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# Faraday rotation and photoluminescence in heavily Tb<sup>3+</sup>-doped GeO<sub>2</sub>-B<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub>-Ga<sub>2</sub>O<sub>3</sub> glasses for fiber-integrated magneto-optics

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We report on the magneto-optical (MO) properties of heavily Tb<sup>3+</sup>-doped GeO<sub>2</sub>-B<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub>-Ga<sub>2</sub>O<sub>3</sub> glasses towards fiber-integrated paramagnetic MO devices. For a Tb<sup>3+</sup> ion concentration of up to  $9.7 \times 10^{21} \text{ cm}^{-3}$ , the reported glass exhibits an absolute negative Faraday rotation of  $\sim 120 \text{ rad/T/m}$  at 632.8 nm. The optimum spectral ratio between Verdet constant and light transmittance over the spectral window of 400–1500 nm is found for a Tb<sup>3+</sup> concentration of  $\sim 6.5 \times 10^{21} \text{ cm}^{-3}$ . For this glass, the crystallization stability, expressed as the difference between glass transition temperature and onset temperature of melt crystallization exceeds 100 K, which is a prerequisite for fiber drawing. In addition, a high activation energy of crystallization is achieved at this composition. Optical absorption occurs in the NUV and blue spectral region, accompanied by Tb<sup>3+</sup> photoluminescence. In the heavily doped materials, a UV/blue-to-green photo-conversion gain of  $\sim 43\%$  is achieved. The lifetime of photoluminescence is  $\sim 2.2 \text{ ms}$  at a stimulated emission cross-section  $\sigma_{\text{em}}$  of  $\sim 1.1 \times 10^{-21} \text{ cm}^2$  for  $\sim 5.0 \times 10^{21} \text{ cm}^{-3} \text{ Tb}^{3+}$ . This results in an optical gain parameter  $\sigma_{\text{em}} * \tau$  of  $\sim 2.5 \times 10^{-24} \text{ cm}^2\text{s}$ , what could be of interest for implementation of a Tb<sup>3+</sup> fiber laser.

The Faraday effect reflects the ability of a material to - in the presence of a magnetic field being parallel to the incident light beam - rotate the polarization plane of linear polarized light by a certain angle<sup>1–3</sup>. The material's magneto-optical (MO) performance is typically described by the Verdet constant  $V_B$ , which represents the degree of rotation as a function of the acting magnetic field strength and the geometrical path length within the material. High performance can hence be achieved via large rotation efficiency or a long path length. Applications of MO materials range from magnetic field sensing and security encoding to optical modulators, diodes, isolators and switches<sup>1–6</sup>. Key for the design of an efficient, optically transparent (bulk) MO material is the incorporation of a high atom concentration of paramagnetic species while, at the same time, avoiding optical absorption to the highest possible degree. While some transition metals have also been considered for this purpose, at present, this calls for the use of rare earth species<sup>7</sup>. Here, due to the electronic transition of  $4f^8 \rightarrow 4f^7 5d^8$ , the Tb<sup>3+</sup> ion offers one of the highest paramagnetic susceptibilities ( $J = 6, g = 1.46$ ) and magnetic moments ( $9.5\text{--}9.72 \mu_{\text{eff}}$ ) of all rare earth ions. Consequently, the most promising bulk MO material is terbium aluminum garnet (Tb<sub>3</sub>Al<sub>5</sub>O<sub>13</sub>, TAG,  $V_B \sim 180 \text{ rad/T/m}$ )<sup>10,11</sup>, which is not yet available commercially, though. Instead, terbium gallium garnet single crystals (Tb<sub>3</sub>Ga<sub>5</sub>O<sub>13</sub>, TGG,  $V_B \sim 134 \text{ rad/T/m}$ )<sup>12</sup> are presently the most widely used commercial MO materials. But also all commercially available MO glasses rely on massive Tb<sup>3+</sup>-doping<sup>4,13–16</sup>. As an alternative to the MO crystals, glassy materials offer a much improved flexibility of forming and processing. Especially glass compositions which are suitable for fiber fabrication could enable fiber-integrated devices. In addition, the higher interaction length which can be achieved in fiber devices could further compensate eventual losses in Faraday rotation efficiency. In this regard, besides the primary optical properties, the thermo-physical stability and the rheological properties of the considered glass and its corresponding (supercooled) melt are key parameters: in order to avoid crystallization of the melt during fiber drawing, a certain crystallization stability is required. This is often expressed as the difference,  $\Delta T$ , between the glass transition temperature  $T_g$  and the onset temperature of crystallization  $T_c$ , or through various other empirical stability indicators such as the Hrubý parameter which is derived from this difference, sometimes further relating



it to the liquidus temperature of the melt or other properties<sup>17,18</sup>. Typically, a large value of  $\Delta T$  is sought for two reasons: fiber drawing must be performed at a temperature sufficiently above  $T_g$  so that a sufficiently low viscosity is reached and the interval of processing temperature must be sufficiently wide to tolerate a certain degree of processing-induced temperature variability. On the other hand, for many of the specialty (non-silica) compositions with often high liquid fragility, fiber drawing cannot be performed above the liquidus temperature (where there would not be any risk of crystallization) because then, the viscosity would be too low.

