via voltage, hence a desired level of phase shift can be obtained. By this, we demonstrate that phase shifters are also important structures for a power combiner that are instrumental in accomplishing a phase balance between the two arms. The idea behind the work displayed here can be extended to applications requiring much higher power levels or operating at higher frequencies.

Keywords: RF Power Amplifiers, Power Combiners, Phase Shifters, Microwave Design

# S-BANDINDA ÇALIŞAN İKİ PARALEL GÜÇ YÜKSELTİCİL̇ VE FAZ KAYDIRICILI BIR GÜÇ BİRLEŞTİRİCİ SİSṪEM TASARIMI 

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RF güç yükselticileri kablosuz iletişim sistemlerinde genel performansı belirleyici bir unsur olarak önemli bir rol oynamaktadır. Radar ya da uzay iletişim sistemleri gibi bazı uygulamalarda, bazen bir tek güç yükselticisinin sağlayabileceği güçten daha fazla bir güce ihtiyaç duyulduğu durumlar olabilir. Bu gibi durumlarda, tek bir güç yükselticisinin verebileceği maksimum gücü aşabilen güç birleştiricileri kullanılmalıdır. Bu tezde, klasik ikili (binary) yapıya sahip bir güç birleştiricisinin performansı incelenmektedir. Birleştirici, 3 GHz 'de (S-bandı) çalışmakta ve 38 dBm doymuş çıkış gücüne sahip iki güç yükselticisi içermektedir. Giriş/çıkış sinyallerini bölmek/birleştirmek amacıyla giriş ve çıkışta Wilkinson birleştiricisi/bölücüsü kullanılmıştır. Bir güç birleştiricisi tasarlarken dikkat edilmesi gereken bir husus, yükseltilmiş çıkış sinyallerinin fazlarının uyumlu olmasıdır. Aksi halde, birleştirme kaybı önemli seviyelere ulaşabilir. $180^{\circ}{ }^{\circ}$ lik bir faz kayması halinde sinyaller tamamen fazdışı olacak ve çıkışta birbirlerini yok edecek şekilde birleşeceklerdir. Bu nedenle, bu çalışmada, güç birleştiricisinin her bir kolundaki fazı control edebilmek amacıyla, aktif devrelerin önüne iki tane ayarlanabilir mikrodalga faz kaydırıcısı konulmuştur. Bu faz kaydırıcılarından elde
edilen faz kaymaları dışarıdan voltaj ile kontrol edilerek istenen değere ayarlanabilmektedir. Böylece, faz kaydırıcılarının güç birleştiricileri için iki koldaki fazlar arasında bir denge ayarlanmasında önemli yapılar olduğu gösterilmektedir. Bu çalışmadaki düşünce, çok daha yüksek güç seviyesinin söz konusu olduğu ya da daha yüksek frekanslarda çalışan uygulamalara da uyarlanabilir.

Anahtar Kelimeler: RF Güç Yükselticileri, Güç Birleştiricileri, Faz Kaydırıcıları, Mikrodalga Tasarım

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Dedicated to my parents

## Chapter 1

## Introduction

Power amplifiers are the blocks which are generally used before the antenna at the front-end of the transmitter side of a communication system. They are generally designed such that they supply the highest power possible. Thus, the main goal of a power amplifier is to boost power. The recent developments on semiconductor technology have allowed very high levels of output powers to be reached with single devices. High electron-mobility transistors (HEMTs) that are generally fabricated on gallium-nitride ( GaN ) substrates have very high output power densities. Examples include a device with a power density of $30 \mathrm{~W} / \mathrm{mm}$ at 4 GHz with a power-added efficiency of $50 \%$ [1], and another with a power density of $9.4 \mathrm{~W} / \mathrm{mm}$ at 10 GHz with a power-added efficiency of $40 \%$ [2]. These devices have also started to be frequently popular in the industry and several companies produce high-power microwave transistors which are suitable for power amplifier design.

On the other hand, there still are applications which may require a level of power that cannot be supplied by a single device alone. For example, at millimeter wave frequencies, large output powers can only be achieved by summing the power from multiple devices [3]. There may also be types of applications where
specific elements cannot endure a high level of power so that the power that is delivered to them should be divided. In these cases, a power dividing/combining technique is used. Space communication systems and radars are the areas where power combining is frequently used.

While combining power, an important issue to be considered is the balance of the phases experienced by the input signal at each of the arms to be combined. Generally the length of the transmission lines used at each arm of the power combiner is the same, but the phase shifts presented by the active devices to the input signals may be different. This causes a difference in the phases of the signals at each arm. When these signals are combined, this leads to a combining loss in the output signal. The phase imbalances can also be due to the variability of the phase and amplitude of the inputs if they do not come from an in-phase power splitter. The power combining structures like couplers or waveguides are also prone to having amplitude and phase imbalances.

In order to show this effect, let us take two sinusoidal signals at the same frequency $\omega$ and same normalized amplitude of 1 but that have a phase difference of $\phi$. When these two signals are added, the combined signal will be:

$$
\begin{align*}
S_{\text {out }} & =\sin (\omega t)+\sin (\omega t+\phi)  \tag{1.1}\\
& =2 \cos \left(\frac{\phi}{2}\right) \sin \left(\omega t+\frac{\phi}{2}\right) \tag{1.2}
\end{align*}
$$

Hence, the combined signal is also a sinusoid with the same frequency as the added signals, and its phase is equal to the arithmetic average of the phases of the combined signals. What is important here is that what determines the amplitude of the signal is also the phase difference between the combined signals. If $\phi$ is equal to 0 , then the amplitude of the resulting signal will be twice the amplitude of each signal. If $\phi$ is equal to $\pi$, then the combined signal will be 0 , which is the case of combining completely destructive signals. This clearly shows that the phases experienced at the arms of a power combiner are vital in designing the power combiner. In order to equal the phases, phase shifters can be
employed either before or after the amplifiers at each arm. Tunable phase shifters can provide the additional phase necessary to obtain a proper phase balance.

In the literature, power combiners utilizing several power amplifiers were proposed in many configurations, in both corporate and spatial fashion. Some of the proposed structures assumed that the power amplifiers were identical and the phase shifts for each amplifier were insignificant and negligible [4]. Others took these phase changes into account and developed structures to be able to control the phase characteristics or observed the effect of phase mismatches on the power combining efficiency, if the phase shifts were not controlled [5-9]. Some works have focused on the effects of the combiner structure and variability of phase and amplitude of the combined sources on parameters like noise, combining efficiency or system power-added efficiency and presented a theoretical analysis [10-13]. The effects of power splitter and combiner imbalances have also been analyzed in the literature [5].

In this work, we present a 1 -stage power combiner in classical binary form comprising two power amplifiers. The power amplifiers operate at 3 GHz and provide a saturated output power of more than 38 dBm . The power amplifiers were designed as a part of a project with Meteksan Savunma A.Ş., and they were then used as the active elements in the power combiner design. The combiner also employs two tunable phase shifters which are used to tune the phases of the two arms. The phase shifters are placed before the amplifiers in order to prevent a high level of power to the phase shifters. The input RF signal is divided via a Wilkinson power splitter and fed to two arms. In the output, a Wilkinson power combiner is used to combine the amplified signals. The effect of phase mismatches on system characteristics like combining efficiency is investigated via this system and it is shown that a phase shifter is an important block in power combiner design.

In Chapter 2, available power combining techniques are explained and the advantages and disadvantages of each method is discussed. In Chapter 3, the design and testing of the power amplifiers are explained. In Chapter 4, phase shifters are discussed and the phase shifter design used in the power combiner is described. In Chapter 5, the testing of the whole system is explained and the obtained results are discussed. Chapter 6 concludes the thesis.

## Chapter 2

## Power Combining Techniques

### 2.1 Types of Power Combiners

Power combining techniques are mainly classified in two groups: Corporate combining techniques and parallel combining techniques like spatial combiners. Corporate power combiners consist of multiple stages and each stage has multiple inputs and an output. The most common configuration of the corporate combiners are in binary configuration, where each stage has two inputs and an output. Therefore, one can only combine a number of signals which is a power of 2 , and the relationship between the number of inputs (N) and the number of corresponding stages ( S ) is given as

$$
\begin{equation*}
N=2^{S} . \tag{2.1}
\end{equation*}
$$

Multiple stage power combiners with binary structure generally consist of Wilkinson couplers, $90^{\circ}$ (quadrature) -hybrid branch line couplers, coupled-line couplers, Lange couplers, rat-race couplers, etc. There are also nonbinary structures that achieve the combining in several stages, which are called a coupled or a serial combiner, in which each successive combiner adds $1 / \mathrm{N}$ of its output power to the total output power [6]. Spatial power combiners are combiner types that
generally employ waveguide or cavity-type structures in order to combine the amplifying blocks in 3 -d [7, 8]. Corporate and spatial power combiner configurations are depicted in Figure 2.1.

(a)

(b)

Figure 2.1: Power combining techniques: a) Corporate power combining, b) Spatial power combining

Power combiners can be realized in many forms like microstrip, stripline or coaxial transmission lines or waveguides and cavities. Many power combiner classes like Wilkinson, coupled-line or branch line couplers are symmetrical and can also be used to divide power as well as to combine it. Power combiners can also be classified according to their number of ports or the phase difference between their two outputs. Wilkinson power combiners and T-junctions are examples of 3 -port structures while directional couplers (branch line couplers, rat-race couplers, Lange couplers, etc.) are 4-port structures. With respect to the phase, the outputs of a branch line coupler or a Lange coupler have $90^{\circ}$ phase difference which are therefore called quadrature couplers while a rat-race coupler, a tapered coupled line coupler or a magic-T are examples of $180^{\circ}$ structures. The outputs of a classical 3-port Wilkinson divider are in-phase. It is also important whether a power divider divides the input power equally between its output ports. Hybrid ( 3 dB ) couplers are a special form of directional couplers such
that when they are used as power dividers, they divide the input signal equally ( 3 dB less than the input) into two equal output signals.

In Table 2.1, several common power combiner types are classified with respect to their configuration, number of ports and output phase characteristics.

| Power Combiner Type | Transmission line <br> or Waveguide | Phase difference <br> between outputs | Number of ports |
| :--- | :---: | :---: | :---: |
| Wilkinson Combiner | TL | $0^{\circ}$ | 3 (in general) |
| Rat-race (Ring) Coupler | TL | $180^{\circ}$ | 4 |
| Branch-line Coupler | TL | $90^{\circ}$ | 4 |
| Lange Coupler | TL | $90^{\circ}$ | 4 |
| Coupled-line Coupler | TL | $90^{\circ}$ | 4 |
| Magic-T | Waveguide | $180^{\circ}$ | 4 |
| Bethe-hole Coupler | Waveguide | $90^{\circ}$ | 4 |

Table 2.1: Frequently used types of power combiners and their classification

All of the structures given in Table 2.1 can be achieved in hybrid form.

As mentioned before, directional couplers are 4-port devices that are used as both power combining and dividing structures. The symbol and ports of a directional coupler are shown in Figure 2.2.


Figure 2.2: The symbol and ports of a directional coupler

The input signal is divided (in equal parts if hybrid) and fed into the through and coupled ports, while no signal is sent to the isolated port. There is generally a $90^{\circ}$ or $180^{\circ}$ of phase difference between the two output ports, which makes the couplers a perfect tool as power combining structures. As mentioned above, the directional couplers can be constructed in many forms such as Lange coupler or branch line coupler. The main compromise in these different types of couplers
is the ease of fabrication versus the bandwidth. For example, Lange couplers are more difficult to design and build but have a higher bandwidth than the branch line couplers. In addition to the corporate and spatial combiners, radial combiners can also be used to combine power. These structures offer a high bandwidth but they are harder to build.

