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Simulating the Radio-Frequency Dielectric Response of Relaxor Ferroelectrics: Combination of Coarse-Grained Hamiltonians and Kinetic Monte Carlo Simulations

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The radio-frequency dielectric response of the lead-free $Ba(Zr_{0.5}Ti_{0.5})O_3$ relaxor ferroelectric is simulated using a coarse-grained Hamiltonian. This concept, taken from real-space renormalization group theories, allows us to depict the collective behavior of correlated local modes gathered in blocks. Freeenergy barriers for their thermally activated collective hopping are deduced from this *ab initio*-based approach, and used as input data for kinetic Monte Carlo simulations. The resulting numerical scheme allows us to simulate the dielectric response for external field frequencies ranging from kHz up to a few tens of MHz for the first time and to demonstrate, e.g., that local (electric or elastic) random fields lead to the dielectric relaxation in the radio-frequency range that has been observed in relaxors.

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Relaxors with a perovskite structure form an important family of functional materials that exhibit intriguing dielectric properties [1,2]: the real part of the frequencydependent dielectric permittivity has a maximum with temperature, at T_{max} , while the system remains macroscopically paraelectric down to the lowest temperature, and $T_{\rm max}$ depends on the frequency of the applied electric field, a phenomenon called dielectric relaxation. Different suggestions have been proposed to explain these macroscopic properties, such as nonlocal (electric or elastic) random fields (RFs) (electric or elastic fields on site *i* depending on the chemical disorder surrounding i [3], and the possible existence and interplay of polar nanoregions (PNRs), i.e., polar instabilities that correlate the elementary dipoles on a few lattice constants. The location and properties of these PNRs would be dependent on the local chemical disorder that relaxors can exhibit on one of their sublattices [4].

The dynamics of the electric dipoles of such structures is believed to be associated with characteristic times much larger than typical atomic times, and being temperature dependent (as a result of thermal activation). These large time scales are responsible for the frequency dependence of the dielectric permittivity in the radio-frequency domain (from kHz up to several tens of MHz). Recently, microscopic description of relaxors, based on model Hamiltonians derived from first principles coupled to Monte Carlo (MC) or molecular dynamics (MD) simulations, have provided precious information about the effect of RFs on relaxor properties and the nature of these PNRs [5–12]. In heterovalent relaxors such as PbMg_{1/3}Nb_{2/3}O₃ (PMN) [13–16], the PNRs are suggested to arise from complex phenomena including strong nonlocal electric RFs [17,18]. In contrast, in homovalent relaxors such as $Ba(Zr, Ti)O_3$ (BZT), Ref. [9] numerically found that PNRs appear in regions where the chemical species driving the polar instability (Ti) is more abundant; i.e., it is the *local* RFs arising from the difference in polarizability between Ti and Zr ions that induce relaxor behavior, while nonlocal electric and elastic RFs have a rather negligible effect. Note that local RFs can lead to very long relaxation times in disordered magnets [19], which may also be the case for relaxors [15].

In order to gain a deeper understanding of relaxor ferroelectrics, it is highly desired to have numerical schemes that are able to simulate the most striking characteristics of relaxors, i.e., the radio-frequency dielectric relaxation. However, to the best of our knowledge, such schemes do not exist. One reason behind this paucity is that MD simulations are limited to a few nanoseconds, and thus cannot give access to the time scales required to mimic the radio-frequency dielectric response of relaxors. However, the kinetic Monte Carlo (KMC) method, which we recently applied to simulate the radio-frequency dielectric response of Li-doped KTaO₃ (KLT) [20], is able to reproduce such time scales. Nevertheless, in KLT, the elementary processes driving the dielectric response involve few degrees of freedom (hoppings of individual Li impurities), with rather temperature-independent energy barriers [20], two assumptions clearly not obeyed in relaxor ferroelectrics; this is evidenced, e.g., by the fact that PNRs do not exist above the Burns temperature and that the processes responsible for the dielectric response involve the collective motion of several microscopic degrees of freedom, since a PNR should extend over several unit cells.