Here, we consider glass forming liquids of the type  $\text{GeO}_2\text{-B}_2\text{O}_3\text{-Al}_2\text{O}_3\text{-Ga}_2\text{O}_3$  enabling high rare earth solubility. In this system, we achieve a  $\text{Tb}_2\text{O}_3$  doping concentration of up to 25 mol%. The glass stability parameters are controlled through tailoring the matrix composition in order to provide the possibility of fiber drawing. We then report on the MO and photoluminescence properties of this material.

## Results

**Magneto-optical properties.** The chemical composition and physical properties of all samples are summarized in Tables 1–2. Figure 1a shows the room-temperature wavelength dependence of  $V_B$  for the full series of GBAG- $x\text{Tb}$  ( $x = 14, 18, 22$  and  $25$ ). As expected, all samples exhibit paramagnetic behaviour over the full range of studied wavelengths, with a strong absolute increase towards the blue. Secondly, there is a notable increase with increasing  $\text{Tb}^{3+}$  dopant concentration, i.e., from  $\sim 48$  to  $119$  rad/T/m at  $632.8$  nm (Fig. 1a and 1b). For similar  $\text{Tb}^{3+}$  ion concentration, the absolute value  $V_B$  of GBAG- $x\text{Tb}$  glasses is in the order of that of other reported record values in  $\text{Tb}^{3+}$ -doped MO glasses, e.g. silicate<sup>2,6</sup>, phosphate<sup>2</sup>, borate<sup>5,22</sup> and borogermanate<sup>23</sup> glasses (Fig. 1b). For the maximum  $\text{Tb}^{3+}$  loading we report here, GBAG-25Tb,  $V_B$  exceeds the rotation efficiency in most of the well-known MO glasses, e.g.,  $30\text{Tb}_2\text{O}_3\text{-}70\text{B}_2\text{O}_3$  ( $\sim 103$  rad/T/m)<sup>22</sup> and  $25\text{Tb}_2\text{O}_3\text{-}15\text{Al}_2\text{O}_3\text{-}60\text{SiO}_2$  ( $\sim 102$  rad/T/m)<sup>6</sup>, and is similar with that of  $33\text{Tb}_2\text{O}_3\text{-}25\text{GeO}_2\text{-}25\text{B}_2\text{O}_3\text{-}5\text{SiO}_2\text{-}12\text{Al}_2\text{O}_3$  ( $\sim 119$  rad/T/m)<sup>23</sup>. For comparison, data for the single crystalline benchmarks of TAG and TGG are also shown in Fig. 1b<sup>11,12</sup>.

In the framework of the Van Vleck-Hebb model of single-oscillator paramagnetic rare earth ions, the relationship between  $V$  and  $\lambda^2$  can be written as<sup>24,25</sup>

$$V_B^{-1} = \frac{g\mu_B ch}{4\pi^2 \chi C_t} \left(1 - \frac{\lambda^2}{\lambda_t^2}\right) \quad (1)$$

In Eq. (1),  $g$  is the Landé factor,  $c$  the velocity of light,  $h$  is the Planck constant,  $C_t$  is the effective transition probability, and  $\lambda_t$  is the effective transition wavelength.  $\lambda_t$  is a weighted average value which is taken as the origin of the paramagnetic Faraday rotation. In rare earth ions, it is close to the position of the electric transition of  $4f^N \leftrightarrow 4f^{N-1}5d^{26}$ . Plotting  $V^{-1}$  over  $\lambda^2$  therefore yields a linear relationship (Fig. 1c). Here,  $\lambda_t$  is the intersection with the  $\lambda^2$  axis which results from extrapolation of the data. The value of  $\lambda_t$  is dependent on  $\text{Tb}_2\text{O}_3$  concentration (inset of Fig. 1c). It increases with  $\text{Tb}_2\text{O}_3$  concentration, i.e., from  $\sim 225$  to  $300$  nm when  $x \leq 22$ . A decrease back to  $\sim 280$  nm is observed for the highest  $\text{Tb}_2\text{O}_3$  concentration. As expected, these values are close to the  $4f^8 \leftrightarrow 4f^75d$  transition of the  $\text{Tb}^{3+}$  ion ( $\sim 250$  nm)<sup>5</sup>, and are also similar to other reported values, e.g.,  $\text{Tb}^{3+}$ -doped phosphate ( $\sim 250$  nm)<sup>27</sup>, borosilicate ( $\sim 259\text{--}280$  nm)<sup>28</sup>, aluminoborate ( $\sim 250$  nm)<sup>24</sup>, sodium borate ( $\sim 220$  nm)<sup>8</sup> and fluorophosphate glasses ( $\sim 217$  nm)<sup>26</sup>.

