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Mobility Management in Multi-Tier LiFi Networks

AHMET BURAK OZYURT^{1,*} AND WASIU O. POPOOLA¹

¹Institute for Digital Communications, School of Engineering, The University of Edinburgh, EH9 3JL, Edinburgh, UK

*Corresponding author: a.b.ozyurt@ed.ac.uk

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Mobility management is an important part of the analysis and design of ultra-dense LiFi networks. This paper presents a two-tier LiFi network and analyses the cross-tier handover rate between the primary and secondary cells. For different conditions of semiangle at half illuminance of the primary and secondary cells, we propose three different coverage models for the secondary cells. Using stochastic geometry, closed-form expressions are derived for the cross-tier handover rate, ping-pong rate and sojourn time in terms of the received optical signal intensity, time-to-trigger and user mobility. The analytical models are validated with simulation results. © 2021 Optical Society of America

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1. INTRODUCTION

The ever increasing demands for wireless communication is making the research community look ahead to the next-generation technologies. Mobile traffic is expected to grow by 31 percent annually between 2019 and 2025; thus, the average traffic per smartphone will increase to around 25 GB per month in 2025 [1]. When we consider that approximately 80 percent of wireless data traffic originates or terminates within a building, new global research should focus on this critical indoor wireless gap [2]. 2G and 3G connectivity still enable the majority of internet of things (IoT) applications, but the number of short-range IoT connections will increase by 13 percent annually and reach close to 20 million connections at the end of the 2025 [3]. User data rate of 1 Gbps, 10^7 devices/km² connection density, 10-100 μ s latency have been proposed as key performance indicators (KPIs) for the emerging 6G [1]. Satisfying these requirements is highly desirable for future wireless technologies. LiFi - a light spectrum based wireless systems- is a viable technology because it offers huge unlicensed spectrum, physical layer security, low-cost, high data rate, and can potentially serve as a complementary technology to the current radio frequency (RF) based systems [4].

From the very beginning of wireless networks, mobility management has been one of the most investigated research areas in communication engineering. In each generation, the radio spectrum has moved up to higher frequencies, so the coverage area of cells has decreased consistently. The cell radius, which was previously expressed in kilometres, has reduced a few meters in LiFi. Also, traffic load in indoor networks varies significantly in time and space depending on various factors such as user mobility. Especially, when multiple tiers are considered in the wireless networks, mobility management becomes more complicated than before. This small radius and multiple tiers have posed a lot of challenges in terms of user mobility management [5], [6].

Multiple tiers in ultra-dense LiFi networks are common phenomena in realistic scenarios. The different tiers can be considered as the different light sources such as the ceiling, floor, and desk lamps. Also, when we take the very small coverage of LiFi tiers into consideration, it is inevitable to face mobility management problems. Thus, the study of handover is of great importance in ultra-dense LiFi networks. In this study, a multi-tier ultra-dense LiFi networks is studied for the first time. To provide a realistic case for such a system, an illustration from an office environment with two different types of light sources was suggested in the IEEE 802.11bb Task Group on Light Communications [7]. However, the authors are not aware of any reported theoretical or practical work on multi-tier concept in LiFi networks.

A. Related Works

There has been a lot of work about mobility management focused not only on RF but also hybrid RF-LiFi networks. The existing LiFi network studies focus on the vertical handover schemes, namely hybrid RF-LiFi networks [8], [9]. In [10], the probability of vertical handover is investigated for a user with random rotations in the hybrid RF-LiFi networks. Also, the Markov decision process is proposed for improving vertical handovers [11]. Another vertical handover scheme, which predicts the parameters in terms of access delays, data size and interruption duration, was proposed in [12]. These parameters are utilized by the system to make handover decisions. Chowdhury and Katz investigated the performance of the hybrid RF-LiFi hot-spot networks in a mobile scenario [13]. A fuzzy logic based vertical handover algorithms were proposed to solve the line-of-sight (LoS) blocking [14]. Due to a change of air interfaces, a vertical handover usually needs a much longer processing time than a horizontal handover [15]. Also, the RF system has a lower system capacity than LiFi, and an excessive number of RF users would cause a substantial decrease in throughput.

For these reasons, dynamic load balancing, resource allocation, and a number of optimization have been mostly investigated in vertical handover schemes[8].

However, the main problem is in horizontal handover among LiFi access points (APs). The works on horizontal handover in the context of LiFi networks are reported in [14]-[25] where there are three main proposed approaches:

- The first approach exploits the received signal strength (RSS) parameter in the optical domain in order to develop an RSS-based handover mechanism for mobile LiFi users. In [16], [17], and [18], soft handover, coordinated multipoint transmission (CoMP) techniques, and link aggregation are introduced, respectively. The user is mainly served by an AP (i.e., luminary) from which it gets the strongest signal. When the user moves towards the cell edge, the received signal from the served AP drops. Based on these handover algorithms, it is decided which AP will serve the user in the handover process. In some cases, the effects of frequency partitioning and rotation for connected user equipment (UE) is also evaluated in regards to RSS value [16], [19]. The handover skipping (HS) technique (based on RSS) which disregarded some adjacent cells is proposed and compared with the standard handover. In addition to these, some closed-form expressions are derived for outage ratio and optimal distance among APs [20]. The vast majority of algorithms use the RSS parameter to reach the final decision.
- The second approach is related to user behaviour and their grouping. The interference management algorithm for a cell-free visible light communication (VLC) network is proposed based on the joint design of user scheduling and precoding. The number of users is no larger than the number of APs that will be served in each time slot [21]. In addition, the awareness of user mobility was used to optimize the overall performance of VLC networks. Due to the stationary nature of indoor optical wireless channels, future channel state information (CSI) is predicted by anticipating the future locations of users. In [22], a resource allocation algorithm is proposed, which uses CSI to dynamically allocate network resources to users. An analysis of the sojourn time for indoor LiFi cellular networks is presented based on the random waypoint (RWP) mobility model in [23].
- The third approach relies on finding optimal coverage while considering various practical parameters such as the transmitted power, the dimming factor, node failure, etc. [24]. Thus, this approach shows how physical layer parameters affect the coverage of a LiFi system [25]. Besides, not only the transmitter side but also the receiver part is investigated very well, especially the receiver angle diversity is evaluated in regards to handover and data rate [26]. In [27], a method to improve traffic distribution in multi-user environments and handover at cell edges when transmitters are capable of dynamically changing their signal power.

