

# Transient simulation of an atmospheric boundary layer flow past a heliostat using the Scale-Adaptive Simulation turbulence model

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## Abstract

Heliostat fields are exposed to changing climatic conditions as they are mostly erected in open environments where the wind naturally features a high unsteadiness at low altitude due to the ground effects. Much of the computational fluid dynamics (CFD) content in the open literature is focused on Reynolds-averaged-Navier-Stokes (RANS) simulations, which can only predict mean loads. This paper considers an isolated heliostat in worst-case orientation. The drag force is numerically modelled by means of a Scale-Resolving Simulation (SRS) in ANSYS v19. This paper firstly deals with two different methods that generate perturbations at the inlet boundary: the spectral synthesizer and the vortex method. In an empty domain, an atmospheric boundary layer (ABL) profile is modelled based on a wind tunnel experiment. Secondly, the wind tunnel test of a single heliostat model in upright orientation is replicated, aiming to model the mean and peak drag forces. Applicable for highly separated flows, the Scale-Adaptive Simulation (SAS) turbulence model is employed as it is computationally more affordable than a Detached Eddy Simulation (DES) approach. The latter would require a higher grid resolution and a reduced time step size. The SAS showed little but acceptable decay of the inlet profiles whilst achieving lateral homogeneity. The mean and root-mean-square error of the drag force signal showed a deviation with the experiment of 0.04% and 5.8%, respectively, whereas the error on the peak drag forces was around 18%, possibly mostly due to the under-prediction of the turbulent integral length scale at the model location.

## Nomenclature

			42	$HCL$	Height of centreline of heliostat	$m$
			43	$I_x$	Longitudinal turbulence intensity	
24	$\Delta$	Cell edge length	$m$	44	$k$	Turbulence kinetic energy $m^2/s^2$
25	$\epsilon$	Turbulence dissipation rate	$m^2/s^3$	45	$L_t$	Turbulence integral length scale $m$
26	$\kappa$	von Kármán constant		46	$L_u^x$	Longitudinal integral length scale of turbulence $m$
27	$\mu_t$	Eddy viscosity	$Pa \cdot s$	47		
28	$\Omega$	Vorticity magnitude	$s^{-1}$	48	$L_u^x$	Longitudinal integral length scale $m$
29	$\omega$	Specific dissipation rate	$s^{-1}$	49	$M_y$	Base overturning moment $N \cdot m$
30	$\Omega_{CV}$	Cell volume	$m^3$	50	$MH_y$	Overturning moment $N \cdot m$
31	$\bar{U}$	Time average of U	$m/s$	51	$n$	Frequency $Hz$
32	$\rho$	Air density	$kg/m^3$	52	$RMSE$	Root-mean-square error
33	$\sigma$	Standard deviation		53	$S$	Strain rate magnitude $s^{-1}$
34	$c$	Heliostat chord length	$m$	54	$S_u$	Power spectral density of the longitudinal fluctuating velocity $m^2 \cdot s^{-2} \cdot Hz^{-1}$
35	$C_{Fx}$	Drag force coefficient		55		
36	$C_{MH_y}$	Overturning moment coefficient		56	$U$	Local velocity magnitude $m/s$
37	$C_{M_y}$	Base overturning moment coefficient		57	$u'_x$	Longitudinal fluctuating velocity $m/s$
38	$Co$	Courant number		58	$U_x$	Longitudinal velocity $m/s$
39	$f$	Normalised frequency		59	$u_*$	Friction velocity $m/s$
40	$f_s$	Sampling frequency	$Hz$	60	$y^+$	Non-dimensional wall distance
41	$F_x$	Drag force	$N$	61	$z_0$	Surface roughness length $m$

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62 Keywords: computational fluid dynamics (CFD); Scale-Adaptive Simulation (SAS); atmospheric boundary  
63 layer (ABL); heliostat; turbulence power spectrum

## 64 1. Introduction

### 65 1.1. Background

66 Due to an increase in greenhouse gas emissions, combined with declining reserves of fossil fuels, there is  
67 a global determination towards investing in renewable energies in order to increase their representation in  
68 the energy mix. Although one can raise the issue of intermittency for some of them, forecasting methods  
69 and models can be improved so that the supply and demand are adjusted accordingly (Zhang et al., 2020).  
70 There is also a considerable drive for the study and design of small-scale power generation technologies  
71 as they can be integrated into urban areas (Longo et al., 2020). Photovoltaic technology has shown the  
72 possibility of harvesting solar energy and is providing hope for previously aborted projects in concentrating  
73 solar power (CSP). However, a cheaper storage capacity and a greater dispatchability offers great advantages  
74 for CSP. The total installed costs of CSP plants could decrease by more than one-third between 2015 and  
75 2025 (IRENA, 2016). A higher storage capacity will increase a CSP plant capacity factor and lower its  
76 capital cost (IRENA, 2020). Namely, in 2018 and 2019, the median capital cost of a CSP project with a  
77 storage capacity between 4 and 8 hours was 5,914 USD/kW versus 4,976 USD/kW for over 8 hours. The four  
78 types of CSP plants are presented in Figure 1. The linear Fresnel and the parabolic dish power plants are  
79 smaller-scale technologies. The electricity generation lies between 0.1 and 0.2 MW hour per year per square  
80 metre of reflective area (National Renewable Energy Laboratory, 2017). The capacity does generally not  
81 exceed 30 MW. Parabolic trough and solar tower power plants generally generate over 0.3 MW hour per year  
82 per square metre of reflective area. They are larger-scale projects as they are designed to feature capacities  
83 over 50 MW.

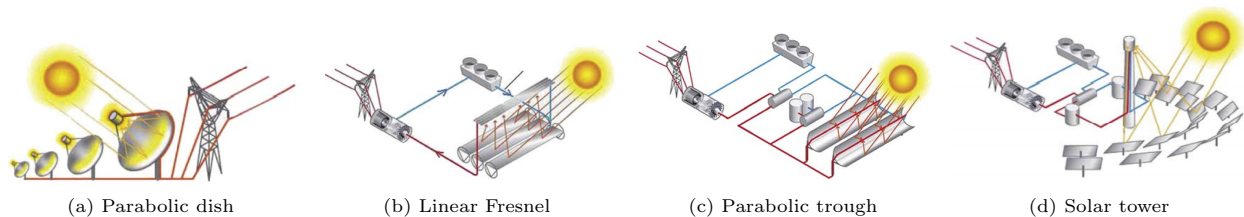


Figure 1: Schematics of the various CSP plants (Blanco and Santigosa, 2016)

84 There has been a growing interest in the solar tower technology since there is a global increase in plant  
85 efficiency relative to parabolic troughs. In 2015, the levelised cost of energy (LCOE) of both technologies  
86 was ranging from 0.15 to 0.19 USD/kWh with a slightly more advantaging reference value for the solar  
87 towers (0.161 USD/kWh versus 0.165 USD/kWh for troughs). In 2025, both reference values should drop to  
88 0.104 USD/kWh for trough plants versus 0.091 USD/kWh for solar tower plants (IRENA, 2016). The latter  
89 offer greater concentration ratios, therefore taking the heat transfer fluid to a higher temperature, which  
90 in return increases the storage efficiency. Molten salt used for storage purposes can also be utilised as the  
91 working fluid. Higher temperatures allow the use of more efficient turbines. All of these make for higher  
92 capacity factors for the solar tower power plants. Another advantage is that the reflectors can be implanted  
93 on uneven ground and moderately hilly terrains. A detailed comparison of the various characteristics of the  
94 different CSP technologies has been reported by IRENA (2012) in the form of a table. In most cases, the  
95 profitability of a power plant is improved by increasing the efficiency of some of its sub-systems. However,  
96 regarding the solar tower technology, one can greatly diminish the total capital cost of a plant by building  
97 the heliostat field at a lower cost. Indeed, every single unit has its own drive mechanism system and must  
98 withstand the wind loads to which it is subjected throughout the lifetime of the power plant. As depicted  
99 on Figure 2, the heliostat field of a solar tower power station can comprise several hundreds of thousands of  
100 units and represents around 40 % of its total capital cost (Pidaparthi, 2017).

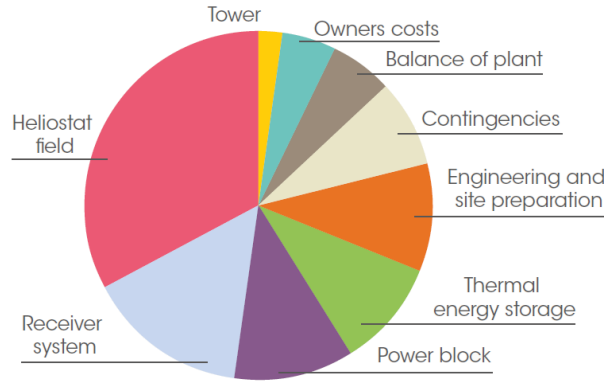


Figure 2: Cost breakdown for a CSP tower plant in South Africa (IRENA, 2012)

101 Although wind tunnel tests are preferred for heliostat design, CFD provides valuable information for the  
 102 design and optimisation of a heliostat structure (e.g. Pfahl et al. (2011b), Emes et al. (2017), Paetzold et al.  
 103 (2014), Marais et al. (2015)). It delivers a good representation of the flow field all around the model whereas  
 104 wind tunnel tests are limited to measured datasets. The number of CFD studies that cover wind loading on  
 105 heliostats remains low, however. These studies are mostly tied to RANS simulations. Besides, this is not  
 106 sufficiently rigorous since RANS models assume the turbulence to be isotropic which is mostly not the case  
 107 in reality. Moreover, due to time-averaging, such simulations do not enable the computation of peak loads  
 108 which are required for heliostat design at operational wind conditions. Wind loading within the atmospheric  
 109 boundary layer (ABL) is strongly time-dependent and this has to appear in the characteristics of the flow.  
 110 The aim of the study is to replicate a wind tunnel test of Peterka et al. (1986) with ANSYS Fluent v19 using  
 111 a SRS turbulence model solving in transient mode.

