

# Development of a dual optical fiber probe for the hydrodynamic investigation of a horizontal annular drive gas/liquid ejector

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## Abstract

A dual-channel optical fiber probe was developed to quantify the bubble characteristics (void fraction, velocity, and bubble size) in a gas–liquid annular ejector system. Water is pumped upstream of the ejector contraction. Since a low pressure region exists downstream in the ejector diffuser, this permits air to be sucked into the flowing liquid by jet pump action and the inlet air volumetric flow rate is measured by a flow meter. Verification of the void fraction (range 0.15 – 0.5) measured by the optical fiber probe was then possible and deviations were generally around  $\pm 5\%$ . Also, bubble velocity was measured using the optical probe by cross-correlating signals from the two fibers whose tips are separated by a known distance. Alternatively measuring bubble velocity using a particle image velocimetry method provided validation for the optical fiber probe system where a high speed camera was used to capture instantaneous bubble images at time intervals of 0.125 ms. Excellent agreement between the velocities using both methods is reported. For bubble size measurements, analyzing the temporal signals from a single probe enabled estimation of the size of a bubble. Bubble sizes measured ranged between 1.5 and 6.0 mm and size distributions were constructed for different ejector water volumetric flow rates ranging from 0.0022 to 0.0063 m<sup>3</sup>/s. LabVIEW provided a convenient platform for coding the algorithms for estimating the void fraction, bubble velocity and bubble size. For further comparison, a CFD study of the ejector system was done, and the vertical radial profiles of the void fraction were compared with those obtained by the optical fiber system and these showed good agreement.

**Keywords:** Fiber optic probe, Fresnel reflection, bubbly flow, annular ejector, void fraction, CFD.

## 1 Introduction

Measurements of local flow characteristics in gas–liquid systems are important for both their design and operation. Of particular importance are industrial applications where bubbly flow occurs due to the high mass transfer and reaction rates that can occur during gas–liquid contacting. Examples of such applications in industry include absorption and stripping [1], aerobic biochemical reactors for large-scale waste water treatment plants [2], hydrogen recirculation devices in proton exchange membrane

34 fuel cell (PEMFC) systems [3], and vapor compression refrigeration systems [4]. Nowadays,  
35 preliminary designs using computational fluid dynamics simulations are increasingly being carried out,  
36 and information on bubble interfacial area is needed. Therefore, knowledge of bubble properties such  
37 as void fraction, bubble velocity, and bubble size distribution are of utmost importance.

38 In a brief review for their paper, Mizushima et al. [5] noted that over the years, many methods  
39 have been devised for the measurement of bubble characteristics in multiphase flows. These include  
40 measuring void fraction by the level of an aerated liquid in comparison with the single phase liquid in  
41 a bubble column [6]; high-speed photography and image processing [7]–[9] for bubble rise velocity,  
42 mean diameter, and low void fractions respectively. Others are double sensor conductivity probes for  
43 bubble velocity and interfacial area concentration measurements [10]; gas holdup, bubble size and shape  
44 distribution using laser Doppler anemometry [11]; bi-optical fiber technique for low bubble velocity in  
45 an airlift column [12]; and highly intrusive wire mesh sensors for bubble void fraction measurements  
46 in conduit flows developed [13]–[15].

47 Serious complications can occur in measuring bubble characteristics while flowing such as  
48 intrusiveness, bubble distortion, and temporal resolution for high velocity bubbly flow. Use of optical  
49 fiber probes is one very promising technique that can satisfactorily reduce these shortcomings due to  
50 its high sensitivity to local phase changes that have different refractive indices. Indeed since the  
51 measuring principle of optical fibers governed by Snell's law was introduced to bubbles [16], both  
52 mono- and multi-fiber systems have been widely used in gas–liquid systems across chemical process  
53 and nuclear applications. For example [17] measured the local gas-phase characteristics in a bubble  
54 column in the presence of paraffin oil and nitrogen at high temperatures ( $T = 100\text{--}175\text{ }^{\circ}\text{C}$ ) using a  
55 mono-optical fiber probe at low gas velocities of between 0.02 and 0.15 m/s. Xue et al. [18] used four-  
56 point optical probes to obtain the bubble velocity vectors and bubble size using the calibration technique  
57 between the probes and a charge-coupled device (CCD) camera to correct for bubble distortion.  
58 However, while the likely obtrusiveness of a four-probe system exists, it was not clear from their study  
59 its ability to adequately measure high velocity bubbly flows. Enrique Julia et al. [19] investigated the  
60 accuracy of the fiber optic probe vis-à-vis its distorting, and non-perpendicular piercing effect on the  
61 bubbles. A synchronized high speed camera was used with bubble velocities of 0.22–0.28 m/s. No  
62 specific application was mentioned and a correction method was not proffered.

63 From the foregoing while a variety of systems have been used, and various corrections applied  
64 to cater for bubble distortion, it is evident optical fiber application to relatively high velocity bubbly  
65 flows e.g. finely dispersed bubbly flow has not been reported in the open literature where mixture  
66 velocities can approach 5 m/s. One of such applications is in gas/liquid ejectors where a high velocity  
67 liquid is pumped through a conduit which has a venturi-type constriction. Ejectors utilize a high speed  
68 fluid jet as a pumping resource to entrain a secondary phase (e.g gas) into the suction chamber. Pumping

69 of the secondary fluid is possible because a low pressure region is formed downstream the ejector  
70 expansion region at high velocities, and the secondary fluid is hence sucked into this region. Ejectors  
71 have found wide applications in liquid–liquid and gas–liquid contacting systems such industrial units  
72 in mixer/settler systems, micro- and milli-bubble formation for water treatment and turbulence  
73 enhancers in bubble column reactors, and heat transfer applications.

74 In this study, a hydrodynamic investigation was performed on an annular drive gas/liquid  
75 ejector using a dual optical fiber probe specifically developed to measure the bubble characteristics  
76 (void fraction, velocity, and bubble size). The gas superficial velocities were between 0.6–1.8 m/s in a  
77 65 mm internal diameter horizontal pipe. Verification of the void fraction and bubble size distributions  
78 was carried out using alternative methods, as well as the bubble velocity. For comparison purposes, a  
79 CFD study of the ejector system is also performed, and the vertical profiles of the void fraction obtained  
80 are compared with those obtained by the optical fiber system.

## 81 **2 Measuring principle of the optical fiber**

82 The optical fiber probe system was developed to estimate the local void fraction, bubble velocity and  
83 bubble diameter. The measuring principle is based on the Fresnel reflection occurring at the interface  
84 between the two media with different refractive indices [20]. Therefore the Fresnel coefficient at the tip  
85 of the probe is dependent upon the refractive index of each phase; and for normal light incident at an  
86 interface between air and water with refractive indices of  $n_1$  and  $n_2$  respectively, the Fresnel  
87 coefficient  $R$  is given by:

$$R = \left( \frac{n_1 - n_2}{n_1 + n_2} \right)^2 \quad (1)$$

88 For an air–water mixture together with a fiber index of  $n_1 = 1.46$ , the following Fresnel coefficients  
89 are obtained:

90  $R_{g-a} = 3.5\%$  (*glass – air*)

91  $R_{g-w} = 0.2\%$  (*glass – water*)

92  $R_{w-a} = 2.0\%$  (*water – air*)

93 According to the Fresnel reflection, approximately 3.5% of the incident light is reflected backward to  
94 the interface between glass and air, but less than 0.2% of incident light is reflected at the interface  
95 between glass and water; and 2% is reflected at the air–water interface. When the tip of the probe is in  
96 contact with water,  $R$  is approximately 17.5 times higher than when it is in contact with air. Therefore,  
97 the amount of light reflected changes with the change in the medium in contact with the probe. The  
98 voltage level was thereafter detected using the changes recorded by the photodetector, and the signal

99 difference can be used for estimating the void fraction. The illuminated light from the light source and  
100 the reflected light at the tip of the probe along the water-air interfacial plane reached the optical fiber  
101 probe and the photodetector, respectively, through the beam coupler. The light reaching the  
102 photodetector was estimated as an electronic signal voltage, and this voltage data was acquired by the  
103 DAQ board and stored in the computer in real-time. High temporal/spatial resolution and stability of  
104 the output signal are the key advantages of measuring the void fraction using an optical fiber probe.

### 105 **3 Probe fabrication**

106 The optical fiber used was FOSTEC 3.0 mm Type OFNR, with 125  $\mu\text{m}$  and 50  $\mu\text{m}$  cladding and core  
107 diameters respectively. The tip of the probe was fabricated using precision hand-held Thorlabs fiber  
108 stripper and cleaver devices (shown in Figure 2) to remove the outer buffer regions, and cut the tip  
109 perpendicular to the fiber axis.

