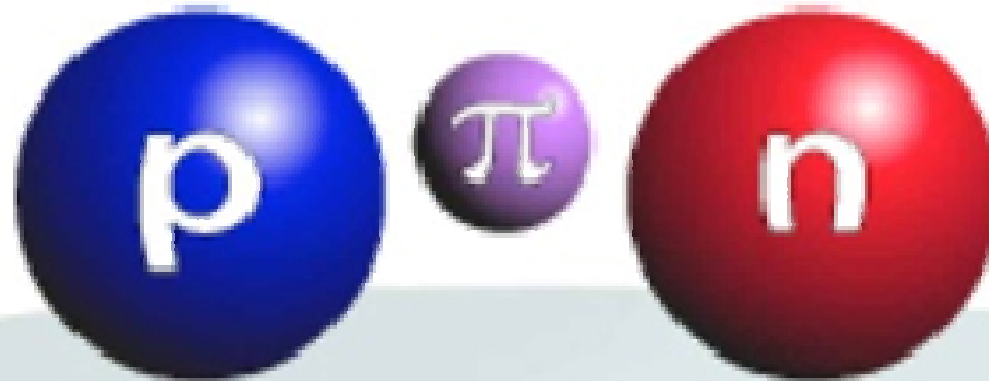


# Introduction – Strong interaction in the nuclear medium: new trends

Denis Lacroix

GANIL-Caen



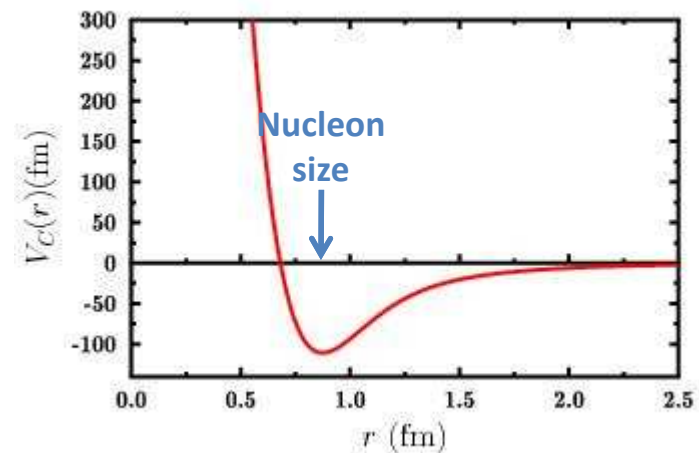
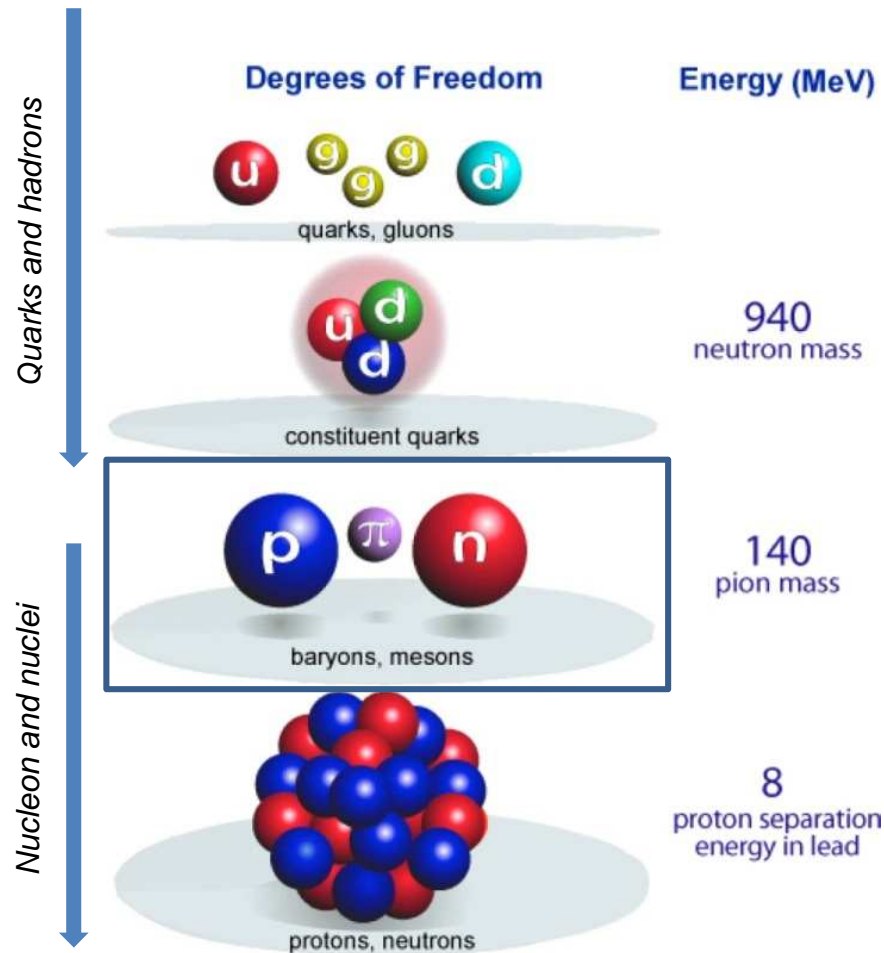
baryons, mesons

# The NN interaction:

*a crossroad between quark, mesons and nuclei*

## The high energy nuclear physicist viewpoint

- From QCD it is clear that NN int. is not a fundamental force
- Quarks and leptons are the elementary entities

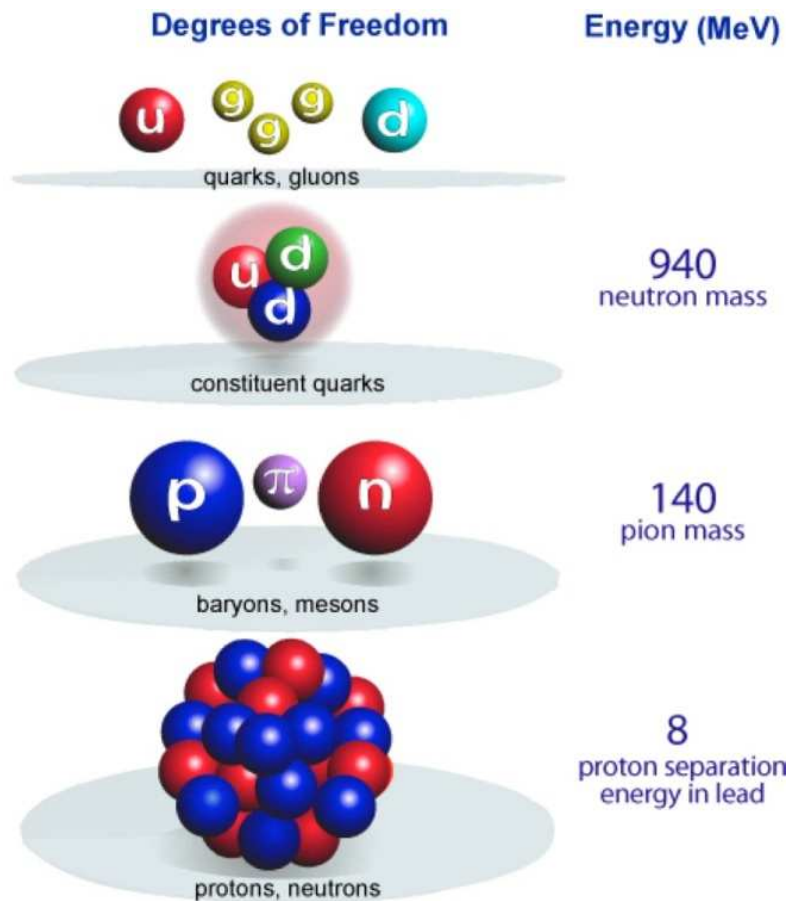


## The low energy nuclear physicist viewpoint

- NN-interaction is a fundamental force
- Nucleons are considered as Elementary (point-like) particles

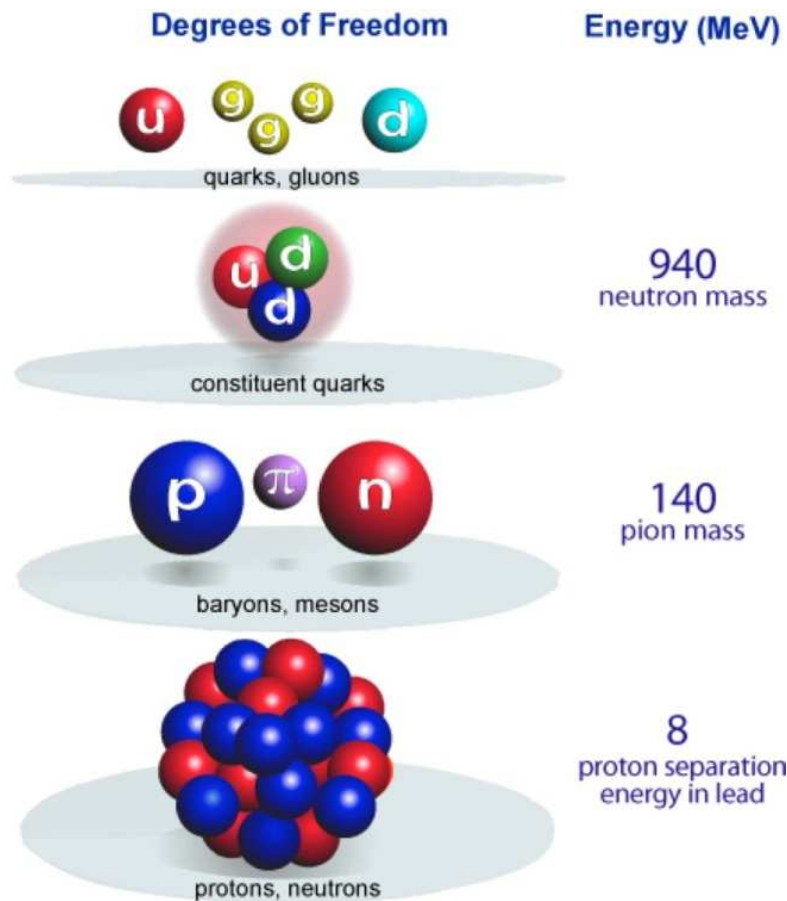
# A school on nuclear interaction: why and why now ?

*Highlights on recent key issues*



- First Lattice QCD calc. of NN interaction
- NN int. from chiral pert. Theory and Effective Field Theory (EFT)
- New “soft” interaction ( $V_{lowk}$ ...)
- Ab-initio calc. for light nuclei and hyperons
- 3-body interaction
- Discussion on spin-orbit, tensor, pairing, 3-body...
- Standard Nuclear models (Energy Density Functional -Shell model) are being now revisited in a “bottom-up” philosophy

# Roadmap of this Lecture



## I -conventional Nuclear Forces

- quantum numbers
- phase shift analysis
- Adjusting semi-empirical forces
- Limitations and difficulties

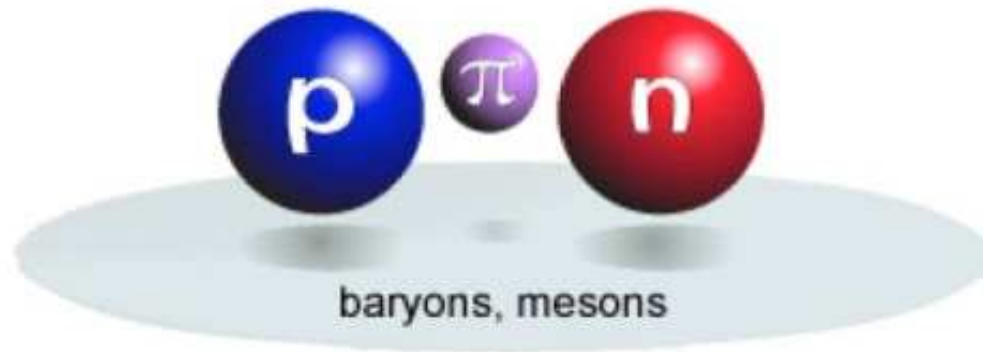
## II-From quarks to nucleons and NN interaction.

- Lattice QCD
- Chiral pert Theory and Effective Field Theory
- Modern Forces

## III-From NN interaction to Nuclei, Hypernuclei, and Stars

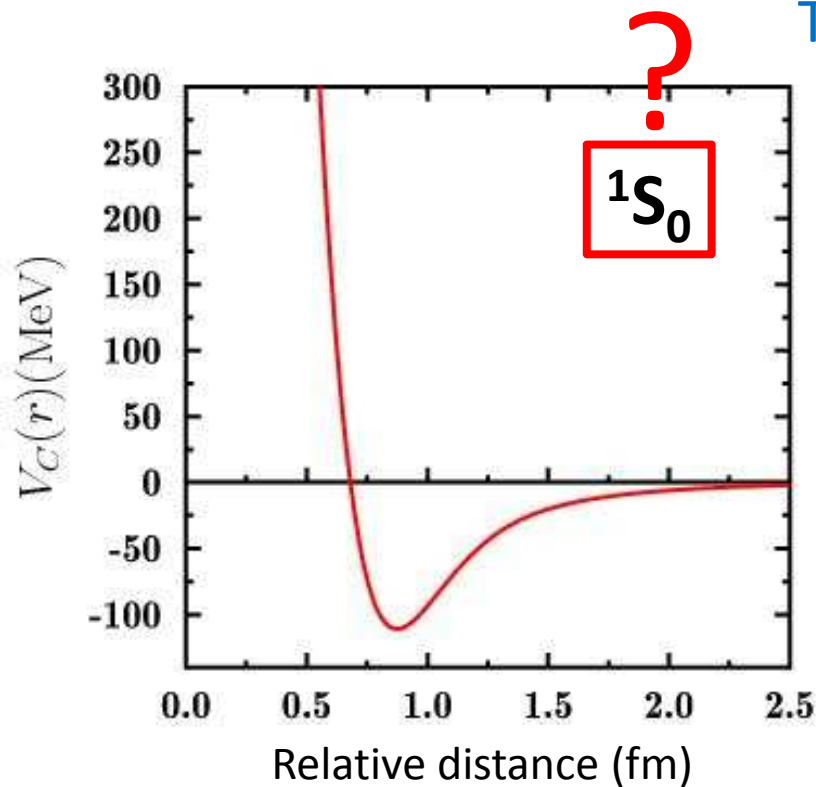
- New soft interaction
- Ab-initio theory and light nuclei
- Selected aspects of Shell Model and Energy Density Functional

# I-Conventional NN interaction



# Conventional NN interaction:

reminder



Two-body wave:  $\Psi_{NN} = \Psi(\mathbf{r}_1\sigma_1\tau_1; \mathbf{r}_2\sigma_2\tau_2)$

