

# On the combination of gravity field time series derived from kinematic positions of Low Earth Orbiting satellites

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# Introduction

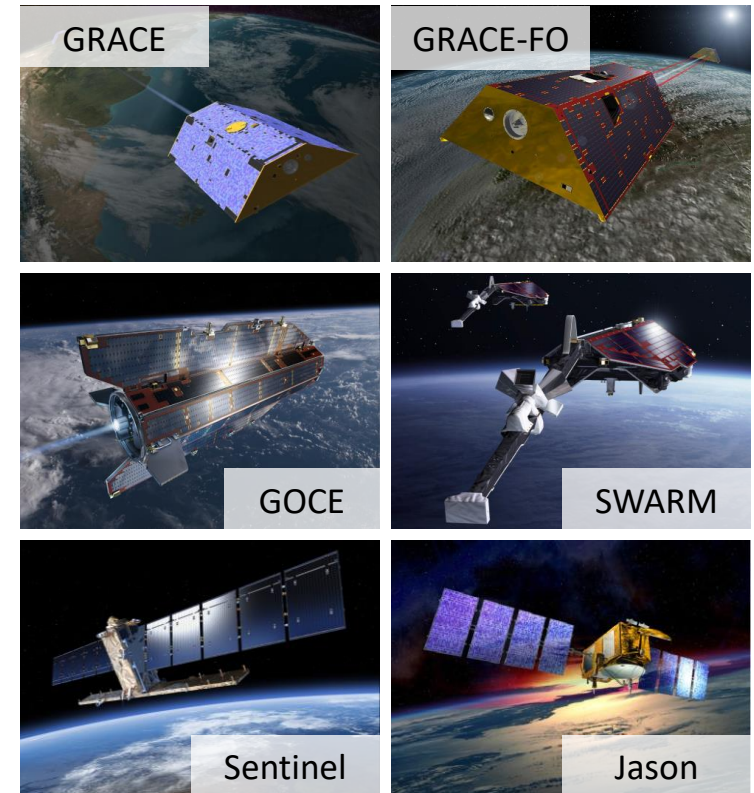
- **Motivation**

- Any Low Earth Orbiting (LEO) satellite with a GPS receiver may serve as a gravity field sensor (in addition to dedicated missions)
- Kinematic LEO positions are used for gravity field recovery in a generalized orbit determination problem

- **Our goal:** Multi-LEO gravity field time series taking advantage of

- Large number of observations
- Complementary orbital configurations

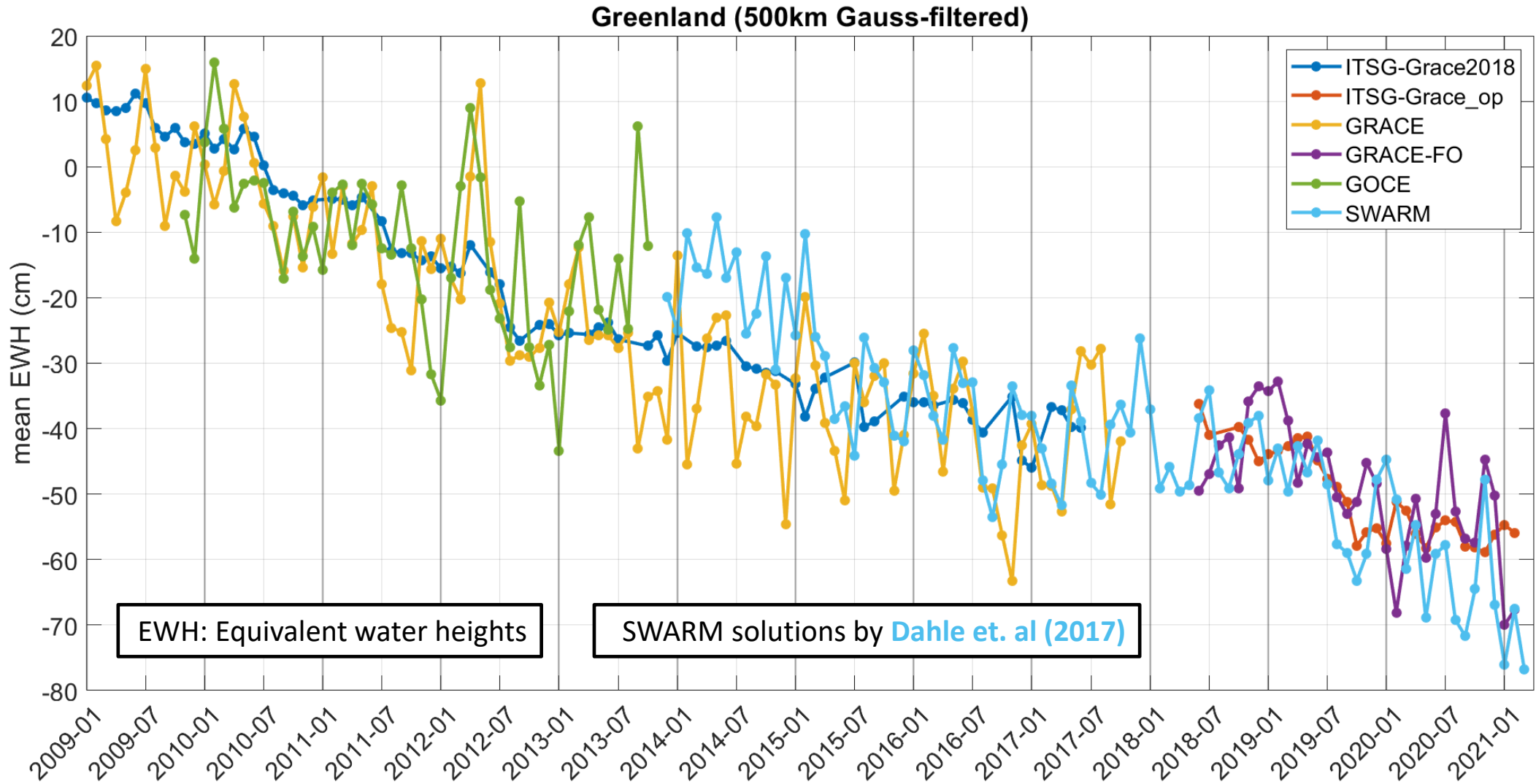
- **Focus here:** Combination of monthly LEO gravity field time series



