# High-Qf value and temperature stable Zn<sup>2+</sup>-Mn<sup>4+</sup> cooperated modified cordierite-based microwave and millimeter-wave dielectric ceramics

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## Abstract

Cordierite-based dielectric ceramics with a lower dielectric constant would have significant application potential as dielectric resonator and filter materials for future ultra-low-latency 5G/6G millimeter-wave and terahertz communication. In this article, the phase structure, microstructure and microwave dielectric properties of Mg<sub>2</sub>Al<sub>4-</sub>  $_{2x}(Mn_{0.5}Zn_{0.5})_{2x}Si_5O_{18}$  ( $0 \le x \le 0.3$ ) ceramics are studied by crystal structure refinement, scanning electron microscope (SEM), the theory of complex chemical bonds and infrared reflectance spectrum. Meanwhile, complex double-ions coordinated substitution and two-phase complex methods were used to improve its  $Q \times f$  value and adjust its temperature coefficient. The  $Q \times f$  values of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> single-phase ceramics are increased from 45000 GHz @ 14.7 GHz (x=0) to 150500 GHz (a) 14.5 GHz (x=0.15) by replacing Al<sup>3+</sup> with Zn<sup>2+</sup>-Mn<sup>4+</sup>. The positive frequency temperature coefficient additive TiO<sub>2</sub> is used to prepare the temperature stable Mg<sub>2</sub>Al<sub>3.7</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>0.3</sub>Si<sub>5</sub>O<sub>18</sub>-ywt%TiO<sub>2</sub> composite ceramic. The composite ceramic of  $Mg_2Al_{3.7}(Mn_{0.5}Zn_{0.5})_{0.3}Si_5O_{18}-ywt\%TiO_2$  (8.7 wt%  $\leq y \leq 10.6$  wt%) presents the nearzero frequency temperature coefficient at 1225 °C sintering temperature:  $\varepsilon_r = 5.68, Q \times f$ = 58040 GHz,  $\tau_f$  = -3.1 ppm/°C (y=8.7 wt%) and  $\varepsilon_r$  = 5.82,  $Q \times f$  = 47020 GHz,  $\tau_f$  = +2.4 ppm/°C (v=10.6 wt%). These findings demonstrate promising application prospects for 5G and future microwave and millimeter-wave wireless communication technologies.

**Keywords:** Cordierite; Microwave and millimeter-wave dielectric ceramics; 5G/6G communication; Infrared reflectance spectrum

# 1. Introduction

With the rapid development and deployment of 5G communication technology from 5G-Sub6GHz to 5G/6G-Sub100GHz till terahertz, microwave and millimeterwave dielectric ceramic materials would have been widely used in 5G/6G communication systems as dielectric materials of the resonators, filters, duplexers, microwave strip, substrate, etc <sup>[1-3]</sup>. There are three key parameters to evaluate the performance of microwave dielectric ceramics, namely the relative permittivity ( $\varepsilon_r$ ), the quality factor  $(Q \times f)$  and the temperature coefficient of resonance frequency  $(\tau_f)$ , which are closely related to the application field, loss and temperature stability <sup>[4]</sup>. Compared with centimeter-wave, decimeter-wave and meter-wave, the wavelength of millimeterwave and terahertz is shorter. Therefore, it is not necessary to select materials with a high dielectric constant to reduce the size of devices. Meanwhile, 5G and 6G require the time delay of signal transmission response to be less than 1 and 0.1 ms, respectively. Because the time delay  $(t_d)$  in the dielectric resonator is proportional to the square root of  $\varepsilon_r$ , materials with a low dielectric constant are selected to reduce it according to the following relationship<sup>[5]:</sup>

$$t_d = L \frac{\sqrt{\varepsilon_r}}{c} \tag{1}$$

where *c* represents the velocity of light and *L* is the signal transmission distance. Hence, the low-dielectric constant cordierite (Mg<sub>2</sub>Al<sub>4</sub>Si<sub>5</sub>O<sub>18</sub>) material will be the leading candidate for future 5G-Sub100GHz and 6G-terahertz communications <sup>[6]</sup>.

