

Joint Component Sizing and Energy Management for Fuel Cell Hybrid Electric Trucks

Downloaded from: https://research.chalmers.se, 2022-07-02 09:36 UTC

Citation for the original published paper (version of record):

Xun, Q., Murgovski, N., Liu, Y. (2022). Joint Component Sizing and Energy Management for Fuel Cell Hybrid Electric Trucks. IEEE Transactions on Vehicular Technology, In press. http://dx.doi.org/10.1109/TVT.2022.3154146

N.B. When citing this work, cite the original published paper.

©2022 IEEE. Personal use of this material is permitted. However, permission to reprint/republish this material for advertising or promotional purposes

This document was downloaded from http://research.chalmers.se, where it is available in accordance with the IEEE PSPB Operations Manual, amended 19 Nov. 2010, Sec, 8.1.9. (http://www.ieee.org/documents/opsmanual.pdf).

Joint Component Sizing and Energy Management for Fuel Cell Hybrid Electric Trucks

Qian Xun, Student Member, IEEE, Nikolce Murgovski, Yujing Liu, Senior Member, IEEE

Abstract—This paper proposes a cost-effective way to design and operate fuel cell hybrid electric trucks (FCHETs) where a chance-constrained optimization is formulated. The aim of the introduced problem is to minimize a summation of component cost and operational cost with consideration of fuel cell (FC) degradation and cycle life of energy buffer. We propose to decompose the problem into two sub-problems that are solved by sequential convex programming. The delivered power satisfies a cumulative distribution function of the wheel power demand, while the truck can still traverse driving cycles with a similar speed and travel time without delivering unnecessarily high power. This allows to downsize powertrain components, including electric machine, FC and energy buffer. A case study considering different energy buffer technologies, including supercapacitor (SC), lithium-ion battery (LiB), and lithium-ion capacitor (LiC) is investigated in a set of trucking applications, i.e. urban delivery, regional delivery, construction, and long-haul. Results show that the power rating of the electric machine is drastically reduced when the delivered power is satisfied in a probabilistic sense. Moreover, the configuration with LiB as the energy buffer has the lowest expense but the truck with LiC can carry more payload.

Index Terms—Fuel cell hybrid electric trucks (FCHETs), chance-constrained, energy buffer, wheel power demand, sequential convex programming.

I. INTRODUCTION

EAVY duty vehicles, and freight transport in general, are known to emit large amount of greenhouse gas (GHG) emissions. One way of reducing these emissions is by exploring energy efficient solutions, such as electrification of transportation [1]. A typical example is battery electric vehicles, which can achieve zero-emissions, but major drawbacks of limited range and long "refueling" time make them less attractive in trucking applications. Alternatively, fuel cell (FC) vehicles might be a promising solution with the superiority in high energy density and fast refueling time. Among all FC types, polymer electrolyte membrane FC (PEMFC) is proved to be commercially suitable for transportation and automotive applications, especially for passenger cars, buses, logistic vehicles, and trucks [2]. A PEMFC-powered truck, without any GHG emissions if green hydrogen is assumed, can achieve a comparable performance to a conventional internal combustion engine vehicle in terms of driving range and refueling time [3]. For example, the XCIENT Fuel Cell [4], with a travel range of about 400 km, can be charged within 8

Manuscript received August 16, 2021;

The authors Qian Xun, Nikolce Murgovski, and Yujing Liu are with the Department of Electrical Engineering at the Chalmers University of Technology, Gothenburg 41296, Sweden (email: qian.xun@chalmers.se; nikolce.murgovski@chalmers.se; yujing.liu@chalmers.se).

to 20 min, depending on the ambient temperature and using a 350 bar tank with a capacity of 31 kg hydrogen.

However, a solely FC truck is prone to slow dynamics and is unable to recover regenerative energy. The hybridization of the FC with an energy storage system, e.g. supercapacitor (SC), lithium-ion battery (LiB), or a Lithium-ion capacitor (LiC), which combines advantages of both LiB and SC, is an essential way to meet the power demand and achieve required performance. Examples of commercial fuel cell hybrid electric trucks (FCHETs) are the Alpha truck [5], XCIENT Fuel Cell [6], and some other available truck models [7], [8]. Furthermore, the FC in an FCHET can be designed and operated to serve different goals, such as range extender or main power supply. In these trucks, component sizing and energy management are critical in reducing purchasing cost, increasing durability of FC stack and decreasing operational cost.

Energy management strategies for FC hybrid electric vehicles can be classified into heuristic and optimal. The heuristicbased methods are developed according to engineering experience and a series of rules, whereas the optimization-based schemes refer to solving a certain objective function subject to constraints. A fuzzy logic-based supervisory controller is implemented in [9] and [10] for FC/SC hybrid vehicles to meet the driving capability and enhance the FC performance. This method is also applied in [8] for an FC extended-range truck. In [11], a wavelet-based algorithm is used to decompose the load power into low- and high-frequency term to meet the vehicle power demand and enlarge the FC lifetime. A detailed study on energy management in FC/SC electric vehicles, especially the energy flow control, is reported in [12], and the short-term future energy demand is estimated to improve the hydrogen economy and power compliance. In [13], optimal energy management strategy is proposed based on mulltimode equivalent energy consumption method with consideration to four states of an FC hybrid electric tram, including traction, coasting, braking and station parking. A comprehensive investigation of energy management for FCHETs is presented in [14], where robustness of the control strategy, hydrogen economy and system lifetime are considered for real-world driving scenarios.

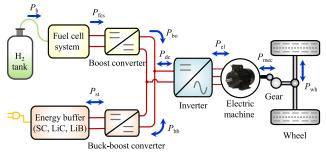
The optimization of component sizing for FC hybrid powertrains is another factor that determines vehicle cost, performance and hydrogen consumption. In [15], an optimal sizing methodology is proposed where SC and different battery technologies are investigated in terms of weight, volume, cost and hydrogen consumption for an FC electric vehicle. Optimal sizing of a plug-in FC hybrid city bus is performed based

on charge depleting and charge sustaining strategy in [16]. Component sizes and hydrogen consumption are estimated in [17] for FCHETs with an equivalent performance as diesel trucks. Moreover, [18] develops an optimum component sizing algorithm for FC/battery hybrid powertrains in class 4 delivery trucks and class 8 line-haul trucks to minimize relevant ownership cost. Energy sources are sized in [19] for an FC-based garbage truck using a statistical description of real-world driving data. In addition to the optimization of power sources in hybrid vehicles, electric drivetrain is optimized for a fleet of trucks using particle swarm algorithm with consideration of degrees of electrical machine commonality [20].

In some cases, component sizing and energy management are addressed at the same time to further optimize FC hybrid electric vehicles. Dynamic programming is applied in [21], [22], [23] to find optimal SC size and control strategies in a combined optimization of component sizing and energy management for an FC hybrid electric bus. In [24], a twoloop framework based on Pareto optimization is presented in combination with dynamic programming to solve a multiobjective optimization problem for an FC hybrid electric bus. Convex optimization has been performed in [25], [26], [27] for optimization of component sizing and energy management of FC electric buses hybridized with SC, battery, or both. Convex programming has also been used in [28] to optimize component sizing and energy management for an FC urban logistics vehicle. In [29], integrated design and control optimization is performed for an FC powered mining truck to minimize lifecycle cost. In [3], powertrain topologies, layout optimization, energy management strategies, and co-design optimization are summarized and reviewed.

Energy management and component sizing of FC hybrid electric vehicles have been separately or sequentially optimized in heavy-duty applications, including buses, trams and trucks. However, their combined optimization has only been well addressed in FC hybrid electric buses [25], [26], [27] and has not been comprehensively studied for trucking applications. To bridge this research gap, this paper presents a joint component sizing and energy management framework via convex optimization for FCHETs. Key contributions are listed as follows:

- A chance-constrained optimization problem is formulated for component sizing of electric machine, FC, and energy buffer, together with the energy management between FC and energy buffer along typical driving cycles. The proposed problem minimizes a summation of component cost and operational cost for a set of trucking applications, including urban delivery, regional delivery, construction, and long-haul.
- We propose decomposing the problem into two subproblems. Convex modeling steps are provided to effectively solve each sub-problem by sequential convex programming.
- Powertrain components are sized to satisfy wheel power demand with a user provided probability. This allows downsizing the components by not delivering unnecessarily high power, while ensuring a similar speed and travel time as those requested by specific driving cycles.



SC: supercapacitor; LiC: li-ion capacitor; LiB: Li-ion battery.

Fig. 1. Architecture of an FCHET propulsion system.

The component sizing and energy management are conducted together where three energy buffer technologies, including SC, LiC, and LiB are investigated. The FC degradation and cycle life of the energy buffer technologies have also been taken into account.

The remainder of the paper is organized as follows. Section II presents the system architecture and component models of an FCHET in detail. The introduced optimization problem is formulated in Section III and optimization method is described in Section IV. A case study and simulation results are discussed in Section V and followed by conclusions summarized in Section VI.

II. MODELING OF FCHET POWERTRAIN

We consider a fully active hybrid architecture, with two DC/DC converters connected to the FC and the energy buffer, as shown in Fig. 1. This architecture allows full controllability of the power allocation between the FC and the energy buffer (SC, LiC, and LiB). For more details see [30], [31], [32]. To better utilize the energy capacity of the energy buffer, the adopted FCHET is considered as a plug-in type. The wheel power is provided by an electric machine through a differential gear. The electric machine can also operate as a generator to recover the regenerative braking energy. A three-phase inverter is connected between DC/DC converters and the electric machine to achieve power conversion between DC and AC. At the DC-side, the FC provides power through a boost converter. An energy buffer i.e. a SC, a LiC or a LiB, delivers or receives power via a buck-boost converter.

The electrical power, which is consumed by driving wheels, is provided by the FC and the energy buffer. Therefore, the power balance equation can be deduced as

$$P_{\text{wh}}(t) + P_{\text{loss,em}}(t) + P_{\text{aux}}(t)$$

$$= \min \left(P_{\text{st}}(t) \eta_{\text{bb}}, \frac{P_{\text{st}}(t)}{\eta_{\text{bb}}} \right) + P_{\text{fcs}}(t) \eta_{\text{bo}},$$
(1)

where $P_{\rm wh}(t)=F_{\rm wh}(t)v(t)$ is the demanded wheel power, $F_{\rm wh}(t)$ is the demanded wheel force and v(t) is the desired truck speed, usually given as a driving cycle speed profile. The term $P_{\rm loss,em}(t)$ is the power losses of the drivetrain system, including the final gear, the electric machine, and the inverter, $P_{\rm aux}(t)$ is the auxiliary power during the truck movement, $P_{\rm st}(t)$ is the terminal power of the energy buffer, $P_{\rm fcs}(t)$ is the FC power, and $\eta_{\rm bo}$ and $\eta_{\rm bb}$ are the efficiencies of the

boost converter and buck-boost converter, respectively. The min function ensures that $\eta_{\rm bb}$ multiplies $P_{\rm st}$ when $P_{\rm st}$ is positive, and divides otherwise.

A. Driving Cycle Specifications

Four driving cycles are considered, which consist of road altitudes and speed profiles varying along travelled distance. They represent urban delivery, regional delivery, construction, and long-haul cycles for trucks, which are developed by the European association of car manufacturers (ACEA). The maximum acceleration and deceleration are defined as $2\,\mathrm{m/s^2}$ and $-1\,\mathrm{m/s^2}$, respectively. The total traveling length for all driving cycles is around $100\,\mathrm{km}$. The driving cycles, including the cumulative distribution function (CDF) of their corresponding accelerations, are illustrated in Fig. 2. The urban delivery cycle has the lowest average speed but includes most frequent accelerations and decelerations, whereas the long-haul cycle has the highest and relatively constant average speed.

