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The compressibility of high purity YbB₂

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Abstract

The compressibility and phase stability of YbB₂ are investigated under high pressure using high-resolution synchrotron x-ray diffraction in a diamond anvil cell. The bulk modulus of high purity YbB₂ is obtained as ~ 182 GPa using the Birch–Murnaghan equation of state. The patterns measured up to 20 GPa and the pressure dependence of normalized lattice parameters, a/a_0 and c/c_0 , reveal that the compressibility of YbB₂ is low and fairly isotropic, and this material can be classified as a hard material. X-ray photoemission studies demonstrate that Yb in YbB₂ has a mostly trivalent valence state at room temperature. Moreover, sample preparation details provide a new insight into the high purity synthesis of YbB₂ at ambient pressure and moderate temperatures. The presented structural and compressibility results are in agreement with the available theoretical and experimental data on binary rare-earth borides and can serve as a reliable reference for future studies.

(Some figures may appear in colour only in the online journal)

1. Introduction

Durable coatings are used industrially to improve the life and performance of mechanical components and cutting tools [1]. Diamond is the material traditionally used in these applications due to its high hardness, high melting point and low plastic deformation [2, 3] but it is not suitable for a number of applications such as cutting steel. This need for improved performance has led to an experimental and theoretical search for alternative materials. There have been two basic approaches used to guide this search. One was to look for materials like diamond that have very low bond polarization, such as boron nitride [4, 5], and the other was to look for materials with very high densities, such as uranium [6]. An alternative approach is to make hybrid materials by combining transition metals with a layered boron or carbon network [7]. Recent examples include OsB₂ and ReB₂ which were shown to have bulk moduli of 365–395 GPa [8] and 360 GPa [9], respectively, approaching that of diamond. Recently published theoretical studies suggest that rare-earth diborides (REB₂) might rival these materials. Density functional calculations showed the bulk modulus of LuB_x to be 166.9, 183.5 and 218.3 GPa for $x = 2, 4$ and 12 [10]. Applying similar techniques, the calculated large bulk modulus (in the 140–200 GPa range)

and high hardness (15–20 GPa) [11] of REB₂ (RE: Tb, Dy, Ho, Er, Tm and Yb) revealed that these are incompressible and hard materials. So far there has been no experimental determination of the bulk modulus or hardness in this system. Here we report the synthesis of high purity YbB₂ and its characterization using powder diffraction and photoemission. We also investigated the phase stability as a function of pressure and report the bulk modulus. The main objectives of this study were to investigate the phase stability under pressure of YbB₂, and to help to fill the gap in the literature regarding the values of the bulk modulus (B_0) and alternative synthesis routine for the REB₂.

2. Experimental details

Samples were prepared by solid-state reaction. The starting boron was in the amorphous powder form (Alfa Aesar, 99.99%) while Yb was in ingot form (Ames Laboratory, 99.95%). Small Yb pieces were scraped from the ingot surface in order to increase the reaction surface of the metal. Appropriate amounts of Yb and B were weighed in a glove box with an oxygen and moisture level below 1 ppm. Several reaction cells which were designed in different geometries and dimensions were used for the heating processes. In line with the results of various preliminary synthesis attempts [12], a

sealed Ta tube was used to realize the heat treatments. Oxides and similar on the Ta tube surface were removed by an etching process in HF: HNO₃:H₂O (1:1:3) solution before each heat treatment. The starting mixture was subjected to heating in a tubular furnace in a flowing Ar atmosphere at designated duration and temperature. Then, the samples were pressed into pellet form under 2200 psi after an intermediate grinding. The pellets were wrapped with Ta foils and sintered at moderate temperatures. In order to investigate the effect of heating temperatures and periods and the starting compositions on the isolation of the YbB₂ phase, four different groups of samples were prepared. The starting composition of the first two groups was in the stoichiometric ratio and the samples were heated at elevated temperatures of 850 and 950 °C for different periods described in the text. The third group of samples was heat treated for 96 h at 650, 750, 850 and 950 °C, respectively. The last sample group with a small excess of Yb metal, Yb_xB₂ ($x = 1.0, 1.1$ and 1.2), in the starting composition was sintered at 850 °C.