Quantum numbers:  $L, S, T$  and  $J = L + S$

| Spin            |   | Isospin         |   |
|-----------------|---|-----------------|---|
| $ S M_S\rangle$ |   | $ T T_z\rangle$ |   |
| $ 0 0\rangle$   | $ \uparrow\downarrow\rangle -  \downarrow\uparrow\rangle$ | $ 0 0\rangle$   | $ \text{np}\rangle -  \text{pn}\rangle$ |
| $ 1 1\rangle$   | $ \uparrow\uparrow\rangle$                                | $ 1 1\rangle$   | $ \text{nn}\rangle$                     |
| $ 1 0\rangle$   | $ \uparrow\downarrow\rangle +  \downarrow\uparrow\rangle$ | $ 1 0\rangle$   | $ \text{np}\rangle +  \text{pn}\rangle$ |
| $ 1 -1\rangle$  | $ \downarrow\downarrow\rangle$                            | $ 1 -1\rangle$  | $ \text{pp}\rangle$                     |

singlet

triplet

Channels:

$$2S+1 [L]_J$$

$$[L = 0, 1, 2, \dots] = \text{S, P, D, } \dots$$

| $S$ | $T$ | $n/p$ state       | $J = 0$   | $J = 1$        | $J = 2$        |
|-----|-----|-------------------|-----------|----------------|----------------|
| 0   | 1   | nn, pp, (np + pn) | $^1S_0$   | $\ominus$      | $^1D_2$        |
| 1   | 0   | (np - pn)         | $\ominus$ | $^3S_1, ^3D_1$ | $\ominus$      |
| 0   | 0   | (np - pn)         | $\ominus$ | $^1P_1$        | $\ominus$      |
| 1   | 1   | nn, pp, (np + pn) | $^3P_0$   | $^3P_1$        | $^3P_2, ^3F_2$ |

## Conventional NN interaction: Semi-phenomenological parameterization

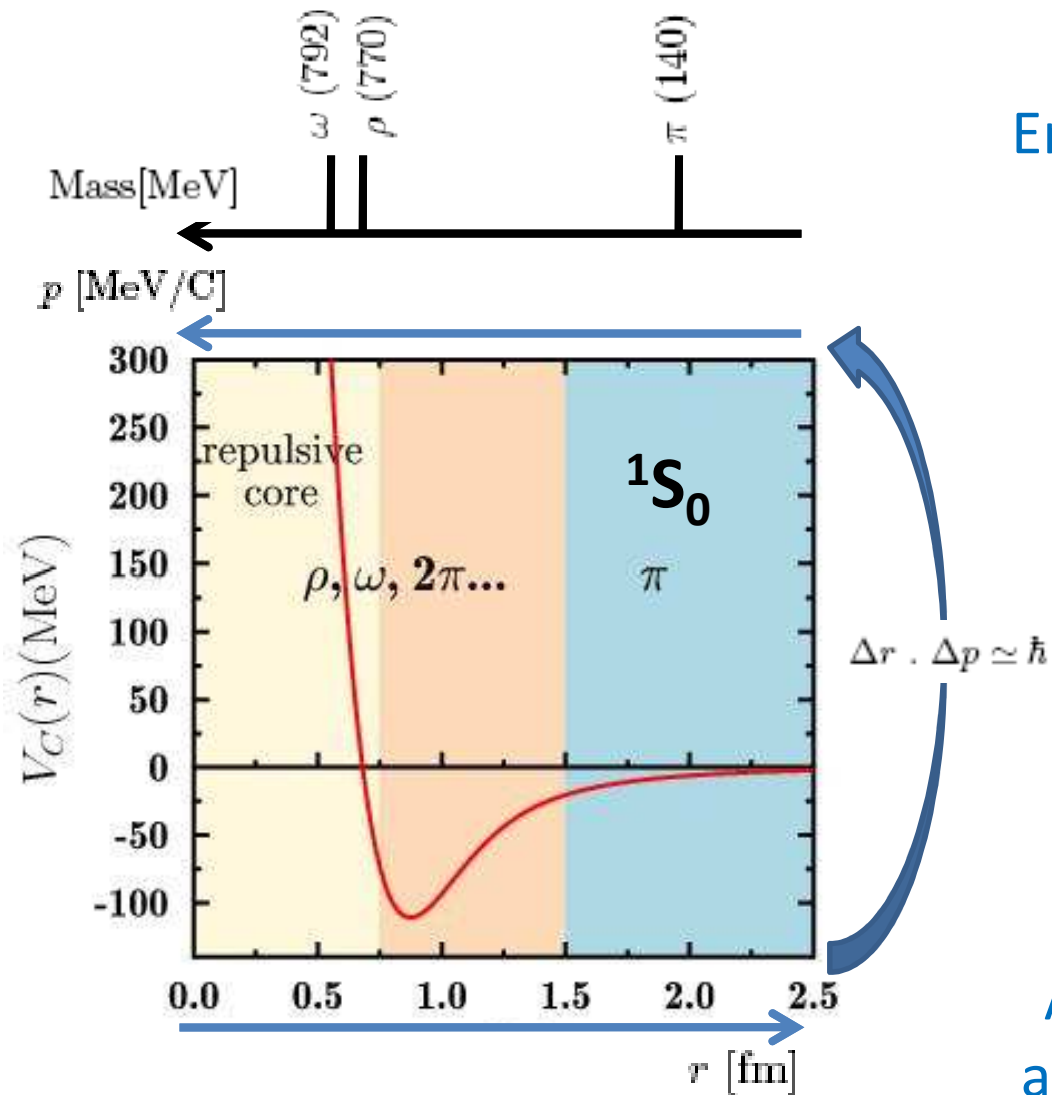
### Energy scale and mesons:

$$V_{NN} = v_{NN}^{\text{EM}} + v_{NN}^{\pi} + v_{NN}^{\text{Rep}}$$

$v_{NN}^{\text{EM}}$  : electro magnetic (Coulomb...)

$v_{NN}^{\pi}$  : long-range (one-pion exchange)

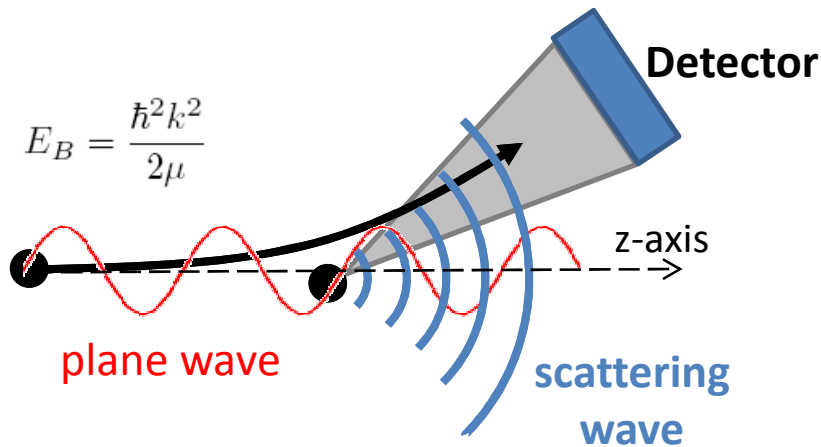
$v_{NN}^{\text{Rep}}$  : short-range + medium range  
(phenomenological repulsive core)



Around 30 parameters to be  
adjusted on experimental data

# Adjusting Conventional NN interaction:

Scattering theory: phase-shift...

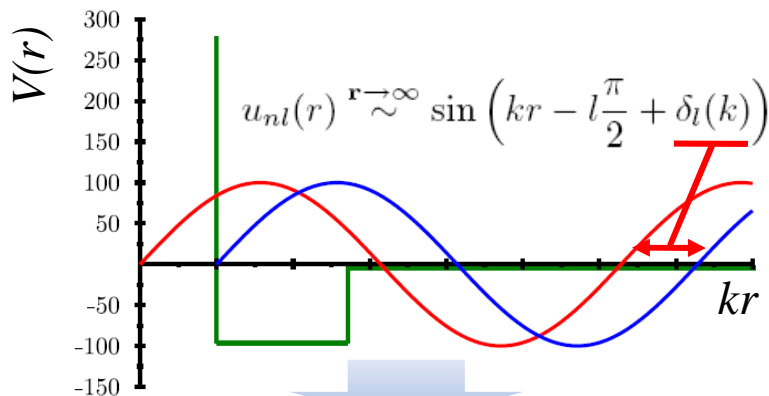


$$\Psi_{\text{scat}}(\mathbf{r}) \xrightarrow{r \rightarrow \infty} e^{ikz} + f(\theta, \varphi) \frac{e^{ikr}}{r}$$

$$\sigma_k(\theta, \varphi) = |f(\theta, \varphi)|^2$$

## Spherical symmetric potential:

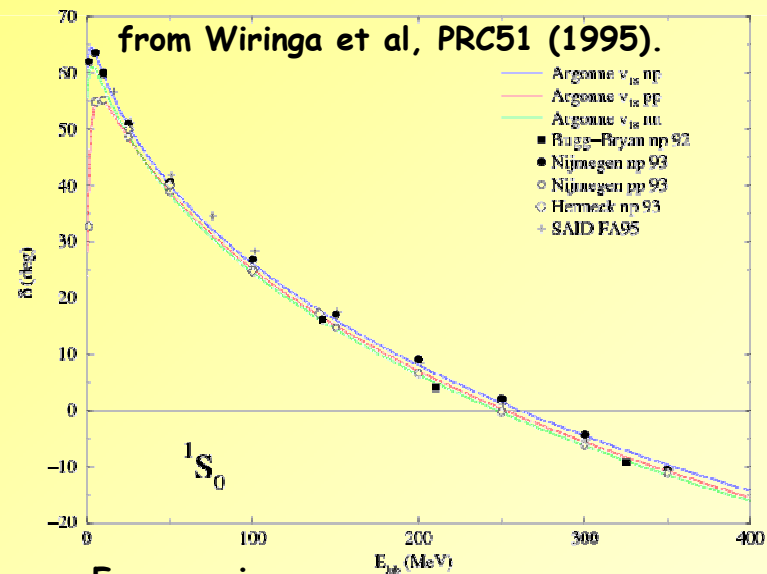
$$\Psi_{\text{scat}}(\mathbf{r}) = \sum_{nlm} c_{nlm} \frac{u_{nl}(r)}{r} Y_{lm}(\theta, \varphi)$$



$$\sigma(k) = \frac{4\pi}{k^2} \sum_l (2l+1) \sin^2[\delta_l(k)]$$

## Example (av18):

→ nn, pp, np data



For a review see Machleidt and Staus, J. Phys. G27 (2001)

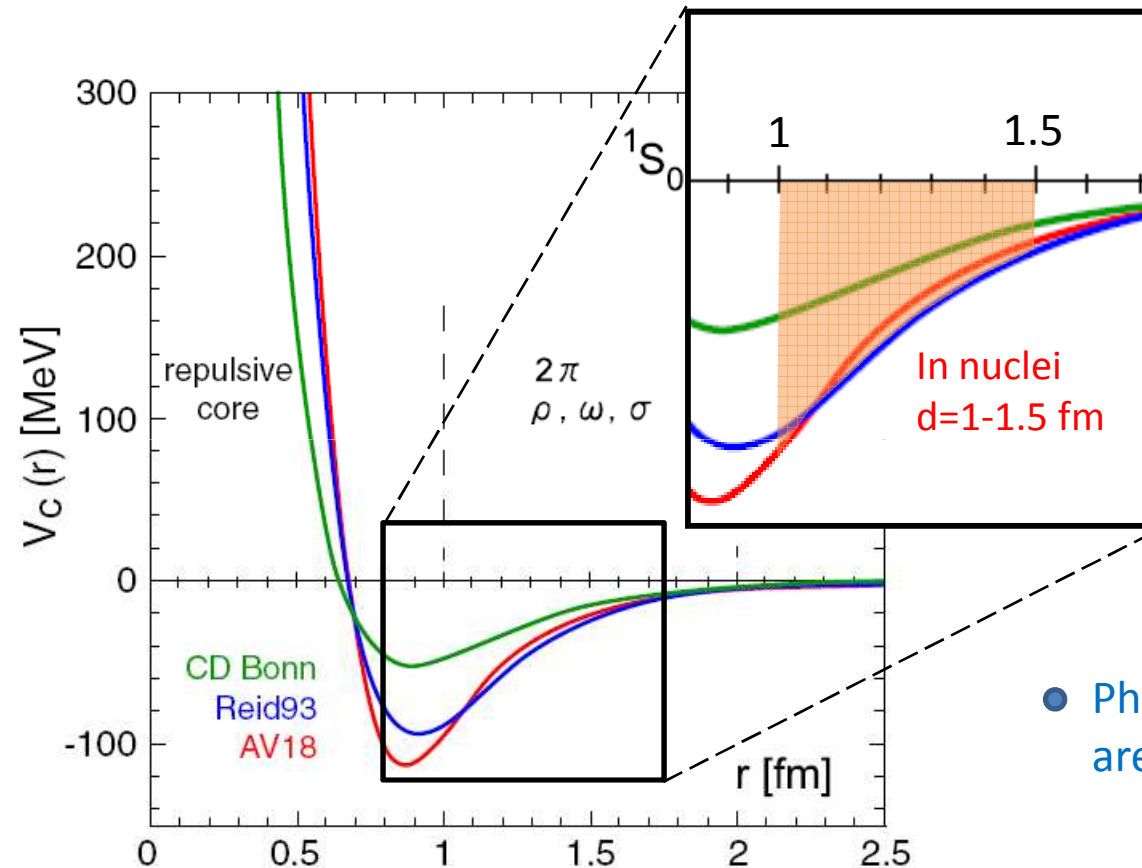
● Adjusted also on deuteron properties (B.E.)



# Conventional NN interaction:

*Drawbacks: non uniqueness*

Adapted from Ishii, Aoki and Hatsuda, PRL 99 (2007)



- Phenomenological NN potentials are not unique  
(partially solved by  $V_{\text{low}k}$ )
- Difficult to improve systematically

➔ Need for a systematic constructive theory  
(Effective Field Theory)

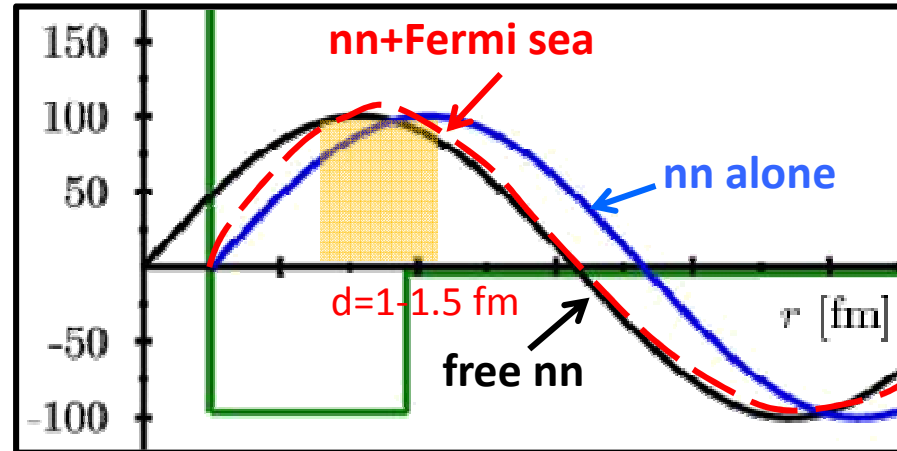
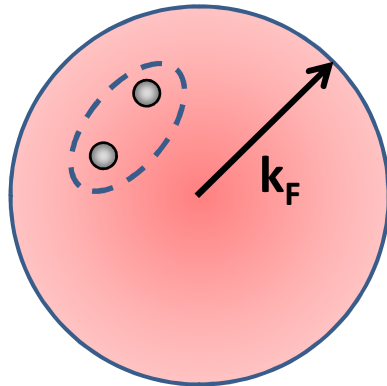
# Conventional NN interaction:

in-medium effects

$$\Delta k = 0.6 k_F$$

What means in-medium effect ?