The foregoing horizontal handover studies focus on one tier system in LiFi networks. They do not consider the realistic scenarios of multi-tier ultra-dense LiFi networks. Although, cross-tier mobility management is a well-studied subject in RF heterogeneous networks. LiFi networks have unique features that make its cross-tier mobility different to that in RF.

B. Contributions and Outline

In this paper, we investigate the cross-tier mobility management in ultra-dense LiFi networks using stochastic geometry. The contributions are as follows:

1. For the first time in literature, we introduce the multi-tiers concept in the LiFi networks for enhancing mobility management in a realistic environment.
2. We propose three different secondary cell coverage scenarios that are based on the half-angle of the primary and secondary AP light sources.
3. Closed-form expressions are presented for cross-tier handover rate, ping-pong rate, and sojourn time as functions of time to trigger (TTT), AP intensities, and user velocity.
4. The closed-form analytical results are verified through simulations. The effect of system parameters such as TTT and user velocity are explained on the mobility performance, which could provide deeper insight for realistic LiFi network planning.

In LiFi, the cell size is considerably smaller than in RF and therefore handover rate, TTT, sojourn time within a cell and prevention of unnecessary back and forth handover via the estimation of the ping-pong rate are all vital mobility management metrics. These are the metrics that we have studied for a LiFi configuration with a number of light sources. In addition to the small coverage area of LiFi, the issue of mobility management is made more desirable due to the dissimilar distribution of light intensity by the different light sources. This is the motivation for considering received optical intensity (ROI) in our mobility management work.

The rest of this paper is organized as follows. The network model, LiFi channel model, and mobility model are introduced as parts of the system model in the next section. In Section 3, the secondary cell coverage area is presented. Section 4 presents the cross-tier handover rate and ping-pong rate with closed-form expressions. Section 5 provides simulation evaluations with verifications of the analytical results. Finally, we give the concluding remarks in Section 6.

2. SYSTEM MODEL

In this section, the network model used is presented. At first, the LiFi network placement model is realized according to multi-tier concept which arises when there are multitude of traffic types with clearly different parameters, such as mobility patterns, and/or different requirements, such as quality-of-service requirements. The two tiers are distinguished by their transmission power and spatial density. The primary access points (PAPs) and the secondary access points (SAPs) are deployed using a poisson point process (PPP) model on the Poisson-Voronoi tessellation (PVT). Secondly, the LiFi channel model used in the analytical calculations is briefly discussed and the user equipment (UE) movement model is presented as well.

A. Network Model

In LiFi, the APs are used as both lighting sources and wireless data communication points. If we consider LiFi networks built on legacy infrastructure, the placement of the APs is mainly determined by the lighting design. Three different scenarios proposed for the location of LiFi APs are: hexagonal, lattice, and PPP [28].

Most of the related works focus on conventional LiFi network deployments of the cells whose shapes are either square or hexagonal. In practice, the ultra-dense LiFi networks typically contains a large number of 'statistically random' APs, such as ceiling luminaries, desktop lamps, and even LED screens [5], [6].

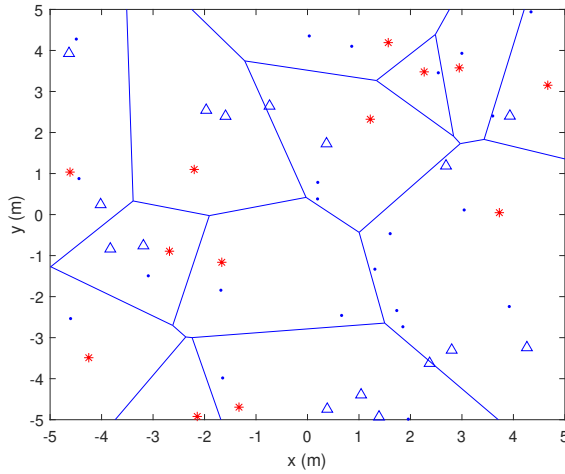


Fig. 1. PVT ultra-dense LiFi network with the primary access points (red stars), the secondary access points (blue triangles) and mobile users (blue dots).

Therefore, the use of a regular/deterministic model for the positioning of these light sources will be unrealistic. Hence, spatial point process provides more accurate and tractable solutions for such a LiFi network modelling.

The point process is defined as a random group of many points that can be counted with a multiple probability, while the PPP is the number of points in a set with a Poisson distribution having parameter λ (mean intensity) [29]. A point process $\Phi = \{x_{(i)} : i = 1, 2, \dots\} \subset R^d$ is a PPP if and only if the number of the points in any compact set $B \subset R^d$ is a Poisson random variable. The R^d is referred to as d dimensional space in real plane. The number of points in disjoint sets are independent and have a Poisson distribution as:

$$P\{t \text{ points in set } B\} = P\{\Phi(B) = t\} = \frac{\Lambda^t}{t!} \exp(-\Lambda), \quad (1)$$

where $\Lambda = \int_B \lambda(x) dx$ is the intensity measure of the Poisson random variable of density $\lambda(x)$. If $\lambda(x)$ is constant ($\lambda(x) = \lambda$), the PPP is said to be uniform or homogeneous PPP (HPPP) [30]. In other words, intensity measure is the expected number of points in a set B as defined below [31]:

$$\Lambda(B) \triangleq E[N(B)], \forall B \in R^d. \quad (2)$$

For every compact set B , $N(B)$ has a Poisson distribution with mean $\lambda|B|$ and $|\cdot|$ is the Lebesgue measure of set B . Then, equation (1) becomes:

$$P\{\Phi(B) = t\} = \frac{(\lambda(B))^t}{t!} \exp(-\lambda(B)). \quad (3)$$

In this work, the set B is considered as a two-dimensional Euclidean space and the APs are distributed on the Voronoi tessellation according to the PPP indicated with Φ and intensity λ [32]. The Voronoi tessellation is a partition of the plane into n convex polytopes. Each partition contains one generator such that every point in the partition is closer to its own generator than any other generator [33]. The APs in the primary tier p and secondary tier s are distributed following two independent PPPs with intensities λ_p and λ_s respectively. Through this approach, the network system design becomes more realistic and

appropriate for optimization studies including the investigation of mobility. Figure 1 shows the network deployment where the PAPs are indicated by red stars, the SAPs are indicated by blue triangles, and the mobile users are shown by blue dots in a 2-D coordinate system.

