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Daniele Muraro, Nathan Mellor, Michael P. Pound, Hanna Help, Mikaël Lucas, et al.. Integration of hormonal signaling networks and mobile microRNAs is required for vascular patterning in *Arabidopsis* roots. Proceedings of the National Academy of Sciences of the United States of America , National Academy of Sciences, 2014, 111 (2), pp.857-862. <10.1073/pnas.1221766111>. <hal-00941028>

HAL Id: hal-00941028

<https://hal.inria.fr/hal-00941028>

Submitted on 12 Jan 2015

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Integration of hormonal signaling networks and mobile microRNAs is required for vascular patterning in *Arabidopsis* roots

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Edited by Ben Scheres, Wageningen University, Wageningen, The Netherlands, and accepted by the Editorial Board December 5, 2013 (received for review December 13, 2012)

As multicellular organisms grow, positional information is continually needed to regulate the pattern in which cells are arranged. In the *Arabidopsis* root, most cell types are organized in a radially symmetric pattern; however, a symmetry-breaking event generates bisymmetric auxin and cytokinin signaling domains in the stele. Bidirectional cross-talk between the stele and the surrounding tissues involving a mobile transcription factor, SHORT ROOT (SHR), and mobile microRNA species also determines vascular pattern, but it is currently unclear how these signals integrate. We use a multicellular model to determine a minimal set of components necessary for maintaining a stable vascular pattern. Simulations perturbing the signaling network show that, in addition to the mutually inhibitory interaction between auxin and cytokinin, signaling through SHR, microRNA165/6, and PHABULOSA is required to maintain a stable bisymmetric pattern. We have verified this prediction by observing loss of bisymmetry in *shr* mutants. The model reveals the importance of several features of the network, namely the mutual degradation of microRNA165/6 and PHABULOSA and the existence of an additional negative regulator of cytokinin signaling. These components form a plausible mechanism capable of patterning vascular tissues in the absence of positional inputs provided by the transport of hormones from the shoot.

mathematical modeling | plant development

Plant vascular tissues (xylem and phloem) provide long distance transport between the root and the shoot. In *Arabidopsis* roots, the xylem and phloem are arranged in a bisymmetric pattern (Fig. 1A). There is a single xylem axis, with two protoxylem cells at the marginal positions and metaxylem cells in the central position. This axis is flanked by two domains of procambial cells and two phloem poles.

Like many other developmental processes in roots, such as the positioning of lateral roots, the specification of the root pole, or the regulation of the root stem cell niche (1), the specification of a vascular pattern is the direct result of the heterogeneous distribution of the hormone auxin (2). Asymmetries in auxin distribution are largely controlled through the subcellular localization of the PIN-formed (PIN) class of auxin efflux carriers (3). Mathematical modeling of PIN-mediated auxin fluxes can generate auxin maxima at the root tip and the sites of organ initiation (4, 5). However, these models have only considered auxin flow within a 2D longitudinal root section and did not investigate the influence of the signaling network responsible for auxin perception at a subcellular level or its possible feedbacks on auxin levels. A 3D model of auxin transport was presented by

Swarup et al. (6), but this model only considers the outer three cell layers (epidermis, cortex, and endodermis).

Mathematical models should account for the global effect of multiple hormonal pathways, consider where these hormones are synthesized, how they move between tissues, and how the pathways communicate within and between cells. Although studies investigating the role of auxin-cytokinin cross-talk in roots have identified nodes at which the hormonal pathways interact (2, 7), they have been unable to show the precise relationship between these two pathways or predict the effect that altering one component would have on the system as a whole.

In root vascular tissues, there is an auxin response maximum throughout the xylem axis (2, 8). This response domain is flanked by two domains of high cytokinin (ck) activity within the procambial and phloem cells (2, 9). High ck signaling promotes the expression and localization on the lateral membranes of PIN1, PIN3, and PIN7. High auxin signaling promotes the

Significance

The vascular tissues form a continuous network providing the long-distance transport of water and nutrients in all higher plants (tracheophytes). To incorporate separate organs into this network, it is essential that the position of different vascular cell types is tightly regulated. Several factors required for root vascular patterning (including hormones and gene products) have previously been identified in the model plant *Arabidopsis*. We have now established a mathematical model formalizing the interaction between these factors, allowing us to identify a minimal regulatory network capable of maintaining a stable vascular pattern in *Arabidopsis* roots. We envisage that this model will help future researchers understand how similar regulatory units can be applied to create alternative patterns in other species.