Other than the power combiners just mentioned, structures which are used to increase the gain can also be discussed. Among these configurations, cascading several devices or using structrues like a traveling-wave (distributed) amplifier are notable options. Traveling-wave structures employ active devices (transistors or vacuum tubes) which are placed between two branches of gate (input) and drain (output) transmission lines whose lengths are set such that the delays at each device at the input and output lines are equal. The input signal propagates through the input line and gets amplificated by each active device, resulting in a signal traveling through the output line. The use of transmission line theory in amplification leads to a gain which shows additive property (overall gain is the sum of the gains from each active device) unlike the cascading of amplifiers where the overall gain is the multiplication of the gains of separate devices. This may seem as a compromise, but in return, the bandwidth can be increased without limits in theory. In reality, what limit the bandwidth are the device parasitics.

A power combining structure where the quadrature directional couplers are used is the balanced amplifier. The balanced amplifiers have two transmission line branches employing power amplifiers in between. Hybrid couplers are placed in the input and the output; where the input coupler divides the signal in two equal parts and the output coupler is used to combine the amplified signals. One advantage of using quadrature hybrid couplers is that the possible reflected signals from the amplifiers combine destructively at the input port of the coupler since there is a $90^{\circ}$ of phase difference between two output ports and the reflected signals which make a round-trip create a $180^{\circ}$ of phase shift. The isolated port
of the coupler is terminated via a resistor, and the reflected signals which add in phase are dissipated there. A similar task is also achieved by the output coupler, and the amplified signals which are added in phase to make up the combined signal are collected at the output.

### 2.2 Some Considerations in Power Combiners

While designing a power combiner, one has to consider the phase delay differences that occur due to both the power combiner/divider structure and to the power amplifiers used in the design. Many designs assume that the phase shifts in each unit amplifier are equal. In practice, unit amplifiers cannot avoid having variations in their output power and transmission phase even if the amplifiers have the same design and are produced in the same lot [9, 10]. This problem makes the phase balance in power combiners a key issue for high power combining efficiencies.

In Figure 2.3, a typical N -way power combiner structure is shown. $L_{i}$ and $L_{o}$ are the power transmission factors. For example, for a $3-\mathrm{dB}$ input loss, $L_{i}=0.5$.


Figure 2.3: A typical power combiner structure

Assuming that all of the power amplifier outputs are in-phase and each of them is equal to $P_{o a}$, and the combiner is well-matched and balanced, the combining efficiency $\eta_{c}$ is given as [11]

$$
\begin{equation*}
\eta_{c}=\frac{P_{o}}{N P_{o a}} . \tag{2.2}
\end{equation*}
$$

Note that this ratio is equal to $L_{o}$, which implies that the combining efficiency is only dependent on the output power transmission factor under the assumptions made above.

DC power consumption is another important concept in power amplifiers. Although it can be expressed in many ways, the most commonly used is the power-added efficiency (PAE). It is given as [3]

$$
\begin{equation*}
P A E=\frac{P_{o a}-P_{i a}}{P_{d c a}} . \tag{2.3}
\end{equation*}
$$

The relationships between important design parameters like power, efficiency, noise or graceful degradation in large power combiner systems are discussed in detail by R.A.York in [11]. This work emphasizes that the ratio of overall PAE of the general combiner system to the PAE of a single combiner is an important indicator of how well several power amplifier outputs are combined without degradation in a power combiner. If we call the PAE of an individual amplifier as $\eta_{a}$, then PAE of the overall system, $\eta_{s y s}$, can be written as

$$
\begin{equation*}
\eta_{s y s}=\frac{P_{o}-P_{i}}{P_{d c}}=\frac{P_{i}\left(L_{i} G L_{o}-1\right)}{N P_{d c a}}=\frac{\left(L_{i} G L_{o}-1\right)}{L_{i}(G-1)} \eta_{a} . \tag{2.4}
\end{equation*}
$$

It is thus seen that in the limit of high gain, $\eta_{s y s} \rightarrow \eta_{a} \eta_{c}$. Therefore, it can be deduced that high gain can compensate for the effect of input losses in a power combiner. Since the combining efficiency is defined solely by the output loss, $\eta_{\text {sys }}$ is limited only by the output loss in the condition of high gain.

The question of which power combining scheme is better to use is also another important consideration. Unlike corporate combiners, the combining efficiency
of parallel combining schemes such as spatial combiners or radial combiners does not change much with the number of devices combined. On the other hand, they offer poorer combining efficiency than classical corporate combiners when small numbers of power amplifiers are combined. Therefore, it is more advantageous to use these schemes at large combining arrays. An ideal binary corporate network has a total output loss of $L_{o}=\alpha^{S}$ where $\alpha$ is the loss per stage and S is the number of stages. If we call the constant output loss of a spatial combiner as $S_{o}$, it is seen that after a specific number of amplifiers combined, the combining efficiency of the spatial combiners start to surpass that of the corporate combiners. This critical number of devices is given as [11]

$$
\begin{equation*}
N_{c}=2^{S_{o}[d B] / \alpha[d B]} . \tag{2.5}
\end{equation*}
$$

A typical value of $\alpha$ for a Wilkinson divider at X-band is about 0.15 dB , while $S_{o}$ of a spatial power combiner is about 0.5 dB [11]. Using these numbers, it is seen that at X-band, spatial power combiners are preferable to corporate power combiners for $N \geq 10$ number of devices combined. For $N<10$, corporate binary networks are favorable.

This analysis assumes that the unit amplifiers used in the combiner are identical and hence the amplifier outputs are in-phase and equal in magnitude. As mentioned before, other than the output losses of the combiner, the phase imbalances also play an important role in determining the combining efficiency. Thus it is essential to take these imbalances into account for accurate results. In the literature, this has been evaluated in several works in terms of its effects on the graceful degradation or power combining efficiency characteristics of the power combiner systems [12, 10, 13].

A simplified approach to power combiners in terms of current and voltage is given by Tokumitsu et. al. in [9]. If $V_{k} e^{j \theta_{k}}$ voltage signals are added in a combiner, where $k=1,2, \ldots, N$ and at each branch a current of $i_{1}, i_{2}, \ldots, i_{N}$ flows
over a generator impedance of $Z_{o}$, then at the output of the combiner, a total current of $i_{1}+i_{2}+\ldots+i_{N}$ flows through a load of $Z_{o} / N$ under the condition of impedance matching. Then, at the $k$ th branch, the relationship between voltage and current can be written as:

$$
\begin{equation*}
V_{k} e^{j \theta_{k}}=Z_{o} i_{k}+\frac{Z_{o}}{N}\left(i_{1}+\ldots+i_{N}\right) \tag{2.6}
\end{equation*}
$$

The power dissipated in the load is obtained as

$$
\begin{align*}
P_{o} & =\left|i_{1}+\ldots+i_{N}\right|^{2} \frac{Z_{o}}{N}  \tag{2.7}\\
& =\frac{1}{4 N Z_{o}}\left|\sum_{k=1}^{N} V_{k} e^{j \theta_{k}}\right|^{2} \tag{2.8}
\end{align*}
$$

The transition from Equation 2.7 to Equation 2.8 is given in Appendix A. The total generated power is given as

$$
\begin{equation*}
P_{T}=\frac{1}{4 Z_{o}} \sum_{k=1}^{N}\left|V_{k} e^{j \theta_{k}}\right|^{2} . \tag{2.9}
\end{equation*}
$$

The combining efficency $\eta_{c}$ is the ratio of the power dissipated in the load to the total generated power and is equal to:

$$
\begin{align*}
\eta_{c} & =\frac{P_{o}}{P_{T}} \mathrm{x} 100(\%)  \tag{2.10}\\
& =\frac{\left|\sum_{k=1}^{N} V_{k} e^{j \theta_{k}}\right|^{2}}{N \sum_{k=1}^{N} V_{k}^{2}} \mathrm{x} 100(\%) \tag{2.11}
\end{align*}
$$

This formula derived in [9] is useful to plot the combining efficiency versus the variations at the phases or the power levels of the combined input signals. This plot is seen below in Figure 2.4.

In order to produce the plot in Figure 2.4, it was assumed that the variations in phase and power were uniformly distributed. For example, a phase variation of $20^{\circ}$ means that each combined signal has a uniformly distributed random phase ranging from $-10^{\circ}$ to $10^{\circ}$ with respect to some arbitrary reference. The same is


Figure 2.4: Change of combining efficiency with input phase and power variations
also valid for the power plot. For example, for 4 dB variation, the amplitude of each of the combined signals uniformly changes between $10^{(-4 / 20)}=0.631$ and 1. The amplitudes of the combined signals were taken as equal for the plot of phase variations, and the phases were taken as equal for the plot of power variations. In order to get smooth-shaped curves, a combined signal number $N=10000$ was assumed. As visible in the figure, in order to achieve a combining efficiency better than $99 \%$, a maximum phase variation of $15^{\circ}$ or a maximum power variation of 2.6 dB is necessary [9]. These numbers are also comparable with the rated phase and amplitude imbalances of power combining structures, which will cause extra variations in both the phases and the amplitudes. For example, a typical specification of a 1 to $12.4 \mathrm{GHz} 180^{\circ} 3 \mathrm{~dB}$ hybrid splitter is given as $\pm 0.8 \mathrm{~dB}$ amplitude imbalance and $\pm 10^{\circ}$ phase imbalance [5]. But since these imbalances are inherent and cannot be improved unless the combiner
structure is changed, a high power combining efficiency can only be obtained by setting the combined phases and amplitudes as close as possible. But as seen in Figure 2.4, an 8 dB of maximum power difference which is a relatively high value only leads to a $6 \%$ loss in combining efficiency, while an $80^{\circ}$ of maximum phase variation reduces the combining efficiency by $15 \%$. This makes the phase imbalance a much more important issue than the power imbalance in terms of combining efficiency.

