

# Bursty Bulk Flow Turbulence as a Source of Energetic Particles to the Outer Radiation Belt

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## Key Points:

A bursty bulk flow near the outer radiation belt displays turbulent electric fields and enhanced  
fluxes of energetic ions and electrons.

Electrons appear to be locally accelerated by turbulent electric fields forming an energetic  
shoulder in the distribution.

Turbulent electric fields in the BBF braking region favors energization of the highest energy  
electrons.

23 **Abstract**

24 We report observations of a Bursty Bulk Flow (BBF) penetrating close to the outer edge of  
25 the radiation belt. The turbulent BBF braking region is characterized by ion velocity fluctuations,  
26 magnetic field ( $\mathbf{B}$ ) variations, and intense electric fields ( $\mathbf{E}$ ). In this event, energetic ( $>100$  keV)  
27 electron and ion fluxes are appreciably enhanced. Importantly, fluctuations in energetic electrons  
28 and ions suggest local energization. Using correlation distances and other observed  
29 characteristics of turbulent  $\mathbf{E}$ , test-particle simulations support local energization by  $\mathbf{E}$  that favors  
30 higher-energy electrons and leads to an enhanced energetic shoulder and tail in the electron  
31 distributions. The energetic shoulder and tail could be amplified to MeV energies by adiabatic  
32 transport into the radiation belt where  $|\mathbf{B}|$  is higher. This analysis suggests that turbulence  
33 generated by BBFs can, in part, supply energetic particles to the outer radiation belt and that  
34 turbulence can be a significant contributor to particle acceleration.

35

## 36 **1. Introduction**

37 Turbulence, by its very nature, cascades energy in driven systems to smaller scales at which  
38 dissipation takes place. In Earth's magnetotail, the energy source is often magnetic field ( $\mathbf{B}$ )  
39 annihilation enabled by magnetic reconnection, the associated ion jet ( $V_{Ion}$ ), or Poynting flux. As  
40  $\mathbf{B}$  and  $V_{Ion}$  energy cascades to smaller scales, the electric field ( $\mathbf{E}$ ) follows suit to carry out the  
41 transfer of  $\mathbf{B}$  and  $V_{Ion}$  energy into thermal energy. We hypothesize that, for electrons in a  
42 magnetized plasma, those with the highest energies have the largest gyroradii and largest parallel  
43 velocities, so they receive energy from both large- and small-scale  $\mathbf{E}$  fluctuations. Particles with  
44 the lowest energies are last in line as they receive energy only from the smallest scales of  $\mathbf{E}$ . As a  
45 result, turbulent energization favors energetic particles, which results in acceleration.

46 In this letter, we concentrate on electron energization on closed field lines in the turbulent  
47 environment created by Bursty Bulk Flows (BBFs, Baumjohann et al., 1989; Angelopoulos et al.,  
48 1992; 1994). BBFs account for a significant fraction of energy transport from the Earth's  
49 magnetotail to the outer radiation belt and can lead to aurora (e.g., Sergeev et al., 1999; 2000;  
50 Nakamura et al., 2001; Sergeev et al., 2014; Ergun et al., 2015; Stawarz et al., 2015; Turner et  
51 al., 2015; 2016; 2021). They usually originate in the magnetotail beyond  $\sim 15 R_E$  (Earth radius)  
52 by magnetic reconnection events that are localized in the GSM  $Y$  (Geocentric Solar  
53 Magnetospheric) direction (Ohtani, Singer, and Mukai, 2006; Runov et al., 2009; 2011; Sitnov,  
54 Swisdak, and Divin, 2009). BBFs often are accompanied by "dipolarization" in which stretched  
55  $\mathbf{B}$  in the magnetotail, dominated by its GSM  $X$  component, relaxes to a more dipole-like  
56 configuration. Dipolarization supports the hypothesis that BBFs are earthward-flowing magnetic  
57 reconnection exhaust (e.g., Sitnov, Swisdak, and Divin, 2009; Nakamura, et al. 2009).

58 The characteristics of BBFs at distances greater than  $\sim 8 R_E$  from Earth are fairly well  
59 described (e. g. Zhang et al., 2016). At  $>12 R_E$ , earthward flow velocities can reach up to 1000  
60  $\text{km s}^{-1}$  (Angelopoulos et al., 1992; 1994). Flow velocities slow to the order of  $100 \text{ km s}^{-1}$  as  
61 BBFs travel from  $\sim 12 R_E$  to  $\sim 8 R_E$  due to stronger  $\mathbf{B}$  and higher densities. This region, called the  
62 BBF braking region, frequently displays strong turbulence along with energized ions and  
63 electrons (Stawarz et al, 2015; Ergun et al., 2015).

64 Properties of BBFs are less well understood inside of  $\sim 8 R_E$ . One of the key unknowns is how  
65 BBFs are related to enhancements of energetic particles in the outer radiation belts known as  
66 flow injections. Inside of  $\sim 8 R_E$ , the flow speeds of the progenitor BBFs are dramatically reduced  
67 and dipolarization is difficult to identify in the strong  $\mathbf{B}$  environment, so correlation between  
68 BBFs and flow injections is challenging (Takada et al, 2006; Ohtani, Singer, and Mukai, 2006;  
69 Dubyagin et al, 2011, Sergeev et al., 2012; Liu et al., 2016).

70 Observations show that a subset of particularly strong BBFs generate turbulence in the  
71 braking region with intense  $\mathbf{E}$  (Ergun et al., 2015; Stawarz et al, 2015). Fluctuations in electron  
72 temperature ( $T_e$ ), ion temperature ( $T_i$ ), and in energetic fluxes indicate possible local energization  
73 (Usanova and Ergun, 2022). Here, we investigate processes by which electrons are energized in  
74 the turbulent BBF braking region. The Magnetospheric Multiscale (MMS) mission (Burch et al.,  
75 2016) has four satellites that, at the time, are separated by distances ranging from  $\sim 39$  to  $\sim 123$   
76 km, which allows us to determine properties of the turbulent  $\mathbf{E}$  including a constraint on the  
77 correlation distances.

78 In this letter, the term “energization” implies generic energy input to a species, “heating” is a  
79 thermal process in the core of a distribution, and “acceleration” is the development of a non-  
80 thermal tail. Particle energization is expected in the turbulent BBF braking region. However, a

81 critical aspect is how the energy is distributed within the electron and ion distributions. Core  
82 heating results in an increase in temperature. If energization favors energetic particles, non-  
83 thermal distributions develop. Here, we show that the observed properties of  $E$  could result in  
84 non-thermal electron distributions that may seed the outer radiation belt.