110

#### 111 **Figure 1: Hand-held precision tools for optical fiber probe fabrication**

112 A micro-grinder/microscope device was used to inspect and finely finish the exposed optical  
113 fiber ends to ensure good quality signals are obtained. These were carefully mounted as a pair in a 20G  
114 hypodermic steel pipe, which was in turn inserted to a 1/16-inch pipe and epoxy glue was applied to  
115 hold them in place. Finally, they were glued in a 1/8-inch pipe to form a solid probe assembly. The  
116 distance between the two exposed probe tips  $\Delta h$  was measured under a microscope as shown in Figure  
117 2. As the size of the probe was very small, measuring the distance accurately was difficult. In advance,  
118 we captured a calibration image with a superimposed ruler and the probe under the microscope. This  
119 enabled the distance per pixel of the image to be calculated. Using image-processing software, the  
120 separation between the two probe tips was determined in pixels, and this was converted to micrometers  
121 using the  $\mu\text{m}/\text{pixel}$  calibration value. This was done three times and a mean value obtained. For the  
122 probes used in the current experiments the tip-to-tip separation  $\Delta h$ , was determined to be 600  $\mu\text{m}$ .

123

#### 124 **Figure 2: Close-up details of dual fiber tips and measurement under a microscope**

### 125 **3.1 Validation of probe velocity measurements using rising bubble experiments and a high** 126 **speed camera**

#### 127 **3.1.1 Description of high speed camera system**

128 In the current experiments, an 8,000 fps frame rate was used to acquire reasonable velocity vector fields.  
129 The depth of focus should be minimized because the lens receives the volume-averaged diffraction  
130 images. The 60 mm lens with  $F = 8$  was chosen so the estimated depth of focus was shorter than 5 mm.

131 The focal plane was placed at an offset distance one-quarter the nozzle diameter behind the central  
132 plane, to enable sharper bubble images to be obtained. A 12W LED lamp was used as a continuous  
133 volume illuminator. Figure 3 is a picture and schematic diagram of the experimental apparatus for  
134 making measurements of the size and velocity of passing bubbles showing the camera setup. A circular  
135 transparent acrylic cylindrical tank with a diameter of 0.3m was used. In order to prevent the distortion  
136 of the image, it was placed in an acrylic rectangular tank filled to an appropriate level with water. Air  
137 injection nozzle was placed in the center of the tank bottom with a diameter of 5 mm. Compressed air  
138 is supplied to the nozzle via a control valve and the flow rate of the air is precisely controlled by a flow  
139 meter. Flow rates of compressed air used were 1, 3, and 5 liter/min.

140

141 **Figure 3: Experimental setup for probe validation and synchronization timing chart**

### 142 3.1.2 Analysis of probe signals for bubble velocity and size measurements

143 Figure 4 shows the time-varying output signal of the fiber optic probe and the corresponding  
144 synchronized image from the high-speed camera. Signals obtained first had to undergo filtering to get  
145 rid of noise. This was done by setting a cut-off level assuming a 95% confidence level, such that signals  
146 outside this threshold are filtered out, and smoother, sharper output signals result.

147 As shown in Figure 5 (b) it can be seen that the moment the first probe hits the upper boundary  
148 of the bubble is 0.1104 s. This indicates a sudden jump in the signal from 0.1 to 1.4 V at the same time  
149 stamp. For the second probe this occurs at exactly in the 0.1146 s as recorded by both graph and high  
150 speed image. An error of 0.0002 s exists due to the reflected light in accordance with the three-  
151 dimensional shape of the bubble as the signal steps-up at 0.1248 before the bubble hits the probe and  
152 reaching full steady signal at 0.125 s. At the exit of the probe from within the bubble to the water, the  
153 same lag is seen between the signal and the image signal at 0.13 s and 0.1288 s respectively. At 0.135 s  
154 there is no reflected light from both probes indicating full exit from within the bubble.

155

156 **Figure 4: Signals from two optical fiber probes and images taken by synchronized high speed camera.**

157 The time delay  $\Delta t$  between the signals is determined by a cross-correlation algorithm and all  
158 computations were done in LabVIEW. Thus, based on the measurement signals from the two probes,  
159 the rise velocity of the bubble  $V_b$  can be precisely calculated since the probes' separation  $\Delta h$  has been  
160 previously determined to be approximately 600  $\mu\text{m}$  as earlier described:

$$V_b = \frac{\Delta h}{\Delta t} \quad (2)$$

161 In addition, by multiplying the rising speed and the transit time within the gas phase for a

162 single probe, we can measure the chordal length of the air bubbles. Here, an assumption is that the  
 163 bubble motion between the probes is uniform; hence, the bubble size can be expressed as:

$$D_b = V_b \times t_r \quad (3)$$

164 where,  $t_r$  is the residence time of the bubble as it traverses a single probe. Bubble size is estimated to  
 165 within a mean value of 2% error between the two probes. As an example, the size of the bubbles was  
 166 measured by 3.43 mm from the first probe, was measured to be 3.47 mm in the second probe. A change  
 167 in length of 0.04 mm while the air bubbles pass through the probes, which is a 1.2% error compared to  
 168 the average size of the bubble. Three repeated tests of each condition reveal that the maximum of such  
 169 errors are around 5% with a mean of around 2%. It should be noted that this error estimate was obtained  
 170 for ideal cases where the bubbles were approximately spherical, and probes penetrate the bubbles at  
 171 the near the midpoint.

172 Since length per pixel calibration was done, the bubble speed and size were able to be validated  
 173 using the images from the high speed camera as given in Figure 4 (b). Results of measuring bubble  
 174 chordal length at the nozzle exit, and beneath the free surface, as well as mean rise velocities are given  
 175 in Table 1 for three different inlet air volumetric flow rates.

176 **Table 1: Bubble diameters and rising velocity at different air flow rates**

$Q_{air}$ (liter/min)	$u_{air}$ (m/s)	$D_b$ (mm) at the nozzle exit	$D_b$ (mm) below the free surface	$V_b$ (m/s)
1	3.3	12.2	18.1	0.46
3	9.8	16.7	24.2	0.60
5	16.4	21.0	29.6	0.75

177 As can be seen, the bubble sizes increase with inlet airflow rate, and these consistently grow  
 178 to 1.5 times their original sizes upon rising to the water surface. This is consistent with their expansion  
 179 during rise to the lower hydrostatic pressures of the lesser water depths. For the bubble rise velocities,  
 180 an increase occurs with increase in inlet air flow rates. It can be seen that the air velocity is highly  
 181 reduced when bubbles are formed on impact with the water due to opposing drag forces within the  
 182 liquid. However, rise velocity does not increase as fast as inlet velocity. A 5-fold rise in inlet velocity  
 183 only results in less than 2-fold increase in rise velocity; indicating more dominance by the liquid on  
 184 bubble properties than those of the gas. Further reading can be done on probe calibration, verification,  
 185 and general feasibility for use in bubbly flows have been published by the authors in previous papers  
 186 [21], [22]. Beneath.

#### 187 **4 Ejector experiments and void fraction measurements**

188 Figure 5 (a) shows a schematic diagram of the ejector experimental setup. Metered flow rates  
 189 of water used as the primary fluid were used to suck (or pump) atmospheric air, the secondary fluid.

190 The flow rate of air pumped is measured by an air flowmeter (KOBOLD model DOG1102) which was  
 191 installed at the entrance of the air inlet pipe and has measurement range of 0–0.0083 m<sup>3</sup>/s with an  
 192 uncertainty margin of ±1.5% of measured value. A centrifugal pump circulates tap water stored in a  
 193 water tank and the inverter is used to control the water flow rate. The water volumetric flow rates used  
 194 were in the range of 0.0077–0.0092 m<sup>3</sup>/s. The water flow rate was measured using an electromagnetic  
 195 flow meter (KOBOLD model UMF2) which has an uncertainty margin of ±0.3% of full scale  
 196 measurement. The measured fluid flow rates can be used to determine the gas void fraction ( $\varepsilon_G$ ) in the  
 197 two-phase mixture as follows:

$$\varepsilon_G = \frac{Q_g}{Q_g + Q_l} \quad (4)$$

198 where  $Q_g$  and  $Q_l$  are the gas and liquid volumetric flow rates (in m<sup>3</sup>/s) measured by the respective  
 199 flowmeters. Water enters the gas/liquid ejector, through a strainer and then mixes with air. Downstream  
 200 of the ejector, bubbly flow results.

201

202 **Figure 5: Setup for ejector experiments (a) schematic showing ejector loop and measuring devices (b)**  
 203 **detailed specification of the annular drive gas/liquid ejector**

204 Pressure measurements were carried out using six 2-wire 4–20 mA output transducers (SUCO  
 205 model DR-10) with measuring uncertainty of ±0.25% full scale. The notation, location and  
 206 measurement range of each transducer is as follows:  $P_i$  (upstream of ejector) 0–500 kPa;  $P_l$  (suction  
 207 chamber) -10–0 kPa;  $P_m$  (center of mixing throat) -10–0 kPa;  $P_d$  (outlet of diffuser) -5–15 kPa;  $P_A$   
 208 (inlet of air pipe) -10–5 kPa; and  $P_{out}$  (outlet of visualization section) -5–35 kPa.

