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Original paper

## Simulation of hypoxia PET-tracer uptake in tumours: Dependence of clinical uptake-values on transport parameters and arterial input function



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## ABSTRACT

Poor radiotherapy outcome is in many cases related to hypoxia, due to the increased radioresistance of hypoxic tumour cells. Positron emission tomography may be used to non-invasively assess the oxygenation status of the tumour using hypoxia-specific radiotracers. Quantification and interpretation of these images remains challenging, since radiotracer binding and oxygen tension are not uniquely related. Computer simulation is a useful tool to improve the understanding of tracer dynamics and its relation to clinical uptake parameters currently used to quantify hypoxia. In this study, a model for simulating oxygen and radiotracer distribution in tumours was implemented to analyse the impact of physiological transport parameters and of the arterial input function (AIF) on: oxygenation histograms, time-activity curves, tracer binding and clinical uptake-values (tissue-to-blood ratio, TBR, and a composed hypoxia-perfusion metric, FHP). Results were obtained for parallel and orthogonal vessel architectures and for vascular fractions (VFs) of 1% and 3%. The most sensitive parameters were the AIF and the maximum binding rate ( $K_{max}$ ). TBR allowed discriminating VF for different AIF, and FHP for different  $K_{max}$ , but neither TBR nor FHP were unbiased in all cases. Biases may especially occur in the comparison of TBR or FHP-values between different tumours, where the relation between measured and actual AIF may vary. Thus, these parameters represent only surrogates rather than absolute measurements of hypoxia in tumours.

## 1. Introduction

Hypoxia is known to negatively impact radiotherapy outcome [1,2]. Positron emission tomography (PET) can be used to assess the hypoxic status of tumours, using a hypoxia-specific radiotracer [3,4]. PET-based assessment of hypoxia has been found to be of prognostic value [5–7], and targeting hypoxia is a powerful therapeutic strategy for the individualized treatment of cancer patients [8,9]. Previous studies have shown that tracer kinetics in PET, represented as time-activity curves (TACs), can provide valuable information, although often only the static signal (e.g. two hours after tracer injection) is used. However, none of these methods have reached the status of clinically accepted routine and assessment of tumour hypoxia still imposes a great challenge [10]. The main obstacle lies in the limited understanding of the

radiotracer dynamics and its binding, which is heavily influenced by various physiological factors.

Mathematical modelling of the underlying processes of oxygenation and hypoxia [11–13], as well as of the hypoxia-PET tracer uptake distributions in tumours [14–23] provide a valuable tool to better understand the resulting PET signal.

The model developed by Mönnich *et al.* [17] allowed reproducing experimental TACs from patients, based on the current understanding on the involved microscopic processes. As for any model, input parameters must be provided and the obtained results therefore depend on such input. For radiotracer dynamics, input parameters modulate diffusion and binding in the tumour, as well as the delivery of the tracer from the vessels into the tumour. Of particular relevance is the arterial input function (AIF), which describes the delivery of the tracer into the

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region of interest. The AIF is usually determined in a large vessel or in the heart, indicating that it might not be representative for the tissue of interest, e.g. the tumour.

The aim of this study is firstly to implement a model to simulate the oxygen and  $^{18}\text{F}$ -fluoromisonidazole (FMISO) distributions in tissue and to analyse the sensitivity on several input parameters that may impact the FMISO uptake. In a second step, the impact of the most relevant parameters on clinical criteria used for PET-based hypoxia assessment is studied. Different oxygenation levels in the tumour are considered by using vascular fractions (VFs) of 1% and 3%, and the effect of vascular geometry variation is studied by random sampling of the vessel distribution. The parametric sensitivity study includes tracer diffusion and binding, necrosis in strongly hypoxic areas, as well as properties of the AIF. Results are represented in terms of oxygen histograms and TACs, and by analysing the relationship between bound tracer and oxygen concentrations. Additionally, the clinical parameter tissue-to-blood ratio (TBR) was calculated and compared with the hypoxia-perfusion compound parameter FHP proposed by Mönnich *et al.* [17].

## 2. Materials and methods

### 2.1. Mathematical models for oxygen and tracer transport

#### 2.1.1. Partial oxygen pressure distribution in tumours

It is assumed that oxygen diffuses from vessels into tumour tissue, where it is consumed by cells. These two processes are described by a reaction-diffusion partial differential equation (PDE), as shown in previous studies [11,12,16,24]:

$$\frac{\partial P}{\partial t} = D_{O_2} \nabla^2 P - g_{\max} \frac{P}{P + P_0} = 0 \quad (1)$$

If the derivative on the left side is set to zero,  $P$  describes the stationary spatial distribution of oxygen partial pressure defined in a cubic volume of tumour tissue ( $V$ ).  $D_{O_2}$  is the oxygen diffusion coefficient and  $g_{\max}$  is the maximum oxygen consumption rate. Oxygen consumption is modelled by the Michaelis-Menten relation (third term in Eq. (1)), in which  $P_0$  is the Michaelis-Menten coefficient (partial oxygen pressure at which consumption is reduced to 50%). Oxygen diffusion through the vessel walls is described by the capillary permeability coefficient  $L_{O_2}$ , and the vessel-to-tissue concentration difference. This is included by the boundary condition at the vessel surface  $\vec{n} \cdot (D_{O_2} \nabla P) = L_{O_2} (P_{iv} - P)$ , where  $P_{iv}$  is the intravessel-value of  $P$  in tumours.