In this Letter, we report the development and results of a novel numerical approach able to simulate the radiofrequency dielectric response of relaxors. It is based on a renormalization group (RG) transformation in real space [21], combined with KMC simulations. In particular, this new scheme allows us to describe radio-frequency dielectric relaxation in BZT compatible with the Vogel-Fülcher law [22,23]; it therefore demonstrates the power and promise of such methodology, and that nonlocal electric or elastic RFs are not absolute requirements to generate relaxor behaviors. In other words, local RFs are enough to induce relaxor properties.

We denote by $\{\mathbf{u}_i^{(1)}\}$ the set of the microscopic local modes, and associate to each elementary unit cell *i* a real number $x_i^{(1)}$ characterizing its composition (0 for Zr, 1 for Ti). The $\{x_i^{(1)}\}$ play the role of a set of parameters (not variables) of the microscopic Hamiltonian [24–27], for which we use the following form:

$$H^{(1)}(\{\mathbf{u}_{i}^{(1)}\};\{x_{i}^{(1)}\}) = \underbrace{\sum_{i}}_{local random fields} H^{(1)}_{loc}(\mathbf{u}_{i}^{(1)};x_{i}^{(1)}) + \frac{1}{2} \underbrace{\sum_{i,j,\alpha,\beta}}_{\substack{(i\neq j) \\ (i\neq j)}} \bar{\bar{C}}_{SR,\alpha\beta}^{(1)}(i,j) u_{i\alpha}^{(1)} u_{j\beta}^{(1)} + \frac{1}{2} \sum_{i,j,\alpha,\beta} \bar{\bar{C}}_{LR,\alpha\beta}^{(1)}(i,j) u_{i\alpha}^{(1)} u_{j\beta}^{(1)}, \quad (1)$$

 $\overline{C}_{SR}^{(1)}(i, j)$ and $\overline{C}_{LR}^{(1)}(i, j)$ being the matrices describing the short-range (SR) and dipole-dipole long-range (LR) interaction between local modes in cells *i* and *j*. In such form, the chemical disorder contributes only to the local part, characterizing local RFs arising from the polarizability difference between Ti and Zr ions. References [9,28] have shown that such RFs are sufficient to reproduce several properties of BZT, such as the temperature evolution of the static- and



FIG. 1. Coarse-graining process. (a) Real system: the microscopic local modes interact through the microscopic Hamiltonian $H^{(1)}$. (b) The unit cells are gathered by blocks, and a block variable is defined in each block as the mean local mode. (c) The coarse-grained Hamiltonian $H^{(N)}$ is constructed, preserving the partition function and the macroscopic observables. In case (a) and (c), *P* denotes the density of probability of the microscopic state $\{\mathbf{u}_{\mathbf{i}}^{(1)}\}$ and of the constrained-block state $\{\mathbf{u}_{\mathbf{k}}^{(N)}\}$.

hyperfrequency dielectric permittivity, and the existence of small PNRs; this contrasts with heterovalent relaxors, for which nonlocal RFs (contributions of the chemical disorder from neighboring cells and related to interaction terms of $H^{(1)}$), are large and play a fundamental role in the dielectric properties [17]. We will show here, by neglecting nonlocal RFs, that local RFs in BZT can generate a radio-frequency dielectric relaxation by themselves.

Our approach consists of coarse-graining the system (Fig. 1), i.e., dividing it in $N \times N \times N$ cubic blocks, and defining in each block *k* a "block variable" (or local order parameter) as the mean local mode over the block, $\mathbf{u}_{\mathbf{k}}^{(N)} = (1/N^3) \sum_{i \in k} \mathbf{u}_i^{(1)}$. We also define a local composition in each block, as $x_k^{(N)} = (1/N^3) \sum_{i \in k} x_i^{(1)}$, which takes fractional values $\in [0;1]$, allowing us to define Ti-rich blocks $(x \to 1)$ and Ti-poor ones $(x \to 0)$. The set of block variables $\{\mathbf{u}_{\mathbf{k}}^{(N)}\}$ is used to define an incomplete partition function [29,30],