Source: ESA, NASA

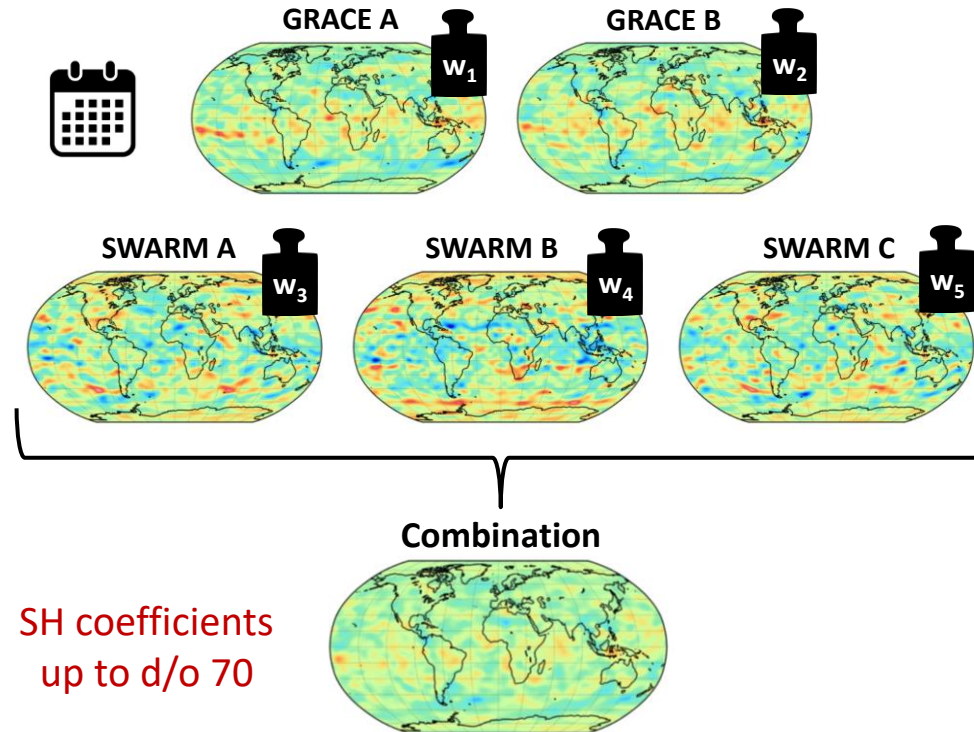
# Overview of LEO gravity field time series

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# Combination of monthly gravity field time series

- Combination strategy on solution level
  - Combination of individual satellite solutions
  - Monthly field-wise weights