#### 2.1.2. Hypoxia-radiotracer dynamics

As for the oxygen, blood vessels are also the source of the FMISO radiotracer, which diffuses into the tissue and binds in hypoxic cells. The total tracer concentration is composed by a free and a bound term  $C = C_f + C_b$ , modelled by reaction-diffusion PDEs [16,17].

$$\frac{\partial C_f}{\partial t} = D_T \nabla^2 C_f - K(P) C_f \quad (2a)$$

$$\frac{\partial C_b}{\partial t} = K(P) C_f \quad (2b)$$

$D_T$  is the FMISO diffusion coefficient and the oxygen-dependent irreversible tracer binding rate is described by the coefficient  $K(P) = F_1(P) \cdot F_2(P)$ . In this expression,  $F_1$  considers a hyperbolic relation between binding rate and the oxygen concentration  $P$  [14]:

$$F_1 = K_{\max} \frac{P_1}{P + P_1} \quad (3a)$$

$K_{\max}$  is the maximum binding rate and  $P_1$  describes the oxygen partial pressure at which the binding rate amounts to 50% of its maximum. Assuming that cells at very low oxygen concentration become necrotic and lose their capability for tracer-uptake, the second term  $F_2$  limits the binding according to:

$$F_2 = \left( \frac{P}{P + P_2} \right)^k \quad (3b)$$

Here,  $P_2$  describes the oxygen concentration at which 50% of the cells become necrotic and  $k$  describes the steepness of this transition.

The tracer flow through the vessels walls depends on the capillary permeability for the tracer  $L_T$ , and the tissue-vessel tracer concentration difference, written as the boundary condition:

$$\vec{n} \cdot (D_T \nabla C_f) = L_T (AIF(t) - C) \quad (4)$$

Through this boundary condition the AIF is introduced into the system: the AIF is the time-dependent tracer concentration of the tumour-supplying artery. As in a previous study by Wack *et al.* [21], the AIF was fitted by the double-exponential decay-function:

$$AIF(t) = A_1 e^{-\tau_1 t} + A_2 e^{-\tau_2 t} \quad (5)$$

In Eq. (5),  $\tau_1$ ,  $\tau_2$ ,  $A_1$ , and  $A_2$  are the fit parameters describing the tracer removal from the blood with two different rates ( $\tau_1$ ,  $\tau_2$ ) and their relative contributions ( $A_1$ ,  $A_2$ ), respectively.

Assuming similar tumour tissue surrounding the simulation volume, zero oxygen and tracer flows into the volume were set as external boundary conditions. All parameters related to this model have been described in previously published studies, and the references and values applied here are summarized in Table 2.

### 2.2. Parametric sensitivity study for the FMISO dynamics

#### 2.2.1. VF and vascular architecture

Vascular architectures were considered as arrays of vessels modelled as circular cylinder with 10  $\mu\text{m}$  radius. Tumour samples of  $500 \times 500 \times 500 \mu\text{m}^3$  were simulated employing VFs of 1% and 3%. Two types of vascular architectures were analysed, similar to those simulated in previously published studies [12,23]: parallel and orthogonal vessels (parallel to the  $x$ ,  $y$ , or  $z$  axis). In both cases, the vessels covered the whole length of the volume. The spatial vessel distribution and direction of the vessels in 3D were generated randomly using a uniform probability distribution. For each combination of VF (1% or 3%) and vascular architecture type, ten different tumour samples were generated.

#### 2.2.2. Experimental and artificial AIFs

The impact of the AIF on the FMISO uptake was analysed using the parallel vessel architecture with VFs 1% and 3%. Experimental patient AIFs were modelled by double-exponential functions (Eq. (5)), fitted to the mean AIF as presented by Wack *et al.* [21], as well as to the upper and lower 95%-confidence limits (CL). Two additional artificial AIFs were generated having the same area under the curve as the mean experimental AIF, during the first 120 min, but showing a slowly decreasing or a flat shape, respectively. The AIFs are shown in Fig. 1 and the corresponding fitting parameters are presented in Table 1.

#### 2.2.3. Parameters related to the FMISO uptake

The sensitivity study for the tracer uptake was performed using the parallel vessel architecture with VFs of 1% and 3%. Parameter values were varied using the minimum, maximum and mean values of the intervals shown in Table 2. The effects of parameter variation on the tracer binding  $C_b$  as a function of  $P$ , as well as the TAC shape, were studied. For this, the TAC was calculated according to:

$$TAC(t) = C_f(t) + C_b(t) + AIF(t) \cdot VF \quad (6)$$

### 2.3. Impact on clinically-relevant PET-parameters for hypoxia assessment

Based on the parametric sensitivity analysis, those input parameters with greater impact on the simulated FMISO uptake were selected to study the resulting variability of the clinically-employed parameters,

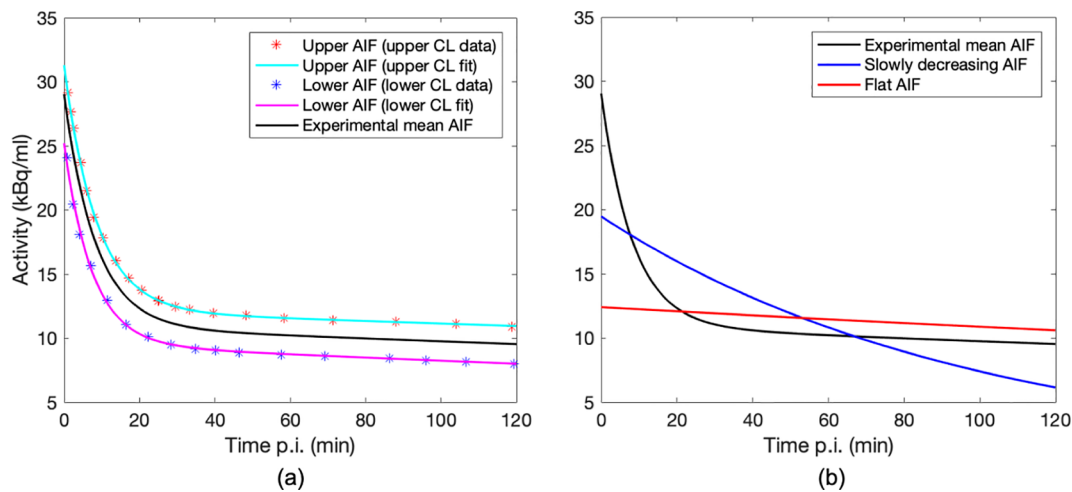


Fig. 1. Experimental AIFs from Wack *et al.* [21] (a) and artificial AIFs (red and blue curves in b).