B. LiFi Channel Model

Mobility management process in LiFi networks is based on the Received Optical Intensity (ROI). Namely, the measured ROIs are the principal criteria for initiating a handover process. In this paper, only LOS is considered for LiFi and the effect of multiple reflections from the walls and human shadowing are ignored. It is shown in [34] that the reflection paths have an insignificant effect on the LiFi APs that are sufficiently far away from the network boundaries. Under this assumption, the ROI of users from the APs in tier i ($i = p, s$) is given by the product of the transmitted power and the path loss [35]:

$$ROI_i(d_{i,u}) = P_i \frac{(m_i + 1) A_r}{2\pi d_{i,u}^2} \cos^{m_i}(\varphi_i) T_s g(\psi_i) \cos(\psi_i), \quad (4)$$

where $d_{i,u}$ denotes the distance from the user to an AP in tier i , P_i is the transmitted power, A_r is the receiver effective area, T_s is the filter transmission, $g(\psi_i)$ and ψ_{con} are the concentrator gain and field-of-view (FOV), respectively, and m_i is the Lambertian index defined as [35]:

$$m_i = -\frac{\ln(2)}{\ln[\cos(\varphi_{1/2})]}, \quad (5)$$

where $\varphi_{1/2}$ is the semiangle at half illuminance of the transmitter. The gain of the optical concentrator at the receiver is defined by [35]:

$$g(\psi) = \begin{cases} n^2 / \sin^2(\psi_{con}), & \text{if } 0 < \psi \leq \psi_{con} \\ 0, & \text{if } \psi_{con} \leq 0, \end{cases} \quad (6)$$

where n is the refractive index.

C. Mobility Model

In this paper, we used an improved Random Way Point (RWP) mobility model which is proposed in [36] due to its simplicity in modelling movement patterns of mobile nodes.

In this model, UEs move in a limited domain such as \mathcal{A} . At each time, the random destination points (referred to as waypoint) are chosen as uniformly distributed in \mathcal{A} . Then, the UE follows a straight line between its current waypoint to the newly selected waypoint at the decided constant velocity. The process repeats at each destination point and the user can have an optional random pause time. In this model, at each waypoint the mobile node chooses 1) a random direction that is uniformly distributed on $[0, 2\pi]$, 2) a transition length that follows uniform distribution, and 3) a mobile user/device with a velocity that is based on uniform distribution. The node then moves to the next waypoint (determined by choice 1 and 2) at the chosen velocity. We acknowledge that human movement has very complex temporal and spatial correlations and its nature has not been fully understood and therefore cannot be perfectly modelled [37], [38]. Human movement within a space will be impacted by the presence of physical objects within that space. Modeling such a movement is highly complex and will depend on the given scenario and environment. Developing such a model is outside the scope of this work. Instead, we assume that the user movement is random and follows the RWP mobility model. The

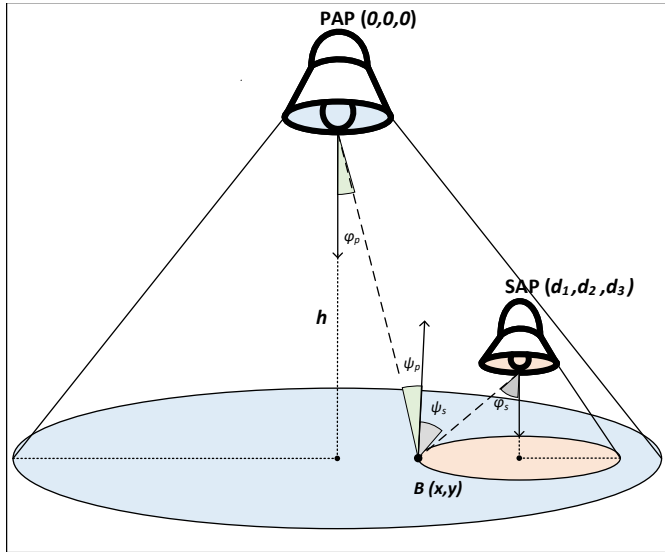


Fig. 2. The multi-tier LiFi network with the primary access point and the secondary access point.

RWP model is tractable and provides a basis to evaluate mobility management in LiFi. By using this model, it is now possible to analyze the impact of user mobility on LiFi networks thereby providing an insight into designing a reliable LiFi network. The framework that we present can be used/extended to any other user mobility model.

The proposed RWP mobility model can be described by an infinite sequence of quadruples $\{(\mathbf{X}_{k-1}, \mathbf{X}_k, V_k, S_k)\}_{k \in K}$, where k denotes the k th movement period. During the k th movement, \mathbf{X}_{k-1} denotes the starting waypoint, \mathbf{X}_k denotes the target waypoint, V_k denotes the velocity, and S_k denotes the pause time at the waypoint \mathbf{X}_k . Given the starting waypoint \mathbf{X}_{k-1} , a homogeneous PPP $\Phi_u(k)$ with intensity λ_u is independently generated and then the nearest point in $\Phi_u(k)$ is selected as the target waypoint. That is:

$$\mathbf{X}_k = \arg \min_{\mathbf{x} \in \Phi_u(k)} |\mathbf{x} - \mathbf{X}_{k-1}|. \quad (7)$$

Therefore, denoting the transition length of the k th movement as $L_k = |\mathbf{X}_{k-1} - \mathbf{X}_k|$, the cumulative distribution function (CDF) of L_k can be written as [39]:

$$P_{L_k}(L_k \leq l) = 1 - \exp(-\lambda_u \pi l^2), \quad l > 0 \quad (8)$$

This is the probability that L_k is smaller than a given distance l is the probability that the points in the area (πl^2) . The transition lengths are Rayleigh distributed [40]. Besides, velocity V_k and pause time S_k are independent, identically distributed (i.i.d.) with distributions $P_V(\cdot)$ and $P_S(\cdot)$, respectively.

