



# Invariance principles for local times at the maximum of random walks and Lévy processes

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Résumé en anglais	<p>We prove that when a sequence of Lévy processes <math>X^{(n)}</math> or a normed sequence of random walks <math>S^{(n)}</math> converges a.s. on the Skorokhod space toward a Lévy process <math>X</math>, the sequence <math>L^{(n)}</math> of local times at the supremum of <math>X^{(n)}</math> converges uniformly on compact sets in probability toward the local time at the supremum of <math>X</math>. A consequence of this result is that the sequence of (quadrivariate) ladder processes (both ascending and descending) converges jointly in law toward the ladder processes of <math>X</math>. As an application, we show that in general, the sequence <math>S^{(n)}</math> conditioned to stay positive converges weakly, jointly with its local time at the future minimum, toward the corresponding functional for the limiting process <math>X</math>. From this we deduce an invariance principle for the meander which extends known results for the case of attraction to a stable law.</p>
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