Structural characterization and phase analysis studies with the sintered samples were realized by x-ray powder diffraction using a HUBER-Guinier Imaging Plate Camera G670 with a RU-200 Cu rotating anode. An asymmetrically ground curved Ge(111) monochromator was aligned to obtain only the Cu K α 1 radiation ($\lambda = 1.5406$ Å), which was calculated by a Si standard. Intensity data were collected over a 2θ range from 5 to 100° at a step width of 0.005° for about 30 min per sample contained in a 0.5 mm Pyrex capillary tube. An extended data acquisition time was preferred to reduce the noise level and realize phase analysis with more accuracy.

High pressure measurements at ambient temperature were made using a standard symmetric diamond anvil cell with 300 μ m culet diamonds and tungsten carbide and boron nitride backing plates. Rhenium gaskets were indented to a thickness of about 30 μ m. For diffraction measurements, a 150 μ m hole was drilled in the center of the indentation and was loaded with the sample, 4:1 methanol:ethanol mixture (MEM) as the pressure transmitting fluid and small spheres of ruby as a pressure marker. Regarding the pressure calibration in these measurements, the ruby fluorescence spectra showed a sharp doublet throughout our measurements, with no measurable broadening of the peaks. A number of small ruby spheres were placed around the sample chamber. Pressure was measured from each of these spheres, and differences in the measured pressure between these spheres were found to be within the experimental accuracy of the pressure scale used. These results lead us to conclude that sample is under hydrostatic pressure in our measurements.

High pressure x-ray diffraction experiments were performed at the high pressure beamline (BL12.2.2) of the Advanced Light Source at Lawrence Berkeley National Laboratory [13]. Angle-dispersive diffraction data were collected at an energy of 30 keV selected using a two-bounce Si(111) double-crystal monochromator. The beam was focused to a 10 μ m \times 10 μ m spot which is necessary for these measurements to avoid any contamination of sample patterns by scattering from the gasket or ruby. The sample–detector distance can be as small as 200 mm to allow the detector

to match the opening angle of the diamond anvil cell. A MAR345 image plate detector was used to collect diffraction images. The sample–detector distance and the detector tilt angles were measured using powder diffraction from a LaB₆ standard. The x-ray beam was 99% horizontally polarized and all geometric and polarization corrections were made during the angular integration using the program FIT2D [14]. The Celref program [15] was used to determine unit cell parameters and volumes.

The crystal structure of YbB₂ at ambient conditions was refined with the Rietveld method using the DBWS program [16]. The background in the raw x-ray diffraction (XRD) pattern was modeled automatically by the Sonneveld method [17]. A full background curve was linearly interpolated from the background points and the interpolated background curve was subtracted from the pattern.

X-ray photoelectron spectroscopy (XPS) measurements and qualitative analysis were carried out on some YbB₂ polycrystalline samples at room temperature to determine the valence state of Yb in YbB₂. This was compared with the spectrum of a partially surface oxidized Yb metal. XPS data were collected using a Kratos ES300 model electron spectrometer with a Mg K α (1253.4 eV) x-ray radiation. XPS data were analyzed using the XPSPEAK 4.1 software [18].

3. Results and discussions

XRD patterns of the sample group heat treated at 650, 750, 850, and 950 °C for 96 h are presented in figure 1. The insets in figure 1 show the 27–37.5° region which is enlarged to identify major impurity phases—YbB₄ and Yb₂O₃. The results pointed out that there is no other binary boride phase of Yb, such as YbB₆, and unreacted Yb in the XRD patterns. It should also be noted that unreacted Yb may have been condensed on the inner surfaces of the Ta tube during the cooling process. The presence of a minor amount of the Yb₂O₃ phase indicates that either the reaction cell or the starting Yb metal is partially oxidized during the synthesis routes. As seen in figure 1, samples heated at 650 and 750 °C show poor crystallinity. With increasing temperature, the diffraction peaks become sharper, narrower and more intensive which indicates enhancement of the crystallinity. However, the presence of a significant amount of impurity phases in the XRD pattern of the sample heated at 950 °C leads us to keep the heat treatment temperature in the range of 750–850 °C which is low enough to eliminate the formation of the higher amount of YbB₄ due to the Yb loss, and high enough to obtain a good crystallinity.