## 112 1.2. Literature review

113 The solar tower technology projects date as far back as the early 1980s (Breeze, 2019). Although wind  
 114 tunnel tests are generally undertaken in the final stages of the structural design in order to assess the strength  
 115 of a prototype that is submitted to wind loading, they are also used to investigate possible innovations.  
 116 Numerous wind tunnel tests have been carried out over the past four decades and one can find results and  
 117 findings in the literature. Peterka et al. performed extensive wind tunnel experiments for the CSP field.  
 118 They gathered data and provided results in several comprehensive reports (Peterka et al., 1986, 1987b, 1988,  
 119 1990) and scientific publications (Peterka et al., 1987a, 1989). They compiled their tests and research and  
 120 issued guidances for the structural design of heliostats and parabolic dish collectors (Peterka and Derickson,  
 121 1992). Pfahl et al. also carried out several wind tunnel experiments aiming at improving heliostat design  
 122 and decreasing the manufactural costs (Pfahl et al., 2011a,b, 2014, Pfahl, 2018). Pfahl (2014) listed the  
 123 concepts for the cost reduction of heliostats, detailed their advantages and drawbacks and contributed to a  
 124 review summarising the state of the art around heliostats (Pfahl et al., 2017). On a techno-economic aspect,  
 125 Blackmon (2013, 2014) made parametric investigations leading to safety factors and fatigue life assessments  
 126 as well as heliostat optimal reflective area estimations, whilst Emes et al. (2015, 2020) worked on correlations  
 127 between ABL characteristics and heliostat structural design. Liu et al. (2014) studied the influence of wind  
 128 fences around the heliostat field on wind loads. This has also been partly investigated by Peterka et al.  
 129 (1986, 1987b, 1988) along with the impact of the collectors field density. Peterka et al. (1987b, 1988) realised  
 130 that the collectors are highly sensitive to the gustiness of the approaching wind. Emes et al. (2017, 2018)  
 131 examined this phenomenon for isolated and tandem heliostats in the stow position. One can also find several  
 132 full-scale studies and validation data in the literature (Sment and Ho, 2014, Vásquez-Arango et al., 2015,  
 133 Zang et al., 2012, Griffith et al., 2011, Rebolo et al., 2011, Gong et al., 2015). Peterka et al. (1987b) has  
 134 studied the shape of the mirror (circular versus square) while Pfahl et al. (2011a) focused on the impact of  
 135 the heliostat aspect ratio. Both studies used wind tunnel tests only. Assuming a gust factor for the ratio of  
 136 peak to mean loads has been found to underestimate the peak loads, especially in stow position. The peak  
 137 coefficients have been shown to be dependent on the turbulence intensity and integral length scales in the  
 138 approaching ABL. This is discussed by Peterka and Derickson (1992), Pfahl (2018), Emes et al. (2019) and

139 Jafari et al. (2019), based on wind tunnel measurements. Since the design strength of a collector should be  
140 rather directly based on the peak wind loads (Peterka et al., 1987b), the objective of the researchers is to  
141 build a CFD model that can compute the peak loads with acceptable accuracy.

142 Although the accuracy of CFD RANS simulations is often not satisfactory enough in a dynamic loading  
143 framework, Huss et al. (2011) showed that the change in the wind loads with both elevation and azimuth  
144 angles matches with trends given by experimental results. Besides, it can provide meaningful information  
145 for a given trend in the experimental data. For instance, Pfahl et al. (2011b) measured a 20% increase of  
146 the hinge moment in its worst case orientation for a heliostat with a wide central gap compared to a solid  
147 heliostat. Through CFD analyses, they realised that the leeward pressure distribution is greatly influenced  
148 by the gap. Another advantage of CFD is the possibility to explore a wide range of structural designs and  
149 variables before fabricating a model that will undergo wind tunnel tests. Marais et al. (2015) and Marais  
150 (2016) developed a numerical method that optimises a heliostat aspect ratio based on wind loading moments  
151 endured by the drive mechanisms. Wu et al. (2010) showed numerically and experimentally that small gaps  
152 between heliostat facets do not have an impact on the wind loading.

153 In this study, the researchers aim to model the air flow past a heliostat. The collector is oriented so as to  
154 be perpendicular to the incoming mean flow, acting as a bluff body in the maximum drag orientation. The  
155 resulting vortex shedding phenomenon excites the structural components of the heliostat, affects the pressure  
156 distribution on the leeward side of the collector and may have a considerable impact on the accuracy of the  
157 solution (Chen and Chiou, 1998). Unfortunately, RANS models fail to resolve the most energy-containing  
158 turbulent structures and represent most of the interactions between the vortices of different scales (Fröhlich  
159 and von Terzi, 2008). Most CFD studies that address wind loading in CSP are done using RANS simulations  
160 (Christo, 2012, Zemler et al., 2013), Large Eddy Simulation (LES) (Boddupalli et al., 2017, Hachicha et al.,  
161 2013, 2014) or hybrid RANS/LES methods such as SAS (Paetzold et al., 2014, 2015, 2016), Stress-Blended  
162 Eddy Simulation (Wolmarans and Craig, 2019) or Detached Eddy Simulation (Poulain et al., 2016b). One  
163 can combine transient simulations with a modal analysis in order to assess the dynamic wind loading of  
164 a structure. Fluid-structure interaction studies have previously been carried out for a heliostat collector  
165 (Vásquez-Arango et al., 2017, Wolmarans and Craig, 2019) in an attempt to link the resolved flow field with  
166 the structural response. Although LES greatly improves the accuracy of a model, the computational cost  
167 of the simulation increases as well. Indeed, the mesh has to be fine enough so that most of the turbulence  
168 energy spectrum is resolved which can become problematic in the near-wall area where both the cell aspect  
169 ratio and the  $y^+$  have to be close to 1. Such a stringent condition will affect the total computational cost  
170 further since a smaller time step has to be set. Therefore, the challenge is to achieve acceptable accuracy in  
171 the results with a minimum computational time. For this reason, this study focuses on the ability of the SAS  
172 turbulence model to compute the drag force on a heliostat collector submitted to ABL flow. The advantage  
173 it has over any RANS model is that it can substantially resolve the turbulent fluctuations (Fröhlich and  
174 von Terzi, 2008) for a much lower computational time compared to solving with LES. It has previously  
175 shown good agreement with experimental values and can sometimes perform better than RANS and hybrid  
176 RANS/LES models (Egorov et al., 2010, Maliska et al., 2012, Zheng et al., 2016). This case, being a flow  
177 past a bluff body, falls in the range of application of this model (Menter, 2012).

### 178 1.3. Layout

179 In the first place, this paper will introduce the SAS turbulence model used in this work and will detail  
180 its specificities and advantages for transient simulations. The next section focuses on the ABL and the  
181 equations developed to model its fully-developed profile. It will also give a view on how one can characterise  
182 the turbulence energy content of the flow with the help of the power spectral density (PSD). The researchers  
183 have conducted two CFD simulations for this study. The first one verifies whether one can reproduce  
184 appropriate wind conditions in the modelled wind tunnel. The second one aims model the drag force on  
185 a heliostat in its upright orientation, which is the worst case in terms of wind loading caused by the drag  
186 force. Both the CFD simulations will be detailed and the results will shed light on data sampling frequency  
187 and solution convergence for the simulation. The researchers also present flow characteristics and compare  
188 the drag force against experimental values before making conclusions.



189 2. Methodology

190 2.1. Scale-Adaptive Simulation turbulence model

191 The concept of SAS has been introduced with the aim of relieving turbulence models of their grid  
 192 dependency for the resolution of turbulent structures (Menter et al., 2003). The SAS model is based on an  
 193 exact transport equation for the turbulence length scale developed by Rotta (1972). In Rotta’s  $k - kL$  model,  
 194 the influence of the second derivative of the velocity field appearing in the source term of the scale equation  
 195 is cancelled under the isotropic turbulence assumption. However, aiming to resolve the bigger turbulent  
 196 structures of a non-homogeneous flow, this assumption is unsatisfactory (Menter and Egorov, 2006). The  
 197 second derivative velocity allows the model to adjust its length scale to those structures already resolved  
 198 in the flow (Menter, 2012), hence the use of the denomination “scale-adaptive”. In ANSYS Fluent, the  
 199 momentum equations are transposed to the  $k - \omega$  formulation (Equations 1 and 2). The additional  $Q_{SAS}$   
 200 term (Equation 3) includes the von Karman length scale,  $L_{vK}$ , which does not appear in any standard RANS  
 201 model (Equation 4). The model originally failed to dissipate the smallest-scale eddies (Egorov and Menter,  
 202 2008). Therefore, a limiter has been designed based on the Wall-Adapting Local Eddy-viscosity model in  
 203 order to achieve high wave number damping. A lower limit on the calculation of the eddy viscosity,  $\mu_t$ , is  
 204 enforced (Menter and Egorov, 2010). This limiter is proportional to the mesh cell size,  $\Delta$ , which is derived  
 205 from the cubic root of the control volume size,  $\Omega_{CV}$  (Equation 4). The values of the model constants are  
 206 presented in Table 1 and their calibration can be found in Menter and Egorov (2010).  $F_1$  refers to the  
 207 blending function defined for the baseline  $k - \omega$  model (ANSYS, 2019).