Fig. 1d shows the UV- NIR optical absorption spectra of GBAG- $x\text{Tb}$  ( $x = 14, 18, 22$  and  $25$ ). The absorption spectra consist of several strongly overlapping but sharp absorption bands in the  $300$  to  $390$  nm range, and another sharp band at  $\sim 484$  nm. These bands can readily be assigned to the  $4f^8 \rightarrow 4f^8$  electronic transitions of  $\text{Tb}^{3+}$  from the ground state of  $^7F_6$  to the labeled excited states (inset of Fig. 1d and Fig. 2e)<sup>29,30</sup>. The intensity of all bands follows well Lambert-Beer's power law. All glasses exhibit high transparency in the  $\sim 400$  to  $1500$  nm range with a transmittance of  $\sim 58\%$  ( $\sim 95\%$ ) with a thickness of  $1$  cm (mm). The increasing absorption intensity with increasing  $\text{Tb}^{3+}$  content in the near-UV region results in a shift of the absorption edge and an apparent coloration under sunlight, gradually varying from colorless to brown (inset of Fig. 1e).

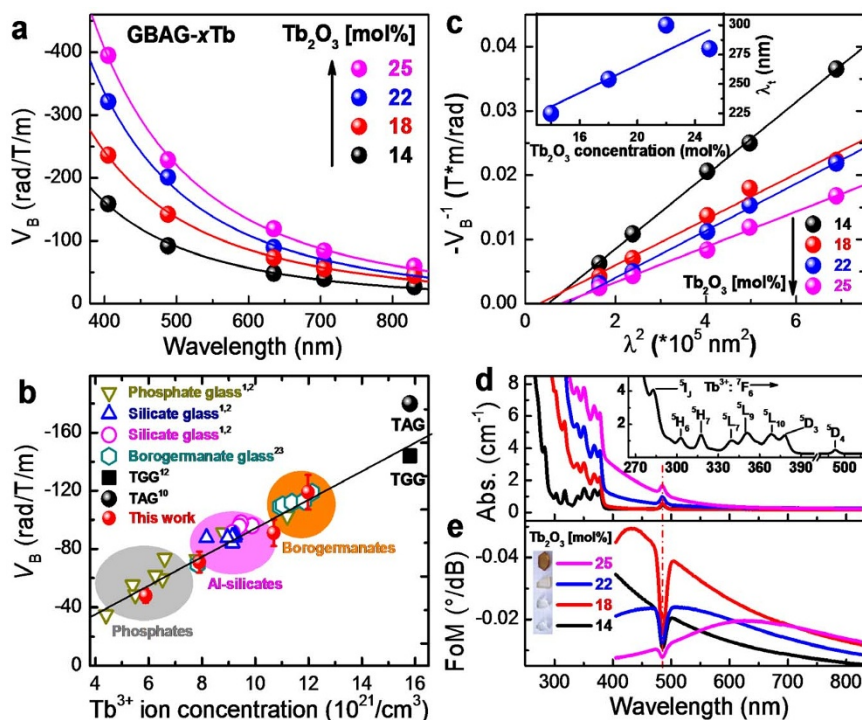
The MO figure of merit (FoM) which is an important parameter for practical applications results from the ratio of  $V_B/a$ , where  $a$  is absorption coefficient<sup>4</sup>. As displayed in Fig. 1e, the spectral FoM exhibits a sharp dip at  $484$  nm, resulting from the  $^7F_6 \rightarrow ^5D_4$  absorption band of  $\text{Tb}^{3+}$ . In the present case, the glass of GBAG-18Tb exhibits the best trade-off between  $V_B$  and  $a$  over the whole spectrum. The highest FoM performance of  $\sim -0.049^\circ/\text{dB}$  is found at

**Table 1 | Nominal and analyzed compositions of the studied glasses (data given in the form “nominal/as-analyzed”, mol%)**

Glass sample	GBAG-14Tb	GBAG-18Tb	GBAG-22Tb	GBAG-25Tb
$\text{GeO}_2$	16.5/17.3	16.5/18.0	16.5/16.4	16.5/17.0
$\text{B}_2\text{O}_3$	21.5/25.3	21.5/25.0	21.5/21.4	21.5/23.0
$\text{Al}_2\text{O}_3$	37.0/27.2	37.0/28.0	37.0/37.0	37.0/32.0
$\text{Ga}_2\text{O}_3$	11.0/15.1	7.0/11.0	3.0/3.2	0.0/0.0
$\text{Tb}_2\text{O}_3$	14.0/15.1	18.0/18.0	22/22.0	25.0/28.0