- Variance component estimation (VCE)
  - SH coefficients are used as pseudo-observations
  - Field-wise weights (Jean et. al, 2018):

$$w_{i,k} = \left( 1 - \frac{w_{i,k-1}}{\sum_i w_{i,k-1}} \right) \frac{1}{\text{RMS}(\mathbf{x}_i - \hat{\mathbf{x}}_{k-1})^2}$$

$$w_{i,0} = 1/n_{\text{sol}}$$

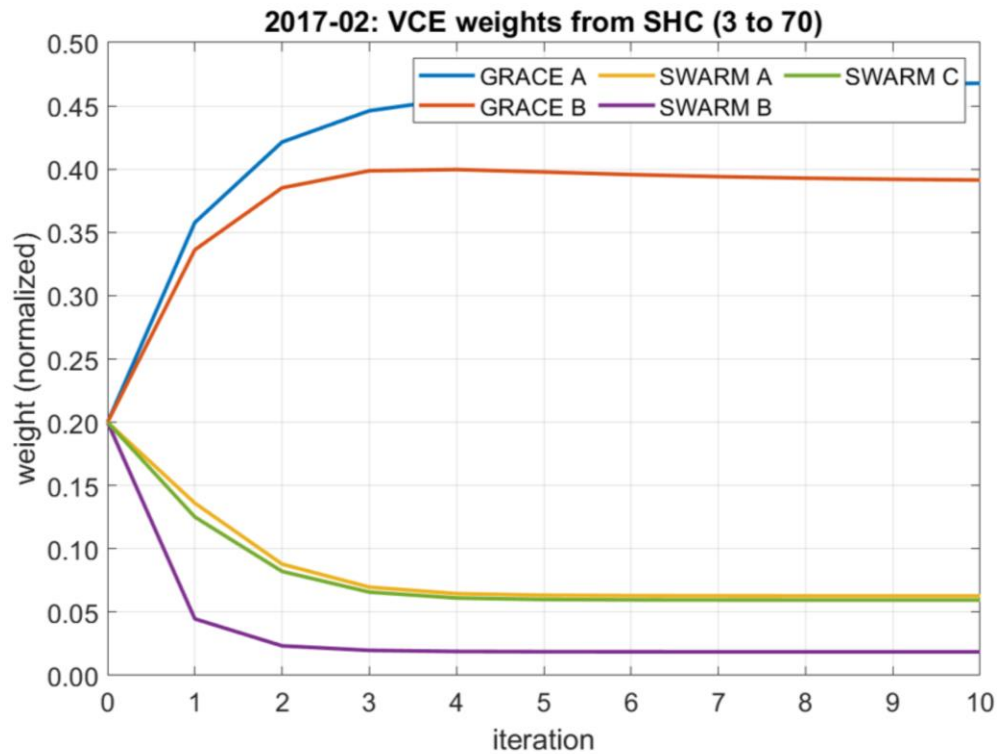
- Combination in iteration step k:

$$\hat{\mathbf{x}}_k = \frac{1}{\sum_i w_{i,k}} \sum_i w_{i,k} \mathbf{x}_i$$

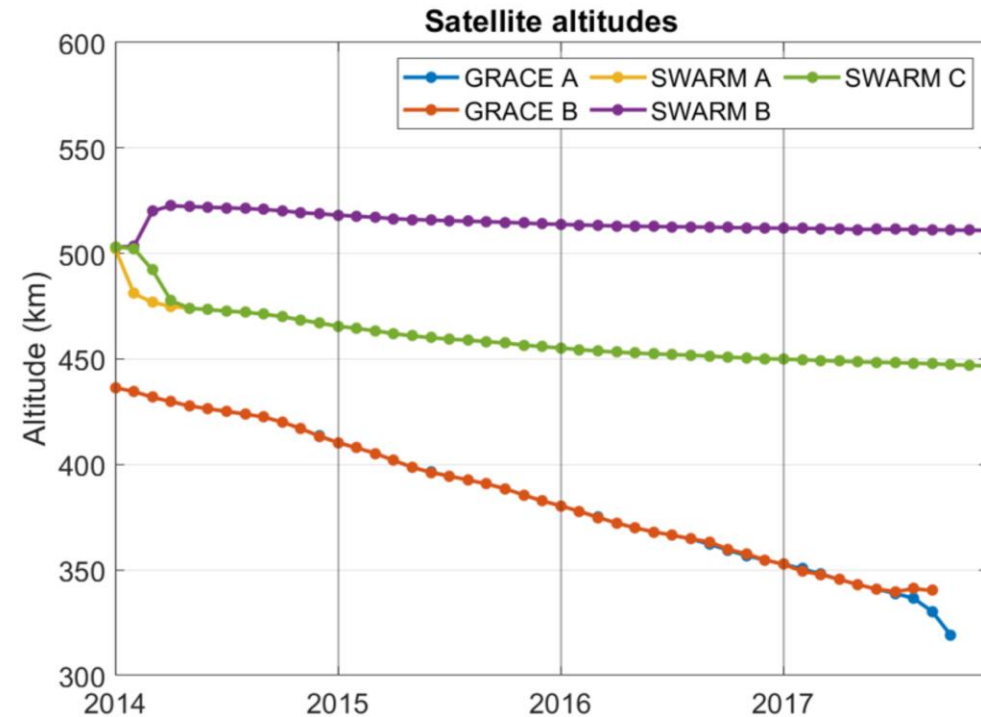
SH coefficients of solution i

# Variance component estimation: GRACE/SWARM

- Weights based on unfiltered SHC



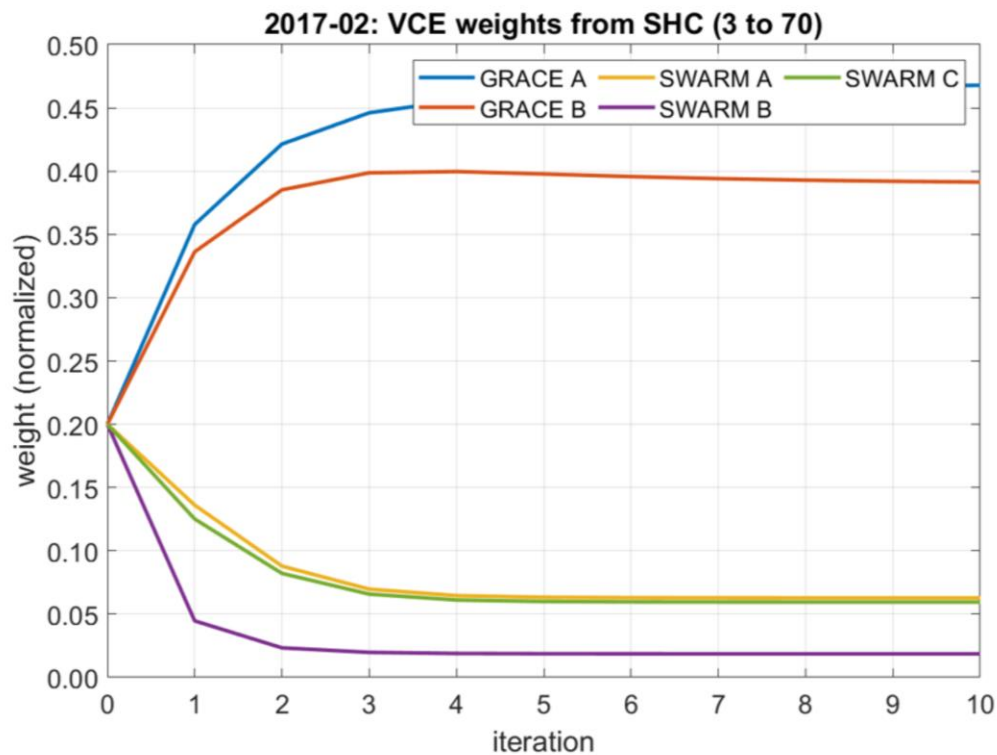
- Satellite altitudes



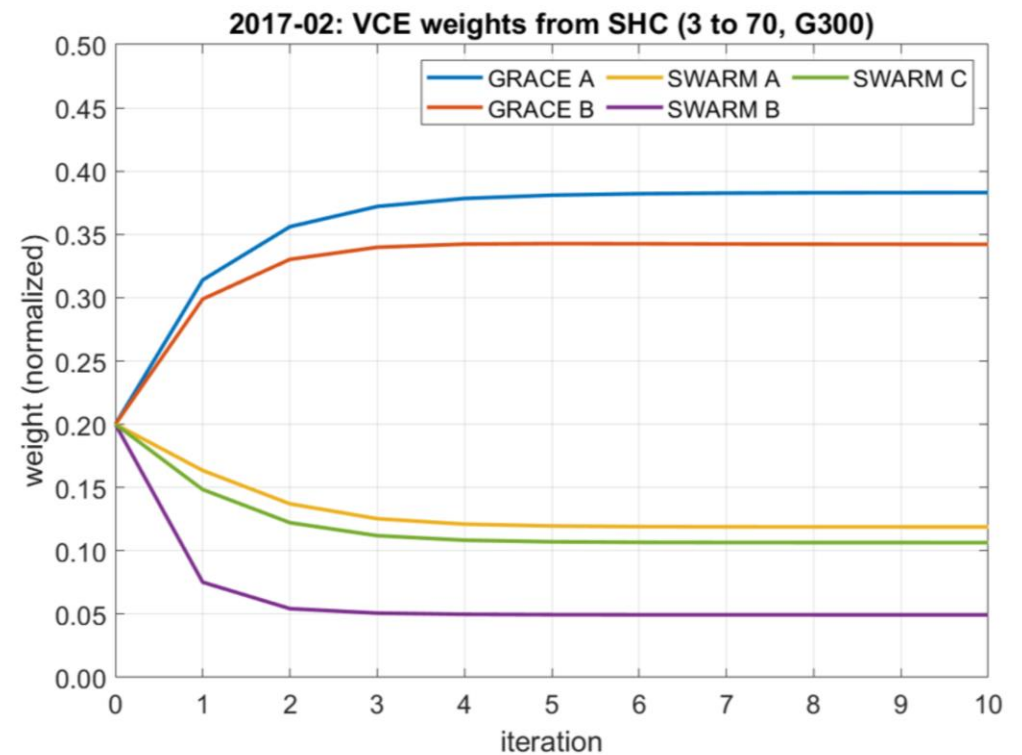
- Weights are dominated by the noise of the high-degree coefficients