$$\frac{\partial \rho k}{\partial t} + \frac{\partial}{\partial x_i}(\rho U_i k) = G_k - \rho c_\mu k \omega + \frac{\partial}{\partial x_j} \left[ \left( \mu + \frac{\mu_t}{\sigma_k} \right) \frac{\partial k}{\partial x_j} \right] \quad \text{with } G_k = \mu_t S^2 \quad (1)$$

$$\frac{\partial \rho \omega}{\partial t} + \frac{\partial}{\partial x_i}(\rho U_i \omega) = \alpha \frac{\omega}{k} G_k - \rho \beta \omega^2 + Q_{SAS} + \frac{\partial}{\partial x_i} \left[ \left( \mu + \frac{\mu_t}{\sigma_\omega} \right) \frac{\partial \omega}{\partial x_j} \right] + (1 - F_1) \frac{2\rho}{\sigma_{\omega,2}} \frac{1}{\omega} \frac{\partial k}{\partial x_j} \frac{\partial \omega}{\partial x_j} \quad (2)$$

$$Q_{SAS} = \max \left[ \rho \eta_2 \kappa S^2 \left( \frac{L}{L_{vK}} \right)^2 - C \frac{2\rho k}{\sigma_\phi} \max \left( \frac{1}{\omega^2} \frac{\partial \omega}{\partial x_j} \frac{\partial \omega}{\partial x_j}, \frac{1}{k^2} \frac{\partial k}{\partial x_j} \frac{\partial k}{\partial x_j} \right), 0 \right] \quad (3)$$

$$L = \frac{\sqrt{k}}{c_\mu^{1/4} \omega}, \quad L_{vK} = \max \left( \kappa \left| \frac{U'}{U''} \right|, C_S \sqrt{\frac{\kappa \eta_2}{\frac{\beta}{c_\mu} - \alpha}} \cdot \Delta \right) \quad \text{with } \Delta = \Omega_{CV}^{1/3} \quad (4)$$

where  $U' = S = \sqrt{2 \cdot S_{ij} S_{ij}}$  with  $S_{ij} = \frac{1}{2} \left( \frac{\partial U_i}{\partial x_j} + \frac{\partial U_j}{\partial x_i} \right)$  and  $U'' = \sqrt{\frac{\partial^2 U_i}{\partial x_k^2} \frac{\partial^2 U_i}{\partial x_j^2}}$

$c_\mu$	$\sigma_k$	$\beta$	$\sigma_\omega$	$\sigma_{\omega,2}$	$\eta_2$	C	$\sigma_\phi$	$C_S$	$\alpha$
0.09	2.0	0.072	2.0	1.168	3.51	2	2/3	0.11	1

Table 1: SAS model constants

208 2.2. Atmospheric boundary layer and inlet boundary conditions

209 2.2.1. General equations

210 The ABL to which the heliostats are subjected is not uniform and features lower velocities closer to  
 211 the ground but higher fluctuations translate into a higher turbulence intensity. Ideally, to generate such  
 212 a profile, one should model the presence of ground elements upstream of the heliostat model. However,  
 213 this would require an extension of the upstream part of the domain as well as a fine mesh around the  
 214 turbulence-generating elements (e.g. spires and surface roughness elements), all of which resulting in a much  
 215 higher number of cells, therefore increasing the computation time. In order to address this issue, the use  
 216 of fully-developed profiles generated at the inlet boundary of the domain is recommended. Richards and  
 217 Hoxey (1993) derived a set of equations (equations 5, 6 and 7) for the  $k - \epsilon$  turbulence model based on three

218 main assumptions in order to achieve a horizontally homogeneous ABL profile: no vertical velocity, constant  
 219 pressure and constant shear stress. The ABL friction velocity,  $u_*$ , can be calculated using reference values  
 220 for height and velocity:

$$u(z) = \frac{u_*}{\kappa} \ln \left( \frac{z + z_0}{z_0} \right) \quad \text{with} \quad u_* = \frac{\kappa u_{ref}}{\ln \left( \frac{z_{ref} + z_0}{z_0} \right)} \quad (5)$$

$$k = \frac{u_*^2}{\sqrt{C_\mu}} \quad (6)$$

$$\epsilon(z) = \frac{u_*^3}{k(z + z_0)} \quad (7)$$

221 The surface roughness length,  $z_0$ , represents the height of the ground roughness elements. One can play  
 222 around with this parameter to alter the inlet profiles. In fact, an increase will globally result in a lower mean  
 223 velocity but a higher turbulence intensity,  $I$ , which represents the fluctuations within the velocity field. For  
 224 RANS simulations, it is calculated with Equation 8. It has been experimentally shown that results are highly  
 225 sensitive to the turbulence intensity level of the incoming velocity profile (Peterka et al., 1987b). For that  
 226 matter, the researchers aimed to obtain a fairly good match of the turbulence intensity inlet profile generated  
 227 in the CFD model with the experimental one that they have extracted from Peterka et al. (1986).

$$I = \frac{\sqrt{\frac{2}{3}k}}{U} \quad \text{where } U \text{ is the local velocity magnitude} \quad (8)$$

### 2.2.2. Mean inlet boundary conditions

228 In the CFD model, the velocity inlet boundary condition generates the profiles by means of a User-Defined  
 229 Function (UDF) that contains the system of equations developed for an ABL profile presented in the previous  
 230 section. Unfortunately, Peterka et al. (1986) do not mention the reference velocity used for the elaboration  
 231 of their profiles. However, they measured a 40.0 ft/s wind speed at a full-scale height of 10 m during the  
 232 run (number 99 in their Appendix B) that the researchers aim to reproduce. Knowing their reference height  
 233 ( $z_{ref} = 44.7$  in at model scale), the researchers deduced their reference velocity,  $U_{ref} = 16.26$  m/s. A surface  
 234 roughness length of  $z_0 = 0.0008$  m was chosen to match both the experimental turbulence intensity and  
 235 velocity profiles (figures 3 and 4). After applying the scale factor of the experiment which is 1/60, the full-  
 236 scale value for the CFD simulation corresponds to an open farmland with few trees and buildings (Burton  
 237 et al., 2001). This corresponds with values for a typical environment surrounding a CSP plant.  
 238

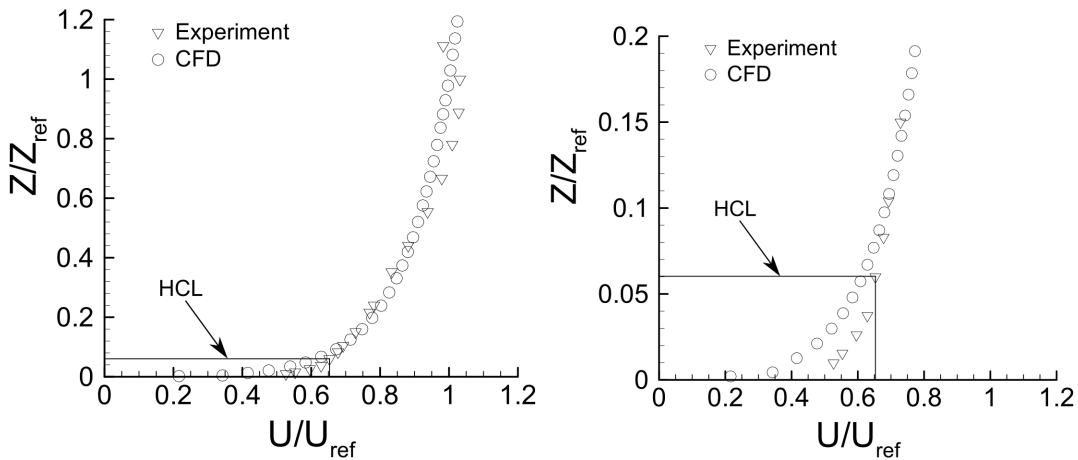


Figure 3: Velocity profile of ABL - Experimental (Peterka et al., 1986) versus CFD, global (left) and zoomed view (right)

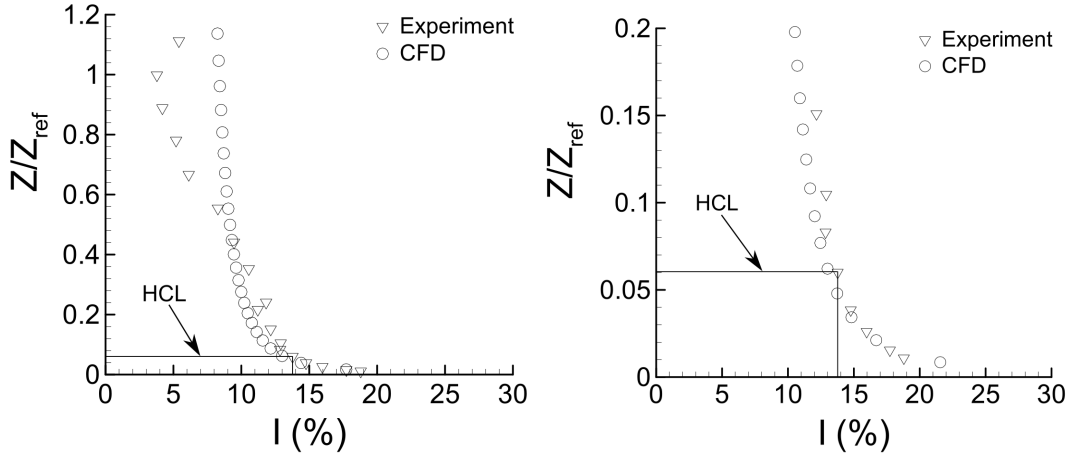


Figure 4: Turbulence intensity profile of ABL - Experimental (Peterka et al., 1986) versus CFD, global (left) and zoomed view (right)

239 Although the turbulence intensity is not exactly matched at the height of the centreline of the heliostat  
 240 (HCL) (13% in the CFD versus 13.7% as the digitised experimental value), it has been decided to proceed  
 241 with these profiles because increasing the surface roughness length would alter them. Indeed, close to the  
 242 ground, the velocity profile would present lower values and a higher gradient, whereas the turbulence intensity  
 243 profile would feature higher values and a higher gradient as well.

### 244 2.2.3. Fluctuating inlet boundary conditions

245 ANSYS Fluent v19 gives four methods for the generation of fluctuating velocity components at the  
 246 velocity inlet boundary: no perturbations, spectral synthesizer, vortex method and synthetic turbulence  
 247 generator. In the current work, the focus will be on the spectral synthesizer and the vortex method. The  
 248 “no perturbations” option is not suitable for ABL flows due to the high levels of turbulence at stake, whereas  
 249 the synthetic turbulence generator method will be investigated at a later stage.