There are two stable forms of cordierite structure:  $\alpha$ -cordierite, which has a

hexagonal structure sintered at high-temperature (1550-1600 °C), and β-cordierite, which has an orthorhombic structure at relative low temperature (1350-1475 °C)<sup>[7]</sup>. The orthorhombic β-cordierite is the most commonly synthesized cordierite. However, βcordierite ceramics with higher sintered temperatures and lower  $Q \times f$  values do not meet the requirements of millimeter-wave communication applications. In the years 2007-2010, H. Oshato *et al.* reported cordierite ceramic for microwave and millimeter-wave applications with  $\varepsilon_r = 6.19$ ,  $Q \times f = 39000$  GHz ~ 99110 GHz, and  $\tau_f = -32$  ppm/°C~ -34 ppm/°C <sup>[8-9]</sup>. Song *et al.* studied the relationship between the crystal structure of cordierite ceramics and their microwave dielectric properties from the viewpoint of hexagonal ring symmetry of inner tetrahedron [Si<sub>4</sub>Al<sub>2</sub>O<sub>18</sub>] and outer octahedron [Mg<sub>6</sub>O<sub>36</sub>] <sup>[10-12]</sup>. The substitution of (Li<sub>0.5</sub>Ga<sub>0.5</sub>)<sup>2+</sup> for Mg<sup>2+</sup> in Mg<sub>2</sub>Al<sub>4</sub>Si<sub>5</sub>O<sub>18</sub> ceramics has improved the microwave dielectric properties of cordierite ceramics <sup>[13]</sup>.

As is well known, the microwave dielectric properties of a material will be affected by changes in its overall structure caused by ion substitution or the filling of other elements. The majority of prior research has been focused on elemental substitution at the Mg<sup>2+</sup> octahedron lattice site of cordierite and temperature stable adjustment complicated by the positive temperature coefficient of resonant frequency of TiO<sub>2</sub> <sup>[14-<sup>16]</sup>. However, complex ionic modification of [AlO<sub>4</sub>] ionic lattice sites in cordierite is the subject of very few studies. Herein, in order to further explore the influence of complex ionic pairs coordinated replacing Al<sup>3+</sup> tetrahedron lattice sites on cordierite dielectric ceramic, this paper designed a strategy of the substitution of [Mn<sup>4+</sup><sub>1/2</sub>Zn<sup>2+</sup><sub>1/2</sub>] on Al<sup>3+</sup> to prepare Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> (0≤x≤0.3) solid solution ceramics, and then</sup> further used TiO<sub>2</sub> to tune its temperature coefficient of resonant frequency. Compared to all previously reported data, a high  $Q \times f$  value (150500 GHz) has been obtained for cordierite. Simultaneously, a series of wonderful temperature stable cordierite type ceramics have been developed with  $\varepsilon_r = 5.68 \times 5.82$ ,  $Q \times f = 47020$  GHz $\sim 58040$  GHz,  $\tau_f = -3.1$  ppm/°C  $\sim +2.4$  ppm/°C, which can be applied to future 5G and 6G communication applications with higher frequency.

# 2. Experimental procedure

Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> cordierite-typed ceramics were prepared by high purity raw materials of MgO (99.99%), Al<sub>2</sub>O<sub>3</sub> (99.99%), SiO<sub>2</sub> (99.99%), MnO<sub>2</sub> (99.5%), ZnO (99.99%), TiO<sub>2</sub> (99.99%). MgO and ZnO were calcined at 950 °C for 3 hours to exclude impurities, while the other raw materials were dried at 100 °C for 24 h to remove moisture. All raw materials were weighted according to the stoichiometric ratio and ball milled for 6 h with ethanol as the solvent in a Teflon tank. The dried powders were calcined at 1200 °C for 4 h, and the calcined powders were re-milled for 6 hours. The calcined powders were mixed with 8 wt% PVA solution and pressed into a cylindrical pellet of  $\Phi$ 12 mm×7 mm. Finally, the samples were sintered at 1250-1450 °C for 4 hours at a heating rate of 3 °C/min.