$$\tilde{Z}^{(N)}(\{\mathbf{u}_{\mathbf{k}}^{(N)}\};\{x_{i}^{(1)}\}) = C \int \dots \int \left[\prod_{\text{blocks } \mathbf{k}} \delta\left(\sum_{i \in \mathbf{k}} \mathbf{u}_{i}^{(1)} - N^{3} \mathbf{u}_{\mathbf{k}}^{(N)}\right)\right] e^{-\beta H^{(1)}(\{\mathbf{u}_{i}^{(1)}\};\{x_{i}^{(1)}\})} \left(\prod_{i} d\mathbf{u}_{i}^{(1)}\right),$$
(2)

by summing over all the microscopic states $\{\mathbf{u}_{i}^{(1)}\}$ such that $\forall k, \sum_{i \in k} \mathbf{u}_{i}^{(1)} = N^{3} \mathbf{u}_{k}^{(N)}$. The $\{\mathbf{u}_{k}^{(N)}\}$ are thus variables of $\tilde{Z}^{(N)}$. The coarse-grained Hamiltonian [29] $H^{(N)}$ is then defined, up to an additive constant, as $H^{(N)}(\{\mathbf{u}_{k}^{(N)}\}; \{x_{i}^{(1)}\}) = -k_{B}Tln\tilde{Z}^{(N)}(\{\mathbf{u}_{k}^{(N)}\}; \{x_{i}^{(1)}\})$. It has the physical meaning of an incomplete free energy, and depends on temperature (in contrast to $H^{(1)}$).

The system of the block variables interacting through $H^{(N)}$ has, by construction, the same partition function as the initial system (up to a multiplicative constant), and thus the same static macroscopic observables. To calculate this

coarse-grained Hamiltonian, we use the following formula [30–32]:

$$\frac{\partial H^{(N)}}{\partial \mathbf{u_n}^{(N)}}(\{\mathbf{u_k}^{(N)}\};\{x_i^{(1)}\}) = -\left\langle \sum_{i \in n} \mathbf{f_i} \right\rangle (\{\mathbf{u_k}^{(N)}\};\{x_i^{(1)}\}),$$
(3)

where $\langle ... \rangle (\{\mathbf{u}_{\mathbf{k}}^{(N)}\})$ denotes thermal conditional average [32] evaluated at fixed $\{\mathbf{u}_{\mathbf{k}}^{(N)}\}$ (see Supplemental Material [33]). $\mathbf{f}_{\mathbf{i}} = -\partial H^{(1)} / \partial \mathbf{u}_{\mathbf{i}}^{(1)}$ is the force on local mode *i*. $H^{(N)}$ is a potential of mean force, as employed in chemical

physics to study chemical reactions along a reaction coordinate [32,34–36]. Here, the reaction coordinate is multidimensional and consists of the set of all the block variables, $\{\mathbf{u}_{\mathbf{k}}^{(N)}\}$.

This coarse-grained Hamiltonian can be approximated by a form identical to that of $H^{(1)}$, i.e., $H^{(N)}(\{\mathbf{u}_{\mathbf{k}}^{(N)}\})$; $\{x_{k}^{(N)}\})$, provided some hypotheses are fulfilled (see Supplemental Material [33]). The most important is that the block size Na_0 remains lower than the correlation length $\xi(\mathbf{T})$; i.e., the local modes must be correlated together all over the block [37,38],

$$H^{(N)}(\{\mathbf{u}_{\mathbf{k}}^{(N)}\};\{x_{k}^{(N)}\}) \approx \sum_{n} H^{(N)}_{\text{loc}}(\mathbf{u}_{\mathbf{n}}^{(N)};x_{n}^{(N)}) + \frac{1}{2} \sum_{n,n',\alpha,\beta} \bar{\bar{C}}^{(N)}_{\text{SR},\alpha\beta}(n,n') u^{(N)}_{n\alpha} u^{(N)}_{n'\beta} + \frac{1}{2} \sum_{n,n',\alpha,\beta} \bar{\bar{C}}^{(N)}_{\text{LR},\alpha\beta}(n,n') u^{(N)}_{n\alpha} u^{(N)}_{n'\beta}.$$
 (4)

