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#### Highly accurate HF dimer *ab initio* potential energy surface

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A very accurate,  $(HF)_2$  potential energy surface (PES) is constructed based on *ab initio* calculations performed at the CCSD(T) level of theory with an aug-cc-pVQZ-F12 basis set at about 152 000 points. A higher correlation correction is computed at CCSDT(Q) level for 2000 points and is considered alongside other more minor corrections due to relativity, core-valence correlation and Born-Oppenheimer failure. The analytical surface constructed uses 500 constants to reproduce the *ab initio* points with a standard deviation of 0.3 cm<sup>-1</sup>. Vibration-rotation-inversion energy levels of the HF dimer are computed for this PES by variational solution of the nuclear-motion Schrödinger equation using program WAVR4. Calculations over an extended range of rotationally excited states show very good agreement with the experimental data. In particular the known empirical rotational constants *B* for the ground vibrational states are predicted to better than about 2 MHz. *B* constants for excited vibrational states are reproduced several times more accurately than by previous calculations. This level of accuracy is shown to extend to higher excited inter-molecular vibrational states *v* and higher excited rotational quantum numbers  $(J, K_a)$ .

#### I. INTRODUCTION

Recently we published an analysis<sup>1</sup> of a 30 years old rotation-inversion spectrum of the HF-dimer because developments in theory meant that it became possible to retrieve new information from such an old study. In particular we used the variational nuclear motion program  $WAVR4^2$  which employs an exact kinetic energy within the Born-Oppenheimer approximation to make predictions whose accuracy are essentially determined by the quality of the potential energy surface (PES) used. Our study used an accurate ab initio PES due to Huang et  $al.^3$ . One of the demonstrations of the accuracy of this PES is the predictions of the B rotational constants for the ground vibrational state with an accuracy of about 50 MHz. Such accuracy allowed us to assign several new branches of an inversion-rotation submillimeter spectrum originally reported in 1990.<sup>4</sup> However, for many purposes the accuracy achieved by our calculations was still not sufficient. In particular, we could not extrapolate reliably to higher rotational quantum numbers such as K greater than 4, where  $K = K_a$  is the asymmetric top quantum number which gives rise to pronounced sub-bands in the HF dimer spectrum. As a result we could not assign lines belonging to the K=5 sub-band; such lines are yet to be assigned in an HF dimer spectrum. We note as well as submillimeter inversion-rotation spectra,<sup>4,5</sup> very extensive experimental studies of the far infrared (FIR) HFdimer spectrum were performed by Quack and Suhm, see

for example<sup>6–8</sup>. Information on states with K > 4 was not obtained in these FIR publications either. Another limitation on analyzing the inversion-rotation spectrum caused by the accuracy of our calculations is the inability to fix definitive J values to the  $v_4 = 1$  branch newly assigned in<sup>1</sup>.

Thus increased accuracy variational calculations for the HF-dimer spectrum are motivated by the desire to complete the analysis of the 1990 spectrum. However, there is another important motivation for accurate studies of  $(HF)_2$ . The similarity between the HF and water dimers, which was described in detail in our previous study,<sup>1</sup> means one can use the HF-dimer observed minus calculated discrepancies to provide an estimates for the corresponding water dimer discrepancies for calculations performed at a similar level of *ab initio* theory. This is important because the HF dimer is one of the few molecular complexes for which gas-phase high resolution spectra exist which means that observed minus calculated discrepancies can be characterised for the highly excited rotational K states of  $(HF)_2$ . In  $(H_2O)_2$  such states are thought to play a significant but poorly characterized role in absorption the Earth atmosphere<sup>9,10</sup> and, by analogy in the atmospheres water-rich exoplanets.<sup>11</sup> These states of  $(H_2O)_2$  currently cannot be characterized in high resolution experiments. As a consequence the HF dimer discrepancies provide a unique means of characterizing the corresponding discrepancies in water dimer spectra. Hence, a high-level *ab initio* model for the rotation-vibration-inversion (RVI) spectrum of the HF dimer will be an important aid in constructing a similarly accurate mode for the RVI spectrum of the water dimer.

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Let us put the present *ab initio* study of the HF-dimer PES in historical context. In the late 1980s analysis of experimental FIR spectra of the HF-dimer had already been facilitated by variational calculations using both ab *initio* and fitted PESs.<sup>12–15</sup> These calculations achieved an accuracy of few wavenumbers for vibrational levels. The 1990s saw a steady improvement in both ab initio  $\rm PESs^{16}$  and the PESs fitted to the experimental values of the tunneling splittings and vibrational energies.<sup>17</sup> Since then major improvement in the PES was achieved by recent calculations which used many more *ab initio* points to characterise the PES: for example, in the recent paper Huang et  $al.^3$  used 100 000 points, whereas in the 1990s the typical number of *ab initio* points per PES was about 3000. Below we show that this increased number of points is important for fully characterizing the PES. At the same time the step-up in the basis from aug-ccpvTZ<sup>12</sup> to aug-cc-pvQZ<sup>3</sup> resulted in important improvements in of the accuracy of the corresponding PES.

However, modern computer power and quantum chemistry software (such as MOLPRO<sup>18</sup> and MRCC<sup>19</sup> used in this work) can provide improvements in *ab initio* theory. In particular, developments have made feasible the use of the explicitly correlated F12 level of theory<sup>20</sup> and inclusion of increased correlation in coupled cluster (CC) calculations from CCSD(T) to CCSDT(Q) and even higher where S means single excitations, D double, T triple and Q quadruple, and the parentheses denote a perturbative treatment. Minor corrections such as those for the corevalence electron correlation, higher-order electron correlation, scalar relativistic effects, as well as the diagonal Born-Oppenheimer correction can also be considered.

The choice of both the level of *ab initio* theory for the base PES and for the various corrections depends on the several factors. One is the time taken for calculation of a single point. Another factor is the coordinate dependence of the correction on the coordinates. In particular, it is possible to quantify the difference between the corrections at some special points, such as dissociation, saddle point, or linear configuration point, and its values at the equilibrium point. In general, the larger such a difference is, the larger is the influence on the RVI levels due to this correction. An important point to consider here is the possible cancellation of errors. Clearly it is not possible to expect that calculations on such a large system will give complete convergence for the resulting PES. It is much more realistic to aim for a so-called Pauling point,<sup>21,22</sup> where a good result is obtained due to judicious exploitation of cancellation of errors.