209 In Figure 5 (b), the dimensions of annular drive gas/liquid ejector are given. The inlet and outlet  
 210 inner diameters are 67 and 69 mm, respectively. The diameter of the ejector venturi neck is 32 mm and  
 211 the inner diameter of the air inlet, 13.5 mm. The lengths of the converging and diverging sections are  
 212 42 mm and 91 mm respectively. In contrast to the conventional gas/liquid ejector, the primary fluid  
 213 flows annularly around the central air nozzle and air is sucked into the ejector unit.

214 The high-speed camera (Photron, SA1.1) capable of capturing at speeds of up to 10,000 fps was also  
 215 installed for the flow visualization with a back illuminator. All measuring devices were connected to an  
 216 8-channel National Instruments NI9401 DAQ digital acquisition boards and data captured were logged  
 217 and stored on a PC. Installation of the optical fiber probe system was done on a traversing device as  
 218 shown in Figure 6 (a). This facilitates measurements along the radial direction of the horizontal tube.

219 Figure 6 (b) is an example of filtered instantaneous signals obtained from the two probes at  $Q_l =$   
 220 0.0077 m<sup>3</sup>/s. Due to the high sensitivity of optical fiber probes in sensing changes in refractive index

221 between different media, passing bubbles produce clear discrete fluctuations in the measured signals,  
 222 each signifying the passage of a single bubble. Tiny overlaps can be seen between the two signals and  
 223 the time stamps are accurately recorded at 8,000 Hz by the LabVIEW DAQ and software, which for 10  
 224 s recording, results in 24,000 data points. The void fraction is then determined using an algorithm based  
 225 on Equation (5) coded in the acquisition software.

226

227 **Figure 6: (a) Two-channel probe, traversing device, and associated equipment (b) example of**  
 228 **instantaneous signals from the two probes during ejector experiments showing distinct detection of**  
 229 **passing bubbles at  $Q_L = 0.0077 \text{ m}^3/\text{s}$**

230 The measuring spot was located 0.35 m away from the visualization area, as shown in Figure 7 (a).  
 231 Associated optical fiber equipment manufactured by Thorlabs Inc. were used: an illuminator to provide  
 232 a continuous light source (1550 nm, S1FC1550), beam coupler (6015-3-FC), and photodiode (1.2 GHz  
 233 DET01CFC/M) which converts the reflected light to output voltage signals.

234

235 **Figure 7: (a) Installed location of the fiber optic probe (b) void fraction determination**

236 To determine the void fraction using the optical fiber probes, signals from a single probe can be used.  
 237 An algorithm determines a step function  $f(t)$  which can only take binary values depending on if the  
 238 probe is in the liquid phase ( $f(t) = 0$ ) or gas phase ( $f(t) = 1$ ). Therefore, the void fraction is  
 239 determined by the summation of the areas under the graph of such a function divided by the total length  
 240 of time  $\Delta T$  which the signals were acquired. Each area is bounded by the transit time  $\Delta t_i$  through a  
 241 gas bubble as shown in Figure 7 (b). Hence, as defined [20], [23], the void fraction at a certain radial  
 242 position for a particular flow condition is calculated as follows:

$$\varepsilon_G = \frac{1}{\Delta T} \int_0^{\Delta T} f(t) dt = \frac{\sum_i \Delta t_i}{\Delta T} \quad (5)$$

243 Figure 8 shows the radial void fraction distribution as the optical fiber probe vertically  
 244 traverses the pipe along the radial direction. These were obtained at different water volume flow rates  
 245 as indicated. The gas void fraction ( $\varepsilon_G$ ) was calculated using  $Q_G/(Q_L + Q_G)$  as given in Equation (4).  
 246 Figure 8 (b) shows the effect of water flow rate on gas pressure. It can be seen that as the water flow  
 247 rate is increased, the gas backpressure increases and as a result, the void fraction. This is in agreement  
 248 with the fact that as water flow rate increases, larger pressure drop occurs across the contraction thereby  
 249 creating more suction at the air inlet to balance the pressure deficit. The average of each measured radial  
 250 void fraction showed good agreement with that estimated using the volumetric flow rates (See Figure  
 251 8 (c)). Due to gas expansion under buoyancy as the bubble rises, the void fraction at bottom was found



252 to be lower than that at the upper side.

253

254 **Figure 8: Comparison of the vertical profile of the void fraction (a) different water flow rates at 12 kPa**  
255 **pressure, (b) different gas pressures for  $Q_L = 0.0087 \text{ m}^3/\text{s}$  (c) comparison between mean measured values**  
256 **and the calculated values at the different flow rates**

#### 257 **4.1 Discussion on ejector bubble velocity and size distributions**

258 Probability density functions (PDFs) were obtained from the bubble velocity measurements for  
259 each water volumetric flow rate condition. These are plotted as shown in Figure 9 together with the  
260 cumulative distribution function which sums up to unity. Measured bubble velocities varied in the range  
261 of 2–5 m/s with increasing peak values as liquid volumetric flow rate increases indicating the liquid  
262 being the principal driving phase.

263

264 **Figure 9: Bubble velocity distribution at  $y/h=0.3$  ( $P = 12 \text{ kPa}$ )**

265 A comparison is made between the measured bubble velocity using the optical fiber probes,  
266 the mixture velocity (calculated as  $[(Q_L/A_L) + (Q_G/A_G)]$ ) and the superficial liquid velocity at the  
267 aforementioned four  $Q_L$  values. Where  $A_L$  and  $A_G$  are the respective pipe areas for the liquid and  
268 gas phases respectively. This is given in Figure 10. The error bars show that the measured velocity by  
269 the probes are within 5% of the mixture velocity. The water superficial velocity is an artificial velocity  
270 provided that the water phase fully fills the entire cross section of the pipe. On the other hand, in reality  
271 air also comprises some portion of the pipe cross-section. Hence, the mixture velocity is always higher  
272 than the water superficial velocity. The calculated mixture velocity showed good agreement with the  
273 velocity from the optical fiber probe.

274

275 **Figure 10: Comparison of the measured and predicted axial velocities downstream of ejector**

276 Figure 11 shows the bubble size distribution expressed by the probability density function as well  
277 as the cumulative density function. The range of bubble sizes was estimated to range from 1.5 to 6 mm.  
278 As can be seen, a variety of bubble sizes were produced by the ejector judging by the multimodal nature  
279 of distributions. As stated earlier (see section 3.1.2), penetration through bubbles may not be  
280 symmetrical and this can affect the normality of the size distributions. As a result, the shapes of the  
281 bubble size distributions in figures (a)–(d) were not similar to that of a standard normal distribution.  
282 Also contributing to the given shapes is the small number of samples (25) used to construct the graphs.  
283 It is expected that the distributions will approach normality with an increase in sampling size, and this  
284 will be implemented in future work.

285

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**Figure 11: Bubble size distribution at  $y/h=0.3$  ( $P_b = 12$  kPa)**

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**Figure 12: Variation of the mean bubble size with respect to  $Q_L$  at a pressure of 12 kPa**

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## **5 CFD simulation of the ejector setup**

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In the previous section, the measured void fraction was compared with the gas fraction ( $\epsilon_G$ ) and good agreement was observed between the values. For additional comparative purposes, CFD analysis using commercially available ANSYS/CFX software was used to simulate the ejector system and to obtain graphical information [27]. The CFX 12.1 User Guide recommended either the Eulerian mixture model or Eulerian particle model is available when analyzing bubbly flows where dispersed-phase volume fractions exceed 10%. Here, the latter was used since fairly well mixed homogeneous bubbly flows inside the ejector and the downstream pipe were observed during the experiments. For initialization, bubble mean diameter was given as 3 mm, based on experimental observations.

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The geometry was constructed using the exact dimensions of the experimental setup, and the 3D modeling parts for CFD analysis include ejector unit, visualization chamber and connecting circular pipes. We conducted a mesh dependency study and the optimal number of nodes chosen contained approximately 500,000 nodes. Three-dimensional tetrahedral/prismatic hybrid mesh was used as obtained by ICEM CFD 12.1. In flow setup dialogue, the air was assumed to be incompressible so as not to achieve supersonic speeds. Temperature was fixed as 25°C and air density 1.185 kg/m<sup>3</sup>. Water was taken as the continuous fluid with air being the dispersed fluid. The  $k-\omega$  based shear stress transport (SST) turbulence model and dispersed zero equation turbulence model were applied both phases [28]. In the SST turbulence model, wall adjacent cells should be located within the viscous sublayer, and generally recommended to be  $y^+ < 1$ . For this flow problem, the maximum deviations in the air flow rate predictions between a fine grid ( $y^+ = 1$ ) and coarse grid ( $y^+ = 100$ ) were less than 7%. Ultimately, a fine grid ( $y^+ < 10$ ) was chosen in the air pipe region and coarse grid ( $y^+ < 100$ ) in the two-

317 phase wall region. Velocity inlet and pressure opening condition with 5% turbulent intensity were  
318 applied to water and air as inlet boundary conditions. At the outlet, a pressure outlet boundary condition  
319 was applied. For outlet to atmospheric, an additional mesh was created for the simulation of the removed  
320 effect caused by the flexible hose connected the downstream elbow. Iterations continued until the  
321 residuals for each equation were less than  $10^{-4}$ .