The renormalized coefficients $\overline{C}_{SR}^{(N)}(n, n')$ and $\overline{C}_{LR}^{(N)}(n, n')$ describe SR and LR interactions between blocks *n* and *n'*, while the local free energy $H_{loc}^{(N)}(\mathbf{u}; x)$ describes locally the thermodynamics of a block having as local order parameter **u** and chemical composition *x*. The condition $Na_0 < \xi(T)$ ensures that the blocks contain at most one PNR. At a given temperature, several values of *N* are thus possible, but the most convenient is $Na_0 \sim \xi(T)$. MC simulations using $H^{(1)}$ reveal that at low temperature, collective behavior of the local modes is observed within Ti-rich blocks of typical size $2 \times 2 \times 2$ [9]: N = 2 is the block size used here. This may appear small, but within Ti-rich blocks, collective motion of six to eight local modes is sufficient to generate a radio-frequency dielectric response, as we will see.

 $\overline{C}_{SR}^{(N)}$ and $\overline{C}_{LR}^{(N)}$ are computed directly from the coefficients of $H^{(1)}$ (see Supplemental Material [33]). Ideally, the local free energy $H_{loc}^{(N)}$ could be obtained from constrained MD simulations [30,31,38,39]. Here, for simplicity, we use the following phenomenological form, expressed as an energy per five-atom cell: $H_{loc}^{(N)}(\mathbf{u}; x) - H_{loc}^{(N)}(\mathbf{0}; x) = x[H_{loc,Ti}^{(N)}(\mathbf{u}/x) - H_{loc,Ti}^{(N)}(\mathbf{0})]$, with $H_{loc,Ti}^{(N)}(\mathbf{u}) - H_{loc,Ti}^{(N)}(\mathbf{0}) = a'_1(T - T_0)(u_X^2 + u_Y^2 + u_Z^2) + a_{11}(u_X^4 + u_Y^4 + u_Z^4)$ the local free energy per unit cell for a Ti-rich block (x = 1). Within this form, all the blocks are polar under T_0 , not above. The polar character increases with decreasing T and with $x \rightarrow 1$. The coefficients are extracted from microscopic MD simulations, $T_0 = 240$ K (the so-called T^* of BZT, according to Ref. [9]), $a'_1 = 0.053654 \text{ eV}/(\text{Å}^2 \text{ K})$, and $a_{11} = 420.8273 \text{ eV}/\text{Å}^4$. There are eight local minima along the $\langle 111 \rangle$ directions, and saddle points between one minimum and another are taken as the minima of $H_{loc}^{(N)}$



FIG. 2. Upper panels: (a) local free-energy barriers $\Delta F_{\rm loc}(T; x)$ (eV) and (b) hopping times $\tau(T; x) = \tau_0 e^{+\Delta F_{\rm loc}(T; x)/k_B T}$ (s) as a function of temperature for the three Ti-richest blocks (x = 1, x = 0.875, and x = 0.75). Lower panels: temperature evolution of χ' and χ'' . (c) Dielectric susceptibility: real part. (d) Dielectric susceptibility: imaginary part. In panel (c), the lines correspond to a fit according to Ref. [42]. In panel (d), the lines are guides for the eyes.

 $\Delta F_{\text{loc}}(T; x)$ thus depend on temperature [Fig. 2(a)] and on the local chemical composition of the block. The associated transition rates are deduced from transition state theory [40,41], as $r(T; x) = r_0 e^{-\Delta F_{\text{loc}}(T; x)/k_B T}$. The corresponding relaxation times $\tau(T; x) = \tau_0 e^{+\Delta F_{\text{loc}}(T; x)/k_B T}$ are plotted in Fig. 2(b) as a function of temperature. Above 240 K, static PNRs do not exist, while below ~130 K (freezing temperature [9]), the relaxation times increase, tending rapidly but continuously towards a freezing of the polar blocks. The phenomenon of freezing, within this phenomenological description of $H_{\text{loc}}^{(N)}$, corresponds to a sharp but continuous increase of the relaxation times (no divergence at T_f for BZT).