Author contributions: D.M., N.M., H.M.B., T.C.H., J.R.K., M.J.B., and A.B. designed research; D.M., N.M., and A.B. performed research; M.P., H.H., M.L., J.C., C.G., T.P.P., and Y.H. contributed new reagents/analytic tools; D.M., N.M., M.P., and A.B. analyzed data; and D.M., N.M., and A.B. wrote the paper.

The authors declare no conflict of interest.

This article is a PNAS Direct Submission. B.S. is a guest editor invited by the Editorial Board. Freely available online through the PNAS open access option.

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This article contains supporting information online at www.pnas.org/lookup/suppl/doi:10.1073/pnas.1221766111/-DCSupplemental.

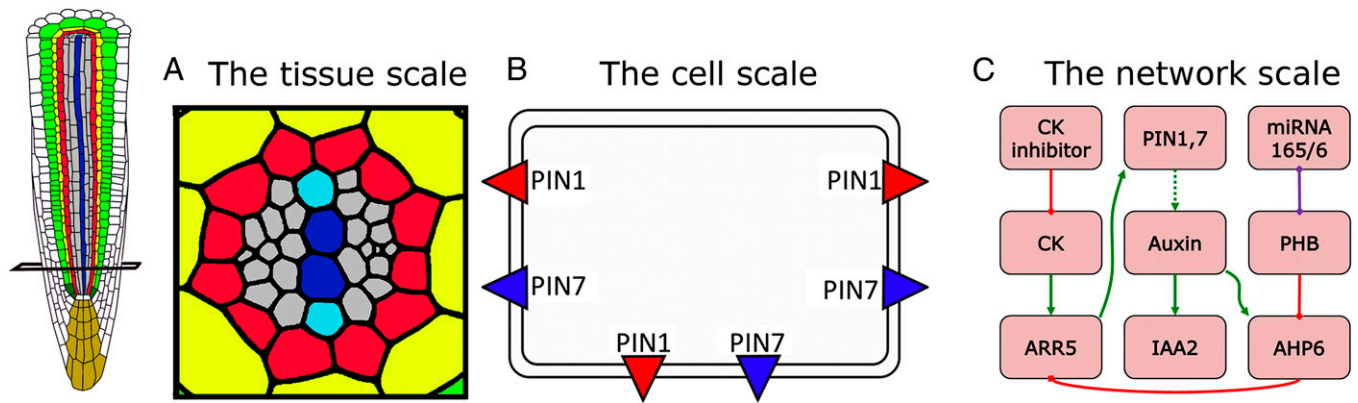


Fig. 1. The multicellular model considers three levels of regulation. (A) Tissue scale. We use a cross-section through the *Arabidopsis* root as a template for our model. The cell lineages are color-coded as follows: yellow, endodermis; red, pericycle cells; gray, procambial cells and phloem initials; blue, the xylem axis (the protoxylem is shown in a lighter shade). (B) Cell scale. Each cell contains the auxin efflux proteins (PIN1, PIN3, and PIN7) positioned on the lateral membranes where they have been experimentally observed. (C) Network scale. The regulatory network has been embedded within each cell. Green arrows indicate transcriptional activation. The dotted green arrow indicates that auxin distribution is affected by polar auxin transport. Red bars indicate repression. The purple bar represents the mutual degradation of mRNAs.

expression of the ck signaling inhibitor *AHP6*. *PHABULOSA* (*PHB*) acts redundantly with other members of the class III homeodomain-leucine zipper (Hd-zip) transcription factor gene family to repress *AHP6* expression in a dose-dependent manner (10). In turn, *PHB* levels are determined through the degradation of *PHB* mRNA by microRNA165/6 (miRNA165/6) (10, 11). The asymmetric input of hormones into the root meristem also affects root vascular patterning. During embryogenesis, there is a migration of auxin response from the cotyledons to the root pole (2), and in the growing root, both auxin and ck are transported through the phloem (12–14).

Here, we present a model for investigating auxin fluxes within the radial root cross-section (Fig. 1). We show that interplay between these elements is capable of generating realistic patterns and that both hormonal signaling and mobile miRNA are required to specify the correct domain of auxin response.