250 The spectral synthesizer method is based on the random flow generation technique developed by Kraich-  
 251 nan (1970) and later modified by Smirnov et al. (2001). This method produces fluctuating velocity compo-  
 252 nents. They are computed from the summation of 100 Fourier harmonics and the result is a divergence-free  
 253 velocity field (ANSYS, 2019). The implementation of the vortex method in ANSYS Fluent v19 derives from  
 254 the work of Sergent (2002). Vortices are injected through the inlet plane and advected into the domain.

255 Figures 5a and 5c present the differences between both these methods in terms of the vortices distribution  
 256 on the inlet face and their vorticity magnitude. Monitoring this quantity in a plane that goes throughout the  
 257 domain, one can see that the spectral synthesizer shows an important decrease streamwise that the vortex  
 258 method seems to somewhat overcome (figures 5b and 5d).

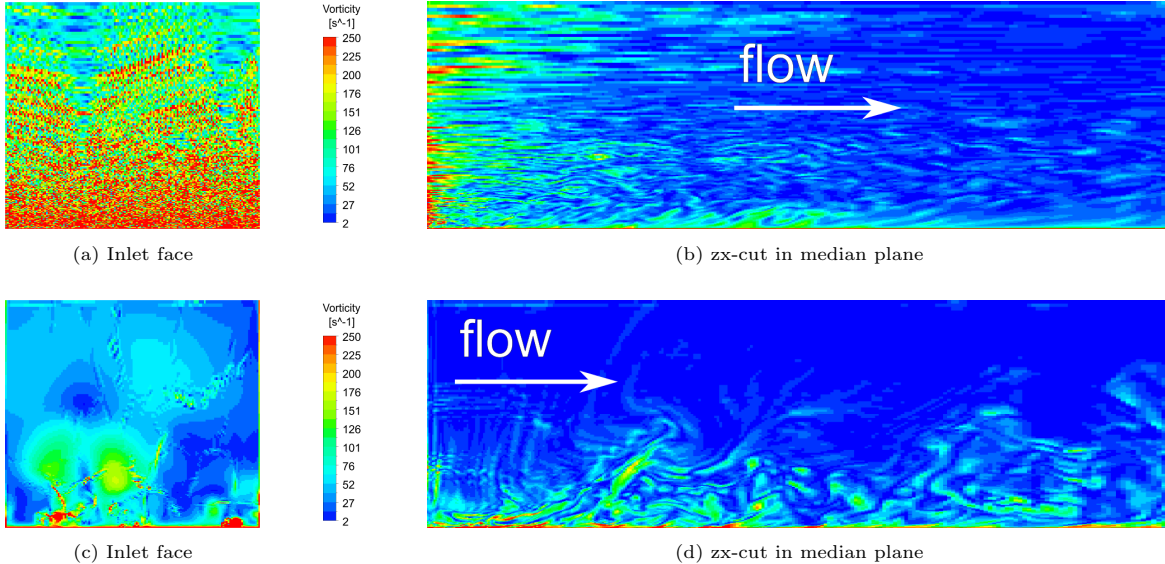


Figure 5: Vorticity magnitude contours with (a,b) illustrating the spectral synthesizer and (c,d) illustrating the vortex method

259 The vortical structures are displayed in Figure 6 using the iso-surfaces of the Q-criterion, which is defined  
 260 as  $\frac{1}{2}(\Omega^2 - S^2)$  with  $\Omega$  being the vorticity magnitude and  $S$  being the strain rate magnitude. This criterion  
 261 delineates flow regions where the vorticity magnitude is greater than the magnitude of the rate of strain.  
 262 As can be seen on Figure 6, there is a great difference in the turbulence kinetic energy level carried by the  
 263 vortices generated at the inlet and the value specified as a boundary condition ( $k = 2.81 \text{ m}^2/\text{s}^2$  from Equation  
 264 6). Such a discrepancy could be corrected by using a turbulent kinetic energy profile at the inlet boundary  
 265 as proposed by Gorré et al. (2010) and Lauriks et al. (2021). This will be done in future work as it is more  
 266 realistic for ABL flows. Downstream of the inlet, the turbulent kinetic energy of the vortical structures  
 267 globally increases as they travel into the domain and interact with one another. The vortices generated by  
 268 the spectral synthesizer expand in a streamwise direction which is not realistic within a non-uniform velocity  
 269 profile. Moreover, most of the turbulent structures start to dissipate after the first third of the domain. It  
 270 has therefore been decided to set aside the spectral synthesizer method and pursue with the vortex method  
 271 regarding the inlet boundary condition of both the CFD models to follow. The vortex method also features  
 272 streamwise velocity fluctuations with a simplified linear kinematic model based on the vorticity field derived  
 273 at the inlet boundary. The size of each vortex derives from a turbulent mixing length hypothesis and the  
 274 known mean profiles of the turbulent kinetic energy and dissipation rate (Mathey et al., 2006).

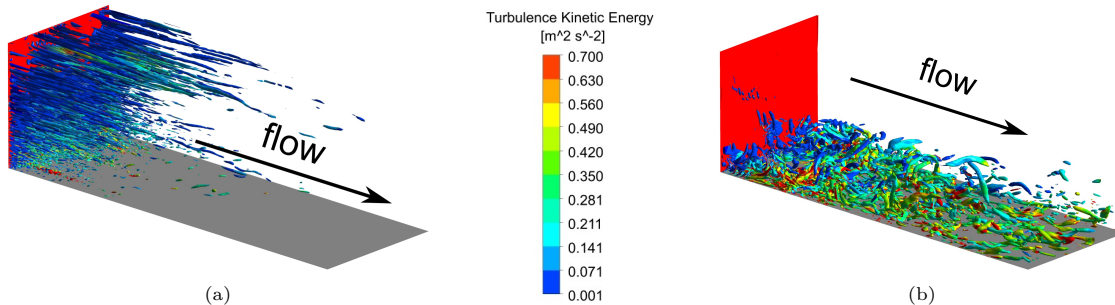


Figure 6: Iso-surface of Q-criterion ( $2,000 \text{ s}^{-2}$ ) coloured by the turbulence kinetic energy with (a) the spectral synthesizer and (b) the vortex method

#### 275 2.2.4. Longitudinal turbulence power spectrum

276 With transient simulations, it becomes possible to observe the frequency content of the velocity fluctu-  
 277 ations and verify that the energy injected into the flow is in accordance with what has been observed in  
 278 the experiment and in full-scale measurements. This is done through the visualisation of the PSD of the

279 velocity fluctuations. Several models have been developed in the past century for the ABL's PSD and one  
 280 can find the expressions presented hereafter in Balendra et al. (2002) for equations 9 and 12 and in Simiu and  
 281 Scanlan (1996) for equations 10, 11 and 13. Most often, the reduced spectrum of the longitudinal velocity  
 282 fluctuations is considered and plotted against the Monin coordinate  $f = nz/U(z)$ ,  $n$  being the frequency.  
 283 In Equation 9, the longitudinal turbulence integral length scale,  $L_u^x$ , represents the size of the eddies in  
 284 the streamwise direction. Peterka et al. (1986) compared their spectrum against one developed by Harris  
 285 through full-scale measurements. They presented it in the form of a normalised spectrum plotted against  
 286 a normalised frequency as it incorporates the variations of a spectrum due to differences in measurement  
 287 height and/or velocity.

$$\text{von Kármán : } \frac{nS_u(z, n)}{u_*^2} = \frac{4 \frac{nL_u^x}{U}}{\left[1 + 70.8 \left(\frac{nL_u^x}{U}\right)^2\right]^{5/6}} \quad (9)$$

$$\text{Davenport : } \frac{nS_u(z, n)}{u_*^2} = 4.0 \frac{x^2}{(1 + x^2)^{4/3}} \quad \text{where } x = \frac{1200n}{U(10)} \quad (10)$$

$$\text{Harris : } \frac{nS_u(n)}{u_*^2} = 4.0 \frac{x}{(2 + x^2)^{5/6}} \quad \text{where } x = \frac{1800n}{U(10)} \quad (11)$$

$$\text{Kaimal : } \frac{nS_u(z, n)}{u_*^2} = \frac{100f}{3(1 + 50f)^{5/3}} \quad (12)$$

$$\text{Simiu : } \frac{nS_u(z, n)}{u_*^2} = \frac{200f}{(1 + 50f)^{5/3}} \quad (13)$$

## 288 2.3. Numerical method

### 289 2.3.1. Geometry and boundary conditions

290 For both an empty wind tunnel and one containing the heliostat model, the computational domain  
 291 expands to 6 m in the streamwise direction ( $x$  ranges from 0 to 6 m) and the cross-section is  $2.05 \times 1.83 \text{ m}^2$  ( $z$   
 292 ranges from 0 to 1.83 m and  $y$  from -1.025 to 1.025 m). In order to replicate the wind tunnel test of Peterka  
 293 et al. (1986), the side and top walls are set to a zero-shear stress boundary condition. This has the effect  
 294 of nullifying the normal velocity gradient at the boundary, forcing the flow in a streamwise direction. To  
 295 address the decay of the inlet profiles noticed in previous work (Poulain et al., 2016a), a retarding shear  
 296 stress of  $\tau_w = \rho u_*^2$  is applied on the ground wall for the precursor RANS simulation (Figure 7). The exit  
 297 of the domain is given a pressure outlet boundary condition. The researchers will subsequently present a  
 298 CFD model of an isolated heliostat with no thickness in upright orientation. As shown on Figure 7, the  
 299 heliostat geometry used is highly similar to the one tested by Peterka et al. (1986). The three panels have  
 300 equal dimensions and are spaced with a 5 mm gap. The diameters of both the pylon and the torque tube  
 301 have not been reported and have been made 3 mm. The torque tube length of the experimental heliostat  
 302 model seems to be slightly greater than the total width of the heliostat. However, this should only have a  
 303 negligible impact on the flow distribution, if any. Another unknown dimension is the distance between the  
 304 reflective area and the torque tube which is set to 3 mm in the CFD model.