The bulk density  $(\rho_b)$  of ceramic samples was measured by the Archimedes method. The theoretical density can be obtained by the following formula:

$$\rho_{theo} = \frac{ZA}{V_c N_A} \tag{2}$$

where Z, A and Vc are the number of atoms in a unit cell, atomic weight and volume of

a unit cell, respectively. The relative density was obtained by the following formula:

$$\rho_r = \frac{\rho_b}{\rho_{theo}} \times 100\% \tag{3}$$

The crystalline structure of the sintered ceramic samples was identified by X-ray powder diffraction (XRD) using Cu K $\alpha$  radiation (Rigaku, Ultima IV, Japan) operated at 40 kV and 30 mA. The surface morphology of ceramic samples was examined using a scanning electron microscopy (SEM, Hitachi S-4800, Hitachi, Japan), which were thermal etched at the 100 °C lower than densification sintered temperature for 30 minutes. The infrared reflectance spectra were collected on the infrared beam line (IFS 66 v/S) of the Hefei National Synchrotron Radiation Laboratory. The microwave dielectric properties of the samples were measured by a Keysight E5071c network analyzer using the TE<sub>01δ</sub> mode dielectric resonator method. The temperature coefficients of resonance frequency ( $\tau_f$ ), were evaluated in the temperature range of 25-85 °C, calculated by the following formula:

$$\tau_{\rm f} = \frac{f_2 - f_1}{f_1 \times (T_2 - T_1)} \times 10^6 (ppm/^{\circ}{\rm C}) \tag{4}$$

where  $f_1$  and  $f_2$  were the resonant frequency at 25 and 85 °C, respectively.

#### 3. Results and discussion

The bulk density of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> (x=0, 0.05, 0.1, 0.15, 0.2, 0.25, 0.3) ceramics at various sintering temperatures are shown in Figure 1(a). As *x* increases, the optimal sintering temperature decreases and the densification sintering range broadens up to 100 °C (0.15 $\leq x\leq$ 0.3). The relative densities of each component are greater than 95% at optimal sintering temperature, as shown in Figure 1(b). The XRD

patterns of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> ceramics are shown in Figure(c). All XRD peaks of sintered samples are well matched with the orthorhombic phase of the cordierite structure (JCPDS No.82-1541) with the space group of *Cccm* (66). Rietveld refinement was applied to the XRD data of the ceramic powder sample. Table S1 and S2 (Supporting Information) list the structural refinement data of all studied compositions. Figure S1 (Supporting Information) shows the Rietveld fitted pattern of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> (*x*=0.15). The low refinement factors (*Rwp* = 8.56%, *Rp* = 4.74%) indicate that the results of Rietveld refinement were reliable. The crystal structure schematic of Mg<sub>2</sub>Al<sub>4</sub>Si<sub>5</sub>O<sub>18</sub> is shown in Figure 1(d).



Figure 1. (a) The bulk density of  $Mg_2Al_{4-2x}(Mn_{0.5}Zn_{0.5})_{2x}Si_5O_{18}$  ceramics as a function of sintering temperature. (b) The relative density of ceramics sintered with different components at the optimal sintering temperature. (c) XRD patterns of ceramics sintered with various components of  $Mg_2Al_{4-2x}(Mn_{0.5}Zn_{0.5})_{2x}Si_5O_{18}$  at 1250-1450 °C for 4 h. (d)

The crystal structure schematic of Mg<sub>2</sub>Al<sub>4</sub>Si<sub>5</sub>O<sub>18</sub> on the a-b plane.