Table 1

Fit parameters according to Equation (5), describing the AIFs used in this study.

Fitting parameters for AIFs	$A_1$ (kBq/ml)	$A_2$ (kBq/ml)	$\tau_1$ (s <sup>-1</sup> )	$\tau_2$ (s <sup>-1</sup> )
<i>Experimental AIFs</i> [21]				
Upper AIF (upper CL)	19.13	12.16	$1.93 \times 10^{-3}$	$1.47 \times 10^{-5}$
Mean AIF	18.11	10.93	$2.00 \times 10^{-3}$	$1.90 \times 10^{-5}$
Lower AIF (lower CL)	15.64	15.64	$2.24 \times 10^{-3}$	$2.48 \times 10^{-5}$
<i>Artificial AIFs</i>				
Slowly decreasing AIF	11.03	8.44	$2.00 \times 10^{-4}$	$1.21 \times 10^{-4}$
Flat AIF	8.40	4.00	$2.00 \times 10^{-5}$	$2.59 \times 10^{-5}$

Table 2

Parameter values (in bold) used to simulate the spatiotemporal oxygen and FMISO distributions.

Parameter	Symbol	Value
<i>Oxygen distribution</i>		
Intravessel $P$ in tumours	$P_v$	40mmHg [17]
Capillary permeability to oxygen	$L_{O_2}$	$4.1 \times 10^{-4} \text{ms}^{-1}$ [17]
Oxygen diffusion coefficient	$D_{O_2}$	$2 \times 10^{-9} \text{m}^2 \text{s}^{-1}$ [17]
Maximum oxygen consumption rate	$g_{max}$	15mmHg s <sup>-1</sup> [17]
Michaelis-Menten coefficient of oxygen consumption	$P_0$	2.0mmHg [17]
<i>FMISO dynamics</i>		
Capillary permeability to FMISO	$L_T$	<b><math>(2.4 - 9.4) \times 10^{-5} \text{ms}^{-1}</math></b> [16]
FMISO diffusion coefficient	$D_T$	<b><math>(5.5 - 7.9) \times 10^{-11} \text{m}^2 \text{s}^{-1}</math></b> [21,25]
$P$ inhibiting binding by 50% of its maximum	$P_1$	<b><math>(0.8 - 1.5) \text{mmHg}</math></b> [26]
Maximum binding rate	$K_{max}$	<b><math>(1.7 - 4.5) \times 10^{-4} \text{s}^{-1}</math></b> [17,23]
$P$ inducing 50% necrosis	$P_2$	<b><math>(0.1 - 1.0) \text{mmHg}</math></b> [17,27]
Viable-necrotic tissue transition steepness factor	$k$	<b><math>(0.3 - 1.0)</math></b> [17]

TBR and FHP [19], at 120 min post injection (p.i.):

$$\text{TBR}(120 \text{ min p.i.}) = \frac{\text{TAC}(120 \text{ min p.i.})}{\text{AIF}(120 \text{ min p.i.})} \quad (7)$$

$$\text{FHP}(120 \text{ min p.i.}) = \frac{\text{TAC}(120 \text{ min p.i.})}{\text{TAC}_{0 \text{ min}}^{1.5 \text{ min}}} \quad (8)$$

#### 2.4. Simulations software tools and analysis of results

Vascular architectures were generated in *Gmsh* [28] and used as

input to solve all PDEs via the finite element method with *FEniCS* [29], both available as open-source softwares. Since the tracer distribution depends on the stationary oxygen distribution, Eq. (1) was solved first. The  $P$  distribution was saved and used as input to solve equations Eqs. (2a) and (2b). The time-dependent tracer distribution was evaluated between 0 and 120 min p.i.. Results were analysed by oxygen histograms, plots of  $C_b$  as a function of  $P$ , and TACs. The behaviour of TBR and FHP with respect to the hypoxic fraction (HF, fractional volume with  $P < 5 \text{ mmHg}$ ) was studied. All plots were generated using MATLAB R2016b (The Mathworks Inc., MA), while the visualization of  $P$  and tracer distributions was performed using the open-source software *Paraview* [30].

### 3. Results

Fig. 2 shows the simulated distributions of  $P$  and  $C_b$  for a sample architecture with parallel vessels and VF 3%. Increased FMISO binding can be seen at large distances from the vessels.

#### 3.1. Parametric sensitivity study for the FMISO dynamics

##### 3.1.1. VF and vascular architecture

Fig. 3 shows the oxygen histograms and TACs simulated for the parallel and orthogonal vessel architectures, with VFs 1% and 3%. The better oxygenation achieved for the 3% VF is reflected by the oxygen histogram exhibiting reduced HF. The largest variability between the different simulated samples was found at the lowest  $P$  values. Increasing the VF from 1% to 3% led to increased peak in the TAC at early time points (from 0 to 20 min p.i.) and decreased tracer uptake at large p.i. times. A larger TAC variability was found for VF 1%. No significant differences in oxygenation and TACs were found when comparing parallel and orthogonal vessel architectures for different VF.