An important part of our *ab initio* study is comparison of our results with the experimental values. Although a direct comparison is impossible, the use of the resulting PES in the variational solution of the nuclear-motion Schrödinger equation produces predictions which can be directly compared with experiment. However, practically all the previous studies were limited to rotationless (J = 0) calculations so that comparisons could only be made with vibrational term values. There is a dearth of high resolution experimental data on vibrational term values for (HF)<sub>2</sub>. In many cases only approximate extrapolated empirical values are available, see table I of<sup>1</sup>. Here we use variational program WAVR4<sup>2</sup> to compute J > 0 energy levels of the HF-dimer. These calculations provide us with the B and  $\Delta_K$  (the K-dependence of the tunneling splitting, see the Eq. (1) below), values which can be directly compared with ones obtained from high resolution experiments. The value of B and  $\Delta_K$  are defined for example in the Refs.<sup>1,4</sup> and are determined from the experimental frequencies using the equation

$$E(J, K, \nu) = \Delta_K \delta_{\nu, 1} + F_K + B_J^{\nu} J(J+1) - D_J^{\nu} J^2 (J+1)^2 + H_J^{\nu} J^3 (J+1)^3.$$
(1)

In this paper we present *ab initio* calculations for the  $(HF)_2$  PES and the variational calculations of J = 0 and excited J states alongside comparison of our results with the experimental data. Section II describes the electronic structure calculations and Section III presents the variational nuclear motion calculations. The comparisons between our results and observations are analysed in the section IV. Section V describes resonances between high K levels with section VI giving results for DF dimer. Section VII presents our conclusions.

# II. AB INITIO CALCULATIONS OF THE HF-DIMER PES

We used the MOLPRO package to calculate 152 000 points on the HF-dimer PES using the CCSD(T)-F12b method with the aug-cc-pVQZ-F12 basis set, denoted F12QZ below. The use of explicitly correlated MP2 and CCSD(T) methods for the HF dimer was discussed already by Klopper et al.<sup>23</sup> In particular, the binding energy  $D_e$  of the HF dimer was obtained, using the CCSD(T)-R12 method with the quadruple/quintuplezeta quality basis set, to be 1610 and 1585  $\rm cm^{-1}$  without and with the counterpoise correction, respectively. The basis sets used in this study were significantly larger. At the highest level of theory applied here, CCSD(T)-F12b/aug-cc-VQZ-F12, the basis set superposition error (BSSE) for  $D_e$  is calculated to be just 1.9 cm<sup>-1</sup>. It is by the order of magnitude smaller than that of  $25 \text{ cm}^{-1}$  reported by Klopper et al.<sup>23</sup> The decision to calculate the PES at this level of theory was taken after the series of tests described in the following subsection.

#### A. Tests of the accuracy of *ab initio* calculations

To test the accuracy of *ab initio* calculations, four special points on HF-dimer PES were chosen. These are: the *trans* equilibrium configuration of  $C_s$  symmetry (E), the saddle point of  $C_{2h}$  symmetry (S), the linear HF– HF configuration (L), and the separated HF molecules at the dissociation limit (D). The total energies of the

TABLE I. Total energies of the HF dimer calculated at four special points (see text for details) at the CCSD(T)/aug-cc-pVnZ and CCSD(T)-F12b/aug-cc-pVnZ-F12 levels of theory. The energies quoted for the points S, L, and D are relative (in  $\text{cm}^{-1}$ ) to the total energy determined at the point E (given in Hartree).

point	n = T	$n = \mathbf{Q}$	n = 5	n = 6	n = 7		
CCS	D(T)/aug-cc	$-\mathbf{p}\mathbf{V}n\mathbf{Z}$					
Е	-200.706849	-200.762297	-200.780678	-200.786923	-200.789879		
$\mathbf{S}$	372.1	374.7	365.2	351.9	344.3		
L	367.6	354.0	343.4	339.4	342.5		
D	1689.0	1652.4	1627.3	1611.5	1602.0		
CCSD(T)-F12b/aug-cc-pV $nZ$ -F12							
Е	-200.781707	-200.791485					
S	353.1	341.7					
L	341.1	341.8					
D	1613.5	1601.6					

HF dimer calculated using the conventional CCSD(T) and explicitly correlated CCSD(T)-F12b methods with various basis sets of increasing quality are given in Table I. The structures of the HF dimer at each of these points were optimized at the corresponding level of theory.

As can be seen, the best results obtained using the conventional and explicitly correlated CCSD(T) methods are very similar. In particular, the dissociation energy of the HF dimer is converged to better than 10 cm<sup>-1</sup> at both the CCSD(T)/aug-cc-pV7Z and CCSD(T)-F12b/aug-cc-pVQZ-F12 levels of theory. Considering the computer resources involved in the calculations, the explicitly correlated method CCSD(T)-F12b with the aug-cc-pVQZ-F12 basis set seems to be the best choice for predicting the PES of the HF dimer; these calculations are denoted F12QZ below.

As a next step, we considered the possible corrections to the total energy of the HF dimer. These were:

- 1. The core-valence electron correlation correction (CV6) determined as a difference in the total energies calculated at the CCSD(T)/cc-pCV6Z level of theory and correlating either only valence or all electrons;
- 2. The first higher-order correlation correction (PQT) determined as a difference in the total energies obtained with the CCSDT(Q) and CCSD(T) methods, both with the aug-cc-pVTZ basis set;
- 3. The second higher-order correlation correction (PPD) determined as a difference in the total energies obtained with the CCSDTQ(P) and CCSDT(Q) methods, both with the aug-cc-pVDZ basis set;
- 4. The scalar relativistic correction (X2C) determined as a difference in the total energies calculated using either the exact-2-component<sup>24</sup> or nonrelativistic Hamiltonian at the CCSD(T)/aug-cc-pV5Z level of theory;

5. the adiabatic correction (DBOC) calculated at the CCSD/aug-cc-pCVTZ level of theory.

The total energy correction values calculated at the four special points of the HF dimer PES are given in Table II. The total sum of the corrections is given in the last column headed "sum".

For the four special points E, S, L, and D, the total corrections appeared to be nearly the same, being different from each other by at most 41  $\mu$ hartree (9.0 cm<sup>-1</sup>). At all of these points, the second higher-order correlation correction (PPD) were found to be by about one order of magnitude smaller than the other corrections. Given its very high computational cost, this correction was therefore not further considered.