Example: two-nucleons in a Fermi sea



Gomes, Walecka and Weisskopf, Ann. Phys. (1958)

Stiff nn  
+  
Pauli

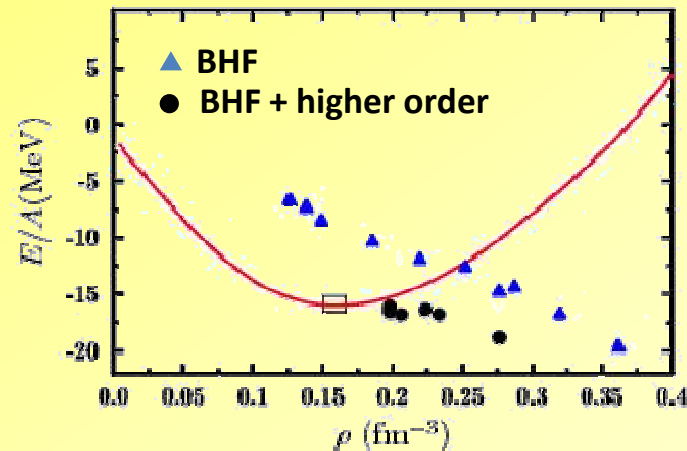
- In medium effects are large and crucial
- Leads to an independent particles + residual int. picture

Formal theory of “dressed” interaction

$$G = V - V \frac{Q}{e} G = V - V \frac{Q}{e} V \frac{Q}{e} V + \dots$$

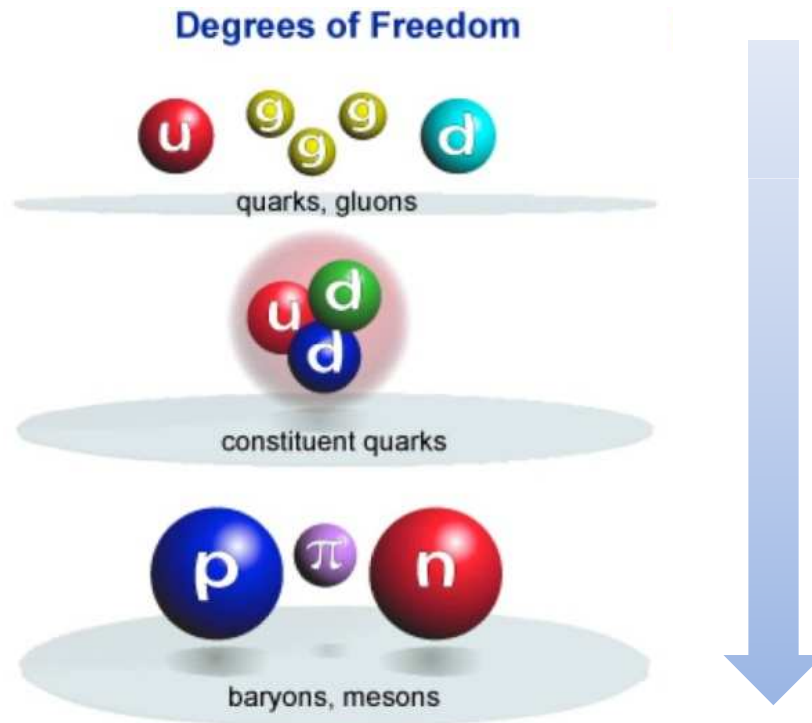
(Bethe-Goldstone Eq.)

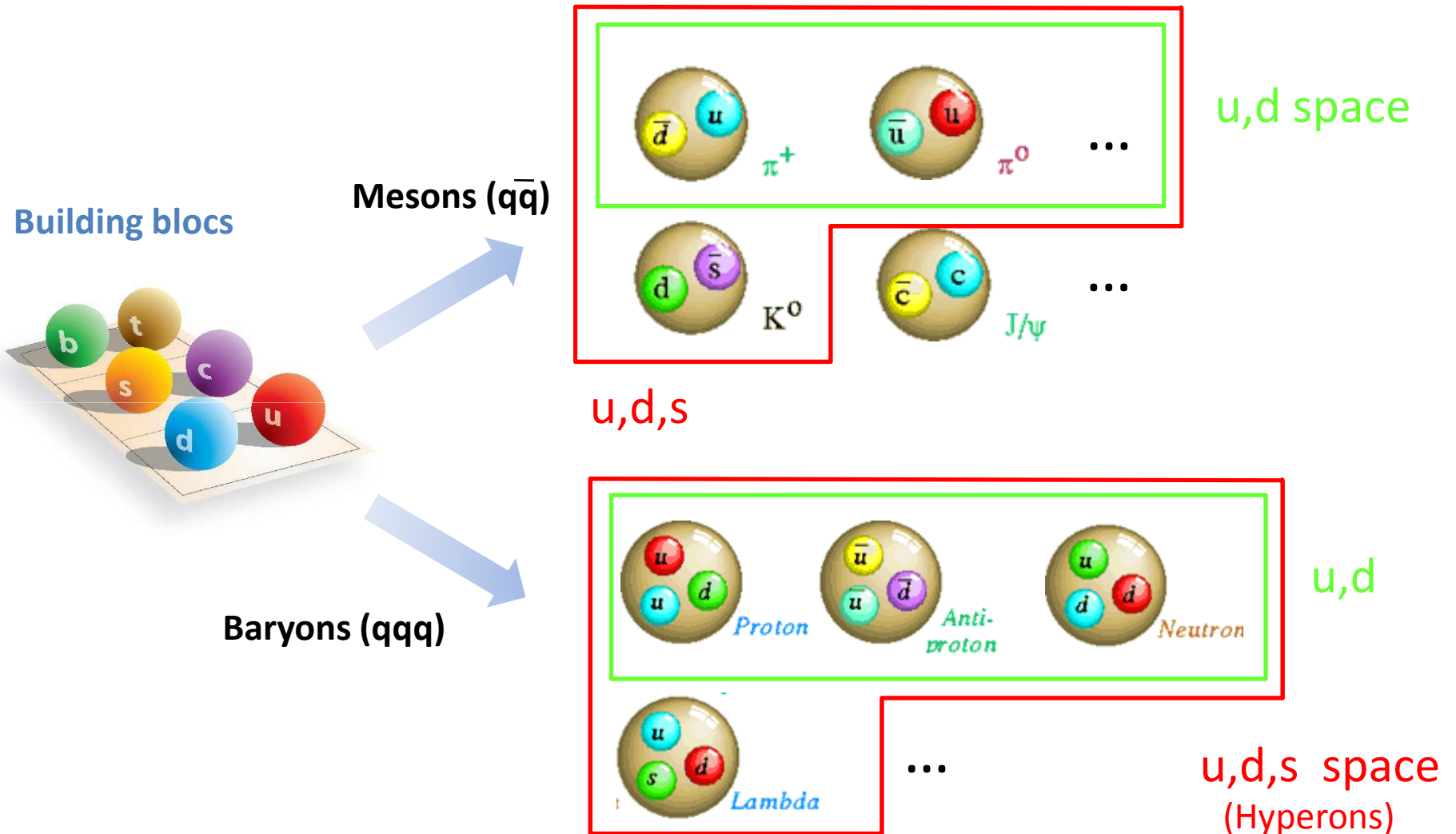
J. Meyer, Ann. Phys. Fr (2001)



- ☹️ Difficult to work with conventional NN
- 😊 Has motivated Energy Density Func. (1972)
- 😊 Solved by  $V_{lowk}$  + 3-body

# II-From quarks to nucleons and NN-interaction: New trends





In low energy nuclear physics we are mainly concerned with  $u, d, s$  space

(see lecture D. Watts)

# First Lattice QCD application

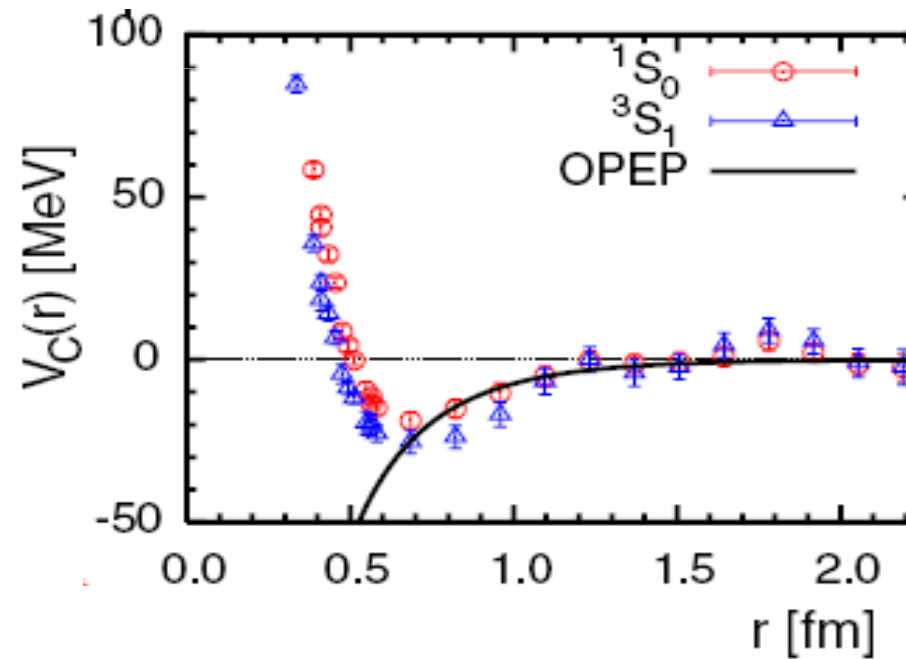
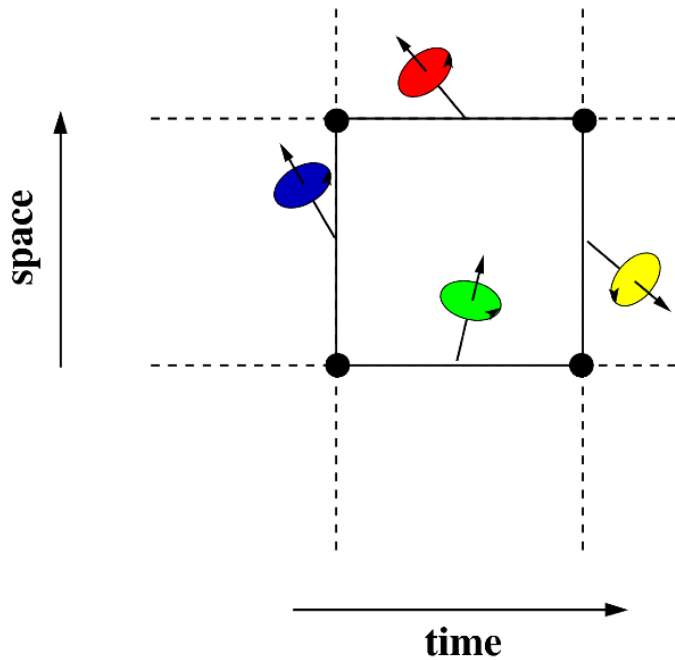
QCD Lagrangian  
discretized on a mesh



Hadrons properties  
(NN-interaction)

$$\mathcal{L}_{QCD}$$

Free parameters:  
Quark masses



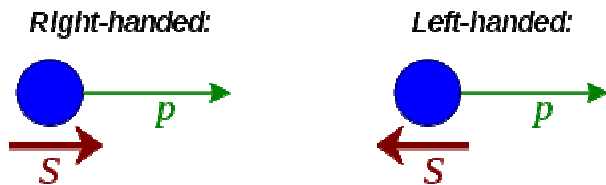
Ishii, Aoki and Hatsuda, PRL 99 (2007)

### QCD Lagrangian

$$\mathcal{L}_{\text{QCD}} = \mathcal{L}_{\text{QCD}}^{\text{MassLess}} - \bar{q}Mq$$

**Chiral symmetric**

**Explicitly breaks The chiral symmetry**



### Quarks Masses

$$\begin{aligned} m_u &\sim 2.4^{+0.9}_{-0.6} \text{ MeV} \\ m_d &\sim 4.75^{+1.25}_{-0.48} \text{ MeV} \\ m_s &\sim 100^{+30}_{-20} \text{ MeV} \end{aligned}$$

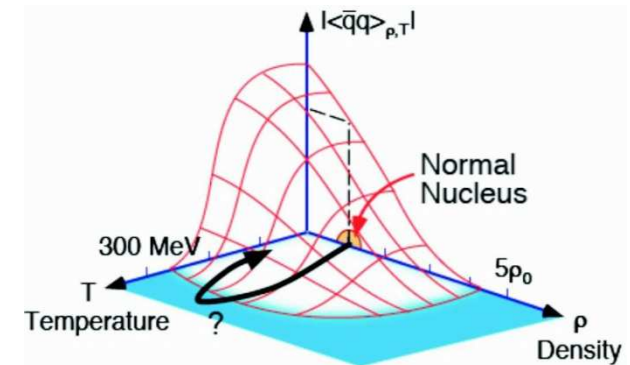
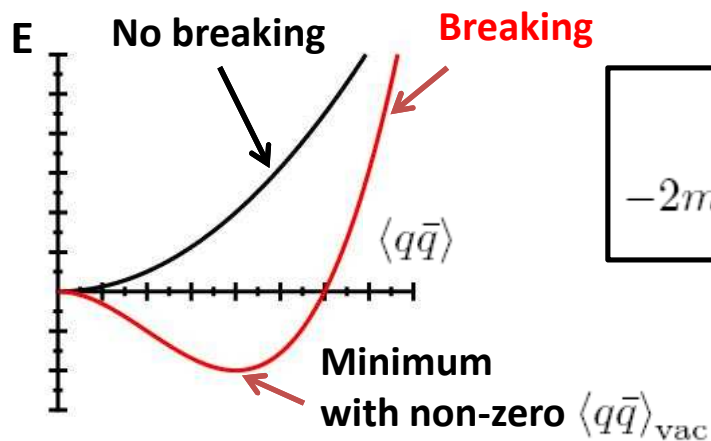
**light quarks**

**GAP (1 GeV)**

$$\begin{aligned} m_c &\sim 1270^{+70}_{-110} \text{ MeV} \\ m_b &\sim 4200^{+170}_{-70} \text{ MeV} \\ m_t &\sim 171200^{+2100}_{-1900} \text{ MeV} \end{aligned}$$

**heavy quarks**

### Illustration of chiral symmetry Breaking consequences



(see lecture C. Djalali)

**→ treat the light quark masses perturbatively (chiral pert. theory) and use Effective Field Theory (EFT)**

# Modern theory of Nuclear Forces

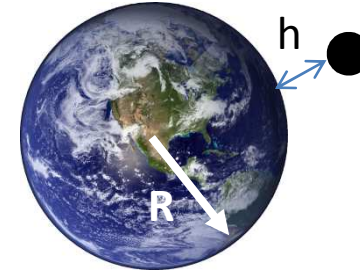
## Effective Field Theory

What is EFT ?

