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Microscopic force for aerosol transport

Nils Roth,^{1,2} Muhamed Amin,^{1,3,4} Amit K. Samanta,¹ and Jochen Küpper^{1,2,5,*}

¹Center for Free-Electron Laser Science, Deutsches Elektronen-Synchrotron DESY, Notkestraße 85, 22607 Hamburg, Germany

²Department of Physics, Universität Hamburg, Luruper Chaussee 149, 22761 Hamburg, Germany

³Department of Sciences, University College Groningen, University of Groningen, Hoendiepskade 23/24, 9718 BG Groningen, Netherlands

⁴Groningen Biomolecular Sciences and Biotechnology Institute, University of Groningen, Nijenborgh 4, 9747 AG Groningen, Netherlands

⁵Center for Ultrafast Imaging, Universität Hamburg, Luruper Chaussee 149, 22761 Hamburg, Germany

A key ingredient for single particle diffractive imaging experiments is the successful and efficient delivery of sample. Current sample-delivery methods are based on aerosol injectors in which the samples are driven by fluid-dynamic forces. These are typically simulated using Stokes' drag forces and for micrometer-size or smaller particles, the Cunningham correction factor is applied. This is not only unsatisfactory, but even using a temperature dependent formulation it fails at cryogenic temperatures. Here we propose the use of a direct computation of the force, based on Epstein's formulation, that allows for high relative velocities of the particles to the gas and also for internal particle temperatures that differ from the gas temperature. The new force reproduces Stokes' drag force for conditions known to be well described by Stokes' drag. Furthermore, it shows excellent agreement to experiments at 4 K, confirming the improved descriptive power of simulations over a wide temperature range.

I. INTRODUCTION

The functionality of molecules and materials is strongly correlated to their atomic structure. Currently, biomolecules with sizes of a few nanometers are of particular interest for visualizing their high-resolution atomic structure in order to unravel the secrets of life and for developing, e. g., pharmaceuticals or novel biomimetic materials. With the advent of modern x-ray free-electron lasers (XFELs) coherent-single-particle diffractive imaging (SPI) has become feasible [1–5]. SPI allows to retrieve the three-dimensional (3D) atomic structure of nanoparticles by processing a series of two dimensional diffraction patterns of the corresponding isolated nanoparticles *in silico*.

SPI does not rely on highly-ordered crystalline sample, as in x-ray crystallography [6], nor on a mechanical sample support as in cryo-electron microscopy (CEM) [7, 8]. However, its diffraction-before-destruction approach [1] requires constant replenishment of identical targets in order to collect the necessary number of diffraction patterns for the 3D reconstruction. Sample sources are typically aerosol injectors producing tightly focused streams of nanoparticles [2]. However, the efficient delivery of identical nanoparticles is still a bottleneck for SPI experiments [9]. Our recently reported approach of using a cryogenic buffer-gas cooled aerosol injector [10] promises to overcome this limitation by increasing the reproducibility and control over the sample. There aerosolized nanoparticles were transported into a cryogenically-cooled helium-filled buffer-gas cell, where the nanoparticles were rapidly cooled [10]. The low temperature reduces particle losses

and broadening of the stream due to diffusion, and it allows for better subsequent nanoparticle control [11–13].

Generally, for best performance it is necessary to optimize the geometry of an aerosol injectors and the flow conditions of the carrier gas for every individual nanoparticle sample. For SPI experiments at room temperature simulations have already shown to be a useful tool to get insights on the sample delivery process and to aid during optimization [14]. However, for the cryogenic buffer-gas cell an improved description of the interaction between the gas and the nanoparticles is required for a better understanding of the particles' trajectories and phase-space distributions. These simulations should also reliably predict the final temperature of the nanoparticles and their cooling rate, an important aspect of buffer-gas cooling [10].