#### B. CCSD(T)-F12 ab initio calculations

Our test of the level of quantum chemistry theory, described in the previous subsection, allowed us to conclude that the basic PES with comprising more than 100 000 points should be calculated using the F12QZ level of theory. The corrections to this PES, which make much smaller contributions, could be adequately represented using a much less dense grid of about 2000 calculated points. These conclusions are supported by the predictive power of both the basic PES and the corrections, as described below.

As the computer cost of one F12QZ calculation using MOLPRO<sup>18</sup> is quite modest, we decided to compute 152 000 points to represent the basic PES. The grid was chosen so that every point should obey restrictions in energy (estimated using the PES of Huang *et al.*<sup>3</sup>), range of geometries, and number of points. We used several sets of points; all points calculated lie in the range  $1.4 \le r_{1,2} \le 2$  $a_0$ , where  $r_1$  and  $r_2$  are the HF bondlengths, and  $3 \le R \le$ 9  $a_0$ , where R is the HF – HF center-of-mass separation, with no restriction on the angles. Set 1 comprised a basic grid of 98 981 points, with  $E \leq 3000 \text{ cm}^{-1}$ , where E = 0is taken to be the minimum on the PES; this set provides coverage for the higher energies; Set 2 comprised 9 199 points with  $E < 900 \text{ cm}^{-1}$  chosen to increase the accuracy of the calculation of the lower-lying energy levels; Set 3 comprised a 731 points with  $E \leq 4 \text{ cm}^{-1}$  to provide particularly accurate calculation of the minimum potential

TABLE II. The total energy correction values (in milihartree) for the HF dimer calculated at the four special points (see Table I).

point	CV6	PQT	PPD	X2C	DBOC	sum
Е	-129.805	-0.596	0.078	-174.219	5.668	-298.874
$\mathbf{S}$	-129.791	-0.601	0.079	-174.231	5.674	-298.870
L	-129.818	-0.579	0.074	-174.208	5.671	-298.859
D	-129.777	-0.576	0.075	-174.243	5.689	-298.833

energy, which is useful for calculating the dissociation energy; Set 4 comprised 42 932 with points  $E < 1500 \text{ cm}^{-1}$ which were not used in the main fit. Set 4 provides only a check on the accuracy of the PES fits determined by the original points. The four regions of space bounded by the energy and geometric parameters were filled with points in the form of a regular, irregular, or random (as in our case) grids. Geometries were generated using standard FORTRAN function RANDU six times to generate random numbers  $ra_{1..6}$  in the range  $0 \leq ra_{1..6} \leq 1$ , giving  $r_{1,2} = 1.4 + 0.6ra_{1,2}$ ,  $R = 3 + 6ra_3$ , and  $\theta_{1,2}$ ,  $\phi =$  $180ra_{4,5,6}$ . We use this random procedure to generate grids with energies below 3000, 900 and 1500  $\mathrm{cm}^{-1}$ . But the grid below  $4 \text{ cm}^{-1}$ , near the equilibrium, was used a regular mesh comprising  $3 \times 3 \times 3 \times 3 \times 3 \times 3 = 729$  points with  $r_{1,2} = 1.742, 1.743, 1.744, R = 5.124, 5.134, 5.144,$  $\theta_1 = 7.17^{\circ}, 8.17^{\circ}, 9.17^{\circ}, \ \theta_2 = 66.712^{\circ}, 67.712^{\circ}, 68.712^{\circ},$  $\phi = 178.0^{\circ}, 179.0^{\circ}, 180.0^{\circ}.$ 

### C. The fit of the CCSD(T)-F12 PES *ab initio* points to the analytical surface

The 152 000 points of the CCSD(T)-F12 surface were fitted as follows. First we fitted these points to a 6D surface in polynomial form. We knew that it would be not a simple undertaking to fit such a complicated surface, however we wanted to see what quality of the fit could be obtained this way. The result was the 6D surface with plenty of holes and several  $cm^{-1}$  standard deviation between the *ab initio* points and the analytical form. As shown in our previous study,<sup>1</sup> the quality of the PES due to Huang  $et al.^3$  is very high, as the discrepancies parameters calculated using this *ab initio* PES and the experimental data are small. This should mean that the difference between the PES of Huang et al. and the ab initio points computed in this work should also be small. Indeed, the deviation of our points from the PES of Huang et al. turned out to be not more than 30  $\text{cm}^{-1}$  so an alternative method of fitting can be used. We decided to fit not the points themselves directly, but rather to represent their difference from the PES of Huang et al.. This reduces the dynamic range of the problem from approximately  $1500 \text{ cm}^{-1}$  to  $30 \text{ cm}^{-1}$ . Since the coordinate dependence of these differences turned out to be smooth, a significant improvement in the standard deviation of the fit could be obtained.

To ensure the best possible representation in the critical region near equilibrium we used different weights in the fit for points depending on their energy above equilibrium. Points with E below 900 cm<sup>-1</sup> were given unit weights. For higher points this weight was decreased exponentially: it was halved for every 100 cm<sup>-1</sup> increase in E above 900 cm<sup>-1</sup>. Inspired by the experience of Huang *et al.*, we similarly did not use angles as variables to define the surface. Instead, they took 6 bond lengths:  $H_1F_1$ ,  $H_2H_1$ ,  $F_2H_1$ ,  $H_2F_1$ ,  $F_2F_1$ ,  $H_2F_2$  and then used symmetrized coordinates:

$$S_{ms} = H_1 F_1 + H_2 F_2 - 2r_{meq}$$

$$S_{ma} = H_1 F_1 - H_2 F_2$$

$$S_h = H_2 H_1 - r_{heq}$$

$$S_{ds} = H_1 F_2 + H_2 F_1 - 2r_{deq}$$

$$S_{da} = H_1 F_2 - H_2 F_1$$

$$S_f = F_2 F_1 - r_{feq}$$
(2)

where  $r_{meq}$  is average monomer equilibrium distance,  $r_{heq}$  is HH equilibrium distance,  $r_{deq}$  is the average of  $H_1F_2$  and  $H_2F_1$  distances at equilibrium configuration and  $r_{feq}$  is FF equilibrium distance. Coordinates  $S_{ms}$ ,  $S_h$ ,  $S_{ds}$  and  $S_f$  are symmetric under inversion. The asymmetric coordinates,  $S_{ma}$  and  $S_{da}$ , only contribute to the potential through even powers or mixed terms containing the product  $S_{ma}S_{da}$ . With these simplifications in mind, the first fit used the functional form

$$V = \sum p_{i_{1..6}} S^{i_1}_{ms} S^{i_2}_{ma} S^{i_3}_h S^{i_4}_{ds} S^{i_5}_{da} S^{i_6}_f \tag{3}$$