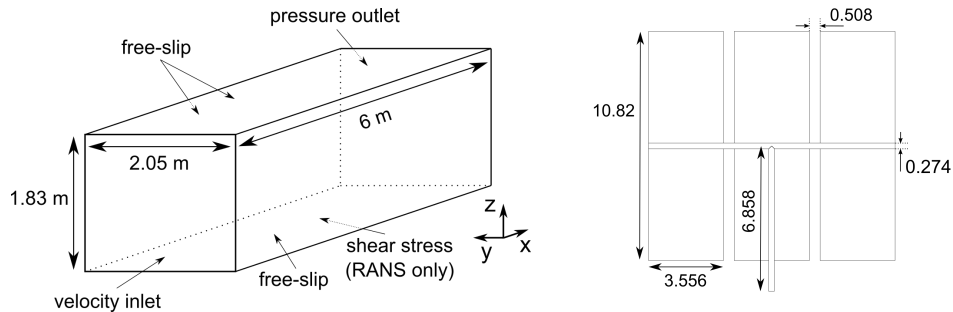


Figure 7: Computational domain and heliostat model (dimensions in cm)

305 2.3.2. Mesh

306 The empty domain has been meshed with 6.2 million hexahedrons, which form a structured grid. Our  
307 second model containing the heliostat in upright orientation has a grid that is mostly structured with 23.4  
308 million cells. Only the vicinity of the hinge has been meshed with tetrahedrons. The mesh count could  
309 have been sensibly higher if the researchers had modelled the heliostat thickness. Not reported in Peterka  
310 et al. (1986), the latter is 3 mm in Peterka et al. (1987b). For instance, using five cells across the heliostat  
311 thickness to model the flow separation that occurs would make a cell length of 0.6 mm in this area. Choosing  
312 a smaller mesh size here would inevitably reverberate on the rest of the grid which would greatly increase  
313 the total mesh count. This highlights the challenge of achieving a good mesh resolution with a minimal  
314 computational time. The mesh becomes finer around all the edges of the heliostat so that it can capture  
315 the vortex shedding phenomenon and feature the shear layer with a high definition (Figure 8). The refined  
316 sections in the middle of a panel are due to the presence of the torque tube or the pylon. Regarding the  
317 wall treatment in ANSYS Fluent v19, the turbulence models based on the specific dissipation rate,  $\omega$ , are  
318 independent of the near-wall  $y^+$  resolution. More specifically, it is done by blending the viscous sublayer  
319 and the logarithmic layer formulations based on the  $y^+$ . Being derived from the  $k - \omega$  turbulence model,  
320 the SAS model features this versatility. With the help of mesh interfaces, several levels of coarsening occur  
321 in the three directions of the grid (Figure 9). At every mesh interface, for three cell edges on the fine side  
322 there are two corresponding cell edges on the coarse side. Nonetheless, there is no mesh interface in the wake  
323 region in order to avoid numerical artefacts within this area. Contrary to the isolated heliostat model, the  
324 empty wind tunnel model has been carried out with the use of a conformal mesh.

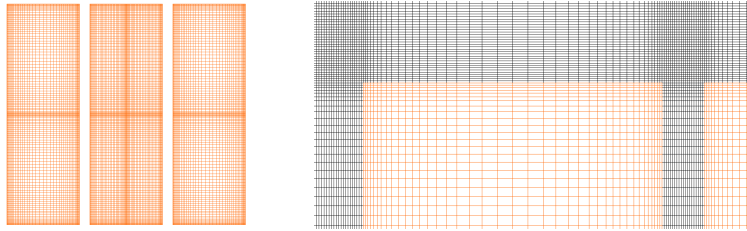


Figure 8: Surface mesh of the heliostat panels (orange) and around (black)

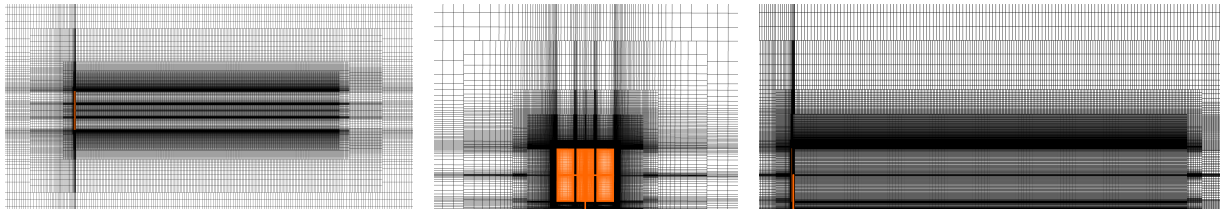


Figure 9: Mesh interfaces in planes xy (left), yz (centre) and zx (right)

325 2.3.3. Grid convergence study

326 For the meshing of the heliostat CFD model, the focus was on the gaps and the torque tube and pylon  
327 diameter as they have smaller dimensions. Three different meshes have been used for a RANS simulation  
328 with the realizable  $k - \epsilon$  model. The coarsest one was composed of 3.3 million cells. The second and third  
329 meshes resulted from the refinement of the former by a factor of 2.6 in the three directions to obtain 8.6 and  
330 then 22.3 million cells. The drag force exerted on the collector computed by CFD simulations on these meshes  
331 was compared with the result given by the fine grid (Figure 10). Through calculations of grid convergence  
332 indices with a safety factor of 1.25 and the order of convergence for the drag force, the researchers verified  
333 that they were in the range of asymptotic convergence as they obtained a factor of 0.974, thus ensuring mesh  
334 independence.

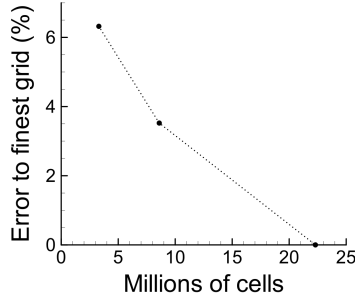


Figure 10: Comparison of the error between the coarser grids and the finest grid on the drag force computed with CFD RANS simulations

### 2.3.4. Mesh size assessment

Performing a precursor steady-state RANS simulation before switching to a transient SRS model is strongly recommended (Gerasimov, 2016). Not only will it give a proper initial state of the flow when switching to the transient mode, but it will also provide information about the relative fineness of the mesh as required when using an SRS model. This has been done for both the CFD models. It is advised to resolve 80% of the turbulence content in order to obtain a solution that is accurate enough (Pope, 2000). This means that the domain should be meshed so as to have approximately five cells across the integral length scale of turbulence,  $L_t$ , computed from the following equation (Gerasimov, 2016):

$$L_t = \frac{k^{\frac{3}{2}}}{\epsilon} \quad (14)$$

With  $\Delta$  the mesh size as defined in Equation 4, displaying the contours of the ratio  $L_t/\Delta$  with the range clipped from 0 to 5 highlights whether and where the mesh needs to be refined. For the empty wind tunnel model, except for the near-wall area, part of the viscous sublayer, the mesh was fine enough as it abides by the requirement of five cells across the integral length scale of turbulence. Regarding the heliostat model, a few zones would need to be refined. On Figure 11, one can see the iso-surface of 5 for the ratio  $L_t/\Delta$ . This iso-surface encapsulates regions of even lower values. Similar to the empty wind tunnel model, the heliostat near-wall area features small length scales for the dissipation of turbulence. The flow separation induced by the pylon in the clearance gap presents a low resolution, as does the whole region located a few centimetres behind the heliostat gaps. This is due to the interaction of the wake with the air flowing through the clearance gap and the proximity of the model. This combination causes a high dissipation rate in this region. However, with the shear layer generated by the edges around the model being the dominant factor for the drag force caused on the collector, the choice was made to perform the transient simulation with this mesh.

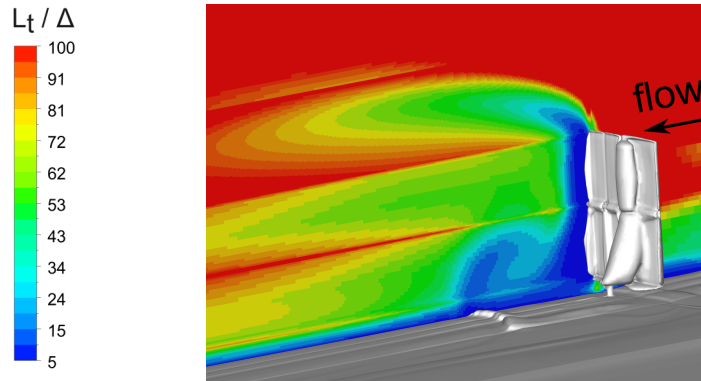


Figure 11: Iso-surface of  $L_t/\Delta = 5$  (grey) and contours of this ratio on a  $zx$ -plane going through the centre of a gap



### 366 2.3.5. Time step

367 One can also assess an appropriate time step size,  $\Delta t$ , for the transient simulation. Ideally, one tries to  
 368 keep the Courant number,  $Co$ , below 1 in order to satisfy the Courant-Friedrichs-Lewy condition. Hence the  
 369 creation of the following custom field function, where  $U$  is the local velocity magnitude given by the RANS  
 360 precursor simulation:

$$\Delta t = \frac{Co \Delta}{U} \quad \text{with} \quad Co = 1 \quad (15)$$

361 For the empty wind tunnel configuration, the researchers obtained a minimum value of  $1.5 \times 10^{-4}$  s in the  
 362 whole computational domain and conservatively chose a time step of  $\Delta t = 10^{-4}$  s for the transient simulation.  
 363 With the presence of the heliostat model, the grid becomes much finer, therefore this minimum value drops to  
 364  $1.2 \times 10^{-5}$  s. It has been decided not to set a lower time step size than the former requirement and to keep the  
 365 same value for the heliostat model simulation in order to avoid a large increase of the total computation time.  
 366 This is acceptable given that an iterative implicit scheme is used for time discretisation (bounded-second  
 367 order). Moreover, the areas that require a smaller time step are located where the turbulence will mostly be  
 368 modelled (Figure 12). The model and wake nearby regions also depict a lower time step requirement due to  
 369 a fine mesh within a free-stream velocity zone.