Next the sample group was heated at 850 °C for 3, 24, 96 and 192 h to optimize the time period of the synthesis route. Analysis of the XRD patterns of samples not presented here clearly showed that YbB₂ phase peaks become sharper and narrower as the annealing period increases. The intensities of impurity reflections decrease with the annealing period up to 96 h, reach a minimum at this period and then increase for the 192 h heating period. These results reveal that the optimum heating temperature and period to synthesize the YbB₂ phase using our preparation routes is in the range of

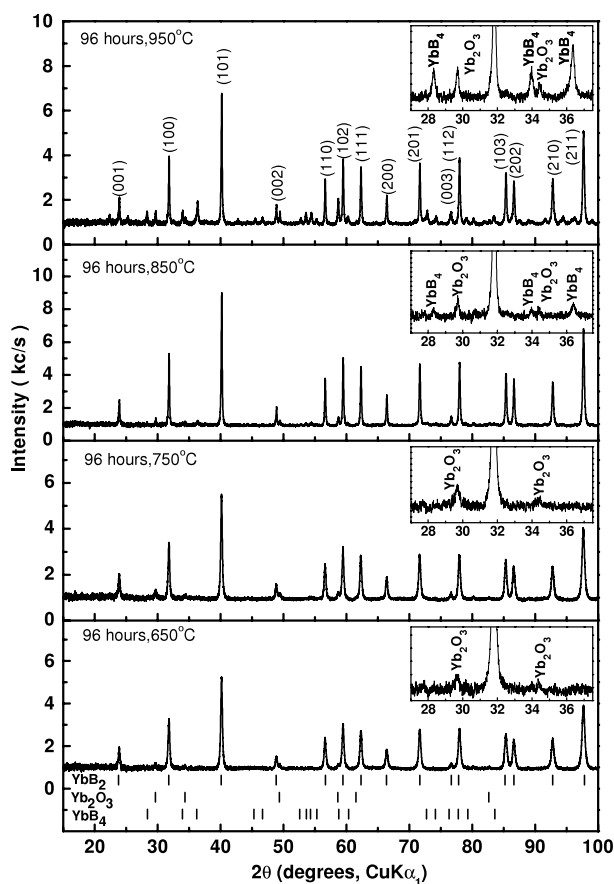


Figure 1. X-ray powder diffraction patterns of YbB_2 samples heat treated at different temperatures for 96 h. Insets: the $27\text{--}37.5^\circ$ region enlarged to identify major impurity phases; YbB_4 and Yb_2O_3 .

$750\text{--}850^\circ\text{C}$ and 96 h, respectively. However, optimization of the heat treatment conditions is not enough to control sample quality sensitively due to the fact that possible loss of Yb metal vapor pressure still allows formation of a YbB_4 impurity phase, as can be seen in figure 1. Therefore, a final series of samples with a composition of Yb_xB_2 ($1.0 \leq x \leq 1.3$) were heat treated at 850°C for 96 h to study the influence of the excess Yb in the starting composition on phase formation. Figure 2, where XRD patterns of Yb_xB_2 samples are plotted in an enlarged range between 27 and 37.5° , shows that the YbB_4 phase disappears and the amount of the Yb_2O_3 phase decreases to $0.5 \pm 0.4\%$ (w/w) by introducing 20% excess Yb. These results show that it is possible to isolate 99% and 99.5% pure YbB_2 phase with 10% and 20% excess Yb reinforcement, respectively. Moreover, we can conclude that the synthesis details presented here serve as alternative route for the synthesis of YbB_2 phase which is more likely to be obtained in high purity form at the thermodynamic conditions reported here.