##### 3.1.2. Experimental and artificial AIFs

Fig. 4 shows the TACs for the parallel vessel architecture with VF 1% simulated using different AIFs as input. The vertical shifts between the three experimental AIFs (Fig. 4a) led to similar shifts of the TACs that were larger than the sampling variability. For the artificial AIFs, the TAC shape changed drastically (Fig. 4b). For the slowly decreasing AIF, the TAC peaked later than for the mean experimental AIF. In contrast, the TAC simulated with the flat AIF did not show any initial peak, but rather a continuously increasing binding with time.

##### 3.1.3. Parameters related to the FMISO uptake

Fig. 5 shows  $C_b$  as a function of  $P$  for different parameter settings in the FMISO dynamics model. The shape of  $C_b(P)$  was basically the same

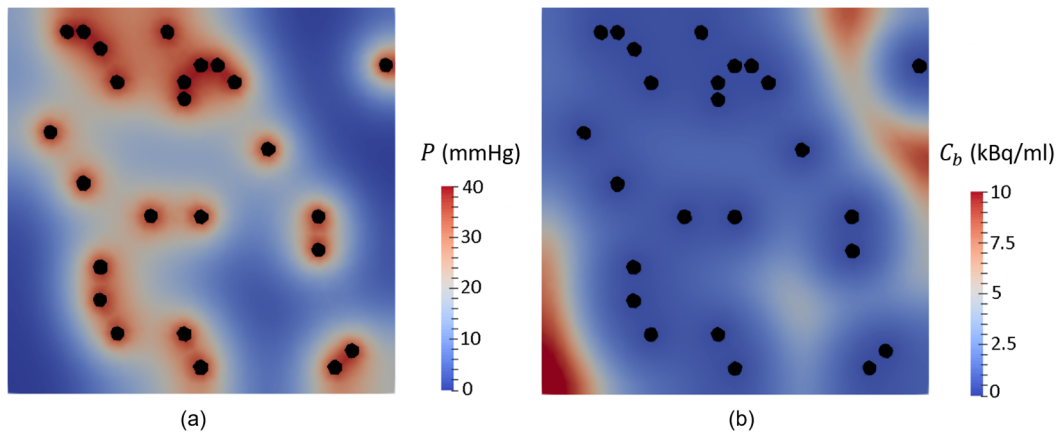


Fig. 2. Example of simulated  $P$  (a) and  $C_b$  distributions, 120 min p.i., for a sample of the parallel vessels (black circles) architecture with VF 3%. Distributions are shown for the central plane of the simulated tumour volume.

for all settings: the binding increased with increasing  $P$ , reached a maximum at around 2 mmHg and decreased after. Essentially, no variation was observed for varying  $L_T$  and  $D_T$  values. Increasing  $P_1$  and  $K_{max}$  separately led to an increased binding, for  $P > 0.1$  mmHg and for all  $P$  values, respectively. Increasing separately the value of  $P_2$  and  $k$  led

to a decreased binding for  $P < 2$  mmHg and a shifting of the binding maximum towards larger  $P$  values.

Fig. 6 displays the TACs for all parameter settings. Increasing VF from 1% to 3% altered significantly the height of the peak at early p.i. times, and the tracer accumulation at late p.i. times. As shown for the