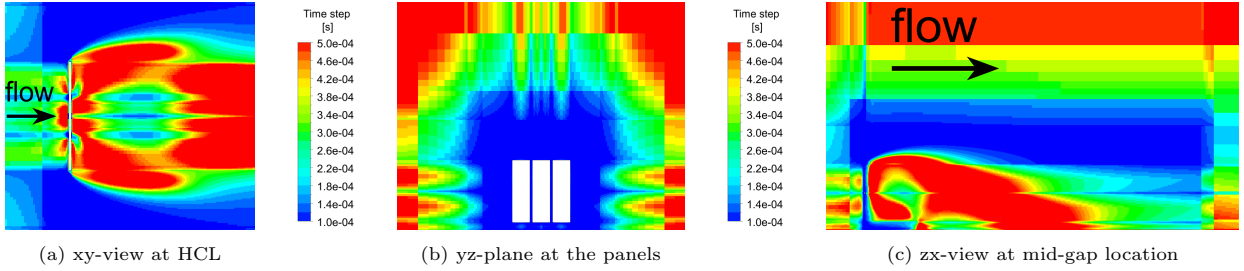


Figure 12: Contours of the time step estimation around the heliostat model and in its wake

## 370 3. Results

### 371 3.1. Empty wind tunnel

#### 372 3.1.1. Solution convergence

373 The empty wind tunnel model simulated 5 seconds of flow time in about 26 hours (including the time  
 374 for data export) at a Centre for High Performance Computing (CHPC), using 10 nodes (Intel Xeon E5-2690  
 375 v3, 2.60 GHz) of 24 cores each. A brief run of the delayed DES turbulence model on the same grid has  
 376 shown to be 35% slower. The monitoring of the solution convergence was done from data collection at  
 377 point surfaces created at  $z = \text{HCL}$  for several streamwise locations. The three components of the velocity  
 378 vector were exported at every time step and statistics were computed. Using the Reynolds decomposition,  
 379 the fluctuating velocity components can be determined by subtracting the velocities time-average from their  
 380 signal (Equation 16). The longitudinal turbulence intensity,  $I_x$ , is calculated from the standard deviation of  
 381 the longitudinal fluctuating velocity (Equation 17). The longitudinal turbulence power spectrum,  $S_u(n)$ , was  
 382 derived from the magnitude squared of the Fast Fourier Transform of the longitudinal fluctuating velocity.

$$U_{x,y,z}(t) = \overline{U_{x,y,z}} + u'_{x,y,z}(t) \quad (16)$$

$$I_x = \frac{\sigma_{u'_x}}{\overline{U}} \quad (17)$$

383 Van der Hoven (1957) made a power spectrum analysis of the longitudinal wind speed. The higher  
 384 frequencies peak, caused by the turbulence within the ABL (Cook, 1986), covers a period between 5 s and  
 385 5 min (Vásquez-Arango et al., 2017) and reaches its maximum for a period of about 72 s. In other words,  
 386 this is the period at which the most energy-containing structures occur. Regarding the CFD model, there  
 387 could be some uncertainty as to whether or when convergence has been reached. Although one may consider

388 the longitudinal velocity time average to be converged from 50 s of the simulated time, the longitudinal  
 389 turbulence intensity keeps increasing for the monitor point placed at  $x = 1$  m and keeps decreasing for all  
 390 the other monitor points (Figure 13). The steep increase that occurs at the inlet 70 s into the simulation  
 391 (Figure 13b) is due to the generation of a vortex near the monitor point. Another method for convergence  
 392 considerations could be the monitoring of a spatial average made in the spanwise direction, in other words  
 393 for a given streamwise location and height, averaging all the values in the lateral direction. By construction,  
 394 the fluctuating components of the velocity should have a time average of 0 m/s (Figure 14a). This is however  
 395 practically impossible and a tolerance has to apply. An idea would be to evaluate the absolute value of the  
 396 ratio  $|\overline{u'_x}/\overline{U_x}|$ . In this case, this ratio drops below 1% after 70 s of simulated time and below 0.1% slightly  
 397 before 150 s (Figure 14b).

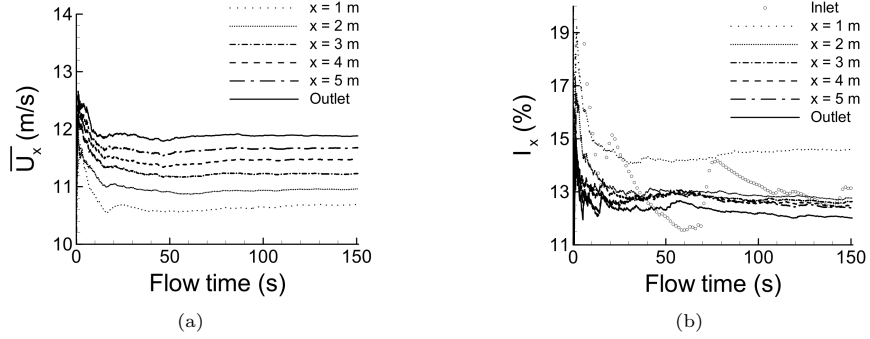


Figure 13: Evolution of (a) the longitudinal velocity time average and (b) the longitudinal turbulence intensity at  $z = \text{HCL}$  for the seven 1 m-spaced monitor points

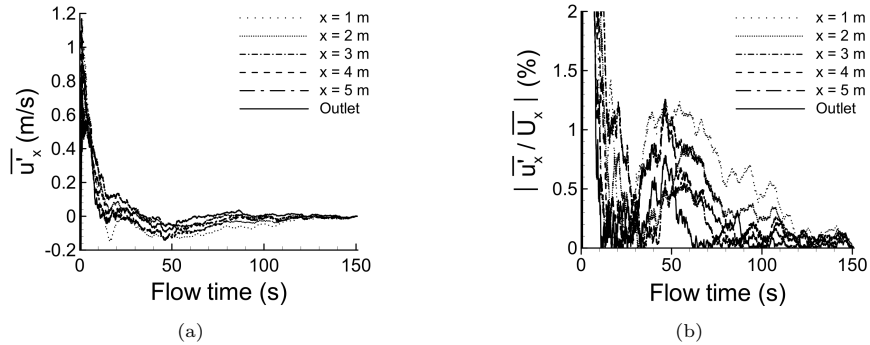


Figure 14: Evolution of (a) the longitudinal fluctuating velocity time average and (b) its ratio with the longitudinal velocity time average at  $z = \text{HCL}$  for several streamwise locations

### 3.1.2. Profiles and longitudinal turbulence power spectrum

398 As the flow travels through the domain, there is a decrease of the turbulence intensity at HCL from 2 m  
 399 onwards conjugated to an increase of the longitudinal velocity time average (Figure 15). One can see that  
 400 this occurs over the whole profile for both quantities (figures 16 and 17). The sudden rise taking place in the  
 401 turbulence intensity profile between  $Z/Z_{ref} = 0.2$  and  $Z/Z_{ref} = 0.5$  for  $x = 1$  m and  $x = 2$  m results from  
 402 vortices generated at the inlet about these heights but dissipated under the mean flow characteristics. As  
 403 the turbulence intensity is a driving parameter for heliostat wind loading (Peterka et al., 1987b), it has been  
 404 decided to place the heliostat model 1.5 m away from the inlet boundary, allowing for the development of the  
 405 vortical structures generated by the vortex method, while remaining close to the experimental turbulence  
 406 intensity value at HCL (14%). Another possibility would be to generate profiles with a higher turbulence  
 407 intensity than the experimental targeted value in order to account for the decay. The model could then  
 408 be placed about 4 m from the inlet, in the area where the turbulence intensity profile is nearly horizontally  
 409 homogeneous. However, this would mean extending the domain size, which would lead to an increase in  
 410 computational time. In this study, because  $Z_{HCL}/Z_{ref} = 0.0604$ , the heliostat model will not experience  
 411

412 the aforementioned sudden rise in turbulence intensity. As evoked in 2.2.3, it would be of interest to see the  
 413 evolution of the turbulence characteristics and profiles with a turbulent kinetic energy varying with height  
 414 at the inlet.

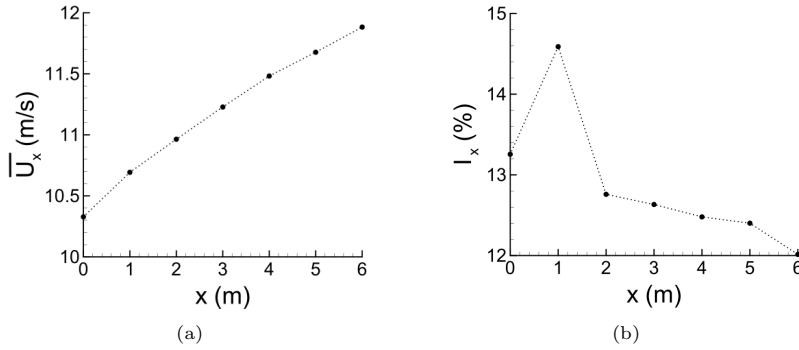


Figure 15: Streamwise evolution at  $z = \text{HCL}$  of (a) the longitudinal velocity and (b) the longitudinal turbulence intensity

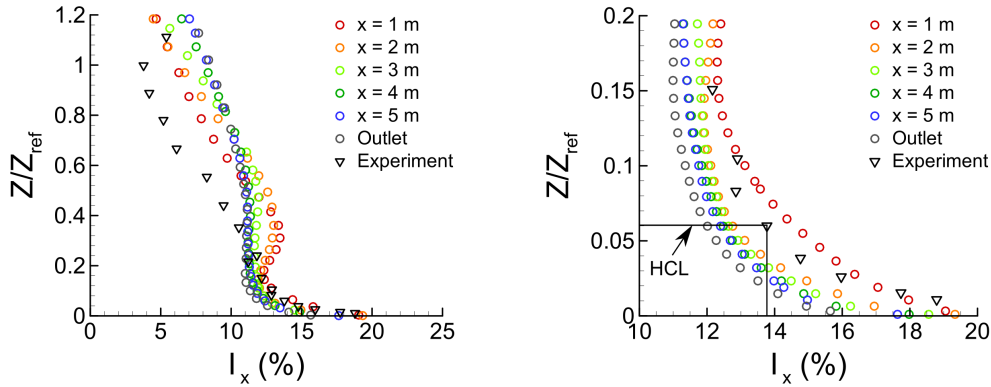


Figure 16: Streamwise evolution of the turbulence intensity profile versus experiment (Peterka et al., 1986), global (left) and zoomed view (right)