Results

Localization of PINs on the Lateral Membranes Is Sufficient to Generate High Auxin Response in the Xylem Axis. In addition to regulating the rootward flux of auxin in the root meristem (4, 15, 16), PIN1, PIN3, and PIN7 act in consort to channel a radial flow of auxin to the xylem axis (2). To test whether the radial transport of auxin alone offers a plausible mechanism to generate an auxin response maximum in the xylem axis, we developed a 2D computational model of the root vascular tissues based on realistic cell geometries taken from a cross-section through the root proximal meristem (*SI Appendix*, Fig. S1). Ordinary differential equations were embedded in each cell within this tissue geometry, and as in ref. 17, the temporal evolution of auxin concentration $[Aux]_i$ in a given cell i is given by

$$\frac{d[Aux]_i}{dt} = -\frac{1}{V_i} \sum_{n \in N_i} S_{i,n} (J_{i \rightarrow n}^D + J_{i \rightarrow n}^T) + p_{Aux} - d_{Aux}[Aux]_i,$$

where V_i is the cell volume, N_i is the set of neighboring cells of cell i , $S_{i,n}$ is the exchange surface between cells i and n , $J_{i \rightarrow n}^D = P_{Aux}([Aux]_i - [Aux]_n)$ represents the passive auxin diffusion at rate P_{Aux} using Fick's First Law, and p_{Aux} and d_{Aux} are the respective intracellular biosynthesis and degradation rates of auxin. Active transport of auxin depends on the efficiency of PIN transporters, and therefore, $J_{i \rightarrow n}^T = T_{Aux}([Aux]_i [PIN]_{p,i,n} - [Aux]_n [PIN]_{p,n,i})$ is the flux of auxin caused by active transport at

rate T_{Aux} proportional to PIN protein concentration ($[PIN]_{p,i,n}$) on $S_{i,n}$. Individual parameters were selected based on the current literature or reasonable estimates. Specific parameters are discussed further in *SI Appendix*.

We used the CellSeT software (18) to determine the polarity of PIN:GFP from confocal images and examined 3D reconstructions of immunolocalizations for plants labeled with α -PIN1 or α -GFP antibodies (*SI Appendix*, Figs. S2–S5).

PIN proteins were incorporated onto specific cell membranes in our multicellular geometry (Fig. 1B and *SI Appendix*, Fig. S6); the total concentration of PIN proteins in each cell was set to zero or one and proportionally divided on any given membrane, resulting in a concentration of $[PIN]_{p,n,i}$. We modeled auxin flux through the root and predicted the response by simulating the activity of the primary auxin response gene *IAA2*. Under these conditions, our model showed that the experimentally observed localization of the PINs on lateral membranes was capable of producing an auxin signaling maximum in the xylem axis closely resembling the observed pattern of *IAA2* (Fig. 2A and B and *Movie S1*). The positioning of this auxin signaling maximum persisted, regardless of whether auxin biosynthesis was assumed to be distributed uniformly across the root or localized in the phloem. We investigated the effect that PIN1, PIN3, and PIN7 exerted individually by running simulations with just one of three PINs (*SI Appendix*, Fig. S6). Simulations that considered only PIN1 or PIN7 did not show significant differences from the previous simulation, suggesting that these proteins play redundant roles in directing the auxin maximum (Fig. 2C and *Movies S2* and *S3*). PIN3 activity alone was insufficient to reproduce the auxin signaling maximum seen in WT plants (*Movie S4*). To simplify our subsequent simulations and construct the minimum network required for vascular patterning, from this point, we only consider PIN7. Collectively, the simulations described above highlight that the observed localization of PINs on the lateral membranes is sufficient to direct auxin response to the xylem axis. We then applied our model to determine the minimum set of components that can operate alongside PIN7 during vascular patterning.

Integrating Signaling Networks into a Multicellular Model of Vascular Patterning. We have incorporated the regulatory pathways that are known to determine vascular patterning (2, 10) in the model by including the following processes (Fig. 1C): (i) The transcription of *IAA2* and *AHP6* is promoted by auxin; (ii) *AHP6* transcription is negatively regulated by PHB; (iii) *PHB* mRNA

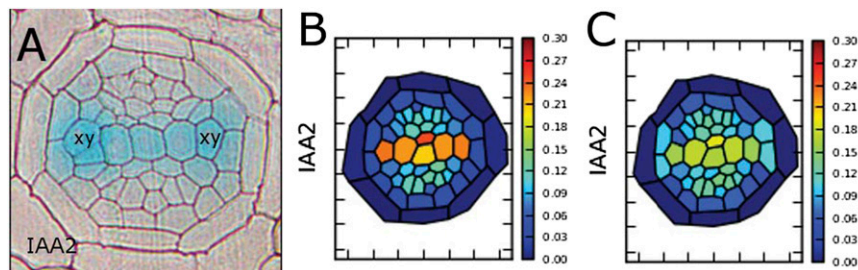


Fig. 2. Coordination of PINs in specifying the auxin response. (A) *pIAA2::GUS* marks high auxin response in the xylem axis (xy). (B) Predicted auxin response based on the collective output of PIN1, PIN3, and PIN7. (C) A similar auxin response is predicted when only PIN7 is active.

and miRNA165/6 mutually degrade each other; (iv) miRNA165/6 is produced in the endodermis but diffuses throughout the vascular tissues; (v) *ARR5* transcription is activated by ck and repressed by *AHP6*; and (vi) *PIN7* transcription is activated by ck response (*ARR5*).