## 85 **2. Observations**

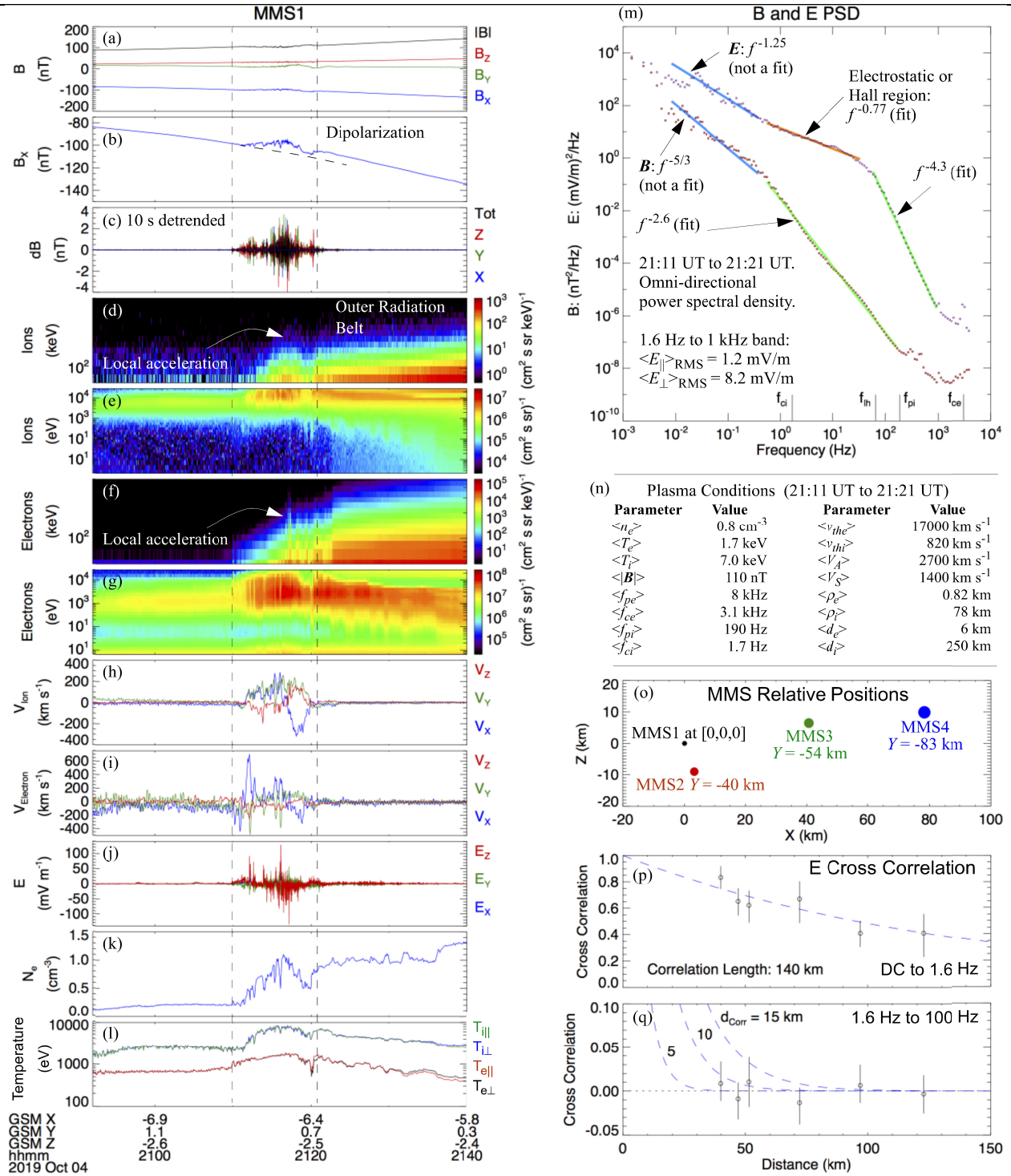
86 Figure 1 displays a BBF with turbulent  $E$ . The data are from the MMS satellites, which are, in  
87 this event, located in the southern magnetosphere. Figure 1a displays  $B$  in GSM coordinates over  
88 a 50-minute period. Colors represent direction and the black trace is  $|B|$ . A magnified view of  $B_x$   
89 is in panel b with a dashed line to highlight dipolarization.  $B_z$  shows little net change, likely due  
90 to the off-equatorial position of MMS. Immediately below, panel c plots  $B$  10-s detrended,  $dB =$   
91  $B - \langle B \rangle_{10s}$ , which accentuates fluctuations in  $B$ . Panels d, e, f, and g plot, respectively, ion flux  
92 as a function of energy from 70 to 600 keV, differential ion energy flux from 3 eV to 25 keV,  
93 electron flux from 60 to 500 keV, and differential electron energy flux from 6 eV to 25 keV. The  
94 MMS instruments are described in a series of articles (Torbert et al., 2016, Russell et al., 2016;  
95 Le Contel et al., 2016; Lindqvist et al., 2016, Ergun et al., 2016; Mauk et al., 2016; Pollock et al.,  
96 2016).

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**Figure 1.** MMS1 observations of a BBF penetrating close to the outer radiation belt. The horizontal axis on the left column is 50 minutes in time. Vectors are in GSM coordinates; colors represent components as marked on the right of a panel. (a)  $B$  at 62.5 ms resolution. The black

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trace is  $|\mathbf{B}|$ . (b) A magnified view of  $B_x$ . (c)  $\mathbf{B}$  detrended by 10 s. (d) Ion flux as a function of energy (vertical axis) from 70 to 600 keV. These data are from all four MMS spacecraft. (e) Differential ion energy flux as a function of energy from 3 eV to 25 keV. (f) Electron flux from 60 to 500 keV. (g) Differential electron energy flux 6 eV to 25 keV. (h)  $V_{Ion}$  at 4.5 s resolution. (i)  $V_{Elc}$  at 4.5 s resolution smoothed over 13.5 s. (j)  $\mathbf{E}$  at 31.25 ms resolution. (k) Electron density at 4.5 s resolution. (l)  $T_i$  and  $T_e$  at 4.5 s resolution. (m) The PSD of  $\mathbf{B}$  and  $\mathbf{E}$  versus frequency. (n) Average plasma conditions. (o) The relative positions of the MMS spacecraft. (p) The cross-correlation of  $\mathbf{E}$  between the MMS spacecraft plotted as a function of separation.  $\mathbf{E}$  is filtered from DC to 1.6 Hz. (q) The cross-correlation of  $\mathbf{E}$  filtered from 1.6 Hz to 100 Hz.

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102 At the beginning of Figure 1, ~20:50 UT, the MMS satellites are in a relatively quiet region of  
103 the magnetotail (auroral electrojet index ~100 nT). A noticeable event begins at ~21:10 UT and  
104 endures until ~21:21 UT. During this period,  $\mathbf{B}$  dipolarizes (Figure 1b) and has visible  
105 fluctuations (Figure 1c). There is an enhancement of energetic (>100 keV) ion and electron  
106 fluxes (panels d-g). Importantly, the energetic fluxes are varying, implying possible local  
107 acceleration. At the same time,  $V_{Ion}$  (Figure 1h) indicates disturbed flow over 200 km/s including  
108 a flow vortex (Birn et al., 1997; Gabrielse et al., 2012; Sergeev et al., 2014). The electron  
109 velocity fluctuations ( $V_{Elc}$ , Figure 1i) differ from  $V_{Ion}$  indicating Hall  $\mathbf{E}$  and Hall currents may be  
110 deflecting the ion flow.  $\mathbf{E}$  fluctuations (Figure 1j) are particularly intense. The plasma density  
111 ( $N_e$ , Figure 1k) changes in consort with the flow vortex in  $V_{Ion}$  (Figure 1h).  $T_i$  and  $T_e$  increase  
112 (Figure 1l). These features are characteristic of a turbulent BBF braking region (Ergun et al.,  
113 2015).

114 Shortly after the fluctuations in  $\mathbf{B}$ ,  $V_{Ion}$ ,  $V_{Elec}$ , and  $\mathbf{E}$  subside ( $\sim 21:21$  UT), the MMS satellites  
 115 enter the outer radiation belt. Starting at  $\sim 21:22$  UT, the intensity of energetic ion and electron  
 116 fluxes gradually increases whereas the fluctuations decrease.  $T_i$  and  $T_e$  also decrease. These  
 117 observations insinuate that the BBF penetrated to near the outer edge of the radiation belt.