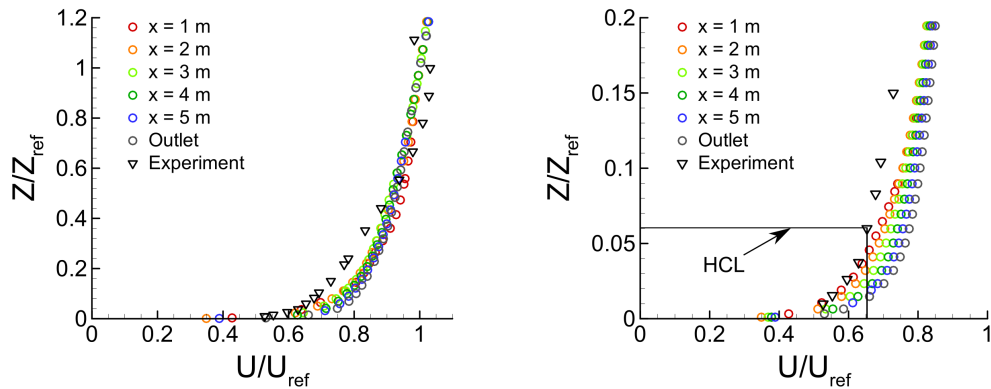


Figure 17: Mean velocity profile at several streamwise locations versus experiment (Peterka et al., 1986), global (left) and zoomed view (right)

415 The spanwise variations of the mean longitudinal velocity and longitudinal turbulence intensity have been  
 416 investigated with the computation of the variables presented in Equation 18. The values of  $y = \pm 0.05842 \text{ m}$   
 417 correspond to the lateral coordinates of the edges of the heliostat model. The profiles at the locations  $x = 1$

418 and 2 m have been exported. Although the previous graphs showed a decay of the inlet profiles, lateral  
 419 homogeneity is achieved with a deviation relative to the centreline values that is between  $\pm 1\%$  for the mean  
 420 longitudinal velocity and between  $\pm 5\%$  for the longitudinal turbulence intensity (Figure 18).

$$\frac{\overline{U_x(x, y, z)} - \overline{U_x(x, 0, z)}}{\overline{U_x(x, 0, z)}} \quad \text{and} \quad \frac{I_x(x, y, z) - I_x(x, 0, z)}{I_x(x, 0, z)} \quad (18)$$

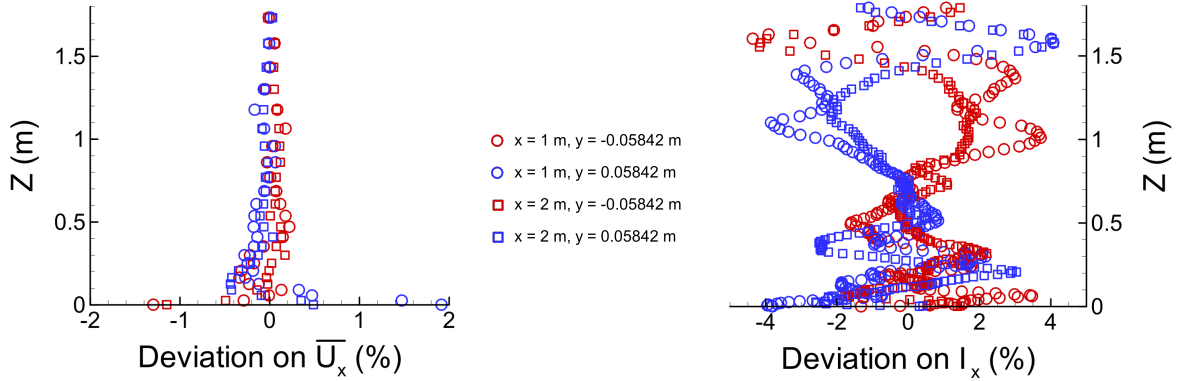


Figure 18: Deviation of the mean longitudinal velocity (left) and the longitudinal turbulence intensity (right) profiles relative to the centreline profile ( $y = 0$  m)

421 The longitudinal turbulence power spectrum has been computed for every point surface and compared  
 422 with the experimental one (Figure 19). In the lower frequency range ( $f$  roughly between 0.001 and 0.03), the  
 423 further downstream the monitor point is located, the bigger the eddies. However, this trend reverses past the  
 424 frequency for which the amplitude is maximum meaning that vortices of a given size occur more frequently  
 425 as one travels upstream. Various total sampled times have been explored to determine the minimum required  
 426 time of the simulation for a converged solution. The simulation has been stopped after 150s of flow time  
 427 has been modelled. For total sampled times of 20 and 30s, although one can see an overprediction of the  
 428 turbulent length scales of the eddies in the lower frequency range, for frequencies greater than 0.01 there is  
 429 no major difference in comparison with the longitudinal turbulence spectrum when the total sampled time  
 430 matches the total duration of the simulation (Figure 20).

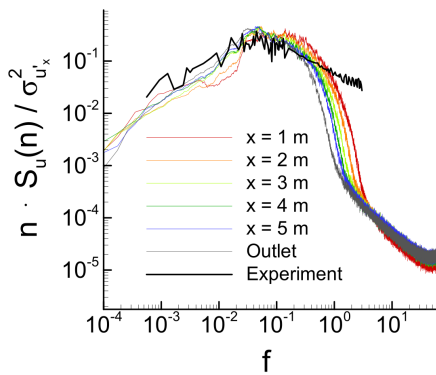


Figure 19: Streamwise evolution of the longitudinal turbulence spectrum at HCL versus experiment (Peterka et al., 1986)

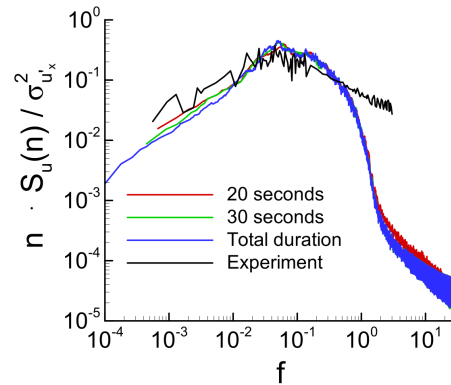


Figure 20: Variations of the longitudinal turbulence spectrum with the total sampled time at HCL for  $x = 3$  m

431 The profile of the longitudinal integral length scale of turbulence,  $L_u^x$ , has been computed for the seven  
 432 streamwise locations (Figure 21) by integrating the autocorrelation function of the longitudinal fluctuating  
 433 velocity over the total sampled time. One can see that the vortices generated at the inlet are not fully  
 434 developed within the first half of the domain. The integral length scale of the experiment was reported

435 as being “four times larger than the characteristic length of the heliostat model” (Peterka et al., 1986).  
 436 Based on the heliostat chord length, this leads to a value of 0.4328 m. In this regard, placing the model  
 437 1.5 m downstream of the inlet boundary might not be appropriate and a distance of 5 m could have been  
 438 considered (Figure 22). This is in line with the longitudinal turbulence spectrum being better approximated  
 439 in the frequency range around the peak (Figure 19). A linear interpolation gives a value of 0.2575 m at  
 440  $x = 1.5$  m which makes an error of 40.5 % with the experimental value aforementioned.

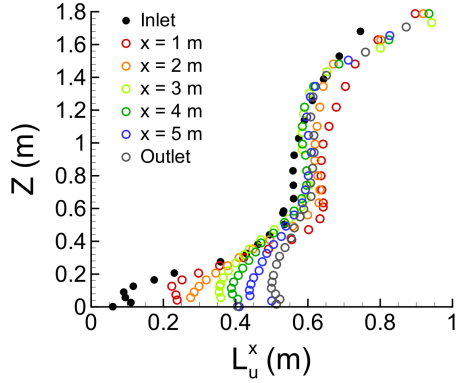


Figure 21: Streamwise evolution of the longitudinal turbulent integral length scale profile at the centreline ( $y = 0$  m)

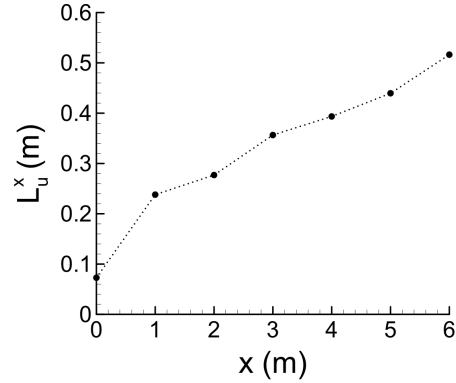


Figure 22: Streamwise evolution at  $z = \text{HCL}$  of the longitudinal integral length scale of turbulence

### 441 3.1.3. Data sampling frequency

442 The large number of time steps required for the convergence of the simulation implied the generation  
 443 of a copious amount of data files, therefore increasing the total computational time, the space disk usage,  
 444 as well as the post-processing time required. For these simulations, datasets were exported at every time  
 445 step, i.e. with a sampling frequency of  $f_s = 10,000$  Hz. However, as depicted in Figure 23, reducing the  
 446 quantity of information collected by a factor of 100 would not have had a negative effect on the results. This  
 447 is important to consider given that exporting data slows down a simulation and also increases the computing  
 448 time during the post-processing step.

