





Agulhas ring formation as a barotropic instability of the retroflection

Weijer, Wilbert; Zharkov, Volodymyr; Nof, Doron; Dijkstra, Henk A.; Ruijter, Wilhelmus P.M. de; Terwisscha van Scheltinga, Arjen; Wubs, Fred

Published in: Geophysical research letters

IMPORTANT NOTE: You are advised to consult the publisher's version (publisher's PDF) if you wish to cite from it. Please check the document version below.

Document Version Publisher's PDF, also known as Version of record

Publication date: 2013

Link to publication in University of Groningen/UMCG research database

Citation for published version (APA): Weijer, W., Zharkov, V., Nof, D., Dijkstra, H. A., Ruijter, W. P. M. D., Terwisscha van Scheltinga, A., & Wubs, F. (2013). Agulhas ring formation as a barotropic instability of the retroflection. *Geophysical research* letters.

Copyright Other than for strictly personal use, it is not permitted to download or to forward/distribute the text or part of it without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license (like Creative Commons).

The publication may also be distributed here under the terms of Article 25fa of the Dutch Copyright Act, indicated by the "Taverne" license. More information can be found on the University of Groningen website: https://www.rug.nl/library/open-access/self-archiving-pure/taverneamendment.

Take-down policy

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

Downloaded from the University of Groningen/UMCG research database (Pure): http://www.rug.nl/research/portal. For technical reasons the number of authors shown on this cover page is limited to 10 maximum.

Supplementary Information to: Agulhas ring formation as a

barotropic instability of the retroflection

Wilbert Weijer, Volodymyr Zharkov, Doron Nof,

Henk A. Dijkstra, Wilhelmus P. M. de Ruijter,

Arjen Terwisscha van Scheltinga, and Fred Wubs

September 29, 2013

1. The length scale of the barotropic instability

To investigate whether the zonal length scale is consistent with theoretical predictions, we compare our results to Talley (1983), who studied the stability of a shear layer U(y) with discontinuities in dU/dy. Fitting her Eq. (22) to our velocity profile $(U_T(y))$; Fig. S1a, dashed black line) suggests a shear layer of only 0.5° wide, or a half-width $L = 2.8 \cdot 10^4$ m. Our maximum westward and eastward velocities of -0.4 m s^{-1} and 0.2 m s^{-1} suggest a velocity scale $U_0 = 0.3 \text{ m s}^{-1}$, in addition to a net westward translation of -0.1 m s^{-1} . With $\beta_0 = 1.8 \cdot 10^{-11} \text{ m}^{-1} \text{ s}^{-1}$, this yields a dimensionless $\beta = \beta_0 L^2/U = 0.05$. Figure S1b shows the (dimensionless) real $(c_r; \text{ solid gray})$ and imaginary $(c_i; \text{ dashed gray})$ parts of the dispersion relation for $\beta = 0.05$ as function of (dimensionless) zonal wavenumber k (cf. Fig. 4 of Talley (1983)), while the curve kc_i (black) shows the (dimensionless) growth rate. The growth rate is optimal for k = 0.4; the corresponding wave length $\lambda = 4.4 \cdot 10^5$ m (about 5°) is consistent with that of the Retroflection Mode (7°). In addition, the (dimensionless) propagation speed for this wavenumber is $c_r = -0.14$, which corresponds to -0.04 m s^{-1} . Taking into account the additional translation speed of -0.1 m s^{-1} , this corresponds well with the -0.13 m s^{-1} speed diagnosed from the Hovmüller diagrams.

REFERENCES

Talley, L. D., 1983: Radiating barotropic instability. J. Phys. Oceanogr., 13, 972–987.

List of Figures

S1 a) Profiles along 25°E of mean zonal velocity of our standard solution (U in ms⁻¹; solid black); the norm of h_m (light gray; arbitrary amplitude); the gradient of potential vorticity (dark gray; 10^{-10} m⁻¹s⁻¹); and the fitted velocity profile $U_T(y)$ according to Eq. (22) of Talley (1983) (dashed black). b) Real (c_r ; solid gray) and imaginary (c_i ; dashed gray) parts of the dispersion relation for $\beta = 0.05$ as function of zonal wavenumber k. Growth rate is given by kc_i (black).



FIG. 1. a) Profiles along 25°E of mean zonal velocity of our standard solution (U in m s⁻¹; solid black); the norm of h_m (light gray; arbitrary amplitude); the gradient of potential vorticity (dark gray; 10^{-10} m⁻¹ s⁻¹); and the fitted velocity profile $U_T(y)$ according to Eq. (22) of Talley (1983) (dashed black). b) Real (c_r ; solid gray) and imaginary (c_i ; dashed gray) parts of the dispersion relation for $\beta = 0.05$ as function of zonal wavenumber k. Growth rate is given by kc_i (black).