The SEM images of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> (x=0.1, 0.15, 0.2) ceramics with various compositions at the optimal sintering temperature are presented in Figure 2. With the Zn<sup>2+</sup>-Mn<sup>4+</sup> doping concentration increasing, the grain size grows slightly and the porosity decreases. At x=0.15, a well-formed and dense microstructure is observed, which is consistent with the theoretical density variation trend in Figure 1(b). However, as the doping concentration increases, the porosity begins to increase, which can be attributed to the abnormal growth of certain grains.



Figure 2. SEM images of the natural cross-sections of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> ceramics (a) x=0.1, (b) x=0.15, (c) x=0.2.

In order to explore the relationship between crystal structure and microwave dielectric properties, the complex chemical bond theory was used to elucidate the intrinsic factors affecting microwave dielectric properties of cordierite ceramics. The detailed calculation methods are included in the Supporting Information<sup>[17-22]</sup>.

Figure 3 shows the  $\varepsilon_r$ , average bond ionicity and calculated permittivity (bar graph) of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> ceramics. We can see that  $\varepsilon_r$  firstly decreases and then increases, showing the same trend as average bond ionicity ( $Af_i$ ). At x=0.15,  $\varepsilon_r$  and  $Af_i$ reach the minimum value at the same time, which indicates that  $\varepsilon_r$  and  $Af_i$  are strongly correlated. The bar graph also displays the calculated permittivity ( $\varepsilon_c$ ) results (4.95~4.963) according to the average bond ionicity, which are clearly close to the measured relative permittivity ( $\varepsilon_r$ ).



Figure 3. The  $\varepsilon_r$ , average bond ionicity and calculated permittivity of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> ceramics as a function of *x* value.

The correlation between the lattice energy U and inherent losses of microwave dielectric ceramics is strong as the U value reflects the ability of anions and cations to bind. Crystals with a greater binding capacity are more stable, which reduces their intrinsic losses. Therefore, U can be used to predict the  $Q \times f$  value. As shown in Figure 4, the  $Q \times f$  value of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> ceramics increases first with the increase of x, reaches a maximum at x=0.15, and then decreases gradually. The lattice energy reaches its maximum value of 117893 kJ/mol at the maximum  $Q \times f$  value of 150500 GHz. In general, the  $Q \times f$  value of ceramics is positively correlated with the lattice energy U.

Furthermore, the change in crystal structure is analyzed by calculating the degree of distortion of the [Si<sub>4</sub>Al<sub>2</sub>O<sub>18</sub>] six-membered ring. The lower standard deviation ( $\sigma$ ) indicates less distortion. Six corners are taken as the internal angles of the hexagonal

six-membered ring as shown in Figure 1(d). In this paper, the Si-Al angles of [Si(2)–Al(2)–Si(3), Si(2)-Si(3)-Al(2), Si(3)–Si(2)–Al(2)] and the oxygen angle of [O(5)–O(4)–O(6), O(4)–O(6)–O(5), O(6)–O(5)–O(4)] were used to evaluate the standard deviation ( $\sigma$ ) of the [Si<sub>4</sub>Al<sub>2</sub>O<sub>18</sub>] six-membered ring. The formula 5 was used to calculate the  $\sigma$  values of the [Si<sub>4</sub>Al<sub>2</sub>O<sub>18</sub>] ring:

$$\sigma = \sqrt{\frac{2 \times (a_1 - 120)^2 + 2 \times (a_2 - 120)^2 + 2 \times (a_3 - 120)^2}{6}} \tag{5}$$

where  $a_1$ ,  $a_2$ , and  $a_3$  are the three adjacent hexagonal angles in the six-membered ring. The detailed bond angles and calculated results are shown in Table S3 (Supporting Information). Figure 4 shows the  $\sigma$  of the [Si<sub>4</sub>Al<sub>2</sub>] ring and [O<sub>6</sub>] ring as a function of xvalue. The fact that when x=0.15, the value is at its lowest and the  $Q \times f$  value is at its highest indicates that the  $Q \times f$  value of ceramics is inversely correlated with the angles of the six-membered ring.