where powers  $i_1$ ,  $i_2$ ,  $i_3$ ,  $i_4$ ,  $i_5$ ,  $i_6$  are non-negative integers, and satisfy  $i_1+i_2+i_3+i_4+i_5+i_6 \leq O$ , where O is the maximal order of the fit, and we set fifth-order (O = 5) in all fits. Our initial fits showed large correlation of 0.987 between the first order terms in the potential expansion, which spoilt the fit and led to a rather inaccurate description of the points: a standard deviation of 4.3 cm<sup>-1</sup>. However, this problem was circumvented by transforming to decorrelated coordinates for the fit:

$$S'_{ms} = S_{ms}$$

$$S'_{ma} = S_{ma}$$

$$S'_{h} = S_{h} + S_{ds}$$

$$S'_{ds} = S_{h} - S_{ds}$$

$$S'_{da} = S_{da}$$

$$S'_{f} = S_{f}$$

$$(4)$$

the use of uniformly weighted points gave a surface describing all points with the standard deviation  $0.5 \text{ cm}^{-1}$ . This fitted potential was supplemented by the long-range interaction at long terms given by Huang *et al.*; we call the result PESp, or PES polynomial. Use of PESp shows improved predictions of spectroscopic parameters compared to the original PES of Huang  $et al.^3$  which already allows us to improve our predictions and identification of experimental spectra. However, inspection of PESp showed that it was not as accurate as the quality of the fit would suggest as new points not used in fit were found to deviate from from it by  $2.4 \text{ cm}^{-1}$ , which provides a more realistic assessment of the quality of the surface than the standard deviation. The polynomial form of the potential itself leads to divergences at large separations, where physically the potential should approach a constant value.

To circumvent this problem, Morse coordinates were used instead of simple combinations of distances. Even

$$S_{ms}'' = 2 - e^{-\alpha_m(H_1F_1 - r_{meq})} - e^{-\alpha_m(H_2F_2 - r_{meq})}$$

$$S_{ma}'' = -e^{-\alpha_m(H_1F_1 - r_{meq})} + e^{-\alpha_m(H_2F_2 - r_{meq})}$$

$$S_h = 1 - e^{-\alpha_d(H_1H_2 - r_{heq})}$$

$$S_{ds}'' = 2 - e^{-\alpha_d(H_1F_2 - r_{deq})} - e^{-\alpha_d(H_2F_1 - r_{deq})}$$

$$S_{da}'' = -e^{-\alpha_d(H_1F_2 - r_{deq})} + e^{-\alpha_d(H_2F_1 - r_{deq})}$$

$$S_{f}'' = 1 - e^{-\alpha_d(F_1F_2 - r_{feq})}$$
(5)

where  $\alpha_d = 0.25$  and  $\alpha_m = 1.05$ . To increase stability of Morse-fit we have to introduce damping of high-order terms in the potential:

$$V'' = \sum p_{i_{1..6}}'' A_i'' S_{ms}''^{i_1} S_{ma}''^{i_2} S_d''^{i_3} S_{da}''^{i_4} S_d'^{i_5} S_f''^{i_6}$$
(6)

where  $A_i$  depends on the order of the term.  $A_0 = A_1 = A_2 = 1$ , while  $A_3=0.3$ ,  $A_4=0.1$ , and  $A_5=0.03$ . Now the points are reproduced with a standard deviation of 0.3 cm<sup>-1</sup>. Exponential weighting overcomes fitting instability in the high order terms. Of course, from a mathematical point of view, we could just replace  $p \times A$  by p' in the final equation. But the  $p \times A$  form demonstrates fitting process, where we have to damp high orders. Probably it would be preferable not to damp the coefficients, but we tested finite difference fitting of high order terms, and obtained the same result. However, this approach is more complicated to code.

The accuracy of the fitted PES is  $0.3 \text{ cm}^{-1}$ . For this fit which we call PESm, or PES Morse, the approximately 43 000 new points calculated at random geometries are predicted by this surface with the same accuracy of  $0.3 \text{ cm}^{-1}$ . Therefore PESm provides a better representation of the F12QZ *ab initio* calculations and is the surface we use below.

In summary, the polynomial fit was chosen as the easiest way to obtain a PES. But the polynomial function has poor extrapolation properties. To get around this problem, we did not fit the full potential, but fit only the difference between our high-precision corrections and the base surface of Huang *et al.*.<sup>3</sup> Therefore, formally, all the PESs obtained in this paper are only corrections to the base surface. For comparison, when using Eq. (6), the total energy fit was performed without subtracting the base surface. In this case, the standard deviation of the points from the resulting surface was  $4 \text{ cm}^{-1}$  that is, the quality of the fit was an order of magnitude worse than using the base surface. We call this potential PESd and will use it below for the Zero Point Energy (ZPE) calculations.

Since the representation of the *ab initio* points by PESm and PESp is an order of magnitude better than PESd, we use these potentials for the further calculations. Morse coordinate representations have the advantage of behaving physically at large distances. That is why the PESm fit represents the points better than the PESp fit, and that is why the Eq. (6) was chosen to represent all subsequent corrections. Our correction surfaces do not change the long-range behavior of the base potential. The base potential itself consists of a short-range potential and a long-range potential, between which switching occurs at intermediate values of the dimer bond length. We add the correction surface not to the entire base potential, but only to its short-range part; the long-range potential and the switching function are left the same as Huang *et al.*.<sup>3</sup>

## D. CCSDT(Q), Core-valence, DBOC and relativistic correction surfaces fit

We sorted corrections by the magnitude of their effect on the rovibrational levels; below we use the terms "biggest" and "smallest" to refer this ordering. The biggest correction to the F12QZ PES come from the higher correlation contribution estimated at the CCSDT(Q) level. Even though it is the biggest correction, it is only a few  $cm^{-1}$  in magnitude, and variations with the change of geometry are small in comparison with the whole PES. This means that fewer points are needed to characterize it which compensate for the fact that CCSDT(Q) levels calculations take significantly more time per point. We computed 2000 points, which we fitted with a standard deviation of  $0.02 \text{ cm}^{-1}$  with 150 parameters using the Morse form Eq. (6), described in the previous subsection. That 2000 points are sufficient to characterize this smoothly varying surface was confirmed by comparison with an 500 calculated points not included in the fit. These randomly chosen points are reproduced with a standard deviation of  $0.13 \text{ cm}^{-1}$ , which means, that our fitted analytical correction PESC gives a good representation of the whole correction surface.