We derived a system of ordinary differential equations governing the dynamics of the interaction network that was embedded in our multicellular geometry. Based on previous subcellular models (19, 20), the transcription of all genes was modeled using Hill Kinetics, with the mRNA M_i produced through the transcription of gene i in response to transcriptional regulator P_j given by

$$\frac{dM_i}{dt} = p_{M_i} F_{M_i} - d_{M_i} M_i,$$

$$F_{M_i} := b_i + \frac{\sum_{j \in A_i} (P_j / \theta_{P_j})^{h_{ij}}}{1 + \sum_{j \in A_i} (P_j / \theta_{P_j})^{h_{ij}} + \sum_{j \in R_i} (P_j / \theta_{P_j})^{h_{ij}}},$$

where A_i and R_i are the sets of activators and repressors acting on gene i , respectively, p_{M_i} and d_{M_i} are production and degradation rates of M_i , respectively, b_i is a dimensionless parameter regulating basal transcription, θ_{P_j} is a protein–DNA binding threshold, and h_{ij} is the Hill coefficient of protein P_j when acting on gene i . Translation of the protein P_i from M_i is then governed by the equation

$$\frac{dP_i}{dt} = p_{P_i} M_i - d_{P_i} P_i, \quad [1]$$

where p_{P_i} and d_{P_i} are the production and degradation rates of P_i , respectively. Mutual degradation of *PHB* mRNA ($[PHB_m]$) and miRNA ($[miRNA165/166]$) is governed by the reaction $[PHB_m] + [miRNA165/166] \rightarrow \emptyset$ at rate $d_{miRNA/mRNA}$, which in the evolution equations of $[PHB_m]$ and $[miRNA165/166]$, is described by the negative term $-d_{miRNA/mRNA} [PHB_m] [miRNA165/166]$ (21). Passive diffusion of ck, miRNA165/6, and SHORT ROOT (*SHR*) are governed by the same rules as auxin. The full set of reactions constituting this signaling network is listed in *SI Appendix*, section 1.

Mutual Degradation of miR165/6 and PHB Generates Sharp Boundaries of Gene Expression. We first considered mobile miRNA165/6. The fate of miRNA after it has regulated its target is not well-understood. However, a previous study has shown that the degradation of miRNA223 is accelerated when its target is present (22). Additionally, a previous modeling study has postulated that the mutual degradation of target and miRNA can sharpen the boundary of its mRNA target's spatial distribution (21). Levine et al. (21) developed a general model based on reaction–diffusion equations in one spatial dimension, in which small RNA molecules interact with a target gene and move from cell to cell through diffusion. Although diffusion generally smoothes spatial

expression patterns, Levine et al. (21) found that intercellular mobility of small RNAs sharpens the boundaries between target expression domains in a robust manner, and this sharpening was because of the codegradation of both small RNAs and their targets. The codegradation means that, when the small RNAs diffuse into areas of low gene expression, they can eliminate the expression of their targets in these cells, whereas they are less able to affect the levels of target genes in cells in which the target is expressed abundantly. Carlsbecker et al. (10) proposed that a similar mechanism may operate during vascular patterning as endodermally produced miRNA165/6 moves into the vascular cylinder and encounters its target mRNA (*PHB*); however, they did not test this prediction with a mathematical model and did not explore whether the mutual degradation of miRNA165/6 and *PHB* mRNA is required to produce the observed expression patterns.

We introduced the molecular circuitry into our model to compare scenarios in which the degradation of both *PHB* and miRNA occurs mutually. In the former scenario, we assume that binding of miRNA and *PHB* mRNA targets both molecules for degradation, and in the latter scenario, miRNA accelerates the degradation of *PHB* but is not itself consumed. In simulations without codegradation of miRNA and target, we observed a diffuse gradient of *PHB*, resulting in accumulation of *AHP6* throughout the xylem axis and ectopically in the procambium (*Movie S5*). By including the mutual degradation, we observed a much sharper boundary of *PHB* with high expression in the central cells and low expression in the outer cell layers, resulting in a much greater repression of *AHP6* in the central cells. These simulations suggest that, under our parameter set, the mutual degradation of these components provides a suitable mechanism to generate distinct domains of expression of both components, where the expression of *PHB* and other network components are remarkably similar to the experimentally observed data (Fig. 3 *A* and *B* and *Movie S6*). We investigated the effect that doubling or halving these parameters had on this gradient and observed that, in almost every scenario, incorporating a mutual degradation between these two components resulted in a sharper gradient of *PHB* expression (*SI Appendix*, section 2).