118 One of the most important questions about this event is if and how the intense, turbulent  $\mathbf{E}$   
 119 locally energizes electrons and ions. As such, the nature of the turbulence and the properties of  $\mathbf{E}$   
 120 deserve further investigation. Figure 1m displays the frequency-domain power spectral density  
 121 (PSD) of  $\mathbf{B}$  and  $\mathbf{E}$  during the event. The circles represent the measured PSDs. The light blue lines  
 122 refer to the inertial region ( $f < \sim 0.4$  Hz) with previously measured spectral indices ( $\alpha$ ) of  
 123 turbulent BBFs. The red and green lines are fits. These  $\mathbf{B}$  and  $\mathbf{E}$  PSDs are remarkably similar to  
 124 others in identified turbulent events in the Earth's magnetotail (Ergun et al., 2015; 2018;  
 125 2020a,b). The spectral index of  $\mathbf{B}$  in the inertial region ( $f < \sim 0.4$  Hz) is consistent with  $-5/3$ ; the  
 126 short period makes a fit uncertain. The ion skin depth ( $d_i$ ) is greater than the ion gyroradius ( $\rho_i$ )  
 127 due to  $\sim 110$  nT background  $\mathbf{B}$  (mean plasma parameters are in Figure 1n). We presume that the  
 128 spectral break ( $\sim 0.4$  Hz) is near a region where the wavevector ( $\mathbf{k}$ ) is such that  $|\mathbf{k}|d_i \sim 1$ . The  $\mathbf{E}$   
 129 PSD  $< \sim 0.4$  Hz is consistent with a shallow index previously observed ( $\alpha = -1.25$ ). The  
 130 electrostatic or Hall region (Franci et al., 2015) of the  $\mathbf{E}$  PSD is between  $\sim 0.4$  Hz and  $\sim 40$  Hz  
 131 with  $\alpha \sim -0.77$  (red line in Figure 1m). At higher frequencies, the  $\mathbf{E}$  PSD steeply declines.

132 From the measured PSD ( $P_E$ ), one can estimate the ion heating rate to be (Chang et al., 1986):

$$\dot{W}_i = \frac{e^2}{2m_i} \eta_L P_E(f_{ci}) \#1$$

133 Here,  $e$  is the fundamental charge,  $m_i$  is the ion mass, and  $\eta_L$  ( $\sim 1/2$ ) is the fraction of  $P_E$  that is  
 134 left-hand polarized. Since  $P_E(f_{ci}) \sim 10 \text{ mV}^2 \text{ m}^{-2} \text{ Hz}^{-1}$  (Figure 1m),  $\dot{W}_i$  is estimated to be  $250 \text{ eV s}^{-1}$ ,



135 which is sufficient to explain the observed values of  $T_i$ . Investigation of energetic ions requires a  
136 much more involved analysis and is reserved for a later study.

137 To the contrary, there is little power at  $f \geq f_{ce}$  (Figure 1m) and  $E_{\parallel}$  is small (written on plot)  
138 which, at first glance, suggests that electron energization should be negligible. Perpendicular  
139 energization requires circumvention of the first adiabatic invariant ( $\mu = p_{\perp}^2/2\gamma m_o B$ ). However,  
140 energization can occur if the correlation length scale ( $d_{corr}$ ) in the  $\mathbf{E}$  turbulence is sufficiently  
141 small. If an electron's parallel velocity is such that  $d_{corr\parallel}/v_{\parallel} < 1/f_{ce}$ , it experiences changes in  
142  $\mathbf{E}$  in less than  $1/f_{ce}$  in its frame and therefore can be energized perpendicular to  $\mathbf{B}$  (Ergun et al.,  
143 2020a,b). Furthermore, if an electron's gyroradius is such that  $\rho_e \geq d_{corr\perp}$ , it can experience  
144 enhanced parallel energization, perpendicular energization, and pitch-angle scattering.

145 Figures 1o, 1p, and 1q investigate the correlation length of  $\mathbf{E}$  beginning with the frequency  
146 range below  $f_{ci}$ , which is of interest for studying ion energization. The MMS spacecraft are  
147 separated from  $\sim 39$  to  $\sim 123$  km (Figure 1o). Figure 1p displays the correlation of  $\mathbf{E}$  filtered to  
148 DC to  $\sim 1.6$  Hz between each spacecraft pair. Each of the  $\mathbf{E}$  components is separately correlated  
149 then averaged. The measured correlations support an exponential with a correlation distance of  
150  $\sim 140 \pm 50$  km, which lies between  $\rho_i$  (thermal average) and  $d_i$ , as expected in a turbulent plasma.

151 The correlation is repeated for the frequency range of  $\sim 1.6$  to  $\sim 100$  Hz (Figure 1q) where  
152 energization of electrons is expected to be governed. These correlations are performed over ten,  
153 one-minute intervals for each component of  $\mathbf{E}$  resulting in 30 individual correlations then  
154 averaged. Correlations using time lags, different periods, and/or separation of  $\mathbf{E}_{\perp}$  and  $E_{\parallel}$   
155 unanimously indicate that  $\mathbf{E}$  is uncorrelated ( $< 0.05$ ) at the minimum separation of 39 km, which  
156 is primarily perpendicular to  $\mathbf{B}$ . This result implies that  $d_{corr} \leq 10$  km (Figure 1q), which is  
157 consistent with  $d_e \sim 6$  km and thermal  $\rho_e \sim 820$  m. Since  $\langle E_{\perp} \rangle_{RMS} \cong 7 \langle E_{\parallel} \rangle_{RMS}$ , the constraint on

158  $d_{corr}$  is likely that of  $d_{corr\perp}$ . Furthermore, even though  $\partial\mathbf{B}/\partial t$  is visible (Figure 1c),  $|\nabla \times \mathbf{E}| \ll$   
 159  $\langle \mathbf{E} \rangle_{RMS}/d_{corr}$ , so  $\mathbf{E}$  is primarily electrostatic in this higher-frequency range (Figure 1m). Using  
 160  $\nabla \times \mathbf{E} \approx 0$ ,  $\langle E_{\parallel} \rangle_{RMS}/d_{corr\perp} \approx \langle E_{\perp} \rangle_{RMS}/d_{corr\parallel}$ , which implies  $d_{corr\parallel}$  is  $\sim 7 d_{corr\perp}$ .

### 161 3. Electron Energization and Test-Particle Simulations

162 In a magnetized plasma, parallel and perpendicular energization are distinct and quite  
 163 complex. Energizing by  $E_{\parallel}$  can be amplified if  $\rho_e \geq d_{corr\perp}$ , which causes an electron's orbit to  
 164 transit regions of uncorrelated  $E_{\parallel}$ . Perpendicular energization is often hindered since  $\mu$  is  
 165 conserved. However, as discussed above, if  $\rho_e \geq d_{corr\perp}$  or  $d_{corr\parallel}/v_{\parallel} < 1/f_{ce}$ , an electron can  
 166 experience impulses on time scales less than  $1/f_{ce}$ . Since  $\rho_e = v_{\perp}/\omega_{ce}$ , these conditions are:

$$167 \quad v_{\parallel} \geq d_{corr\parallel} f_{ce} \text{ or } v_{\perp} \geq d_{corr\perp} \omega_{ce} \#2$$

168  
 169 In a turbulent environment, it is not unusual that  $d_{corr\perp} \approx d_e = c/\omega_{pe}$  ( $\omega_{pe}$  is the electron  
 170 plasma frequency) so the condition for “full energization” (breaking of  $\mu$ ) can be estimated as:

$$171 \quad \frac{p_{\perp}}{m_0 c} \geq \frac{\omega_{ce0}}{\omega_{pe}} \text{ or } \frac{p_{\parallel}}{m_0 c} \geq \frac{\omega_{ce0}}{\omega_{pe}} R_{corr} \text{ where } R_{corr} = \left( \frac{d_{corr\parallel}}{2\pi d_{corr\perp}} \right) \#3$$

172  
 173 Here,  $m_0$  is the electron rest mass and  $\omega_{ce0}$  represents the rest-mass electron cyclotron frequency.  
 174  $R_{corr}$ , a weighted parallel to perpendicular correlation ratio, is approximately unity in the  
 175 observed event. Importantly, the conditions in Equation (3) favor higher-energy particles and  
 176 therefore support acceleration. At the location of the MMS satellites,  $\omega_{ce0}/\omega_{pe} \sim 0.38$ , so only  
 177 electrons with energies  $>40$  keV are expected to experience full energization.