A general theory for describing the forces of an aerosol in a gas flow has yet to be found. For the purpose of modelling particle trajectories through aerodynamic focusing devices it is important to consider the usual working conditions that apply during the experiment. The pressure regimes can be described by the Knudsen number $Kn = \lambda/d_p$, which is the ratio of the mean free path of the fluid λ to the diameter of the particle d_p . In the experiment the pressure ranges, in principle, from atmosphere to ultrahigh vacuum. However, the actual focusing and transport that we are mainly interested in occurs in pressure regimes below 10 mbar, leading to $Kn \geq 100$ for nanometer size particles. The regime with $Kn \gg 1$ is called molecular flow. For this regime the boundary conditions assumed for Stokes famous drag equation do not hold any more and an empirical correction factor to the drag force, called “Cunningham correction factor”, was introduced [15] and quickly improved to today's formalism [16]. The empirical parameters were determined several times by fitting the drag force to experimental data, mostly

* Email: jochen.kuepper@cfel.de; website: <https://www.controlled-molecule-imaging.org>

from Milikan’s oil droplet experiments [17, 18]. Hence, this original description of the drag force is valid for the exact conditions in Milikan’s experiment, namely, air at room temperature and particles of hundreds nanometers or larger. The Cunningham correction factor depends on the gas and temperature [19] and the temperature-dependent correction factors were derived from kinetic theory considerations and related to experimental data for temperatures from 200 to 1000 K [20]. However, we are now trying to describe experiments in helium gas at temperatures down to 4 K [10].

Another approach to model the force of a rarefied fluid on a particle is to use the kinetic theory of gases. For the momentum transfer from gas molecules impinging and emerging from the surface of a particle, Epstein was able to reproduce the experimental data measured by Milikan by assuming 10 % specular reflection and 90 % diffuse reflection and the particle to be a perfect conductor [21]. This approach is valid across all gas types and temperatures. For particle sizes of current interest, which are in the order of 10–300 nm, the assumptions of a rigid body and the mainly diffuse scattering of Epstein’s model are still good approximations. For smaller systems more advanced treatment might be necessary: For particles with sizes of a few nm specular reflection become dominant and for small molecular sizes the treatment as rigid spheres fails and long range interactions, e. g., van der Waals interactions and electric multipole interactions, have to be taken into account [19].

The dimensions of the current aerodynamic focusing devices are on the order of millimeter to centimeter. When miniaturizing these devices it might become necessary to include forces important for microfluidic channels such as the Saffman force [22].

Epstein’s description would match the experimental conditions [10, 14] if it wasn’t for the large relative velocities between particles and gas and the temperature differences between gas and particles. These effects are incompatible with Epstein’s approach, although we note that Epstein’s model was improved in several ways, e. g., to the description of molecular-size particles based on Chapman-Enskog theory and the kinetic theory of gases [19, 23], by accounting for quantum effects [24], by deriving an analytical expression for the ratio between specular and diffuse reflection [25], through molecular dynamics simulations [26–28], or for non-isothermal fluids [29, 30] and lift forces due to the rotation of the particle or the velocity gradient in the flow field [22, 31, 32]. Unfortunately, none of these advances treats the needed adaptation for our experimental conditions. Hence, a new model based on Epstein’s original approach is formulated.

II. MODELING THE PARTICLE TRANSPORT IN AN AEROSOL INJECTOR FOR SPI EXPERIMENTS

A. Drag force in an aerosol injector for SPI experiments

For molecular flow the mean free path of the gas is much larger than the diameter of the particle. Hence, it is a valid assumption that the presence of the particle does not change the gas flow, e. g., the velocity distribution of the gas molecules. Assuming a Maxwell distribution, the number of gas molecules with velocities between (v_x, v_y, v_z) and $(v_x + dv_x, v_y + dv_y, v_z + dv_z)$ is

$$N_{v_x, v_y, v_z} dv_x dv_y dv_z = N \left(\frac{h}{\pi} \right)^{\frac{3}{2}} e^{-h(v_x^2 + v_y^2 + v_z^2)} dv_x dv_y dv_z, \quad (1)$$

with

$$h = \frac{m}{2kT}, \quad (2)$$

where N is the Number of molecules per unit Volume, m is the mass of the gas molecule, k is the Boltzmann constant and T is the gas temperature. From the point of view of a particle moving in a gas with speed U and velocity components $U_x = \alpha U$, $U_y = \beta U$ and $U_z = \gamma U$, with velocities along the x, y, z axes according to the fractions of speed α, β, γ , the velocity distribution is

$$N_{v_x, v_y, v_z} dv_x dv_y dv_z = N \left(\frac{h}{\pi} \right)^{\frac{3}{2}} e^{-h((v_x + \alpha U)^2 + (v_y + \beta U)^2 + (v_z + \gamma U)^2)} dv_x dv_y dv_z. \quad (3)$$