322 Figure 13 illustrates the CFD results obtained showing contours for the water volume fraction. The  
323 section given is the cross-sectional axial view of the ejector system at different water volume flow rates.  
324 Gas intake was from atmospheric for all the conditions shown and low pressure regions at the ejector  
325 diffuser results in the air being sucked into the pipe by jet pump action. As can be seen, several bubbly  
326 flow regions occur, and their propagation length along the tube axis increases with increasing water  
327 flow rate. As expected, aeration was greatest at the immediate downstream of gas inlet judging by the  
328 void fraction contour and is more so at higher liquid flow rates. This may seem counterintuitive at first.  
329 However, it is reasonable considering that the increased velocity of the driving liquid phase means more  
330 air can be sucked in; and an elongation occurs of this highly aerated initial bubbly flow region.

331

332 **Figure 13: Void fraction fields under each operating condition**

333 The stratification of the regions is more apparent when radial cross-sectional views of the results are  
334 considered as shown in Figure 14. Cross-sections were examined at four streamwise positions located  
335 at the injector inlet, halfway the diffuser, at the entire length of the diffuser, and at an advanced straight  
336 tube location. These occur at 1.7, 48, 93, and 740 mm axial locations respectively downstream of the  
337 gas inlet. Homogeneous bubbly flow occurs at the diffuser outlet, and as observed earlier, this occurs  
338 in several regions. Considering the most developed flow cross-section as shown in Figure 15 (i.e.  
339 Section 4 at 0.74 m from the gas inlet), these regions are concentric, but with thicker water volume  
340 fractions at the bottom due to the effect of gravity. Initially, three bubbly flow regions occur at the lowest  
341 liquid flow rate considered ( $0.0077 \text{ m}^3/\text{s}$ ). At this condition, water volume fractions range between 0.6  
342 and 0.9 corresponding to void fraction ( $\varepsilon_G$ ) values of 0.1–0.4. The central core of highest value  
343 corresponding to  $\varepsilon_G \approx 0.4$  widens as the liquid flow rate is increased to  $0.0082 \text{ m}^3/\text{s}$  and it splits into  
344 two distinct regions of  $\varepsilon_G \approx 0.4 - 0.5$  thus increasing the bubbly flow regions from three to four.  
345 Further concentric stratification occurs as liquid flow increases to  $0.0092 \text{ m}^3/\text{s}$  with pipe core peaking  
346 of the void fraction. This core-peaking behavior is consistent with the experimental measurements of  
347 the void fraction using the optical fiber probes as the profiles given in Figure 8 show. Good quantitative  
348 agreement exists between the experimental void fraction and the simulated values. The combined  
349 experimental–CFD profiles are given in Figure 15, by comparing the local void fractions at 0.35 m from  
350 the air inlet. The coincidence between CFD and experimental local void fractions is very good at the

351 core region but under-estimations occur towards the wall. These may be due to limitations of the SST  
352 model at the boundary layer near the wall at the high Reynolds number conditions of the system and  
353 necessity of turbulence damping at the free surface towards the gas–liquid interface [29]. Nevertheless,  
354 overall deviation of  $\varepsilon_G$  between the experiment and CFD is satisfactory.

355

356 **Figure 14: Cross sectional void fraction distribution at different streamwise locations**

357

358 **Figure 15: Void fraction comparison between the experiment and CFD**

## 359 **6 Conclusion**

360 A dual fiber optic probe system was developed for the measurement of bubble parameters: mean  
361 velocity, size, and void fraction in gas–liquid bubbly flows in an annular drive ejector. These are  
362 important local parameters that not only enable further understanding of the flow behavior, but are used  
363 to obtain physical models of the interfacial area concentration for example, which is useful for the  
364 numerical simulation of bubbly flows. Optical fiber probes have the advantage of high sensitivity, and  
365 minimal intrusiveness due to their micrometer size, and can be used where other instrumentation are  
366 either difficult to deploy or do not give the high temporal resolutions obtainable with fiber optic probes.  
367 Experiments were carried out using a PIV method with bubbles as tracer particles to validate the  
368 readings of the probes and a high-speed camera system with the capability of 8,000 fps was used. Bubble  
369 velocities, and sizes measured by the fiber optic probe showed good agreement with those estimated  
370 using the high-speed camera system. Bubble size determination, sizes distributed in range 1.5 to 6 mm  
371 were obtained and mean bubble sizes decreased with increasing water flow rate due to bubble break-up  
372 by rising wall and gas/liquid shear stresses. Also, void fraction values were obtained using the  
373 developed optical fiber probes, and these showed good agreement with the sucked air fraction in the  
374 two-phase mixture as measured by a flowmeter. Numerical simulations were also performed for the  
375 ejector system using commercial CFD software ANSYS/CFX with the Shear Stress Transport model  
376 used for turbulence modelling. The trend of radial void fraction profiles obtained from the numerical  
377 simulations closely matched the experimental optical probe values.

## 378 **Acknowledgement**

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384 University, Republic of Korea.

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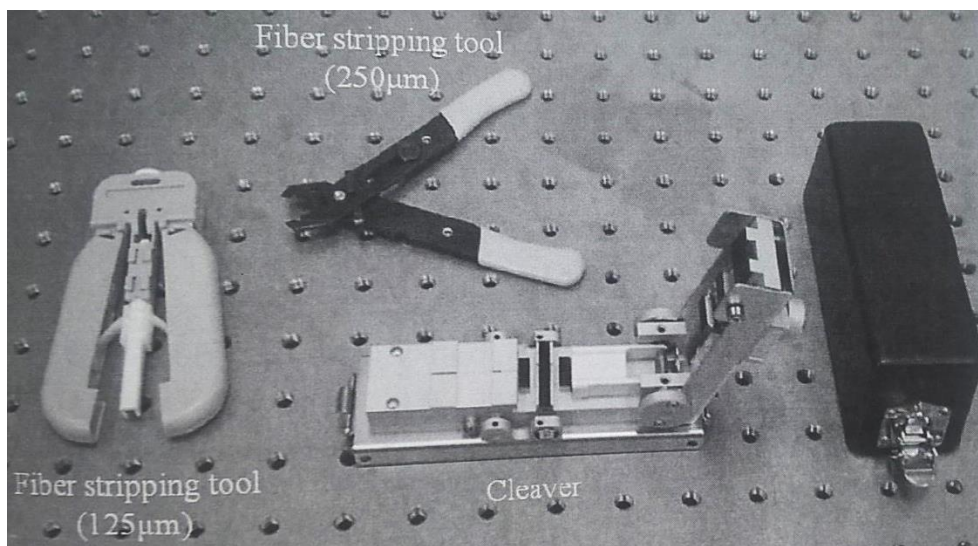
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## Figures



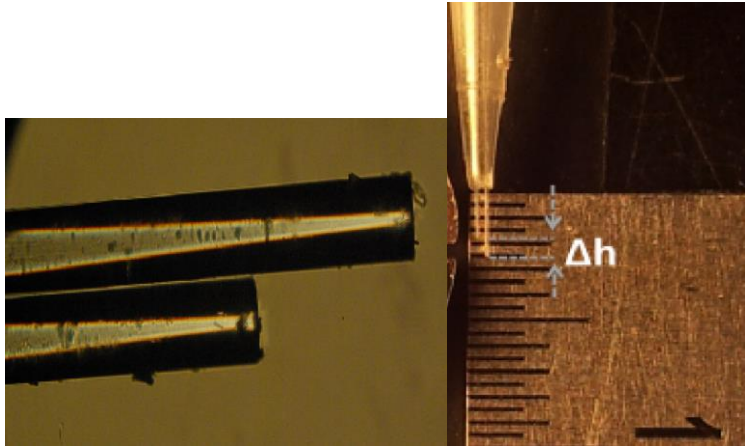
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**Figure 1: Hand-held precision tools for optical fiber probe fabrication**





