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Light hadrons from $N_f = 2 + 1 + 1$ dynamical twisted mass fermions

R. Baron^a, B. Blossier^b, P. Boucaud^b, J. Carbonell^c, A. Deuzeman^d, V. Drach^e, F. Farchioni^f, V. Gimenez^g, G. Herdoiza^e, K. Jansen^e, C. Michael^h, I. Montvayⁱ, E. Pallante^j, O. Pène^b, S. Reker*†j; C. Urbach^k, M. Wagner^l and U. Wenger^d

^aCEA, Centre de Saclay, IRFU/Service de Physique Nucléaire, F-91191 Gif-sur-Yvette, France
 ^bLaboratoire de Physique Théorique (Bât. 210), Université de Paris XI, Centre d'Orsay, 91405
 Orsay-Cedex, France

^cLaboratoire de Physique Subatomique et Cosmologie, 53 avenue des Martyrs, 38026 Grenoble, France

^d Albert Einstein Center for Fundamental Physics, Institute for Theoretical Physics, University of Bern, Sidlerstr. 5, CH-3012 Bern, Switzerland

^eNIC, DESY, Platanenallee 6, D-15738 Zeuthen, Germany

^f Universität Münster, Institut für Theoretische Physik, Wilhelm-Klemm-Straße 9, D-48149 Münster, Germany

^gDep. de Física Teòrica and IFIC, Universitat de València-CSIC, Dr.Moliner 50, E-46100 Burjassot, Spain

^hDivision of Theoretical Physics, University of Liverpool, L69 3BX Liverpool, United Kingdom

ⁱDeutsches Elektronen-Synchrotron DESY, Notkestr. 85, D-22603 Hamburg, Germany

^jCentre for Theoretical Physics, University of Groningen, Nijenborgh 4, 9747 AG Groningen, the Netherlands

^kHelmholtz-Institut für Strahlen- und Kernphysik (Theorie) and Bethe Center for Theoretical Physics, Universität Bonn, 53115 Bonn, Germany

¹Humboldt-Universität zu Berlin, Institut für Physik, Newtonstraße 15, D-12489 Berlin, Germany

We present results of lattice QCD simulations with mass-degenerate up and down and mass-split strange and charm ($N_f=2+1+1$) dynamical quarks using Wilson twisted mass fermions at maximal twist. The tuning of the strange and charm quark masses is performed at three values of the lattice spacing $a\approx 0.06\,\mathrm{fm}$, $a\approx 0.08\,\mathrm{fm}$ and $a\approx 0.09\,\mathrm{fm}$ with lattice sizes ranging from $L\approx 1.9\,\mathrm{fm}$ to $L\approx 3.9\,\mathrm{fm}$. We perform a preliminary study of SU(2) chiral perturbation theory by combining our lattice data from these three values of the lattice spacing.

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^{*}Speaker.

[†]For the ETM Collaboration

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1. Introduction

The twisted mass formulation of Lattice QCD [1, 2] has been studied extensively with $N_f = 2$ dynamical flavours by the European Twisted Mass (ETM) collaboration. In this formulation of QCD, the Wilson term is chirally rotated within an isospin doublet. The effects of the strange and charm dynamical quarks are included through a mass-split doublet as discussed in [3, 4, 5, 6]. Results using two of the three lattice spacings discussed in these proceedings have recently been published in [7], where we describe our setup in more detail. Furthermore, at this conference, other investigations into the physics of $N_f = 2 + 1 + 1$ twisted mass fermions have also been presented: [8, 9, 10, 11, 12]. We will briefly describe our lattice setup and recapitulate our procedure for tuning to maximal twist and the strategy for the tuning of the heavy doublet in section 2. We give an overview of the runs we have carried out in section 3, where we also examine the status of the tuning. Finally section 4 gives preliminary results for some observables in the light-quark sector, obtained using fits to next-to-leading order (NLO) SU(2) chiral perturbation theory.