**Table 2 | Experimental data of density  $\rho$ ,  $\text{Tb}^{3+}$  ion concentration, refractive index  $n_d$ , Verdet constant  $V_B$  (at  $632.8$  nm), FoM (at  $435$  nm),  $\tau$ ,  $T_g$ ,  $T_c$ ,  $\Delta T$  and  $E_a$  for the studied glasses**

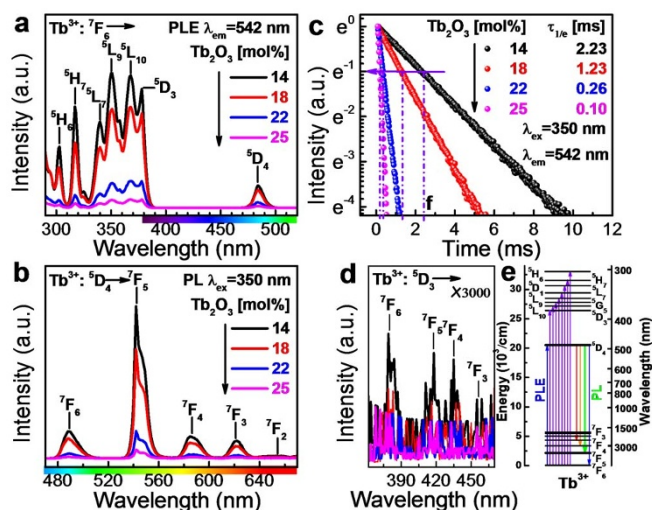
Glass sample	GBAG-14Tb	GBAG-18Tb	GBAG-22Tb	GBAG-25Tb
$\rho \pm 0.01$ (g/cm <sup>3</sup> )	4.08	4.53	4.79	4.85
$\text{Tb}^{3+}$ concentration ( $10^{21}$ cm <sup>-3</sup> )	5.0	6.5	8.1	9.7
$n_d @ 587$ nm $\pm 0.01$	1.69	1.73	1.74	1.75
$V_B$ (rad/T/m)	-48	-71	-91	-119
FoM ( $^\circ/\text{dB}$ )	-0.029	-0.049	-0.023	-0.008
$\tau$ (ms)	2.23	1.23	0.26	0.10
$T_g \pm 1$ ( $^\circ\text{C}$ )	740	767	772	777
$T_c \pm 1$ ( $^\circ\text{C}$ )	848	880	905	928
$\Delta T \pm 1$ (K)	108	113	133	151
$E_a$ (kJ/mol/K)	520	593	533	482



**Figure 1** | Magneto-optical properties of GBAG- $x$ Tb glasses. (a) Variation of the Verdet constant with wavelength for GBAG- $x$ Tb glasses as a function of  $Tb_2O_3$  concentration at room-temperature. The solid lines represent a fit of the data to the power function  $y = a(1-x)^b$ . (b) Dependence of  $V_B$  on  $Tb^{3+}$  ion concentration and comparison to other reported data glasses at a fixed wavelength of 632.8 nm. (c) Van Vleck-plot of the inverse  $V_B$  ( $V_B^{-1}$ ) over the square wavelength ( $\lambda^2$ ). The solid lines in (c) represents a linear fit of the data. The inset of (c) shows the value of the transition wavelength  $\lambda_t$  versus  $Tb_2O_3$  concentration. In (d), the UV-VIS-NIR optical absorption spectra are given, from which the spectral MO figure of merit is obtained (shown in (e)). The inset of (d) exemplarily shows a zoom at the absorption spectrum in the spectral region of 260–550 nm for GBAG-14Tb.

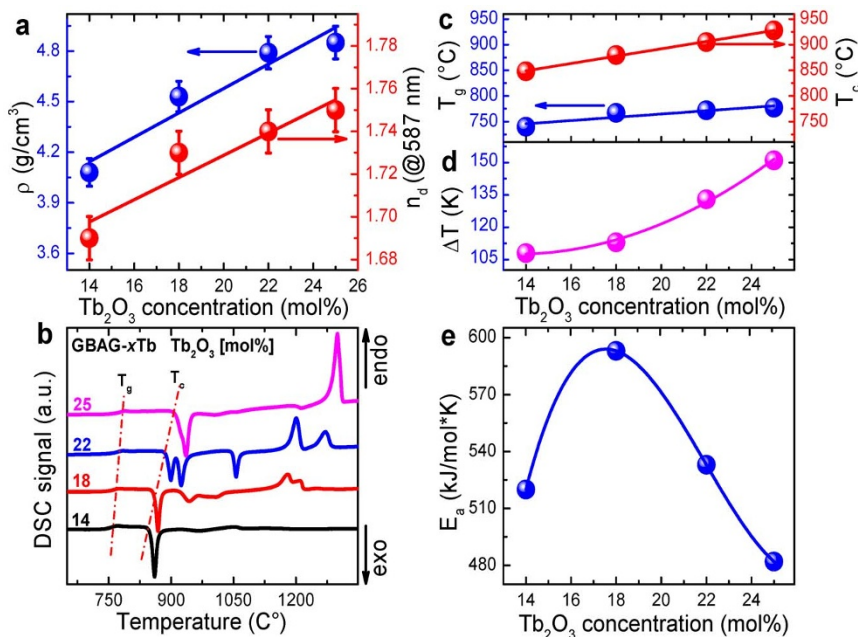
~435 nm, which matches the emission characteristics of various blue laser diodes.