# Variance component estimation: GRACE/SWARM

- Weights based on unfiltered SHC

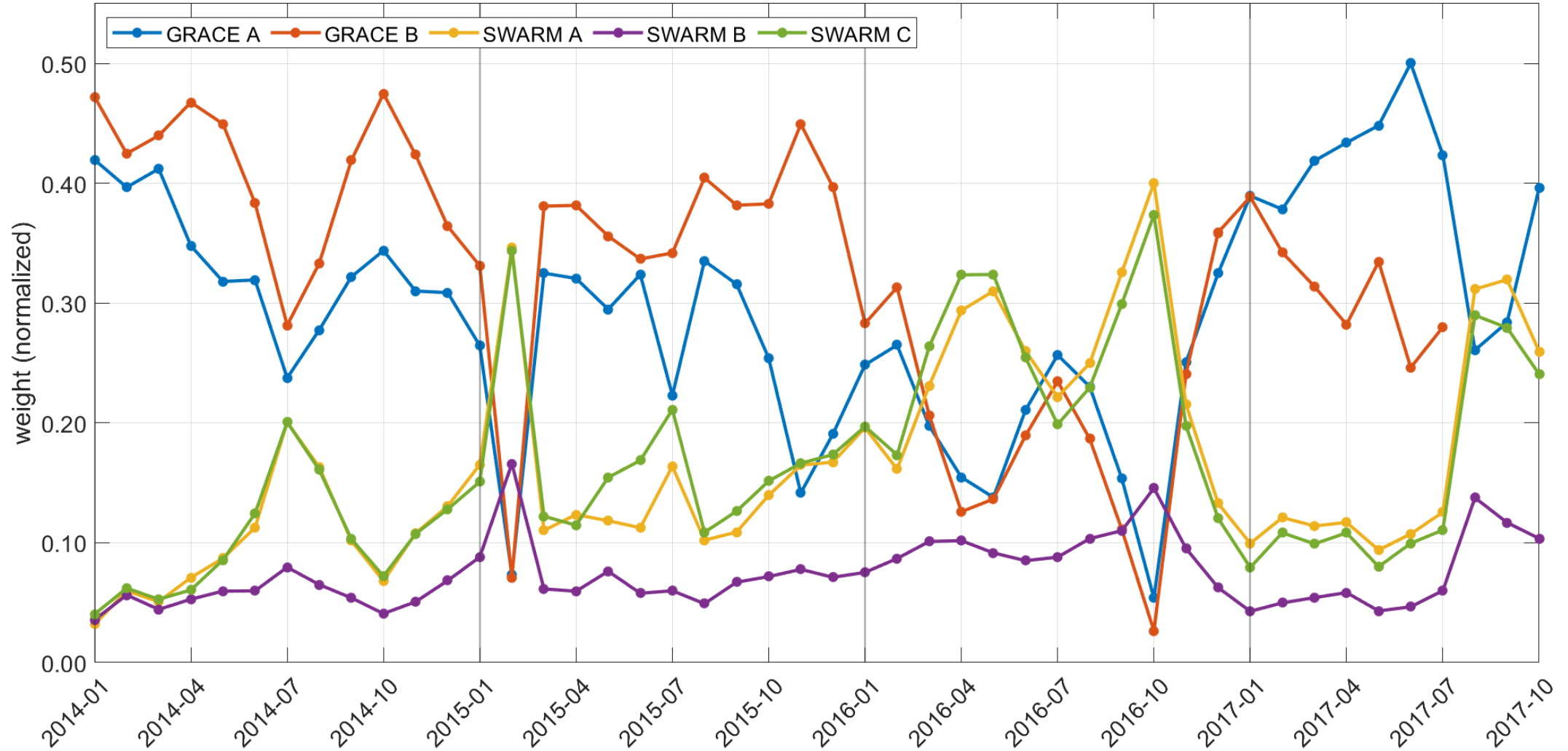


- Weights based on filtered SHC ([here](#): 300km Gauss)