178 In a global-scale picture, electrons are free to travel along Earth's magnetic field lines and  
179 visit a range of values of  $|\mathbf{B}|$ , so  $\omega_{ce0}/\omega_{pe}$  also has an appreciable range since  $N_e$  remains relatively  
180 constant far from Earth. MMS's location (Figures 2a) is off the equatorial plane, so mapping is  
181 required to determine the magnetic field line geometry. Unfortunately, the BBF presents a large  
182 disturbance making accurate mapping difficult. The measured  $\mathbf{B}$  direction and a model are  
183 combined for a rough mapping (see supplemental material) to estimate a L-shell of  $\sim 10 \pm 1 R_E$ ,  
184 which, at  $L = 10 R_E$ , implies that lowest  $|\mathbf{B}|$  is  $\sim 31$  nT near the equator with  $\omega_{ce0}/\omega_{pe} \sim 0.11$ .  
185 There, only electrons with energies  $> \sim 5$  keV (if isotropic) meet the conditions for full  
186 energization (Equation 3). As a result, nowhere along the field line do core electrons ( $< 2.5$  keV)  
187 experience full energization.

188 To investigate electron energization by  $\mathbf{E}$  further, we perform a quasi-1D test-particle  
189 simulation of electrons along a  $L = 10 R_E$  stretched field line (Figures 2a and 2b). The simulation  
190 code is modified from a previously-described version (Ergun et al., 2020b). The simulation  
191 domain ( $Z$ ) is 3D ( $25 R_E \times 36 d_e \times 36 d_e$ ), which is a long, narrow box. Electron velocities are  
192 tracked in 3D. The perpendicular dimensions are periodic; electrons can travel along  $\mathbf{B}$ , orbit  $\mathbf{B}$ ,  
193 magnetically mirror, and receive impulses from  $\mathbf{E}$ , but cannot carry out curvature or  $\nabla_{\perp} B$  drifts  
194 (discussed later).  $E_{DC} = 0$  so there is no net drift.

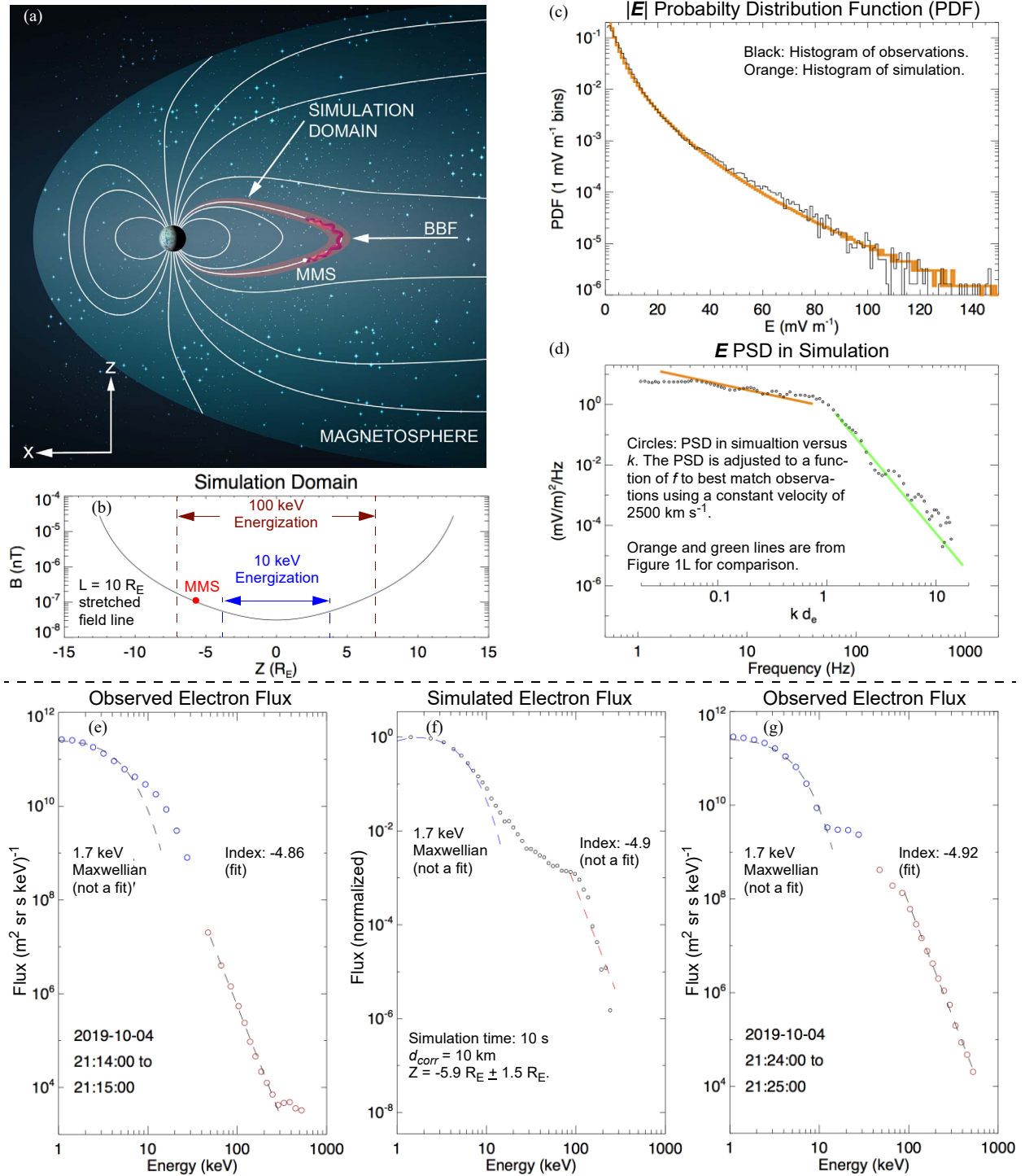
195 The test-particle simulation is not self-consistent as it imposes  $\mathbf{E}$  and constant  $\mathbf{B}$ . A key  
196 feature of the simulation, however, is that  $\mathbf{E}$  is constructed to match the observed  $\langle \mathbf{E} \rangle_{RMS}$ , PDF  
197 (Figure 2c), spectrum (Figure 2d), and correlation lengths (Figure 1q). Since a realistic  
198 reproduction of  $\mathbf{E}$  is central to understanding local acceleration, we provide further detail (also  
199 see Figure 6 in Ergun et al., 2020b). Reconstructed  $\mathbf{E}$  is limited to the frequency range of  $\sim 1.6$  to  
200  $\sim 100$  Hz, where most of the power lies. Since  $\mathbf{E}$  is primarily electrostatic, a scalar potential ( $\Phi$ )

201 is pseudo-randomly assigned so that the PDF of the reconstructed  $\mathbf{E}$  matches the observed PDF  
 202 and  $\langle \mathbf{E} \rangle_{RMS}$  (Figure 2c).  $\Phi$  is on a grid with perpendicular spacing proportional to  $d_{corr\perp}$ . Since  
 203  $d_{corr}$  is only constrained by observations,  $d_{corr\perp}$  is treated as a variable; the simulation is  
 204 performed with  $d_{corr\perp}$  ranging from 2 km to 10 km. As discussed earlier, the electrostatic  
 205 condition enforces  $d_{corr\parallel} = d_{corr\perp} \langle E_{\perp} \rangle_{RMS} / \langle E_{\parallel} \rangle_{RMS}$ . An example of the resulting PSD versus  
 206  $|\mathbf{k}|d_e$  ( $d_{corr\perp} = 10$  km) is plotted in Figure 2d. Mapping between  $|\mathbf{k}|$  and  $f$  with a fixed velocity of  
 207  $2500 \text{ km s}^{-1}$  (nearly  $V_A$  the Alfvén velocity, Figure 1n) yields a good match to the measured  $\mathbf{E}$   
 208 PSD versus  $f$  (Figure 1m). As time advances,  $\Phi$  is regenerated every 10 ms to 500 ms, pseudo-  
 209 randomly. This imposed time variation is consistent with observations and slow compared to  
 210  $1/f_{ce}$ . At the equator, for example, an electron undergoes 8 to 400 orbits before  $\Phi$  is altered.  
 211  $\langle \mathbf{E} \rangle_{RMS}$  is constant between  $Z = \pm 7 R_E$  (Figure 2b) but is reduced at larger values of  $Z$ . MMS is  
 212 located at  $-5.9 R_E$  in the simulation domain (Figure 2b). A primary assumption is that  $\mathbf{E}$   
 213 turbulence extends through the equator, which is consistent with previous reports (e.g. Ergun et  
 214 al., 2015).