To determine the amount of gas molecules that hit the particle we assumed a surface element dS of the particle normal to the x direction. The volume that contains all particles with velocity $v_x + dv_x$ that will hit the surface in unit time is given by $v_x dS$ and the amount of particles in this volume is

$$n_{v_x, v_y, v_z} dv_x dv_y dv_z dS = v_x N_{v_x, v_y, v_z} dv_x dv_y dv_z dS. \quad (4)$$

The amount of momentum transferred to the particle in a given direction by an individual gas molecule impinging and sticking to the particle is given by $m(\alpha' v_x + \beta' v_y + \gamma' v_z)$. For a sphere with radius R , the z -axis defined to be normal to the plane through x and U , and the angle θ between y and U we obtain $\alpha = \cos(\theta)$, $\beta = \sin(\theta)$, $\gamma = 0$. Furthermore, for the momentum transferred in the direction of U we obtain $\alpha' = \cos(\theta)$, $\beta' = \sin(\theta)$, $\gamma' = 0$. The total amount of momentum transferred in the direction of U can be calculated analog to Epstein’s model, directly using (3) instead of an approximation for small U , by integrating over all surface elements $dS = R^2 \sin(\theta) d\theta d\phi$ and

all gas molecules impinging the particle in unit time. The amount of gas molecules impinging the particle per time is constant in the statistical limit, so is the momentum transferred per time, the force. It is given by

$$F_{\text{imp}} = \frac{p\sqrt{\pi}R^2}{2hU^2} \left(-2e^{-hU^2} \sqrt{h}U \left(1 + 2hU^2 \right) + \sqrt{\pi} \left(1 - 4hU^2 - 4h^2U^4 \right) \text{erf} \left(\sqrt{h}U \right) \right). \quad (5)$$

For specular reflection the x component of the velocity U of all gas molecules is changing sign, as does α , while everything else stays the same. Performing the integration, the momentum transferred by the reflecting gas molecules, and so the force due to reflection F_r , averages to zero and the total force in case of specular reflection F_{spec} is

$$F_{\text{spec}} = F_{\text{imp}} + F_r = F_{\text{imp}}. \quad (6)$$

Calculating the force for diffuse scattering F_{diff} requires to appropriately take the temperature difference between the gas and the particle into account. Assuming the gas molecule to thermalize to the particle's temperature during accommodation and it thus leaving the particle with a Maxwell Boltzmann distribution according to the particles temperature [21], it is possible to calculate the amount of momentum transfer by considering the conservation of the number of gas molecules:

$$n_{v_x, v_y, v_z, \text{imp}} dv_x dv_y dv_z dS = n_{v_x, v_y, v_z, \text{leav}} dv_x dv_y dv_z dS \quad (7)$$

The left side of (7) is identical to (4) and

$$n_{v_x, v_y, v_z, \text{leav}} = C_{\text{leav}} e^{-h'(v_x^2 + v_y^2 + v_z^2)}. \quad (8)$$

h' is defined equivalent to (2), but using the temperature of the particle instead of the gas temperature. Integrating (7) over the whole surface and all velocities, C_{leaving} is determined and thus the force on the particle:

$$F_{\text{diff}} = F_{\text{imp}} - \frac{2}{3} \frac{h}{\sqrt{h'}} p (\pi)^{\frac{3}{2}} R^2 U \quad (9)$$