YbB_2 has a simple hexagonal (hex) AlB_2 type ($P6/mmm$, 191) crystal structure and contains graphene like boron layers separated by hexagonal close-packed Yb layers, similar to MgB_2 [19]. Yb atoms occupy the center of boron hexagons and face both directly above and below each Yb in the metal layers. The hexagonal framework of Yb in 2a (0, 0, 0) and B in 2d ($1/3, 2/3, 1/2$) Wyckoff positions is shown in the

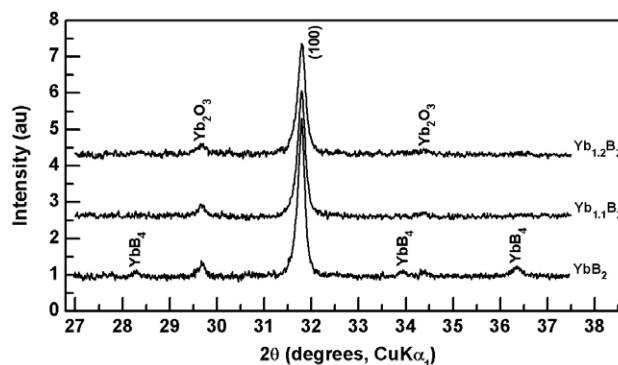


Figure 2. The $27\text{--}37.5^\circ$ range in the XRD patterns of the samples synthesized with different starting compositions; Yb_xB_2 ($x = 1, 1.1$ and 1.2). Impurity peaks are labeled with their chemical formulae.

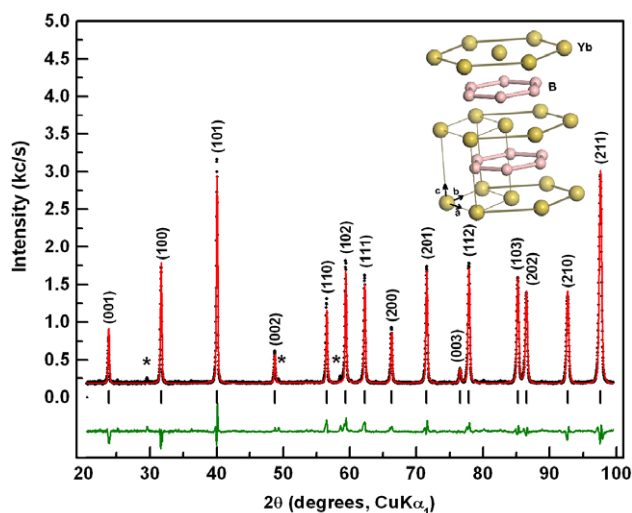


Figure 3. Observed XRD pattern of $\text{Yb}_{1.1}\text{B}_2$ prepared at 850°C for 96 h (dots) and the calculated pattern of the modeled structure of YbB_2 (red line). The difference between the two patterns is plotted in the lower part of figure as a solid trace (green line). The vertical bars refer to the calculated allowed Bragg reflections. No region was excluded from the refinement. Impurity peaks are labeled with asterisks. The inset is the molecular structure of YbB_2 .

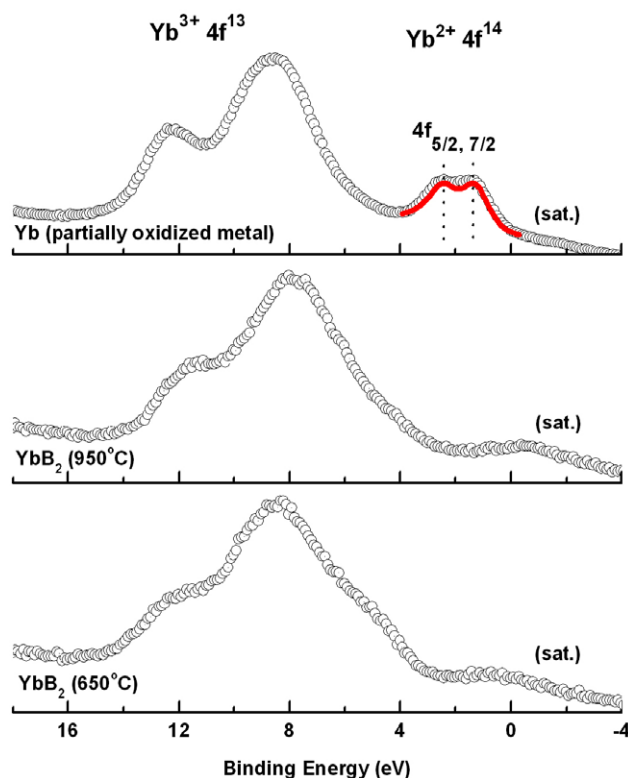
inset of figure 3, and is used as the structural model for Rietveld refinement applied to the XRD pattern of a YbB_2 sample synthesized at 850°C for 96 h. In the initial steps of refinement, the scale factor and background coefficients were refined, and other parameters were then included. Coefficients of the sixth-order polynomial function were refined with a few iteration cycles to fit the background of the measured XRD data. In the following process, zero offset and lattice parameters were refined to optimize peak positions of the calculated pattern and volume of the model structure. After a few iteration cycles, zero offset was converged to a minimal negligible value. Analytical profile fitting was realized with the refinement of mixing and parameters U, V, W using the pseudo-Voigt peak function. During refinement cycles, special Wyckoff positions of Yb and B atoms were fixed. Towards the end of refinement, atomic temperature factors of Yb and B atoms were allowed to refine systematically. Iterations were cycled many times until $R_p, R_{wp}, R_{\text{Bragg}}$ (Bragg R -factor)