Figure 4. The  $Q \times f$ , lattice energy and  $\sigma$  of the [Si<sub>4</sub>Al<sub>2</sub>] and [O<sub>6</sub>] ring of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> ceramics as a function of *x* value.

The bond energy E is a performance indicator for evaluating the strength of chemical bonds and structural stability. The greater the bond energy of a chemical bond, the greater the energy required to break it, and the greater the structural stability. The

fact that the average bond energy of the Mg-O bond is the largest when compared to the Si-O and Al-O bonds suggests that the Mg-O bond energy plays a major role in the temperature stability of cordierite. The  $\tau_{\rm f}$  value and the Mg-O bond energy of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> ceramics are shown in Figure 5. In this work, the  $\tau_{\rm f}$  value fluctuates from -25.3 to -38.2 ppm/°C. Similar variation trends between  $\tau_{\rm f}$  and the Mg-O bond energy can also be observed.



Figure 5. The  $\tau_f$  value and the Mg-O bond energy of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> ceramics as a function of *x*.

Based on the optimal point of microwave dielectric properties at x=0.15, the temperature coefficient is modified. Figure 6 (a) shows the relationship between the bulk density and the sintering temperature of Mg<sub>2</sub>Al<sub>3.7</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>0.3</sub>Si<sub>5</sub>O<sub>18-y</sub>TiO<sub>2</sub> ceramics. In comparison to pure cordierite ceramic, the addition of TiO<sub>2</sub> enables the production of well-compacted ceramics at a lower temperature of sintering. The bulk density of each group initially increases with the sintering temperature. When the maximum density is reached, the bulk density begins to decrease gradually. This may be the phenomenon of over-sintering. The maximum bulk density is 2.68 g/cm<sup>3</sup> at

1225 °C. Figure 6 (b) displays the XRD patterns of Mg<sub>2</sub>Al<sub>3.7</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>0.3</sub>Si<sub>5</sub>O<sub>18</sub>-yTiO<sub>2</sub> (y=0, 1.6, 3.3, 5.0, 6.8, 8.7, 10.6 wt%) ceramics. With the increase of y, the TiO<sub>2</sub> diffraction peaks appear simultaneously with those of the cordierite phase at y=1.6 wt%.



Figure 6. (a) The bulk density of  $Mg_2Al_{3.7}(Mn_{0.5}Zn_{0.5})_{0.3}Si_5O_{18}-yTiO_2$  (y=0, 1.6, 3.3, 5.0, 6.8, 8.7, 10.6 wt%) ceramics as a function of sintering temperature. (b) XRD patterns of  $Mg_2Al_{3.7}(Mn_{0.5}Zn_{0.5})_{0.3}Si_5O_{18}-yTiO_2$  ceramics.

Figure 7 shows the relationship between the microwave dielectric properties of  $Mg_2Al_{3.7}(Mn_{0.5}Zn_{0.5})_{0.3}Si_5O_{18}-yTiO_2$  (y=0, 1.6, 3.3, 5.0, 6.8, 8.7, 10.6 wt%) ceramics. When y=1.6 wt%, a two-phase composite phenomenon occurs. Therefore, the composite rule can be used to predict the microwave dielectric properties of the two-phase composite ceramic. The dielectric constant and temperature coefficient of the resonance frequency were calculated by the compound formulas 6 and 7.

$$\ln \varepsilon_r = V \ln \varepsilon_1 + V 2 \ln \varepsilon_2 \tag{6}$$

$$\tau_f = V_1 \tau_{f1} + V_2 \tau_{f2} \tag{7}$$

As *y* increases, the  $\varepsilon_r$  increases from 4.95 to 5.82 in Figure 7(a), which is caused by the addition of TiO<sub>2</sub> with higher  $\varepsilon_r$ . The red line represents the actual measured value, and the blue line represents the calculated theoretical value. The  $Q \times f$  value decreases from 150500 GHz to 47020 GHz in Figure 7(b), indicating that the addition of TiO<sub>2</sub> can increase dielectric loss (tan $\delta$ ). The  $\tau_f$  value is adjusted to near-zero (+2.4 ppm/°C) at y=10.6 wt%, which shows excellent temperature stability.