2. Lattice setup

In the gauge sector we use the Iwasaki gauge action [13] since it improves the behavior of the lattice theory in relation to the unphysical first order phase transition for values of the hopping parameter κ around its critical value $\kappa_{\rm crit}$ (see [7] and references therein). With this gauge action we observe indeed a smooth dependence of phase sensitive quantities for $\kappa \simeq \kappa_{\rm crit}$. The fermionic action for the light doublet is given by:

$$S_{l} = a^{4} \sum_{x} \left\{ \bar{\chi}_{l}(x) \left[D_{W}[U] + m_{0,l} + i \mu_{l} \gamma_{5} \tau_{3} \right] \chi_{l}(x) \right\}, \tag{2.1}$$

using the notation used in [7]. In the heavy sector, the action becomes:

$$S_h = a^4 \sum_{x} \left\{ \bar{\chi}_h(x) \left[D_W[U] + m_{0,h} + i\mu_\sigma \gamma_5 \tau_1 + \mu_\delta \tau_3 \right] \chi_h(x) \right\}. \tag{2.2}$$

At maximal twist, physical observables are automatically $\mathcal{O}(a)$ improved without the need to determine any action or operator specific improvement coefficients. The gauge configurations are generated with a (Polynomial) Hybrid Monte Carlo updating algorithm [14, 15, 16], where the HMC is used for the light doublet and the PHMC for the heavy doublet.

Tuning to maximal twist requires to set $m_{0,l}$ and $m_{0,h}$ equal to some proper estimate of the critical mass $m_{\rm crit} = m_{\rm crit}(\beta)$ [3]. As has been shown in [4], this is consistent with $\mathcal{O}(a)$ improvement defined by the maximal twist condition $am_{\rm PCAC,l} = 0$ (see also ref. [7]). The numerical precision at which the condition $m_{\rm PCAC,l} = 0$ is fulfilled in order to avoid residual large $\mathcal{O}(a^2)$ effects when the pion mass is decreased is, for the present range of lattice spacings, $|\varepsilon/\mu_l| \lesssim 0.1$, where ε is the deviation of $m_{\rm PCAC,l}$ from zero [17, 18]. As explained in [7], tuning to $\kappa_{\rm crit}$ was performed independently for each set of values of μ_l , μ_σ and μ_δ . From table 1 we observe that the estimate of $\kappa_{\rm crit}$ depends weakly on μ_l . The heavy doublet mass parameters μ_σ and μ_δ should be adjusted in order to reproduce the values of the renormalized s and c quark masses. The latter are related to μ_σ and μ_δ via [3]:

$$(m_{s,c})_{\rm R} = \frac{1}{Z_{\rm P}} (\mu_{\sigma} \mp \frac{Z_{\rm P}}{Z_{\rm S}} \mu_{\delta}),$$
 (2.3)

where the minus sign corresponds to the strange and the plus sign to the charm. In practice we fix the values μ_{σ} and μ_{δ} by requiring the resulting kaon and D meson masses to match their physical values. A detailed description of the determination of the kaon and D meson masses has recently been given in [19].

3. Ensemble overview

We list in table 1 the action parameters for the runs considered in our current analysis. Those runs labeled with an asterisk (*) are ongoing at the time of the writing of these proceedings and have incomplete statistics, all other runs have around 5000 thermalized trajectories with length $\tau = 1$. Ensemble names which end in s or c are used to control the tuning of the strange and charm quark masses respectively. This is not an exhaustive overview of all runs performed within of our $N_f = 2 + 1 + 1$ work. Other runs have been carried out in the context of tuning, reweighting, finite volume effects analysis and in order to measure the renormalization factors.

Ensemble	β	κ_{crit}	$a\mu_l$	$a\mu_{\sigma}$	$a\mu_{\delta}$	$(L/a)^3 \times T/a$
A30.32	1.90	0.1632720	0.0030	0.150	0.190	$32^3 \times 64$
A40.32		0.1632700	0.0040			$32^3 \times 64$
A50.32		0.1632670	0.0050			$32^3 \times 64$
A60.24		0.1632650	0.0060			$24^{3} \times 48$
A80.24		0.1632600	0.0080			$24^{3} \times 48$
A100.24		0.1632550	0.0100			$24^{3} \times 48$
A80.24s		0.1631204	0.0080	0.150	0.197	$24^{3} \times 48$
A100.24s		0.1631960	0.0100			$24^3 \times 48$
B25.32	1.95	0.1612420	0.0025	0.135	0.170	$32^3 \times 64$
*B35.48		0.1612400	0.0035			$48^3 \times 96$
B35.32		0.1612400	0.0035			$32^3 \times 64$
B55.32		0.1612360	0.0055			$32^3 \times 64$
B75.32		0.1612320	0.0075			$32^3 \times 64$
B85.24		0.1612312	0.0085			$24^3 \times 48$
*D115.64	2.10	0.1563640	0.00115	0.120	0.1385	$64^3 \times 128$
D15.48		0.1563610	0.0015			$48^3 \times 96$
D20.48		0.1563570	0.0020			$48^3 \times 96$
D30.48		0.1563550	0.0030			$48^3 \times 96$
*D45.32sc		0.1563550	0.0030	0.0937	0.1077	$32^3 \times 64$