As mentioned above, the imbalance characteristics of the combining structures like splitters or couplers are also effective in determining the combining efficiency. In the calculations above, these effects were not taken into consideration and a perfect matching between the generators and the combining structure was assumed. Another way of defining the combining efficiency is to write the ratio of $\eta_{c}$ to $\eta_{\max }$, where $\eta_{\max }$ is the combining efficiency obtained when the added signals are completely equal in magnitude and are in-phase. This way, the effect of the combining structure losses is included in $\eta_{\max }$. Since $\eta_{c}$ has information about the phase and power mismatches, this ratio not only gives information about the combiner losses, but also about the phase and amplitude mismatches of the added signals. In order to obtain this ratio, a general expression for $\eta_{c}$ can be written in general form as [10]

$$
\begin{equation*}
P_{o}=\eta_{c} \sum_{k=1}^{N} P_{a v, k} \tag{2.12}
\end{equation*}
$$

where $P_{o}$ is again the power at the output of the combiner and $P_{a v, k}$ is the available power from each of the $k$ combined signals. In order to relate $\eta_{c}$ to $\eta_{\max }$, another expression for $P_{o}$ in terms of $\eta_{\max }$ is necessary. When the signals are not equal in amplitude and phase, they are added vectorially so the summation in Equation 2.12 can be written as [10, 14]

$$
\begin{equation*}
P_{o}=\eta_{\max } \frac{1}{N}\left[\left(\sum_{k=1}^{N} \sqrt{P_{a v, k}} \cos \theta_{k}\right)^{2}+\left(\sum_{k=1}^{N} \sqrt{P_{a v, k}} \sin \theta_{k}\right)^{2}\right] . \tag{2.13}
\end{equation*}
$$

The ratio of Equation 2.13 to Equation 2.12 gives $\eta_{c} / \eta_{\max }$ as below:

$$
\begin{equation*}
\frac{\eta_{c}}{\eta_{\max }}=\frac{\left[\left(\sum_{k=1}^{N} \sqrt{P_{a v, k}} \cos \theta_{k}\right)^{2}+\left(\sum_{k=1}^{N} \sqrt{P_{a v, k}} \sin \theta_{k}\right)^{2}\right]}{N \sum_{k=1}^{N} P_{a v, k}} \tag{2.14}
\end{equation*}
$$

It is worthwhile to consider the effects of some special cases of the phases and powers of the combined inputs on Equation 2.14. One of these special cases is the identical-phases, unequal-amplitudes case. If we assume that $m$ out of $N$ combined input signals have a reduced power level $r P_{a v}$ and the remaining $N-m$ signals have the same power level of $P_{a v}$, Equation 2.14 reduces to $[12,10]$

$$
\begin{equation*}
\frac{\eta_{c}}{\eta_{\max }}=\frac{\left[1-\frac{m}{N}(1-\sqrt{r})\right]^{2}}{1-\frac{m}{N}(1-r)} . \tag{2.15}
\end{equation*}
$$

Another special case is the identical-amplitudes, unequal-phases case. Here, $m$ out of $N$ signals are out of phase with respect to the remaining $N-m$ signals by an angle of $\phi$. In this case, Equation 2.14 is rewritten as $[12,10]$

$$
\begin{equation*}
\frac{\eta_{c}}{\eta_{\max }}=1-2\left(\frac{m}{N}\right)\left(1-\frac{m}{N}\right)(1-\cos \phi) . \tag{2.16}
\end{equation*}
$$

The last special case is the two-input case, which is also the configuration of the power combiner designed in this thesis. If one of the inputs has a power reduced by a factor of $r$ and a phase shifted by an angle of $\phi$ with respect to the other input, then Equation 2.14 reduces to [10, 13]

$$
\begin{equation*}
\frac{\eta_{c}}{\eta_{\max }}=\frac{1}{2}+\frac{\sqrt{r}}{r+1} \cos \phi . \tag{2.17}
\end{equation*}
$$

Equation 2.17 is useful in analyzing the experimental results obtained from the power combiner in this thesis, since the combiner is also in a binary 1-stage configuration.

## Chapter 3

## Design of Power Amplifiers

### 3.1 Project with Meteksan Savunma A.Ş.

The power amplifers were first designed as a part of a joint project with Meteksan Savunma A.Ş. based on the idea that they could be used in the ongoing projects of the company. The overall specifications set as the goals of the project were outlined as follows: Two different designs would be made, the first of which contained a fully distributed matching network, and the second of which contained a matching network with lumped elements. The amplifiers would have a frequency range of $2.8-3.2 \mathrm{GHz}$ and produce a saturated output power of about $10 \mathrm{~W}(40 \mathrm{dBm})$ out of a 8-12 V DC supply, benefiting a GaAs device as the active element. The amplifiers would have a gain of about 9-13 dB with a maximum of 2 dB peak-to-peak flatness in the given bandwidth. The desired input return loss, $\mathrm{S}_{11}$, was required to be below -10 dB . Both the lumped and the distributed designs would be fabricated on 20-mil-thick Rogers 4003 substrate.

TGA2923-SG from Triquint was chosen as the active element. It is a partially matched packaged amplifier with a center frequency of 3.5 GHz , providing a saturated output power of 10 W at that frequency [15]. Although the device
is rated as partially matched for 3.5 GHz , the center frequency of our design is 3 GHz ; therefore matching networks at the input and output along with DCbiasing networks for the gate and the drain are necessary. The device technology used in TGA2923-SG is Heterojunction Field Effect Transistor (HFET), or High Electron Mobility Transistor (HEMT) which is a technology that has been subject to attention in recent years due to its good high-frequency and high-power performance [1].

For the simulations, a new Touchstone file (.s2p format) was formed for TGA2923-SG based on the measurements taken with the actual device, rather than using the one provided by the company since the first design trials yielded inaccurate results. The new Touchstone file was created for the bias conditions of $\mathrm{V}_{\mathrm{D}}=8 \mathrm{~V}, \mathrm{~V}_{\mathrm{G}}=-1.4 \mathrm{~V}$ and $\mathrm{I}_{\mathrm{D}}=1200 \mathrm{~mA}$ and this file was used at all designs with TGA2923-SG.

### 3.1.1 Agilent ADS and Momentum

While making the designs, Agilent ADS (Advanced Design System) was benefited as a CAD tool. ADS has both a schematic simulator and an EM simulator called Momentum. The schematic simulator makes use of the ADS or SPICE models of the electrical components in the design while Momentum benefits the method of moments technique to solve Maxwell's electromagnetic equations. The microwave mode or full-wave mode of Momentum uses full-wave Green functions which are general frequency dependent Green functions that fully characterize the planar structures embedded in a multilayered dielectric substrate without making any simplification to the Maxwell equations [16].

Momentum also has an RF-mode or quasi-static mode that makes an approximation by assuming the Green functions frequency-independent in order to reduce the simulation time, but in all the simulations performed during the
preparation of this thesis, microwave mode of Momentum was utilized. The designs were made and optimized at the schematic simulator and were checked by Momentum, and recursive changes were made between schematic and EM simulators when necessary.

### 3.1.2 Distributed Design

Design of the amplifier with distributed components was based on a Touchstone file which gives the s-parameters of the device for different frequencies at a particular bias point. By looking at $\mathrm{S}_{11}$ and $\mathrm{S}_{22}$, without any matching networks, TGA2923-SG is observed to have an inductive reactance at both the input and the output throughout the 2.8-3.2 GHz bandwidth. This is shown in Figure 3.1.


Figure 3.1: Input and output impedances of TGA2923-SG between 2-4 GHz

In order to match the device to $50 \Omega$ which is the characteristic impedance of the input line and also of all the measurement tools that are used, it is clear that a negative reactance has to be introduced to the input. For the output, the impedance seen by the transistor should be $R_{\text {opt }}$, which is the optimum impedance that yields the maximum output power of a power amplifier. Hence, the output matching network should transform the $50 \Omega$ to $R_{\text {opt }}$. For the ideal
case, at the input, starting from the active device, matching can be achieved most easily first by a relatively large series capacitor and then a relatively small shunt capacitor. For a distributed matching network, these capacitances have to be created with transmission lines. On the other hand, it is also important to keep the bandwidth requirement in mind while doing the design. Therefore, the matching networks get relatively complex to achieve the high bandwidth. But ultimately, the main goal is to converge to $50 \Omega$ by a group of distributed elements that show capacitive characteristics.

Lumped elements can be realized by distributed components in a number of ways. One of them is to change the thickness of the microstrip line. In 20-mil thick Rogers 4003 substrate, $50 \Omega$ corresponds to a line thickness of about 46 mils in microstip configuration. Lines that are thicker and thinner correspond to lower and higher impedance lines respectively. A series high impedance transmission line of a specific value roughly corresponds to a series inductor while a series low impedance line corresponds to a shunt capacitor. Shunt transmission lines can also be used. A short shunt transmission line with an open-circuit termination means a shunt capacitor while a short shunt transmission line with a short-circuit termination implies a shunt inductor. In the distributed design matching network, only varying thicknesses and lengths of transmission lines were benefited.

In Figures 3.2-3.7, the final form of the distributed design is shown. These are screenshots from the ADS schematic window. In Figures 3.2 and 3.3, the input and output matching networks can be seen respectively. The networks are fully composed of microstrip transmission lines of different widths and lengths which are optimized for the best S-parameters. The widths of the transmission lines used in the distributed design are parametrized and their values can be seen in the list named 'VAR' in Figure 3.2. It can be deduced from Figure 3.1 that in the input matching, the most important component is the shunt capacitor
since it directly carries the input impedance of the device to the proximity of 50 $\Omega$. Thus, as shown in Figures 3.2, several low impedance lines were used at the input matching network.


Figure 3.2: Input matching network of the distributed design with TGA2923-SG


Figure 3.3: Output matching network of the distributed design with TGA2923SG

The path that the input matching network transmission lines form on the Smith chart at 3 GHz is shown in Figure 3.4. Starting from $0.194+j 0.5$ point which is the normalized input impedance of TGA2923-SG, the impedance of the network converges to the vicinity of $50 \Omega$. This is also shown at the right of the figure for the whole bandwidth. With this result, the input return loss can be expected to be satisfying the asked conditions.


Figure 3.4: a) Input matching network displayed in the Smith chart for 3 GHz ; b) The termination point of the input matching network for all frequencies within the bandwidth

For Class A operation, $R_{\text {opt }}$, the optimum impedance that allows the maximum output power is given by

$$
\begin{equation*}
R_{o p t}=\frac{\mathrm{V}_{\max }}{\mathrm{I}_{\max }}=\frac{\mathrm{V}_{\mathrm{DD}}}{\mathrm{I}_{\mathrm{RF}}} . \tag{3.1}
\end{equation*}
$$

The bias conditions of TGA2923-SG are $\mathrm{V}_{\mathrm{D}}=8 \mathrm{~V}$ and $\mathrm{I}_{\mathrm{D}}=1200 \mathrm{~mA}$. For a more realistic approach, the efffect of the knee voltage on the voltage swing should also be considered, resulting in $R_{\text {opt }}=7 \mathrm{~V} / 1.2 \mathrm{~A}=5.83 \Omega$. In Figure 3.5, it can be observed that the designed output matching network transforms $50 \Omega$ to an impedance whose real part is about $25 \Omega$. This value is higher than the $R_{\text {opt }}$ value of Class A operation. Although the designed matching network provides a good return loss, this variation from the optimum value means that the maximum power performance of near 40 dBm may not be achieved. Actually, the input and output matching networks function to shift the center frequency of the TGA2923-SG to 3 GHz . As mentioned before, the transistor is normally
matched to $50 \Omega$ with a bandwidth of 200 MHz at a center frequency which is about 3.5 GHz [15]. This also creates a partial matching effect at 3 GHz , which is the main reason why the distributed power amplifier design made in this thesis is able to work with an impedance presented to its output higher than $R_{\text {opt }}$, at high input levels, delivering a saturated power of about 38 dBm , as will be mentioned later on.


Figure 3.5: a) Output matching network displayed in the Smith chart for 3 GHz ; b) The impedance of the output matching network seen from the transistor side

The DC-bias networks for the input and output are shown in Figures 3.6 and 3.7 respectively. The bias networks also include distributed elements along with surface-mount by-pass capacitors of $1 \mu \mathrm{~F}, 120 \mathrm{nF}$ and 100 pF . The networks were designed to present an open-circuit to the matching networks at 3 GHz , thus not to disturb the RF characteristics. Shunt radial stubs were benefited to increase the bandwidth of the DC-bias network, observable in Figures 3.6 and 3.7. The radii and the angle of the shunt radial stubs were among the optimization parameters. The width of the drain bias line was chosen thicker than that of the gate bias line in order to have the lines withstand higher currents since the


Figure 3.6: Gate DC-bias network of the distributed design with TGA2923-SG
rated quiescent drain current is 1200 mA for TGA2923-SG. A resistor of $10 \Omega$ was included in the gate bias network to make the circuit stable at 3 GHz .