3. ANALYTICAL MODEL FOR SECONDARY CELL COVERAGE AREA

Generally, a network consists of multiple cells that are adjacent to one another. The cell coverage area is delimited by the adjacent cells. In other words, borders among cells are determined by the received signal which is ROI in LiFi [41]. In this paper, all UEs faces are directed upward. Also, it is considered that UEs and APs are moving only in a 2D plane. Thus, their height from the ground has been taken as constant.

When the P2S (primary-to-secondary) cross-tier handover process is taken into account, it is assumed that the user is initially deployed inside the coverage of the PAP such as in Figure

2. In multi-tier LiFi networks, PAPs are deployed with low spatial density, high transmit optical power and wider coverage area. On the other hand, SAP, will be a set of other light sources, with lower and smaller coverage area than the PAP. The SAP can be very localised and could support higher data rates. In addition, the PAP is considered as an umbrella tier and the SAPs are located under this umbrella. Namely, each SAP is covered by a PAP. It is assumed that the PAPs and the SAPs are both connected to the same backbone and coordinated. Without loss of generality, we assume that a typical PAP l_p is located at the origin, and a SAP l_s is located at position $\mathbf{x}_s(d_1, d_2, d_3)$. According to the ROI, the coverage boundary of the SAP l_s can be determined as,

$$B = \{(x, y) \in \mathbb{R}^2 \mid \text{ROI}_p(d_{p,u}) = \text{ROI}_s(d_{s,u})\}. \quad (9)$$

Thus, a set of equal ROI points in (9) form the coverage boundary of the SAP. These points will help in calculating the mobility management parameters in a LiFi network. For a user located at $(x, y) \in \mathbb{R}^2$ and the height from the ground is h , the distance from user to the PAP, and the SAP are given, respectively, by,

$$d_{p,u} = \sqrt{x^2 + y^2 + h^2}, \quad (10)$$

$$d_{s,u} = \sqrt{(x - d_1)^2 + (y - d_2)^2 + (h - d_3)^2}. \quad (11)$$

In addition, $\cos(\varphi_p) = \cos(\psi_p) = \frac{h}{\sqrt{x^2 + y^2 + h^2}}$ and $\cos(\varphi_s) = \cos(\psi_s) = \frac{h - d_3}{\sqrt{(x - d_1)^2 + (y - d_2)^2 + (h - d_3)^2}}$ are considered because UEs faces are assumed to be directed upward. By substituting (10) and (11) into (9), we obtain,

$$W \cdot (x^2 + y^2 + h^2)^{\hat{m}} - [(x - d_1)^2 + (y - d_2)^2 + (h - d_3)^2] = 0 \quad (12)$$

where, $W = \left(\frac{P_s(m_s+1)(h-d_3)^{m_s+1}}{P_p(m_p+1)h^{m_p+1}} \right)^{\frac{2}{m_s+3}}$, $\hat{m} = \frac{m_p+3}{m_s+3}$. At this point, there are three different cases about Lambertian indexes: $m_p = m_s$, $m_p > m_s$, and $m_p < m_s$.

In a special case, where both the PAP and the SAP share an equal Lambertian index ($m_p = m_s$), \hat{m} equals 1. Thus, the defined function in (12), can be simplified into a circular equation. The corresponding center $\mathbf{x}_c = (x_c, y_c)$ as well as the radius R_c is calculated as:

$$\mathbf{x}_c = \left(\frac{d_1}{1 - W}, \frac{d_2}{1 - W} \right) \quad (13)$$

$$R_c = \sqrt{\frac{W(d_1^2 + d_2^2)}{(1 - W)^2} + \frac{Wh^2 - (h - d_3)^2}{(1 - W)}}. \quad (14)$$

However, it is very possible to have different Lambertian indexes for the PAP and the SAP. Thus, we need to find new approximation methods for the quadratic part of the function $f = (x^2 + y^2 + h^2)^{\hat{m}}$. On one hand, if we consider as $m_p < m_s$, then \hat{m} is lower than 1. $(x^2 + y^2 + h^2)$ is a polynomial of order 2 and $0 < \hat{m} < 1$; thus, a second-order Taylor series expansion method is proposed in [42] to approximate f . After carrying out some manipulations, a generalized ellipse function with the center $\mathbf{x}_e(x_e, y_e)$ and the two semi-axes s_1, s_2 is derived as:

$$ax^2 + 2bxy + cy^2 + 2dx + 2fy + g = 0 \quad (15)$$

$$\mathbf{x}_e = \frac{cd - bf}{b^2 - ac}, \quad y_e = \frac{af - bd}{b^2 - ac} \quad (16)$$

$$s_1 = \sqrt{\frac{2(af^2 + cd^2 + gb^2 - 2bdf - acg)}{(b^2 - ac)[\sqrt{(a-c)^2 + 4b^2} - (a+c)]}} \quad (17)$$

$$s_2 = \sqrt{\frac{2(af^2 + cd^2 + gb^2 - 2bdf - acg)}{(b^2 - ac)[-\sqrt{(a-c)^2 + 4b^2} - (a+c)]}} \quad (18)$$

where a, b, c, d, f, g are defined as in Appendix A.

On the other hand, the PAP's lambertian index can be higher than the SAP's lambertian index ($m_p > m_s$). In this case, $\hat{m} > 1$. As can see from (5), semiangle half illuminance of the transmitter dictates the value of Lambertian index. For realistic scenarios, with $90^\circ > \varphi_{1/2} > 10^\circ$, the average value of \hat{m} is only slightly larger than 1. Thus, we propose a linear approximation approach which is defined as follows:

$$\hat{f} = \alpha(x^2 + y^2 + h^2). \quad (19)$$

Substituting $x = r \cos \theta$ and $y = r \sin \theta$ into (19), we have $\hat{f} = \alpha(r^2 + h^2)$. By denoting the absolute error incurred in approximating function f as $E(r)$, then we can express $E(r)$ as

$$E(r) = |f - \hat{f}| = \sqrt{[(r^2 + h^2)^{\hat{m}} - \alpha(r^2 + h^2)]^2}. \quad (20)$$