**Photoluminescence properties.** Fig. 2a and 2b present static photoexcitation (PLE) and luminescence (PL) spectra of  $Tb^{3+}$  in



**Figure 2** | Photoluminescence of GBAG- $x$ Tb glasses. Static (a) PLE and (b) PL spectra, and (c) normalized dynamic decay curves of photoluminescence from GBAG- $x$ Tb as a function of  $Tb_2O_3$  concentration at room-temperature. (d) is a zoom (by a factor of 3000) into the PLE spectra at the spectra region of 360–470 nm. (e) represents the energy level diagram of  $Tb^{3+}$ . The labels in (a–b) indicate the respective band assignment.

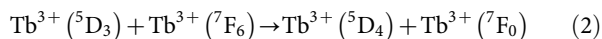
GBAG- $x$ Tb ( $x = 14, 18, 22$  and  $25$ ) at room temperature. Fully consistent with the optical absorption data (Fig. 1d), the PLE spectra of  $Tb^{3+}$  consist of a series of sharp overlapping PLE bands in the NUV region with maxima at 378, 368, 358, 350, 340, 325, 317 and 303 nm, and another sharp PLE line in the blue with a maximum at 484 nm. These bands are attributed to the intra-configurational parity-forbidden  $4f^8 \rightarrow 4f^8$  electronic transitions from the ground state  $^7F_6$  to the labeled excited states, also indicated in energy level diagram of  $Tb^{3+}$  (Fig. 2a and 2e)<sup>30–34</sup>. The strongest PLE band is the  $^7F_6 \rightarrow ^5L_9$  at 350 nm, used in the following as excitation wavelength to record the PL spectra. Here, the five typical PL bands of  $Tb^{3+}$  are observed, i.e., at 488, 542, 585, 622 and 655 nm, deriving again from the intra-configurational parity-forbidden  $4f^8 \rightarrow 4f^8$  transitions from  $^5D_4$  to the  $^7F_J$  ( $J=6, 5, 4, 3$  and  $2$ ) multiplet, Fig. 2b and 2e<sup>35</sup>. The green PL line of the magnetic dipole allowed transition ( $\Delta J = 1$ )  $Tb^{3+}: ^5D_4 \rightarrow ^7F_5$  at 542 nm with a full width at half maximum (FWHM) of ~10 nm (~337  $cm^{-1}$ ) dominates the PL spectra for all samples. As a result, the corresponding International Commission on Illumination (CIE) 1931 PL chromaticity coordinates of all samples are ( $\sim 0.344 \pm 0.002, \sim 0.592 \pm 0.002$ ), which are located in the green region. The aforementioned green PL band is Stark-split into two peaks due to the distorting effect of the disordered glass network on the  $Tb^{3+}$  ions (Fig. 2b). For lower amounts of  $Tb_2O_3$  loading ( $x \leq 18$ ), the intensity of all PL lines of  $Tb^{3+}$  decreases only slightly with  $Tb_2O_3$  concentration while for  $x \geq 18$ , we observe strong concentration quenching<sup>36,37</sup>. This is related to an increasing probability for the formation of Tb-O-Tb entities in the first coordination shell of  $Tb^{3+}$ .<sup>38</sup> The concentration quenching effect is further confirmed by the decay data of the  $Tb^{3+}: ^5D_4 \rightarrow ^7F_5$  emission (Fig. 2c). All decay curves follow a single exponential function of the form  $I = I_0 \exp(-t/\tau)$  (with time  $t$  and intensity  $I$ ). The effective lifetime  $\tau$  decreases with increasing  $Tb^{3+}$  concentration,



**Figure 3 | Thermal properties of GBAG- $x$ Tb glasses.** (a) Physical properties density and refractive index of GBAG- $x$ Tb as a function of  $Tb_2O_3$  concentration. (b) DSC curves of GBAG- $x$ Tb as dependent on  $Tb_2O_3$  concentration. From (b), the variation of the glass transition temperature  $T_g$  and the onset temperature of crystallization  $T_c$  are extracted (c). (d–e) show the glass stability parameter  $\Delta T$  and the apparent activation energy of crystallization, respectively, of GBAG- $x$ Tb as a function of  $Tb_2O_3$  concentration. Solid lines are drawn as guides for the eye.