The S-parameter magnitude simulation results for the distributed design are shown in Figure 3.8. As already mentioned, the simulations were performed in both ADS Schematic Simulator and EM Simulator; and a comparison between these two results is provided in Figure 3.8.

It is observed that $\mathrm{S}_{11}$ is less than -10 dB in the $2.8-3.2 \mathrm{GHz}$ range in both simulations. The gain, $\mathrm{S}_{21}$ is around 10 dB . The differences between EM and schematic simulation results are due to different approaches to the same problem,


Figure 3.7: Drain DC-bias network of the distributed design with TGA2923-SG


Figure 3.8: S-parameters of the distributed design obtained via ADS Schematic and ADS Momentum (EM) simulations plotted together
but in terms of the reliability, EM simulation is preferable since it is the direct simulation of the physical layout rather than the model. The simulation results were satisfying in terms of attaining the goals set for the S-parameters, therefore the development process went on with the fabrication of the amplifier. The fabrication layout formed in Momentum and the fabricated amplifier with all the components soldered are shown in Figure 3.9 and 3.10 respectively. As visible in Figure 3.9, there are several vias in the ground plane pad on which the transistor is placed. Thin wires are used to short this pad to the bottom ground plane of the microstrip. The vias are also important in the process of transferring the heat from the transistor to the bottom ground and the heat sink.

### 3.1.3 Measurement Results for the Distributed Design

The S-parameters and input-output power, efficiency, gain and intermodulation characteristics of the distributed design with TGA2923-SG were measured by


Figure 3.9: Fabrication layout of the distributed PA design


Figure 3.10: The photograph of the fabricated distributed PA design
using the measurement tools in Meteksan Savunma. Measured S-parameters of the design with a comparison with the EM simulation results are shown in Figure 3.11.


Figure 3.11: S-Parameters of the distributed PA: Measured vs. simulated

As mentioned before, the S-parameter measurements were taken at the bias conditions of $\mathrm{V}_{\mathrm{D}}=8 \mathrm{~V}, \mathrm{~V}_{\mathrm{G}}=-1.4 \mathrm{~V}$ and $\mathrm{I}_{\mathrm{D}}=1200 \mathrm{~mA}$. $\mathrm{S}_{11}$ satisfies the requirements in most of the bandwidth except after 3.15 GHz where it drops down to about -5 dB ; but $\mathrm{S}_{22}$ seems to be the limiting factor though not worse than a rather acceptable level, which is better than -8 dB in the whole bandwidth. The gain, $\mathrm{S}_{21}$ varies between 8.8 dB to 9.9 dB in $2.8 \mathrm{GHz}-3.15 \mathrm{GHz}$ range. After 3.15 GHz , it drops to about 8.2 dB . This value for gain is in agreement with the rated gain values of TGA2923-SG, whose nominal gain is stated as 9 dB in the datasheet. Measured S-parameters of the amplifier show a degree of consistency with the simulations since the center frequency and the bandwidth goals are observed as attained despite the differences in the magnitudes of the S-parameters.

The diagram of the experimental setup used for the power measurements is given below in Figure 3.12 and the setup is shown in Figure 3.13.


Figure 3.12: Diagram of the experimental setup for power measurements

As can be seen in Figure 3.12, the input signal is produced by an RF signal generator. Since the power levels provided by the signal generator is generally rather low, in order to test the power amplifier at high power levels, it is necessary to amplify this input signal to above 30 dBm . Therefore a driver amplifier by Cree was benefited before the DUT. The driver amplifier consisted of a demonstration board for CMPA2560025F, a Cree high-power GaN HEMT. This driver amplifier could provide up to 44 dBm saturated power and 27 dB power gain at 3 GHz [17]. Thus it is more than enough for the measurements as a driver amplifier.

SMA plug DC block capacitors were placed both before and after the driver amplifier and the DUT for proper operation. SMA cables were used for making the connections. Two 20 dB atteunators from Aeroflex/Weinschel were connected after the DUT and the power levels were observed at the spectrum analyzer from Rohde\&Schwarz. Since the cables and DC blocks are not ideal, it is also important to find their loss in order to correctly calculate the saturated power of the DUT. For this reason, the whole system was tested bypassing the amplifiers and was found to create a loss of 41.9 dB including the attenuators, meaning a loss of 1.9 dB . Hence, all of the data that have resulted from the power measurements were added 41.9 dB .


Figure 3.13: Photograph of the experimental setup for power measurements

Heatsinks were used at both the driver amplifier and the DUT. Heating is an important issue for power transistors, degrading the performance seriously in a rapid way when caution is not taken. Since the back side of the TGA2923SG, which is also the source terminal, has to be grounded and in the microstip configuration only the lower conductor serves as ground (unlike some of the other transmission types like coplanar waveguide), many vias of 0.4 mm diameter were drilled on the top conductor where the transistor would be soldered, and thin conducting wires were used to short the source of the transistor to the ground. Same technique was also used to make the ground connections of the surface mount (SMT) parts. Then the amplifier was located on a heat sink after putting some thermal grease between the heatsink and the location where the transistor would be placed. Thermal grease is a frequently used fluidic substance with high thermal conductivity but also electrical nonconductivity that transfers the heat directly from the active device to the sink.

As mentioned, it is important that the active devices stay below a certain temperature limit for safe operation. TGA2923-SG datasheet gives the maximum
operating channel temperature and channel-to-backside of package thermal resistance as $200^{\circ} \mathrm{C}$ and $8^{\circ} \mathrm{C} / \mathrm{W}$ respectively under the bias conditions of $\mathrm{V}_{\mathrm{D}}=8 \mathrm{~V}$ and $\mathrm{I}_{\mathrm{D}}=1.20 \mathrm{~A}[15]$. For an ambient temperature of $25^{\circ} \mathrm{C}$ and total DC power consumption of about 10 W , the case-to-ambient thermal resistance is found as

$$
\begin{equation*}
\frac{(200-25)^{\circ} \mathrm{C}}{10 \mathrm{~W}}-8^{\circ} \mathrm{C} / \mathrm{W}=9.5^{\circ} \mathrm{C} / \mathrm{W} \tag{3.2}
\end{equation*}
$$

This is the maximum value of thermal resistance for the heat sink to be selected. It should be noted that in this analysis, the case-to-heatsink and heatsink-to-ambient transfer characteristics were not considered separately. This is because that the thermal resistance of the thermal grease which grants the heat transfer between the case and the heatsink is very small (about $0.03{ }^{\circ} \mathrm{C} / \mathrm{W}$ ) [18], and can be neglected. One of the most frequently used heatsinks for cooling of such a system is an aluminium flatback profile heatsink. One such example is Aavid Thermalloy 60630, which is a flatback with gap profile heatsink with dimensions of $99.1 \times 32.5 \mathrm{~mm}$. The rated thermal resistance for this model is $2.29^{\circ} \mathrm{C} / \mathrm{W}$ [19], which is a much lower value than the number calculated above. In the power measurements, a heatsink which is about twice the size of the given example was used. In order to be completely safe, fans were also benefited for cooling the driver amplifier and the DUT.

The change of output power with respect to the input power is plotted in Figure 3.14. Nonlinear effects start to be observed after an input power level of about 26 dBm , which corresponds to an output power level of 34.3 dBm . The 1- dB compression ( P 1 dB ) point is an important parameter for determining the nonlinear characteristics of a power amplifier. The ideal behavior of the amplifier which is characterized by a line is also plotted in Figure 3.14. By utilizing the input-output power curve and this line, input and output 1-dB compression points, which are named as $\mathrm{P} 1 \mathrm{~dB}_{\text {in }}$ and $\mathrm{P} 1 \mathrm{~dB}_{\text {out }}$ respectively can be determined. $\mathrm{P}_{1} \mathrm{~dB}_{\text {in }}$ and $\mathrm{P} 1 \mathrm{~dB}_{\text {out }}$ of the amplifier are found to be 28.9 dBm and 36.4 dBm respectively from Figure 3.14.


Figure 3.14: Output power vs. the input power in distributed PA design

The nonlinear characteristics of the amplifier is also visible in the power gain curve, which is plotted in Figure 3.15. Gain in the linear region seems to be around 8.6 dB , and starts to deteriorate after a point, dropping down to around 5 dB at 33 dBm of input power in a nonlinear fashion.

Another important parameter in power amplifier design is efficiency. Efficiency-linearity trade-off constitutes one of the main challenges in power amplifier design. Class A power amplifiers are the most linear but the least efficient class of PA's with a maximum $25 \%$ PAE since they conduct all the time. If an inductor or a transformer is used to couple the load from the amplifier, theoretical maximum efficiency can be increased up to $50 \%$ by making use of the back (counter) electromotive force of the inductor. Class B type power amplifiers are more efficient offering a maximum theoretical efficiency of $78.5 \%$ but less linear since they conduct only at half of the cycle. This means that Class B power amplifiers have a conduction angle of $180^{\circ}$, where conduction angle is the angle over one period for which the device remains conducting. Classes $\mathrm{C}, \mathrm{D}, \mathrm{E}$ and F


Figure 3.15: Power gain vs. the input power in distributed PA design
provide much increased efficiency (up to theoretical 100\%) but they are highly nonlinear. In order to achieve an amplifier with a good compromise between efficiency, power and gain, generally class AB is used. As their name implies, Class AB type amplifiers are a mixture of the Classes A and B , meaning that their quiescent points are set such that they conduct between a half and a full cycle, i.e., they have a conduction angle of between $180^{\circ}$ and $360^{\circ}$ degrees.

The distributed design was also based on Class AB configuration. In the literature, Class AB amplifiers have been shown to produce the same amount of fundamental RF output power (in fact a few tenths dB better) with Class A PA's with increased efficiency and relatively low harmonic content [20]. In the ideal case, throughout the Class AB range, the largest harmonic other than the fundamental is observed as the second. The third harmonic is less dominant while the effect of the fourth and the fifth harmonics are nearly negligible. The effect of the second harmonic is to reduce the dips of the fundamental sinewave and
sharpen the peaks. The main purpose of the reduction of the conduction angle is to increase efficiency, and effects of this sort are tolerable in case the fundamental power level does not decrease very much. It is understood from the proposed use of the active device TGA2923-SG that it has been optimized for Class AB operation. The quiescent drain current recommended in the datasheet is 1.20 A , while the device can withstand currents up to 4 A . It is clear that the device gives the best performance in the AB range. Therefore, the distributed design has been based on the recommended bias points of $\mathrm{V}_{\mathrm{D}}=8 \mathrm{~V}$ and $\mathrm{I}_{\mathrm{D}}=1200 \mathrm{~mA}$, which corresponds to a gate voltage of $\mathrm{V}_{\mathrm{G}}=-1.4 \mathrm{~V}$ for the particular device used. The value of the gate voltage that yields the given drain current level for the given drain voltage value varies from device to device. The suitable gate voltage values have been found to be ranging from -1.56 V to -0.93 V experimentally for several devices.

The power added efficiency versus the input power plot is shown in Figure 3.16. This curve was obtained by applying Formula 3.1 and taking $\mathrm{P}_{\mathrm{DC}}$ as $1.2 \mathrm{x} 8=9.6 \mathrm{~W}$ for all input drive levels. The maximum PAE level is found to be close to $45 \%$ for an input power of about 32 dBm . Small signal efficiency is low as expected. Because the quiescent point does not change with the variation of the RF input power, for small AC signals, efficiency is expected to be low. Then for increasing RF drive level, the efficiency is expected to exponentially increase and when the gain starts to drop, it is expected to decrease after reaching a maximum. The datasheet of TGA2923-SG also gives similar curves for efficiency and again a maximum level of about $45 \%$ for several application circuits from 3.5 GHz to $3.7 \mathrm{GHz}[15]$.