An even higher quality fit was obtained for the fits of the DBOC, relativistic and core-valence correlation corrections. The DBOC correction was fitted with an accuracy standard deviation of  $0.0078 \text{ cm}^{-1}$ , the relativistic correction was fitted to  $0.0082 \text{ cm}^{-1}$ , whole the core-valence correction resulted in a standard deviation of  $0.0075 \text{ cm}^{-1}$ . Tests of the quality of predictions using random unfitted points gave similar results to the CCSDT(Q) correction case (designated as PQT in Table II). The higher correlation correction CCSDTQ(P) contribution to the four test geometries used in the section IIA is very small and we did not calculate the surface corresponding to this correction. All the analytical correction surfaces, described in this section are given in the supplementary material ("pot.rar" archive).

TABLE III. Quality of the PES fit as a function of n, the number of points used in the fit.  $\operatorname{rms}_n$  is the accuracy of a fit, and  $\operatorname{rms}_{N-n}$  the accuracy with which the fit reproduces the remaining points N - n, where N is the number of all points calculated in this work.

n	$\mathrm{rms}_n$	$\mathrm{rms}_{N-n}$
1000	0.38	0.63
3000	0.38	0.41
5000	0.37	0.39
10000	0.38	0.38

#### E. PES quality estimation

To aid future calculations including ones on the water dimer, it is necessary to understand how the quality of the PES depends on the number of points used to fit the surface. We therefore checked how the accuracy of the surface depended on the number of points used for its determination. Out of a total of 152 000 *ab initio* points, only a portion of them were randomly selected, and only selected points were used to fit the test surface. The quality of the test surfaces was checked by how accurately this surface reproduces the *ab initio* points not included in the fit. The results of this check are shown in the Table III, which shows that 3000 points is enough to predict points with an accuracy, close to the fit accuracy. For 10 000 points, accuracy of the prediction and the fit become indistinguishable to two significant figures.

#### III. VARIATIONAL CALCULATIONS OF HF DIMER TUNNELING ROTATION VIBRATION ENERGY LEVELS

Variational calculations of excited rovibrational tunneling levels energy of the HF dimer are performed using the PESp, PESm+PESc+PEScv6, PESm, PESm+PESc, PESm+PESc+PEScv6+PESrel,

PESm+PESc+PEScv6+PESrel+PESdboc potenials. Nuclear motion calculations were performed with WAVR4<sup>25,26</sup>. Two basis sets were used: BIG  $(r_e=1.03 \text{ Å}, w_{er}=7500 \text{ cm}^{-1}, n_r=10, R_e=7.7 \text{ Å}, w_{eR}=16 \text{ cm}^{-1}, n_R=90, l_{max}=20, k_{max}=6)$  and SMALL  $(r_e=0.95 \text{ Å}, w_{er}=7500 \text{ cm}^{-1}, n_r=8, R_e=2.7 \text{ Å}, w_{eR}=300 \text{ cm}^{-1}, n_R=20, l_{max}=15, k_{max}=4)$ , where  $r_e$ ,  $w_{er}$ , and  $n_r$  are HF Morse-like oscillator basis set parameters: equilibrium distance, equilibrium frequency and a number of integration points respectively,  $R_e$ ,  $w_{eR}=16$  and  $n_R$  are basis set parameters for monomers canter of mass vibration,  $l_{max}$  determines sizes of  $H_1F_1F_2$  and  $H_2F_2F_1$  bending basis sets and  $k_{max}$  gives the size of  $H_1F_1-H_2F_2$  internal rotation basis set.<sup>25,26</sup> We used the BIG basis set for accurate calculation and the SMALL one for calculating quick estimates.

To calculate rotationally excited energy levels of the  $(HF)_2$  molecule, it is enough to set the values of the pa-

rameters  $J_{\text{max}} = 9$  and  $K_{\text{max}} = 9$  in the WAVR4 input file. We also had to increase from 10 to 500 the maximum number of levels written out by the program for each symmetry at the fourth stage when J > 0 energy levels are calculated. The published version of WAVR4 was generalized to allow calculations with J > 9. Additionally, for calculations  $9 < J \leq 20$ , the angular vibrational basis set rotational momentum parameter  $l_{max}$  had to be increased from 16 to 20. The final ro-vibrational calculations involved diagonalisation of a Hamiltonian matrix of dimension 40(J+1). This was sufficient to converge the energy levels of interest to better than  $0.1 \text{ cm}^{-1}$ . Relative convergence of the neighboring-J levels is much better and, in particular, B constants are converged to better than 1 MHz. Our  $(HF)_2$  vibrational-rotational energy levels with  $J \leq 9$  are given in file "rvenergies.txt" of the Supplementary Materials.

#### IV. RESULTS

Here we compare the results of our variational calculations to all known experimental data. In particular, we compare our calculations with the experimental dissociation energy, (Table IV); experimentally measured and empirically extrapolated (indirectly determined) values of the inter-molecular band origins (Tables V); experimentally derived J = 0 excited K energy levels (Table VI); tunneling splittings (Table VIII); finally the most numerous experimental data are the rotational B constants for the ground and excited vibrational states with K=0 and excited K > 0 states, which are compared in the Table IX. We consider each item in turn.

#### A. Dissociation energy

We start with the comparison of HF dimer dissociation energy which has been measured experimentally<sup>28</sup> and is calculated here using our basic PES and various corrections. Table IV compares various calculations of the dissociation energy of the HF dimer including the two most recent *ab initio* calculations due to Huang *et al.*<sup>3</sup> and Řezáč and Hobza<sup>27</sup>, and our *ab initio* calculations.

The zero-point energy (ZPE) correction to the dissociation energy is calculated as the difference  $E_{\rm ZPE}^{\rm HFHF} - 2 * E_{\rm ZPE}^{\rm HF}$ , where  $E_{\rm ZPE}^{\rm HFHF}$  is the total ZPE of the (HF)<sub>2</sub> molecule and  $E_{ZPE}^{\rm HF}$  is the HF monomer ZPE of 2050.5 cm<sup>-1</sup> which was obtained from calculations with HF potential energy curve from<sup>29</sup>. We computed the ZPE using different PESs and their ZPE values differ from each other by about 40 cm<sup>-1</sup>. We managed to converge the ZPE calculations using two PESs - 1)PESd and 2) PES from paper<sup>23</sup>. For our final calculations we decided to take the PESd because the ZPE determination using PESm and PESp failed to converge properly in our ZPE calculations. We intend to consider the issue

TABLE IV. Calculations of the HF dimer dissociation energy, in  $cm^{-1}$ , with different PESs.