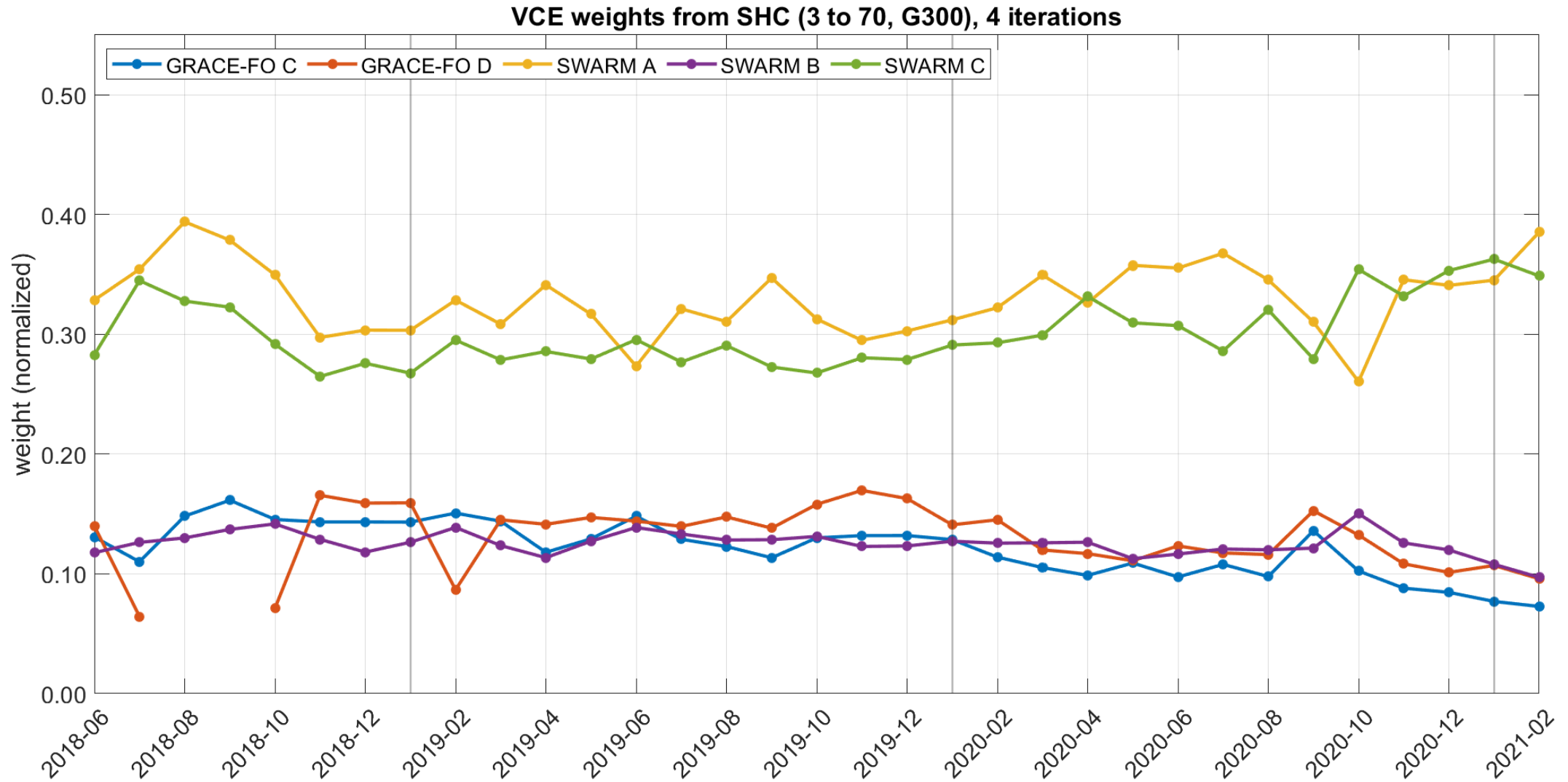
# Variance component estimation: GRACE/SWARM

VCE weights from SHC (3 to 70, G300), 4 iterations



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# Variance component estimation: GRACE-FO/SWARM