### Gravitation (Papenbrock -2008)

$$h \ll R$$

$$V(h) = -\frac{GMm}{R+h} = V(0) + \frac{GMm}{R} \left(\frac{h}{R}\right) + O\left(\frac{h^2}{R^2}\right)$$



### Toy NN interaction (Meissner-CISS08)

$$V(\vec{r}) = \underbrace{\frac{\alpha_l}{4\pi r} e^{-M_l r}}_{\text{long-range}} + \underbrace{\frac{\alpha_h}{4\pi r} e^{-M_h r}}_{\text{short-range}}$$

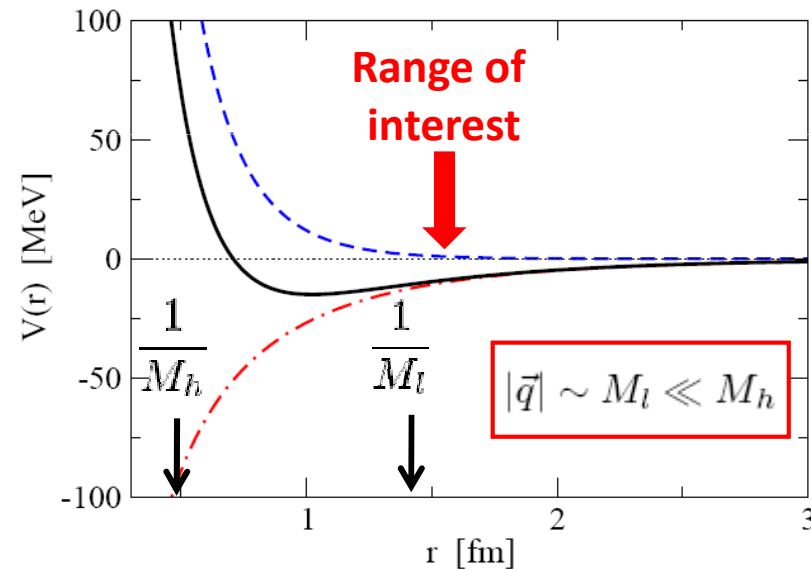
$$V(\vec{q}) = \frac{\alpha_l}{\vec{q}^2 + M_l^2} + \frac{\alpha_h}{\vec{q}^2 + M_h^2}$$

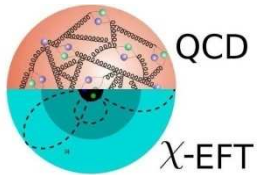
$$V(\vec{q}) = V_{long}(\vec{q}) + V_{short}(0) - \frac{\alpha_h}{M_h^2} \left(\frac{\vec{q}}{M_h}\right)^2 + \dots$$

$$V(\vec{q}) = V_{long}(\vec{q}) + \left[ \underbrace{C_0}_{\text{LO}} + \underbrace{C_2 \left(\frac{\vec{q}}{\Lambda}\right)^2}_{\text{NLO}} + \dots \right] f_\Lambda(\vec{q}^2)$$

Diverge at large  $q$  - Introduce a cutoff

$$\Lambda \sim M_h$$





# Modern theory of Nuclear Forces

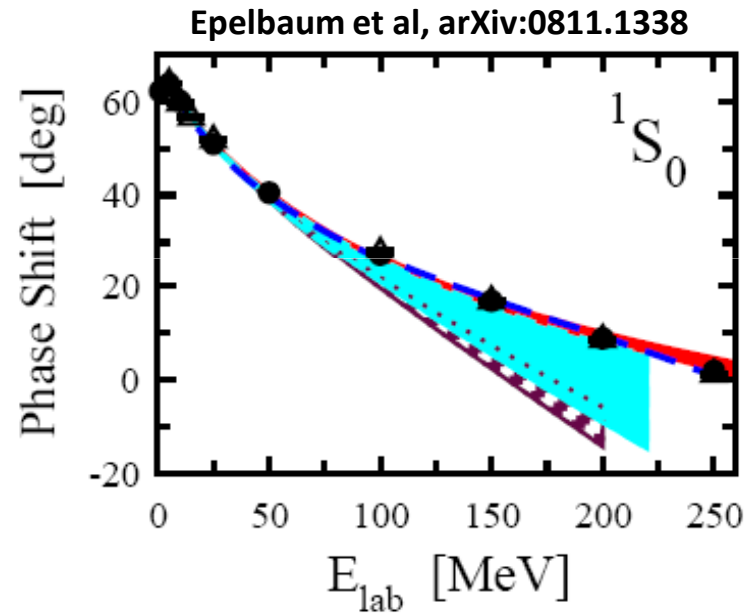
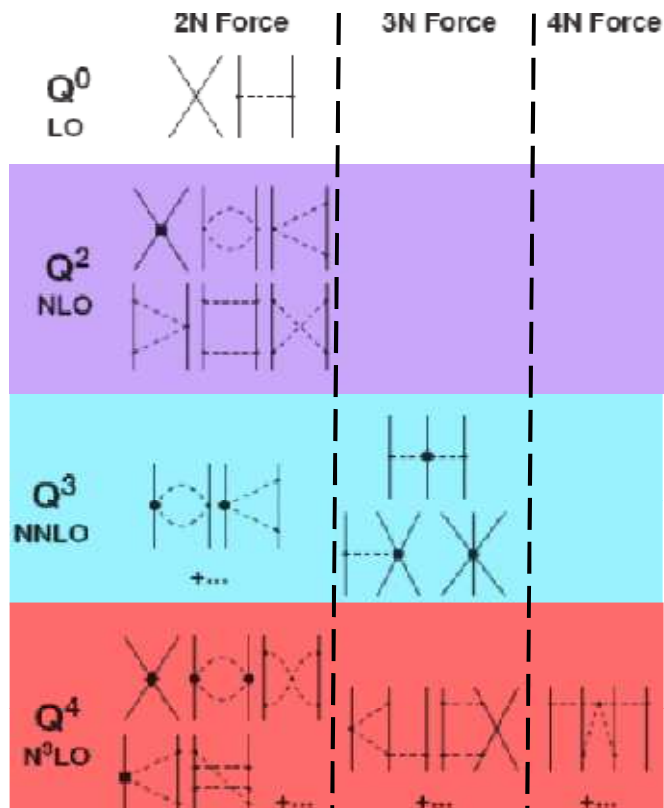
## Chiral Lagrangian and Effective Field Theory

Starting point : Chiral Lagrangian

$$\mathcal{L}_{QCD} \longrightarrow \mathcal{L}_{EFT} = \mathcal{L}_{\pi\pi} + \mathcal{L}_{\pi N} + \mathcal{L}_{NN} + \dots$$

$|\vec{q}| \sim M_\pi \simeq 140 \text{ MeV}$   
 $\Lambda_{QCD} \simeq 1 \text{ GeV}$   
 develop in  $\left(\frac{\vec{q}}{\Lambda}\right)$

### Feynman diagrams



- ➔ Direct link to QCD (chiral)
- ➔ Systematic Constructive method
- ➔ Consistent NN, 3N, 4N ...

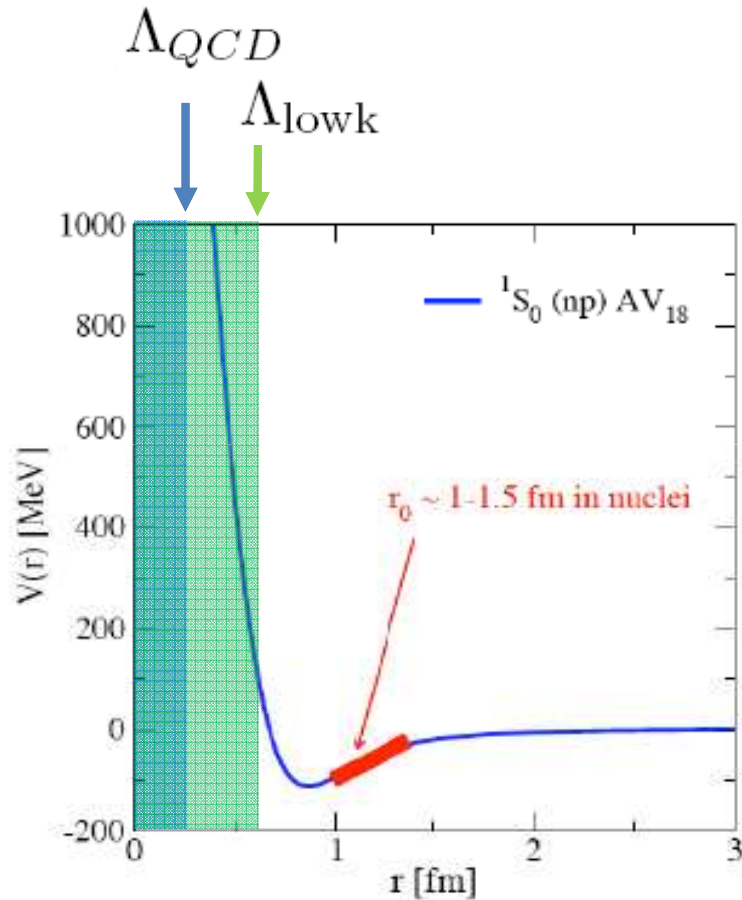
(see lecture E. Epelbaum)



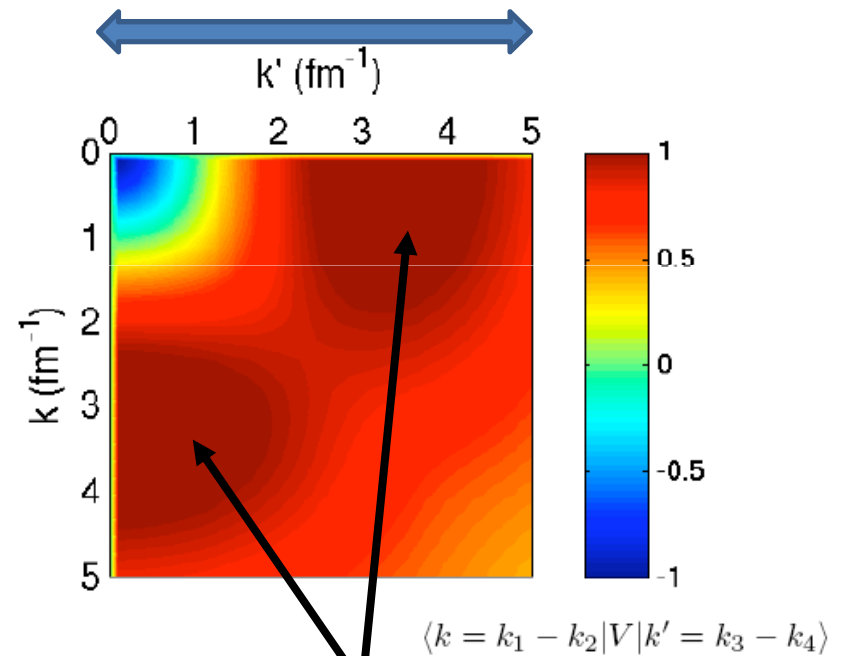
# Modern theory of Nuclear Forces

Soft interaction

- ~~Systematic Improvement~~
- Hard to work with bare NN interaction (Hard core)



Potential suited to understand physics of high and low energy nuclear physics



Difficult high momentum component

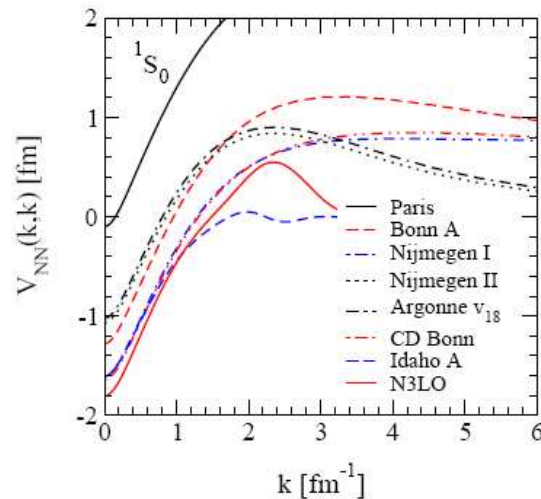
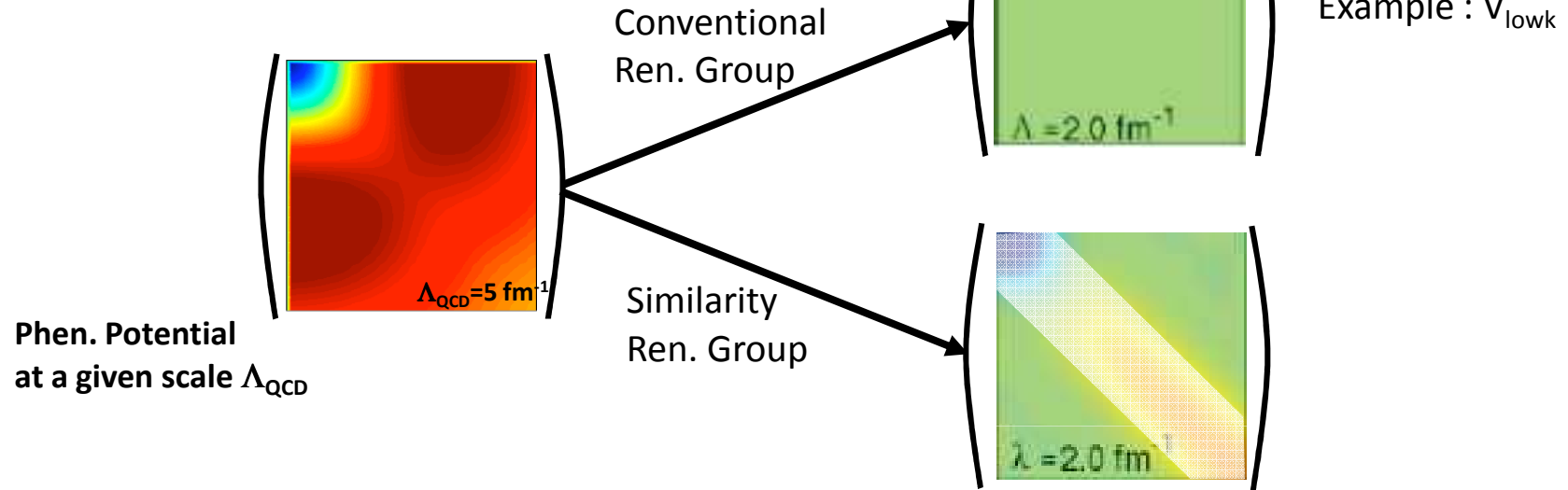
(adapted from Bogner -Trento2009)

# Modern theory of Nuclear Forces

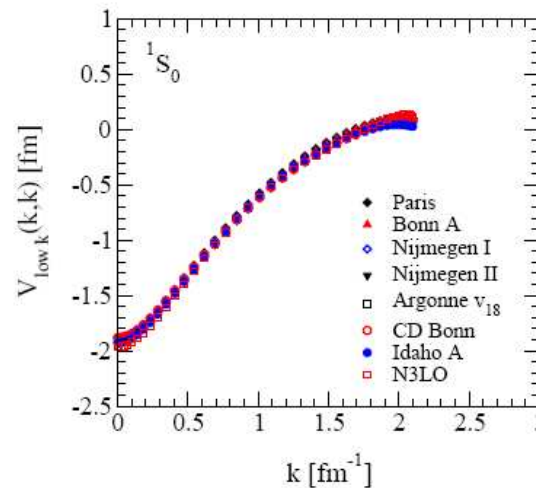
Soft interaction

➔ ~~Systematic Improvement~~

➔ Hard to work with bare NN interaction (Hard core)