		This	Ref.[ 27]	Ref.[3]	Ref.[ 17]	Ref.[ 23]	Ref.[ 28]
		work	(ab initio)	(ab initio)	(SQSBDE)	(GSC-2.9)	Experiment
$D_e$		1601.6	1611.68	1573.50	[1559.3]	[1598.31]	
ZPE		544.88	566.61	535.98	[497.3]*	$[536.58]^*$	
Cor	rections	to CCS	D(T) PES	$\mathbf{D}_e$ value			
	CV6	6.07					
	PQT	4.42	3.15				
	PPD	-0.76	-0.35				
	X2C	-5.28	-5.60				
	DBOC	4.45	4.20				
	deform.		-9.79				
	total	8.90	-8.39				
$\mathbf{D}_0$		1065.62	1036.68	1037.51	1062	1061.73	1061.86

\* Value obtained as difference between  $D_e$  and  $D_0$ .

Headings are:

D<sub>e</sub>: the best estimate of the binding energy, including the corrections listed below;

ZPE: the zero-point energy;

 $D_0$ , the dissociation energy;

CV6 = CCSD(T)/cc-pCV6Z, core-valence corrections; PQT = CCSDT(Q)-CCSD(T)/aug-cc-pVTZ and PPD = CCSDTQ(P)-CCSDT(Q)/aug-cc-pVDZ, higher-order correlation corrections,;

X2C = CCSD(T)/aug-cc-pV5Z, scalar relativistic correction; DBOC = CCSD/aug-cc-pCVTZ, adiabatic correction.

of ZPE convergence for different potentials in the subsequent studies. For completeness we also present the  $D_0$  values obtained by Quack and Suhm<sup>17</sup> and Klopper, Quack and Suhm<sup>23</sup> whose PESs rely on fits to experimental HF dimer spectra and who used the measured  $D_0$ as part of their fits. It should be noted that Řezáč and Hobza<sup>27</sup> use one extra correction, the deformation energy, which was evaluated as the difference between the energy of fully optimized monomers and monomers in the geometry taken from the dimer. We do not require explicit inclusion of this correction as our calculations includes this difference already because we perform full 6-D calculatioms, which include the monomer vibrational motions.

#### B. Intramolecular vibrations

Table V gives our results for the four inter-molecular band origins. Among all the experimental data these are the least accurate, as none of them have been directly observed experimentally; the values presented were extrapolated from the other measurements. Since the accuracy of such these extrapolations is not very high, our results for all the PESs considered are more or less within the experimental uncertainty and this table does not help to characterize the relative accuracy of the different PESs.

More accurately determined and derived directly from high resolution experiments are the energies of the excited K levels belonging to the ground and floppy excited vibrational states presented in the Table VI. In this case the M columns - the calculations using the basic F12QZ PES fitted with the Morse coordinates (denoted as 'M' in tables V,VI,VII,VIII,IX) and K column - the calculations of the levels using this surface plus the core-valence correction, clearly give better agreement with the observations than the other columns. The agreement to about one wavenumber can be compared with differences of up to 4 cm<sup>-1</sup> given in column p1 which used the PES of Huang *et al.*<sup>3</sup>. Similar improvement can be seen in Table VIII, which compares calculations of the experimentally determined tunneling splitings for different *v* and *K* states.

TABLE V. Empircal inter-molecular vibrational band origins obtained by extrapolation and (obs. - calc.) values in cm<sup>-1</sup>. Uncertainties in units of the final digit are given in parenthesis. See Table IX for a description of the column headings.

	extrapolated	p1	Р	Μ	Κ	CV	DBOC	pall
$\Delta_{K=0}$	$0.6587(1)^{\rm a}$	-0.020	-0.014	-0.010	-0.029	-0.003	-0.020	-0.019
$\nu_4$	$125.1(1)^{\rm b}$	0.2	-0.4	-1.1	-1.3	-1.6	-1.6	-1.7
$\nu_5$	$160.6(6)^{\rm b}$	-2.1	-3.5	-4.2	-4.4	-4.8	-4.8	-4.9
$\nu_6$	$395(8)^{c}$	-18.1	-21.4	-22.2	-22.2	-23.7	-23.3	-23.4
$\nu_6$	$420(5)^{d}$	6.9	3.6	2.8	2.8	1.3	1.7	1.6
$\nu_3$	$475(3)^{c}$	-5.5	-7.0	-10.1	-10.8	-11.4	-11.1	-11.4
$\nu_3$	$480(10)^{d}$	-1.8	-2.0	-5.1	-5.8	-6.4	-6.1	-6.4

<sup>a</sup> Ref. [7]

<sup>b</sup> Ref. [ 30] <sup>c</sup> Ref. [ 31]

<sup>d</sup> Ref. [23]

1ten [ 20]

TABLE VI. Experimentally-determined band origins with K > 0 and (obs. - calc.) values in cm<sup>-1</sup>. See Table IX for a description of the column headings.

$(v_3v_4v_5v_6)$	obs.	p1	Р	Μ	Κ	$\mathrm{CV}$	DBOC	pall
(0000) K = 1	$35.4^{\mathrm{a}}$	-1.0	-0.6	-0.5	-0.2	-0.5	-0.3	-0.3
(0010) K = 1	$36.5^{\mathrm{a}}$	1.1	-0.6	-0.6	-0.3	-0.5	-0.3	-0.3
(0000) K = 2	$116.1^{\mathrm{a}}$	-1.9	-1.3	-1.1	-0.5	-1.1	-0.7	-0.8
(0010) K = 2	$118.1^{\mathrm{a}}$	-1.9	-1.2	-1.0	-0.4	-1.0	-0.6	-0.7
(0000) K = 3	$232.6^{\rm a}$	-2.7	-2.1	-2.0	-1.1	-2.1	-1.5	-1.6
(0010) K = 3	$236.5^{\mathrm{a}}$	-2.9	-2.1	-1.9	-1.0	-2.0	-1.4	-1.5
(0010) K = 4	$386.7^{\rm a}$	3.8	-3.2	-3.0	-1.9	-3.3	-2.5	-2.7
(0020) K = 3	$393.6^{\rm b}$	0.5	-2.1	-1.6	-1.3	-3.3	-2.3	-2.7

<sup>a</sup> Ref. [7]