Having the free-energy landscape of the $\{\mathbf{u}_{\mathbf{k}}^{(N)}\}\)$, we can perform a KMC simulation of the dielectric response. A supercell of $12 \times 12 \times 12$ blocks is constructed, starting from a $24 \times 24 \times 24$ supercell of five-atom cells in which the Ti and Zr are randomly distributed with equal probability. Each polar block *n* has a local free-energy surface depending on *T* and chemical composition x_n . However, for physical and practical reasons, we do not consider the hoppings in *all* the blocks as elementary events, because Ti-rich blocks may have large free-energy barriers, and the poorest ones may have very small barriers. Thus, very rare events can coexist with very frequent ones, making the KMC algorithm untractable. Moreover, our phenomenological form for $H_{loc}^{(N)}$ does not stand for Zr-rich blocks, which remain nonpolar down to 0 K [9]. The events kept for the KMC therefore correspond to the hopping times relevant to the radio-frequency dielectric response. This is equivalent to retaining only the Ti-richest blocks as polar (x = 1, x = 0.875, and x = 0.75), the other ones being considered as a dielectric medium. The system thus becomes equivalent to a dipole glass [43] embedded in a dielectric matrix, as in KLT, with the exception that the energy barriers depend on temperature and on local chemical composition, and that each block variable has eight possible local minima along $\langle 111 \rangle$ [9].

The radio-frequency dielectric response is obtained by applying a sinusoidal external electric field along $\mathbf{e}_{\mathbf{x}}$ (unit vector along the pseudocubic [100] axis), $\mathbf{E}_{ext}(t) = E_0 \cos(\omega t) \mathbf{e}_{\mathbf{x}}$. Each block variable *n* feels a local field consisting of this external field plus an internal field $\mathbf{E}_{int}(n)$ associated with the (renormalized) SR and LR interactions between blocks, $\mathbf{E}_{loc}(n) = \mathbf{E}_{ext}(t) + \mathbf{E}_{int}(n)$. We assume that $\mathbf{E}_{loc}(n)$ does not modify the position of the transition states (saddle points of $H_{loc}^{(N)}$), but changes the free-energy barrier from site *k* to *k'* according to $\Delta F_{loc}(T;x) \rightarrow \Delta F_{loc}(T;x) + Z_b^*(\mathbf{u}_k - \mathbf{u}_{k,k'}) \cdot \mathbf{E}_{loc}(n), Z_b^*$ being the block effective charge, \mathbf{u}_k the position of stable site *k* (among the eight possible), and $\mathbf{u}_{k,k'}$ that of the transition state from *k* to *k'*.

When \mathbf{E}_{ext} is applied, the sites $\mathbf{u}_{\mathbf{k}}$ that are in the same direction as \mathbf{E}_{ext} are stabilized, and the energy barriers towards these sites are lowered with respect to the barriers of the backwards motions. Thus, the local order parameters tend to align along the external field, producing a macroscopic polarization P_X . An example at $f \approx 16$ kHz is shown in Fig. 3. However, this alignment occurs with a delay related to the relaxation time of the block variables compared to the external field period ($t_e = 2\pi/\omega$), so



FIG. 3. Example of time evolution of the macroscopic polarization (red curve, in C/m²) under a sinusoidal electric field (black curve, amplitude 1.0×10^7 V/m) of frequency ≈ 16 kHz, for different temperatures.

that P_X takes the form $P_X(t) = P_0(\omega) \cos[\omega t + \phi(\omega)]$ (assuming a linear response). A fit is then performed, providing the amplitude $P_0(\omega)$ and the phase $\phi(\omega)$, from which the real and imaginary parts χ' and χ'' of the dielectric susceptibility are obtained as $\chi' = [P_0(\omega)/\epsilon_0 E_0] \times \cos[\phi(\omega)]$ and $\chi'' = [P_0(\omega)/\epsilon_0 E_0] |\sin[\phi(\omega)]|$.