Bogner et al, Phys. Rep. (2005)



(adapted from Bogner -Trento2009)

➔ Soft interaction are adjusted to not change low energy properties

➔ All interaction leads to Same soft int. 😊

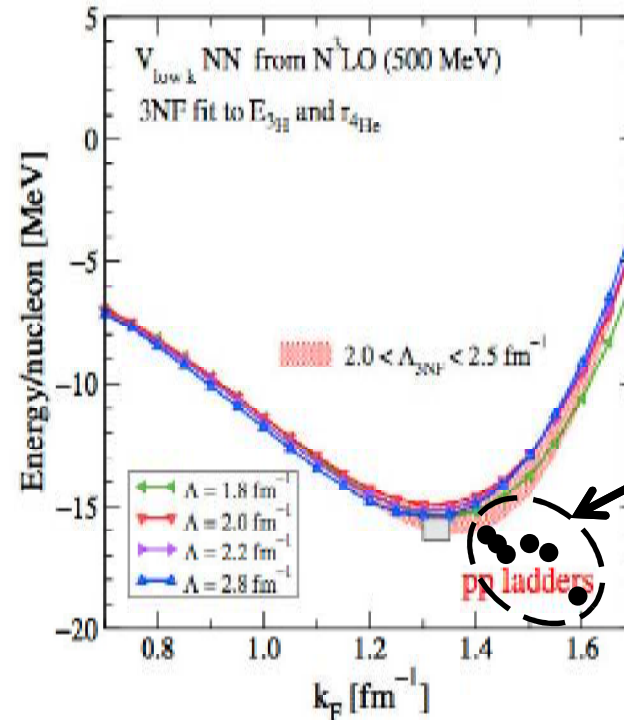
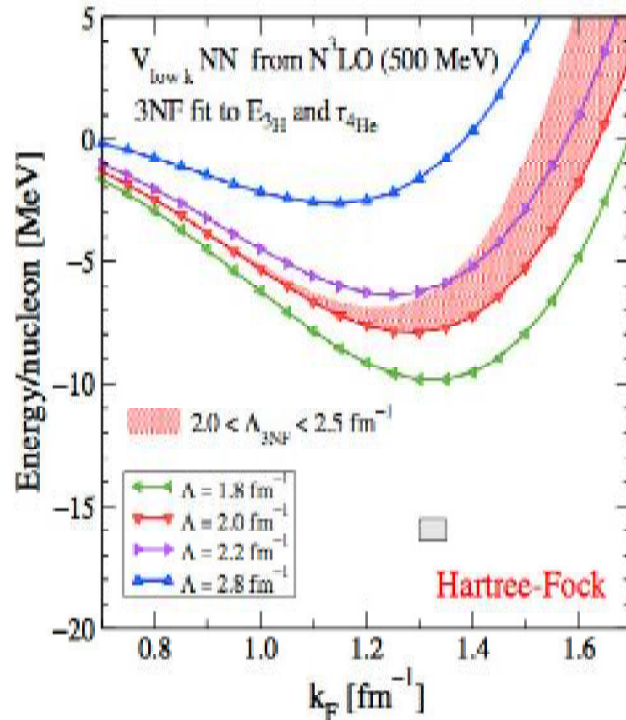
➔ Easier to work with soft int. 😊

➔ Renormalization generates 3-body, 4-body...

# New perspective with soft interaction

## Nuclear matter properties

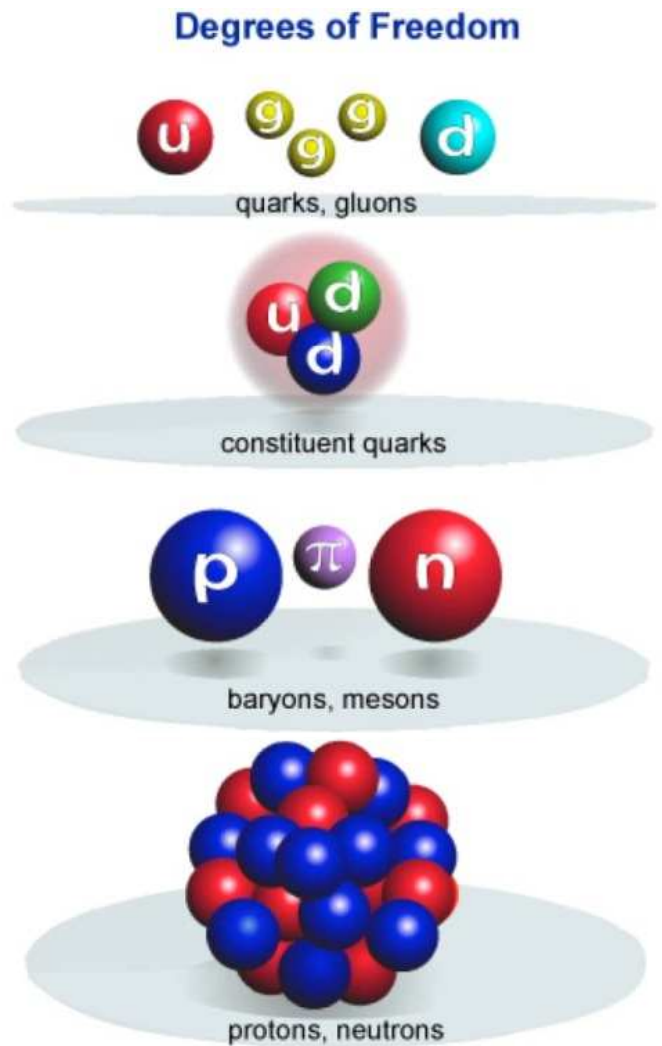
Bogner, Schwenk, Furnstahl, Nogga, NPA 763 (2005) .



old calculation  
with conventional  
forces

- ➔ Already at the Hartree-Fock level saturation is obtained.
- ➔ Perturbative does now converge
- ➔ Note that three-body is essential.

# III - From NN-interaction to nuclei, hypernuclei

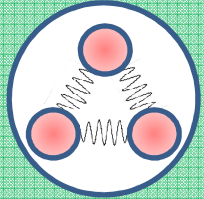
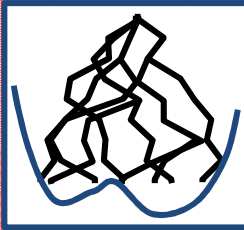
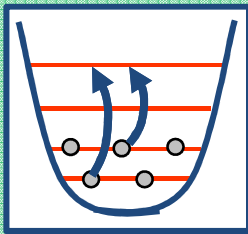
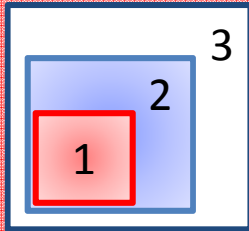


Ab-initio  
calculations of nuclei



# Ab-initio methods

A non-exhaustive guiding tour

| Name                                    | Short description  | Variational | Scale as              | Up to                                     |
|---|--|-------------|-----------------------|---|
| Few-body<br>(Faddeev...)                | $H\Psi = E\Psi$<br>  | Yes         | $M^A$                 | $A = 2-4$                                 |
| Green-Function<br>Monte-Carlo<br>(GFMC) | $\Psi(\tau) = e^{-(H-E_0)\tau}\Psi_T,$<br>$= [e^{-(H-E_0)\Delta\tau}]^n \Psi_T$<br>+ auxiliary field<br> | Yes         | $\frac{M!}{(M-A)!A!}$ | $A < 12$                                  |
| No-core<br>Shell Model                  | $H\Psi = E\Psi$<br>   | Yes         | $4^A$                 | $A < 16$                                  |
| Coupled-Cluster<br>(CC)                 | $ \Psi\rangle = e^S  \Psi_0\rangle$<br>$S = S_1 + S_2 + \dots$<br>                                     | No          | $(M-A)^4 A^2$         | $A < 100$<br>Only doubly-magic<br>for now |

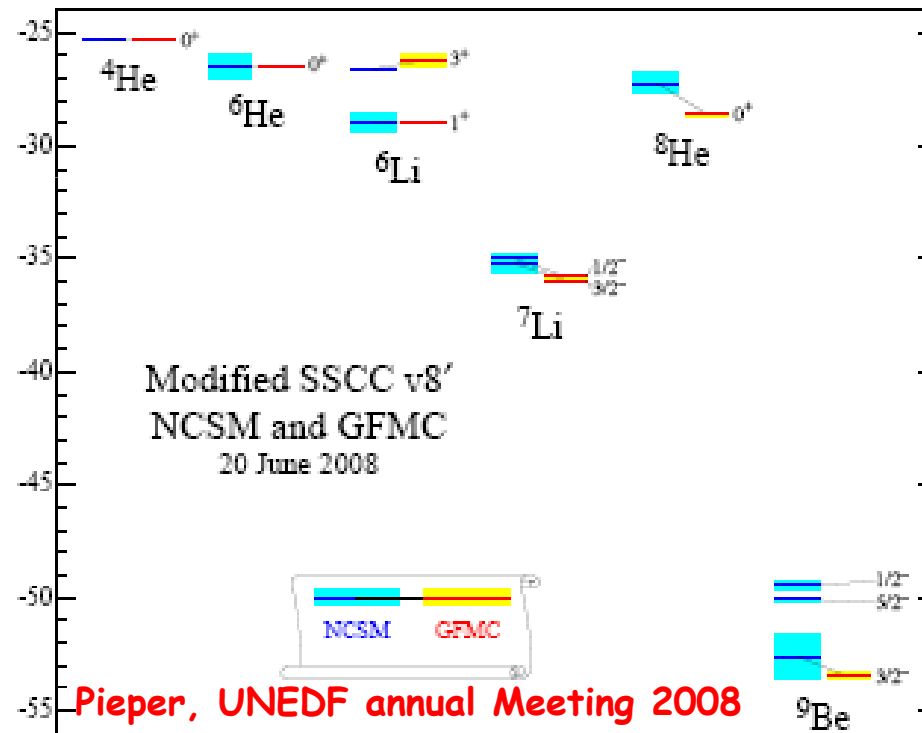
M : configuration space size

Benchmark (A = 4)

Kamada et al, PRC64 (2001)

|                | Faddeev    | GFMC       | NCSM       |
|----------------|------------|------------|------------|
| E (MeV)<br>A=4 | -25.94 (5) | -25.93 (2) | -25.8 (20) |

Benchmark (A > 4)



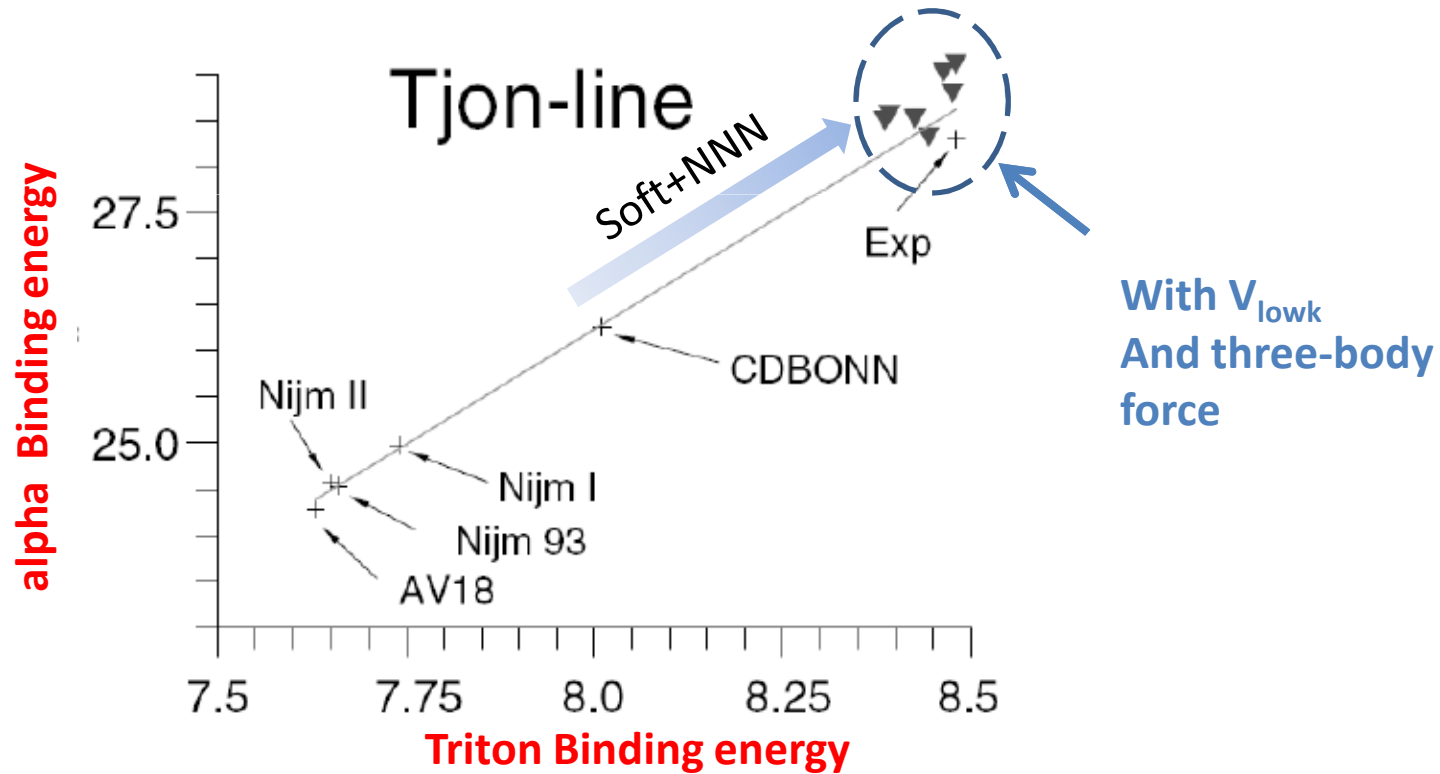
GFMC: Pieper et al, PRC (2004).