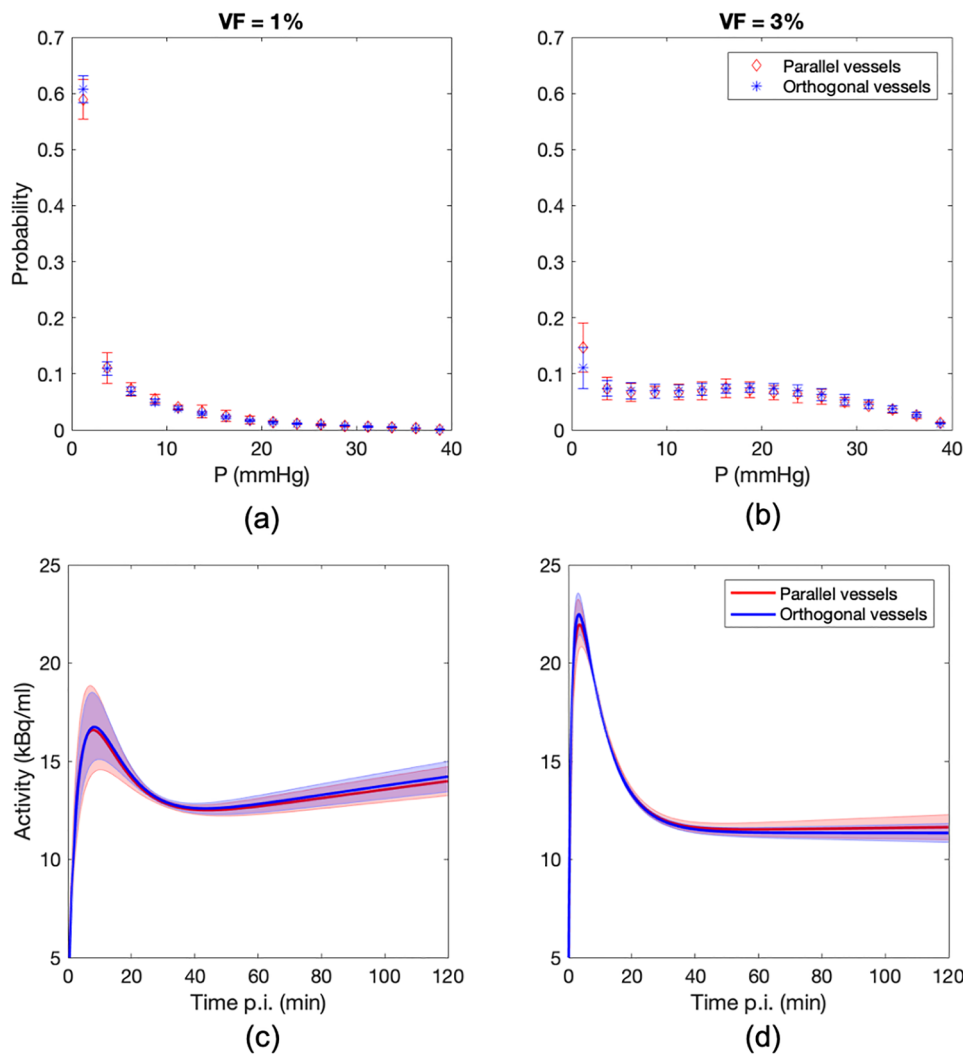


Fig. 3. Simulated probability distributions for  $P$  (a, b) and TACs (c, d) for parallel (red) and orthogonal (blue) vessel distributions, using VFs of 1% (a, c) and 3% (b, d). Errors bars represent single standard deviations over the ten simulated samples. TAC shaded regions represent the 95% confidence interval for the ten simulated samples.

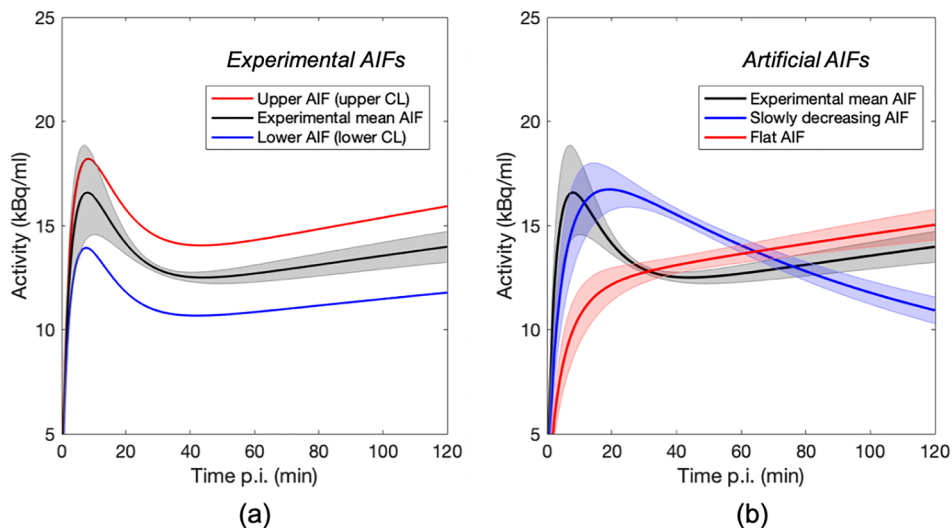


Fig. 4. Simulated TACs for experimental AIFs from Wack *et al.* [21] (a) and for artificial AIFs (blue and red curves in b) for the parallel vessel architecture and VF 1%. Shaded regions show the 95% confidence interval for the ten simulated samples. For better visibility, confidence intervals are shown only for the mean AIF in (a).

central parameter settings (Table 2) by the shaded regions, the TAC was sensitive to the sampling variability, and the TAC variation was larger for VF 1% than for 3%. Regarding the different parameter settings, TACs did not differ significantly for varying  $L_T$ , and only small differences in the peak were found for  $D_T$ . Also, for  $P_1$  only minor differences in the uptake were seen at large p.i. times. The largest sensitivity of the TAC was found for variations of  $K_{max}$ , which exhibited identical peak heights but markedly different tracer uptakes at large p.i. times. Varying the values of  $P_2$  and  $k$  did not change the peak height but led to changes of the late uptake, of the same magnitude as the sample variation.

### 3.2. Impact on clinically-relevant parameters for PET-based hypoxia assessment

Based on Figs. 4–6, the most relevant parameters influencing the FMISO uptake were  $K_{max}$  and the AIF. For different settings of these two parameters, TBRs and FHPs were calculated for VFs 1% and 3%, and the obtained values are shown Table 3.

For the mean AIF, increased  $K_{max}$  led to increased TBR, and this trend was more pronounced for VF 1%. For the same value of  $K_{max}$ , larger TBR was obtained for smaller VF, and therefore in this case TBR allowed discriminating between the two VF and the related HF. However, a comparable TBR was obtained for  $K_{max} = 1.7 \times 10^{-41}/s$  at VF 1% and for  $K_{max} = 4.5 \times 10^{-41}/s$  at VF 3%.

Only small differences in TBRs were obtained for the flat AIFs at VF 1% and 3%. In contrast, TBR-differences were markedly larger for the slowly decreasing AIF. Assuming the same AIF, differentiation of VF based on TBR-values was possible.

For the mean AIF, increased  $K_{max}$  led to increased FHP and lower FHPs were obtained at VF 3% for all  $K_{max}$  values, in comparison to VF 1%. Therefore, FHP also allowed discriminating between the two VF.

Compared to the mean AIF at the same value of  $K_{max}$ , FHP was larger for the flat than for the slowly decreasing AIF. For the same AIF, FHP allowed discriminating different VF and HF, however, FHP for the flat AIF at VF 3% was larger than that for the mean and slowly decreasing AIF at VF 1%.