<sup>b</sup> Ref. [ 32]

#### C. Rotational B constants

Table IX presents values for our calculated B rotational constants. For convenience and completeness Table IX also presents predicted values for K = 5 of the (0000) and (0010) states. Rotational constants were obtained from the calculated energy levels values by fitting J=K levels up to J=9. From Table IX it can be seen

TABLE VII. Representation of the difference between neighboring levels, leading to the resonances between closely lying states. Difference between levels with J = K and K=3, 4, 5 of (0000) and (0010) tunneling states in cm<sup>-1</sup>. E(p1) is the energy of the level under study calculated in<sup>1</sup>, the following columns show the distance between the neighboring levels with above and below the studied level; Table IX for a description of the other column headings.

level	E(p1)	p1	Р	Μ	Κ	$\mathrm{CV}$	DBOC	pall
		4.6	3.2	2.8	2.1	2.5	2.1	2.1
K=3 (0000)	235.3							
		3.9	3.8	3.7	3.8	3.7	3.7	3.7
K=3 (0010)	239.3							
		5.7	8.3	9.6	10.7	10.7	11.1	11.2
		4.2	3.8	2.9	2.4	2.5	2.4	2.4
K=4 (0000)	383.1							
		0.5	2.9	4.5	5.5	5.8	6.0	6.0
		3.8	4.2	2.6	1.6	1.2	1.0	1.0
K=4 (0010)	387.3							
		1.2	0.4	2.4	3.6	3.9	4.2	4.2
		5.9	3.3	0.6	1.0	0.4	0.1	0.4
K=5 (0000)	557.8							
		2.7	3.6	6.4	6.9	6.4	6.8	6.9
		4.1	1.2	1.7	0.8	0.4	0.03	0.03
K=5 (0010)	571.6							
		0.6	2.9	1.0	2.3	2.5	2.7	2.7

TABLE VIII. Measured tunneling splittings of HF dimer band origins and (obs. - calc.) values in cm<sup>-1</sup>. See Table IX for a description of the column headings.

$(v_3v_4v_5v_6)$	$\operatorname{Exp.}^7$	p1	Р	М	Κ	CV	DBOC	pall
$(0000) \ K = 0$	0.659	-0.020	-0.014	-0.010	-0.029	-0.003	-0.020	-0.019
(0000) K = 1	1.064	-0.063	-0.035	-0.030	-0.051	-0.018	-0.038	-0.032
(0000) K = 2	2.004	0.003	0.085	0.095	-0.070	0.122	0.095	0.108
(0000) K = 3	3.813	-0.123	0.049	0.070	-0.046	0.124	0.090	0.120
(0000) K = 4	7.123	-0.384	-0.024	0.025	0.023	0.141	0.105	0.158
(0100) K = 0	3.152	0.195	0.310	0.212	0.105	0.207	0.146	0.169

that the values of the ground state B constants taken from experiment<sup>4</sup> and our variational calculations coincide within a few MHz for the ground vibrational state for both K=0 and excited K levels. The improvement in comparison with the B constants calculated with the PES of Huang *et al.*<sup>3</sup> is dramatic - about an order of magnitude.

Less satisfactory is our description of the precisely tuned resonances of the states K = 4. The discrepancy between the calculated *B* constant in the K=4 (0000) state with its observed value is up to 67 MHz for the PESs tested. We discuss this disagreement in the following subsection.

#### V. RESONANCES INVOLVING K = 3, 4, 5

The resonances which distort the values of the B constants are described for K=3 by Quack and Suhm<sup>32</sup> and our previous study.<sup>4</sup> The major factor causing an energy level to be affected by resonance is the closeness of neighboring levels with the same J and symmetry. Table VII shows the distance between the K=3, 4, 5 levels of the (0000) and (0010) vibrational states and neighboring levels above and below the levels in question. The close positions of the interacting levels which move the energy levels of the K = 3 (0000) branch have been noted previously<sup>1</sup> and are shown in the Table VII. The B constants for the K = 0 - 5 (0000) and (0010) vibrational states presented in Table IX display different behavior for different vibrational states. In the (0010) state the rotational constants increase monotonically with K, but the B values with K > 2 in the ground vibrational state show unusual behavior.

E(p1) given in Table VII is the energy of the levels of ground vibrational state for two tunneling states: (0000) and (0010). The lines above and below these levels give the difference in energy between this level and its neighboring levels with the same J and symmetry lying directly below and above the level in question as these are levels which participate in resonance interactions. The separation between the K = 3 (0000) level and its neighbor lying lower in energy K = 1 (0030) is about 2.5 cm<sup>-1</sup> on average for the different levels of theory. The separation of the K = 3 (0010) level from K = 0 (0200)higher neighbour is about  $10 \text{ cm}^{-1}$  on average. Thus the lower level lies much closer and the K = 3 (0000) level is affected by a resonance with K = 1 (0030) branch of levels. For both K = 5 (0000) and (0010) levels there are neighboring levels as close as  $0.03 \text{ cm}^{-1}$  which occur in different calculations in an unsystematic way. These resonance interactions significantly distort the values of the B constants of the affected levels, which makes it impossible to estimate the values of rotational constants for the K = 5 states from the levels with lower K values of (0000) and (0010) vibrational states without including proper allowance for these resonances.

#### VI. DF DIMER

We also checked the quality of our new PES on calculation of DF dimer levels. If, to calculate the energy levels of the (DF)<sub>2</sub> molecule, we use the same parameters for the Morse-like basis functions that were used for (HF)<sub>2</sub> (r:  $w_e$ =7500, R:  $w_e$ =16), then the integration area for (DF)<sub>2</sub> turns out to be smaller: r varies from 0.85 to 1.17 Å, R from 2.04 to 13.24 Å, instead of r from 0.79 to 1.22 Å and R from 1.90 to 13.38 Å for (HF)<sub>2</sub>. Because of this, the well of the potential was effectively narrowed, which led to inaccuracies in calculating energy levels. Therefore, the parameters of the basis functions for (DF)<sub>2</sub> were changed (r:  $w_e$ =4500, R:  $w_e$ =15.48), so

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TABLE IX. Observed rotational constants,  $B_{obs}$ , and (obs. – calc.) values in MHz. For K = 5 there are no observations and the absolute calculated values are given.