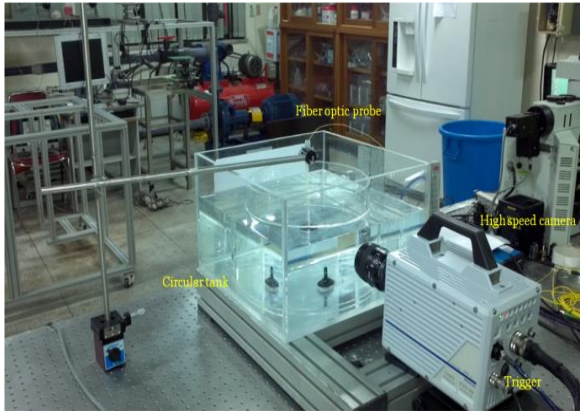
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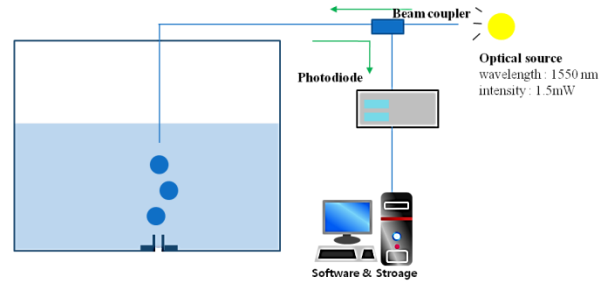
**Figure 2: Close-up details of dual fiber tips and measurement under a microscope**

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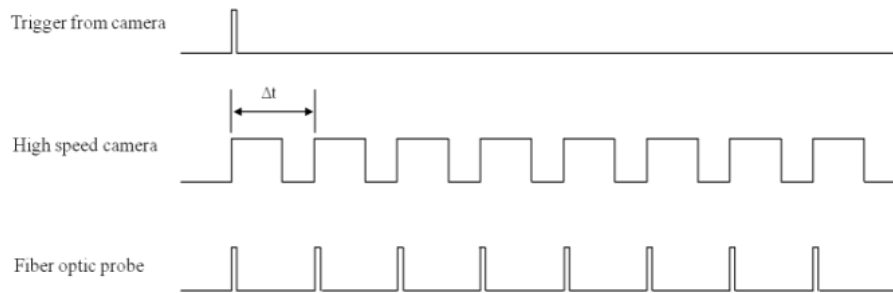
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(a) Setup for probe validation



(b) Schematic of setup

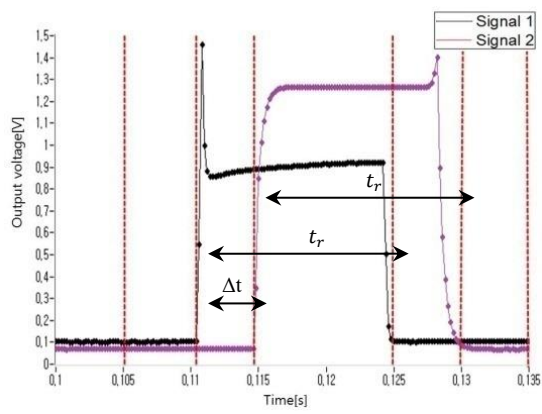


(c) Timing chart for probe and high speed camera synchronization

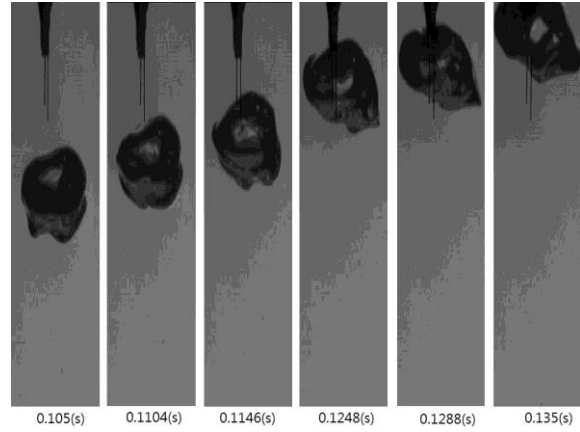
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**Figure 3: Experimental setup for probe validation and synchronization timing chart**

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(a) Temporal voltage signal form optical probes

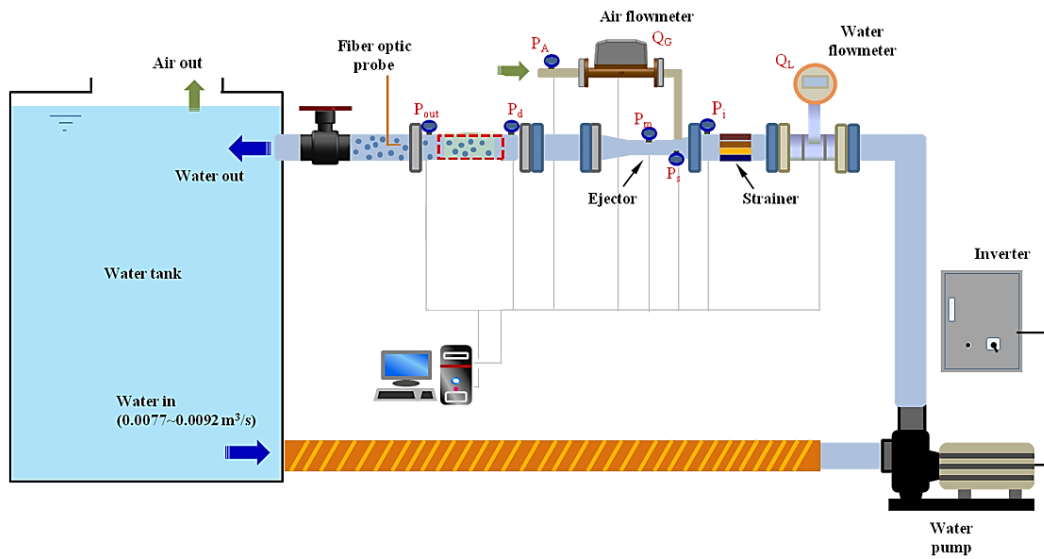


(b) Bubble images taken by the high speed camera

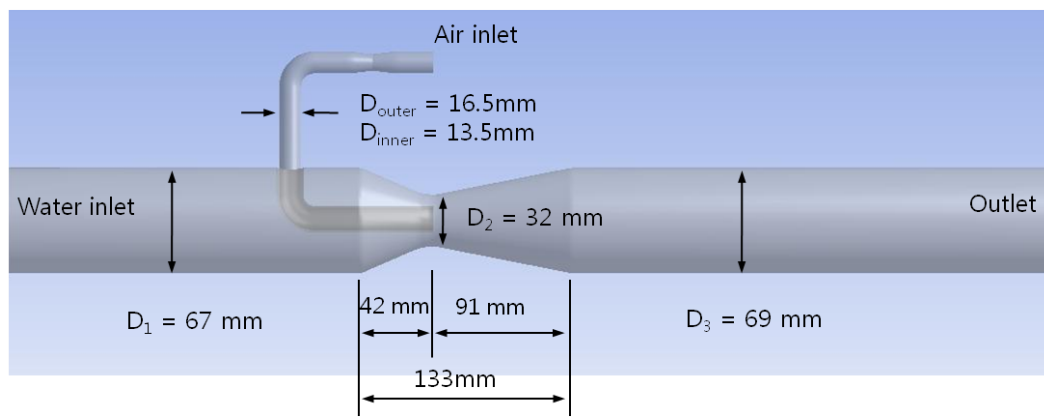
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**Figure 4: Signals from two optical fiber probes and images taken by synchronized high speed camera.**

475



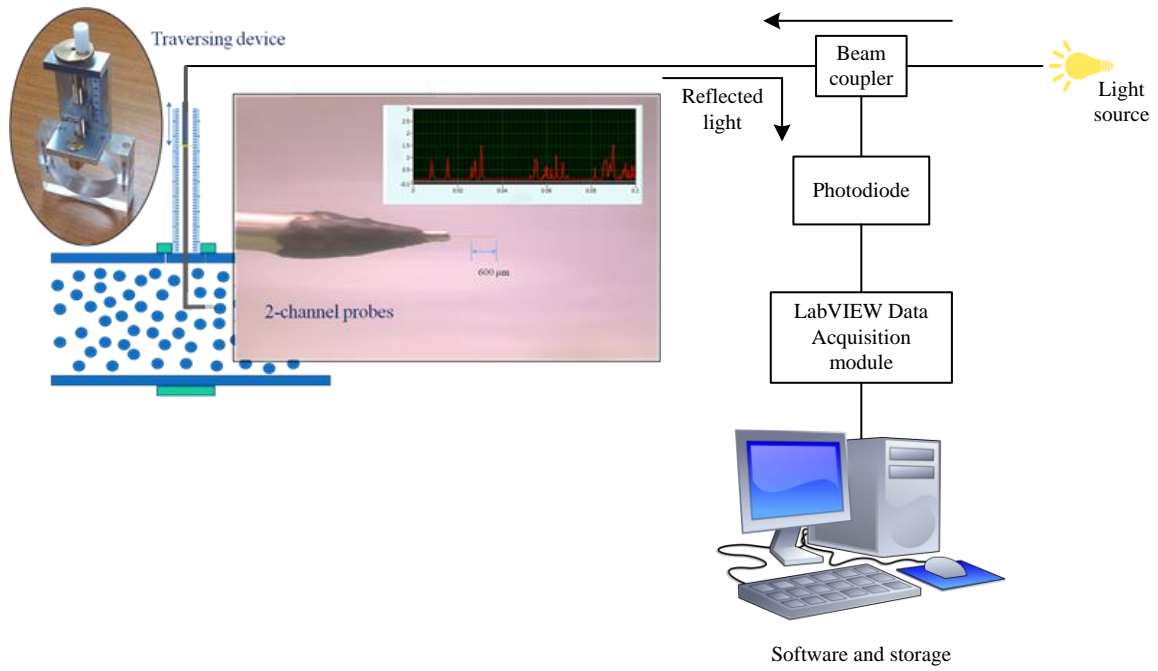
(a)