## 4. Discussion

### 4.1. Parametric sensitivity study for the FMISO dynamics

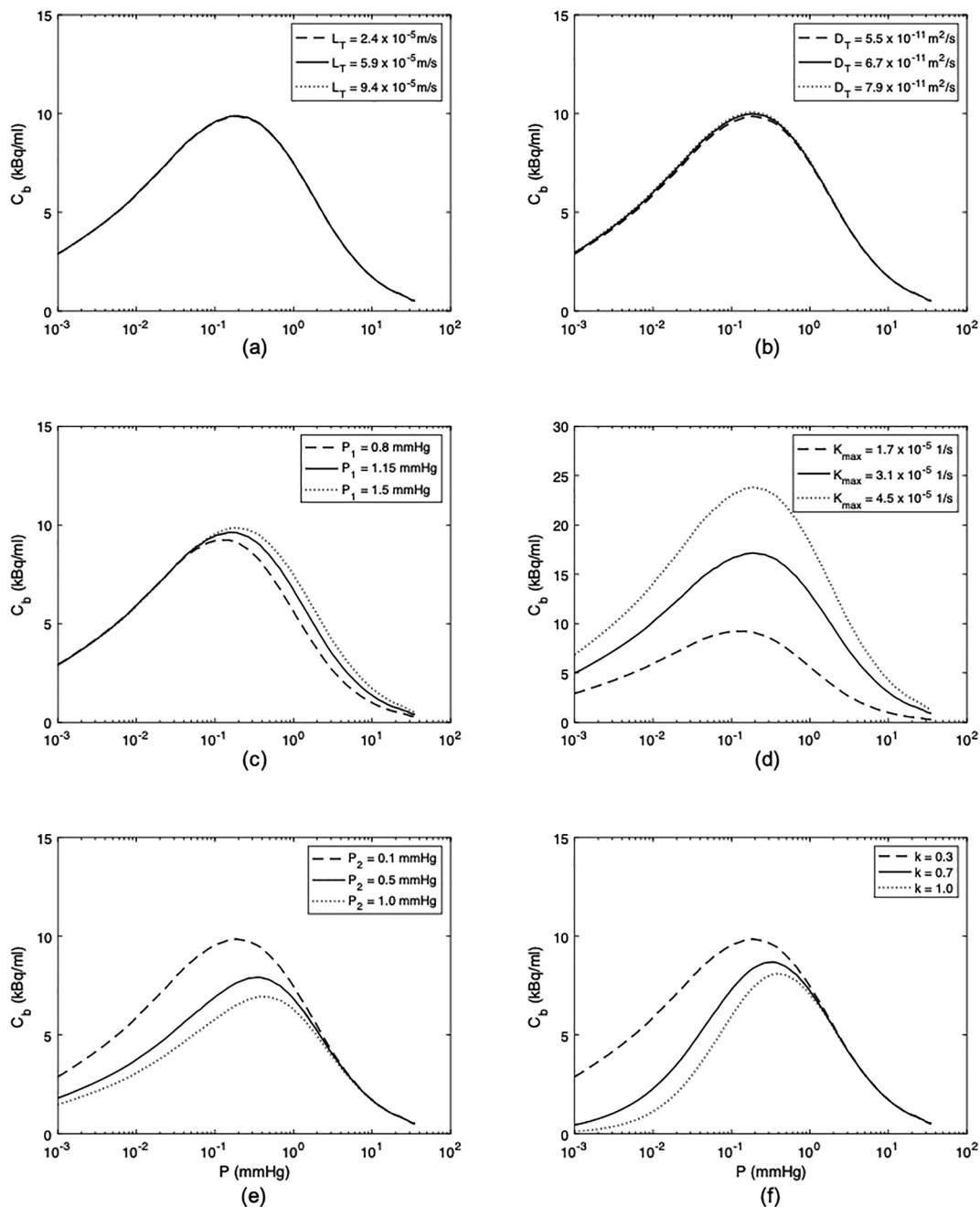
In accordance with previous studies [12,23], very similar oxygen

distributions were found for architectures with parallel and orthogonal vessels, as long as the same VF and the same degree of heterogeneity in the vessel distribution were used. This is in accordance with the study by Warren and Partridge [23], who analysed vascular architectures with isotropic vessel orientations and showed similar oxygen distributions. This leads to the conclusion that oxygen distributions for these three types of vascular architectures are the same on a macroscopic level, for identical VF and degree of heterogeneity in the vessel distribution. We therefore restricted further analysis to the parallel vessel architecture.

While high  $P$  values may result from a small distance from a single vessel or moderate distances to multiple vessels, low  $P$  values depend critically on the largest distance to the nearest vessels, which is in the order of the oxygen diffusion radius. Low  $P$  values are therefore more dependent on the individual vessel position and thus exhibit larger variations in the sampling experiments. The impact of the VF can be clearly seen in the TACs. While the TAC at VF 3% exhibits a prominent initial peak, which indicates a good perfusion, the TAC at VF 1% resulted in a reduced peak with an increased uptake at large p.i. times, indicating a reduced perfusion with increased hypoxia.

TACs clearly reflect differences in VF, and it also depends critically on the AIF (Figs. 1 and 4), as previously shown by Wack *et al.* [21]. For different investigated AIFs, the TAC variations were larger than sampling variability. In principle, the AIF can be measured simultaneously with the TAC and may then be used to remove or reduce the dependence of the measured parameters on the AIF. Examples for such parameters are the TBR, where TACs are normalized to AIF-values, or physiological parameters, determined in more advanced pharmacokinetic analyses. In real measurements, however, the AIF is typically measured in the heart or in a large artery proximal to the tumour to avoid partial volume effects. Depending on how the tumour is connected to the vascular system, an initially sharply peaked AIF will spread and the actual AIF in the tumour may be less sharp or even flat as simulated in our study by the “slowly decreasing” or “flat” AIF. Thus, even if the measured parameters are corrected for the impact of the AIF, it may still include some uncertainty resulting from the fact that the measured rather than the actual AIF of the tumour has been used. The strong dependence of the TAC on the AIF may also explain the very different TAC shapes observed by Mena-Romano *et al.* [31] in three different rat prostate tumour sublines.