B. Longitudinal Vehicle Dynamics

The truck is considered to be a rigid body, where the total mass is assumed to be constant, set to the maximum allowed value. According to the Newton's law of motion, the demanded wheel force can be written as

$$F_{\rm wh}(t) = (m_{\rm trk} + m_{\rm r})\dot{v}(t) + \frac{\rho_{\rm a}}{2}C_{\rm d}A_{\rm f}v^2(t) + C_{\rm r}m_{\rm trk}g\cos\alpha(t) + m_{\rm trk}g\sin\alpha(t),$$
(2)

where $m_{\rm trk}$ is the total truck mass including payload, $m_{\rm r}$ is the equivalent mass of all rotational parts, $\rho_{\rm a}$, $C_{\rm d}$, $A_{\rm f}$, $C_{\rm r}$, g and $\alpha(t)$ are the air density, drag coefficient, front area, rolling resistance coefficient, gravitational constant, and road slope, respectively.

The total truck mass consists of three parts and the mass balance is described as

$$m_{\rm trk} = x_{\rm fc} m_{\rm fc} + x_{\rm s} m_{\rm s} + m_0,$$
 (3)

where $x_{\rm fc}$ and $x_{\rm s}$ are the scaling factors of the FC system and the energy buffer. The terms $m_{\rm fc}$ and $m_{\rm s}$ are the baseline mass of the FC system and the energy buffer with the associated DC/DC converters, respectively. The term m_0 is the mass of the remaining parts, which is a function of decision variables for a constant truck mass. The equivalent mass of the rotational parts can be written as

$$m_{\rm r} = \frac{1}{r_{\rm wh}^2} \left(k_{\rm gr}^2 J_{\rm em} x_{\rm em} + J_{\rm wh} \right),$$
 (4)

where $r_{\rm wh}$ is the wheel radius, $k_{\rm gr}$ is the gear ratio, $x_{\rm em}$ is the scaling factor of the electric machine, and $J_{\rm em}$ and $J_{\rm wh}$ are the inertia of the baseline electric machine and all wheels, respectively. We denote $J_{\rm trk}=k_{\rm gr}^2J_{\rm em}x_{\rm em}+J_{\rm wh}$.

According to (2), the demanded torque on the shaft between the electric machine and the final gear can be derived in (5) when a lossless gear is assumed,

$$T_{\text{dem}}(t) = \frac{r_{\text{wh}}}{k_{\sigma r}} F_{\text{wh}}(t). \tag{5}$$

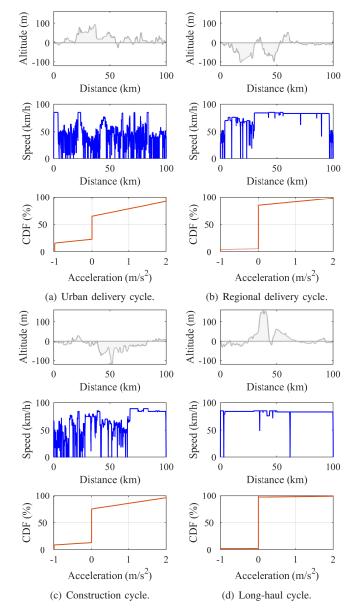


Fig. 2. Typical driving cycles and CDF of their acceleration sampled at every $1\,\mathrm{s}$.

Therefore, the wheel power demand can also be written as

$$P_{\rm wh}(t) = T_{\rm dem}(t)\omega(t),\tag{6}$$

where ω is the rotational speed of the electric machine.

C. Electric Drive System

A permanent magnet synchronous electric machine, with peak power of $200\,\mathrm{kW}$, peak torque of $2850\,\mathrm{Nm}$ and peak speed of $2500\,\mathrm{rpm}$, respectively, is used as a baseline in this case study. The power loss of the baseline electric machine, including losses of associated three-phase inverter, can be expressed as a quadratic function of electromagnetic torque T_{emb} ,

$$P_{\text{loss,emb}}(\omega(t), t) = a_0(\omega(t))T_{\text{emb}}^2(t) + a_1(\omega(t))T_{\text{emb}}(t) + a_2(\omega(t)),$$
(7)

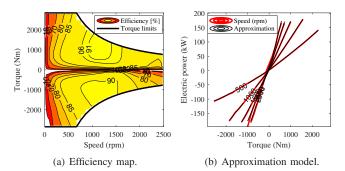


Fig. 3. Efficiency map and approximation model of the electric machine with the associated inverter.

where a_0 , a_1 and a_2 are speed-dependent parameters. Here, a_0 is non-negative, which guarantees that the loss model is convex in $T_{\rm emb}$ [33], [34], [35]. Therefore, the electrical power at the DC-side of the three-phase inverter is also a quadratic function of the torque. The efficiency map of the baseline electric machine with the associated inverter is shown in Fig. 3(a), and the approximated model and the measured data is shown in Fig. 3(b).

To meet the power demand of different driving cycles and various types of trucks, the electric machine can be scaled with a proper scaling factor $x_{\rm em}$. The power loss of the scaled electric machine with the associated inverter can be derived as

$$P_{\text{loss,em}}(t) = P_{\text{loss,emb}}(t)x_{\text{em}}.$$
 (8)

By substituting $T_{\rm em}(t)=T_{\rm emb}(t)x_{\rm em}$ into (7), (8) can be rewritten as

$$P_{\text{loss,em}}(t) = a_0(\omega(t)) \frac{T_{\text{em}}^2(t)}{x_{\text{em}}} + a_1(\omega(t)) T_{\text{em}}(t) + a_2(\omega(t)) x_{\text{em}}.$$
(9)

The torque balance can be written as

$$T_{\rm em} = T_{\rm dem}(t) + T_{\rm brk}(t), \tag{10}$$

where $T_{\rm brk}$ is the dissipated torque due to mechanical braking. Electromagnetic torque is constrained as

$$T_{\text{emb,min}}(\omega(t))x_{\text{em}} \leqslant T_{\text{em}}(t) \leqslant T_{\text{emb,max}}(\omega(t))x_{\text{em}},$$
 (11)

where $T_{\rm emb,min}$ and $T_{\rm emb,max}$ are the minimal and maximal torque limits of the baseline electric machine. The torque limits are functions of the rotational speed.

D. Fuel Cell System

1) Hydrogen Consumption Model: The PEMFC is an electrochemical energy conversion device that converts chemical energy directly into electrical energy. A baseline FC system model with power rating of $P_{\rm fcb,max}=50\,\rm kW$ is obtained from the Advanced Vehicle Simulator (ADVISOR) software (labeled as FCANL_50H2). The system conversion efficiency of the baseline model is illustrated in Fig. 4(a), which shows that the peak efficiency of 60% is achieved at around $20\,\rm kW$. Let $P_{\rm fcb}(t)$ denote the power of the baseline FC system that is limited within

$$0 \leqslant P_{\text{fcb}}(t) \leqslant P_{\text{fcb,max}}.$$
 (12)

Now, let

$$P_{\rm fcs}(t) = P_{\rm fcb}(t)x_{\rm fc} \tag{13}$$

be the scaled power of FCANL_50H2. Clearly, the power limit will now translate to

$$0 \leqslant P_{\text{fcs}}(t) \leqslant P_{\text{fcb,max}} x_{\text{fc}},$$
 (14)

with $x_{\text{fc,min}} \leqslant x_{\text{fc}} \leqslant x_{\text{fc,max}}$, where $x_{\text{fc,min}}$ should be greater than 0

The consumed hydrogen of the baseline FC model, $P_{\rm hb}$, can be approximated as a quadratic function of the electrical power,

$$P_{\rm hb}(t) = b_0 P_{\rm fcb}^2(t) + b_1 P_{\rm fcb}(t) + b_2, \tag{15}$$

where $b_j \ge 0$, $j \in \{0, 2\}$. The efficiency map of the baseline FC system and the corresponded approximated model are shown in Fig. 4(b). It can be seen that the fitted quadratic function captures the hydrogen consumption of the FC system with high accuracy. Similar quadratic model has also been used for system-level powertrain analysis in [25], [27].

Let

$$P_{\rm h}(t) = P_{\rm hb}(t)x_{\rm fc} \tag{16}$$

be the hydrogen consumption of the scaled FC system. By substitution of (13) and (16) into (15), hydrogen consumption in the scaled model can be written as

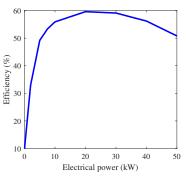
$$P_{\rm h}(t) = b_0 \frac{P_{\rm fcs}^2(t)}{x_{\rm fc}} + b_1 P_{\rm fcs}(t) + b_2 x_{\rm fc}.$$
 (17)

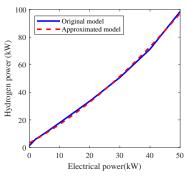
2) Degradation Model: During the FC operation, a degradation takes place, the rate of which depends on internal conditions, such as temperature, pressure, membrane water content, etc. Membrane electrode assembly degradation, which is mainly due to the fading of catalyst layer [36], proton exchange membrane [37] and gas diffusion layer [38], is recognised as the main factor that influences performance and lifetime [39], [40], [41]. This kind of degradation is closely determined by the load profile that is often classified into 5 categories [22], [42], [43], including constant load current, current cycling, extra-low current, extra-high current and open-circuit voltage. The state of the FC degradation is therefore simply characterized as the summation of the voltage degradation rate under each load profile. This model is usually used for statistical analysis of different load conditions.

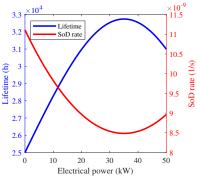
FC degradation in terms of insufficient humidification with gas starvation or flooding problems, occurs mainly due to large power variation $\dot{P}_{\rm fcs}(t)$. To reduce such degradation, $\dot{P}_{\rm fcs}(t)$ is bounded within a certain range, typically between 2% and 20% of maximum power per second [44]. In this work, a limit of $\pm 10\,\%$ is adopted.

The FC is considered as always in "ON" state and thus the start/stop-cycle-based degradation is ignored. To prevent the FC system operating at relatively low and high power, the state of degradation (SoD) in the baseline model at time instance t is defined as the integration of the degradation rate over time [45], [46]. This is mathematically expressed as

$$\operatorname{sod}_{\mathbf{b}}(t) = \int_{0}^{t} \dot{\operatorname{sod}}_{\mathbf{b}}(\tau) d\tau, \tag{18}$$







- (a) Efficiency map of the original model.
- (b) Approximation on hydrogen consump- (c) State of degradation with respect to power.

Fig. 4. Quasi-static fuel cell system modeling.

where $sod_b(t)$ is the degradation rate that is defined as a quadratic function determined by the FC operation power in a baseline model, which can be described as

$$\dot{\text{sod}}_{\text{b}}(t) = d_0 \left(\frac{P_{\text{fcs}}(t)}{x_{\text{fc}}}\right)^2 + d_1 \frac{P_{\text{fcs}}(t)}{x_{\text{fc}}} + d_2,$$
 (19)

where $d_j \ge 0$, $j \in \{0, 2\}$. This is depicted in Fig. 4(c), showing FC lifetime of at least 25000 hours according to the 2030 target for long-haul trucks. It can be seen that the fading rate of the SoD is greater when the FC operates at high or low power.

The SoD increasement over one driving cycle in a scaled model is constrained by

$$\operatorname{sod}(t_{\mathbf{f}}) - \operatorname{sod}(0) \leqslant \Delta \operatorname{sod}, \tag{20}$$

with $\Delta \mathrm{sod} = \frac{s_\mathrm{f}}{L_\mathrm{a} y_\mathrm{trk}} \mathrm{sod}_\mathrm{max}$, where s_f is the length of the driving cycle, L_a is the average travel distance per year, y_trk is the truck service years, and $\mathrm{sod}_\mathrm{max}$ is the maximum allowed degradation during its lifetime, which is usually set to 1. Notice that the degradation rate in a scaled FC model is assumed to be the same as that in the baseline model.

E. Energy Buffer

Different energy buffer technologies, including SCs, LiCs and LiBs, are examined in this study. For the respective technologies, the cells Maxwell BCAP3000, Aowei UCK42V28000, and Toshba SCiB20Ah are selected for the investigation, with their main parameters listed in Table I. The cells are modelled as a series connection of a resistor, $R_{\rm s}$, and an open circuit voltage (OCV), $u_{\rm s}$. The baseline model of energy buffer packs consists of several strings in parallel, with each string containing the same number of cells connected in series, as shown in Fig. 5, where $i_{\rm s}$ is the cell current, $n_{\rm s}$, $n_{\rm ss}$ and $n_{\rm sp}$ are the total numbers of the cells in the pack, number of series connected cells in a string and number of parallel connected strings, respectively.