In order to minimize the approximation error $E(r)$ within the range of $r \in [0, \sqrt{d_1^2 + d_2^2 + h^2}]$, we can calculate the optimum value of α as,

$$\alpha = \arg \min \int_0^{\sqrt{d_1^2 + d_2^2 + h^2}} E(r) dr = (d_1^2 + d_2^2 + h^2)^{\hat{m}-1} \quad (21)$$

According to (13) and (14), the corresponding center $\mathbf{x}_c' = (x_c', y_c')$ and the radius R_c' of the coverage area of secondary cell for $\hat{m} > 1$ is expressed as,

$$\mathbf{x}_c' = \left(\frac{d_1}{1 - \alpha W}, \frac{d_2}{1 - \alpha W} \right) \quad (22)$$

$$R_c' = \sqrt{\frac{\alpha W(d_1^2 + d_2^2)}{(1 - \alpha W)^2} + \frac{\alpha W h^2 - (h - d_3)^2}{(1 - \alpha W)}}. \quad (23)$$

4. CROSS-TIER MOBILITY ANALYSES FOR RESILIENT LIFI

A. P2S Handover Rate

Network densification through multiple-tiers is an inevitable part of next-generation LiFi systems. However, the handover rate is higher in smaller and denser cells, and handover rate directly affects the network signalling overhead. Among the different types of handover, the cross-tier handover showed the highest handover failure rate [43]. The P2S handover rate can be defined as follows [19]:

$$H = H_t \times P(S > TTT), \quad (24)$$

where the P2S handover trigger rate H_t represents the number of times that the UE that resides in a primary tier moves across a secondary tier coverage boundary in a unit time. $P(S > TTT)$ is the probability that the UE's sojourn time S inside the secondary tier coverage area is larger than the TTT duration. **The TTT is the time window during which handover needs to happen provided the handover requirement is met. The handover requirement considered in this work is based on received optical intensity ROI. This parameter can decrease the number of unnecessary handovers and effectively avoid ping-pong effects [44].**

According to RWP mobility model, the movement trace of the UEs can be divided into infinite parts. Thus, the P2S handover trigger rate can be defined as the expected number of triggered P2S handovers $E[N]$ during one movement period divided by the expected period of time $E[T]$. So, the P2S handover trigger rate is expressed as follows [36],

$$H_t = \frac{E[N]}{E[T]}. \quad (25)$$

The trajectory line in the k -th movement period is defined with the two successive waypoints, \mathbf{X}_{k-1} and \mathbf{X}_k . Thus, we assume that user follows the movement traces of $\dots, \mathbf{X}_{k-1}, \mathbf{X}_k, \dots$. We can derive the number of triggered P2S handovers by calculating the number of intersection between the secondary tier boundaries and the UE's trajectory line, denoted as $L(\mathbf{X}_{k-1}, \mathbf{X}_k)$.

Let l_{x_i} denote the coverage area delimited by the SAP. According to (14), $l_{x_i} = C(\mathbf{x}_i, R_i)$, where R_i is the radius of the SAP. We can assume that $L_{(+R_i)}$ can be the set of points laying in the intersection of the following two conditions:

1. At most R_i units distant from the line segment $L(\mathbf{X}_{k-1}, \mathbf{X}_k)$, and
2. At least R_i units distant from the start point \mathbf{X}_{k-1} , which will be expressed as,

$$L_{(+R_i)} = \{\mathbf{x} \in \mathbb{R}^2 \mid D(\mathbf{x}, L(\mathbf{X}_{k-1}, \mathbf{X}_k)) \leq R_i \cap D(\mathbf{x}, \mathbf{X}_{k-1}) \geq R_i\}, \quad (26)$$

where $D(\mathbf{x}, L(\mathbf{X}_{k-1}, \mathbf{X}_k))$ is the shortest Euclidean distance from \mathbf{x} to the UE's trajectory line $L(\mathbf{X}_{k-1}, \mathbf{X}_k)$, and

$$|L_{(+R_i)}| = 2|L(\mathbf{X}_{k-1}, \mathbf{X}_k)|R_i. \quad (27)$$

Assume the segment $L(\mathbf{X}_{k-1}, \mathbf{X}_k)$ is fixed and moves towards the circle center. If the circle center falls within the coverage of $L_{(+R_i)}$, the segment intersects with the secondary cell coverage circle. Based on geometry probability theory, the probability that an P2S handover event occurs in the SAP l_{x_i} during the k th period is $|L_{(+R_i)}|/|\mathcal{A}|$, where $|L_{(+R_i)}|$ has been derived in (27). Averaged over the entire probability space, the expected P2S handover trigger rate for one target SAP is derived as follows,

$$\begin{aligned} P_{ho,t} &= \int_0^\infty \int_0^\infty \frac{|L_{(+R_i)}|}{|\mathcal{A}|} f_{L(\mathbf{X}_{k-1}, \mathbf{X}_k)}(l) f_{R_i}(r) dl dr \\ &= \frac{2}{|\mathcal{A}|} E[|L(\mathbf{X}_{k-1}, \mathbf{X}_k)|] E[R_i] \\ &= \frac{2}{|\mathcal{A}|} \frac{1}{2\sqrt{\lambda_u}} \sqrt{\frac{WE[X_{s2p}]^2}{(1-W)^2} + \frac{Wh^2 - (h-d_3)^2}{(1-W)}} \\ &= \frac{1}{|\mathcal{A}|\lambda_u} \sqrt{\frac{W}{4\lambda_p(1-W)^2} + \frac{Wh^2 - (h-d_3)^2}{(1-W)}} \end{aligned} \quad (28)$$

where $f_{L(\mathbf{X}_{k-1}, \mathbf{X}_k)}(l)$ is the probability density function (PDF) of the UE's transition length and it follows Rayleigh distribution because of RWP specifications. Also, $f_{R_i}(r)$ is the PDF of the secondary cell radius. In fact, Rayleigh distribution of the RWP ensures that $E[|L(\mathbf{X}_{k-1}, \mathbf{X}_k)|] = \frac{1}{2\sqrt{\lambda_u}}$. In addition, it is obtained that $E[X_{s2p}] = \frac{1}{2\sqrt{\lambda_p}}$ based on stochastic geometry.