Table 1. Crystallographic data and some parameters for the structural refinement of YbB₂.

Formula	YbB ₂
Crystal system	Hexagonal
Space group	<i>P6/mmm</i> (191)
<i>a</i> (Å)	3.2522(2)
<i>b</i> (Å)	= <i>a</i>
<i>c</i> (Å)	3.7297(4)
Cell volume (Å ³)	34.162(8)
Calculated density (g cm ⁻³)	9.465(3)
<i>Z</i> (formula units per unit cell)	1
Data points	3925
Reflections	15
<i>R_p</i> , <i>R_{wp}</i>	0.0679, 0.0892
<i>R_{Bragg}</i> , <i>S</i> (χ ²)	0.0510, 1.24
Atomic parameters:	
Yb	2a (0, 0, 0), B (Å ²) = 0.39(3), <i>N</i> = 1
B	2d (1/3, 2/3, 1/2), B (Å ²) = 1.83(2), <i>N</i> = 1

and *S* (χ², goodness of fit), which were the figures of merit for refinement, converged to their minimal values as 0.0679, 0.0892, 0.0510 and 1.24, respectively (see table 1). The refined pattern of model structure was presented in figure 3. In total, 15 reflections were refined by 17 parameters. The refined lattice parameters, *a* = *b* = 3.2522(2) Å and *c* = 3.7297(4) Å, of the YbB₂ phase are found to be slightly smaller than the values reported by Avila *et al* [12]. As expected, the refined temperature factors of the B atoms are significantly larger than those for Yb, which is much more massive than B. It should also be noted that our XRD patterns and structural refinements reveal (003) reflection at 77° 2θ that could not be observed in any previous study and it is the only reflection out of those observed that cannot be explained as a reflection of hex-YbB₂ phase.

The valence state of Yb in the obtained YbB₂ phase was investigated with XPS measurements. The spectral analysis is presented in figure 4. The 4f band spectra collected from YbB₂ samples synthesized at 650 °C and 950 °C are displayed in the same binding energy range with the valence band spectrum of the partially oxidized Yb metal sheet to identify both of the valence states of Yb. XPS data of the surface oxidized Yb metal clearly reveal four peak structures at 1.3, 2.5, 8.6, and 12.3 eV below the Fermi energy. The two peaks located at 1.3 and 2.5 eV below the Fermi level correspond to the 4f_{7/2} and 4f_{5/2} spin-orbit doublet of the divalent Yb²⁺ (4f¹⁴) pure metal, respectively [20]. The positions and relative intensities of these peaks are very well known [21] and are in good agreement with the previous published data [22]. The red line in the same spectrum also indicates a fit obtained using the XPSPEAK program. The peaks located at 8.6 and 12.3 eV belong to the 4f complex multiplet structure of the Yb₂O₃ phase where the Yb metal is in the form of a trivalent Yb³⁺ (4f¹³) valence state [23, 24]. In the 4f spectra of the samples synthesized at 650 and 950 °C, it can be seen that the pronounced multiplet in the 8–13 eV energy range becomes prominent, and the spin-orbit doublet of Yb²⁺ part is not