Following the model by [27], [47], a linear approximation of the OCV of each technology can be uniformly presented as

$$u_{\rm s}(t) = \frac{Q_{\rm s}}{C_{\rm s}} {\rm soc_s}(t) + u_{\rm 0s}, \tag{21}$$

TABLE I SPECIFICATIONS OF SC, LIC, AND LIB.

	SC	LiC	LiB
Rated voltage (V)	2.7	3.5	2.3
Rated capacitance/capacity (F/As)	3000	28000	72000
Max. charge/discharge current (A)	-210/ 210	-150/ 150	-100/ 100
Internal resistance (Ω)	2.9×10^{-4}	3.5×10^{-4}	8.9×10^{-4}
Cycle lifetime (cycles)	1 000 000	1 000 000	15 000
Minimal SoC (%)	50	20	30
Maximal SoC (%)	95	90	80
Cell mass (kg)	0.51	0.83	0.52
Power density (W/kg)	5900	-	2200
Energy density (Wh/kg)	6	26	86

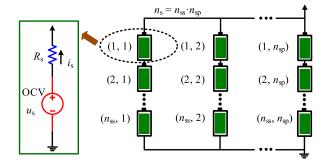


Fig. 5. Pack configuration of the energy buffer with $n_{\rm ss}$ cells connected in each string and $n_{\rm sp}$ strings connected in the pack.

where $Q_{\rm s}$, $C_{\rm s}$, ${\rm soc_s}$ and $u_{0\rm s}$ represent the rated capacity, rated capacitance, state of charge (SoC) and the initial voltage of the single cell. It should be noted that for SCs, the OCV changes linearly with the SoC level and that $u_{0\rm s}=0$. The LiC and LiB have non-zero minimum operation voltage, and linear approximations are implemented to fit the relationship between the OCV and the recommended SoC level, as shown in Fig. 6. The terminal pack power can be calculated as

$$P_{\rm stb}(t) = (u_{\rm s}(t)i_{\rm s}(t) - R_{\rm s}i_{\rm s}^2(t)) n_{\rm s},$$
 (22)

and the associated pack energy can be derived as

$$E_{\rm sb}(t) = n_{\rm s} Q_{\rm s} \int_0^{\rm soc_s(t)} \left(\frac{Q_{\rm s}}{C_{\rm s}} \rm soc_s(\tau) + u_{0\rm s} \right) d\rm soc_s(\tau)$$

$$= \frac{n_{\rm s} C_{\rm s}}{2} \left(u_{\rm s}^2(t) - u_{0\rm s}^2 \right). \tag{23}$$

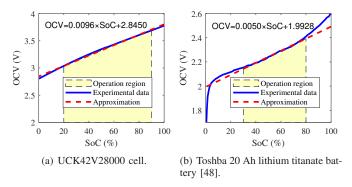


Fig. 6. OCV model of LiC and LiB with respect to the SoC levle.

By substitution of (23) into (22), the terminal pack power can be rewritten as

$$P_{\rm stb}(t) = P_{\rm sb}(t) - \left(\frac{P_{\rm sb}(t)}{n_{\rm ss}u_{\rm s}(t)}\right)^{2} \cdot \frac{n_{\rm ss}R_{\rm s}}{n_{\rm sp}}$$

$$= P_{\rm sb}(t) - \frac{R_{\rm s}C_{\rm s}P_{\rm sb}^{2}(t)}{2E_{\rm sb}(t) + u_{\rm 0s}^{2}C_{\rm s}n_{\rm s}}.$$
(24)

It can be seen that the pack energy and power are only dependent on the total number of cells and are not affected by the connection pattern. The pack dynamics is given as $E_{\rm sb}(t) = -P_{\rm sb}(t)$ where a positive power indicates that discharging current is applied to the energy buffer. The targeted energy buffer is a scaled version of the pack shown in Fig. 5 with $n_{\rm s}$ known a priory. The scaling factor $x_{\rm s}$ should satisfy

$$x_{\text{s,min}} \leqslant x_{\text{s}} \leqslant x_{\text{s,max}},$$
 (25)

where $x_{s,min}$ should be greater than 0.

When scaling the energy buffer, the targeted pack energy and power can be expressed as $E_{\rm s}=x_{\rm s}E_{\rm sb}$ and $P_{\rm s}=x_{\rm s}P_{\rm sb}$, respectively. Due to the physical limitation of the SoC level and the operation current for a single cell, the internal energy and power of the target pack during the operation need to be restricted to a safe range, which can be described as

$$\begin{split} &\frac{x_{\rm s}n_{\rm s}C_{\rm s}}{2}\left(u_{\rm s}^{2}({\rm soc_{\rm s,min}})-u_{0{\rm s}}^{2}\right)\leqslant E_{\rm s}(t)\\ &\leqslant \frac{x_{\rm s}n_{\rm s}C_{\rm s}}{2}\left(u_{\rm s}^{2}({\rm soc_{\rm s,max}})-u_{0{\rm s}}^{2}\right),\\ &i_{\rm s,min}\sqrt{x_{\rm s}n_{\rm s}\left(\frac{2E_{\rm s}(t)}{C_{\rm s}}+x_{\rm s}n_{\rm s}u_{0{\rm s}}^{2}\right)}\leqslant P_{\rm s}(t)\\ &\leqslant i_{\rm s,max}\sqrt{x_{\rm s}n_{\rm s}\left(\frac{2E_{\rm s}(t)}{C_{\rm s}}+x_{\rm s}n_{\rm s}u_{0{\rm s}}^{2}\right)}, \end{split} \tag{26}$$

where $soc_{s,min}$ and $soc_{s,max}$ are the minimal and maximal SoC of the cell while $i_{s,min}$ and $i_{s,max}$ denote the maximal charge and discharge current, respectively. Apparently, the following equations hold, $0 \le soc_{s,min} \le soc_{s,max}$ and $i_{s,min} \le 0 \le i_{s,max}$.

Additionally, to easily compare the investigated energy buffer technologies, the cycle life of the energy buffers is used as the evaluation index for the degradation. The energy throughput during their cycle lifetime is distributed evenly between each driving cycle. Therefore, the energy throughput for a given driving cycle should satisfy

$$\int_{0}^{t_{\rm f}} |P_{\rm s}(t)| \, \mathrm{d}t \leqslant \frac{2N_{\rm cl}x_{\rm s}n_{\rm s}E_{\rm cl}s_{\rm f}}{y_{\rm trk}L_{\rm a}},\tag{27}$$

where $N_{\rm cl}$ is the number of cycles in a whole lifetime and $E_{\rm cl}$ is the maximum allowable energy change per cell.

III. PROBLEM FORMULATION

The introduced optimization problem is aiming to find the optimal capacity of the FC and the energy buffer, optimal power rating of the electric machine and the optimal power allocation between the FC and the energy buffer, such that the truck can traverse the driving cycle with a similar speed and travel time to those demanded. The performance metrics of trucks considered in this paper include total cost, driving range with one-time refueling, average service time, annual travel distance, acceleration characteristics, and typical driving cycle performance. The FC degradation and cycle life constraint of energy buffers are also considered, which are included into the capital cost of FC and energy buffers.

A. Objective Function

The optimization objective is formulated to minimize a cost function J, consisting of operational cost and component cost over the pre-defined driving cycle. It can be described as

$$J = C_{\rm H2} + C_{\rm ele} + C_{\rm fcs} + C_{\rm eb} + C_{\rm em},$$
 (28)

where $C_{\rm H2}$, $C_{\rm ele}$, $C_{\rm fcs}$, $C_{\rm eb}$ and $C_{\rm em}$ are the cost of hydrogen consumption, electricity consumption, FC system, energy buffer and electric machine, respectively. To make the costs comparable, each cost is normalized in euros per km. Therefore, the hydrogen cost is written as

$$C_{\rm H2} = \frac{\beta_{\rm h}}{L_{\rm dc}C_{\rm h}} \int_0^{t_{\rm f}} P_{\rm h} {\rm d}t,$$
 (29)

with β_h being the hydrogen cost per kg and C_h being the lower heating value of hydrogen in J/kg. The electricity cost is written as

$$C_{\text{ele}} = \frac{\beta_{\text{ele}}}{L_{\text{de}}} (E_{\text{s}}(0) - E_{\text{s}}(t_{\text{f}})),$$
 (30)

with $\beta_{\rm ele}$ being the unit price of electricity, $E_{\rm s}(0)$ and $E_{\rm s}(t_{\rm f})$ being the stored energy of energy buffer at the beginning and the end of a driving cycle, respectively. The energy change during a travel range $L_{\rm range}$, typically in the order of 600-800 km, should be limited to the maximum stored energy. As a driving cycle has shorter length than $L_{\rm range}$, we assume that this energy change is evenly distributed into each driving cycle. Therefore, the energy change over one driving cycle should satisfy

$$-\frac{s_{\rm f}}{L_{\rm range}} \Delta E_{\rm s,max} \leqslant E_{\rm s}(0) - E_{\rm s}(t_{\rm f}) \leqslant \frac{s_{\rm f}}{L_{\rm range}} \Delta E_{\rm s,max}, \quad (31)$$

where $\Delta E_{\rm s,max}$ is the maximum allowable energy change during the travel range, which can be calculated as

$$\Delta E_{\text{s,max}} = \frac{x_{\text{s}} n_{\text{s}} C_{\text{s}}}{2} \left(u_{\text{s}}^2 (\text{soc}_{\text{s,max}}) - u_{\text{s}}^2 (\text{soc}_{\text{s,min}}) \right). \quad (32)$$

The cost of the FC system includes the capital cost and the degradation cost. The degradation is converted into its equivalent capital cost according to the FC SoD. Then the FC cost is computed by

$$C_{\text{fcs}} = \frac{(1 + \text{sod}(t_{\text{f}})) \beta_{\text{fcs}} P_{\text{fcb,max}} x_{\text{fc}}}{L_{\text{a}} y_{\text{trk}}} \text{CF}, \qquad (33)$$

with $\beta_{\rm fcs}$ being the FC system price per kW and CF denoting the cost factor that is related to the truck service period and the yearly interest rate $p_{\rm v}$. The cost factor is described as

$$CF = 1 + p_y \frac{y_{trk} + 1}{2},$$
 (34)

and it also applies to the cost of energy buffer and electric machine. The cost of the energy buffer is calculated as

$$C_{\rm eb} = \frac{\beta_{\rm eb} x_{\rm s} n_{\rm s} C_{\rm s}}{2L_a y_{\rm trk}} \left(u_{\rm s,max}^2 - u_{\rm s,min}^2 \right) \text{CF}, \tag{35}$$

with $\beta_{\rm eb}$ being the energy buffer price per kWh, $u_{\rm s,min}$ and $u_{\rm s,max}$ denoting the minimal and maximal OCV of the cell. The cost of the electric machine is computed as

$$C_{\rm em} = \frac{\beta_{\rm em} x_{\rm em} P_{\rm emb, max}}{L_{\rm a} y_{\rm trk}} \text{CF}, \tag{36}$$

where $\beta_{\rm em}$ is the electric machine price per kW and $P_{\rm emb,max} = \max_k (T_{\rm emb,max,k} \, \omega_k)$ represents the peak power of the baseline electric machine, where k is any feasible operating point.

B. Chance-constrained Optimization

The wheel power demand in (1) directly translates to a minimum size of electric machine and cumulative power provided by the FC system and energy buffer. It is of interest to investigate smaller component sizes that provide requested power most of the time, except perhaps at a few instances. The idea is to get robust component sizes by removing outliers in noisy measurements (or unrealistic reference points), and also enabling a sensitivity analysis on how component sizes change with demanded power, while trying to maintain travel time requirements.