$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	7] 7] 7] 7] 1]
	7] 7] 7] 7] 1]
K = 1       6531       41       2       2       2       -11       -13       -13       Ref. [ $K = 2$ 6553       36       -4       -4       -7       -16       -18       -18       Ref. [ $K = 3$ 6538       36       -6       -6       -9       -19       -21       -20       Ref. [ $K = 4$ 6408       54       14       26       52       69       66       27       D       D       5	7] 7] 7] 1]
$K = 2 \ 6553 \ 36 \ -4 \ -4 \ -7 \ -16 \ -18 \ -18 \ \text{Ref.} [$ $K = 3 \ 6538 \ 36 \ -6 \ -6 \ -9 \ -19 \ -21 \ -20 \ \text{Ref.} [$ $K = 4 \ 6498 \ 54 \ -14 \ -26 \ 52 \ -69 \ -19 \ -21 \ -20 \ \text{Ref.} [$	7] 7] 1]
$K = 3\ 6538\ 36\ -6\ -6\ -9\ -19\ -21\ -20\ \text{Ref.}$	7] 1]
	1]
$\Lambda = 4 \ 0498 \ 04 \ -14 \ -30 \ -53 \ -02 \ -00 \ -07 \ \text{Ref.}$	
K = 5 6732 6780 6783 6789 6801 6802 6805	
(0010)	
K = 0 6493 41 0 0 -4 -13 -15 -15 Ref. [	7]
$K = 1 \ 6526 \ 40 \ 1 \ 1 \ 1 \ -12 \ -14 \ -14$ Ref. [	7]
$K = 2 \ 6551 \ 37 \ -3 \ -2 \ -5 \ -15 \ -17 \ -17$ Ref. [	7]
K = 3 6558 36 -5 -5 -7 -17 -19 Ref. [	7]
$K = 4 \ 6576 \ 37 \ 4 \ 6 \ 10 \ -20 \ -22 \ -22$ Ref. [	7]
K = 5 6467 6528 6528 6532 6543 6545 6545	
(0100)	
K = 0 6488 135 106 97 91 84 82 83 Ref. [	1]
(0110)	
K = 0 6433 128 97 89 84 89 75 75 Ref. [	1]
(0020)	
$K = 3 \ 6645 \ -34 \ -57 \ -44 \ -40 \ -49 \ -49 \ -49 \ \text{Ref.}$ [ 3	32]

<sup>a</sup>Constants calculated from  $\nu_4$  constants determined in Ref. [1]and values for  $\Delta X$  (X = B, D) in Ref. [8]

Description of headings:

p1: Variational calculations using potential from Huang  $et al.^3$ ;

P: Polynomial fit of *ab initio* points from this work;

M: Morse-fit of *ab initio* points from this work;

K: Morse-fit plus higher-order correlation, K = M +

CCSDT(Q)-CCSD(T)/aug-cc-pVTZ;

CV: Morse-fit plus higher-order correlation plus core-valence, CV = K + CCSD(T)/cc-pCV6Z; DBOC: CV plus scalar relativistic and adiabatic correction, CV + CCSD/aug-cc-pCVTZ + CCSD(T)/aug-cc-pV5Z; pall: polynomial fit with all listed above corrections included.

that the integration areas became almost the same as they were in the  $(HF)_2$  calculations: r from 0.8 to 1.22 Å and R from 1.94 to 13.34 Å, which improved the accuracy of calculated energy levels.

In the first papers on HF dimer<sup>33,34</sup> there are two experimental B constants for DF dimer. The experimental values are reproduced by our calculations with accuracy of about 10 MHz. In particular B(K=0) experimental value is 6252 MHz against calculated 6263 MHz, B(K=1)

experimental value is 6268 MHz with 6279 MHz calculated. The tunneling splitting of the ground state experimental value 1580.5 MHz is reproduced as 1546.5 MHz by theory. The bigger difference than for HF dimer is explained by the use of adiabatic correction for HF dimer in calculation of DF dimer levels. We have not yet calculated the adiabatic correction for DF dimer.

#### VII. CONCLUSIONS

We present results of *ab initio* calculations for the tunneling-rotation-vibration spectrum of the HF dimer performed using the variational nuclear motion program  $WAVR4^{25,26}$  and *ab initio* HF dimer PES, calculated in this work. In particular, we have calculated some 152 000 points at CCSD(T) level of theory with F12QZ basis set and considered all the major corrections, such as the higher correlation CCSDT(Q) correction, corevalence correction, as well as DBOC and relativistic correction. These corrections were calculated on a reduced grid of only 2000 points. The use of exact kinetic energy, variational nuclear motion program WAVR4 to solve the rotation-vibration-tunneling Schrodinger equation allowed us to compare all the parameters measured for the HF dimer with *ab initio* calculated ones using PES of Huang  $et al.^3$  and the ones obtained in this work. We compare the dissociation energy  $D_0$ , the inter-molecular band origins, excited K energy levels, tunneling splitting in various v and K states as well as rotational B constants in various v and K states. Our calculation give ab initio predictions of the B rotational constants within the experimental error for the first time. Our calculated dissociation energy  $(D_0)$  is about 3.8 cm<sup>-1</sup> above the observed value. Attempts to further improve agreement will require first of all the achievement of full convergence of the ZPE calculations independently of the particular PES used.

The observed minus calculated discrepancies for the HF dimer which are based on both direct experimental and empirically-derived data provide important information for estimating the accuracy of the corresponding *ab initio* water dimer energy levels and line positions. This will constitute the first step in the estimating the accuracy of any water dimer line list, while future calculations of the line intensities will complete such a comparative analysis. Our results show that, due to the cancellation of errors, some of these corrections may be considered unnecessary in a future calculation on the water dimer, substantially reducing the cost of such calculations. Clearly this will be the case when *ab initio* calculations on the water dimer are performed at the same level of electronic structure theory. The importance of understanding HF dimer is underscored by the fact that the corresponding water dimer experimental studies cannot readily be performed due to intrinsic limitations on gas phase high resolution observation of water dimers. The similarity of discrepancies of both dimers follows from the similarity of their electronic structure. All that should assist the solution of an important unsolved scientific problem - determination of the role of the water dimer in the gaseous phase in the water continuum of the Earth atmosphere and the atmospheres of the exoplanets.

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#### DATA AVAILABILITY

The data that supports the findings of this study are available within the article and its supplementary material. The code WAVR4 is available via the ExoMol github pages https://github.com/ExoMol/wavr4.

#### SUPPLEMENTARY MATERIAL

A text file giving the calculated HF dimer energy levels is provided as supplementary data. We also provide the the basic F12QZ PES fitted with the Morse coordinates together with all the computed corrections surfaces.

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