215 The simulation is initiated with a  $T_e = 600$  eV Maxwellian distribution (see Figure 11 at 21:10  
 216 UT) with a constant density. Electrons then evolve in time under gyration, the magnetic mirror  
 217 force, and  $\mathbf{E}$ . The  $\pm Z$  boundaries of the simulation are open. A particle that exits the domain is  
 218 replaced by a randomly-generated thermal particle ( $T_e = 600$  eV) at the boundary. More than  
 219 95% of particles initialized between  $Z = \pm 6 R_E$  remain in the simulation domain after 10 s due to  
 220 the robust magnetic mirror. The simulation is tested for 50 s with  $\mathbf{E} = 0$  to assure conservation of  
 221 energy. Tests also verify that energization is proportional  $\langle E^2 \rangle$ .

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223



**Figure 2.** Details of and results from the test-particle simulation. (a) A cartoon depicting the simulation domain. (b)  $|B|$  in the simulation domain. (c) The PDF of  $|E|$  as observed (black) and in the simulation domain (orange). The near-exact match is by design. (d) An example of a PSD

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versus  $k$  in the simulation (circles) and the fits to the observed PSD versus  $f$  in Figure 1m (orange and green lines). Mapping between  $k$  and  $f$  using a velocity of  $2500 \text{ km s}^{-1}$  creates the best match. (e) The electron flux as observed during the turbulent event. (f) The electron flux from the test-particle simulation with  $d_{corr} = 10 \text{ km}$  at  $10 \text{ s}$ . (g) The electron flux as observed in the outer radiation belt.

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225 After initiation, the simulation is advanced until electrons attain an energy density similar to  
226 that observed. In the simulation, curvature and  $\nabla_{\perp} B$  drifts do not influence an electron's  
227 evolution. These drift speeds are proportional to energy ( $W$ ) and inversely proportional to  $|\mathbf{B}|$ . A  
228 concern is that high-energy electrons drift relative to the thermal electrons and may have a  
229 different dwell times in the turbulent region. For example, a  $100 \text{ keV}$  electron trapped near the  
230 equator can drift relative to core electrons up to  $\sim 200 \text{ km s}^{-1}$ . If the scale size of a BBF is  $1 R_E$ ,  
231 higher-energy ( $\sim 100 \text{ keV}$ ) electrons separate from the core in roughly  $30 \text{ s}$ . This interval is less  
232 than the observed duration of the turbulence ( $\sim 600 \text{ s}$ ; Figure 1) but greater than the simulation  
233 run times ( $10 \text{ s}$ ). As a result, curvature drifts and  $\nabla_{\perp} B$  drifts are inconsequential in the  
234 simulation, but should be significant for data interpretation.

235 Figures 2e-2g compare observed electron flux (intensity) with electron flux in the simulation.  
236 On the left (Figure 2e, circles) is the observed electron flux as a function of energy compiled  
237 inside of the turbulent region. The time is written in the plot. In the center (Figure 2f) is a flux  
238 distribution ( $Z = \pm 5.9 \pm 1 R_E$ ) from the simulation at  $t = 10 \text{ s}$  with  $d_{corr\perp} = 10 \text{ km}$ . On the right  
239 (Figure 2g) is an observed flux distribution from the outer radiation belt. The shapes of the  
240 simulated and observed fluxes have several common characteristics. The core of the flux  
241 distributions have a similar  $T_e \sim 1.7 \text{ keV}$  (see dashed blue lines). Most noticeably, the observed

242 and simulation fluxes have a “shoulder” between  $\sim 10$  keV and  $\sim 100$  keV and a steep power-law  
243 tail at energies  $> 100$  keV. Setting  $d_{corr}$  to  $< 10$  km results in faster energization. Simulations  
244 suggest that  $\mathbf{E}$ , as measured and if extended along  $\mathbf{B}$ , can be responsible for local acceleration.

245 The simulation’s  $\sim 10$  s run time to reach observed electron energy levels seems fast when  
246 compared to the duration of the BBF event (600 s), but is somewhat consistent with the time that  
247 curvature and  $\nabla_{\perp} B$  drifts separate electron populations. Furthermore,  $V_{ion}$  (Figure 1h),  $V_{Elc}$   
248 (Figure 1i), and  $\mathbf{E}$  (Figure 1j) indicate substantial Hall fields (ions are decoupled).  $V_{Elc}$  reaches  
249  $1000 \text{ km s}^{-1}$  and often differs from  $V_{ion}$  by more than  $100 \text{ km s}^{-1}$ , which may limit an energetic  
250 electron’s dwell time in the region of turbulence to  $\sim 10$  s, which the simulation suggests.

251 There is one notable discrepancy between the simulation results and observations. The  
252 observed electron distributions are nearly isotropic (Figure 1l) whereas the simulated electron  
253 distributions have  $T_{e\perp} > T_{e\parallel}$ . This discrepancy likely results in part from the imposition of  
254  $\langle E_{\perp} \rangle_{RMS} / \langle E_{\parallel} \rangle_{RMS} = 7$  over the entire simulation domain. This ratio is closer to 3 in turbulent  
255 BBF events nearer to the equator (Ergun et al., 2015). Additionally, coherent waves such as  
256 Alfvén and whistler waves may act to pitch angle scatter electrons (e. g. Chaston et al, 2018).

#### 257 **4. Discussion and Conclusions**

258 The MMS satellites detected a turbulent BBF braking region close to the outer radiation belt.  
259 Of primary interest,  $T_i$  and  $T_e$  increase and high-energy ion and electron fluxes vary concurrently  
260 with  $\mathbf{E}$ ,  $\mathbf{B}$ , and  $V_{ion}$  suggesting local energization and acceleration.

261 The properties of  $\mathbf{E}$  are investigated in detail including the spectra, correlation distance, PDF,  
262 and RMS amplitude. The four-spacecraft MMS mission constrained  $d_{corr}$  to be  $\leq 10$  km in the  
263  $\sim 1.6$  to  $\sim 100$  Hz frequency range (Figure 1q). The fact that  $\mathbf{E}$  is uncorrelated at a relatively small  
264 separation is critical. Perpendicular energization requires violation of  $\mu$  conservation and there is

265 little power in  $\mathbf{E}$  with  $f > f_{ce}$ . We hypothesize that if  $p_{\perp}/m_0c$  or  $p_{\parallel}/m_0c$  exceed  $\omega_{ce0}/\omega_{pe}$ , an electron  
266 experiences changes in  $\mathbf{E}$  faster than  $1/f_{ce}$ , which breaks conservation of  $\mu$ . This postulation also  
267 implies that the highest-energy electrons receive more energy than do the lower-energy  
268 electrons, which leads to the development a non-thermal shoulder and energetic tail in the  
269 electron distribution.