Additional Component Is Required to Position the ck Signaling Maximum Correctly. When *PHB* regulation by miRNA165/6 is incorporated into our model, our simulations recreate the experimentally observed responses of some but not all markers. The predicted outputs of *IAA2* and *AHP6* match the data; *IAA2* expression has been observed throughout the xylem axis, and *AHP6* has only been observed in the marginal positions and the protoxylem-associated pericycle cells (Fig. 3 *E* and *F* and *Movie S6*). However, whereas in our experimental observations, *ARR5*, *PIN7*, and the synthetic cytokinin reporter *TCSn* (23) were always absent throughout the xylem axis (Fig. 3 *D* and *SI Appendix*, Fig. *S7*), our simulations predict that both *ARR5* and ck are present in the metaxylem (Fig. 3 *C* and *D* and *Movie S6*), suggesting that an additional factor may be required to restrict ck homeostasis/

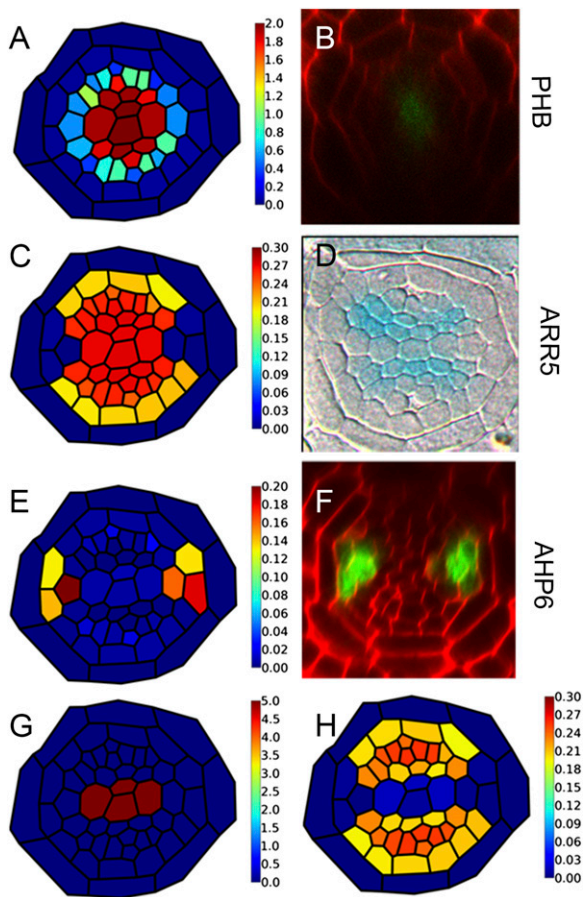


Fig. 3. Integration of hormonal signaling and Hd-zip activity is sufficient to create a bisymmetric auxin response. (A–F) Model predictions and experimental observations of key marker genes are shown side by side. (A and B) Simulated *PHB* mRNA levels are shown alongside the experimentally observed pattern of *pPHB::PHB::GFP*, (C and D) predicted *ARR5* output is shown alongside *pARR5::GUS*, and (E and F) predicted *AHP6* output is shown alongside *pAHP6::GFP* activity. These simulations are based on the original regulatory network lacking an additional inhibitor of ck. Although the simulations recover the observed pattern of *PHB* and *AHP6*, they fail to recover the observed pattern of *ARR5*. (G) By including the repressive effect of CKIN in the metaxylem, (H) our model reproduces the experimental pattern of *pARR5::GUS*.

signaling in these cells. Likely candidates include type A ARRs, which are known to inhibit ck signaling (24), or a member of the CKX family of proteins, which is known to degrade ck (25). Inclusion of either a *CKX* gene or an inhibitor of ck signaling driven in the metaxylem (CKIN) into our model (Fig. 3G) alters the pattern of ck response, such that all network components become similar to experimental observations (Fig. 3H and [Movie S7](#)).