Thus, the constraint (1) can be rewritten as a chance-constraint,

$$\mathbb{P}\left(\begin{array}{c} \min\left(P_{\rm st}(t)\eta_{\rm bb}, \frac{P_{\rm st}(t)}{\eta_{\rm bb}}\right) + P_{\rm fcs}(t)\eta_{\rm bo} \\ \geqslant P_{\rm wh}(t) + P_{\rm loss,em}(t) + P_{\rm aux}(t) \end{array}\right) \geqslant \gamma, \quad (37)$$

where $\gamma \in (0,1]$ is a pre-assigned probability for constraint satisfaction. Notice that the equality (1) has been relaxed to inequality, within the parentheses in (37), in order to ensure problem convexity. However, it has been shown in previous studies that for the optimal solution, the relaxation will indeed hold with equality, as otherwise energy will be wasted unnecessarily [49], [50]. Furthermore, the inequality outside the parentheses in (1) requires that the FC and the energy buffer are able to deliver what is demanded by the driving cycle, up to a given probability. Any $\gamma < 1$ in (37) allows downsizing the FC, energy buffer, electric machine and the power electronics by delivering less power than demanded for some time intervals, which consequently will cause the truck

speed to deviate from that requested by the driving cycles. In this study we require delivering demanded speed as close as possible and traversing the cycle with as close travel time as possible, but still not delivering unnecessarily more power than what is needed to satisfy (37). Due to didactic reasons, we state this as a verbal constraint in the problem description below. Later, in Section IV, a detailed mathematical treatment is provided after the main idea of the proposed method is explained.

By summarizing the objective function and all constraints, the problem can be formulated as

$$\min_{x_{\text{em}}, x_{\text{fc}}, x_{\text{s}}, P_{\text{fcs}}, P_{\text{s}}, T_{\text{brk}}, E_{\text{s}}, \text{sod}} J, \tag{38a}$$

s.t.
$$\mathbb{P}\left(\begin{array}{c} \min\left(P_{\rm st}(t)\eta_{\rm bb}, \frac{P_{\rm st}(t)}{\eta_{\rm bb}}\right) + P_{\rm fcs}(t)\eta_{\rm bo}, \\ \geqslant P_{\rm wh}(t) + P_{\rm loss,em}(t) + P_{\rm aux}(t) \end{array}\right) \geqslant \gamma,$$
(38b)

$$T_{\rm em}(t) = T_{\rm dem}(t) + T_{\rm brk}(t), \tag{38c}$$

$$T_{\mathrm{emb,min}}(\omega(t))x_{\mathrm{em}} \leqslant T_{\mathrm{em}}(t) \leqslant T_{\mathrm{emb,max}}(\omega(t))x_{\mathrm{em}},$$
 (38d)

$$0 \leqslant P_{\text{fcs}}(t) \leqslant x_{\text{fc}} P_{\text{fcb,max}},\tag{38e}$$

$$x_{\text{fc,min}} \leqslant x_{\text{fc}} \leqslant x_{\text{fc,max}},$$
 (38f)

$$x_{\rm fc}R_{\rm fcb,min} \leqslant \dot{P}_{\rm fcs}(t) \leqslant x_{\rm fc}R_{\rm fcb,max},$$
 (38g)

$$\dot{\text{sod}}(t) = d_0 \left(\frac{P_{\text{fcs}}(t)}{x_{\text{fc}}}\right)^2 + d_1 \frac{P_{\text{fcs}}(t)}{x_{\text{fc}}} + d_2, \tag{38h}$$

$$sod(0) = 0, (38i)$$

$$sod(t_f) \leqslant \Delta sod,$$
 (38j)

$$\dot{E}_{\rm s} = -P_{\rm s}(t),\tag{38k}$$

$$\frac{x_{\rm s} n_{\rm s} C_{\rm s}}{2} \left(u_{\rm s}^2({\rm soc_{\rm s,min}}) - u_{0\rm s}^2 \right) \leqslant E_{\rm s}(t), \tag{381}$$

$$\frac{x_{\rm s}n_{\rm s}C_{\rm s}}{2}\left(u_s^2({\rm soc_{\rm s,max}}) - u_{0\rm s}^2\right) \geqslant E_{\rm s}(t),$$
 (38m)

$$-\frac{s_{\rm f}}{L_{\rm range}} \Delta E_{\rm s,max} \leqslant E_{\rm s}(0) - E_{\rm s}(t_{\rm f}) \leqslant \frac{s_{\rm f}}{L_{\rm range}} \Delta E_{\rm s,max}, \tag{38n}$$

$$i_{s,\min} \sqrt{x_s n_s \left(\frac{2E_s(t)}{C_s} + x_s n_s u_{0s}^2\right)} \leqslant P_s(t),$$
 (380)

$$i_{\text{s,max}}\sqrt{x_{\text{s}}n_{\text{s}}\left(\frac{2E_{\text{s}}(t)}{C_{\text{s}}} + x_{\text{s}}n_{\text{s}}u_{0\text{s}}^{2}\right)} \geqslant P_{\text{s}}(t),$$
 (38p)

$$\int_{0}^{t_{\rm f}} |P_{\rm s}(t)| \, \mathrm{d}t \leqslant \frac{2N_{\rm cl}x_{\rm s}n_{\rm s}E_{\rm cl}s_{\rm f}}{y_{\rm trk}L_{\rm a}},\tag{38q}$$

$$x_{s,\min} \leqslant x_s \leqslant x_{s,\max},$$
 (38r)

drive as close as possible to demanded speed and travel time. (38s)

The optimization variables consist of the scalar scaling variables $x_{\rm em}$, $x_{\rm fc}$, $x_{\rm s}$, the time dependent control variables $P_{\rm fcs}$, $P_{\rm s}$ and $T_{\rm brk}$, and the time dependent state variables $E_{\rm s}$ and sod. The problem has, in fact, two additional state variables that are not written in a standard form. The constraint (38g) limits the baseline FC power variation rate to be within $[R_{\rm fcb,min}, R_{\rm fcb,max}]$, which means that $P_{\rm fcs}$ can be regarded as a state in the problem. Similarly, the constraint on the cycle life (38q) can be written without the integral form, by

introducing an additional state with the time derivative equal to the absolute value of the energy buffer power.

The objective function is convex with respect to $P_{\rm fcs}$, $E_{\rm s}$, $x_{\rm fc}$, $x_{\rm s}$ and $x_{\rm em}$. The convexity of the chance-constraint (38b) for power balance and the verbal constraint (38s) will be discussed in Section IV. The constraints (38c)-(38g), (38i)-(38n), (38r) are affine relations, and therefore convex. The constraints (38o)-(38q) are nonlinear, but they define a convex set. The former two can be recognized as a geometric mean function, which is concave in $x_{\rm s}$ and $E_{\rm s}$, while the latter is an absolute value, which is convex in $P_{\rm s}$. The constraint (38h) is a nonlinear equality constraint and thus is not convex.

It can be concluded that in the present form, problem (38) is a nonlinear and non-convex dynamic program that includes both time dependent and scalar optimization variables. Moreover, the problem includes a chance constraint and related constraints in (38s) that are yet to be defined. As the problem is difficult to solve, we propose first decomposing it into two subproblems. Then, remodelling steps are performed to convexify both sub-problems.

IV. OPTIMIZATION METHOD

In this section, we show that problem (38) can be translated to an equivalent deterministic problem, decomposed into two sub-problems. Then, we show convex modelling steps such that the problem can be solved by sequential convex programming.

A. Deterministic Programming

It is possible to translate the chance-constrained optimization problem (38) into a deterministic program. The constraint satisfaction with a selected probability $\gamma \in (0,1]$ can be seen as finding an upper bound, $P_{\rm wh}^{\rm max}(\gamma)$, on the wheel power demand to make (39) hold, i.e.

$$P_{\text{wh}}^{\text{max}}(\gamma) = \max \left(P_{\text{wh}}(t) \in \mathcal{P}_{\text{wh}} : \text{cdf}(P_{\text{wh}}(t)) \leqslant \gamma \right).$$
 (39)

Here.

$$\operatorname{cdf}(P_{\operatorname{wh}}(t)) = \mathbb{P}\left(P_{\operatorname{wh}}(t) \in \mathcal{P}_{\operatorname{wh}} : P_{\operatorname{wh}}(t) \leqslant P_{\operatorname{wh}}^{\max}(1)\right) \tag{40}$$

defines the CDF of the wheel power demand $P_{\rm wh}(t)$, with

$$\mathcal{P}_{\text{wh}} = \left\{ P_{\text{wh}}(t) \right\}, \quad \forall t \in [0, t_{\text{f}}],$$

$$P_{\text{wh}}^{\text{max}}(1) = \max \left(P_{\text{wh}}(t) \in \mathcal{P}_{\text{wh}} \right),$$
(41)

where $P_{\rm wh}^{\rm max}(1)$ is the upper limit of constraint satisfaction with a probability $\gamma=1$.

For the given driving cycles, the wheel power demand can be calculated from longitudinal vehicle dynamics, noting that the truck mass significantly differs with its vocation. We assume that the maximum gross weight of trucks for applications of urban delivery, regional delivery, construction and long-haul is 18, 27, 33, and 40 tons, respectively [20], [51]. The truck specifications and environmental parameters are listed in Table II. According to ACEA driving cycles, the maximum demanded acceleration is $2\,\mathrm{m/s^2}$, which might not be reasonable for all trucks. The excessive acceleration can result in unrealistic power requirements. For example, the

TABLE II
TRUCK SPECIFICATIONS AND ENVIRONMENT PARAMETERS.

Parameter (unit)	Value	
Max. gross weight, $m_{\rm trk}$ (ton)	18 /27 /33 /40	
Front area, $A_{\rm f}~({\rm m}^2)$	10	
Final gear ratio, $k_{\rm gr}$ (-)	3	
Wheel radius, $r_{\rm wh}$ (m)	0.5	
$^{ m a}$ Wheel inertia, $J_{ m wh}$ (kgm 2)	90	
Baseline electric machine inertia, $J_{\rm em}~({\rm kgm^2})$	1.92	
Auxiliary power, P_{aux} (kW)	5.6	
Gravitational acceleration, g (m/s ²)	9.81	
Air density, ρ_a (kg/m ³)	1.184	
Rolling resistance coefficient, $C_{\rm r}$ (-)	0.007	
Aerodynamic drag coefficient, $C_{ m d}$ (-)	0.7	

^aEstimated according to 4×2 axle configuration.

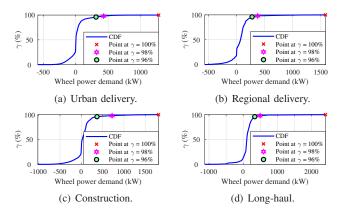


Fig. 7. Cumulative distribution function of the wheel power demand for different trucking applications.

peak wheel power demand is estimated to reach $1.30\,\mathrm{MW},$ $1.61\,\mathrm{MW},$ $1.84\,\mathrm{MW},$ and $2.44\,\mathrm{MW}$ in applications of urban delivery, regional delivery, construction, and long-haul trucking.

The cumulative distribution function of the estimated power demand for the four trucking applications is shown in Fig. 7. It can be seen that high peak power demands happen rarely. For instance, the probability is only 4% when the power demand exceeds $319\,\mathrm{kW}$ for urban delivery, $275\,\mathrm{kW}$ for regional delivery, $370\,\mathrm{kW}$ for construction, and $339\,\mathrm{kW}$ for long-haul application. Therefore, a selected $\gamma \in (0,1]$ makes it possible to use a lower power rating of the electric machine, the FC, the energy buffer and the associated power electronic converters, leading to a lower cost. Example points when γ equals to 96%, 98%, and 100% are marked in Fig. 7, while the upper bounds of the corresponded delivered power satisfying these probabilities are listed in Table III. Clearly, the selection of γ also determines driveability, as bigger γ allows more aggressive driving.