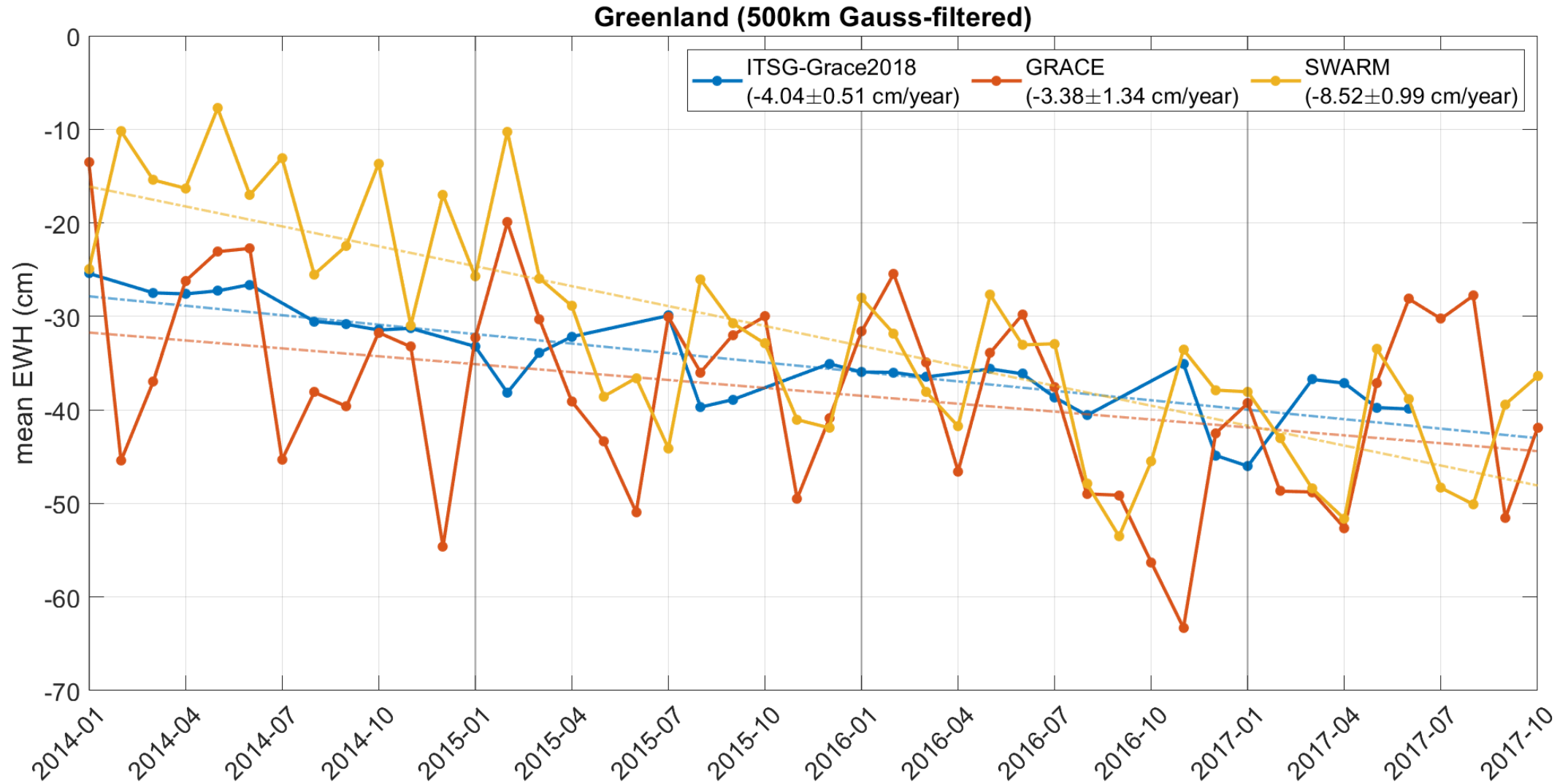


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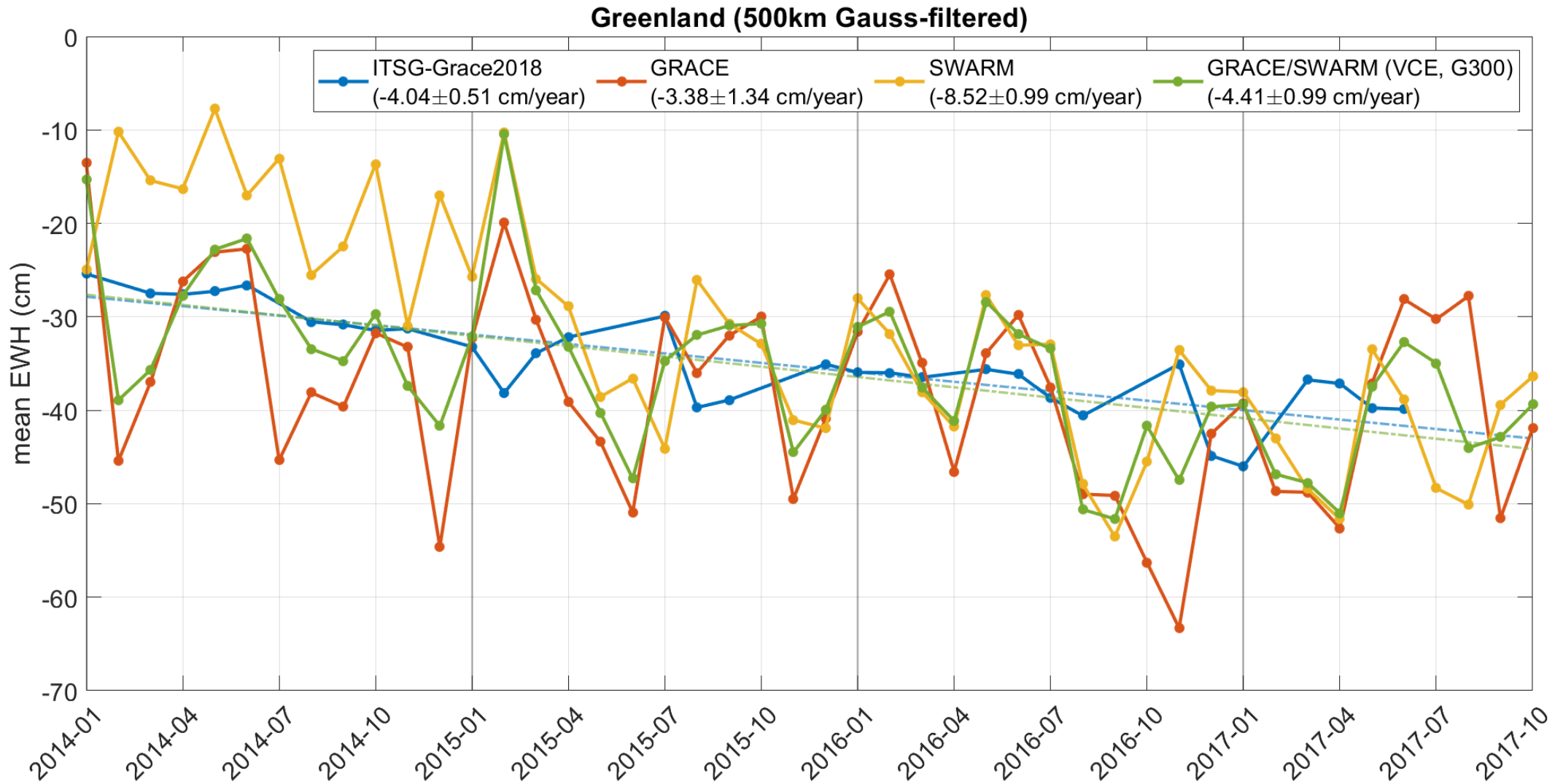


# Evaluation of mass trends and changes

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# Evaluation of mass trends and changes



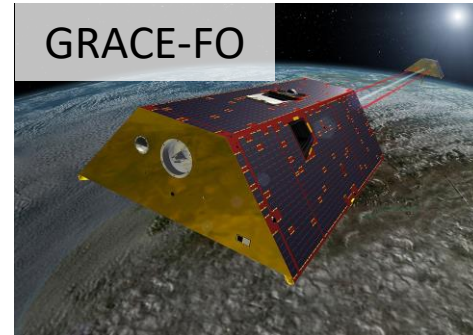
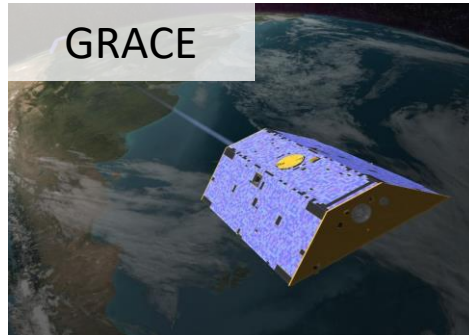
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# Summary and Outlook

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- Time-variable gravity field recovery from kinematic LEO positions
- Combination of monthly LEO gravity field time series on solution level
- Combination of GRACE/-FO and SWARM time series
  - Field-wise weights derived from variance component estimation
  - Filtering helps to reduce the impact of high-degree coefficients on the VCE weights
  - Combined time series provide an improved estimation of mass trends and changes
- Next steps
  - VCE settings still need to be optimized → choice of applied filter, iteration
  - Combination of LEO gravity field time series on normal equation level
  - Extension of GRACE/-FO time series + inclusion of new LEO satellites

Thank you for your attention



Source: ESA, NASA

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# References

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[Dahle C, Arnold D, Jäggi A \(2017\)](#): Impact of tracking loop settings of the Swarm GPS receiver on gravity field recovery. *Advances in Space Research* 59(12):2843–2854, DOI:10.1016/j.asr.2017.03.003

[Jean Y, Meyer U, Jäggi A \(2018\)](#): Combination of GRACE monthly gravity field solutions from different processing strategies. *Journal of Geodesy* 92:1313–1328, DOI: 10.1007/s00190-018-1123-5