The total force is assumed to be a combination of 10 % specular reflections and 90 % diffuse reflections [21]:

$$F_{\text{total}} = 0.1F_{\text{spec}} + 0.9F_{\text{diff}} \quad (10)$$

B. Temperature changes of the aerosol

The drag force (9) on a particle depends on its temperature. In the process of diffuse scattering the gas molecules are assumed to thermalize to the particle's temperature. This means, that that the velocity distribution of the impinging gas molecules differs from the the velocity distribution of the reflected ones not only due to U , but also due to different temperatures. Depending on whether

the particle's temperature is higher or lower than the gas temperature, the gas molecules take away energy from or deposit energy in the particle, respectively, in addition to the energy deposited in kinetic energy of the particle due to U . We assume this additional energy change will exclusively lead to a change in particle temperature, because it is even present with $U = 0$. Integrating over all molecules that hit the particle in unit time the change in energy is

$$\Delta E = \frac{p\sqrt{\pi}R^2}{4hh'} \left(-2e^{-hU^2} \sqrt{h} \left(5h' + 2h \left(2 + h'U^2 \right) \right) - \frac{\sqrt{\pi} \text{erf} \left(\sqrt{h}U \right)}{U} \left(3h' + 4h^2U^2 \left(2 + h'U^2 \right) + 4h \left(1 + 3h'U^2 \right) \right) \right) \quad (11)$$

which for small values of U , using the same velocity approximation as in Epstein's model, simplifies to

$$\Delta E = \frac{4p\sqrt{h\pi}R^2}{h'} - \frac{4p\sqrt{\pi}R^2}{\sqrt{h}} \quad (12)$$

A change of the particle's temperature is considered as a change ΔE of the total energy stored in all its degrees of freedom, i. e., its specific heat c_p . Thus the change in particle temperature per unit time is

$$\Delta T = \frac{\Delta E}{c_p m_p}, \quad (13)$$

with the particle's mass m_p .

C. Brownian Motion

So far we calculated the force by averaging over all single collisions the particle undergoes per unit time, which appropriately predicts the mean force on the particle. However, its actual trajectory depends further on its Brownian motion. For a numerical description of the Brownian motion using the Langevin equation [33] the force on the particle is split into a part F_{drag} that is proportional to U and a part F_b that is a random force. F_{drag} is in our case Equation 10, but using the same velocity approximation as in Epstein's model. F_b is assumed to be white noise consisting of an amplitude A and a random number r with zero mean and unit variance. The fluctuation-dissipation theorem defines the amplitude of the random force to be

$$A = \langle F_b(t_1)F_b(t_2) \rangle = 2kT\mu\delta(t_1 - t_2), \quad (14)$$

with $\mu = F_{\text{drag}}/U$. F_b considers the particle at rest with the gas and μ is calculated for the case of small U , where