Figures 2(c) and 2(d) show the temperature evolution of χ' and χ'' in Ba(Zr_{0.5}Ti_{0.5})O₃, for external field frequencies between 16 kHz and 16 MHz. As in KLT, the dielectric relaxation is well reproduced by the KMC simulations, with a maximum of χ' , $T_{max}(\omega)$ evolving with ω and the curves $\chi'(T)$ enveloping each other as ω decreases. The temperature T'_{max} of the maximum of χ'' are $< T_{max}$, as experimentally observed [44–46]. The peak positions are in rather good agreement with experiments [44,46–48]. The values of χ' , however, are ~1 order of magnitude too low compared to experiments [46,48]; we attribute this, as in KLT [20], to the fact that the response of the dielectric matrix is not included, as well as its effect on the PNRs.

At low temperature, the hopping times $\tau(T;x) = \tau_0 e^{+\Delta F_{\text{loc}}(T;x)/k_BT}$ are much larger than the period t_e : the block variables do not have the time to follow the external field (no dielectric response). As *T* increases, $\tau(T;x)$ decreases, but the emerging macroscopic polarization exhibits a delay ϕ as long as $\tau(T;x) > t_e$. When $\tau(T;x) \sim t_e$, a resonance between the hopping times of the PNRs and the characteristic time of external solicitation yields the maximum of the response: **P** and the solicitation **E**_{ext} evolve in phase (the block variables have the time to follow the external field). Above T_{max} , the hopping times are so short that the block variables instantaneously, almost adiabatically, adapt their state to the external field: the dielectric response decreases owing to the thermal agitation, which tends to equalize the probabilities of the different minima.

 $T_{\rm max}$ therefore naturally depends on ω , and the resonance condition $\tau(T_{\max}; x) \sim t_e$; i.e., $f = f_0 e^{-\Delta F_{\text{loc}}(T_{\max}; x)/k_B T_{\max}}$ should provide the relation between T_{max} and the external field frequency f. If there was a single relaxation time (one relaxor entity), with one single hopping barrier U not dependent on T (as in KLT), this would simply provide $f = f_0 e^{-U/k_B T_{\text{max}}}$. Here, several relaxation times $\tau(T; x)$ coexist, associated to the existence of blocks with different chemical compositions x that, moreover, interact with each other (which changes the local barriers). The relation $f(T_{\text{max}})$ is thus complex and is mainly controlled by the form of $H_{\text{loc}}^{(N)}$. Keeping in mind that the phenomenological form chosen for $H_{\text{loc}}^{(N)}$ directly influences $f(T_{\text{max}})$, we can perform a fit of these data (i) on the Arrhenius law, $\ln f = \ln f_0 - U/k_B T_{\text{max}}$, (ii) on the Vogel-Fülcher law, $\ln f = \ln f_0 - U/k_B(T_{\text{max}} - T_f)$, and (iii) on a relation of the form $\ln f = \ln f_0 - \alpha [(T_{\text{max}} - T_1)^2/T_{\text{max}}]$, reflecting the temperature evolution of the free-energy barriers in our phenomenological model [Fig. 2(a)]. We find the data compatible with (ii) and (iii), with $T_f = 127.6$ K, U = 0.019 eV, and $f_0 \sim 1.0 \times 10^{10} \text{ Hz}$ in case (ii), in reasonable agreement with experiments [44], and $f_0 = 2.5 \times 10^7$ Hz, $\alpha = 1.89753$, and $T_1 = 167.3$ K in case (iii).

Finally, we add that two kinds of relaxation are observed in BZT, the first one in the hyperfrequency range and the second one in the radio-frequency range [47,49]. While the classical MD simulations of Refs. [28,50] showed that the first relaxation is due to single Ti motions, our present method reveals that the second relaxation instead originates from collective motions of local modes inside PNRs, demonstrating the complementary of classical MD (which can mimic the faster individual hoppings, but not the slower collective dynamics in the whole PNRs) and our developed scheme (which can model such latter dynamics, as a result of our block compartments).