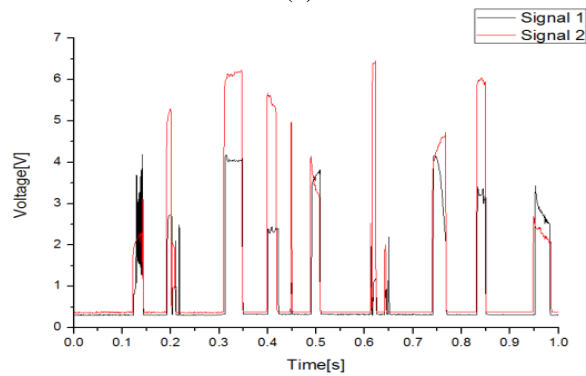
(b)

476 **Figure 5: Setup for ejector experiments (a) schematic showing ejector loop and measuring devices (b)**  
 477 **detailed specification of the annular drive gas/liquid ejector**

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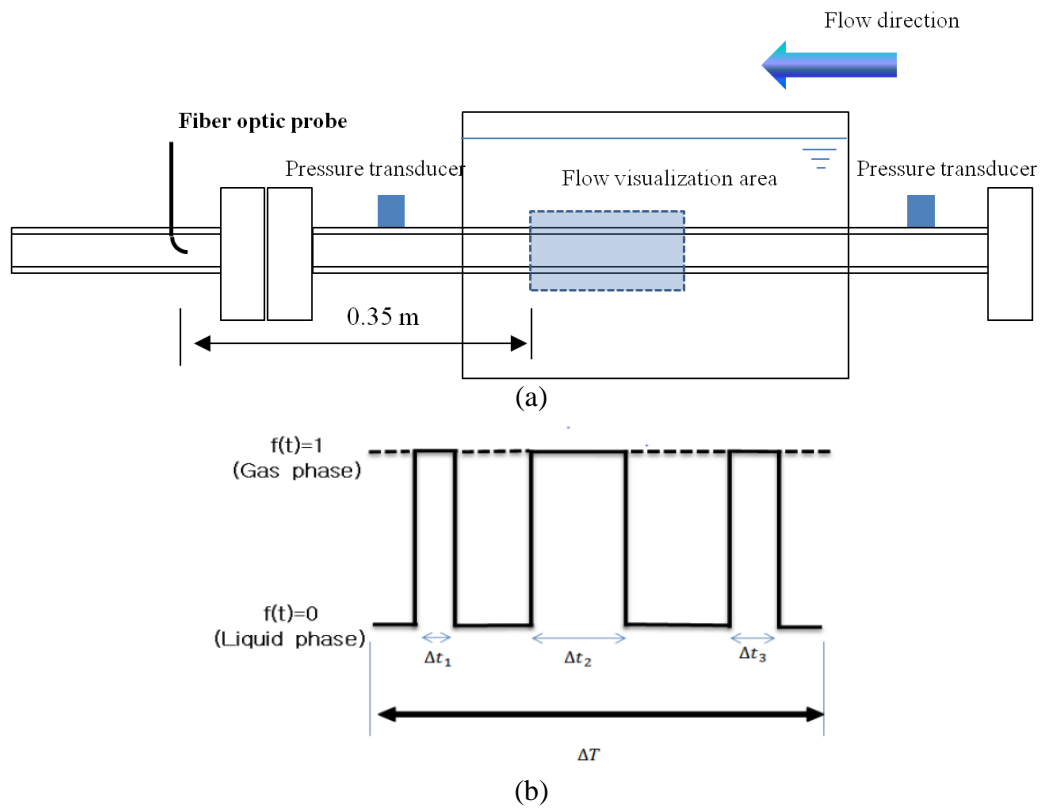
(a)



(b)

480 **Figure 6: (a) Two-channel probe, traversing device, and associated equipment (b) example of**  
 481 **instantaneous signals from the two probes during ejector experiments showing distinct detection of**  
 482 **passing bubbles at  $Q_L = 0.0077 \text{ m}^3/\text{s}$**   
 483

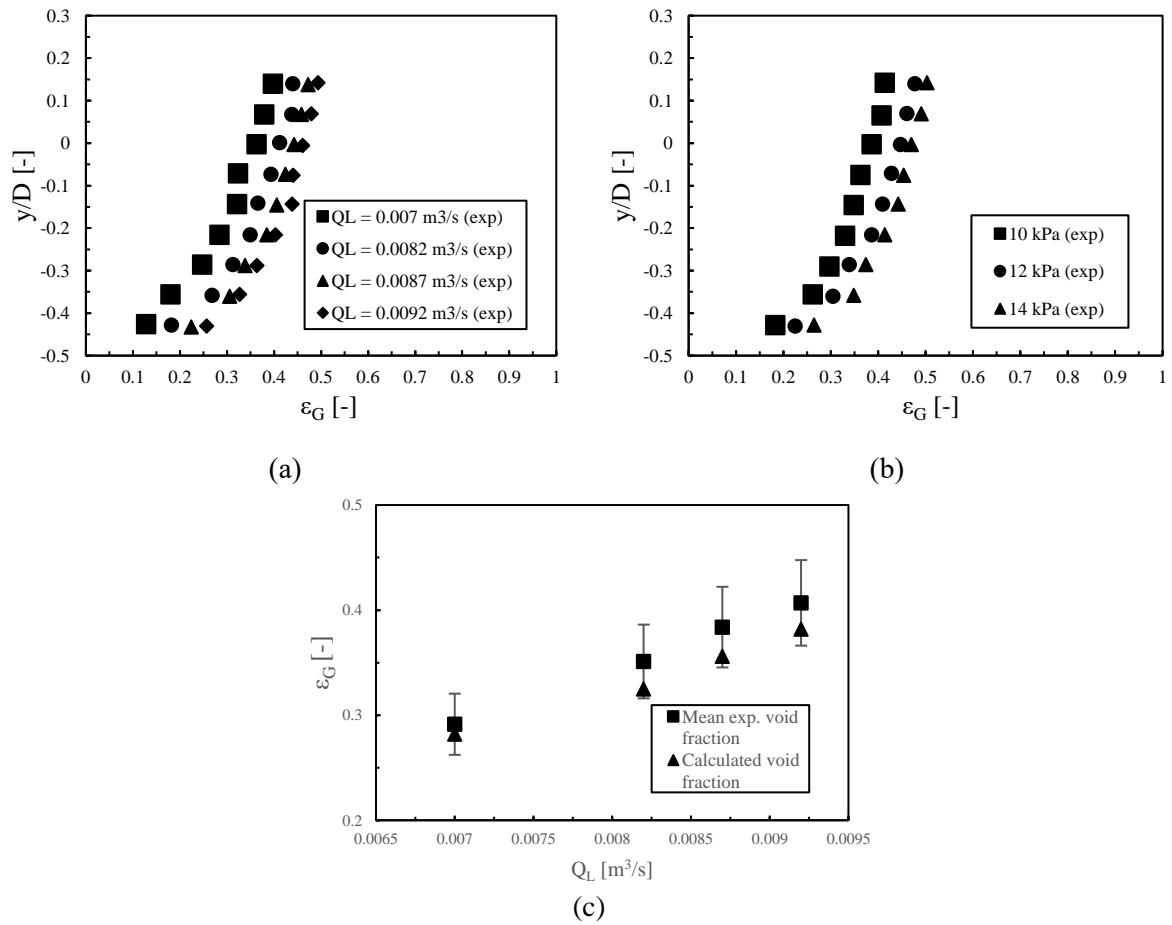
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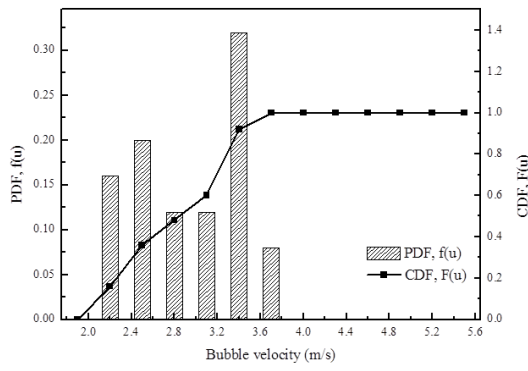
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**Figure 7: (a) Installed location of the fiber optic probe (b) void fraction determination**