Stability is also another important concept for power amplifiers. When unstability starts to be observed, the amplifier starts to act as an oscillator. In order to check whether a 2-port network is stable, a commonly used test is called


Figure 3.16: Power-added efficiency vs. the input power in distributed PA design the $K-B_{1}$ test. $K$ and $B_{1}$ factors of a 2-port network are defined as [6];

$$
\begin{gather*}
\Delta=S_{11} S_{22}-S_{12} S_{21}  \tag{3.3}\\
K=\frac{1-\left|S_{11}\right|^{2}-\left|S_{22}\right|^{2}+|\Delta|^{2}}{2\left|S_{12} S_{21}\right|}  \tag{3.4}\\
B_{1}=1+\left|S_{11}\right|^{2}-\left|S_{22}\right|^{2}-|\Delta|^{2} \tag{3.5}
\end{gather*}
$$

With these definitions, a 2-port network is unconditionally stable if and only if the criteria below are satisfied:

$$
\begin{align*}
K & >1  \tag{3.6}\\
B_{1} & >0 \tag{3.7}
\end{align*}
$$

$K$ and $B_{1}$ factors extracted from the measured S-parameters of the distributed design are shown in Figures 3.17 and 3.18 respectively.

As can be seen in the plots, the conditions of 3.6 and 3.7 are satisfied for the distributed PA design. In the given bandwidth, the $K$-factor does not drop


Figure 3.17: $K$-factor stability of the distributed PA
below 1 while the $B_{1}$ factor also stays above 0 . This ensures the stability of the design. As mentioned before, a $10 \Omega$ resistor was placed in the gate bias network in order to get rid of possible oscillations. This was an experimentally determined value. The detractive effect of this resistor on the gain is observed not to be very significant since the gain values specified in the datasheet of TGA2923-SG were achieved.

The third order intermodulation products of the amplifier were also measured by another setup using two-tone measurement technique. Instead of one signal, two sinusoidal signals of the same power level ( -9 dBm ) but of slightly different frequencies ( 3 GHz and 2.998 GHz ) produced by two different RF signal generators were combined via a Wilkinson power combiner and were fed into the setup shown in Figure 3.12. Since the most dominant intermodulation products are $2 \mathrm{f}_{1}-\mathrm{f}_{2}$ and $2 \mathrm{f}_{2}-\mathrm{f}_{1}$, two signals at frequencies 2.996 GHz and 3.002 GHz are expected to be observed most closely to the fundamentals $f_{1}$ and $f_{2}$ at the spectrum


Figure 3.18: $B_{1}$-factor stability of the distributed PA
analyzer. The experimental results verify this expectation. Third order intermodulation products observed at the spectrum analyzer (whose power levels are added by 41.9 dB of loss) are given in Table 3.1 below.

| Frequency (GHz) | Power $(\mathrm{dBm})$ |
| :---: | :---: |
| 2.996 | -39.54 |
| 2.998 | 19.05 |
| 3.000 | 18.98 |
| 3.002 | -39.69 |

Table 3.1: Power Levels of Fundamentals and Intermodulation Products Observed at the Output

Third-order intercept point, which is shown as IIP3 for input and OIP3 for the output, is an important indicator of how well the undesired intermodulation products are suppressed and how linear the amplifier is. The intercept point due to second-order intermodulation products, OIP2, is not as much dominant because its level is above OIP3 and it and can be much easier to filter the second-order products since they are not as close as the third-order products to the fundamentals. By drawing a linear input-output power plot as the one in

Figure 3.14, and also another plot with a slope which is three times the slope of this line and intersecting these two lines at the IP3, one can calculate the OIP3. After simple analytical geometry calculations, following equation gives OIP3 [6]

$$
\begin{equation*}
O I P 3=P_{f_{1}}+\frac{\Delta_{P}}{2}(d B m) \tag{3.8}
\end{equation*}
$$

where $P_{f_{1}}$ is the fundamental power at the output and $\Delta_{P}$ is the difference between the fundamental power and the intermodulation product power in dB , $P_{2 f_{1}-f_{2}}$. By observing Table 3.1, we can take $P_{f_{1}}$ as 19 dBm and $P_{2 f_{1}-f_{2}}$ as -39.6 dBm . Thus, $\Delta_{P}=58.6 \mathrm{~dB}$. By applying 3.8, OIP3 is calculated as $19+58.6 / 2=48.3 \mathrm{dBm}$. Generally, OIP3 is found to be about 10 dB higher than the output $1-\mathrm{dB}$ compression point, $\mathrm{P} 1 \mathrm{~dB}_{\text {out }}$ for amplifiers. $\mathrm{P} 1 \mathrm{~dB}_{\text {out }}$ of the distributed design had already been calculated as 36.4 dBm , which implies about 12 dB of difference between two points.

### 3.1.4 Lumped Design

Another design was also developed based on the specifications set by the project with Meteksan Savunma which was a power amplifier containing lumped elements in the matching networks. The specifications were the same with the distributed design. As pointed out before, the matching network has to include a dominant shunt capacitor along with other elements. This time, in order to realize those elements, surface mount capacitors along with shunt stubs with short and open terminations were used instead of transmission lines with varying thicknesses. Using ideal lumped elements, the input matching network can be constructed as shown in Figure 3.19.

In a realistic design, the connections are made with transmission lines. Therefore, the lengths of the transmission lines should be optimized, too. In order to obtain a high bandwidth with a realistic matching network, along with the two series capacitors, a shunt short-circuited stub and several $50 \Omega$ lines were also


Figure 3.19: a) An ideal 2-element input matching network; b) The S-parameter performance of this network; c) The matching displayed on Smith Chart
benefited at the input and output. The ADS screenshots of the final form of the matching networks are shown in Figures 3.20 and 3.21.


Figure 3.20: Input matching network of the lumped-element design with TGA2923-SG

In Figure 3.22, the input matching network of the lumped design is displayed on the Smith chart. It can be observed that for the most of the bandwidth, the impedance seen at the input side of the matching network approaches $50 \Omega$.


Figure 3.21: Output matching network of the lumped-element design with TGA2923-SG


Figure 3.22: a) Input matching network displayed in the Smith chart for 3 GHz ; b) The termination point of the input matching network for all frequencies within the bandwidth

For the output matching network, the impedance seen from the transistor side should again be close to $R_{\text {opt }}$ for maximum output power. The designed network carries the $50 \Omega$ to an impedance whose real part is about $15 \Omega$, which is a value higher than $R_{\text {opt }}$. Again it can be expected that the deviation from $R_{\text {opt }}$ at the output may reduce the saturation power of the amplifier. On the other hand, the return loss and gain characteristics of the simulated design show
good characteristics. The output matching network elements displayed on Smith Chart are shown in Figure 3.23.


Figure 3.23: a) Output matching network displayed in the Smith chart for 3 GHz ; b) b) The impedance of the output matching network seen from the transistor side

Matching network designs using lumped elements are generally more compact than the distributed designs and are easier to optimize after fabrication. But it is more difficult to obtain an agreement between the simulation and experimental results. This is because the simulation models of the surface mount lumped elements do not exactly mimic the real behavior of the components. It is necessary to experimentally obtain the high frequency models of each lumped component that would be used in the design, but since a discrete optimization that changes the values of the components in a discrete way (unlike the one for the distributed case which is continuous) is needed, it is difficult to obtain models for a wide range of numerous surface mount components. The measured S-parameters of the amplifier are plotted along with the Momentum simulation results in Figure 3.24. This is in fact a post-fabrication optimized version of the lumped design. The original design was found to have worse S-parameters, and
the surface mount capacitors were replaced with different values which finally resulted in the S-parameter behavior shown in Figure 3.24. The final capacitor values from left to right are $20 \mathrm{pF}, 1 \mathrm{pF}, 2.2 \mathrm{pF}$ and 0.4 pF .


Figure 3.24: S-Parameters of the PA with lumped components: Measured vs. simulated

The s-parameters shown in Figure 3.24 are the best results among a set of different combinations of surface mount capacitor values. Nevertheless, this best combination still cannot satisfy the bandwidth requirement and $S_{11}$ and $S_{21}$ are found to be several dB's worse from the levels achieved by the distributed design. On the other hand, the design displays a good symmetrical behavior, with the s-parameters centered around 3 GHz . But $\mathrm{S}_{11}$ and $\mathrm{S}_{21}$ are only good at the center frequency, and this is the best result among a several number of trials. It can be deduced from these results that the difference between the ideal and non-ideal performance of a matching network employing lumped elements is far greater than that of a distributed matching network, which is closely related with the imperfect modeling of the components, as mentioned before.

### 3.1.5 A Design with NPT1004

As an extra part of the project, an amplifier capable of producing a high output power (which is about pulsed 30 W or higher) was also asked to be designed. In order to supply such a high power, a GaN transistor, NPT1004 from Nitronex was used. The frequency range was this time chosen as $3-3.5 \mathrm{GHz}$. The S-parameter requirements were still valid. The amplifiers would be designed with respect to 8 -mil Rogers 4003 substrate. A design was made based on these specifications, but the measurements revealed that the center frequency of the design was about 2.95 GHz. This frequency shift can again be attributed to the inaccuracy of the Touchstone files provided by the company. The design parameters and the layout obtained in ADS are given in Figures 3.25 and 3.26 respectively.


Figure 3.25: Input \& output matching and bias networks of the amplifier design with NPT1004

A fully distributed network was designed for matching. To ensure stability, $3.9 \Omega$ was placed in the input matching network. 100 pF surface-mount capacitors were placed at the input and output for DC blocking. This time for AC-DC separation, RF choke inductors were employed at the gate and drain bias networks. For the gate bias network, an inductor with model number of


Figure 3.26: Fabrication layout of the NPT1004

0603CS-15-NX-L was selected. This inductor is rated as having a 4 GHz selfresonance frequency. Its DC resistance at 3 GHz is rated as $0.170 \Omega$. For the drain bias network, an inductor that could stand high currents was necessary, and for that reason a conical inductor from Coilcraft with high current specifications was used. The simulations and the measured S-parameters for the device are shown in Figures 3.27 and 3.28 respectively. The bias conditions for the measurements were $\mathrm{V}_{\mathrm{D}}=28 \mathrm{~V}$ and $\mathrm{I}_{\mathrm{D}}=350 \mathrm{~mA}$.

As can be observed in Figure 3.27, both the schematic and Momentum simulations yield similar s-parameter results, which are satisfying for the whole bandwidth. But the measurement results show that the center frequency of the design has shifted to 2.95 GHz . Due to the lack of a GHz pulsed driver system at that time, the pulsed power measurements were skipped but a good pulsed power performance can be expected from the amplifier at that shifted frequency range. On the other hand, the amplifier was tested with very brief continuous RF drives at 3 GHz , and it was observed to perform decently up to about $43.05 \mathrm{dBm}(20.18$ W) of output power. Since the device is optimized for pulsed performance, the device was not tested with further drive levels. The measurement results are shown in Table 3.2.