Table 1: Summary of the $N_f = 2 + 1 + 1$ ensembles generated by ETMC at three values of the lattice coupling $\beta = 1.90$, $\beta = 1.95$ and $\beta = 2.10$. From left to right, we quote the ensemble name, the value of inverse coupling β , the estimate of the critical value κ_{crit} , the light twisted mass $a\mu_l$, the heavy doublet mass parameters $a\mu_{\sigma}$ and $a\mu_{\delta}$ and the volume in units of the lattice spacing. Our notation for the ensemble names corresponds to $X\mu_l L$, with X referring to the value of β used.

3.1 Tuning to maximal twist

Figure 1 shows the status of the tuning for the main ensembles considered in these proceedings.

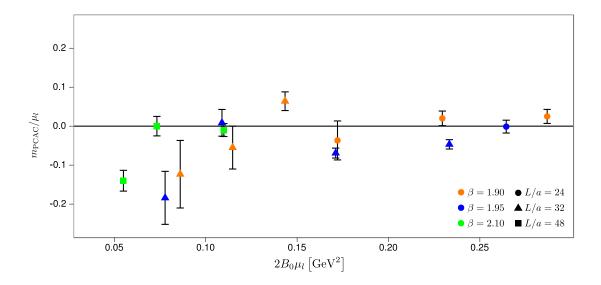


Figure 1: Status of the tuning. The ratio $m_{PCAC,l}/\mu_l$ is plotted as a function of the mass parameter $2B_0\mu_l$. When $|m_{PCAC,l}/\mu_l| \lesssim 0.1$, the ensemble is adequately tuned. Orange, blue and green symbols respectively correspond to $\beta = 1.90$, $\beta = 1.95$ and $\beta = 2.10$ ensembles respectively.

3.2 Heavy doublet tuning

Figure 2 shows the dependence of $(2m_K^2 - m_{PS}^2)$ and m_D upon the light pseudoscalar mass squared for both ensembles, together with the physical point denoted by the black star. The kaon mass appears to be properly tuned at $\beta = 1.95$. The ensembles at $\beta = 1.90$, $a\mu_{\delta} = 0.190$ and $\beta = 2.10$ appear to have a value of the strange quark mass larger than the physical one, while the red point at $\beta = 1.90$, $a\mu_{\delta} = 0.197$ appears to be well tuned. The D meson appears heavier than in experiment for all three values of the lattice spacing. We currently have runs ongoing at both $\beta = 1.90$ and $\beta = 2.10$ with lower charm masses.

4. Light meson chiral perturbation theory fits

In order to extract the lattice spacing and light quark mass from our data, we perform a NLO SU(2) chiral perturbation theory fit of the m_{π} and f_{π} lattice data. We group our ensembles into sets with the same lattice spacing (set A at $\beta=1.90$, B at $\beta=1.95$ and set D at $\beta=2.10$). We have performed fits for various combinations of these sets, using the procedure described in [7]. We use continuum formulae and currently correct for finite volume effects as described in [20]. Note that since the quark mass enters the χ PT expression, in order to combine ensembles at different lattice spacings, we need to know the renormalization factor of the quark mass $Z_{\mu}=1/Z_{P}$, a computation which is not yet complete. Assuming that Z_{P} is effectively a function of β in the range of parameters

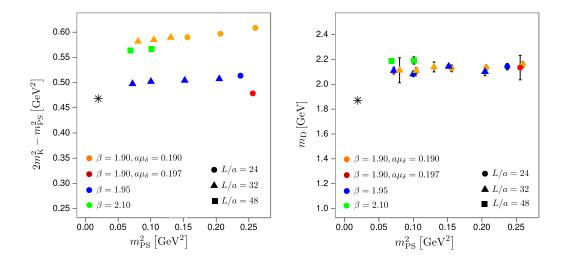


Figure 2: $2m_K^2 - m_{PS}^2$ and m_D as a function of m_{PS}^2 . The physical point is shown (black star) [21]. Data points have been scaled with the lattice spacing a = 0.0863(4) fm for $\beta = 1.90$, a = 0.0779(4) fm for $\beta = 1.95$ and a = 0.0607(2) fm for $\beta = 2.10$, where the errors quoted on the lattice spacing are only statistical.