i.e., from  $\sim 2.2$  to  $\sim 1.2$  ms when  $x \leq 18$ , and further to  $\sim 0.1$  ms for  $x > 18$  (Fig. 2b and 2c). The lifetime of  $Tb^{3+}$ :  $^5D_4 \rightarrow ^7F_5$  PL for GBAG-14Tb glass ( $\sim 2.23$  ms) is larger than what is found in similar  $B_2O_3$ - $GeO_2$ - $Gd_2O_3$  glasses before concentration quenching,  $\sim 1.80$  ms<sup>39</sup>. This further indicates that particularly weak concentration quenching occurs in the present case. The internal quantum efficiency  $\eta_{iQE}$  for GBAG-14Tb is  $\sim 63\%$ . This value is close to the highest reported  $\eta_{iQE}$  of  $Tb^{3+}$ -based PL in literature, e.g.,  $Tb^{3+}$ -doped phosphate glass ( $\sim 78\%$ )<sup>40</sup> and silicone hybrid materials ( $\sim 68\%$ )<sup>41</sup>. For higher doping concentration, it decreases to only 0.3% at  $x = 25$ . The high  $Tb^{3+}$  loading results in a large absorption cross-section of incoming light and, hence, high photo-conversion gain. That is, the absorbance of GBAG-14Tb at 350 nm is  $\sim 69\%$ . Thus, the external quantum efficiency  $\eta_{eQE}$  is  $\sim 43\%$ , meaning that at the considered excitation wavelength,  $\sim 43\%$  of the incoming photons are converted through photoluminescence.

PL of  $Tb^{3+}$  from the higher excited states, i.e.,  $^5D_3 \rightarrow ^7F_J$  ( $J = 6, 5, 4, 3, 2$  and 1) is almost fully quenched even in GBAG-14Tb (Fig. 2d). This is a result of the strong cross-relaxation processes which occur at the high doping levels used in this study. The cross relaxation process is caused by the closeness of the  $^5D_3$  and  $^5D_4$  ( $\sim 5629$   $cm^{-1}$ ), and the  $^7F_6$  and  $^7F_0$  energy levels ( $\sim 5791$   $cm^{-1}$ , Fig. 2e)<sup>42</sup>,



The absorption cross-section  $\sigma_{abs}$  of  $Tb^{3+}$  at 350 ( $Tb^{3+}$ :  $^7F_6 \rightarrow ^5L_9$ ) and 484 nm ( $Tb^{3+}$ :  $^5F_6 \rightarrow ^7D_4$ ), and the stimulated emission cross-section  $\sigma_{em}$  of  $Tb^{3+}$  PL at 542 nm ( $Tb^{3+}$ :  $^5D_4 \rightarrow ^7F_5$ ) can be estimated through McCumber's and Füchtbauer-Ladenburg's equation<sup>43–45</sup>,

$$\sigma_{abs} = \frac{2.303OD(\lambda)}{N_0d} \quad (3)$$

$$\sigma_{em} = \frac{\lambda_0^2 \eta}{4\pi c n^2 \tau \Delta\nu_{1/2}} \times \left(\frac{\ln 2}{\pi}\right)^{1/2} \quad (4)$$

In Eqs. (3)–(4),  $N_0$  is the ion concentration of  $Tb^{3+}$ ,  $d$  is the sample thickness,  $\lambda_0$  is the emission wavelength,  $OD(\lambda)$  is the optical density,  $\eta$  is the internal quantum efficiency,  $n$  is the refractive index of the

host material,  $\tau$  is the emission lifetime and  $\Delta\nu_{1/2}$  is the FWHM of the transition. The  $\sigma_{abs}$  value of  $Tb^{3+}$  in GBAG- $x$ Tb glasses at 350 and 484 nm is calculated to be  $\sim 4.94$  and  $0.95 \times 10^{-22}$   $cm^2$ , respectively. This value is comparable to that of phosphate glasses ( $\sim 1.1 \times 10^{-22}$   $cm^2$ )<sup>40</sup>. The  $\sigma_{em}$  value of  $Tb^{3+}$  in GBAG- $x$ Tb glasses at 542 nm is  $\sim 1.1 \times 10^{-21}$   $cm^2$ , notably larger than in phosphate glasses ( $\sim 7.4 \times 10^{-22}$   $cm^2$ )<sup>40</sup>. The product of  $\sigma_{em}^* \tau$ , the optical gain parameter for laser applications, is proportional to the amplification gain and inverse laser oscillation threshold<sup>45</sup>. A relatively high value of  $\sim 2.5 \times 10^{-24}$   $cm^2s$  is obtained for the GBAG-14Tb glass, what suggests a large amplification gain and low oscillation threshold and, hence, potential interest for further examination as a green laser gain material.