Phloem Transport Does Not Provide an Essential Source of Positional Information During Root Vascular Patterning. Transport of both auxin and ck through the phloem provides an important source of hormones in the root meristem (12, 13). Plants with impaired phloem transport show unstable patterns of auxin response in the root meristem (14). However, it is unclear whether these unstable patterns are purely the result of decreased levels of auxin and ck in the vascular tissues or whether the phloem is required to provide a positional bias in the input of these hormones. We ran simulations to investigate the effect that introducing a spatial bias in the input of hormones had on vascular patterning. In the first simulation, auxin and ck were produced uniformly in all

cells, and in subsequent simulations, we allowed synthesis of auxin or ck in the phloem at two times the rate in other cells. We found that both scenarios were able to produce robust domains of hormonal output ([Movies S7](#) and [S8](#)). However, when we specified the phloem as the main source of ck, we saw a non-uniform gradient of *ARR5* response, with the highest response close to the phloem ([Movie S8](#)). We have never observed such a distribution in our experimental data. Together, our simulations suggest that phloem-mediated ck transport is unlikely to act as a source of positional information but rather, ensures that there is a sufficient supply of ck in the root meristem.

Auxin influx carriers also control auxin transport in the vascular tissues (12). As previously published (26), we also observed localization of *AUX1::AUX1::YFP* on the lateral membranes of protophloem cells ([SI Appendix, Fig. S7](#)). To test whether such a component would have a significant effect on vascular patterning, we incorporated a phloem-localized auxin importer into our model and observed only modest changes in the predicted patterns, with a very slight increase in auxin response in protophloem and no change in the expression of key components, such as *AHP6* ([Movie S9](#)).

Evaluation of Model Sensitivity. By encapsulating the interaction network and the experimentally observed localization of PIN proteins, our model can reproduce the observed expression patterns of many network components in each cell. As in most models of signaling networks based on differential equations, the predicted outcome of the model is reliant on the choice of its parameters (production and degradation rates, protein–DNA binding thresholds, and Hill coefficients) (27, 28). We have based certain parameters, such as the rates of auxin transport and permeability, on parameters used in previous models (4, 5), whereas we have had to estimate others. To explore the degree to which our choice of parameters affects the outcome of our model, we performed local and global sensitivity analyses of a 1D subcellular network model ([SI Appendix, section 3](#)). These analyses identified the parameters to which the model is most sensitive. These parameters were mainly associated with auxin and ck levels and, specifically in the metaxylem, the cooperativity of CKIN. We investigated the effect of perturbing all of these parameters alongside transport and permeability rates in the spatial model. Although there was some variation in intensities, the pattern of key network components was maintained in all these simulations ([SI Appendix, section 3](#)).

Maintenance of Steady State Vascular Pattern. We next investigated whether the model was robust to small changes in the multicellular geometry. We repeated the simulations in new templates based on root cross-sections taken at $\sim 40 \mu\text{m}$ from the quiescent center (QC), representing smaller vascular cylinders in which the cellular pattern is less developed. Although these alterations in geometry inevitably brought some small variation in the output of individual markers, the key patterning events were maintained in all these simulations ([SI Appendix, Fig. S8](#)). Vascular pattern is maintained robustly in living roots; therefore, small changes in hormone input have negligible effects, and only extreme changes (such as treatments with very high levels of ck) have dramatic effects on vascular patterning (9).

We next tested whether our model conferred a similar robustness. To test robustness, we moved away from simulations where the expression of the PINs were fixed based on experimental observations and allowed every cell the potential to express PIN7, meaning that all vascular cells could potentially express any network component (with the exception of miRNA165/6 and CKIN). We used the output from our previous simulation ([Movie S7](#)) as a set of initial conditions that closely resembled WT. We then ran this simulation to steady state and observed that, despite the fact that each cell had