we are considering, we can fit the ratio of those Z_P -values and lattice spacings and extract lattice spacings from the combined fit. In every fit we use as inputs the physical values of f_{π} and m_{π} , and extract f_0 , \bar{l}_3 , \bar{l}_4 and the lattice spacing. The results are listed in table 2, while figure 3 shows the fit to sets A, B and D combined.

set	pts	$f_0(\text{MeV})$	\bar{l}_3	\bar{l}_4	$a_{\beta=1.90}(\text{fm})$	$a_{\beta=1.95}(\text{fm})$	$a_{\beta=2.10}(\text{fm})$
A	5	120.96(7)	3.44(6)	4.77(2)	0.0859(5)	,	,
В	4	121.15(8)	3.70(7)	4.67(3)		0.0782(6)	
A & B	9	121.03(5)	3.54(5)	4.74(2)	0.0861(4)	0.0778(4)	
A & D	7	120.99(7)	3.42(7)	4.76(3)	0.0861(5)		0.0606(3)
B & D	6	121.20(8)	3.68(7)	4.65(3)		0.0785(6)	0.0609(3)
A & B & D	11	121.05(5)	3.53(5)	4.73(2)	0.0863(4)	0.0779(4)	0.0607(2)

Table 2: Results from the NLO SU(2) χ PT fits for various combinations of the ensembles. Errors are statistical only, extracted from 200 bootstrap samples. The column "pts" refers to the number of ensembles used in that fit.

The observed agreement between the extracted parameters suggests that our data for m_{PS} and f_{PS} are fairly well described by NLO SU(2) chiral perturbation theory. Using the spread of parameters as a rough estimate of the systematic error, it appears to be smaller than the statistical error for all quantities, with the exception of \bar{l}_3 . A more complete analysis of the systematic effects (analogous to [22]) is in progress. We expect to extend our analysis by including twisted mass chiral perturbation theory formulae as described in [23] and to use twisted mass finite volume effects formulae [24] when our neutral pion measurements are more complete.

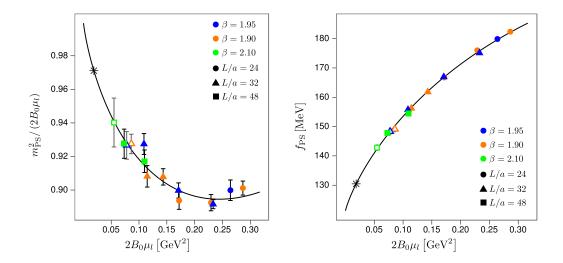


Figure 3: The charged pseudoscalar mass ratio $m_{\rm PS}^2/2B_0\mu_l$ and the pseudoscalar decay constant $f_{\rm PS}$ as a function of the mass parameter $2B_0\mu_l$, for the combined ensembles at $\beta=1.90$, $\beta=1.95$ and $\beta=2.10$. The scale is set by $a\mu_{\rm phys}$, the value of $a\mu_l$ at which the ratio $f_{\rm PS}^{[L=\infty]}/m_{\rm PS}^{[L=\infty]}$ assumes its physical value [21] $f_\pi/m_\pi=130.4(2)/135.0$ (black star). Open symbols refer to runs with full statistics, but not properly tuned to maximal twist within our criterion. Runs not at full statistics and those aimed at controlling the tuning of the strange and charm mass are not included in the plot.

5. Summary and Outlook

We have given an update of the status of the runs performed by the ETM Collaboration using $N_f = 2 + 1 + 1$ flavours of Wilson twisted mass fermions. We have given first results at a new finer $(\beta = 2.10)$ lattice spacing and attempted to combine them with existing datasets at two other lattice spacings $(\beta = 1.90 \text{ and } \beta = 1.95)$. The production of ensembles at the finest lattice spacing is still ongoing. As already stated, a complete control of the different systematic effects present in chiral fits of pion observables is still missing. ETMC is currently pursuing the direct determination of the renormalisation factor Z_P [12] appearing in the fits combining ensembles at several values of the lattice spacing. The preliminary results presented in this work are nevertheless very encouraging and suggest a fairly good description of our lattice data for m_{PS} and f_{PS} by NLO SU(2) chiral perturbation theory.

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