**Thermal properties.** The values of  $\rho$ ,  $n_d$ ,  $T_g$ ,  $T_c$  and  $\Delta T$  of GBAG- $x$ Tb are summarized in Tab. 1. Density and refractive index increase from  $\sim 4.08$  to  $4.85$   $g/cm^3$  and from  $1.69$  to  $1.75$  respectively with increasing  $Tb_2O_3$  concentration due to the much higher molar mass of  $Tb_2O_3$  (365.85  $g/mol$ ) as compared to  $Ga_2O_3$  (187.44  $g/mol$ ) (Fig. 3a).

Figure 3b shows DSC curves of GBAG- $x$ Tb. Here,  $T_g$  and  $T_c$  gradually increase from  $740$  to  $777^\circ C$  and from  $848$  to  $928^\circ C$ , respectively, with increasing  $Tb_2O_3$  concentration (Fig. 3c). In order to empirically judge glass stability,  $\Delta T = T_c - T_g$  is calculated from these data.

Generally speaking, larger values of  $\Delta T$  reflect an improved stability against crystallization. Here,  $\Delta T$  increases from  $108$  to  $151$  K with increasing of  $Tb_2O_3$  concentration (Fig. 3d). Overall, this suggests a comparably high crystallization stability of the glasses of this study.

The apparent activation energy  $E_a$  of crystallization is calculated from the DSC data for varying heating rates by a Kissinger equation<sup>46</sup>,

$$\ln\left(\frac{\phi}{T_x^2}\right) = -\frac{E_a}{RT_x} + constant \quad (5)$$

In Eq. (5),  $R$  is the ideal gas constant,  $T_x$  is the temperature of crystallization, and  $\phi$  is the heating rate of the DSC experiment.  $E_a$  can



therefore be estimated from the slope of a linear fit of  $\ln(\phi/T_x^2)$  versus  $1/T_x$  plot. The obtained value depends on  $Tb_2O_3$  concentration. It reaches a maximum of  $\sim 593$  kJ/(mol  $\times$  K) at GBAG-18Tb and decreases to 482 kJ/(mol  $\times$  K) for  $x = 25$  (Fig. 3e). Hence, while, GBAG-18Tb and GBAG-14Tb exhibit the highest MO FoM and the highest PL performance, they also exhibit large  $\Delta T$  and comparatively high  $E_a$ .

## Conclusions

In summary, we reported on the magneto-optical (MO) properties of heavily  $Tb^{3+}$ -doped  $GeO_2$ - $B_2O_3$ - $Al_2O_3$ - $Ga_2O_3$  glasses towards fiber-integrated paramagnetic MO devices. For  $Tb^{3+}$  ion concentrations of up to  $9.7 \times 10^{21}$  cm $^{-3}$ , the reported glass exhibits an absolute negative Faraday rotation of  $\sim 120$  rad/T/m at 632.8 nm. The underlying effective transition wavelength  $\lambda_i$  is close to the  $4f^8 \leftrightarrow 4f^75d$  transition of the  $Tb^{3+}$  ion,  $\sim 250$  nm. The optimum FoM is found for a  $Tb^{3+}$  concentration of  $\sim 6.5 \times 10^{21}$  cm $^{-3}$  (GBAG-18Tb),  $\sim -0.05^\circ$ /dB at  $\sim 435$  nm, matching the emission characteristics of blue light-emitting diodes. For this glass, the crystallization stability, expressed as the difference between glass transition temperature and onset temperature of melt crystallization exceeds 100 K, which is a prerequisite for fiber drawing. In addition, a high activation energy of crystallization is achieved using this composition. Optical absorption occurs in the NUV and blue spectral region, accompanied by  $Tb^{3+}$  photoluminescence. In the heavily doped materials, a UV/blue-to-green photo-conversion gain of  $\sim 43\%$  is achieved. The  $Tb^{3+}$  ions are well dispersed in GBAG- $x$ Tb glasses without notable concentration quenching of photoluminescence up to a dopant concentration of  $\sim 14$  mol% of  $Tb_2O_3$  (GBAG-14Tb). The lifetime of photoluminescence is  $\sim 2.2$  ms with a stimulated emission cross-section  $\sigma_{em}$  of  $\sim 1.1 \times 10^{-21}$  cm $^2$  for  $\sim 5.0 \times 10^{21}$  cm $^{-3}$   $Tb^{3+}$ . This results in an optical gain parameter  $\sigma_{em}^* \tau$  of  $\sim 2.5 \times 10^{-24}$  cm $^2$ s, what could be of interest for implementation of a  $Tb^{3+}$  fiber laser.