The upper bound of the wheel power demand, $P_{\rm wh}^{\rm max}(\gamma)$, can be obtained from Fig. 7 once the value of γ is determined. Then, the power balance in constraint (38b) can be written as a deterministic constraint

$$\min \left(P_{\text{st}}(t) \eta_{\text{bb}}, \frac{P_{\text{st}}(t)}{\eta_{\text{bb}}} \right) + P_{\text{fcs}}(t) \eta_{\text{bo}}$$

$$- P_{\text{loss,em}}(t) - P_{\text{aux}}(t) \geqslant \min(P_{\text{wh}}(t), P_{\text{wh}}^{\text{max}}(\gamma)),$$
(42)

TABLE III UPPER BOUNDS OF WHEEL POWER DEMAND SATISFYING PROBABILITIES.

Driving cycles	$P_{\mathrm{wh}}^{\mathrm{max}}(1)$	$P_{\rm wh}^{\rm max}(0.98)$	$P_{\rm wh}^{\rm max}(0.96)$
Diffing cycles	kW	kW	kW
Urban delivery	1296	438	319
Regional delivery	1605	375	275
Construction	1837	735	370
Long-haul	2444	496	339

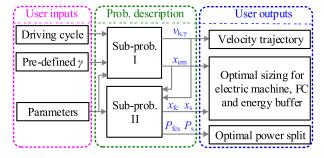


Fig. 8. Problem decomposition and optimization framework.

for all time instances, which means that the delivered power series is saturated with $P_{\rm wh}^{\rm max}(\gamma)$ during the truck movement.

Therefore, the stochastic program (38) is then translated to a deterministic program with the chance-constraint (38b) replaced by the deterministic constraint (42).

B. Problem Decomposition

Since the power rating of the electric machine is only determined by the CDF of the wheel power demand for a given driving cycle, the electric machine sizing can be performed offline. Once the electric machine is sized, the velocity trajectory of trucks can be obtained with respect to the verbal constraint (38s). The remaining component sizing and energy management can be dealt with using the determined electric machine size and the obtained velocity trajectory.

Therefore, the solution to the deterministic program derived from the stochastic program (38) can be decomposed by solving two sub-problems sequentially, as shown in Fig. 8. The aim of each sub-problem can be summarized as

- Sub-problem I: find a proper sizing of the electric machine and filter out the velocity trajectory corresponding to the wheel power demand $P_{\text{wh},\gamma}(t)$ with the aim to drive as close as possible to the demanded speed and travel time but with the delivered wheel power following a cumulative probability γ ;
- Sub-problem II: find an optimal sizing for FC and energy buffer as well as the optimal power split between each power source to minimize the summation of the components cost and the operational cost by using the electric machine sizing and velocity trajectory obtained from Sub-problem I.

We assume that the equivalent mass of all rotational parts does not change significantly with the electric machine sizing in Sub-problem I.

After solving Sub-problem I, the delivered power trajectory, denoted as $P_{\text{wh},\gamma}(t)$, is possible to obtain from the new velocity trajectory. This is enforced by

$$\min \left(P_{\text{st}}(t) \eta_{\text{bb}}, \frac{P_{\text{st}}(t)}{\eta_{\text{bb}}} \right) + P_{\text{fcs}}(t) \eta_{\text{bo}}$$

$$- P_{\text{loss,em}}(t) - P_{\text{aux}}(t) \geqslant P_{\text{wh},\gamma}(t).$$
(43)

With $P_{\mathrm{wh}}^{\mathrm{max}}(\gamma)$ determined, constraint (42) can be replaced by constraint (43) after solving Sub-problem I, which is used as the power balance constraint in Sub-problem II. The reason for this is that (43) is more restrictive, i.e.

$$P_{\text{wh},\gamma}(t) \geqslant \min(P_{\text{wh}}(t), P_{\text{wh}}^{\text{max}}(\gamma)), \forall t \in [0, t_{\text{f}}]. \tag{44}$$

C. Sub-problem for Limiting Demanded Power and Electric Machine Sizing

Since Sub-problem I can be separated from problem (38), the sampling in distance is performed to simplify the introduction of constraints on the travel time. Let the following sets define driving and stand-still instances

$$S_{\text{drv}} = \{ s \in [0, s_f] \mid E_k(s) > 0 \}, \tag{45}$$

$$S_{ss} = \{ s \in [0, s_f] \mid E_k(s) = 0 \}, \tag{46}$$

where s is the distance instance. The kinetic energy of the truck in the distance-domain, when $\gamma = 1$ is assumed, can be computed by

$$E_{\rm k}(s) = \frac{1}{2}(m_{\rm trk} + m_{\rm r})v(s)^2,$$
 (47)

with v(s) being the distance-based speed from the original driving cycle. Once $P_{\mathrm{wh}}^{\mathrm{max}}(\gamma)$ is obtained, the maximum power of the electric machine can be determined with the scaling factor calculated as

$$x_{\rm em} = \frac{P_{\rm wh}^{\rm max}(\gamma)}{P_{\rm emb,max}}.$$
 (48)

The problem of closely following the original speed, while keeping the delivered power limited and trying to finish the route in about the same time, can be formulated as

$$\begin{split} \min_{\sigma, E_{\mathbf{k}, \gamma}, F_{\mathbf{wh}, \gamma}, t_{\gamma}} c_{\text{time}} \sigma + \int_{0}^{s_{\text{f}}} \left(E_{\mathbf{k}, \gamma}(s) - E_{\mathbf{k}}(s) \right)^{2} \mathrm{d}s, \quad \text{(49a)} \\ \frac{\mathrm{d}E_{\mathbf{k}, \gamma}(s)}{\mathrm{d}s} &= -\frac{\rho_{a} C_{d} A_{f}}{m_{\text{trk}} + m_{r}} E_{\mathbf{k}, \gamma}(s) + F_{\mathbf{wh}, \gamma}(s) - F_{\alpha}(s), \end{split} \tag{49b}$$

$$\frac{\mathrm{d}t_{\gamma}(s)}{\mathrm{d}s} = \begin{cases} \frac{1}{\sqrt{2E_{k,\gamma}(s)/(m_{\mathrm{trk}} + m_r)}}, & \forall s \in \mathcal{S}_{\mathrm{drv}} \\ \Delta t_{\mathrm{ss}}(s)\delta(s), & \forall s \in \mathcal{S}_{\mathrm{ss}} \end{cases}, \tag{49c}$$

$$0 < E_{k,\gamma}(s) \leqslant \max_{s}(E_k(s)), \quad \forall s \in \mathcal{S}_{drv},$$
 (49d)

$$E_{\mathbf{k},\gamma}(s) = 0, \quad \forall s \in \mathcal{S}_{ss},$$
 (49e)

$$t_{\gamma}(0) = 0, \quad t_{\gamma}(s_{\rm f}) \leqslant t(s_{\rm f}) + \sigma,$$
 (49f)

$$t_{\gamma}(0) = 0, \quad t_{\gamma}(s_{\mathrm{f}}) \leqslant t(s_{\mathrm{f}}) + \sigma, \tag{49f}$$

$$F_{\mathrm{wh},\gamma}(s) \geqslant -\frac{P_{\mathrm{wh}}^{\mathrm{max}}(\gamma)}{\sqrt{2E_{\mathrm{k},\gamma}(s)/(m_{\mathrm{trk}} + m_{\mathrm{r}})}}, \forall s \in \mathcal{S}_{\mathrm{drv}}, \tag{49g}$$

$$F_{\text{wh},\gamma}(s) \leqslant \frac{P_{\text{wh}}^{\text{max}}(\gamma)}{\sqrt{2E_{\text{k},\gamma}(s)/(m_{\text{trk}} + m_{\text{r}})}}, \forall s \in \mathcal{S}_{\text{drv}}, \quad (49\text{h})$$

$$\frac{T_{\mathrm{emb,min}}(s)x_{\mathrm{em}}k_{\mathrm{gr}}}{r_{\mathrm{wh}}} \leqslant F_{\mathrm{wh},\gamma}(s) \leqslant \frac{T_{\mathrm{emb,max}}(s)x_{\mathrm{em}}k_{\mathrm{gr}}}{r_{\mathrm{wh}}}, \forall s,$$
(49i)

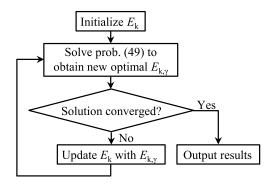


Fig. 9. Iterative procedure for solving Sub-problem I to minimize linearization error

where the objective function in (49a) is trying to deliver similar speed and travel time as the original driving cycle. In practice, this means that the acceleration is limited for some instances due to the limited power rating of the electric machine while higher speed is allowed for some other instances to make sure that the truck still arrives on time. When γ is too low it may not be possible to maintain the desired travel time and, hence, the constraint on final time is modeled as a soft constraint, where σ is a slack variable and $c_{\rm time}$ is a weighting coefficient penalizing longer time. The variable $E_{k,\gamma}(s)$ denotes the truck kinetic energy when the delivered power has a cumulative probability not greater than γ . The constraint (49b) represents the dynamics of the kinetic energy and can be derived from (2) with $F_{\alpha}(s)$ being the summation of all forces related to the road slope. The constraint (49c) describes the time dynamics where the time difference is computed by integration of the inverse speed over the traveled distance when the truck is moving; when the truck is standing still, a Dirac function, $\delta(s)$, is used to account for the standstill time, $\Delta t_{\rm ss}$. The constraint (49d) ensures $E_{k,\gamma}(s)$ to be greater than 0 but smaller than the maximum original kinetic energy. The constraint (49e) keeps the truck having zero kinetic energy at stand-still instances. The constraint (49f) enforces the initial time to 0 and includes the soft constraint on the final time to ensure the truck driver arrives at the destination in a similar time as that of the original driving cycle. The constraints (49g) and (49h) limit the wheel force with the upper bound of the wheel power demand $P_{\rm wh}^{\rm max}(\gamma)$. The constraint (49i) is the wheel force limit computed from the torque bound of the electric machine. In principle, only upper bound of the wheel force is required for a given γ , but here the lower bound is also applied to limit the regenerative braking torque, which does not affect the component sizing [52], [53].

The optimization variables include the scalar scaling variable σ , distance dependent control variable $F_{\mathrm{wh},\gamma}$, and state variables $E_{\mathrm{k},\gamma}$ and t_{γ} . As can be seen, the objective function is convex with respect to σ and $E_{\mathrm{k},\gamma}$. The constraints (49b), (49d)-(49f) are affine relations, and thus convex. The constraints (49c), (49g) and (49h) are nonlinear and (49i) also contains the same nonlinear term that describes the torque limit at the constant power region of the electric machine. Therefore, both of them are not convex.

To preserve the convexity, the constraint (49c) can be

relaxed as an inequality,

$$\frac{\mathrm{d}t_{\gamma}(s)}{\mathrm{d}s} \geqslant \begin{cases} \frac{1}{\sqrt{2E_{\mathrm{k},\gamma}(s)/(m_{\mathrm{trk}} + m_{\mathrm{r}})}} & \forall s \in \mathcal{S}_{\mathrm{drv}} \\ \Delta t_{\mathrm{ss}}(s)\delta(s) & \forall s \in \mathcal{S}_{\mathrm{ss}} \end{cases}, \tag{50}$$

thus becoming a convex constraint. It has been shown in a similar problem [54] that the constraint is tight at the optimal solution and the solution to the relaxed problem is identical to the solution of the original problem. The nonlinear term in the constraints (49g)-(49i), $\frac{P_{\rm wh}^{\rm max}(\gamma)}{\sqrt{E_{\rm k,\gamma}(s)/(m_{\rm trk}+m_{\rm r})}}, \ {\rm can}$ be linearized by a first-order Taylor expansion at the kinetic energy when $\gamma=1$, shown as

$$\frac{P_{\text{wh}}^{\text{max}}(\gamma)}{\sqrt{nE_{\text{k},\gamma}(s)}} = \frac{P_{\text{wh}}^{\text{max}}(\gamma)}{\sqrt{nE_{\text{k}}(s)}} - \frac{P_{\text{wh}}^{\text{max}}(\gamma)}{2\sqrt{nE_{\text{k}}(s)^3}} \left(E_{\text{k},\gamma}(s) - E_{\text{k}}(s)\right),\tag{51}$$

with $n=2/(m_{\rm trk}+m_{\rm r})$. Therefore, (51) shows affine relation and constraints (49g)-(49i) are converted into convex constraints. To reduce the linearization error, sequential convex programming is performed by iteratively updating $E_{\rm k}$ with the latest $E_{\rm k,\gamma}$ after solving problem (49) until the solution stops changing. The iterative procedure for minimizing linearization error is illustrated in Fig. 9.