Besides VF and AIF, the highest sensitivity of the TACs was found for the maximum binding rate  $K_{max}$ . While the exact value of this parameter is unknown, it is primarily a chemical reaction constant, which



**Fig. 5.** Simulated FMISO binding concentration  $C_b$  as a function of  $P$  at 120 min p.i., for all parameters related to the FMISO dynamics model using the experimental mean AIF: FMISO capillary permeability  $L_T$  (a), FMISO diffusion coefficient  $D_T$  (b),  $P_1$  indicating the value of  $P$  for 50% binding (c), maximum binding rate  $K_{max}$  (d),  $P_2$  indicating the value of  $P$  for 50% necrosis (e), and transition steepness factor for necrosis  $k$  (f). Simulations were performed for the parallel vessel architecture and VF 1% using the reference parameter settings and in each plot, the denoted parameter was varied within the ranges shown in Table 2.

should not differ between different cell lines although it cannot be ruled-out that there is an additional dependence on the tracer uptake into the cell and the nucleus.

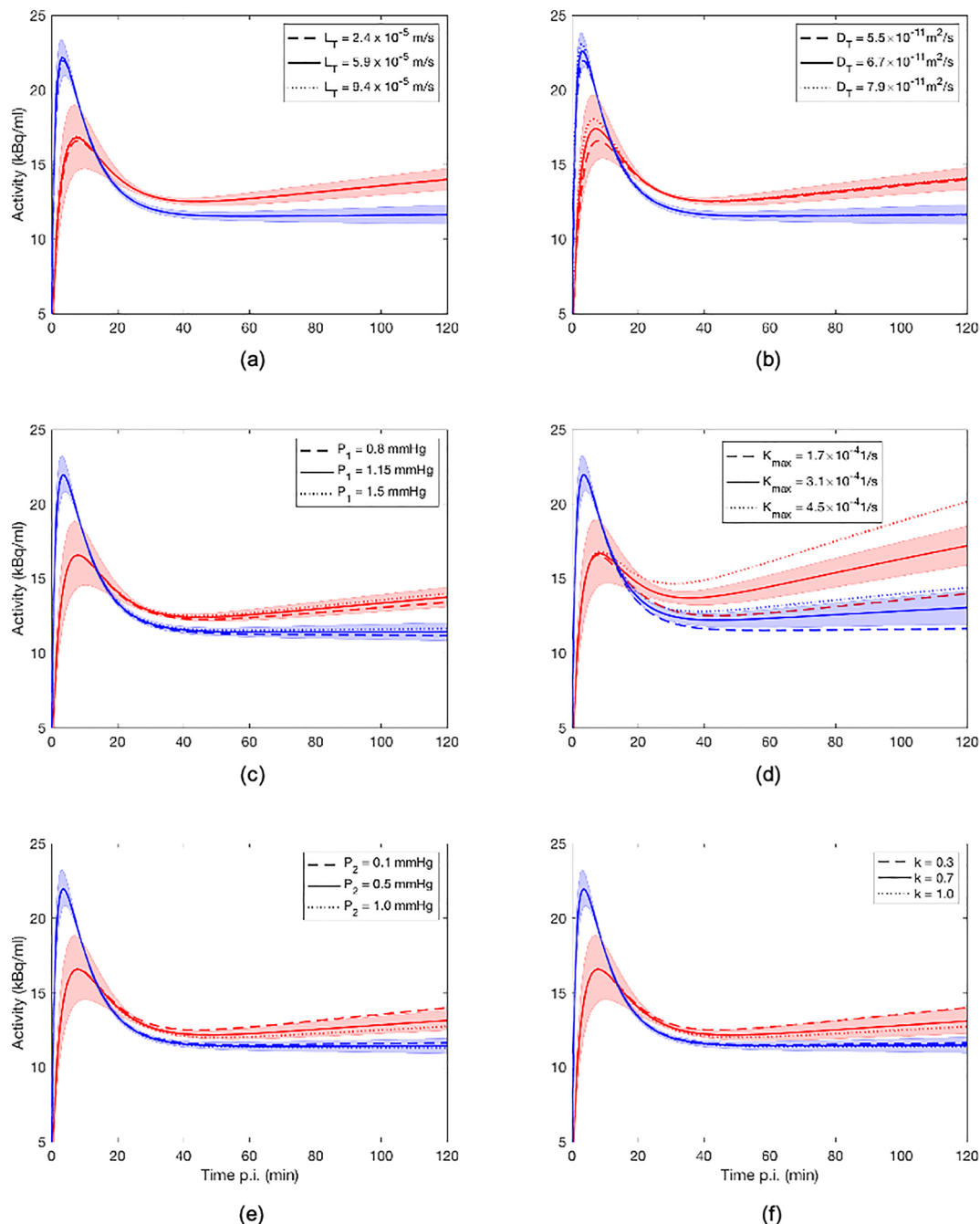
The model used to simulate the FMISO dynamics showed the complex behaviour of tracer binding, exhibiting a reduced binding for both well-oxygenated and very poorly oxygenated regions, which are assumed to become necrotic (Fig. 5). While it is undoubted that severe hypoxia can lead to necrosis and that FMISO will not bind to necrotic regions, the oxygen level leading to necrosis as well as the underlying time scale is unknown and may vary between cell lines as they may adapt differently to the hypoxic environment. With this respect, the modelling of the uptake in necrotic regions by the function  $F_2(P)$  has to be considered as a heuristic approach, which may be questioned. In

contrast, the uptake function in hypoxic but viable tissue regions,  $F_1(P)$  appears more reliable as the underlying mechanism is better understood. In addition, only minor changes of the uptake was found for variations of the related parameter  $P_1$ .