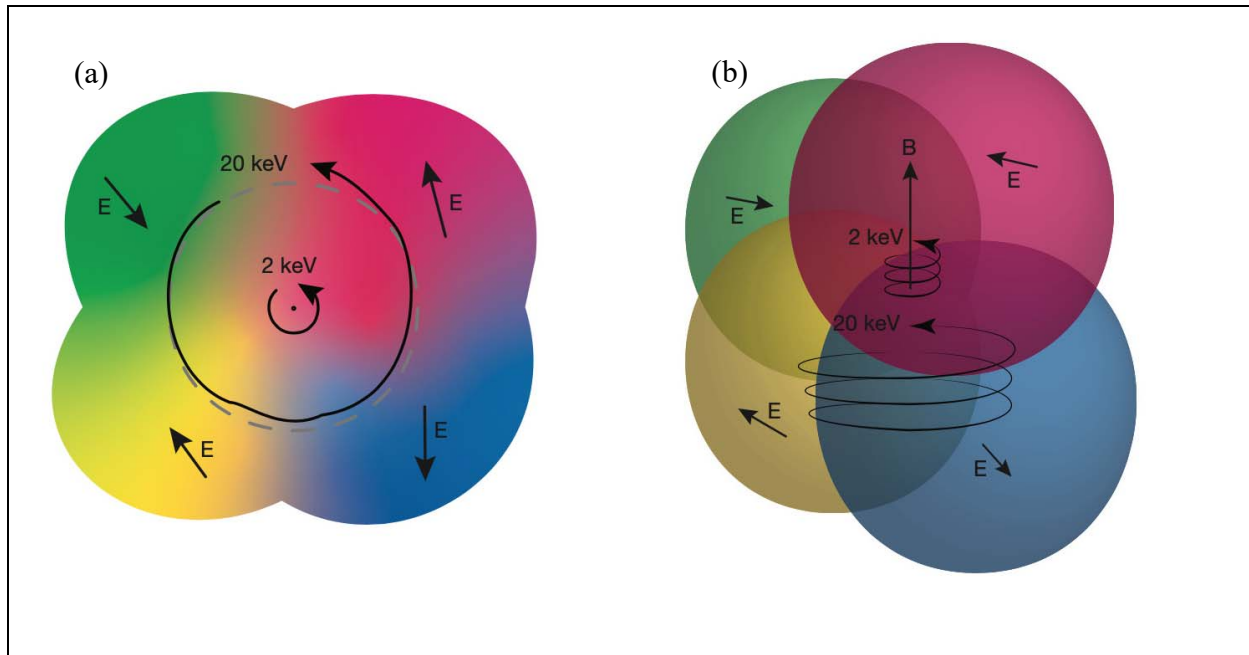
270 Figure 3 illustrates the underlying process of particle acceleration by turbulent, uncorrelated,  
271 electrostatic  $\mathbf{E}$ . In the plane of the gyration, a low-energy electron (2 keV in the drawing)  
272 experiences a nearly constant  $\mathbf{E}$  whereas a higher-energy electron (20 keV in the drawing)  
273 transits regions of changing  $\mathbf{E}$  during its gyration. Even though  $\mathbf{E}$  is primarily electrostatic, the  
274 particle does not necessarily return to the same location in the perpendicular plane (Figure 3a) or  
275 in the same location along  $\mathbf{B}$  (Figure 3b) and therefore can experience energy change. The time  
276 dependence of  $\mathbf{E}$ , albeit slow, is crucial in that an electron's energy gain or loss is not limited to  
277 the largest variation in  $\Phi$ . A finite  $\nabla \times \mathbf{E}$  can enhance acceleration.

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**Figure 3.** A drawing of electron orbits in an uncorrelated, electrostatic  $\mathbf{E}$  illustrating how turbulent acceleration favors higher-energy electrons. (a) A view of the orbital plane. The higher-energy (20 keV) electron's orbit transits several uncorrelated regions of  $\mathbf{E}$  (including  $E_{\parallel}$ ) as it gyrates and therefore does not necessarily follow a closed path. It can gain or lose energy. A lower-energy electron (2 keV) sees very little change in  $\mathbf{E}$  over an orbit. (b) A 3D view of an electron's helical path along  $\mathbf{B}$ . A high-energy electron can experience changes in  $\mathbf{E}$  faster than its gyration period.

281

282 This hypothesis is tested with a quasi-1D test-particle simulation. Electrons are magnetized  
 283 and therefore well represented by a 1D simulation whereas ions require a much more complex  
 284 investigation. A key aspect of the simulation is the careful reproduction of the observed  $\mathbf{E}$   
 285 including the  $d_{corr}$ , spectrum, parallel and perpendicular RMS power, and PDF. The salient result  
 286 (Figures 2e-2g) is that the electron distributions develop an extended shoulder above  $\sim 10$  keV  
 287 and an energetic tail. Despite its short-comings, (not self-consistent, RMS  $\mathbf{E}$  extends  $\pm 7 R_E$  from

288 the equator, simulation distributions are not isotropic, drifts are not included), the simulation  
 289 demonstrates the feasibility of local electron acceleration.

290 Analytically, one can estimate electron energization rates from random impulses via Equation  
 291 7 in Ergun et al, (2020b):

$$\dot{W} \approx \frac{e^2 \langle E_{eff}^2 \rangle \langle \delta t \rangle}{2 W / c^2} \#4$$

292  
 293 where  $W = \gamma m_0 c^2$  and  $\langle E_{eff}^2 \rangle$  represents the effective RMS  $E$  (that with  $f > f_{ce}$  in the electron  
 294 frame) experienced along an electron's helical path. Significantly,  $\langle E_{eff}^2 \rangle$  strongly increases with  
 295 increasing  $W$  (Equation 3). The period of the impulses,  $\langle \delta t \rangle$ , is a fraction of the gyroperiod. For  
 296 example, in Figure 3a,  $\langle \delta t \rangle \approx 1/(4 f_{ce})$  for the 20 keV electron. From observations,  $\langle E_{eff}^2 \rangle \approx 70$   
 297  $\text{mV}^2 \text{m}^{-2}$  and  $\langle \delta t \rangle \approx 8 \times 10^{-5} \text{ s}$ . A  $> \sim 20 \text{ keV}$  electron experiences  $\sim 500 \text{ eV/s}$  of energization on  
 298 average, supporting the simulation results. Core electrons ( $< 2.5 \text{ keV}$ ) experience a much smaller  
 299  $\langle E_{eff}^2 \rangle$  and receive significantly less energization. This analytical exercise illustrates why the  
 300 electron distribution (Figure 2f) develops an extended shoulder above  $\sim 5 \text{ keV}$ ; high energy  
 301 electrons receive full acceleration while core electrons are heated at a slower pace. For high- $\gamma$   
 302 electrons, we note that  $\langle \delta t \rangle$  is proportional to  $\gamma$ , so  $\dot{W}$  increases with energy.

303 Another interesting aspect unique to electrons trapped in a dipole field is illustrated in Figure  
 304 2b. The extent along  $B$  in which an electron experiences full energization increases with an  
 305 electron's energy (Equation 3). For example, a 100 keV electron is subject to full energization  
 306 between  $Z = \pm 7 R_E$  whereas a 10 keV electron only has full energization between  $Z = \pm 4 R_E$ .  
 307 Consequently, higher-energy electrons again receive more energy further favoring acceleration.

308 In conclusion, MMS observations of electron and ion acceleration from a turbulent BBF  
309 suggest local acceleration by  $E$ . Electron acceleration is supported by test-particle simulation that  
310 used a realistic reproduction of the observed  $E$ . The resulting enhanced shoulder and energetic  
311 tail in the electron distribution just outside of the radiation belts could supply electrons to the  
312 outer radiation belt. If these electrons are adiabatically transported closer to Earth (higher  $|B|$ ,  
313 Gabrielse et al, 2012; Turner et al., 2015; 2016; Ukhorskiy et al., 2017; Sorathia et al., 2018;  
314 Turner et al., 2021), they can account for MeV electrons. A more far-reaching conclusion is that,  
315 since turbulence is pervasive in plasmas, it is likely a significant contributor to charged particle  
316 acceleration.

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320 the International Space Sciences Institute for support. JES is supported by the Royal Society  
321 University Research Fellowship URF\R1\201286.