In this manner, the expected number of triggered P2S handovers during the n th movement period is given by:

$$E[N] = \lambda_s |\mathcal{A}| P_{ho,t}. \quad (29)$$

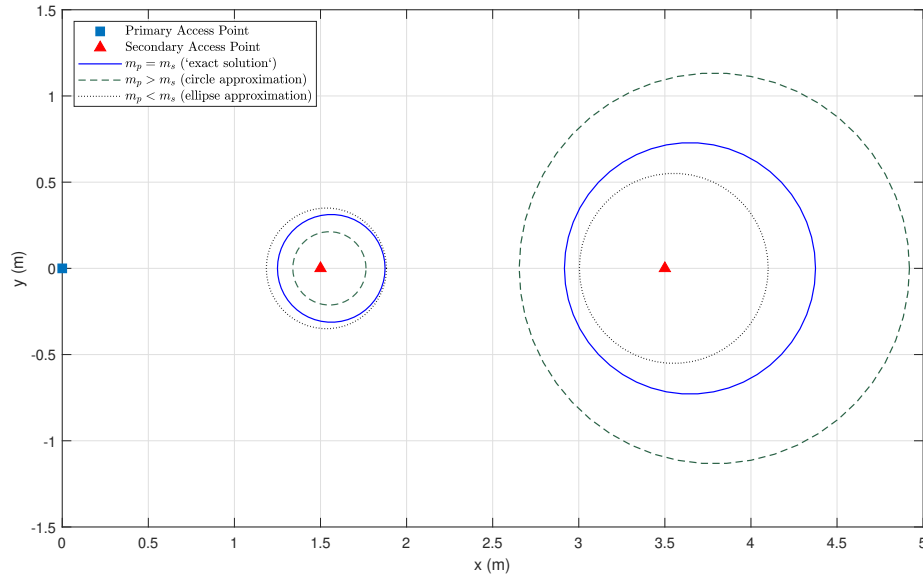


Fig. 3. Evaluation of SAP coverage area boundaries in the presence of an PAP at the origin.

On the other side, we note that $E[T] = E[T_s] + E[T_t]$, where $E[T_s]$ and $E[T_t]$ are the mean pause time and the mean transition time, $E[T_t] = E[|L(\mathbf{X}_{k-1}, \mathbf{X}_k)|/v]$. By combining (25) and (29), the closed-form expression of the P2S handover trigger rate with considering user velocity becomes:

$$H_t = \frac{\lambda_s v}{\sqrt{\lambda_u v E[T_t]} + \sqrt{\lambda_u v E[T_s]}} \times \sqrt{\frac{W}{4\lambda_p(1-W)^2} + \frac{Wh^2 - (h-d_3)^2}{(1-W)}} = \frac{2\lambda_s v}{1 + 2\sqrt{\lambda_u v E[T_s]}} \sqrt{\frac{W}{4\lambda_p(1-W)^2} + \frac{Wh^2 - (h-d_3)^2}{(1-W)}}. \quad (30)$$

According to (24), cross-tier handover will happen when the UE sojourn time S inside that secondary cell is larger than TTT duration. After obtaining handover trigger rate, we need to find the probability of sojourn time which is larger than TTT.

Firstly, the expected trajectory length inside a secondary cell with radius R_c is given as,

$$L_c(R_c) = \frac{\pi}{2} R_c. \quad (31)$$

By replacing R_c with X_{p2m} in (14), the sojourn time inside a secondary cell is given as:

$$S = \frac{L_c(R_c)}{v} = \frac{\pi}{2v} \sqrt{\frac{WX_{s2p}^2}{(1-W)^2} + \frac{Wh^2 - (h-d_3)^2}{(1-W)}}. \quad (32)$$

According to the CDF of X_{p2m} , the probability that the handover UE's sojourn time inside the secondary cell is larger than TTT,

$$P(S \geq TTT) = \exp \left\{ -\lambda_p \pi \frac{(1-W)^2}{W} \times \left[\left(\frac{2vTTT}{\pi} \right)^2 - \left(\frac{Wh^2 - (h-d_3)^2}{(1-W)} \right) \right] \right\}. \quad (33)$$

Table 1. Parameters of the access points.

Lambertian Indices	Semiangle at Half Illuminance	
	Primary Acces Point	Secondary Access Point
$m_p = m_s$ (‘exact solution’)	60°	60°
$m_p > m_s$ (circle approximation)	30°	60°
$m_p < m_s$ (ellipse approximation)	60°	30°

By plugging (30) and (33) into (24), the closed-form expression of the expected P2S handover is derived below, this denotes the P2S handover rate,

$$H = \frac{2\lambda_s v}{1 + 2\sqrt{\lambda_u v E[T_s]}} \sqrt{\frac{W}{4\lambda_p(1-W)^2} + \frac{Wh^2 - (h-d_3)^2}{(1-W)}} \times \exp \left\{ -\lambda_p \pi \frac{(1-W)^2}{W} \times \left[\left(\frac{2vTTT}{\pi} \right)^2 - \left(\frac{Wh^2 - (h-d_3)^2}{(1-W)} \right) \right] \right\}. \quad (34)$$

B. Ping-Pong Rate

The ping-pong is defined as the UE has a time-of-stay inside a small cell less than the threshold T_p , e.g. 1 s, and then handover back to the PAP, then the handover that terminates this time-of-stay is considered an unnecessary handover. Thus, the sojourn time S , which is defined as the duration that a mobile node resides in a typical secondary cell coverage area, is one of the most essential parameters for evaluating the ping-pong events. Thus, the ping-pong rate can be defined as:

$$H_p = H_t \times [P(S < T_p) - P(S < TTT)]. \quad (35)$$

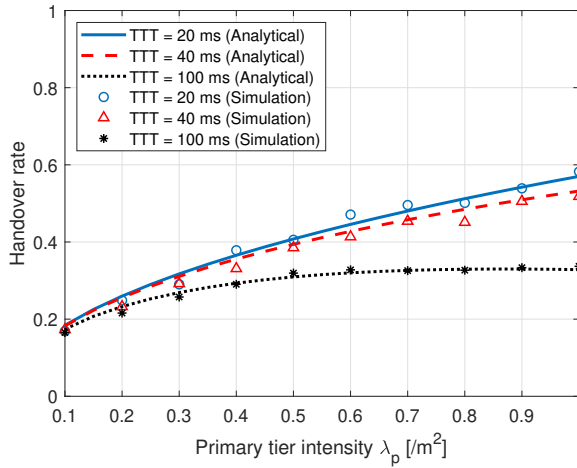


Fig. 4. P2S handover rate.