Figure 7. (a-c) Microwave dielectric properties of Mg<sub>2</sub>Al<sub>3.7</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>0.3</sub>Si<sub>5</sub>O<sub>18</sub>-yTiO<sub>2</sub> ceramics as a function of TiO<sub>2</sub> weight fraction (y). (d) Experimental and fitted infrared reflection spectrum of Mg<sub>2</sub>Al<sub>3.7</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>0.3</sub>Si<sub>5</sub>O<sub>18</sub>-yTiO<sub>2</sub> (y=8.7 wt%). (e-f) The complex dielectric constants in the microwave region.

To advance research into the intrinsic microwave dielectric properties of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> ceramics, their infrared reflectance spectra were analyzed using a classical harmonic oscillator model:

$$\varepsilon^*(\omega) - \varepsilon(\infty) = \sum_{j=1}^n \frac{(z_j e)^2 / m_j V_j \varepsilon_0}{\omega_{T_j}^2 - \omega^2 - i\omega \gamma_j}$$
(8)

The relevant parameters in the above formula are described in detail in the literature <sup>[23]</sup>. The relationship between complex reflectivity permittivity and  $R(\omega)$  can be expressed as:

$$R(\omega) = \left| \frac{\sqrt{\varepsilon^*(\omega)} - 1}{\sqrt{\varepsilon^*(\omega)} + 1} \right|^2 \tag{9}$$

The infrared reflection spectrum can be well fitted with 14 modes in Figure 7 (d). Table S4 (Supporting Information) lists the relevant phonon parameters of Mg<sub>2</sub>Al<sub>3.7</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>0.3</sub>Si<sub>5</sub>O<sub>18</sub>-8.7wt%TiO<sub>2</sub> ceramic. Figure 7(e-f) presents the complex dielectric constants. The theoretical  $\varepsilon_r$  is 5.21 at 15.24 GHz, which is very close to the measured value of 5.68. It has been demonstrated that phonon absorption in the infrared region is the main reason for the dielectric polarization<sup>[24]</sup>.

# 4. Conclusions

In this work, single-phase solid solution ceramics of Mg<sub>2</sub>Al<sub>4-2x</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>2x</sub>Si<sub>5</sub>O<sub>18</sub> ( $0 \le x \le 0.3$ ) were prepared using a traditional solid-state reaction method. The correlation between bond ionicity, lattice energy, bond energy and microwave dielectric properties were analyzed through complex chemical bond theory and the  $\sigma$  values of [Si<sub>4</sub>Al<sub>2</sub>O<sub>18</sub>] six-membered ring. By fitting the infrared reflection spectrum, the theoretical  $\varepsilon_r$  was very close to the measured value. When sintered at 1350 °C, the composition of x=0.15 obtains the best microwave dielectric properties:  $\varepsilon_r = 4.53$ ,  $Q \times f = 150500$  GHz @ 14.5 GHz. The results prove that Zn<sup>2+</sup>-Mn<sup>4+</sup> can effectively improve the quality factor of cordierite ceramics without reducing the temperature stability, while also expanding their sintering range and decreasing their sintering temperature. Finally, temperaturestable composites of Mg<sub>2</sub>Al<sub>3.7</sub>(Mn<sub>0.5</sub>Zn<sub>0.5</sub>)<sub>0.3</sub>Si<sub>5</sub>O<sub>18</sub>-*y*TiO<sub>2</sub> (*y*=0, 1.6, 3.3, 5.0, 6.8, 8.7, 10.6 wt%) ceramics were prepared by two-phase compounding with TiO<sub>2</sub>. When dielectric properties:  $\varepsilon_r = 5.82$ ,  $Q \times f = 47020$  GHz,  $\tau_f = +2.4$  ppm/°C.

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