D. Sub-problem for Power Sources Sizing and Energy Management

After performing the electric machine sizing in Sub-problem I, the cost of the electric machine can be excluded from the objective function in problem (38). Sub-problem II can then be written as

$$\min(C_{\rm H2} + C_{\rm ele} + C_{\rm fcs} + C_{\rm eb}),$$
 (52)

subject to (38c)-(38r) and (43).

The FC and the energy buffer are designed to prioritize the delivery of propulsion power while the excessive braking power can be handled by mechanical braking. The amount of mechanical braking torque is affected by the capacity of the energy buffer. To avoid the calculation of mechanical braking torque in the optimization [55], the equality constraint in (38c) can be relaxed as an inequality constraint, which can be expressed as

$$T_{\rm em}(t) \geqslant T_{\rm dem}(t),$$
 (53)

and the optimization variable $T_{\rm brk}$ can be dropped out.

To convexity the constraint (38h), a variable change sodx is introduced, which is also used to scale up the SoD variation over one driving cycle to improve the solver convergence. The term sodx can then be written as

$$\operatorname{sodx}(t) = \frac{\operatorname{sod}(t)}{\Delta \operatorname{sod}} x_{\operatorname{fc}}, \tag{54}$$

where $sod(t) \in [0, \Delta sod]$ with $t \in [0, t_f]$. At the beginning of the driving cycle sodx(0) = 0 and at the end of the driving cycle, $sodx(t_f) \leq x_{fc}$. Take the derivative of (54) to obtain

$$\dot{\text{sodx}}(t) = \dot{\text{sod}}(t) \frac{x_{\text{fc}}}{\Delta \text{sod}}.$$
 (55)

TABLE IV
MAIN PARAMETERS FOR CASE STUDY.

Parameter (unit)	Value
aHydrogen price, β _h (€/kg)	3.94
Hydrogen lower heating value, $C_{\rm h}$ (J/kg)	120×10^{6}
^b Electricity unit price, β _{ele} (€/kWh)	0.12
^c Fuel cell system price, β _{fcs} (€/kW)	77
	3880 for SC
^d Energy buffer price, β _{eb} (€/kWh)	1939 for LiC
	243 for LiB
Travel range with one-time refueling, $L_{\rm range}$ (km)	600/ 600/ 600/ 800
Yearly average travel distance, $L_{\rm a}$ (km/year)	80 000
Truck average service year, $y_{\rm trk}$ (year)	10
Yearly interest rate, p_y (-)	5%
Efficiency of DC/DC converters, η_{bo} & η_{bb} (-)	0.98

^aAdopted from [57] for renewable hydrogen.

Therefore, constraint (38h), in a relaxed form, can be rewritten as

$$\dot{\operatorname{sodx}}(t) \geqslant \frac{1}{\Delta \operatorname{sod}} \left(d_0 \frac{P_{\operatorname{fcs}}(t)^2}{x_{\operatorname{fc}}} + d_1 P_{\operatorname{fcs}}(t) + d_2 x_{\operatorname{fc}} \right), \quad (56)$$

which becomes a convex constraint [56].

To avoid the absolute value in constraint (38q), one more variable $P_{\rm sx}$ is introduced and (38q) can be relaxed as

$$\int_{0}^{t_{\rm f}} P_{\rm sx}(t) \mathrm{d}t \leqslant \frac{2N_{\rm cl}x_{\rm s}n_{s}E_{\rm cl}s_{\rm f}}{y_{\rm trk}L_{\rm a}},\tag{57a}$$

$$P_{\rm sx} \geqslant P_{\rm s},$$
 (57b)

$$P_{\rm sx} \geqslant -P_s$$
. (57c)

Since constraint (43) contains a min function, it can be reformulated as

$$P_{\rm st}(t)\eta_{\rm bb} + P_{\rm fcs}(t)\eta_{\rm bo} - P_{\rm loss,em}(t) - P_{\rm aux}(t) \geqslant P_{\rm wh,\gamma}(t),$$

$$\frac{P_{\rm st}(t)}{\eta_{\rm bb}} + P_{\rm fcs}(t)\eta_{\rm bo} - P_{\rm loss,em}(t) - P_{\rm aux}(t) \geqslant P_{\rm wh,\gamma}(t).$$
(58)

We can see that Sub-problem II is convex and can be effectively solved by convex programming.

V. CASE STUDY

All simulations are conducted with CVX toolbox using solver MOSEK in MATLAB R2020b on a PC with the configuration of Intel Core i7-7700K CPU 4.2 GHz and 64 GB RAM. The main parameters used for the case study are listed in Table IV.

A. Electric Machine Sizing and Modification of Velocity Trajectory

In this section, the electric machine sizing and the modification of the velocity trajectory for each driving cycle are analyzed and discussed.

- 1) Electric machine sizing: The maximum power of the electric machine is designed to satisfy a CDF of the upper bound of the wheel power demand. Fig. 7 shows that the upper bound of the wheel power demand monotonically decreases with the decrease of CDF. This means that a lower CDF value gives a lower upper bound of the wheel power demand, leading to a lower power rating of the electric machine and a lower cost accordingly. However, the power rating of the electric machine significantly influences the acceleration characteristic. The minimum upper bound of wheel power required for trucks specified in Table II with acceleration from 0 to 50 km/h within 25 s is computed to be 170 kW, 247 kW, 330 kW, and 360 kW for applications of urban delivery, regional delivery, construction, and long-haul, respectively. To satisfy this acceleration characteristic, the electric machine should have a corresponded rated power that covers 92.8 %, 94.3 %, 95.3%, and 96.5% of each driving cycle power demand. In the case study, we select electric machines to meet the above acceleration characteristics and also to be able to cover at least 94% of the wheel power demand in each driving cycle application. Therefore, the rated power of the electric machine is set as 218 kW, 247 kW, 330 kW, and 360 kW for applications of urban delivery, regional delivery, construction, and long-haul, respectively. The scaling factors are computed to be 1.09, 1.235, 1.65, and 1.8, respectfully.
- 2) Modification of Velocity Trajectory: With the maximum power of the electric machine determined, the velocity trajectory and the travel time for trucks in applications of urban delivery, regional delivery, construction, and long-haul can be obtained by solving problem (49). The problem is efficiently solved within 230 s for 6 iterations under the CVX environment. The optimal results at the selected γ for each driving cycle are compared with the original driving cycle for $\gamma = 1$ in Fig. 10-Fig. 13. In the application of urban delivery, the velocity trajectory at $\gamma = 94\%$ almost exactly follows the original velocity of the driving cycle, see Fig. 10(a). The same trends can also be found in applications of regional delivery, construction, and long-haul. From the enlarged view of the velocity trajectory as shown in sub-figure (b) in Fig. 10-Fig. 13, it can be seen that the velocity derivatives are reduced for the selected γ , due to the saturated delivered power, see sub-figures (c). We can also see that the velocity at some instances is higher than that at $\gamma = 100\%$. This is due to the time penalty in the objective function that ensures that the truck finishes the journey without much delay, even though the delivered peak wheel power is limited. Fig. 10-Fig. 13(d) show that travel times along each journey at the selected γ and $\gamma = 100\%$ have a good coherence. The trucks can finish all journeys at about the same time compared to cases when $\gamma = 100\%$.

B. Fuel Cell and Energy Buffer Sizing

In this section, we show the optimal sizing of FC and energy buffer for several trucking applications using the determined electric machine and the modified velocity trajectories from Sub-problem I. Three different energy buffer technologies are also compared for each driving cycle.

^bAdopted from world average price for household users in over 100 countries, which are calculated using the average annual household electricity consumption per year.

^cEstimated according to the data based on 100,000 systems/year presented at the Annual Merit Review and Peer Evaluation Meeting in 2019.

^dProvided by the vendors.

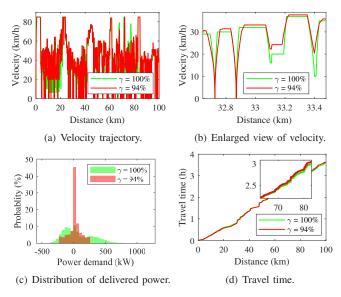


Fig. 10. Optimal results in the application of urban delivery.

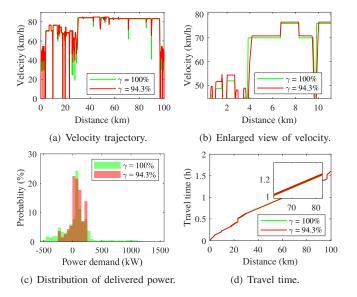


Fig. 11. Optimal results in the application of regional delivery.

The optimal sizing of power sources and their optimal power split are simultaneously obtained by solving Sub-problem II, which took in average $130\,\mathrm{s}$. The optimal values of the FC system and the energy buffer for the four driving cycles are shown in Table V. Since the total truck mass is assumed to be constant, the payload significantly differs with the change of the scaling parameters of FC and energy buffer. Therefore, a heavier FC and energy buffer will result in a less payload. This is reflected in the difference in m_0 , which is also listed in Table V for comparison.

The FC maximum power in the case with an SC is much higher than that with LiC and LiB in all driving cycles, whereas the power rating of the FC is similar for all energy buffers with LiC and LiB. This is because SC has the lowest energy density and it cannot provide high power for a long time duration. By contrast, the LiC and LiB have a certain amount of energy capacity and they can provide relatively

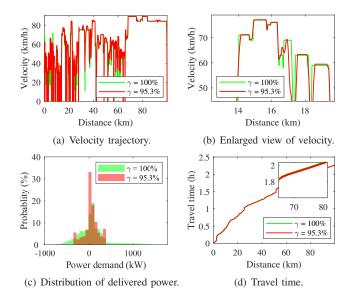


Fig. 12. Optimal results in the application of construction.

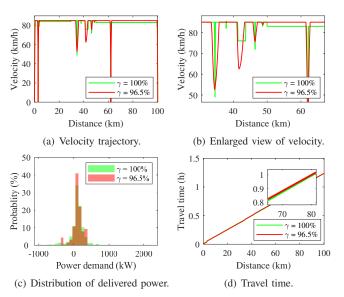


Fig. 13. Optimal results in the application of long-haul.

TABLE V
OPTIMAL PARAMETERS OF FUEL CELL, ENERGY BUFFERS, CHASSIS
MASS, AND TOTAL COST.

Driving cycles	Buffers	$P_{\mathrm{fcs,max}}$	$P_{s,\max}$	$E_{\rm s,max}$	m_0	$C_{\rm total}$
		kW	kW	kWh	kg	€/100km
Urban delivery	SC	111	652	3.43	16812	25.07
	LiC	76	223	9.93	17246	25.35
	LiB	73	478	59.51	16870	24.56
Regional delivery	SC	210	665	3.48	25375	29.30
	LiC	176	221	9.78	25822	29.37
	LiB	165	376	46.82	25642	27.52
Construction	SC	190	1496	7.82	30576	35.85
	LiC	158	336	14.92	31652	35.06
	LiB	147	512	64.71	31437	32.47
Long-haul	SC	340	791	4.14	37685	37.64
	LiC	266	226	10.15	38421	37.10
	LiB	248	517	64.98	38047	34.92

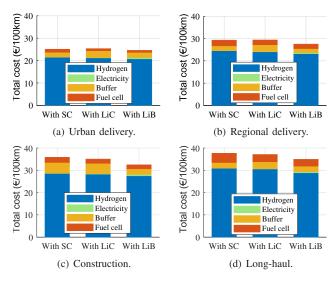


Fig. 14. Comparative total costs in the hybridization of different energy buffers among driving cycles.

higher power resulting in relatively lower power ratings of FC. However, the energy capacity of the LiB in all driving cycles is much higher than that of the other energy buffers. For instance, the energy capacity of the LiB in urban delivery application is almost 6 times and 17 times than that of the LiC and the SC, respectively. Among all driving cycle applications, the truck using LiB shows the cheapest cost, which is around 2%, 6%, 9%, and 7% lower than that with SC as the energy buffer in urban delivery, regional delivery, construction, and long-haul application, respectively. However, the cost in the case of SC and LiC as the energy buffer does not seem to have big difference. In the driving cycles of urban delivery and regional delivery, the cost of the truck with the SC is slightly lower than that with LiC, but the trend is opposite for the construction and long-haul driving cycles. It is of interest to see that trucks with the LiC can accommodate more payload than others even though they show higher cost than trucks with LiB. The major reason for the difference in payloads is due to the different energy density of the three energy buffer technologies. As can be seen from Table I, the energy density of the LiB is 13.3 times and 3.3 times than that of the SC and the LiC. The difference of energy capacity also contributes to the difference in payloads. Taking the long-haul driving cycle as an example, the truck with LiC can carry 374 kg and 736 kg more payload than that with LiB and SC. The optimal design parameters with LiB in long-haul application are comparable with the parameters chosen in the XCIENT Fuel Cell truck.