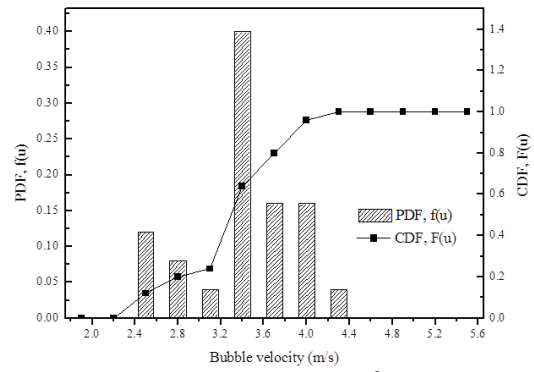
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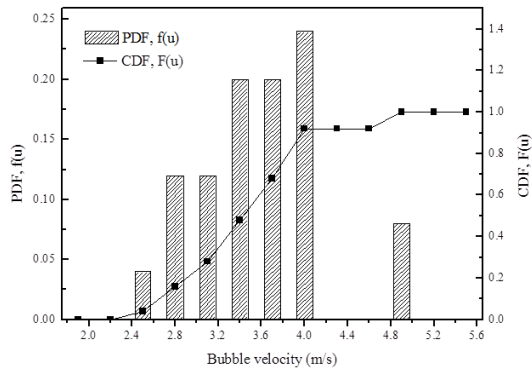
488 **Figure 8: Comparison of the vertical profile of the void fraction (a) different water flow rates at 12 kPa**  
 489 **pressure, (b) different gas pressures for  $Q_L = 0.0087$  m³/s (c) comparison between mean measured values**  
 490 **and the calculated values at the different flow rates**



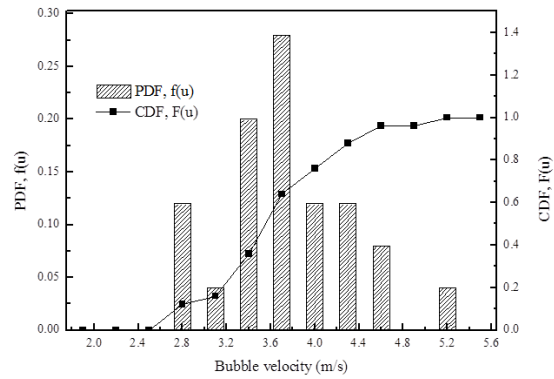
(a)  $Q_L = 0.0077 \text{ m}^3/\text{s}$



(b)  $Q_L = 0.0082 \text{ m}^3/\text{s}$



(c)  $Q_L = 0.0087 \text{ m}^3/\text{s}$



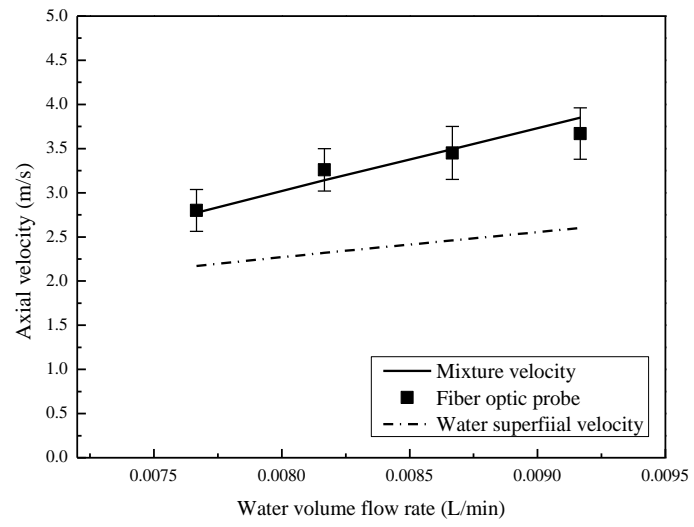
(d)  $Q_L = 0.0092 \text{ m}^3/\text{s}$

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**Figure 9: Bubble velocity distribution at  $y/h=0.3$  ( $P = 12 \text{ kPa}$ )**

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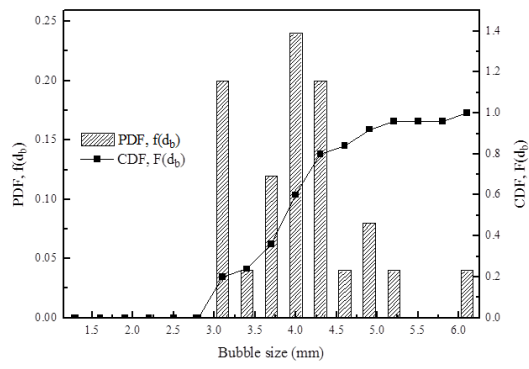


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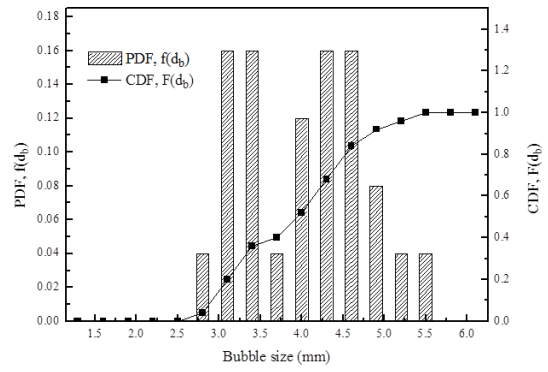
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**Figure 10: Comparison of the measured and predicted axial velocities downstream of ejector**

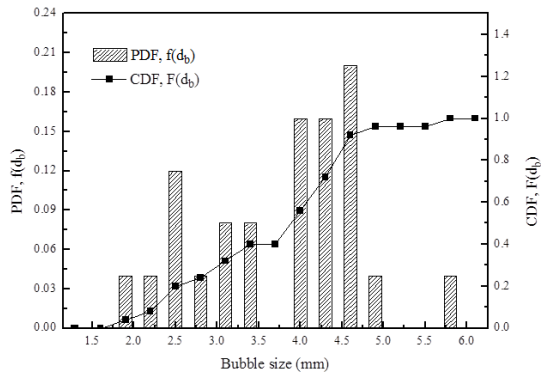
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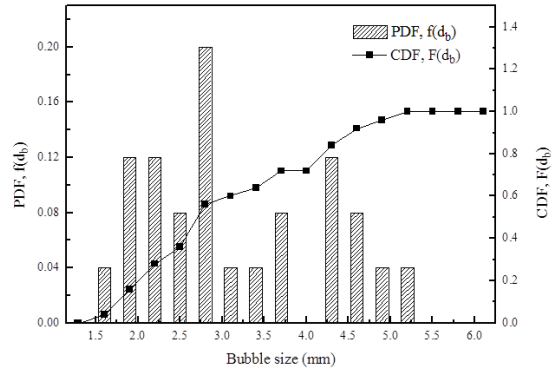
(a)  $Q_L = 0.0077 \text{ m}^3/\text{s}$



(b)  $Q_L = 0.0082 \text{ m}^3/\text{s}$



(c)  $Q_L = 0.0087 \text{ m}^3/\text{s}$

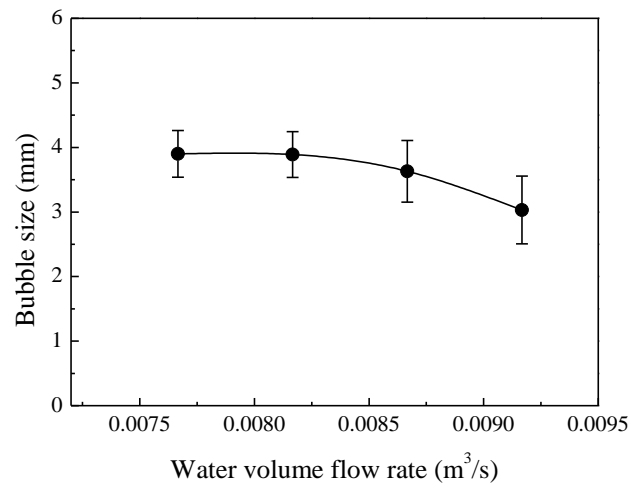


(d)  $Q_L = 0.0092 \text{ m}^3/\text{s}$

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**Figure 11: Bubble size distribution at  $y/h=0.3$  ( $P_b = 12 \text{ kPa}$ )**