Figure 3.27: Schematic and EM simulation results of the amplifier design with NPT1004


Figure 3.28: S-parameter measurement results for the amplifier design with NPT1004 for $V_{D}=28 \mathrm{~V}$ and $\mathrm{I}_{\mathrm{D}}=350 \mathrm{~mA}$

| $\mathrm{P}_{\text {IN }}(\mathrm{dBm})$ | $\mathrm{P}_{\text {OUT }}(\mathrm{dBm})$ |
| :---: | :---: |
| 7.8 | 15.6 |
| 17.8 | 25.6 |
| 22.8 | 30.5 |
| 27.8 | 35.4 |
| 32.6 | 40.3 |
| 36.0 | 43.05 |

Table 3.2: Output Power vs. Input Power for the design with NPT1004

### 3.2 Final Form of the Amplifiers

For the amplifiers that would be used in the power combiner, the distributed design with TGA2923-SG was chosen and two new power amplifiers with the same design were fabricated. This time the DC block capacitors were integrated with the circuit and two 100 pF capacitors were placed at the proper places within the input and output matching networks so that they could have minimum effect on the s-parameters. An extra amplifier was also fabricated in case one of the two available ones failed. These power amplifiers were named as 'I', 'II', and 'III' respectively. The photograph of these amplifiers placed on heatsinks is given in Figure 3.29, while the magnitudes and phases of the $\mathrm{S}_{21}$ 's of the amplifiers I and II are plotted in Figure 3.30.

Figure 3.30 shows that the phases experienced through PA I and PA II are not exactly the same, although these two amplifiers are basically the same design formed by the same elements. The main source of difference between the gains and the phases of these amplifiers can be assumed to be the the transistors. Although they are of the same model number, they are not the same. It had already been noted that the value of the gate voltage that yields the given drain current level for a given drain voltage value varies from device to device. For the bias conditions of $\mathrm{V}_{\mathrm{D}}=8 \mathrm{~V}$ and $\mathrm{I}_{\mathrm{D}}=1200 \mathrm{~mA}, \mathrm{~V}_{\mathrm{G}}$ corresponds to about -1.4 V and -1.0 V respectively for the PA I and PA II, which is also a proof of difference between the transistors. In Figure 3.30, it is visible that there is more than $40^{\circ}$


Figure 3.29: Final form of the amplifiers available for use in power combiner


Figure 3.30: a) Magnitudes and b) Phases of the $\mathrm{S}_{21}$ 's of PA I and PA II
of phase difference between the amplifiers. It shows that the phase shifters will indeed be important to compensate for the phase imbalance between the arms since these amplifiers would be used in a power combiner. The center frequency
of the new amplifiers also shows a shift, the best s-parameter characteristics are observed at about 3.07 GHz . Since this frequency is within the predetermined range of 2.8-3.2 GHz for many elements like Wilkinson power combiners or the couplers of the phase shifters which are used in the power combiner system, it is possible to test the power combiner at this frequency.

## Chapter 4

## Phase Shifters

### 4.1 Information on Phase Shifters

Phase shifters are blocks that can be used to change the phase characteristics of an input voltage or current by using a control signal. There are several applications where the phase shifters are frequently used. An important example is the phased-array antennas, where beam scanning is controlled by shifting the phase [6]. The change of phase in a phase shifter can either be continuous or in discrete steps. Both analog and digital phase shifters are available. Analog phase shifters make use of either passive microwave elements like transmission lines or active components like transistors. Digital phase shifters offer discrete phase steps with respect to the state of the phase bits which also determine the resolution of the shifter structure.

The working principles of analog phase shifters are diverse. An analog phase shifter can be transmission or reflection type. As the name implies, the output of a transmission type phase shifter is the signal that transmits through the 2port network, while the output of a reflection type phase shifter is the signal that reflects back from the 2-port. Each group may have various configurations.

Probably the most basic example of a transmission type phase shifter is the switched line configuration, shown in Figure 4.1. The idea behind the switched line phase shifters is to change the distance that the RF signal travels, and therefore the electrical length and the phase of the signal, since the electical length is given by $\beta l$ where $\beta=\frac{2 \pi}{\lambda}=\frac{\omega}{v_{p}}$. It can be done by forming several transmission line paths and then by switching between one of these paths by using a certain mechanism. This mechanism can be in the form of using two SPDT switches for selecting one of the two available transmission lines which are of different lengths. The resulting phase shift is thus given as $l_{1}-l_{2}$ where $l_{1}$ and $l_{2}$ are lengths of the two transmission lines. Unless a mechanism which enables the continuous changing of the length of the line (such as mechanically changing the length of the line) is used, the phase shift obtained by this method is fixed. On the other hand, there is no limit of the maximum phase shift generated via this method.


Figure 4.1: a) Switched-line and b) Loaded-line phase shifters

Another transmission type phase shifting method is the loaded-line structure, depicted in Figure 4.1. In this configuration, the transmission line is loaded by a shunt reactance (either a lumped element such as an inductor or a capacitor, or a shunt open or short stub) and the signal that transmits through experiences a phase shift depending on the reactance value of the shunt element. If a shunt element with a reactance of $j B$ is placed between two transmission lines of characteristic impedances $Z_{o}$ as seen in Figure 4.1, then the reflection and
transmission coefficients are given by

$$
\begin{align*}
\Gamma & =\frac{Z_{I N}-Z_{o}}{Z_{I N}+Z_{o}}=\frac{1-y_{i n}}{1+y_{i n}}  \tag{4.1}\\
\mathrm{~T} & =1+\Gamma \tag{4.2}
\end{align*}
$$

where $y_{i n}$ is the normalized input admittance of the phase shifter and given by $\left(Y_{o}+j B\right) / Y_{o}=1+j b$. Then, the reflection and transmission coefficients are found as

$$
\begin{align*}
\Gamma & =\frac{-j b}{2+j b}  \tag{4.3}\\
\mathrm{~T} & =\frac{2}{2+j b} . \tag{4.4}
\end{align*}
$$

Here, the phase shift generated is equal to the phase of T , which is equal to $-\tan ^{-1}(b / 2)$ and the insertion loss of the phase shifter is equal to $-10 \log _{10}|\mathrm{~T}|^{2}=$ $10 \log _{10}\left(1+\frac{b^{2}}{4}\right)$ in dB . Insertion loss is an important parameter that can be defined as the attenuation ratio in a 2-port device. Although they can be used as a variable continuous phase shifter by employing an element like a variable capacitor, loaded-line phase shifters have important drawbacks. One of these drawbacks is that the maximum phase shift obtained from these structures is limited to $45^{\circ}$. Also, in order to get a higher phase shift, one has to increase $b$; which in turn results in an increase in the insertion loss [6]. A method that can be used to overcome these drawbacks is to use two identical shunt elements with a quarter wave transformer in between instead of only one shunt element. This leads to better return loss characteristics by having the two reflected waves cancel out by making them $180^{\circ}$ out of phase.

The other phase shifter category is the reflection type phase shifters. Here, the load that is placed at the end of the shifter is made switchable or continuously variable so the reflection coefficient is modified in phase. Again there are several implementation methods for reflection type phase shifters. One of them is to change the length of the transmission line at the output by a switch. Another one is to put a variable reactance at the output and change it by a control signal.

The latter method was benefited for the phase shifter used in our power combiner. A 3-dB quadrature hybrid coupler (a branch line coupler) was used at the input of the phase shifter, and the 2nd and 3rd ports, which are the through and coupled ports, were terminated with varactors that can offer changeable capacitance with changing DC bias. Since all arms of the branch line coupler have a length of $\lambda / 4$, the input signal fed from Port 1 splits into two $90^{\circ}$ out of phase but equal amplitude signals to Port 2 and Port 3. These two signals reflect back from the terminations with a phase that is altered depending on the value of the capacitance of the varactor. Since the same DC bias is used for the identical varactors, it can be assumed that the additional phases that are presented to these two signals are the same. Afterwards, as described in Chapter 2 , the reflected signals combine destructively at the input port because now they have $180^{\circ}$ of phase difference due to the round trip, and they add up in Port 4 which is the output port since they are in-phase. The varactors used here should be able to completely reflect the signals back without dissipating any power. In order to achieve this, the varactors must have a reasonably high Q and thus, low loss. The schematic of this phase shifter is given in Figure 4.2


Figure 4.2: Reflection type phase shifter with hybrid coupler and varactors

### 4.2 The Phase Shifter with Varactors

As mentioned above, in order to be able to equal the phases of the signals at each arm of the power combiner, a reflection type phase shifter employing varactors
at the output of a hybrid coupler was used in our work. In literature, this phase shifting method has been shown to work well at different frequency bands with high bandwidths [21, 22]. In this work, we have benefited two phase shifters at the two branches of the power combiner. Here, the bandwidth is not critical so a branch line coupler topology operating at the center frequency of 3 GHz was preferred as a coupler. The coupler was designed by using Agilent ADS and again tested with Momentum. The measured S-parameters of the branch line coupler are given in Figure 4.3.


Figure 4.3: Measured s-parameters of the branch line coupler used in the phase shifter

The $S_{21}$ and $S_{31}$ should be the same for the center frequency since they stand for the amount of signal transmitting through the ports 2 and 3 respectively. Here, at 3 GHz , they are both close to -3 dB showing that the input signal is divided into two equal parts at ports 2 and 3 . The 4th port is the isolated port, therefore ideally no signal is expected to go there. This is visible in Figure 4.3 since $\mathrm{S}_{41}$ is below -10 dB at the center frequency. The return losses are good and
they are below -10 dB for the whole band of 1 GHz and are below -20 dB at the center frequency.

The varactors were chosen as MA46483 from MA-COM. These GaAs varactors are able to offer high Q, which is critical in completely reflecting the incident signals and thus decreasing the insertion loss of the phase shifter. The junction capacitance of MA46483 changes between 1.3 pF and 12 pF for reverse tuning voltages of 20 V and 2 V respectively. Since it is also important that the same amount of phase should be added to the signals at ports 2 and 3 by the varactors, the reverse voltage-capacitance characteristics of the two varactors used at a coupler should ideally be the same. In reality they should be as close as possible to each other. For each MA46483 purchased, the measured junction capacitance values versus a set of voltage levels are given. For example, for one phase shifter, the two varactors used had the following capacitance values: The first varactor is measured to have a $C_{j}$ of $11.817 \mathrm{pF}, 6.743 \mathrm{pF}$ and 1.386 pF and the second varactor is measured to have a $C_{j}$ of $11.847 \mathrm{pF}, 6.750 \mathrm{pF}$ and 1.379 pF for voltage levels of $2 \mathrm{~V}, 4 \mathrm{~V}$ and 20 V respectively. These values are close enough for the varactors to be used in the output of the same coupler. The Q's are given as greater than 1500 for both varactors. As given in Figure 4.2, DC block capacitors and DC bias networks are necessary in order to separate the DC and RF signal paths. Instead of using quarter-wave transformers, again the DC bias networks which are used to present an open circuit for RF were optimized with Agilent ADS for a better bandwidth as was done for the power amplifier design. The photograph of the fabricated phase shifters along with the measured s-parameters at a reverse voltage of 10 V are given in Figure 4.4.

As emphasized before, the insertion loss of a phase shifter is an important parameter that shows how much signal is lost from the input to the output port. From Figure 4.4, it is clear that the insertion loss is less than 1 dB . When compared to the commercially available phase shifters and other phase shifters


Figure 4.4: a) The photograph of the phase shifters, b) S-parameters of one of the phase shifters
in the literature, it can be concluded that this value is quite satisfactory. For example, the insertion loss of HMC928LP5E, a $2-4 \mathrm{GHz}$ analog phase shifter from Hittite Microwave Corporation, is given as 3.5 dB at the center frequency while the insertion loss of P8P-48N-5, a digitally controlled 2-6 GHz phase shifter from GT Microwave Inc., is given as 11 dB at maximum. The return losses are also low, $\mathrm{S}_{11}$ and $\mathrm{S}_{22}$ are below -10 dB in the bandwidth of 400 MHz .