By combining equations (30) and (35), we can obtain the expression of the ping-pong rate as:

$$\begin{aligned}
 H_p = & \frac{2\lambda_s v}{1 + 2\sqrt{\lambda_u v} E[T_s]} \sqrt{\frac{W}{4\lambda_p(1-W)^2} + \frac{Wh^2 - (h-d_3)^2}{(1-W)}} \\
 & \times \left(\exp \left\{ -\lambda_p \pi \frac{(1-W)^2}{W} \right. \right. \\
 & \quad \left[\left(\frac{2vTTT}{\pi} \right)^2 - \left(\frac{Wh^2 - (h-d_3)^2}{(1-W)} \right) \right] \left. \right\} \\
 & - \exp \left\{ -\lambda_p \pi \frac{(1-W)^2}{W} \right. \\
 & \quad \left[\left(\frac{2vT_p}{\pi} \right)^2 - \left(\frac{Wh^2 - (h-d_3)^2}{(1-W)} \right) \right] \left. \right\} \Bigg). \quad (36)
 \end{aligned}$$

Notice that, according to 3GPP TS 36.839 specification, TTT timer has 4 typical values. These values are 40 ms, 80 ms, 160 ms, and 480 ms respectively. However, these values must be lower in LiFi. Furthermore, the recommended T_p value is 0.5 second. Obviously, since T_p is larger than TTT, $P(S < T_p)$ is always greater than $P(S < TTT)$.

5. NUMERICAL RESULTS AND DISCUSSIONS

In this section, we discuss the analytical results of P2S cross-tier handover performance metrics and compare with the simulation results. For the purpose of illustration, we consider a room with dimensions: $10 \times 10 \times 3$ m³. In Figure 3, the coverage area of secondary cells in regard to different Lambertian indices are shown when a PAP is located at the origin. The SAPs are located at (1.5 m, 0) and (3 m, 0). To illustrate the different approximation methods mentioned in Section 3, the semiangle at half illuminance of the transmitters are selected as in Table I. Furthermore, $P_p = 25P_s$ is assumed as the relationship among transmit powers for this illustration scenario. The height of UEs and SAPs from the ground has been taken as 0.75 m and 1.2 m, respectively. As stated before, the ellipse approximation is used for $0 < \hat{m} < 1$. When $\hat{m} = 1$, it is shown the exact results and the circle approximation is proposed for $1 < \hat{m}$. In Figure 3, the coverage areas of the SAPs in different locations can be seen together. In the location of (3.5 m, 0), the coverage area of exact result is wider than ellipse approximation. Although they

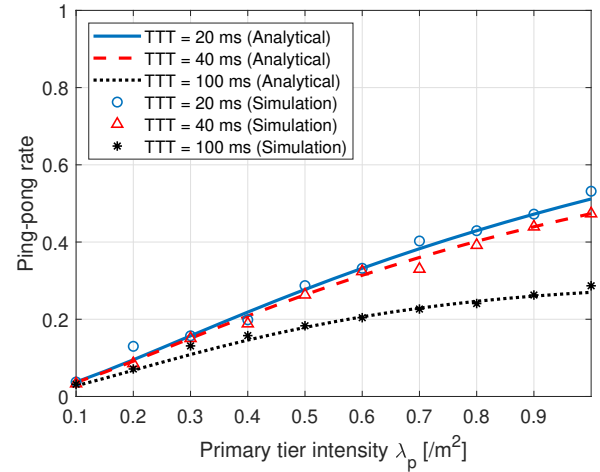


Fig. 5. P2S ping-pong rate.

are covered by the same PAP, the semiangle at half illuminance of the SAPs are different. As expected, bigger semiangle at half illuminance provides a wider coverage area for the exact result when compared with ellipse approximation. However, in the location of (1.5 m, 0), the coverage of the exact result is narrower than the ellipse approximation because the SAP is closer to the PAP. Actually, the PAP is a kind of interference source and delimits the coverage area of the SAPs. At location (1.5 m, 0), the PAP presents a much stronger interference to the SAP compared to the location (3.5 m, 0). It is worth noting that the transmit powers of the SAPs are fixed, but their half-angles are different. Although the 'exact solution' case has the same transmit power as the ellipse approximation and bigger half-angle at the location of (1.5 m, 0), the 'exact solution' case cannot cover a wider area due to lower received power. Thus, the received power from the 'exact solution' case is lower than in the case of ellipse approximation and it is more limited when approaching the PAP. For the same reasons, in the location (1.5 m, 0), the coverage area of the 'exact solution' case is wider than the circle approximation. However, the PAP is a limited interference source to the SAP at location (3.5 m, 0), see Fig. 3.

In Figures 4, 5, and 6, we present simulation results to verify the analytical results of the P2S cross-tier handover performance metrics which are derived in Section 4. The movement of an UE is based on the mobility model given in Section 2. We consider a two-tier ultra-dense LiFi network deployment scenario, where the PAPs and the SAPs are distributed using two independent homogenous PPPs, Φ_p, Φ_s , with intensities λ_p and λ_s , respectively. Additionally, $\lambda_s = 2\lambda_p$ is assumed and UEs velocity is considered as $v = 1.4$ m/s. The case of $\hat{m} = 1$ is used for numerical results; thus, the semiangles at half illuminances are taken as equal to 60° .