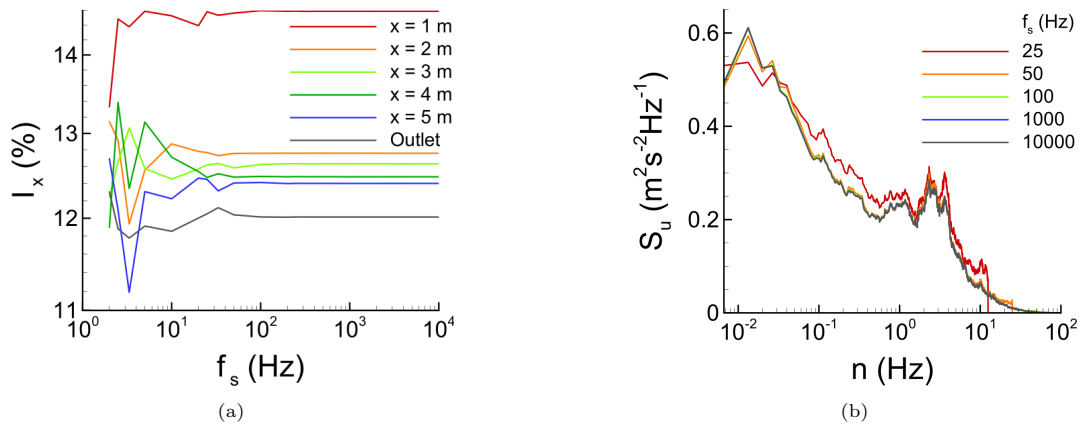


Figure 23: Influence of the sampling frequency on (a) the longitudinal turbulence intensity and (b) the PSD of the longitudinal fluctuating velocity at  $x = 3$  m (both at HCL)

### 449 3.2. Heliostat model

450 In the experiment, the peak loads refer to “the largest and smallest values recorded during a time of [...]”  
 451 32 seconds model scale” Peterka et al. (1986). As it was unsure how much simulation time was required  
 452 to achieve statistical convergence, the transient simulations were run at the Centre for High Performance  
 453 Computing (CHPC) in Cape Town, South Africa. **For the empty wind tunnel model, 5 seconds of flow time**

454 could be run in about 17 hours using 10 nodes (Intel Xeon E5-2690 v3, 2.60 GHz) of 24 cores each. Regarding  
 455 the heliostat model, 25 seconds could be simulated within one month using the same resources and a total of  
 456 46 seconds was sampled. In Figure 24, one can see the presence of vortical structures in the incoming flow,  
 457 as well as the vortex-shedding phenomenon caused by the collector. A lower Q-criterion value displays more  
 458 vortices, but a higher one shows the turbulent structures that contain the most energy.

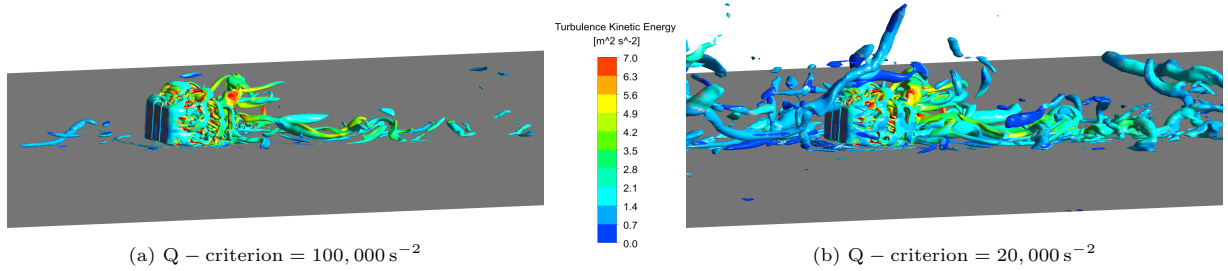


Figure 24: Iso-surfaces of Q-criterion coloured by the turbulence kinetic energy

459 Because of time-averaged velocity variations upstream of the model and the fact that the distance between  
 460 the measuring probe and the heliostat model was not reported in Peterka et al. (1986), it was decided to  
 461 monitor the drag force,  $F_x$ , rather than its non-dimensional coefficient,  $C_{Fx}$  (Equation 19). The peak and  
 462 mean drag forces of the wind tunnel experiment can be deduced based on the reference values. Note that the  
 463 reference area includes the gaps between the panels. Therefore, a drag force coefficient of 1.26 corresponds  
 464 to a force of 1.45 N and the minimum and maximum drag force coefficients measured at 0.60 and 2.56,  
 465 respectively, give a minimum of 0.69 N and a maximum of 2.95 N. A sample of the drag force signal and its  
 466 running time average is depicted in Figure 25 and the results of the CFD simulation are presented in Table  
 467 2. The SAS turbulence model shows that it can accurately predict the mean drag force on the heliostat.  
 468 However, there is a non-negligible imprecision with regard to the peak drag forces, although the accuracy of  
 469 the experiment “was about 5 to 10 percent or better of the maximum value recorded” (Peterka et al., 1986).  
 470 The amplitude of the signal should indeed be greater and this is in line with the lower root-mean-square  
 471 error (RMSE) obtained with the CFD simulation. Nevertheless, an error of about 18% is found for the  
 472 peak values and one can investigate on introducing a safety factor for the peak loads modelled with the SAS  
 473 turbulence model. It is noteworthy that, although the thickness of the collector was not modelled, this did  
 474 not have a negative impact on the mean drag force.

$$F_x = \frac{1}{2} \rho A_{ref} U_{10m}^2 C_{Fx} \quad \text{with} \quad A_{ref} = 126.43 \text{ cm}^2 \quad \text{and} \quad U_{10m} = 12.192 \text{ m/s} \quad (19)$$

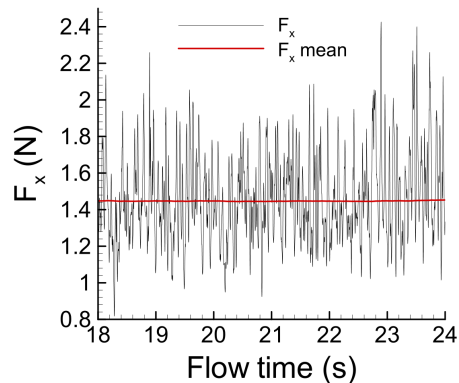


Figure 25: Sample of the evolution of the drag force and its time average

$F_x$ (N)	Mean	RMSE	Min	Max
Peterka et al. (1986)	1.45	0.24	0.69	2.95
CFD	1.4509	0.2251	0.8176	2.4260
Error	0.04 %	5.8 %	18.4 %	17.7 %

Table 2: Results for the drag force from the CFD SAS compared against the experiment

475 The overturning moment at the hinge,  $MH_y$ , has also been modelled. The base moment will, however,  
476 be compared since it also reaches a maximum under the heliostat orientation presented. The combination of  
477 equations 19, 20 and 21 (Peterka et al., 1987b) leads to Equation 22, given that the reference length is equal  
478 to the heliostat chord length. Table 3 shows an error of 8 % for the base overturning moment relatively to  
479 the experiment.

$$MH_y = \frac{1}{2} \rho A_{ref} L_{ref} U_{10m}^2 C_{MH_y} \quad \text{with} \quad L_{ref} = 10.82 \text{ cm} \quad (20)$$

$$C_{M_y} = C_{MH_y} + C_{F_x} \frac{HCL}{c} \quad (21)$$

$$M_y = MH_y + F_x \times HCL \quad (22)$$

	$M_y$ mean (N.m)
Peterka et al. (1986)	0.11
CFD	0.0994
Error	8.1 %

Table 3: Results for the mean base overturning moment from the CFD SAS compared against the experiment

480 One can also question whether the pylon and torque tube have to be represented, given their insignificant  
481 share in the results (Table 4). They may, however, play a role in the flow separation in the clearance gap and  
482 in the pressure distribution on the back of the panels. If this is not verified, excluding both of them from  
483 the geometry would contribute to a gain of time during the meshing step, as well as reduced computational  
484 cost.

Elements	Panels	Torque tube	Pylon	Hinge
Ratio to $F_x$	99.7 %	0.15 %	0.19 %	$4 \times 10^{-5}$ %

Table 4: Contribution of the various heliostat components towards the mean drag force

#### 485 4. Conclusion

486 This study focused on the possibility of modelling an ABL flow with a reasonable computational cost.  
487 It showed the ability of the SAS turbulence model to reproduce an ABL profile **with limited horizontal**  
488 **inhomogeneity**, unlike RANS models applied in their standard form. The modelling of the transient mean  
489 and peak drag forces exerted on a heliostat in an upright orientation was assessed and comparisons were  
490 made with the wind tunnel test of Peterka et al. (1986). Good agreement was found regarding the mean and  
491 the RMSE values. However, the error on the peak drag forces remains in the range of 18 %. This could be  
492 linked to the longitudinal turbulence spectrum being under-predicted in the low frequency range.



493 Another important result is that it does not seem necessary to model the thickness of the heliostat in this  
494 orientation, which has the direct effect of decreasing the computational cost considerably as the mesh size  
495 around the collector would be of the order of 0.1 mm otherwise. However, the modeling of the peak loads for  
496 other orientations, such as the ones that produce a maximum lift force and hinge overturning moment (panels  
497 inclined by  $30^\circ$  relative to the horizontal plane) and a maximum azimuthal moment (upright heliostat, but  
498 turned so as to form a  $65^\circ$  angle with the incoming flow), should be undertaken. The necessity of modelling  
499 the torque tube and the pylon is questioned since their absence would allow for bigger mesh cells in the  
500 related areas.

501 Further work will be done with the SAS turbulence model as it leads to computationally affordable  
502 CFD simulations. However, the horizontal homogeneity issue depicted in this study needs to be adressed.  
503 The focus will be set on the influence of the streamwise domain length on the evolution of the longitudinal  
504 turbulence intensity and power spectrum as well as the integral length scale. The impact of having a turbulent  
505 kinetic energy profile at the inlet boundary will also be investigated in this regard. It could indeed alleviate  
506 the important streamwise variations seen for the various profiles. Finally, the synthetic turbulence generator  
507 will be tested and compared against the vortex method utilised in this study.

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