NCSM: Navratil et al, arXiv:0904.0463

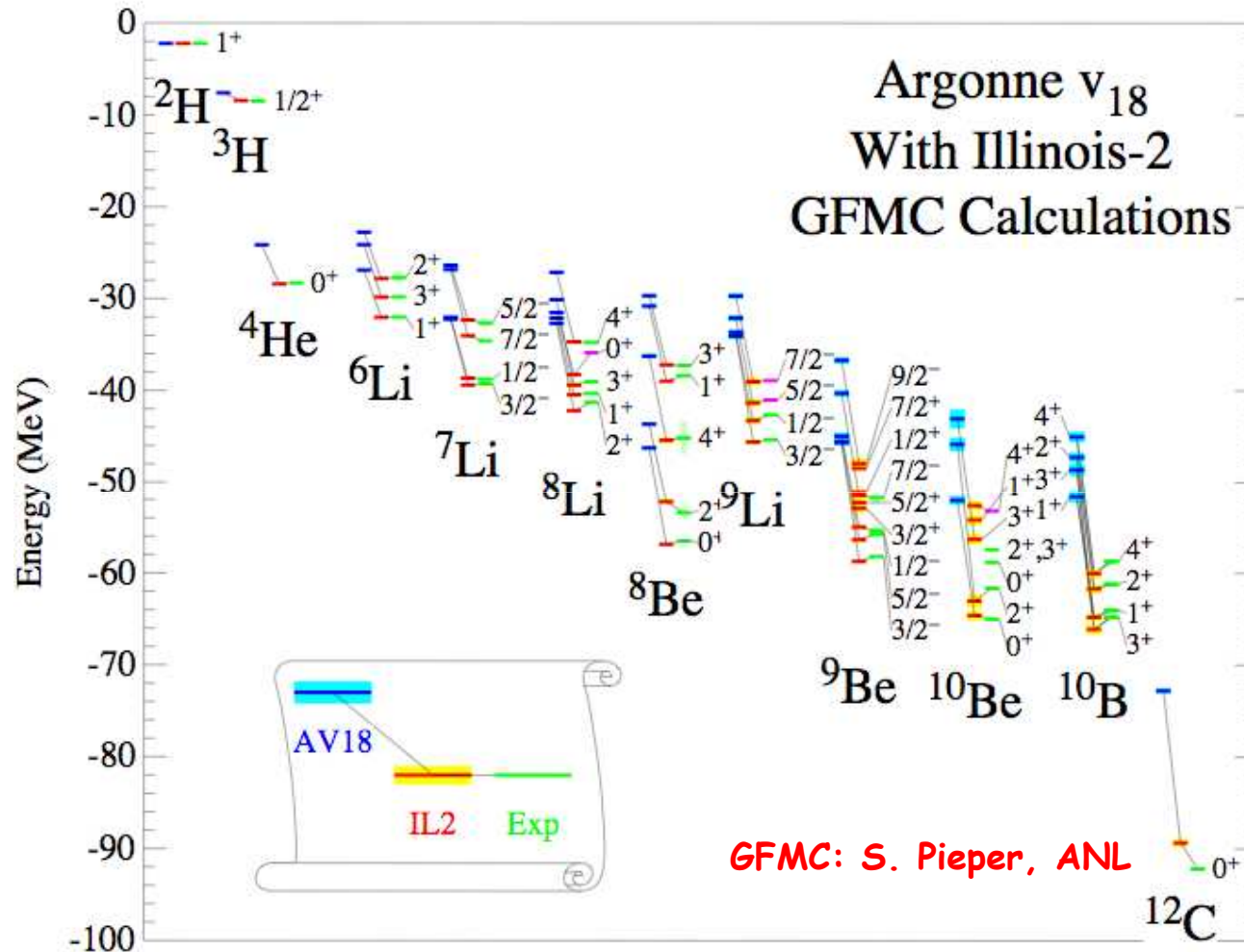
Powerfulness :Light nuclei and three body force

Why we need a three-body force ?

- ➔ For saturation of nuclear matter
- ➔ For B. E. of nuclei
- ➔ Spin-orbit splitting



Nogga et al, PRL 85 (2000).



The complete  
Bottom-up approach

QCD (chiral)



NN+NNN (EFT)

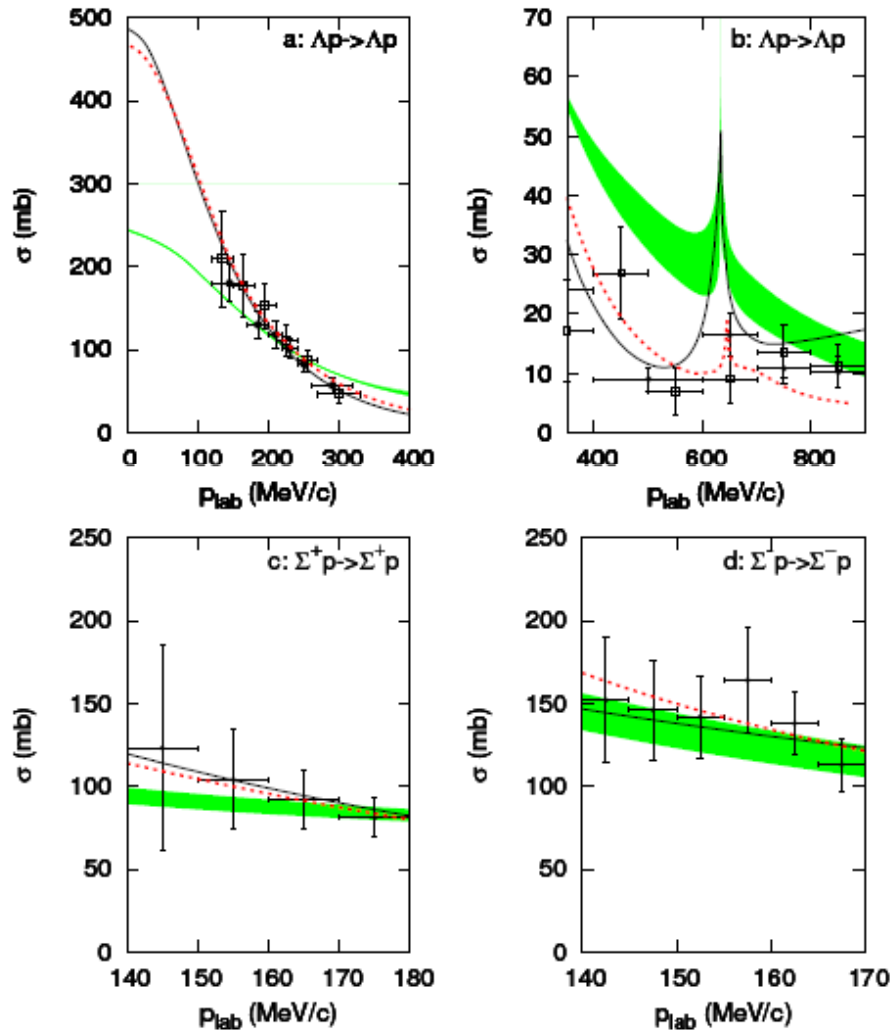


nuclei

(see lecture W. Catford)

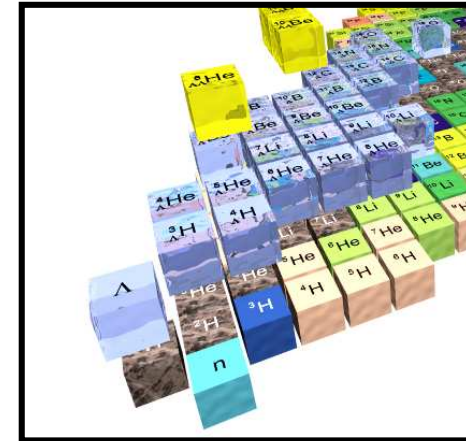


### YN Interaction

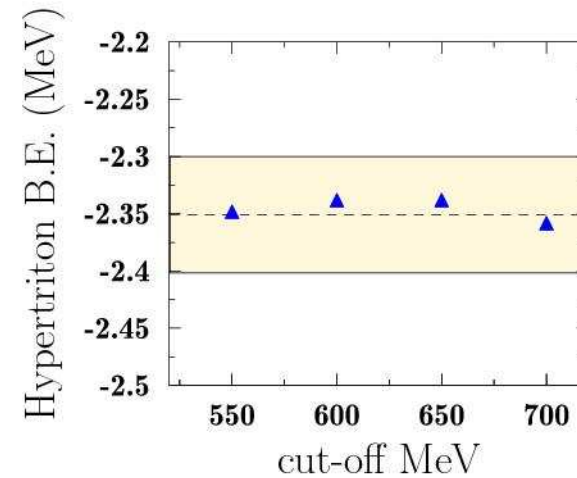


Polinder et al, NPA (2006)

■ LO EFT  
— Jülich 04  
— Nijm 97f



35 data only  
 (for comparison  
 nn, np... between 2000/3000 data)



(see lecture I. Vidana)

# Nuclear structure for heavier nuclei

## Conventional Shell model

Highlights on “standard” shell-model

$$\Psi = \Phi_{[0p0h]} + \Phi_{[1p1h]} + \Phi_{[2p2h]} + \dots$$

Configuration interaction

$$H = \text{SPME (Exp)} + \text{TBME (G)}$$

ex : sp shell

 $\epsilon_i$ 
 $G_{ijkl}$ 

number

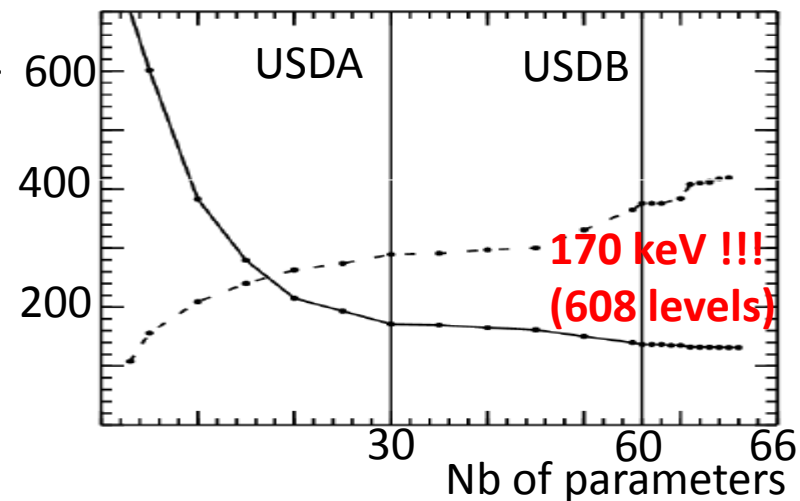
**3**

**63**

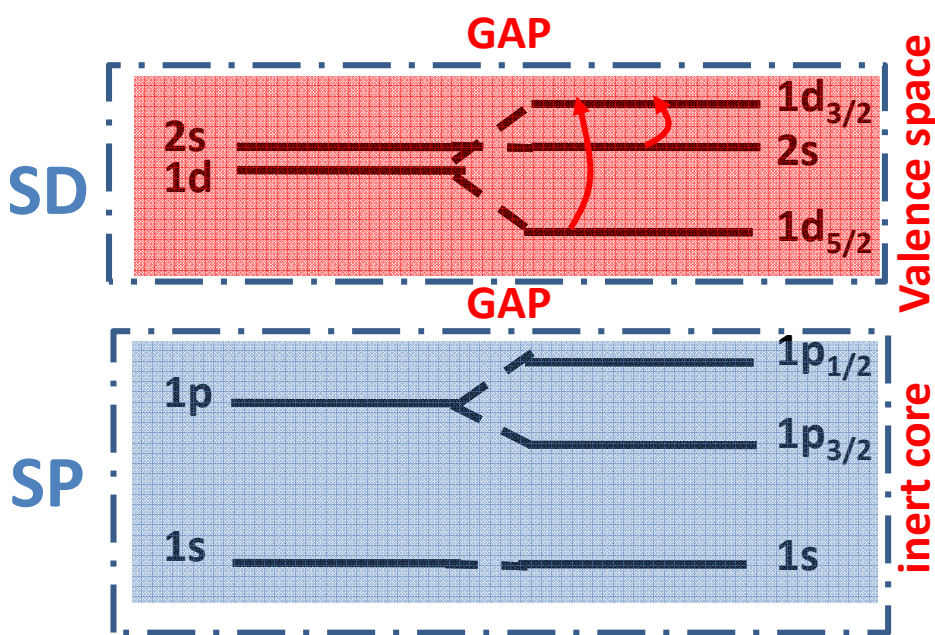
Monopole(exp)

refitting

Standard deviation (keV)

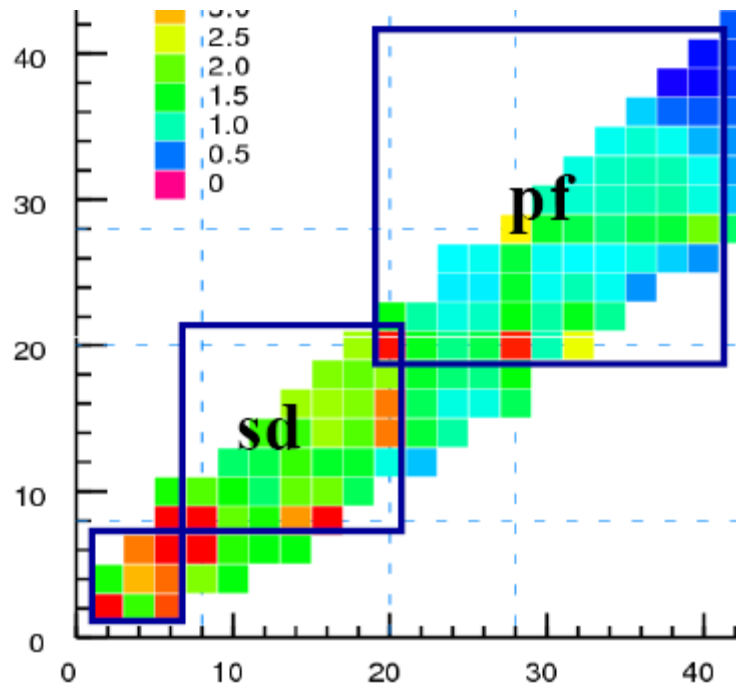


A. Brown ECT\* (2007).

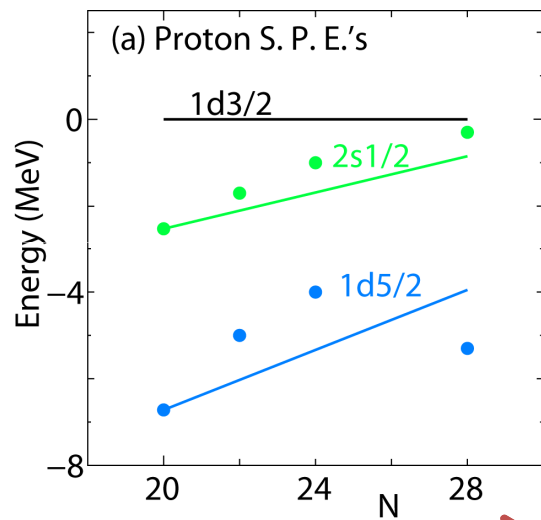


(see lecture N. Smirnova)

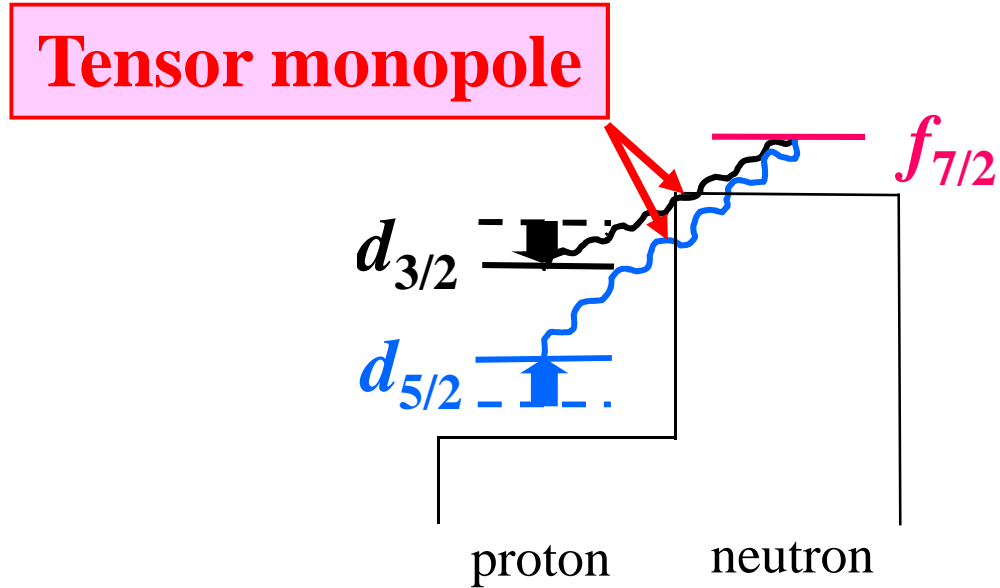
FP



- ➔ Shell Model is the tool of choice to understand level scheme
- ➔ Physics of *Shell evolution, magicity, pairing, deformation, spin-orbit, tensor, ...*  
(see lecture O. Sorlin)