The phase shift generated by a varactor-based reflection type phase shifter can be calculated by using the relationship between the capacitance and electrical length, i.e., the phase. The input impedance of an open-circuited lossless transmission line is given as [23]

$$
\begin{equation*}
\mathrm{Z}_{\mathrm{i}}=-\frac{\mathrm{j} \mathrm{Z}_{0}}{\tan \beta \mathrm{l}} \tag{4.5}
\end{equation*}
$$

This is the reactance of a capacitance of $\tan \beta 1 /\left(\omega \mathrm{Z}_{0}\right)$ farads. From this formula, one can find out how many degrees of phase a capacitance value corresponds to. If we replace $\beta l$ with $\theta$, then the phase corresponding to a capacitance
value can be calculated as

$$
\begin{equation*}
\theta=2 \tan ^{-1}\left(\omega \mathrm{CZ}_{0}\right) \tag{4.6}
\end{equation*}
$$

where C is the capacitance. The factor 2 comes because the signal travels the same distance twice. At another capacitance value, a different phase value will be obtained. Therefore, the phase shift generated by this phase shifter is the difference between these phase values corresponding to different capacitances. By this method, a theoretical assumption of the phase shift that our phase shifter can produce can be calculated by placing the values of 1.386 pF and 11.817 pF for minimum and maximum capacitances. At 3 GHz , the theoretical maximum phase shift $\Delta \theta$ is thus found as $170^{\circ}-105^{\circ}=65^{\circ}$. The actual measured phase characteristics of the two phase shifters versus the reverse voltage are plotted in Figure 4.5. Since the normally isolated 4th port acts as the output port in reflection type phase shifters, the phase shown in Figure 4.5 is denoted as the phase of $\mathrm{S}_{41}$.


Figure 4.5: Measured phase versus reverse voltage for the phase shifters

As seen in the plot, the maximum phase shifts obtained by the phase shifters 1 and 2 are equal to $5.50^{\circ}-(-43.4)^{\circ}=48.9^{\circ}$ and $-3.10^{\circ}-(-53.0)^{\circ}=49.9^{\circ}$ respectively. These results are close to the theoretically predicted value of $65^{\circ}$. An offset of about $10^{\circ}$ is observed between the phase shifters, which is related with the differences in varactor capacitances. As mentioned before, these phase shifters are placed at each branch of the power combiner. This means that a variable phase shift of about $5.50^{\circ}-(-53.0)^{\circ}=58.5^{\circ}$ and $-3.10^{\circ}-(-43.4)^{\circ}=40.3^{\circ}$ can be achieved for the 1st and 2nd arms of the power combiner respectively. Therefore, the phase shifters are able to maintain a phase balance when an imbalance within this range is in question. As plotted in Figure 3.30, the difference between the phases of the two fabricated power amplifiers is close to $50^{\circ}$, which is a value that can be overcome by this system.

### 4.3 An Alternative Phase Shifter Design

During the studies of this thesis, an alternative microwave phase shifter has been designed and the results were published in a letter at Microwave and Optical Technology Letters [24]. A reflection-type shifter in nature, the structure makes use of the flow of a conducting fluidic substance (in this case, mercury) in order to change the length of the transmission lines placed at the end of a coupler. The through and coupled ports of a wideband quadrature hybrid coupler are connected to two transmission lines in coplanar waveguide configuration, which are terminated in open circuit at first. On top of these two separate transmission lines, microfluidic channels are formed as two slots in a layer of polydimethylsiloxane (PDMS). The same level of mercury is injected into the two containers (in the form of two circular cavities in PDMS layer), and the position of the mercury is changed by varying the pressure exerted on the containers by two micropositioners. This way, these two channels can be short-circuited at any desired point, and every position of mercury corresponds to a specific degree of
phase shift. The phase shift obtained by this microfluidic phase shifter is nearly continuous and can be changed between 0 to $360^{\circ}$ in a bandwidth of $2-6 \mathrm{GHz}$. The phase shift characteristics obtained at 3 different frequencies are plotted versus the distance traveled by mercury in Figure 4.6. The main drawback of such a system is the difficulty of its fabrication and setup. Also a high level of loss was observed, but much of this can be attributed to the imperfect characteristics of the wideband coupler that was built. Due to the level of insertion loss and the difficulty of operation of this phase shifter, it has not been employed in the power combiner system. The fabrication process and more details on the design and the experimental results can be found in [24].


Figure 4.6: Measured phase shift versus the distance traveled by mercury

## Chapter 5

## Measurements on the Power

## Combiner

### 5.1 Integration of the System Setup

The final step in the power combiner design was to put together all the components and measure the effect of phase changes at the output power. The overall power combiner testing setup diagram is given in Figure 5.1.


Figure 5.1: The overall power combiner test diagram

In order to obtain a sinusoidal RF signal, a voltage controlled oscillator was benefited. ZX95-3100+, a linearly tuned, low phase-noise voltage controlled oscillator from Mini Circuits was chosen. The frequency range provided is $2300-$ 3100 MHz and the DC voltage value corresponding to 3.07 GHz is about 8.9 V, with a power level of 8.8 dBm . This power level was increased by using an RF driver amplifier, HP 8347A, which offered a leveled output power as high as 22 dBm . As mentioned before, in order to separate the input into two equal parts, a Wilkinson power divider was used. The same design was also employed as a combiner at the output. In order to design the Wilkinson power divider, again Agilent ADS and Momentum were utilized. The photograph and measured s-parameters of the fabricated Wilkinson power divider is shown in Figure 5.2.


Figure 5.2: a) The photograph of Wilkinson power dividers, b) S-parameters of Wilkinson power divider \#1

It can be observed that the Wilkinson divider operates at a wide frequency range, offering an $S_{21}$ and $S_{31}$ which is around -3 dB throughout the whole bandwidth. This means that the input signal is divided into two equal parts and is sent through the ports 2 and 3 without much loss or imbalance of signal divison. The return losses are also good, below -10 dB for nearly the whole
bandwidth. After the signal is splitted into two arms, it is fed through the phase shifters and the power amplifiers at each arm. The power amplifiers are PA I and II explained in Chapter 3 and the phase shifters are the reflection type shifters using couplers terminated with varactors, as described in Chapter 4. The DC control voltages which are in the $2-20 \mathrm{~V}$ range are used to set the phase shift level of each arm. As stated before, with this system, it is possible to obtain about $\pm 50^{\circ}$ phase shift.

The two amplified signals are then combined with a Wilkinson power combiner. They are then sent to a power detector after passing through a 40 dB attenuator. The power detector is ZX47-40+ from Mini Circuits, a device that can detect a $10-8000 \mathrm{MHz}$ signal power level in the power range of -40 dBm to 20 dBm . The detected power levels are converted to DC voltage values between the terminals of a $1000 \Omega$ resistor connected as a load to the output of ZX47-40+ and can easily be read with a multimeter. Although not as perfectly precise and reliable as a spectrum analyzer, this power detector is much more practical to use integrated in a system and is able to detect a wide range of power with quite good accuracy. Of course, the detected power should be as harmonic-free as possible; but, since the VCO has a very good harmonic performance (about -20 dBc ), the only possibly serious harmonic level is produced at the power amplifiers in the system. But since the power amplifiers are operated in the linear region (leveled output power from the driver amplifier was set as 20 dBm at maximum), and $\mathrm{P} 1 \mathrm{~dB}_{\text {in }}$ of the power amplifiers are about 29 dBm , a serious harmonic generation should not be expected. Although the main function of a power combiner is to provide a power level that each amplifier alone cannot offer, here the experiments are made at a reduced power level. But the results obtained by these experiments are also valid for the PA's that are operated at their saturated output power levels.

The experiment setup photograph is shown in Figure 5.3. Male-to-male and male-to-female SMA cables from Emerson along with male-to-male adapters were used for making the connections between the components. Several different voltages are necessary for DC feed of power amplifiers, phase shifter control, VCO tuning, power detector and fans that are used for cooling the amplifiers.


Figure 5.3: The photograph of the overall system setup

### 5.2 Measurement Results and Discussions

The power combiner system with a phase shifter was implemented as shown in Figure 5.1. On this system, the effect of changing the phase of each arm of the power combiner on the output power and combining efficiency can be observed. The output power was measured for several phase combinations of the two phase shifters, which are determined by DC voltages of values between 2 and 20 V . For each combination, the phase difference between the arms and the corresponding combining efficiency is calculated and plotted in Figures 5.4 and 5.5 for the respective driving power levels of 4 dBm and 20 dBm obtained from HP 8347A. It should be noted that the output power values in the figures are obtained when the measured total loss due to the cables is added to the output power.


Figure 5.4: Change of the output power and combining efficiency versus the phase for 4 dBm drive level


Figure 5.5: Change of the output power and combining efficiency versus the phase for 20 dBm drive level

In the plots, the phase axis varies from $-40^{\circ}$ to $60^{\circ}$. The adoption here is as the following: Positive phases mean that the first arm is leading in phase and negative phases mean that the second arm is leading in phase. For example, for the obtained phases of $-43^{\circ}$ and $-33^{\circ}$ from the phase shifters, the phase of the overall combiner is denoted as $-10^{\circ}$. These plots verify that the output power and the efficiency of a power combiner indeed depend very much on the variations in phase of each branch. A 3 and 4 dB variation in the output power is visible in Figures 5.4 and 5.5 with changing the phase. It is clear that the maximum output power and efficiency are obtained when the system has a phase of $60^{\circ}$, i.e. when the first phase shifter is set such that it gives an additional $60^{\circ}$ of phase to the first branch of the power combiner. This can be predicted from the previously obtained Figure 3.30. In that plot, it is clear that phase of PA II is about $45^{\circ}$ ahead of PA I. Therefore, by setting the phase shifter before PA I to give an additional amount close to this value, the phase balance between the arms is achieved, leading to an increased output power and combining efficiency.

It is seen in Figures 5.4 and 5.5 that the maximum combining efficiency is $73 \%$ for an input power of 4 dBm and $76 \%$ for an input power of 20 dBm . The results are about the same as expected since the output power in this situation is about 7.5 dB above the drive levels for both 4 dBm and 20 dBm inputs from HP 8347A. This implies the gains of the power combiner are approximately equal for both power levels since the measurements were made at the linear region as emphasized before. These plots can also be compared to that in Figure 2.4. Although the graph in Figure 2.4 is plotted for a combiner with $N=10000$ amplifiers and although it shows the effects of phase and gain variation on the combining efficiency separately, the general form of the curve is quite similar to those in Figures 5.4 and 5.5. The rate of change of efficiency starts to slow with gradually decreasing phase variation between the added signals in both figures. If the additional phase for the first branch of the combiner was increased even more, then the efficiency and the output power would naturally start to drop
again. It can be deduced that the maximum levels reached at these plots are the maximum values for the efficiency and output power. Certainly, the difference between the power levels of the added signals is also one of the factors that plays an important role in diminishing the combining efficiency in our power combiner. It is clear from Figure 3.30 that the gains of the two amplifiers are not exactly the same at 3.07 GHz . A difference of more than 1 dB was also measured in the power levels at the outputs of PA I and PA II for both the 4 dBm and 20 dBm drive levels. This fact has also contributed to a lower combining efficiency.