In contrast to the parameters describing the tracer uptake, tracer binding (Fig. 5) and TAC shape (Fig. 6) turned out to be essentially independent of the permeability  $L_T$  and the diffusion coefficient  $D_T$ . As shown by Kelly and Brady [16], relevant TAC changes may be observed only when these parameters are varied by an order of magnitude.

#### 4.2. Reliability of clinically-relevant PET-parameters

PET-based hypoxia assessment is often performed using parameters



**Fig. 6.** TACs simulated with the experimental mean AIF and different parameter settings of the FMISO dynamics model, for the parallel vessel architecture with VFs of 1% (red curves) and 3% (blue curves): FMISO capillary permeability  $L_T$  (a), FMISO diffusion coefficient  $D_T$  (b),  $P_1$  indicating the value of  $P$  for 50% binding (c), maximum binding rate  $K_{max}$  (d),  $P_2$  indicating the value of  $P$  for 50% necrosis (e), and transition steepness factor for necrosis  $k$  (f). Simulations were performed for the reference parameter settings and in each plot, the denoted parameter was varied within the ranges shown in Table 2. Each TAC represents an average over ten samples shown in solid, dashed and dotted lines. Shaded regions represent the 95% confidence interval of the simulations performed with the central parameter setting (solid line).

such as tissue-to-blood ratios, tissue-to-muscle ratios, or standardized uptakes values (SUV), which are uptake measurements, normalized to that of a reference volume or to the injected activity per mass and which can be used without additional use of detailed pharmacokinetic models. TBR is determined in a region of interest at a certain p.i. time and is normalized to the activity in the blood (Eq. (7)). FHP was suggested by Mönnich *et al.* [19] as a “measure of hypoxia-related tracer retention that is normalized by a simple measure of perfusion” (Eq. (8)) and it was found that FHP allowed assessing the median  $P$  with higher accuracy than with a simple measurement at 4 h p.i.

As shown in Table 3, larger or comparable TBRs may be obtained for VF 3% than for 1%, for different  $K_{max}$  values. Therefore, if  $K_{max}$  varies within the tumour, discriminating between hypoxic and non-hypoxic tissues may become difficult. In contrast, the parameter FHP can still discriminate these conditions. On the other hand, if  $K_{max}$  is considered only as a chemical reaction constant, independent of the transport capabilities of the cell membranes, either TBR or FHP may be used to distinguish different degrees of oxygenation.

Regarding the dependence on the AIF, the parameter FHP could not always distinguish different VF, since this metric depends on the



**Table 3**

TBR and FHP (mean  $\pm$  standard deviation) for different maximum binding rates  $K_{max}$  and AIFs, for VFs 1% and 3% (and corresponding HFs, mean  $\pm$  standard deviation). Standard deviations were calculated for the ten simulated samples.

AIF	Flat	Slowly decr.	Mean	Mean	Mean
$K_{max}$ [ $\times 10^{-4}$ 1/s]	1.7	1.7	1.7	3.1	4.5
<b>TBR</b>					
VF = 1%*	1.42 $\pm$ 0.04	1.78 $\pm$ 0.05	1.47 $\pm$ 0.04	1.81 $\pm$ 0.07	2.12 $\pm$ 0.10
VF = 3% <sup>+</sup>	1.20 $\pm$ 0.03	1.34 $\pm$ 0.06	1.22 $\pm$ 0.03	1.37 $\pm$ 0.06	1.51 $\pm$ 0.08
<b>FHP</b>					
VF = 1%*	1.67 $\pm$ 0.08	0.81 $\pm$ 0.04	0.94 $\pm$ 0.04	1.14 $\pm$ 0.04	1.33 $\pm$ 0.05
VF = 3% <sup>+</sup>	1.10 $\pm$ 0.08	0.48 $\pm$ 0.04	0.63 $\pm$ 0.02	0.70 $\pm$ 0.04	0.77 $\pm$ 0.05

\* HF = 70.3%  $\pm$  2.7%.

<sup>+</sup> HF = 22.5%  $\pm$  5.4%.

relation between late and early values of the TAC, which changes drastically between the different AIFs. Especially for the flat AIF, the lack of an initial peak led to markedly increased FHP-values. This complicates especially the inter-individual comparison of FHP-values if the tumours have significantly different AIFs. The parameter TBR, on the other hand, allowed distinguishing the different VF independently of the actual AIF. However, inter-individual variations of the AIF will lead to variation of TBR, which introduces additional uncertainty in the comparison of TBR-values between different tumours. This problem persists for both parameters TBR and FHP as long as the measured AIF does not truly reflect the actual AIF in the tumour.

## 5. Conclusion

This study implemented a model for hypoxia-PET radiotracer dynamics and performed a parametric sensitivity study to gain insight in the relationship between  $^{18}\text{F}$ -fluoromisonidazole (FMISO) transport processes and time-activity curves (TACs), tissue-to-blood ratios (TBRs) and the hypoxia-perfusion compound parameter FHP. The input parameters considered were vascular architecture, vascular fraction (VF), arterial input function (AIF) and parameters related to the FMISO dynamics. The most sensitive parameters were the AIF and the maximum binding rate ( $K_{max}$ ). TBR allowed discriminating VF for different AIF, and FHP for different  $K_{max}$ , but neither TBR nor FHP were unbiased in all cases. This bias may especially occur in the comparison of TBR- or FHP-values between different tumours, where the relation between measured and actual AIF may vary. Thus, these parameters represent only surrogates rather than absolute measurements of hypoxia in tumours.

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## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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