### 322 **Data Availability Statement**

323 The MMS data set is available at <https://lasp.colorado.edu/mms/sdc/public/datasets/>.

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467 **Figure Captions**

468 **Figure 1.** MMS1 observations of a BBF penetrating close to the outer radiation belt. The  
469 horizontal axis on the left column is 50 minutes in time. Vectors are in GSM coordinates; colors  
470 represent components as marked on the right of a panel. (a)  $\mathbf{B}$  at 62.5 ms resolution. The black  
471 trace is  $|\mathbf{B}|$ . (b) A magnified view of  $B_x$ . (c)  $\mathbf{B}$  detrended by 10 s. (d) Ion flux as a function of  
472 energy (vertical axis) from 70 to 600 keV. These data are from all four MMS spacecraft. (e)  
473 Differential ion energy flux as a function of energy from 3 eV to 25 keV. (f) Electron flux from  
474 60 to 500 keV. (g) Differential electron energy flux 6 eV to 25 keV. (h)  $V_{Ion}$  at 4.5 s resolution.  
475 (i)  $V_{Elec}$  at 4.5 s resolution smoothed over 13.5 s. (j)  $\mathbf{E}$  at 31.25 ms resolution. (k) Electron density  
476 at 4.5 s resolution. (l)  $T_i$  and  $T_e$  at 4.5 s resolution. (m) The PSD of  $\mathbf{B}$  and  $\mathbf{E}$  versus frequency. (n)  
477 Average plasma conditions. (o) The relative positions of the MMS spacecraft. (p) The cross-  
478 correlation of  $\mathbf{E}$  between the MMS spacecraft plotted as a function of separation.  $\mathbf{E}$  is filtered  
479 from DC to 1.6 Hz. (q) The cross-correlation of  $\mathbf{E}$  filtered from 1.6 Hz to 100 Hz.

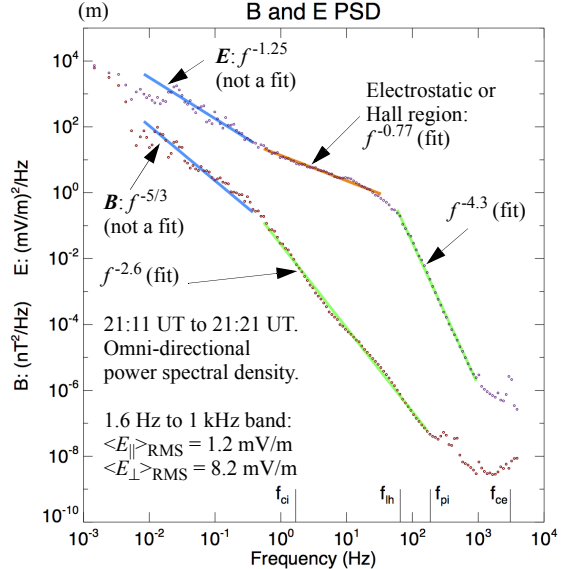
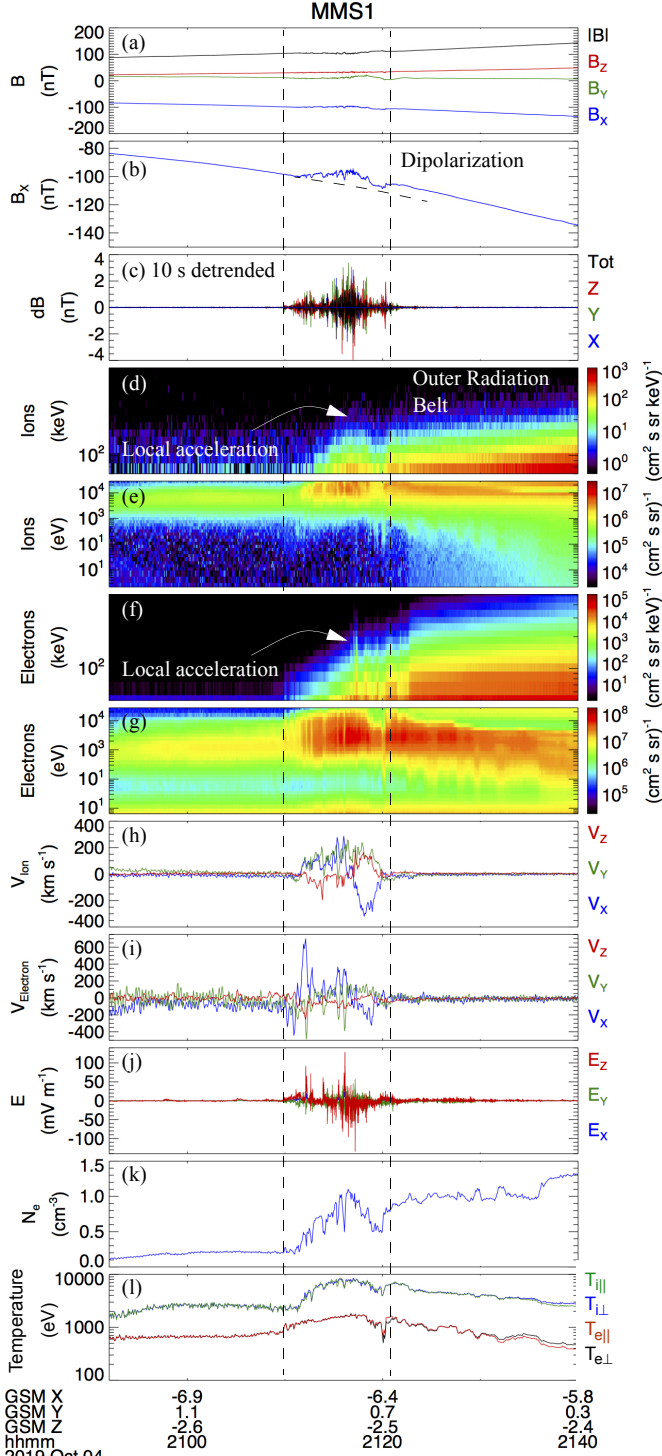
480

481 **Figure 2.** Details of and results from the test-particle simulation. (a) A cartoon depicting the  
482 simulation domain. (b)  $|\mathbf{B}|$  in the simulation domain. (c) The PDF of  $|\mathbf{E}|$  as observed (black) and  
483 in the simulation domain (orange). The near-exact match is by design. (d) An example of a PSD  
484 versus  $k$  in the simulation (circles) and the fits to the observed PSD versus  $f$  in Figure 1m (orange  
485 and green lines). Mapping between  $k$  and  $f$  using a velocity of  $2500 \text{ km s}^{-1}$  creates the best match.  
486 (e) The electron flux as observed during the turbulent event. (f) The electron flux from the test-  
487 particle simulation with  $d_{corr} = 10 \text{ km}$  at 10 s. (g) The electron flux as observed in the outer  
488 radiation belt.

489

490 **Figure 3.** A drawing of electron orbits in an uncorrelated, electrostatic  $\mathbf{E}$  illustrating how  
491 turbulent acceleration favors higher-energy electrons. (a) A view of the orbital plane. The higher-  
492 energy (20 keV) electron's orbit transits several uncorrelated regions of  $\mathbf{E}$  (including  $E_{\parallel}$ ) as it  
493 gyrates and therefore does not follow a closed path. It can gain or lose energy. A lower-energy  
494 electron (2 keV) sees little change in  $\mathbf{E}$  over an orbit. (b) A 3D view of an electron's helical path  
495 along  $\mathbf{B}$ . A high-energy electron can experience changes in  $\mathbf{E}$  faster than its gyration period.  
496

Figure 1.