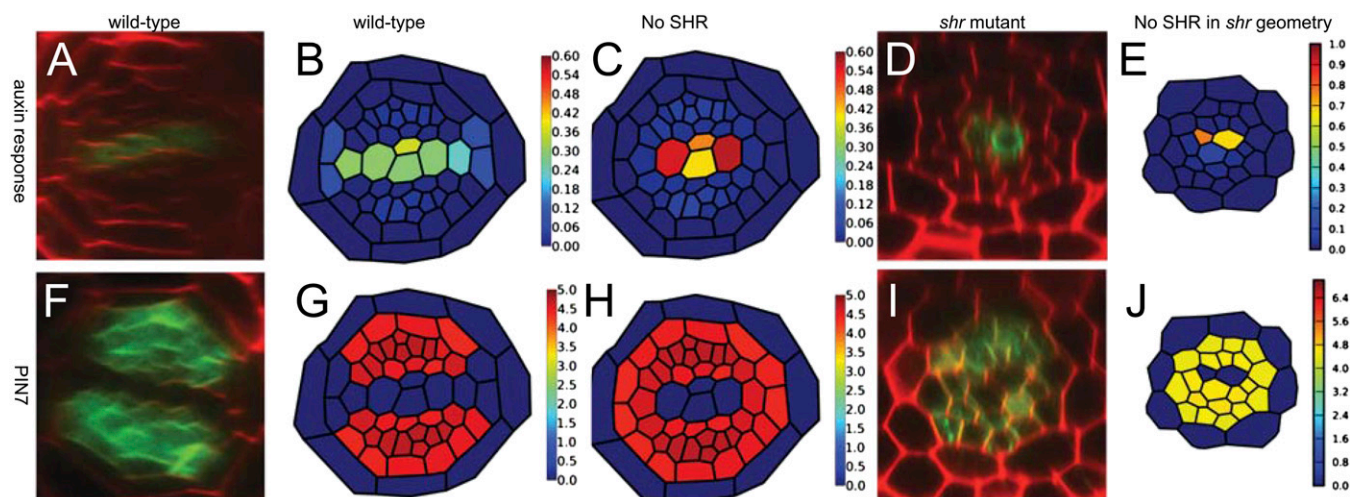


Fig. 4. Mobile miRNA165/6 is required to maintain stable vascular pattern. Simulations and experimental observations of (A–E) auxin output and (F–J) PIN7 activity. (B and G) When all network components are present, the auxin response in the xylem axis is robustly maintained in accordance with experimental data. The synthetic *pDR5rev::GFP* reporter line (used here) and *pIAA2::GFP* line are primary auxin targets and have near-identical expression in vascular tissues. (C and H) In simulations where there is no SHR, the expression domain of *PIN7* expands into the position normally occupied by protoxylem, and auxin response becomes restricted to the central cells. (D and I) We observed the same effect in *shr* mutants and when we ran the simulations using the geometry of an *shr* mutant.

a similar potential to express both ck and auxin marker genes and the same auxin and cytokinin production rates, the initial vascular pattern was maintained robustly (Fig. 4 A, B, F, and G and Movie S10). For patterning to be maintained, adjacent cells of similar size and shape must be able show significantly different levels of steady state gene expression in response to a uniform auxin and cytokinin signal.

Robust patterning under homogenous conditions can be explained by the existence of multiple steady states of gene expression within each cell in the model, conferring a switch-like property in which different subsets of vascular cells can have either high *AHP6* expression (protoxylem) or high *ARR5* and *PIN7* expression (procambium). This possibility was tested by finding the steady states of a simplified version of the model in a tissue structure consisting of two cells of equal size with a single shared cell wall (SI Appendix, section 4). The analysis shows that, using the default parameter set, at very low and very high auxin production rates, there is a single stable steady state for the model system that is equal in both cells. However, for a broad range of intermediate values for auxin production, there are two possible steady states, in which one cell has high *ARR5* and *PIN7* and low *AHP6* and auxin and vice versa in the other cell. This bistability is also seen for a range of intermediate values of ck and sufficiently low *PHB* expression, suggesting that, at least in the two-cell model, after an asymmetry between neighboring cells has been established, it should be robust to small changes in auxin, ck, and *PHB*; however, for sufficiently large changes, the asymmetry is lost, and gene expression is equalized in both cells.

Maintenance of Stable Vascular Pattern Requires Integration of Mobile miRNA165/6 with Hormonal Signaling. The apparent affect of ck and *PHB* levels on pattern maintenance was additionally tested using the full model in the realistic tissue structure. The effect of exogenous treatment of ck was simulated by repeating the simulation shown in Movie S10 but increasing the rate of ck synthesis in all vascular cells. In a similar manner to previous experimental observations (2, 9), we observed loss of *AHP6* expression and restriction of auxin response to the metaxylem (Movie S11). We next considered whether miRNA165/6 is required to maintain a stable auxin response in the xylem axis. The total levels of miRNA165/6 are dramatically reduced in the *shr*

mutant. *SHR* is transcribed in the stele, but the protein is actively transported into the endodermis (29, 30). *SHR* is sequestered to the nucleus by the transcription factor *SCR*, where it promotes the expression of *miRNA165/6* (10, 11).