Figure 4 depicts the P2S handover rate versus different primary cells intensity λ_p . It is clear that the handover rate increases within the denser deployment. This is because the secondary cell deployment gets denser as λ_p increases, which means that the cross-tier handover will be triggered more. On the other side, the handover rate decreases as TTT values increase because users are less likely to enter a new secondary cell. In addition, the ping-pong rate illustrated in Figure 5 increases as the TTT duration decreases because a larger TTT causes more triggering rate. In Figure 6, the average sojourn time inside a secondary cell decreases with high velocity and denser deployment. As

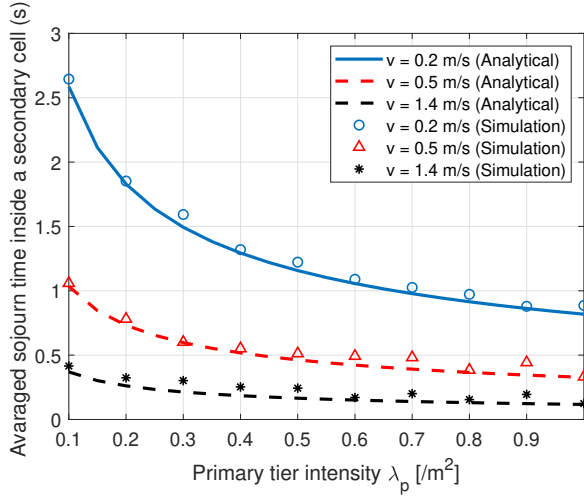


Fig. 6. Average sojourn time inside a secondary cell by analyses and simulation.

expected, higher UE velocity is a reason for shorter residence time in a secondary cell and the coverage area of a SAP decreases with high intensity.

The results show that the analytical expressions match the simulations quite well. The above simulation results not only validate our analytical results in Section 4, but also provide deeper knowledge for mobility enhancement in ultra-dense LiFi networks. For instance, if we have a value of the SAP intensity in a certain area, we can estimate the velocity of the user by applying the analytical expression of the cross-tier handover rate. Also, these analytical expressions can be beneficial for increasing the positioning accuracy such as using the sojourn time when the results are not enough or the position error is very large. In the case of TTT and APs deployment being fixed, various mobility management strategies can be applied to UEs with different velocities. For example, high mobility users can always connect to the P2S and avoid P2S handover due to its possible high handover and ping-pong rate.

6. CONCLUSION

In this paper, the key performance metrics in ultra-dense LiFi networks are analyzed for handover from the primary tier to the secondary tier. Based on three different cases for semiangle at half illuminance, we presented the analytical models for the coverage areas of the SAPs. We derived closed form expressions for the P2S cross-tier handover and ping-pong rate as functions of the system parameters. These expressions show that TTT, AP intensity of each tier, and user velocity have a critical impact on the mobility management in LiFi. In addition, simulation results are presented to validate the theoretical models presented. The findings will be valuable in practical LiFi deployment and planning as well as handover optimization in ultra-dense networks.

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APPENDIX A

Due to $(x^2 + y^2 + h^2)$ is a polynomial of order 2 and $0 < \hat{m} < 1$, the order of (12) is at most 2. The second-order Taylor series

expansion method can be applied for $(x^2 + y^2 + h^2)^{\hat{m}}$ at point (i, j)

$$T(i, j) = f(i, j) + (x - i)f_x(i, j) + (y - j)f_y(i, j) + \frac{1}{2}(x - i)^2 f_{xx}(i, j) + \frac{1}{2}(y - j)^2 f_{yy}(i, j) + (x - i)(y - j)f_{xy}(i, j) \quad (37)$$

where

$$f(i, j) = (i^2 + j^2 + h^2)^{\hat{m}} \quad (38)$$

$$f_x(i, j) = 2\hat{m}i f(i, j)^{\frac{\hat{m}-1}{m}} \quad (39)$$

$$f_y(i, j) = 2\hat{m}j f(i, j)^{\frac{\hat{m}-1}{m}} \quad (40)$$

$$f_{xx}(i, j) = 2\hat{m}f(i, j)^{\frac{\hat{m}-1}{m}} + 4\hat{m}i^2(\hat{m} - 1)f(i, j)^{\frac{\hat{m}-2}{m}} \quad (41)$$

$$f_{yy}(i, j) = 2\hat{m}f(i, j)^{\frac{\hat{m}-1}{m}} + 4\hat{m}j^2(\hat{m} - 1)f(i, j)^{\frac{\hat{m}-2}{m}} \quad (42)$$

$$f_{xy}(i, j) = 4ij\hat{m}(\hat{m} - 1)f(i, j)^{\frac{\hat{m}-2}{m}} \quad (43)$$

Plugging (37) into (12) and carrying out some manipulations, we get

$$ax^2 + 2bxy + cy^2 + 2dx + 2fy + g = 0 \quad (44)$$

where

$$a = \frac{W}{2} f_{xx}(i, j) - 1 \quad (45)$$

$$b = \frac{f_{xy}(i, j)W}{2} \quad (46)$$

$$c = \frac{W}{2} f_{yy}(i, j) - 1 \quad (47)$$

$$d = 0.5[Wf_x(i, j) - Wif_{xx}(i, j) - Wjf_{xy}(i, j) + 2d_1] \quad (48)$$

$$f = 0.5[Wf_y(i, j) - Wjf_{yy}(i, j) - Wif_{xy}(i, j) + 2d_2] \quad (49)$$

$$g = W \left[f(i, j) - if_x(i, j) - jf_y(i, j) + \frac{i^2}{2} f_{xx}(i, j) + \frac{j^2}{2} f_{yy}(i, j) + ijf_{xy}(i, j) \right] - [d_1^2 + d_2^2 + (h - d_3)^2]. \quad (50)$$

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AUTHOR BIOGRAPHIES



Ahmet Burak Ozyurt (S'21) received the B.S. and M.S. degrees all in communication engineering from Istanbul Technical University, Turkey, in 2018 and 2020, respectively. He was with Ericsson, Istanbul, Turkey working as a Networks Researcher. Since August 2020, he has been with The University of Edinburgh, United Kingdom, where he is currently both Ph.D. student and Marie Curie Early Stage Researcher. His research interests include energy efficiency in cellular networks and light communication.



Wasiu O. Popoola (S'05 – A'12 – M'13 – SM'16) is currently a University Senior Lecturer with the School of Engineering, Institute for Digital Communications, University of Edinburgh, U.K. He has published over 100 journal articles/conference articles/patent and over seven of those are invited articles. He also coauthored the book *Optical Wireless Communications: System and Channel Modeling with MATLAB* and many other book chapters. His primary research interests include digital and optical communications.