(n) Plasma Conditions (21:11 UT to 21:21 UT)

Parameter	Value	Parameter	Value
$\langle n_e \rangle$	0.8 cm <sup>-3</sup>	$\langle v_{\text{the}} \rangle$	17000 km s <sup>-1</sup>
$\langle T_e \rangle$	1.7 keV	$\langle v_{\text{thi}} \rangle$	820 km s <sup>-1</sup>
$\langle T_i \rangle$	7.0 keV	$\langle V_A \rangle$	2700 km s <sup>-1</sup>
$\langle B \rangle$	110 nT	$\langle V_S \rangle$	1400 km s <sup>-1</sup>
$\langle f_{\text{pe}} \rangle$	8 kHz	$\langle \rho_e \rangle$	0.82 km
$\langle f_{\text{ce}} \rangle$	3.1 kHz	$\langle \rho_i \rangle$	78 km
$\langle f_{\text{pi}} \rangle$	190 Hz	$\langle d_e \rangle$	6 km
$\langle f_{\text{ci}} \rangle$	1.7 Hz	$\langle d_i \rangle$	250 km

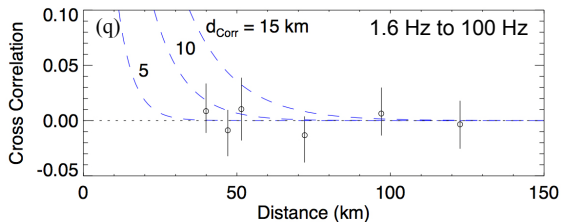
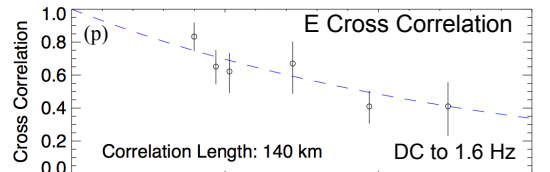
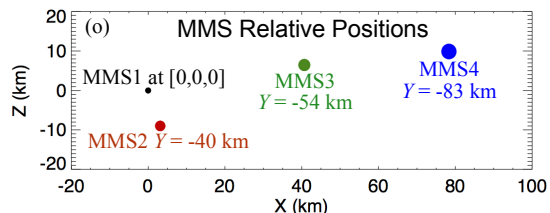


Figure 2.

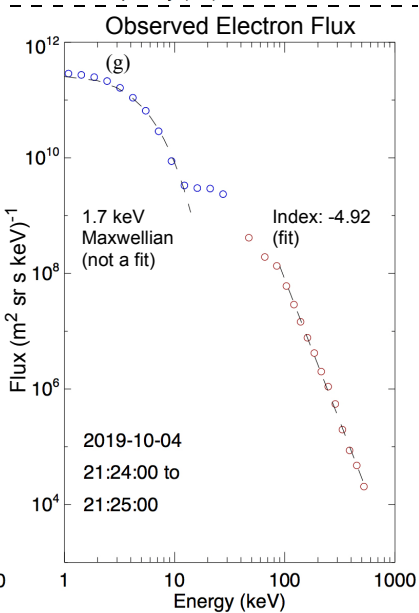
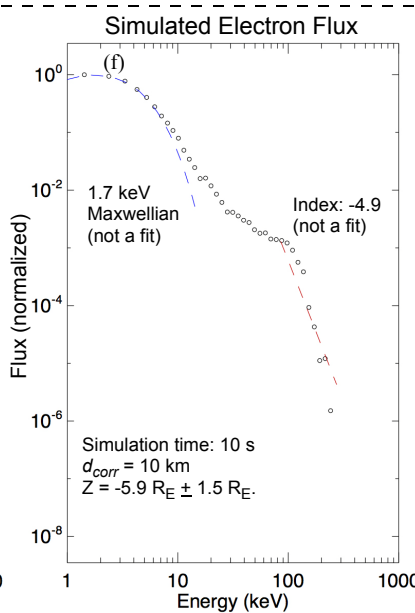
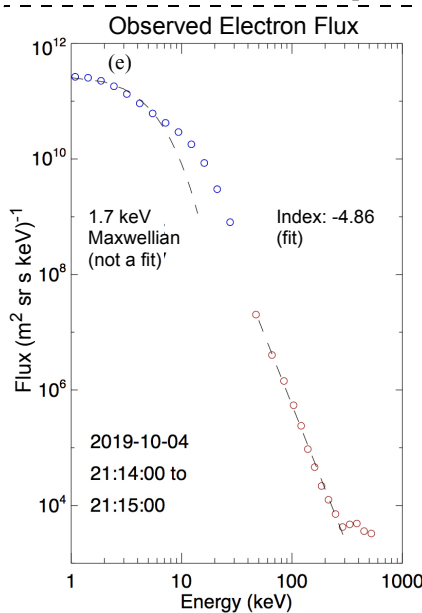
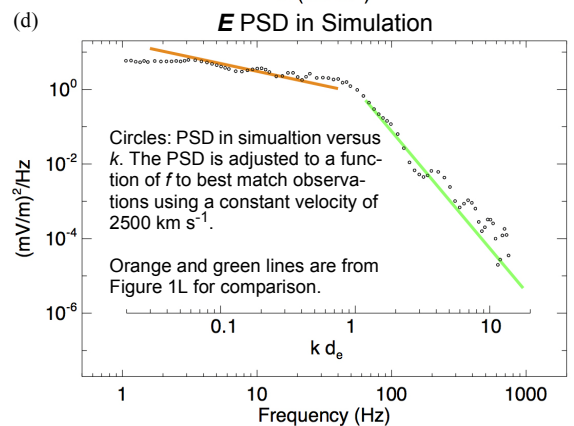
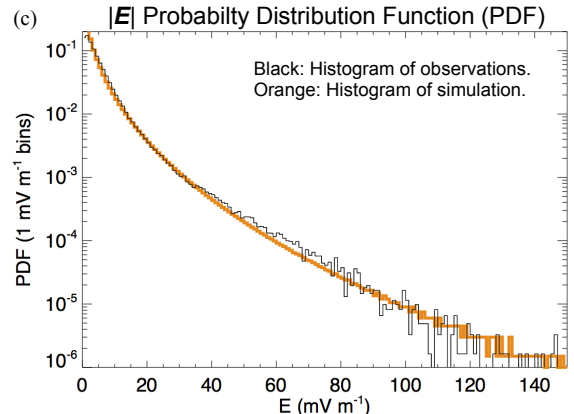
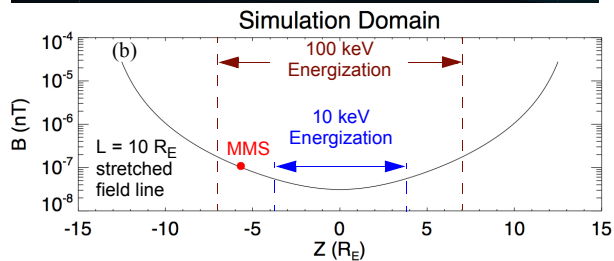
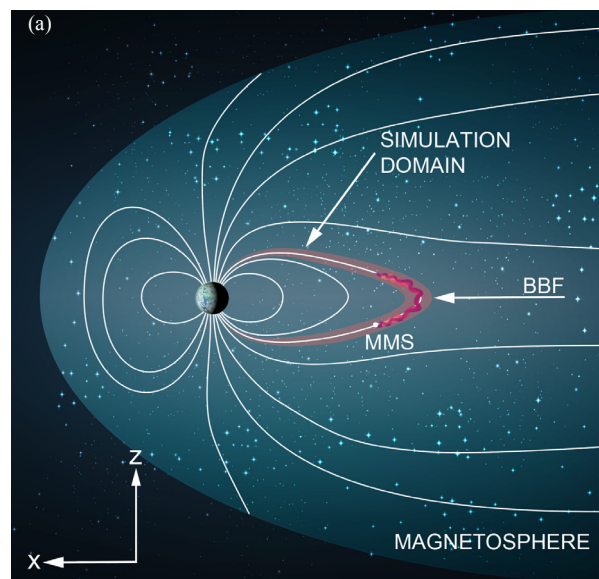
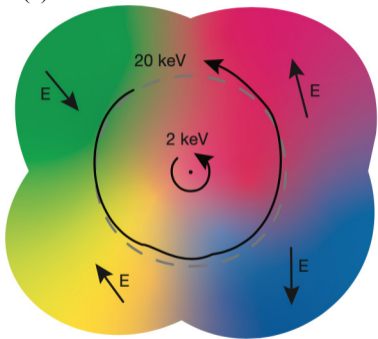


Figure 3.



(a)



(b)