In summary, we have developed a methodology to simulate the radio-frequency dielectric response of relaxor materials. It is based on a RG transformation combined with KMC simulations. We have shown that, in BZT, this methodology allows to model the collective motions of correlated local modes and reproduces the radio-frequency dielectric relaxation for the first time ever with a potentially fully atomistic-based method. In particular, the local RFs related to the difference in polarizability between Ti and Zr ions are sufficient to explain radio-frequency relaxation, an important step toward a deep understanding of relaxors (nonlocal electric and elastic RFs are weak in BZT [9], while they play an important role in heterovalent relaxors [17]; this implies that they likely contribute to the radiofrequency response of PMN and similar systems). Our approach still needs to be tested on systems with larger correlation lengths, for which theoretical difficulties have been pointed out in the past [51,52]; this will be the topic of a future study. In such systems, it may be more difficult to construct an approximate coarse-grained Hamiltonian as in Eq. (4). We hope that our approach will be applied and/or generalized to many complex materials and phenomena in the future.

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- [1] G. Burns and F. H. Dacol, Phys. Rev. B 28, 2527 (1983).
- [2] L. E. Cross, Ferroelectrics 76, 241 (1987).
- [3] W. Kleemann, J. Dec, and S. Miga, Phase Transitions 88, 234 (2015).
- [4] J.-M. Kiat and B. Dkhil, in Handbook of Advanced Dielectric, Piezoelectric and Ferroelectric Materials: Synthesis, Properties and Applications, edited by Z. G. Ye (Woodhead Publishing Ltd., Cambridge, 2007), p. 391.
- [5] B. P. Burton, E. Cockayne, S. Tinte, and U. V. Waghmare, Phase Transitions 79, 91 (2006).

- [6] B. P. Burton, E. Cockayne, and U. V. Waghmare, Phys. Rev. B 72, 064113 (2005).
- [7] B. P. Burton, E. Cockayne, S. Tinte, and U. V. Waghmare, Phys. Rev. B 77, 144114 (2008).
- [8] S. Tinte, B. P. Burton, E. Cockayne, and U. V. Waghmare, Phys. Rev. Lett. 97, 137601 (2006).
- [9] A. R. Akbarzadeh, S. Prosandeev, E. J. Walter, A. Al-Barakaty, and L. Bellaiche, Phys. Rev. Lett. 108, 257601 (2012).
- [10] S. Prosandeev, D. Wang, and L. Bellaiche, Phys. Rev. Lett. 111, 247602 (2013).
- [11] I. Grinberg, P. Juhas, P. K. Davies, and A. M. Rappe, Phys. Rev. Lett. 99, 267603 (2007).
- [12] I. Grinberg, Y.-H. Shin, and A. M. Rappe, Phys. Rev. Lett. 103, 197601 (2009).
- [13] D. Viehland, S. Jang, L. E. Cross, and M. Wuttig, J. Appl. Phys. 68, 2916 (1990).
- [14] V. Westphal, W. Kleemann, and M. D. Glinchuk, Phys. Rev. Lett. 68, 847 (1992).
- [15] G. Xu, G. Shirane, J. R. D. Copley, and P. M. Gehring, Phys. Rev. B 69, 064112 (2004).
- [16] I.-K. Jeong, T. W. Darling, J. K. Lee, T. Proffen, R. H. Heffner, J. S. Park, K. S. Hong, W. Dmowski, and T. Egami, Phys. Rev. Lett. 94, 147602 (2005).
- [17] A. Al-Barakaty, S. Prosandeev, D. Wang, B. Dkhil, and L. Bellaiche, Phys. Rev. B 91, 214117 (2015), and references therein.
- [18] D. Phelan, C. Stock, J. A. Rodriguez-Rivera, S. Chi, J. Leao, X. Long, Y. Xie, A. A. Bokov, Z.-G. Ye, P. Ganesh, and P. M.Gehring, Proc. Natl. Acad. Sci. U.S.A. 111, 1754 (2014).
- [19] D. S. Fisher, Phys. Rev. Lett. 56, 416 (1986).
- [20] G. Geneste, J.-M. Kiat, H. Yokota, and Y. Uesu, Phys. Rev. B 83, 184202 (2011).
- [21] J. J. Binney, N. J. Dowrick, A. J. Fisher, and M. E. J. Newman, *The Theory of Critical Phenomena. An Introduction to the Renormalization Group* (Clarendon Press, Oxford, 1999).
- [22] H. Vogel, Phys. Z. 22, 645 (1921).
- [23] G. S. Fülcher, J. Am. Ceram. Soc. 8, 339 (1925).
- [24] W. Zhong, D. Vanderbilt, and K. M. Rabe, Phys. Rev. B 52, 6301 (1995).
- [25] W. Zhong, D. Vanderbilt, and K. M. Rabe, Phys. Rev. Lett. 73, 1861 (1994).
- [26] I. A. Kornev, L. Bellaiche, P.-E. Janolin, B. Dkhil, and E. Suard, Phys. Rev. Lett. 97, 157601 (2006).
- [27] I. A. Kornev, S. Lisenkov, R. Haumont, B. Dkhil, and L. Bellaiche, Phys. Rev. Lett. 99, 227602 (2007).
- [28] D. Wang, J. Hlinka, A. A. Bokov, Z.-G. Ye, P. Ondrejkovic, J. Petzelt, and L. Bellaiche, Nat. Commun. 5, 5100 (2014).
- [29] K. Binder, Rep. Prog. Phys. 50, 783 (1987).
- [30] G. Geneste, Phys. Rev. B 79, 064101 (2009).
- [31] G. Geneste, J. Phys. Condens. Matter 23, 125901 (2011).
- [32] M. Sprik and G. Cicotti, J. Chem. Phys. 109, 7737 (1998).
- [33] See Supplemental Material at http://link.aps.org/ supplemental/10.1103/PhysRevLett.116.247601 for detailed description, and construction of the coarse-grained hamiltonian, and for details about the KMC simulation.
- [34] E. Paci, G. Cicotti, M. Ferrario, and R. Kapral, Chem. Phys. Lett. 176, 581 (1991).