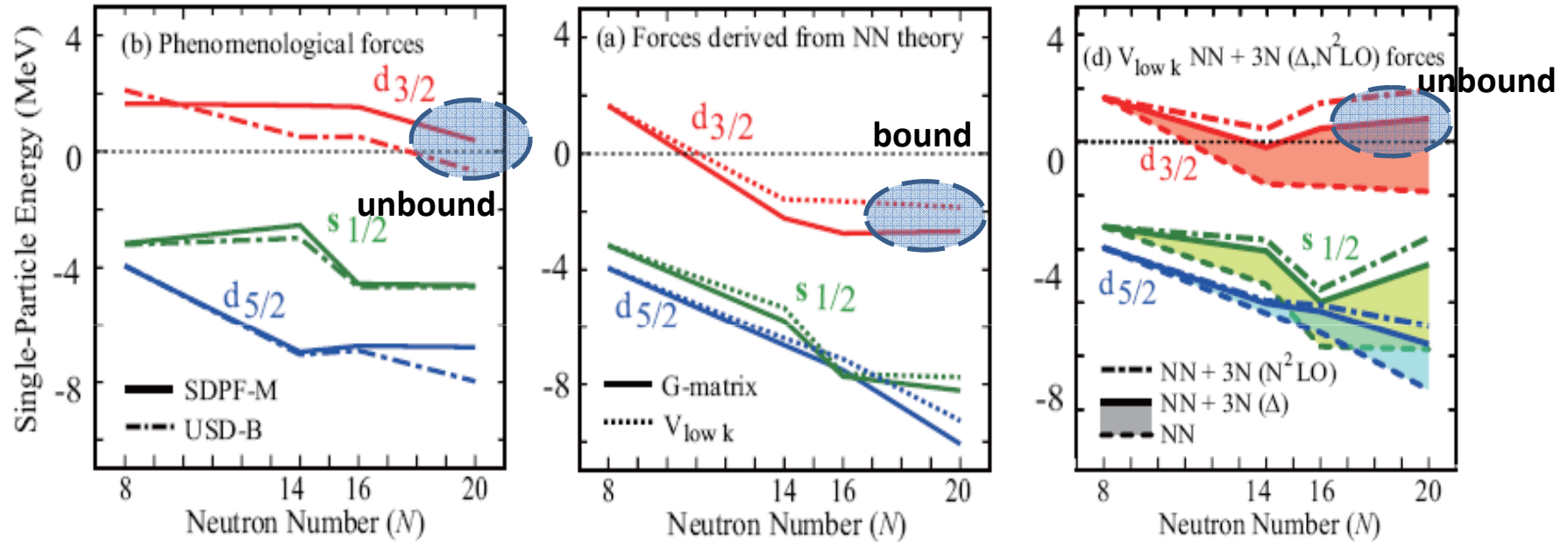
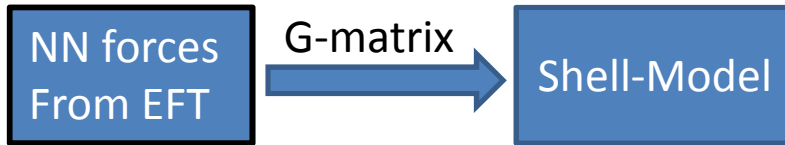
➔ neutrons in  $f_{7/2}$



Otsuka *et al.*, PRL 95 (2005)

- ➔ Still very phenomenological (empirical monopoles, refitting procedure)

# Towards the next generation of Shell Model

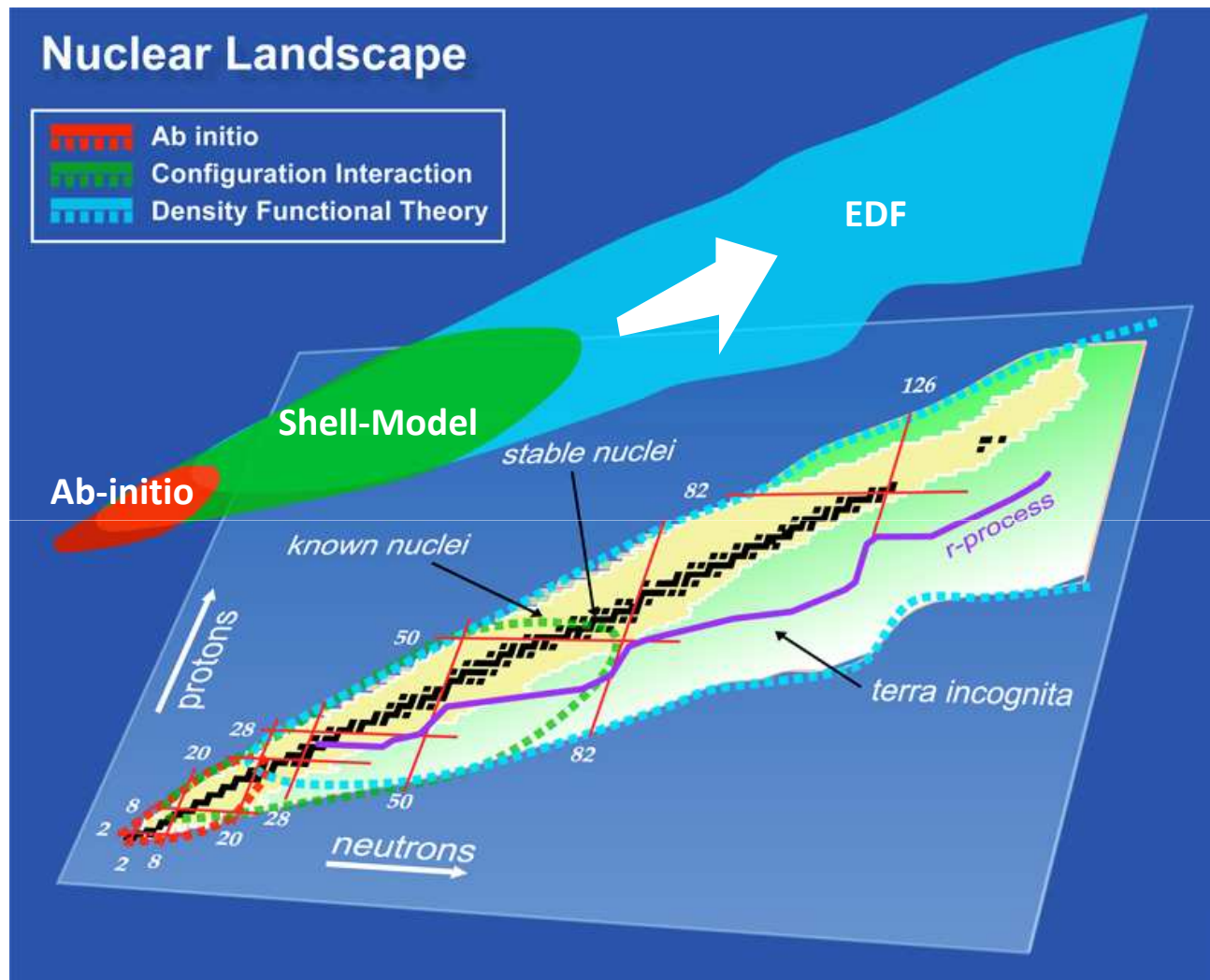


Otsuka et al, arXiv:0908.2607

- ➡ Conventional interaction contain much more than dressed “two-body”
- ➡ Predicting power and interpretation ?
- ➡ Shell model : restricted to -nuclear structure  
-low energy excitation  
- $A < 130$  (now fp shell)

# A unified theory for nuclear structure, reactions and stars

## The Energy Density Functional (EDF) Concept

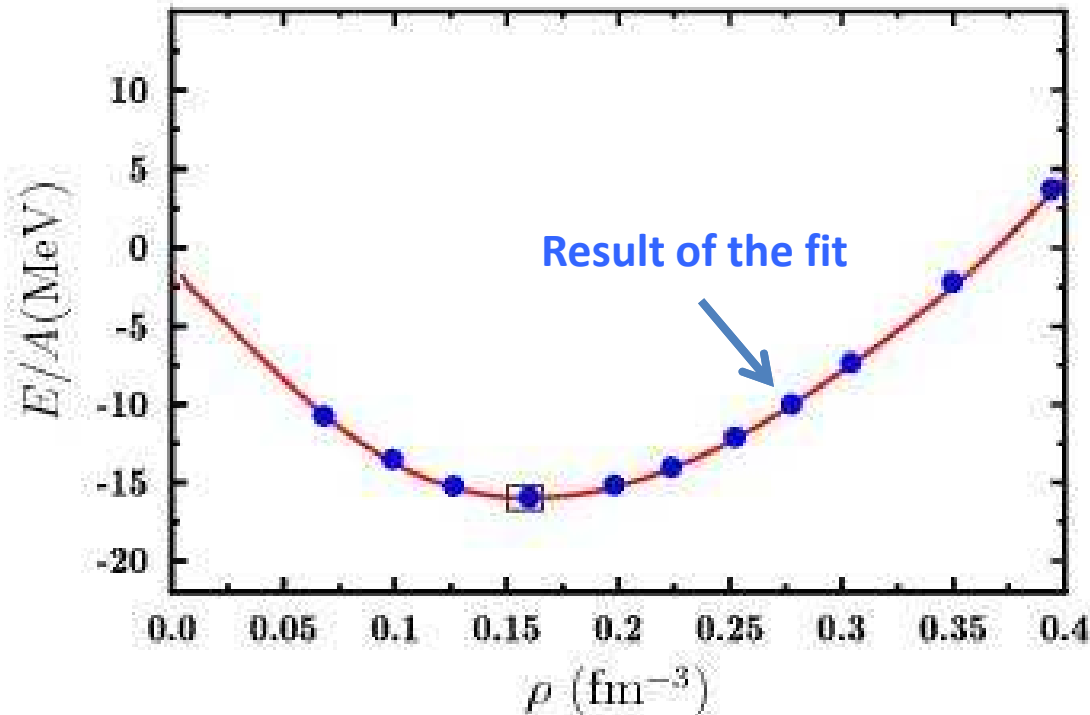


<http://unedf.org/>

# A unified theory for nuclear structure, reactions and stars

## The Energy Density Functional (EDF) Concept

### EDF from a simple perspective



Exercise : fit the curve with

$$E = \left\langle \frac{p^2}{2m} \right\rangle + U[\rho]$$

In nuclear matter:

$$\left\langle \frac{p^2}{2m} \right\rangle = \frac{3}{5} \left( \frac{3\pi^2}{2} \right)^{2/3} \rho^{5/3}$$

Fit with

$$U[\rho] = \sum_n c_n \rho^n$$

➡ An excellent fit is obtained

➡ Example of functional

- Skyrme –Vautherin and Brink, PRC (1972)
- Gogny –Dechargé and Gogny, Phys. Rev. C (1980) .

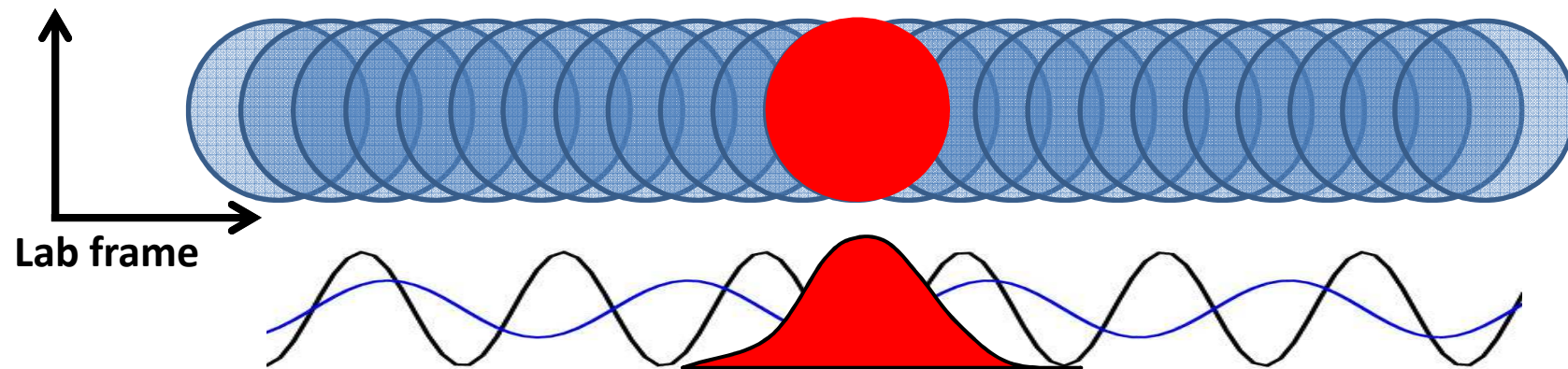
# A unified theory for nuclear structure, reactions and stars

Beyond the simple picture

## EDF:

- ➔ Pre-suppose the existence of a universal functional of the density matrix (looks like Density Functional Theory)
- ➔ Use and abuse of Broken symmetries (should be restored)

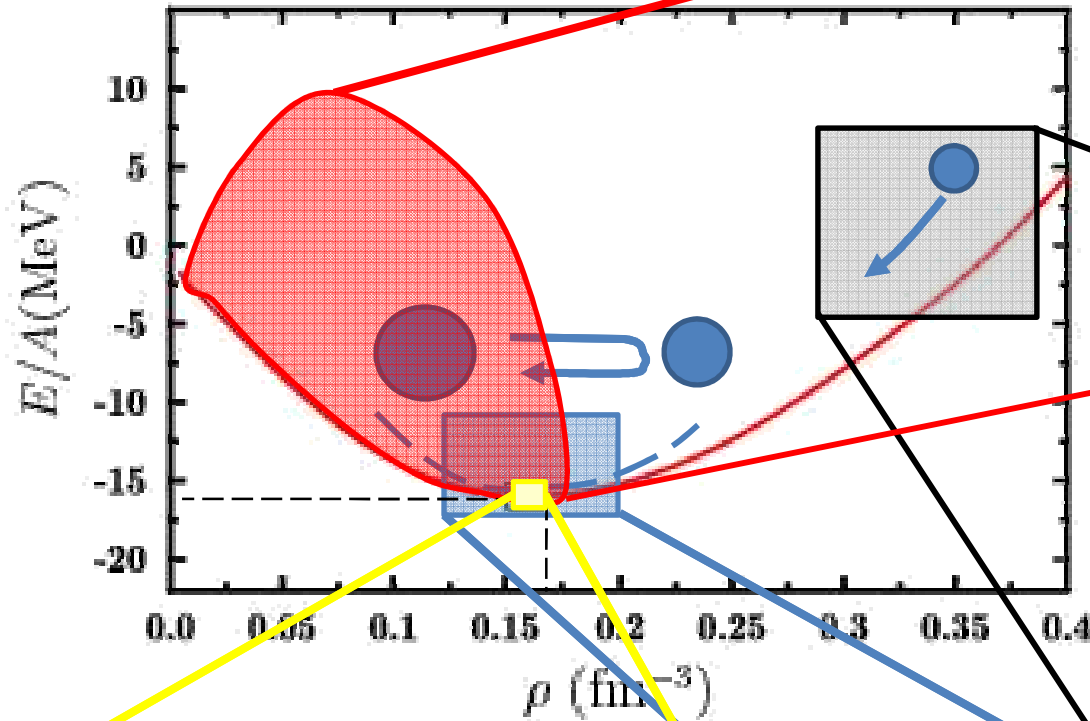
Translation, Rotation, Particle number.