**Figure 4.** Valence band x-ray photoemission spectra of Yb for three different samples. The peaks designated as (sat.) refer to *Kα*_{3,4} satellites of the x-ray source.

observed. The small shift of the characteristic lines towards lower binding energy in the spectrum of the YbB₂ samples compared with the partially oxidized Yb metal is related to the different chemical environment of the Yb atom in diboride structures and Yb₂O₃ compounds. Relative intensities of the 4f¹³ doublets do not change significantly, although the peaks are broadened, due most probably to structural and/or chemical inhomogeneities. Based on these results, it can be summarized that XPS measurements on high purity samples, clearly exhibit the valence state of the Yb atom in the YbB₂ compound as mostly 3+ as indicated in a previous study where the calculation of effective magnetic moment from the susceptibility measurements using the Curie–Weiss law was done [12].

Room temperature XRD patterns of YbB₂ crystal collected under compression are shown in figure 5. The compression cycle results in a simple shift of diffraction Bragg peaks to higher angles, indicating a decrease in the unit cell dimensions. The results clearly reveal that YbB₂ does not show a significant structural change and remains stable up to 20.2 GPa, the highest measured pressure in this study. The normalized lattice parameters, *a/a*₀ and *c/c*₀, as a function of pressure are illustrated in figure 5. Refined lattice parameters decrease very slowly with increases in pressure, consistent with the high hardness property for this material. Moreover, both *a/a*₀ and *c/c*₀ exhibit very similar pressure dependence, indicating that the compressibility along *a* and *c* axes is fairly isotropic even though the structure is classified as a layer structure. This result is inconsistent

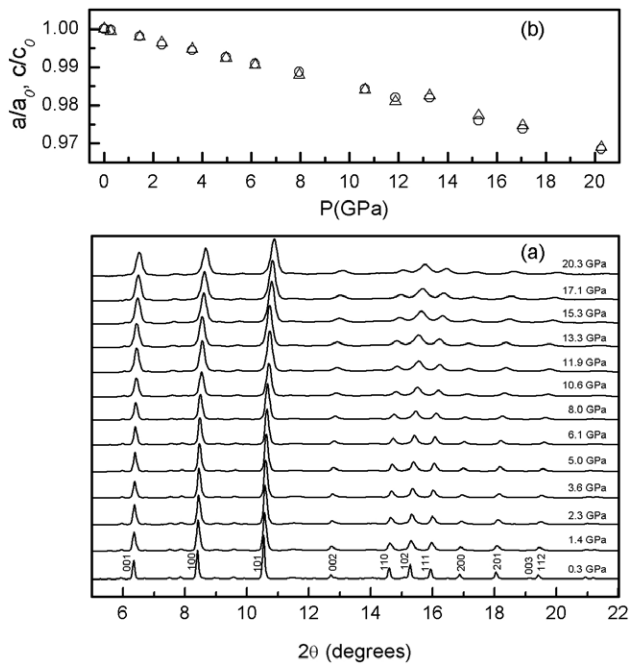


Figure 5. (a) XRD patterns collected upon compression. (b) Pressure dependence of the normalized lattice parameters, a/a_0 (circles) and c/c_0 (triangles).