To further understand the difference in total cost, cost distribution is presented in Fig. 14. The hydrogen cost accounts for the highest percentage, while the electricity cost is the lowest in each hybridization among all driving cycles. Also, the hydrogen cost in the hybridization with LiB shows the lowest expense compared to the hybridization with the SC and LiC among all driving cycles, due to a cheaper electricity unit price and high energy capacity of LiB. The FC cost in the case of LiB is the lowest compared to other energy buffers among all driving cycles, owing to the smallest FC power rating. The

TABLE VI REGENERATIVE BRAKING ENERGY.

Buffers	Generated energy	Recaptured energy	Percentage
Duncis	kWh	kWh	%
SC		59.88	74.69
LiC	80.17	59.67	74.43
LiB		59.95	74.77
SC		21.95	73.36
LiC	29.92	22.35	74.72
LiB		23.36	78.11
SC		58.40	76.61
LiC	76.24	58.82	77.16
LiB		59.36	77.87
SC		11.41	44.76
LiC	25.50	14.12	55.38
LiB		20.65	80.97
	SC LiC LiB SC LiC LiB SC LiC LiB SC LiC LiC LiC LiC LiC LiC LiC LiC LiC	kWh SC LiC 80.17 LiB SC LiC 29.92 LiB SC LiC 76.24 LiB SC LiC 25.50	kWh kWh SC 59.88 LiC 80.17 59.67 LiB 59.95 SC 21.95 LiC 29.92 22.35 LiB 23.36 SC 58.40 LiC 76.24 58.82 LiB 59.36 SC 11.41 LiC 25.50 14.12

energy buffer cost differs for all driving cycles due to the big difference of the unit price and the energy capacity. For example, in the construction driving cycle, the energy capacity of the LiB and the LiC is around 8.27 times and twice that with the SC. However, the unit price of the SC is around 16 times and twice that of the LiB and the SC, respectively. For these reasons, the LiC cost is almost the same as the SC cost, whereas the LiB cost is around half of the SC cost. Due to the extremely cheap unit price of the LiB, its cost is still the lowest among all energy buffers for all driving cycles, despite its highest energy capacity.

C. Illustration of Power Allocation

Based on the optimal power rating of the FC and the energy capacity of the buffers, the optimal power allocations in longhaul driving cycle are illustrated as an example in Fig. 15. It is evident that the energy buffer mainly charges when the truck decelerates and discharges when the truck accelerates. Also, the power variation tendency of the energy buffer is severe and in general similar to the changes in demanded load power. By contrast, the FC power is relatively stable due to the FC power variation rate being limited within $\pm 10\%$ of the power rating per second. We can also see that in propulsion mode, the FC and energy buffer together provide the load demanded power. In the hybridization with the SC, the FC is forced to provide more power compared to that with the LiC and the LiB when the demanded power is continuously high. This is because the SC has limited energy capacity and cannot provide high power constantly, which can be seen in 25-28 min. Moreover, the FC power maintains a minimum output power, which is set as 10% of its power rating in the case study. This enforces the energy buffer to be also charged by the FC power when working in regenerative braking mode. Among the investigated energy buffers, the LiB attempts to recuperate as much power as possible since it has relatively big energy capacity. The SC can only receive very small part of the negative power as shown in 30-34 min.

The recuperated braking energy of the different trucking appellations are compared in Table VI. In applications of urban delivery, regional delivery, and construction, the recaptured

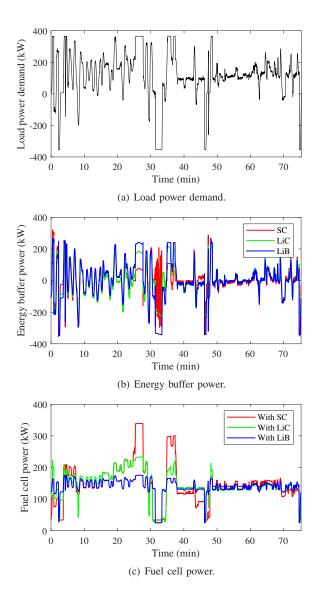


Fig. 15. Optimal power allocations in long-haul driving cycle.

energy of the three energy buffers is similar and its percentages vary from $73\,\%$ to $78\,\%$. However, in long-haul application, the recaptured energy shows very big difference for the three energy buffers. As LiC has moderate energy capacity, the recaptured energy is slightly higher that that of the SC. The LiB shows moderate power capability and big energy capacity, which allows LiB to recuperate as much energy as possible.

VI. CONCLUSIONS

To investigate the cost-benefit of designing and operating FCHETs, we formulate a chance-constrained program. The component cost including the FC, the energy buffer, and the electric machine as well as the operational costs including hydrogen and electricity are considered when delivered power is satisfied in a probabilistic sense. The introduced chance-constrained nonlinear program is decomposed into two subproblems and convex modeling steps are proposed to effectively solve them by sequential convex programming.

A case study is investigated showing that the maximum delivered power dramatically decreases as the satisfaction probability of the wheel power demand decreases. This allows downsizing the electric machine, FC, and energy buffer. Furthermore, it is shown that (1) the power rating of the electric machine is only around 18% of the wheel peak power demand when the delivered power satisfying a given probability; (2) with the reduced power rating of the electric machine, trucks can finish the journey with a similar speed and in about the same time with that from the original driving cycle but without delivering unnecessarily high power; (3) using LiB as the energy buffer shows lowest total expense among all investigated energy buffer technologies, whereas using LiC as the energy buffer allows trucks to carry more payload. For example, in long-haul application, the truck with LiC can carry 374 kg and 736 kg more payload than that with LiB and SC. (4) The proposed algorithm can be easily tailored to other types of hybrid EVs, including FC hybridized with SC and LiB simultaneously, and more details see [27].

A limitation of this study is that the proposed algorithm cannot be applied directly to general non-convex problems, which means that convex modeling steps are possibly required. Also, linear scaling is applied for the powertrain components, which may not be accurate when the optimal sizes are far from the baseline.

Future work related to this paper will be focused on several aspects. First, a more generic non-linear algorithm needs to be further developed for non-convex problems. Second, the selection of FC type for various vehicle applications can be conducted according to the specific requirement of each application. Third, the introduced method might be used to investigate a robust design optimization for FCHETs according to real-word truck operation. Forth, a moving horizon real-time energy management of FCHETs can be considered to improve the system efficiency and minimize the hydrogen consumption.

APPENDIX

A list of nomenclature is provided as a supplementary document.

ACKNOWLEDGMENT

The authors would like to thank the Chalmers Area of Advance (Transport) for financial support. The authors would also like to acknowledge Prof. Torbjörn Thiringer for the support and helpful discussions.

REFERENCES

- [1] Reducting CO₂ emissions from heavy-duty vehicles. [Online]. Available: https://ec.europa.eu/clima/policies/transport/vehicles/heavy_en.
- [2] L. Fan, Z. Tu, and S. H. Chan, "Recent development of hydrogen and fuel cell technologies: A review," *Energy Reports*, vol. 7, pp. 8421–8446, 2021
- [3] T. Rudolf, T. Schurmannü, S. Schwab, and S. Hohmann, "Toward holistic energy management strategies for fuel cell hybrid electric vehicles in heavy-duty applications," *Proceedings of the IEEE*, vol. 109, no. 6, pp. 1094–1114, 2021.
- [4] "Hyundai upgrades XCIENT Fuel Cell truck," Fuel Cells Bulletin, vol. 2021, no. 6, p. 4, 2021.
- [5] "Toyota unveils project portal 2.0 heavy truck," Fuel Cells Bulletin, vol. 2018, no. 7, p. 1, 2018.
- [6] "Hyundai delivers first XCIENT Fuel Cell trucks to Switzerland," Fuel Cells Bulletin, vol. 2020, no. 8, p. 3, 2020.

- [7] X. Wu, X. Hu, X. Yin, Y. Peng, and V. Pickert, "Convex programming improved online power management in a range extended fuel cell electric truck," *Journal of Power Sources*, vol. 476, p. 228642, 2020.
- [8] C. Geng, X. Jin, and X. Zhang, "Simulation research on a novel control strategy for fuel cell extended-range vehicles," *International Journal of Hydrogen Energy*, vol. 44, pp. 408–420, 2019.
- [9] B. Vural, A. R. Boynuegri, I. Nakir, O. Erdinc, A. BalikciM, m. Uzunoglu, and H. G. S. Dusmez, "Fuel cell and ultra-capacitor hybridization: a prototype test bench based analysis of different energy management strategies for vehicular applications," *International Journal* of Hydrogen Energy, vol. 35, pp. 11161–11171, 2010.
- [10] Y. Eren, O. Erdinc, H. Gorgun, M. Uzunoglu, and B. Vural, "A fuzzy logic based supervisory controller for an FC/UC hybrid vehicular power system," *International Journal of Hydrogen Energy*, vol. 34, pp. 8681– 8694, 2009.
- [11] M. Uzunoglu and M. S. Alam, "Modeling and analysis of an FC/UC hybrid vehicular power system using a novel-wavelet-based load sharing algorithm," *IEEE Transactions Energy Conversion*, vol. 23, no. 1, pp. 263–272, Mar. 2008.
- [12] M. G. Garignano, R. Costa-Castelló, V. Roda, N. M. Nigro, S. Junco, and D. Feroldi, "Energy management strategy for fuel cell-supercapacitor hybrid vehicles based on prediction of energy demand," *Journal of Power Sources*, vol. 360, pp. 419–433, 2017.
- [13] Y. Y. Q. Li, B. Su, J. Liu, and L. Ma, "Optimal energy management and control in multimode equivalent energy consumption of fuel cell/supercapacitor of hybrid electric tram," *IEEE Transactions Industrial Electronics*, vol. 66, no. 8, pp. 263–272, Aug. 2019.
- [14] A. Ferrara, S. Jakubek, and C. Hametner, "Energy management of heavy-duty fuel cell vehicles in real-world driving scenarios: robust design of strategies to maximize the hydrogen econoy and system lifetime," *Energy Conversion and Management*, vol. 232, p. 113795, 2021.
- [15] B. Bendjedia, N. Rizoug, M. Boukhnifer, F. Bouchafaa, and M. Benbouzid, "Influence of secondary source technologies and energy management strategies on energy storage system sizing for fuel cell electric vehicles," *International Journal of Hydrogen Energy*, vol. 43, pp. 11614–11628, 2018.
- [16] L. Xu, M. Ouyang, J. Li, F. Yang, L. Lu, and J. Hua, "Optimal sizing of plug-in fuel cell electric vehicles using models of vehicle performance and system cost," *Applied Energy*, vol. 103, pp. 477–478, 2013.
- [17] J. Marcinkoski, R. Vijayagoopal, J. Kast, and A. Duran, "Driving an industry: medium and heavy duty fuel cell electric truck component sizing," World Electric Vehicle Journal, vol. 8, pp. 78–89, 2016.
- [18] K. Sim, R. Vijayagopal, N. Kim, and A. Rousseau, "Optimization of component sizing for a fuel cell-powered truck to minimize ownership cost," *Energies*, vol. 12, pp. 1124–1136, 2019.
- [19] A. Ravey, N. Watrin, B. Blunier, D. Bouquain, and A. Miraoui, "Energy-source-sizing methodology for hybrid fuel cell vehicles based on statistical description of driving cycles," *IEEE Transactions on Vehicular Technology*, vol. 60, no. 9, pp. 4164–4174, Nov. 2011.
- [20] M. Lu, G. Domingues-Olavarría, F. J. Márquez-Fernández, P. Fyhr, and M. Alaküla, "Electric drivetrain optimization for a commercial fleet with different degrees of electrical machine commonality," *Energies*, vol. 14, p. 2989, 2021.
- [21] Z. Song, H. Hofmann, J. Li, X. Han, X. Zhang, and M. Ouyang, "A comparison study of different semi-active hybrid energy storagesystem topologies for electric vehicles," *Journal of Power Sources*, vol. 274, pp. 400–411, 2015.
- [22] Z. Hu, J. Li, L. Xu, Z. Song, C. Fang, M. Ouyang, G. Dou, and G. Kou, "Multi-objective energy management optimization and parameter sizing for proton exchange membrane hybrid fuel cell vehicles," *Energy Conversion and Management*, vol. 129, pp. 108–121, 2016.
- [23] H. Jiang, L. Xu, J. Li, Z. Hu, and M. Ouyang, "Energy management and component sizing for a fuel cell/battery/supercapacitor hybrid powertrain based on two-dimensional optimization algorithms," *Energy*, vol. 177, pp. 386–396, 2019.
- [24] L. Xu, C. D. Mueller, J. Li, M. Ouyang, and Z. Hu, "Multi-objective component sizing based on optimal energy management strategy of fuel cell electric vehicles," *Applied Energy*, vol. 157, pp. 664–674, 2015.
- [25] N. Murgovski, X. Hu, L. Johannesson, and B. Egardt, Combined design and control optimization of hybrid vehicles. John Wiley & Sons, Ltd, 2015.
- [26] X. Hu, N. Murgovski, L. M. Johannesson, and B. Egardt, "Optimal dimensioning and power management of a fuel cell/battery hybrid bus via convex programming," *IEEE/ASME Transactions on Mechatronics*, vol. 20, no. 1, pp. 457–468, Feb. 2015.