It has been stated in Chapter 2 that $\eta_{c} / \eta_{\max }$ formula gives important insight about the effect of phase and power mismatches. For a binary power combiner case, this formula is given in Equation 2.17. As mentioned before, without the phase shifters, the phase difference between the two power amplifiers is about $45^{\circ}$ while the difference between their gains, hence their output powers is about $1 \mathrm{~dB} .-1 \mathrm{~dB}$ corresponds to 0.794 in linear scale. Therefore, by putting 0.794 for $r$ and $45^{\circ}$ for $\phi$, we obtain

$$
\begin{equation*}
\frac{\eta_{c}}{\eta_{\max }}=\frac{1}{2}+\frac{\sqrt{0.794}}{1+0.794} \cos 45^{\circ}=0.85 . \tag{5.1}
\end{equation*}
$$

If we neglect the combining structure losses and impedance mismatches and take $\eta_{\max }$ as 1 , then $\eta_{c}$ is found as $85 \%$. This means a $15 \%$ decline in $\eta_{c}$ from the maximum. If we inspect Figures 5.4 and 5.5, it is seen that the difference between the $\eta_{c}$ when the offset phases are not provided by the phase shifters (when the system phase is equal to 0 ) and the maximum $\eta_{c}$ is also close to this value. It is equal to $73 \%-56 \%=17 \%$ in Figure 5.4 and $76 \%-58 \%=18 \%$ in Figure 5.5. As mentioned before, the maximum value of the efficiency is determined by $\eta_{\text {max }}$.

As mentioned previously, the measurements were taken at 4 dBm and 20 dBm input levels. These points are within the linear region of the power amplifiers. The phases of the amplifiers may deviate even further if the drive level approaches
the saturation point, especially because the transistors are not identical. In such a case, the phase and power combining efficiency may not have a quasi-linear fashion as in the curves of Figures 5.4 and combeff2. Even still, the phase shifters are able to establish the phase balance between the arms by looking at the effect of the phases on output power.

To sum up, controlling the phases in the fabricated binary power combiner enables the combining efficiency to be increased about $15 \%$, and the output power is increased by more than 1 dB . The power amplifiers are normally expected to have identical phase and gain characteristics since they are fabricated from the same design by using the same transistor, but as shown, in practice they do not. In real life applications, power combiners generally have higher number of stages. Thus, if the phases are not correctly set at each binary branch and at each stage, the combining losses can reach to significant levels.

## Chapter 6

## Conclusions

In this study, an S-band corporate binary power combiner comprising two power amplifiers was designed and fabricated. In order to maintain a phase balance between the two arms, two phase shifters were placed before the amplifiers. Since the amplifiers used may have different phase characteristics in a power combiner, phase shifters are necessary for a lower combining loss.

The power amplifiers were designed in a project with Meteksan Savunma. CAD tools ADS and Momentum from Agilent were utilized while making the designs. Both the frequency domain and time domain measurements of the amplifiers were made and the distributed design was found to produce a saturated output power of 38 dBm along with a PAE up to more than $40 \%$ at saturated output power levels and a power gain close to 9 dB at linear power levels. Other designs were also created with lumped elements, but the distributed design was found to be superior in terms of bandwidth and s-parameters and it was chosen to be used in the power combiner.

The phase shifters were designed based on reflection type phase shifting method. For this purpose, a branch line coupler was used to have an input and output signal. Two varactors were placed at the through and coupled ports
and they reflected back the incident signal with a phase changing with the reverse DC bias applied on them. In order to have a very small insertion loss, it was essential that the varactors could reflect back all of the signal without dissipating any power. For this purpose, two high-Q varactors whose voltage-capacitance characteristics were very similar were chosen for each phase shifter. The fabricated phase shifters were found to be able to create a phase that could vary in a range of $50^{\circ}$. This value for each phase shifter is sufficient to compensate for the phase imbalance created by the power amplifiers.

Finally, the power combiner system was formed by integrating all of the separate components. Two Wilkinson couplers were fabricated to divide and combine the signals at the input and output. The change of the output power and combining efficiency were examined with changing the phases of each branch of power combiner. In the $60^{\circ}+40^{\circ}=100^{\circ}$ phase shifting range, it was observed that $\eta_{c}$ and the output power were indeed affected negatively by the phase difference at each arm. A maximum $\eta_{c}$ of $76 \%$ was obtained for 20 dBm of input power to the combiner. This value was found as $58 \%$ in case the phases were not controlled. The power loss and hence the reduction in the combining efficiency would be even more alarming at higher stage power combiners.

Although this power combiner has been designed and fabricated comprising of several discrete elements, all of these elements can be integrated into one single structure, which may make the system more compact and convenient. The system can also be operated at the saturated output power or at a higher frequency. The combining scheme can also be changed into e.g. a spatial configuration. But the phase and gain dependency of the combiner will not change and will bear the characteristics shown by the system in this thesis. As mentioned in Chapter 2, corporate power combiners are easier to design and they have a higher combining efficiency for relatively small number of combined amplifiers. Hence, they stand as an almost inevitable solution at microwave power systems.

A future enhancement in such a combiner system may be to automatically control the additional phases produced by the phase shifter. This can be achieved by processing the DC voltages produced by the power combiner and selecting the phase levels for both phase shifters where the maximum power is observed. The settling time of the whole system which is strongly dependent on the heating of power amplifiers and the power detector should also be taken into account for a better result. By automating the power combiner, it will be possible to obtain the highest combining efficiency without controlling the phase shifters manually. This automation process is especially important for higher stage power combiners, where it would be much more difficult to manually control a high number of phase shifting structures.

## APPENDIX A

## Derivation of Equation 2.8 from

## Equation 2.7

If we write the generator voltages at each branch seperately we get;

$$
\begin{aligned}
V_{1} e^{j \theta_{1}}= & Z_{o} i_{1}+\frac{Z_{o}}{N}\left(i_{1}+\ldots+i_{N}\right) \\
& \vdots \\
V_{N} e^{j \theta_{N}}= & Z_{o} i_{N}+\frac{Z_{o}}{N}\left(i_{1}+\ldots+i_{N}\right)
\end{aligned}
$$

When these terms are summed at both sides, we get:

$$
\sum_{k=1}^{N} V_{k} e^{j \theta_{k}}=Z_{o} \sum_{k=1}^{N} i_{k}+\frac{Z_{o}}{N} N \sum_{k=1}^{N} i_{k}
$$

Then,

$$
i_{1}+\ldots+i_{N}=\frac{\sum_{k=1}^{N} V_{k} e^{j \theta_{k}}}{2 Z_{o}}
$$

Therefore, $P_{o}$ of Equation 2.7 can be rewritten as

$$
P_{o}=\left|i_{1}+\ldots+i_{N}\right|^{2} \frac{Z_{o}}{N}=\frac{1}{4 N Z_{o}}\left|\sum_{k=1}^{N} V_{k} e^{j \theta_{k}}\right|^{2}
$$

which is Equation 2.8.

## Bibliography

[1] Y.-F. Wu, " $30-\mathrm{w} / \mathrm{mm}$ gan hemts by field plate optimization," IEEE ELECTR DEVICE L, vol. 25, no. 3, pp. 117-119, 2004.
[2] K. Chu, P. Chao, M. Pizzella, R. Actis, D. Meharry, K. Nichols, R. Vaudo, X. Xu, J. Flynn, J. Dion, and G. Brandes, " $9.4-\mathrm{w} / \mathrm{mm}$ power density algangan hemts on free-standing gan substrates," IEEE ELECTR DEVICE L, vol. 25, no. 9, pp. 596-598, 2004.
[3] R. Gilmore and L. Besser, Practical RF Circuit Design for Modern Wireless Systems, Volume II. Norwood, MA, USA: Artech House, 2003.
[4] N. Cheng, A.Alexanian, M.G.Case, D.B.Rensch, and R. York, "40-w cw broad-band spatial power combiner using dense finline arrays," IEEE T MICROW THEORY, vol. 47, no. 7, pp. 1070-1076, 1999.
[5] D. Bockelman and W. Eisenstadt, "Combined differential and commonmode analysis of power splitter and combiners," IEEE T MICROW THEORY, vol. 47, no. 7, pp. 1077-1082, 1999.
[6] M. M. Radmanesh, Radio Frequency and Microwave Electronics. Upper Saddle River, NJ 07458, USA: Prentice Hall, 2001.
[7] N. Cheng, P. Jia, D. Rensch, and R. York, "A 120-w x-band spatially combined solid-state amplifier," IEEE T MICROW THEORY, vol. 47, no. 12, pp. 2557-2561, 1999.
[8] J. Jeong, Y. Kwon, S. Lee, C. Cheon, and E. Sovero, "1.6- and 3.3-w poweramplifier modules at 24 ghz using waveguide-based power-combining structures," IEEE T MICROW THEORY, vol. 48, no. 12, pp. 2700-2708, 2000.
[9] Y. Tokumitsu and T. Saito and N. Okubo and Y. Kaneko, "A 6-GHz 80-W GaAs FET Amplifier with a TM-Mode Cavity Power Combiner," IEEE T MICROW THEORY, vol. 32, no. 3, pp. 301-308, 1984.
[10] M. Gupta, "Degradation of power combining efficiency due to variability among signal sources," IEEE T MICROW THEORY, vol. 40, no. 5, pp. 1031-1034, 1992.
[11] R. York, "Some considerations for optimal efficiency and low noise in large power combiners," IEEE T MICROW THEORY, vol. 49, no. 8, pp. 14771482, 2001.
[12] R. Ernst, R. Camisa, and A. Presser, "Graceful degradation properties of matched n-port power amplifier combiners," in IEEE MTT-S Int. Microwave Symp. Dig., June 1977.
[13] J. Nevarez and G. Herskowitz, "Output power and loss analysis of $2^{n}$ injection-locked oscillators combined through an ideal and symmetric hybrid combiner," IEEE T MICROW THEORY, vol. 17, no. 1, pp. 2-10, 1969.
[14] K. Lee, "A 25 kw solid state transmitter for l-band radars," in IEEE MTT-S Int. Microwave Symp. Dig., May 1979.
[15] TGA2923-SG Datasheet. 2009. URL: http://www.triquint. com/prodserv/more_info/download.aspx?file=/docs/t/TGA2923/ TGA2923-SG.pdf.
[16] Theory of Operation for Momentum. 2008. URL: http://cp. literature.agilent.com/litweb/pdf/ads2008/mom/ads2008/Theory_ of_Operation_for_Momentum.html.
[17] CMPA2560025F Datasheet. 2011. URL: http://www.cree.com/products/ pdf/CMPA2560025F.pdf.
[18] Scythe Thermal Grease Datasheet. 2011. URL: http://www.scythe-eu. com/en/products/pc-accessory/thermal-grease.html.
[19] Aavid Thermalloy Heatsink 60630 Datasheet. 2011. URL: http://www.aavidthermalloy.com/cgi-bin/exdisp.pl?Pnum= 60630\&LengthUnits=in\&ExLength=3\&airflow=57.2.
[20] S. C. Cripps, RF Power Amplifiers for Wireless Communications. Norwood, MA, USA: Artech House, 2006.
[21] T. Morawski, J. Zborowska, and P. Miazga, "Multi-octave phase modulators," in IEEE MTT-S Int. Microwave Symp. Dig., 1984.
[22] D.M. Krafcsik and S.A. Imhoff and D.E. Dawson and A.L. Conti, "A DualVaractor Analog Phase Shifter Operating at 6 to 18 GHz ," IEEE T MICROW THEORY, vol. 36, no. 12, pp. 1938-1941, 1988.
[23] D. K. Cheng, Field and Wave Electromagnetics. Boston, MA, USA: Addison Wesley, 1989.
[24] B. Ozbey, S. Ozturk, and O. Aktas, "Design of a high-resolution microfluidic microwave mems phase shifter," MICROW OPT TECHN LET, vol. 53, no. 8, pp. 1902-1905, 2011.