## Methods

**Synthesis of Glasses.** Precursor glasses with nominal compositions of  $16.5GeO_2$ - $21.5B_2O_3$ - $37Al_2O_3$ -( $25-x$ ) $Ga_2O_3$ - $xTb_2O_3$  (GBAG- $x$ Tb with  $x = 14, 18, 22$  and  $25$  mol%) were prepared by conventional melting and quenching. Batches of  $\sim 50$  g of  $GeO_2$  (99.99%),  $H_3BO_3$  (99.99%),  $Ga_2O_3$  (99.99%) and  $Tb_4O_7$  (99.99%) were thoroughly mixed and melted in a resistive heating furnace at 1500°C for 3 h in  $Al_2O_3$  crucibles, heating to 700°C at 5 K/min and to 1500°C at 10 K/min. Melting conditions were kept identical for all batches to ensure a homogenous dilution of  $Al_2O_3$  in the melt. Subsequently, melts were poured onto preheated brass plates, annealed for 1 h and finally cooled down to room temperature at the intrinsic furnace rate ( $\sim 1$  K/min). The obtained glass slabs were cut and polished on both sides for optical characterization.

**Magneto-optical properties.** Frequency-dependent MO analyses were done by using a series of laser diodes as light sources (405, 488, 635, 705 and 830 nm) and fitting the obtained data of Faraday rotation to a power function of the form  $V_B = a(1-\lambda)^b$  with wavelength  $\lambda$ .  $V_B$  is calculated from the Faraday rotation angle  $\theta_F$ , the strength of the external magnetic field  $B$ , and the length of the light path  $L$  in the sample,  $V_B = \theta_F/BL$ .<sup>58,19</sup> For this, the rotation of the polarization plane was measured with a polarimeter (PAX570VIST/PAX570IR-1T). In this set-up, the magnetic field was applied through a permanent magnet, achieving a constant magnetic flux of 0.23 T. In a second set of experiments, the value if  $V_B$  was derived from the  $\theta_F$  versus  $B$  dependencies in an iron-yoke magnet ( $-0.1$  T <  $B$  <  $0.1$  T), using a light-emitting diode with the central wavelength of 625 nm. For this, the magnetic flux was swept in the given range with a step-width of  $\sim 1$  mT. Then, the obtained data on  $\theta_F$  versus  $H$  were linearly extrapolated to obtain the slope  $d\theta_F/dH$ , which was used to estimate  $V_B$ . Error bars on the value of  $V$  were obtained from the comparison of those two experiments. UV-VIS-NIR absorption spectra were recorded over the spectral range of 200 nm to 2500 nm in a UV-NIR spectrophotometer (Perkin Elmer, Lambda 950).

**Photoluminescence properties.** Static photoexcitation (PLE) and luminescence (PL) spectra and dynamic decay curves of the  $Tb^{3+}$ -related photoluminescence were recorded with a high-resolution spectrofluorometer (Horiba Jobin Yvon Fluorolog FL3-22) at room temperature. PLE spectra were corrected over the lamp intensity with a silicon photodiode. PL spectra were corrected by the spectral response of employed photomultiplier tube. Absorbance ( $a$ ), internal ( $\eta_{IQE}$ ) and external quantum efficiency ( $\eta_{EQE}$ ) of  $Tb^{3+}$  PL were obtained through recording all spectra on samples and on a blank reference, using a  $BaSO_4$ -coated integration sphere<sup>20,21</sup>.

**Thermal properties.** The values of  $T_g$ ,  $T_c$  and  $T_x$  (peak temperature of crystallization) were obtained from differential scanning calorimetry (DSC, Netzsch DSC 404 F1), using a heating rate of 10 K/min. Non-isothermal crystallization dynamic were studied by DSC (Netzsch DSC 404 F1) on polished bulk glasses ( $\sim 25$ – $40$  mg) at different heating rates of 5, 10, 15 and 20 K/min in order to evaluate the apparent activation energy of crystallization.

**Other properties.** The composition of all glasses was verified by wavelength-dispersive electron probe microanalysis (WD-EPMA, microprobe JXA-8800L; Jeol). The ion concentration of  $Tb^{3+}$  was calculated according to these compositions. Nominal and as-received compositions are given in Tab. 1. The absence of crystals from the as-made glasses was verified by X-ray diffraction analyses (XRD Siemens Kristalloflex D500, Bragg-Brentano, 30 kV/30 mA, Cu K $\alpha$ ) on bulk samples. The glass density  $\rho$  was determined in an Archimedes balance, using distilled water as the immersion liquid. The refractive index was determined at the  $d$  line ( $n_d, \lambda = 587$  nm) with a Pulfrich reactometer.

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## Author contributions

L.W. and M.S. conceived of the experiment. A.W. prepared all glass samples. G.G., A.W., O.S., J.D. and C.D. performed the experiments. G.G., A.W. and L.W. analyzed the data. G.G. and L.W. wrote the manuscript. All authors contributed to the scientific discussions and manuscript review.

## Additional information

**Competing financial interests:** The authors declare no competing financial interests.

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