- [27] X. Hu, L. Johannesson, N. Murgovski, and B. Egardt, "Longevity-conscious dimensioning and power management of the hybrid energy storage system in a fuel cell hybrid electric bus," *Applied Energy*, vol. 137, pp. 913–924, 2015.
- [28] X. Wu, X. Hu, X. Yin, L. Li, Z. Zeng, and V. Pickert, "Convex programming energy management and components sizing of a plugin fuel cell urban logistics vehicle," *Journal of Power Sources*, vol. 423, pp. 358–366, 2019.
- [29] Y. Feng and Z. Dong, "Integrated design and control optimization of fuel cell hybrid mining truck with minimized lifecycle cost," *Applied Energy*, vol. 270, p. 115164, 2020.
- [30] Q. Xun, Y. Liu, and E. Holmberg, "A comparative study of fuel cell electric vehicle hybridization with battery or supercapacitor," in *Interna*tional Symposium on Power Electronics, Electrical Drives, Automation and Emotion, June 2018, pp. 390–395.
- [31] H. S. Das, C. W. Tan, and A. Yatim, "Fuel cell hybrid electric vehicles: a review on power conditioning units and topologies," *Renewable and Sustainable Energy Reviews*, vol. 76, pp. 268–291, 2017.
- [32] Q. Xun, S. Lundberg, and Y. Liu, "Design and experimental verification of a fuel cell/supercapacitor passive configuration for a light vehicle," *Journal of Energy Storage*, vol. 33, p. 102110, 2021.
- [33] X. Hu, N. Murgovski, L. Johannesson, and B. Egardt, "Energy efficiency analysis of a series plug-in hybrid electric bus with different energy management strategies and battery sizes," *Applied Energy*, vol. 111, pp. 1001–1009, 2013.
- [34] B. Egardt, N. Murgovski, M. Pourabdollah, and L. J. Mårdh, "Electromobility studies based on convex optimization: design and control issues regarding vehicle electrification," *IEEE Control System Magazine*, vol. 34, pp. 32–39, 2014.
- [35] X. Hu, N. Murgovski, L. M. johannesson, and B. Egardt, "Comparison of three electrochemical energy buffers applied to a hybrid bus powertrain with simultaneous optimal sizing and energy management," *IEEE Transactions on Intelligent Transportation Systems*, vol. 15, no. 3, pp. 1193–1205, 2014.
- [36] P. Schneider, C. Sadeler, A.-C. Scherzer, N. Zamel, and D. Gerteisen, "Fast and reliable state-of-health model of a PEM cathode catalyst layer," *Journal of the Electrochemical Society*, vol. 166, no. 4, pp. F322–F333, 2019
- [37] P. Ren, P. Pei, Y. Li, Z. Wu, D. Chen, and S. Huang, "Degradation mechanisms of proton exchange membrane fuel cell under typical automotive operating conditions," *Progress in Energy and Combustion Science*, vol. 80, p. 100859, 2020.
- [38] Y. Yang, X. zhou, B. Li, and C. Zhang, "Recent progress of the gas diffusion layer in proton exchange membrane fuel cells: material and structure designs of microporous layer," *International Journal of Hydrogen Energy*, vol. 46, no. 5, pp. 4259–4282, 2021.
- [39] Y. Wang, S. J. Moura, S. G. Advani, and A. K. Prasad, "Power management system for a fuel cell/battery hybrid vehicle incorporating fuel cell and battery degradation," *International Journal of Hydrogen Energy*, vol. 44, pp. 8479–8492, 2019.
- [40] X. Hu, C. Zou, X. Tang, T. Liu, and L. Hu, "Cost-optimal energy management of hybrid electric vehicles using fuel cell/battery healthaware predictive control," *IEEE Transactions on Power Electronics*, vol. 35, no. 1, pp. 382–392, 2019.
- [41] T. Flecher, R. Thring, and M. Watkinson, "An energy management strategy to concurrently optimise fuel consumption & PEM fuel cell lifetime in a hybrid vehicle," *International Journal of Hydrogen Energy*, vol. 41, no. 46, pp. 21503–21515, 2016.
- [42] X. Zhang, Y. Rui, Z. Tong, X. Sichuan, S. Yong, and N. Huaisheng, "The characteristics of voltage degradation of a proton exchange membrane fuel cell under a road operating environment," *International Journal of Hydrogen Energy*, vol. 39, no. 17, pp. 9420–9429, 2014.
- [43] H. Chen, P. Pei, and M. Song, "Lifetime prediction and the economic lifetime of proton exchagne membrane fuel cells," *Applied Energy*, vol. 142, pp. 154–163, 2015.
- [44] M. G. Carignano, R. Costa-Castelló, V. Roda, N. M. Nigro, S. Junco, and D. Feroldi, "Energy management strategy for fuel cell-supercapacitor hybrid vehicles based on prediction of energy demand," *Journal of Power Sources*, vol. 360, pp. 419–433, 2017.
- [45] C. Dépature, S. Jemeï, L. Boulon, A. Bouscayrol, N. Marx, S. Morando, and A. Castaings, "IEEE VTS motor vehicles challenge 2017 energy management of a fuel cell/battery vehicle," in 2016 IEEE Vehicle Power and Propulsion Conference (VPPC), 2016, pp. 4635–4640.
- [46] K. Davis and J. G. Hayes, "Fuel cell vehicle energy management strategy based on the cost of ownership," *IET Electrical Systems in Transportation*, vol. 9, no. 4, pp. 226–236, 2019.

- [47] S. Wei, J. Jiang, N. Murgovski, J. Sjöberg, W. Zhang, C. Zhang, and X. Hu, "Optimisation of a catenary-free tramline equipped with stationary energy storage systems," *IEEE Transactions on Vehicular Technology*, vol. 69, no. 3, pp. 2449–2462, 2020.
- [48] N. Takami, H. Inagaki, Y. Tatebayashi, H. Saruwatari, K. Honda, and S. Egusa, "High-power and long-life lithium-ion batteries using lithium titanium oxide anode for automotive and stationary power applications," *Journal of Power Sources*, vol. 244, pp. 469–475, 2013.
- [49] N. Murgovski, L. J. Mårdh, A. Grauers, and J. Sjöberg, "Dimensioning and control of a thermally constrained double buffer plug-in hev powertrain," 2012 IEEE 51st IEEE Conference on Decision and Control (CDC), pp. 6346–6351, 2012.
- [50] N. Murgovski, L. M. Johannesson, and B. Egardt, "Optimal battery dimensioning and control of a CVT PHEV powertrain," *IEEE Transactions* on Vehicular Technology, vol. 63, no. 5, pp. 2151–2161, 2014.
- [51] H. Liimatainen, M. Pöllänen, and L. Nykänen, "Impacts of increasing maximum truck weight - case Finland," European Transport Research Reviews, vol. 12, no. 4, 2020.
- [52] N. Murgovski, L. Johannessona, J. Sjöberg, and B. Egardta, "Component sizing of a plug-in hybrid electric powertrain via convex optimization," *Mechatronics*, vol. 12, no. 1, pp. 106–120, 2017.
- [53] L. Johannesson, N. Murgovski, S. Ebbesen, B. Egardt, E. Gelso, and J. Hellgren, "Including a battery state of health model in the HEV component sizing and optimal control problem," *IFAC Proceedings Volumes*, vol. 46, no. 21, pp. 398–403, 2013.
- [54] N. Murgovski, X. Hu, L. Johannesson, and B. Egardt, "Filtering driving cycles for assessment of electrified vehicles," in Workshop for New Energy Vehicle Dynamic System and Control Technology, 2013.
- [55] N. Murgovski, L. Johannesson, J. Hellgren, B. Egardt, and J. Sjöberg, "Convex optimization of charging infrastructure design and component sizing of a plug-in series HEV powertrain," *IFAC Proceedings Volumes*, vol. 44, no. 1, pp. 13052–13057, 2011.
- [56] S. Boyd and L. Vandenberghe, Convex Optimization. UK: Cambridge University Press, 2004.
- [57] G. Glenk and S. Reichelstein, "Economics of converting renewable power to hydrogen," *Nature Energy*, vol. 4, pp. 212–216, 2019.



Qian Xun received B. Eng. and M.Sc. from Hohai University and Nanjing University of Aeronautics and Astronautics in China, in 2012 and 2015, respectively. After that, she worked as a lecturer at Huzhou University, China for 2 years. At present, she is pursuing a Ph.D. degree at Chalmers University of Technology in Sweden. Her research interests include modelling, control, and optimization of fuel cell hybrid electric vehicles.



Nikolce Murgovski Nikolce Murgovski received the M.S. degree in software engineering from University West, Trollhattan, Sweden, in 2007, and the M.S. degree in applied physics and the Ph.D. degree in systems and control from the Chalmers University of Technology, Gothenburg, Sweden, in 2007 and 2012, respectively. He is currently an Associate Professor with the Department of Electrical Engineering, Chalmers University of Technology. His research interest includes optimization and optimal control in the automotive area.



Yujing Liu received the B.Sc., M.Sc., and Ph.D. degrees in electrical engineering from Harbin Institute of Technology, Harbin, China, in 1982, 1985, and 1988, respectively. From 1996 to 2013, he worked in ABB Corporate Research, Västerås, Sweden. Since 2013, he has been a Professor of Electric Power Engineering with the Chalmers University of Technology, Gothenburg, Sweden. He is interested in research on motors, converters, wireless charging for electric vehicles, generators, and power electronics for tidal power conversion and high-efficiency ma-

chines for energy saving in industrial applications. Dr. Liu is a member of the Swedish Standard Committee on Electrical Machines.