To allow us to compare our simulation results with subsequent experimental data, we introduced *SHR* into our model. Guided by a previous modeling study (31), we allowed *SHR* transcription and protein synthesis within the stele and for *SHR* protein (but not mRNA) to move throughout the stele and into the endodermis through passive diffusion. Our model does not explicitly include *SCR*, but we have simulated its effect by allowing the production of miRNA165/6 by *SHR* only in the endodermis and assigning a Hill coefficient that reflects this cooperative binding. This mechanism reproduced the WT expression of all marker genes and produced similar results to our previous model (Movie S12). We then investigated whether vascular pattern could be maintained without *SHR* using the same conditions as shown in Movie S10 but setting *SHR* transcription to zero. Under these conditions, we predicted that *PHB* mRNA is present throughout the vascular tissues, and *AHP6* is repressed in all cells. Uniformly low levels of *AHP6* expression causes up-regulation of ck response at the protoxylem position and approximately homogeneous levels of *PIN7* in all tissues except for the metaxylem. As a consequence, auxin is transported from the cells with high *PIN7* concentration to the central cells in the xylem axis (Fig. 4 C and H and Movie S13). We then imported our entire regulatory network into the geometry of an *shr* mutant and ran another simulation from zero initial conditions, which predicted a highly similar pattern to the previous simulation (Fig. 4 E and J and Movie S14).

We tested these predictions by analyzing the expression of both *PIN7* and the auxin response marker *DR5rev::GFP* in the *shr* mutant. Consistent with model predictions, we observed that the domain of auxin response was confined to the central cells of the xylem axis, and *PIN7* was present in a radially symmetric pattern in all but the central vascular cells (Fig. 4 D and I). Together our results show that, in addition to the documented roles of *SHR* in specifying cell identity, stem cell function, and lateral root growth (10, 29, 32), *SHR* also directs hormonal responses during vascular patterning.

Discussion

We have used a multicellular mathematical model to probe whether the mutually inhibitory interaction between the transport/signaling of two hormones can act as a plausible vascular patterning mechanism. Previous models based exclusively on auxin transport in roots have analyzed the flux of auxin in the longitudinal sections (4, 5, 33). We have extended this concept to account for the lateral transport of auxin and shown that it determines radial patterning.

Our multicellular model also incorporates auxin and ck signaling networks together with *PHB*, miRNA165/6, and *SHR*. It has previously been suggested that small RNA species could repress their targets with a tunable threshold to create sharp boundaries of gene expression (21). We have modeled this interactive mechanism at the organ scale and showed that it is capable of creating the sharp gradient of *PHB* seen in WT roots. Previously, it has been shown that miRNA165/6 can regulate *PHB* through *ARR1* to control root growth (34). However, because *ARR1* is absent in the domain that we have modeled, it suggests that similar components can regulate the same targets in a developmentally specific context. Our study provides insights into how these species may be regulated in vascular tissues, and it will be interesting to see whether these concepts can be applied more widely to the role of *PHB* in controlling root growth as well as other developmental contexts.

Our simulations show that the restriction of *PHB* by miRNA165/6 is required in establishing a bisymmetric auxin response, and we have verified this prediction experimentally by showing that *shr* mutants (which lack miRNA165/6) are unable to generate a bisymmetric auxin response throughout the xylem axis. Our model also revealed that a missing component is required to explain the spatial expression of *ARR5*. By including such a component, our model yields gene expression patterns that are

consistent with the experimental data, illustrating the power of computational modeling as a predictive tool for determining minimum network requirements. We have identified a minimum framework necessary for establishing vascular pattern in *Arabidopsis* roots. We recognize that, in biological systems, the minimal network is rarely used, and there is often a high degree of genetic redundancy. We have addressed this redundancy for the PINs and investigated the role of each PIN protein.

In conclusion, we have presented a multicellular computational model that embodies the concepts that mobile miRNAs and mutually inhibitory domains of hormonal signaling can act as mechanisms for generating pattern. This regulatory network for vascular patterning differs conceptually from other mechanisms that have been shown to generate pattern in plants based on either reaction–diffusion dynamics or reflux patterns (4, 35). Our model shows that the integration of movement by diffusion (miRNA165/6), the targeted transport of auxin, and the mutual degradation of *PHB* and miRNA165/6 offer a plausible way to generate vascular pattern.

Materials and Methods

The mathematical model is described in detail in the *SI Appendix, section 1*. Plant lines were all in the Columbia background and are described in *SI Appendix, section 6*. Confocal microscopy was performed on an inverted Leica SP5 confocal with propidium iodide used to counterstain the roots. Visualization of the GUS marker was performed as previously described (2).

ACKNOWLEDGMENTS. We thank Leah Band for helpful comments. We acknowledge the Biotechnology and Biological Sciences Research Council and the Engineering and Physical Sciences Research Council for funding. H.M.B. was funded, in part, by King Abdullah University of Science and Technology (KAUST) Award KUK-013-04, J.R.K. was funded by the Royal Society and Wolfson Foundation, and A.B. was funded by a Royal Society University Research Fellowship. J.G. and C.G. were funded by the Institut de Biologie Computationnelle de Montpellier and the Morphogenetics Inria Project-Lab.

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