with the chemical bonding characteristics reported by Spear *et al* [25] that respective bond distances and Yb–Yb/Yb–B bond strengths are comparable. Also, B and Yb layers seem therefore to be tightly bound together by Yb–B bonding [25]. Surprisingly, the compressions along the a and c axes display an abrupt kink in the 12–14 GPa pressure range, while there is no significant change in XRD patterns presented in figure 5. We believe that the change in slope of a/a_0 and c/c_0 could be due to the solidification of the MEM instead of a possible phase transition in this pressure range. The unit cell volume at each measured pressure was calculated using the respective lattice parameters. The pressure dependence of the normalized unit cell volume of the YbB_2 can be described by the second order (assuming that $K'_0 = 4$) Birch–Murnaghan equation of state (EOS) [26] that yields the bulk modulus (K_0) 182.2 ± 5.3 GPa for YbB_2 (the continuous curve in figure 6). The calculated K_0 value in this study is slightly larger than the values ranging between 147 and 163 GPa [11] predicted with *ab initio* calculations for YbB_2 . Moreover, the Birch–Murnaghan EOS fit gives $V_0 = 34.3 \pm 0.1 \text{ \AA}^3$ that is very close to the experimental ambient unit cell volume of $V_0 = 34.21 \pm 0.04 \text{ \AA}^3$ determined with Rietveld refinement in figure 3. It should also be noted that the hydrostatic conditions were estimated at this relatively low pressure range in a MEM based on a previous report and our pressure measurements. Therefore, we can conclude that there is no overestimated trend on the value of K_0 . To better understand the compressibility of YbB_2 the experimental volume compression as a function of pressure is plotted in figure 6 with the results for diamond [27], c-BN [28], ReB_2 [29], OsB_2 [30], LuB_2 [11] and GdB_2 [11] determined via experimental data and first-principles calculations. Compared

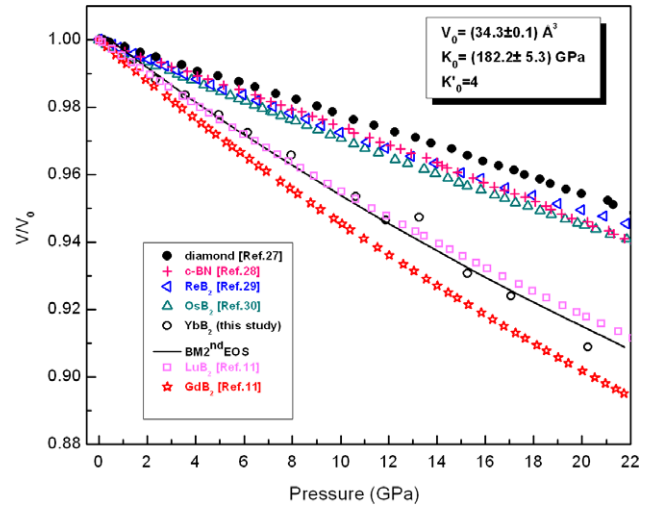


Figure 6. Volume compression of YbB_2 as a function of pressure with a Birch–Murnaghan second EOS fit. The calculated and experimental compressibility curves of some other hard and super-hard materials are also depicted for comparison.

to predicted hard materials such as GdB_2 and LuB_2 , YbB_2 is less and slightly more compressible, respectively while its compressibility is higher than that of diamond, c-BN, ReB_2 and OsB_2 , known as super-hard materials. It can be concluded that the compressibility of the lanthanides is correlated with the size of the lanthanide atom.

4. Conclusions

The crystal structure of YbB_2 up to 21 GPa has been investigated using high-resolution x-ray diffraction at ambient temperature. YbB_2 is found to be stable throughout the whole pressure range and does not show a structural phase transition. The bulk modulus of YbB_2 derived from P – V measurement was determined to be 182.2 ± 5.3 GPa, which is, to date, the only and most accurate experimental value available. The high value of the bulk modulus indicates that YbB_2 has low compressibility and may be classified as a hard material. The compressibility along the c axis is close to that along the a axis, indicating that the compressibility of YbB_2 is fairly isotropic in the studied 0–21 GPa pressure range. Besides the high pressure structural properties, we developed a process for the synthesis of YbB_2 phase with a purity of 99.5% at relatively low temperatures. Single phase Rietveld refinement confirms the hexagonal structure in $P6/mmm$ space group with the lattice parameters of $a = b = 3.2522(2) \text{ \AA}$ and $c = 3.7297(4) \text{ \AA}$. The valence band in XPS measurements is presented in the 0–20 eV energy range, which is dominated by the complex $4f^{13}$ multiplet of Yb. Based on these results, it is concluded that Yb ions are in the trivalent form in the YbB_2 compound and this valence state does not depend on the annealing history of the samples.

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