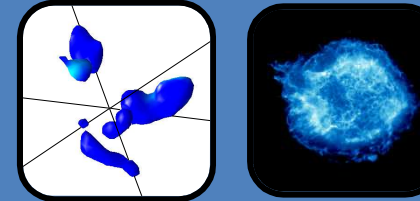
- ➔ Goes much beyond the Hartree-Fock theory
- ➔ Should a priori be considered and named “Ab-initio” theory” (not yet)
- ➔ Around 10-20 parameters-Deviation of 500 keV for ground state energy

# A unified theory for nuclear structure, reactions and stars

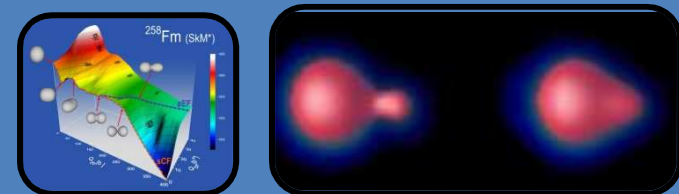
Range of application



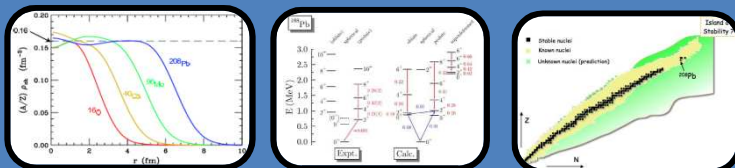
**THERMODYNAMIC**  
(Eq. or non equilibrium)  
(finite or infinite systems)



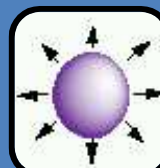
**LARGE AMPLITUDE DYNAMICS**



**GROUND STATE**



**VIBRATION**



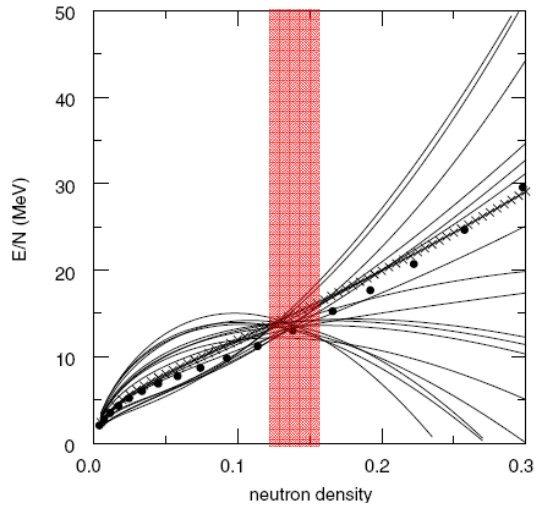
(see lecture M. Grasso)



# A unified theory for nuclear structure, reactions and stars

Uncertainties and Predicting power in conventional EDF

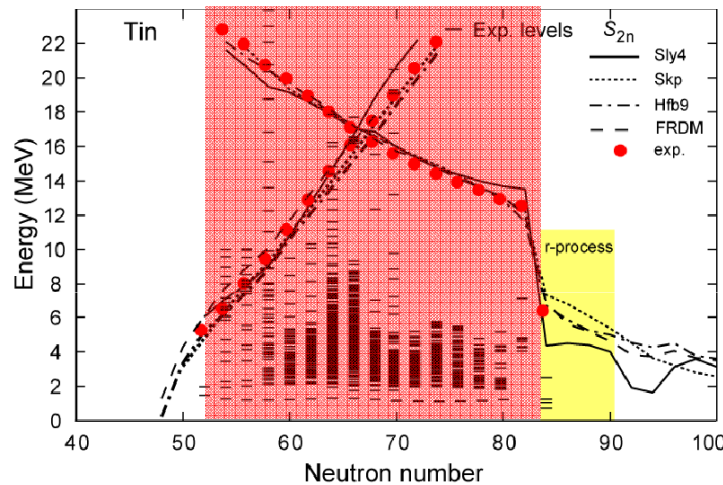
## EOS of pure neutron matter



Brown, PRL85 (2000).

Conventional EDF are adjusted on a selected set of experimental data in finite and infinite systems

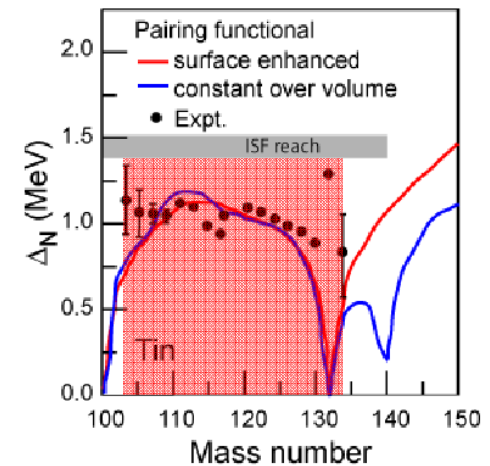
## $S_{2n}$ and $S_{2p}$ in Tin isotopic chain



<http://www.nsl.msu.edu/future/isf>

Experimentally known

## Pairing gap



➡ Large uncertainty in unknown region

## Strategy

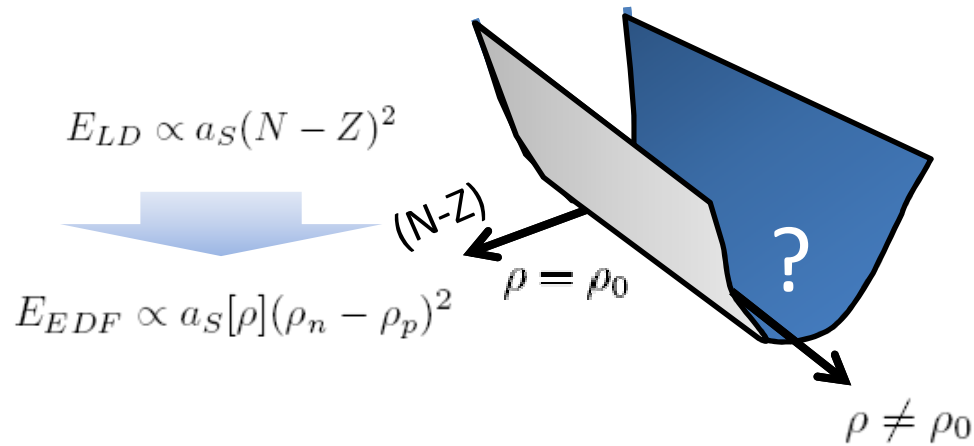
Exp./Th. ➡ Add more data (RIB, reactions, stars)

Th./Exp. ➡ Use the "bottom-up" approach

# A unified theory for nuclear structure, reactions and stars

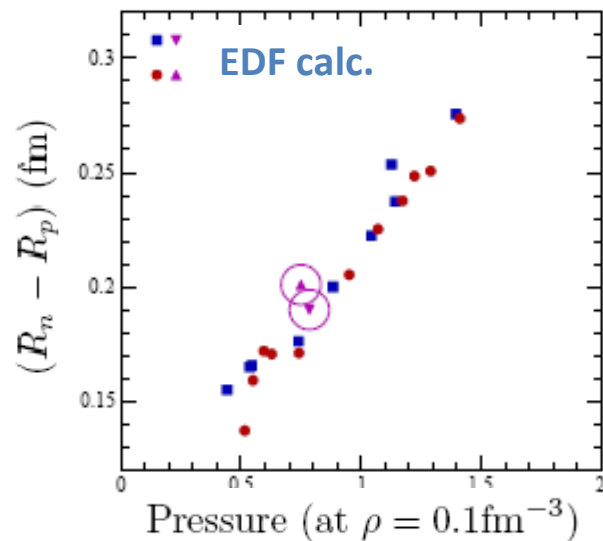
Strategy 1: exploring unknown region

## Illustration with the Symmetry energy



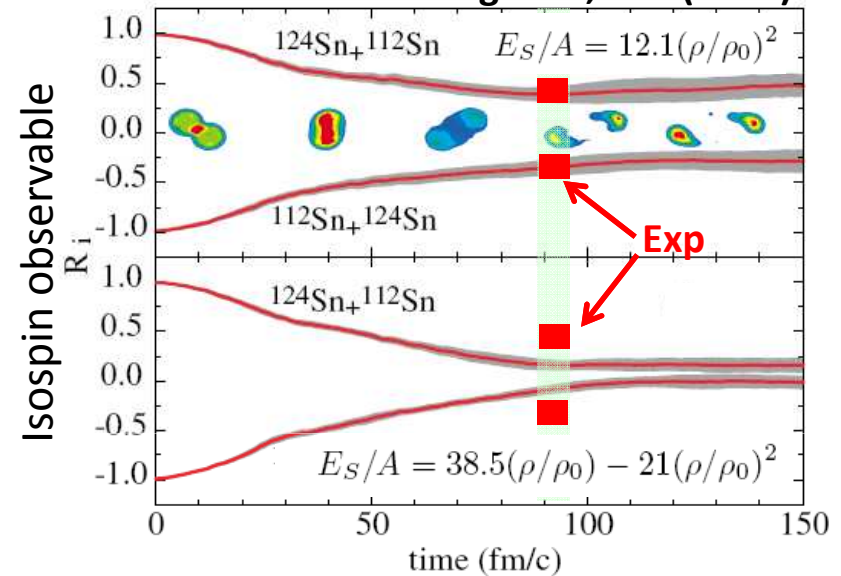
## Constraint from Astrophysics

Steiner et al, Phys. Rep. (2005)



## Constraint from Heavy-Ion reactions

Tsang et al, PRL (2004)



(see lecture M.F. Rivet)

Radius  $\times$  Pressure $^{-1/4} \simeq \text{cte}$

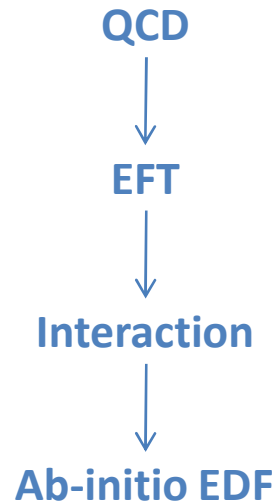
Lattimer et al, Phys. Rep. (2000)

- ➔ Measurement of neutron star radii  
constraint the asymmetry energy
- ➔ Cooling of proto-neutron star
- ➔ Exotic phases (see lecture P. Pizzochero)

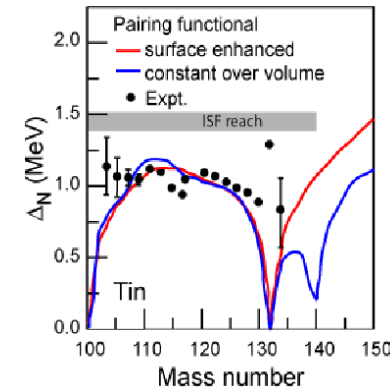
# A unified theory for nuclear structure, reactions and stars

Strategy 2: From QCD to EDF

The long term plan

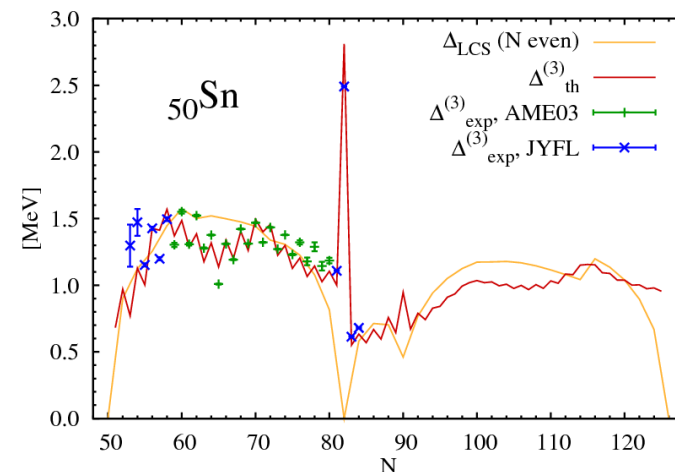


## Illustration with the pairing gap



NSCL  
white paper

$V_{\text{lowk}} + \text{Coulomb}$



Duguet and Lesinski, arXiv:0907.1043

Different strategies

➔ Direct use of new NN interaction  
In specific channels

➔ Compute exactly well identified  
limits and use them in the EDF  
adjustment

➔ Combine Many-body Theory with EDF concept

(see lecture T. Duguet)

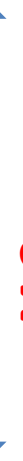
Lectures (Th)

Degrees of Freedom

Lectures (Exp)

**N.Smirnova**

Shell-Model



**M.Grasso**

EDF

**T.Duguet**

From bare to effective int.

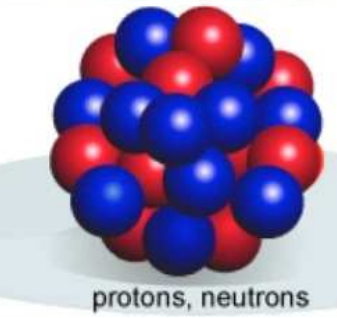


**E. Epelbaum**

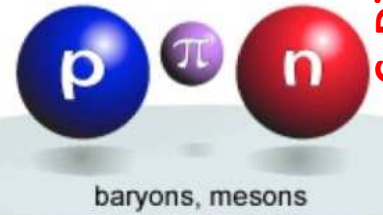
From quark to meson and nuclei

**I.Vidana**

Hypernuclei



protons, neutrons



baryons, mesons



constituent quarks



quarks, gluons

**C. Djalali**

Light mesons



**W. Catford**

Light nuclei

**D.Watts**

Strongly int. matter



**O.Sorlin**

Nuclear Structure



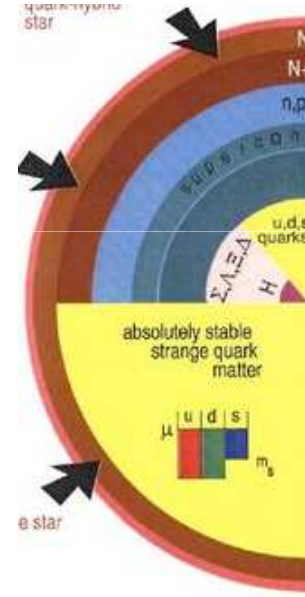
**M.F. Rivet**

Equation Of State



**P.Pizzochero**

Astrophysics





**Many thanks to the lecturers and organizing committee!**