- [35] E. Darve, in *Free Energy Calculations. Theory and Applications in Chemistry and Biology*, edited by C. Chipot and A. Pohorille (Springer, New York, 2007), pp. 119–170.
- [36] E. Darve and A. Pohorille, J. Chem. Phys. 115, 9169 (2001).
- [37] A. Tröster, C. Dellago, and W. Schranz, Phys. Rev. B 72, 094103 (2005).
- [38] G. Geneste, Comput. Phys. Commun. 181, 732 (2010).
- [39] A. Kumar and U. V. Waghmare, Phys. Rev. B 82, 054117 (2010).
- [40] H. Eyring, J. Chem. Phys. 3, 107 (1935).
- [41] P. Hänggi, P. Talkner, and M. Borkovec, Rev. Mod. Phys. 62, 251 (1990).
- [42] Z.-Y. Cheng, R. S. Katiyar, X. Yao, and A. S. Bhalla, Phys. Rev. B 57, 8166 (1998).
- [43] D. Sherrington, Phys. Rev. Lett. 111, 227601 (2013).
- [44] A. Dixit, S. B. Majumder, R. S. Katiyar, and A. S. Bhalla, J. Mater. Sci. 41, 87 (2006).

- [45] W. Kleemann, S. Miga, J. Dec, and J. Zhai, Appl. Phys. Lett. 102, 232907 (2013).
- [46] M. Usman, A. Mumtaz, S. Raoof, and S. K. Hasanain, Appl. Phys. Lett. 103, 262905 (2013).
- [47] D. Nuzhnyy, J. Petzelt, M. Savinov, T. Ostapchuk, V. Bovtun, M. Kempa, J. Hlinka, V. Buscaglia, M. T. Buscaglia, and P. Nanni, Phys. Rev. B 86, 014106 (2012).
- [48] T. Maiti, R. Guo, and A. S. Bhalla, J. Am. Ceram. Soc. 91, 1769 (2008).
- [49] J. Petzelt, D. Nuzhnyy, M. Savinov, V. Bovtun, M. Kempa, T. Ostapchuk, J. Hlinka, G. Canu, and V. Buscaglia, Ferroelectrics 469, 14 (2014).
- [50] D. Wang, A. A. Bokov, Z.-G. Ye, J. Hlinka, and L. Bellaiche, Nat. Commun. 7, 11014 (2016).
- [51] E. Pytte, Y. Imry, and D. Mukamel, Phys. Rev. Lett. 46, 1173 (1981).
- [52] J.Z. Imbrie, Phys. Rev. Lett. 53, 1747 (1984).