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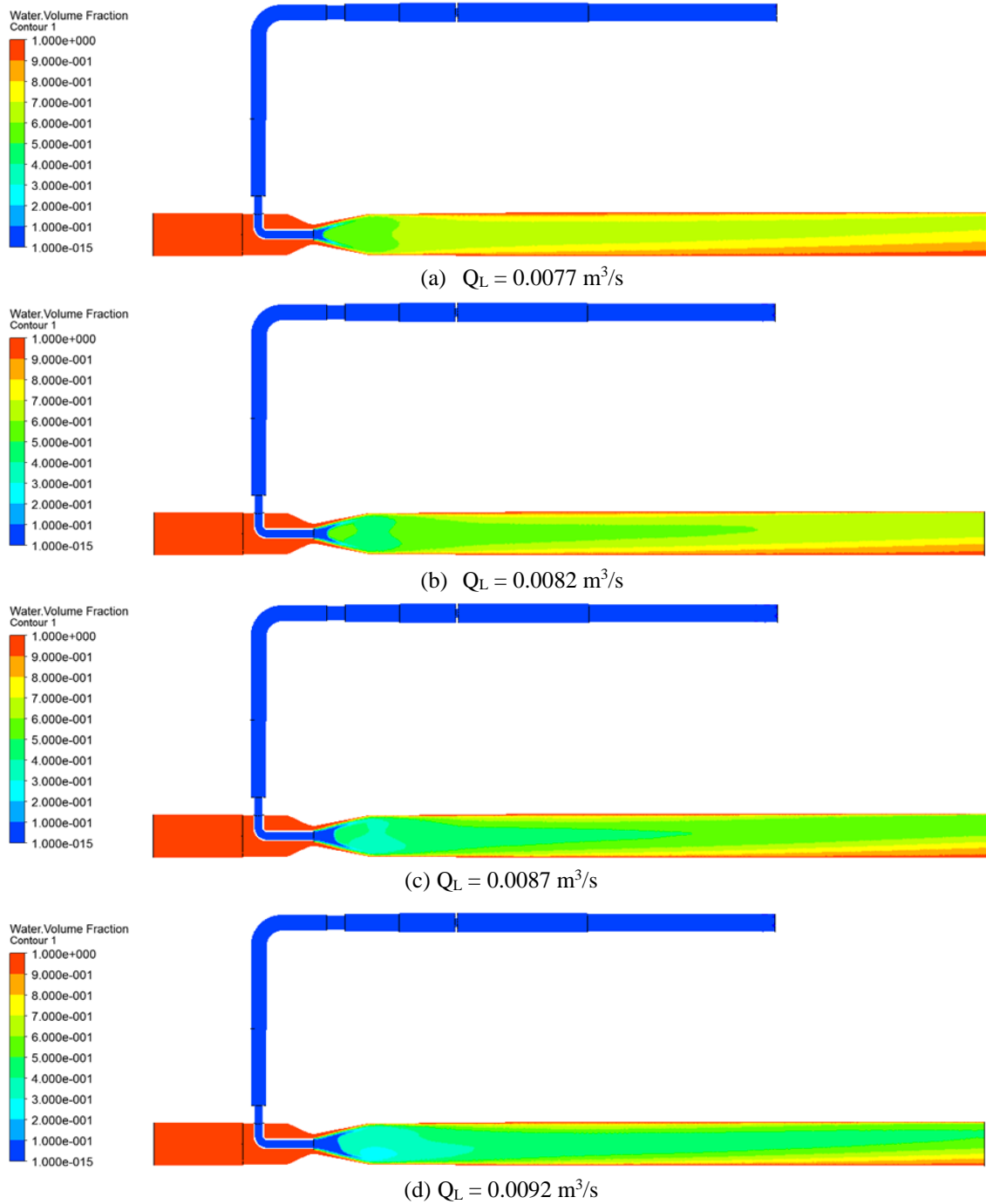


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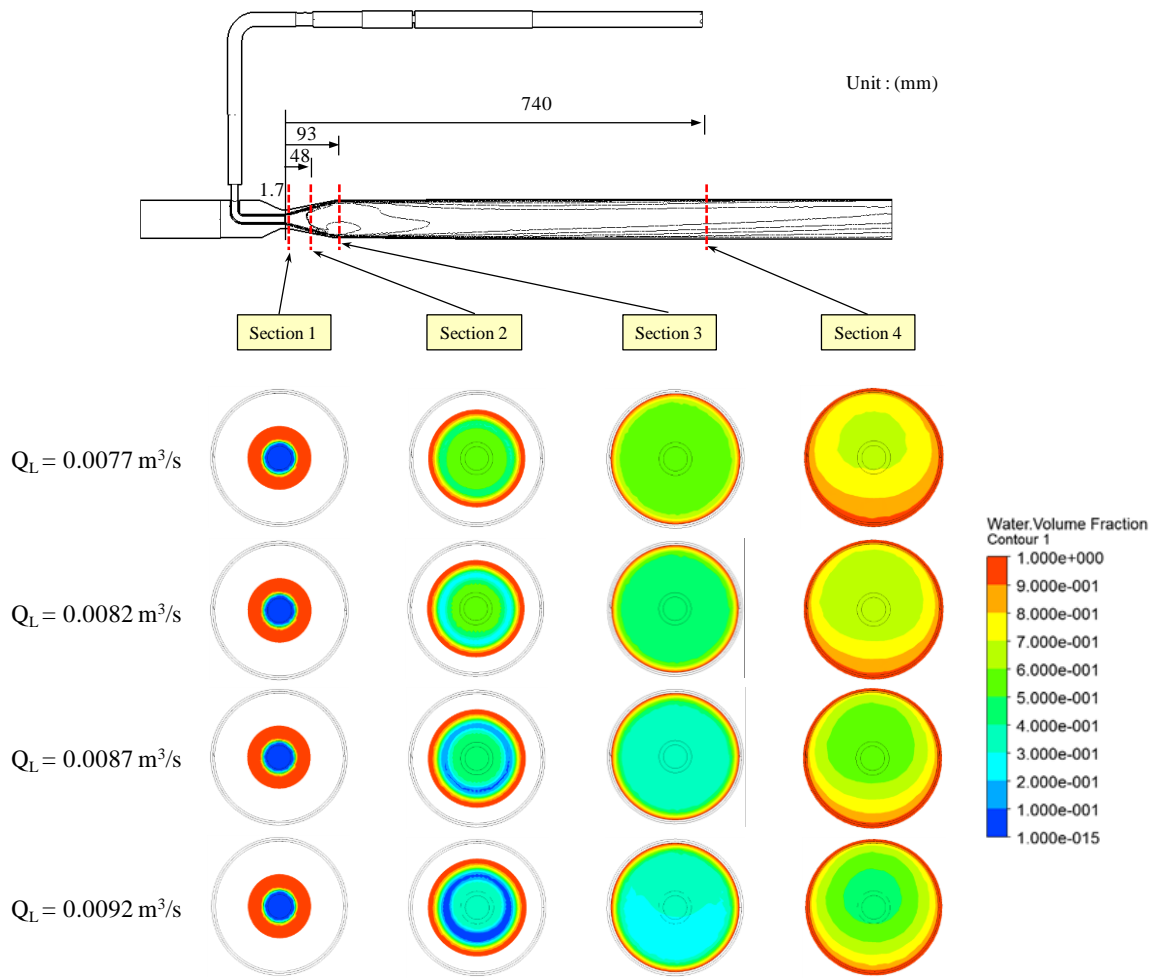
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**Figure 12: Variation of the mean bubble size with respect to  $Q_L$  at a pressure of 12 kPa**

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**Figure 13: Water volume fraction fields under each operating condition**

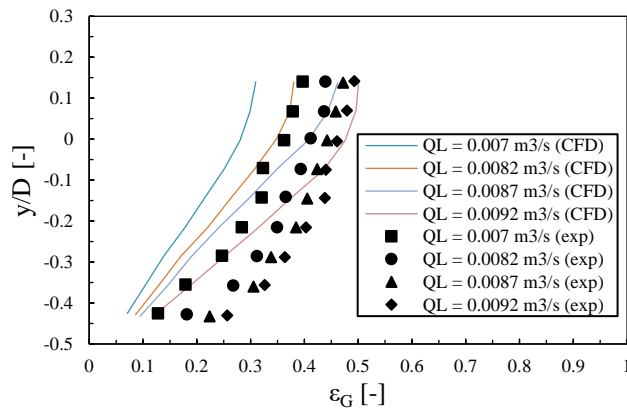


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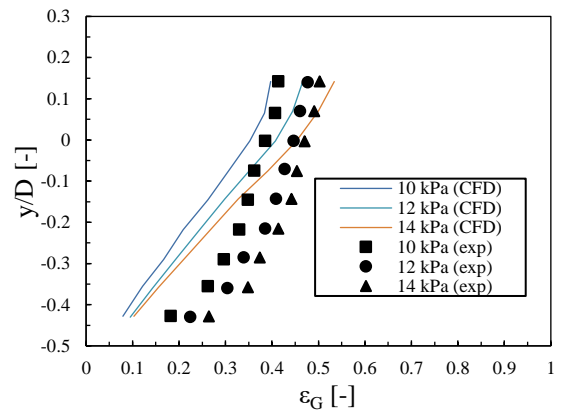
**Figure 14: Cross sectional water volume fraction distribution at different streamwise locations**

506

507



(a)  $P_b = 12 \text{ kPa}$



(b)  $Q_L = 0.0087 \text{ m}^3/\text{s}$

508

**Figure 15: Void fraction comparison between the experiment and CFD**

509

510