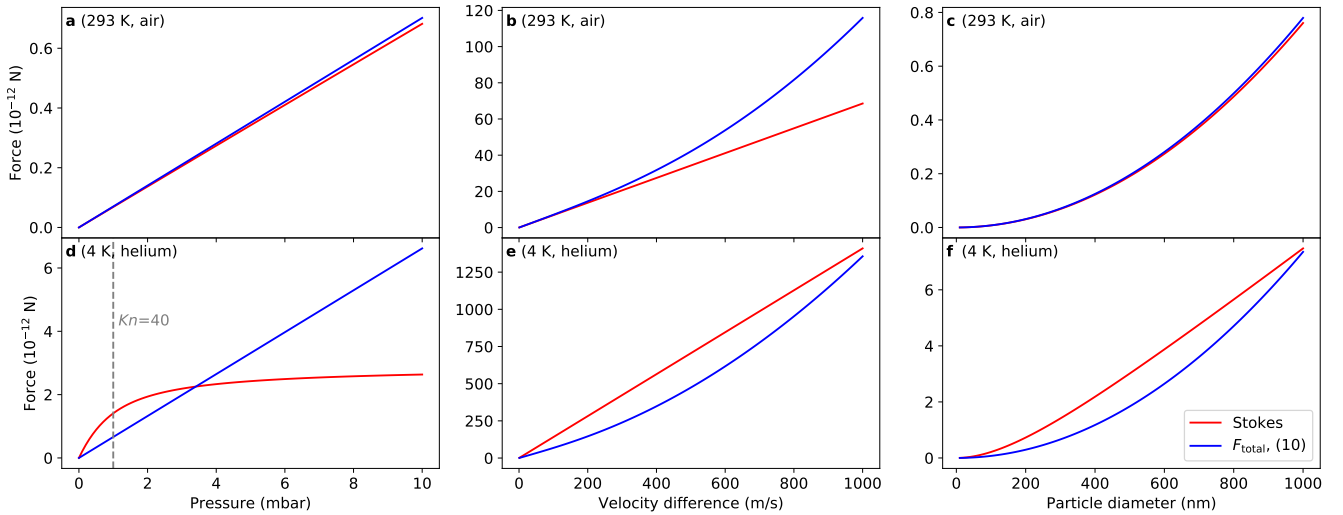


FIG. 1. Calculated drag force (10) in comparison to Stokes’ drag force as a function of (a, d) pressure, (b, e) velocity difference, and (c, f) particle diameter at (a–c) room temperature and (d–f) 4 K. Stokes’ drag force was calculated as described by Roth *et al.* [14] for room temperature and as described by Samanta *et al.* [10] for 4 K. While one of the parameters is varied the others are fixed at 1 mbar, 1 m/s, and 300 nm, respectively. The dashed gray line in (d) indicates the pressure where $Kn = 40$; see text for further details.

F_{total} is proportional to U . With a numerical representation of the delta function with a time step size Δt the Brownian force is

$$F_b = r \sqrt{\frac{\left(\frac{16}{3} + \frac{2}{3}\pi\sqrt{\frac{h}{h'}}\right) \sqrt{\frac{\pi}{h}} pmR^2}{\Delta t}}. \quad (15)$$

III. BENCHMARKING THE NEW FORCE

A. Comparison to Stokes’ drag force

In order to validate the new force, i.e., the model derived above, we compare it to the established model of Stokes’ drag force, which is known to produce reliable results for specific conditions, *vide supra*. Fig. 1 shows the calculated values of the new proposed drag force compared to Stokes’ drag force in dependence of the gas pressure, the velocity difference between particle and gas, and the particle diameter for room temperature and 4 K, respectively.

For room temperature, Fig. 1 a–c, and in a regime comparable to that in the Millikan experiment both models lead to nearly identical results. When the velocity differences becomes larger than 200 m/s the models diverge, which is expected as Stokes’ drag force is only applicable for comparable slow flows [34], whereas (10) appropriately describes that not only the amount of momentum transferred per gas molecule depends on U , but also the amount of gas molecules that hit the particle increases significantly when U approaches values comparable to the average speed of a single gas molecule.

For a cold gas at 4 K, Fig. 1 d–f, the functional behavior of the models differ. Here, Stokes’ force [20] is calculated as described by Samanta *et al.* [10]. For low pressures (large Kn) both forces have a linear pressure dependency, but with a flatter slope in case of (10). In general the results from (10) are below the calculated forces using Stokes in this region. However, for high pressures (small Kn) Stokes’ force approaches a constant value. The transition occurs around 1 mbar ($Kn \approx 40$). It is important to note that the region on the left to that transition ($Kn \gg 1$) is the region where the assumption for (10), that the presence of the particle is not influencing the gas flow, holds. Smaller predicted magnitudes of the force using (10) can be observed in Fig. 1 e,f as well. These lower values are in accordance with our previous experience using Stokes’ force at these conditions: In order to successfully describe the available experimental data using Stokes’ force, it was necessary to scale the force down by roughly a factor of 4 [10].

B. Comparison to Newton’s law of cooling

We validated the cooling rates (13), using (11), of our model against Newton’s law of cooling [10]. The resulting cooling rates are shown in Fig. 2. Newton’s law of cooling and our model show the same qualitative behaviour. As expected they both linearly depend on the temperature difference between the particle and the gas. Also the dependencies of pressure and particle diameter are very similar. In general, our new model leads to overall somewhat higher cooling rates, with the largest deviations roughly within a factor of two of Newton’s law of cooling.

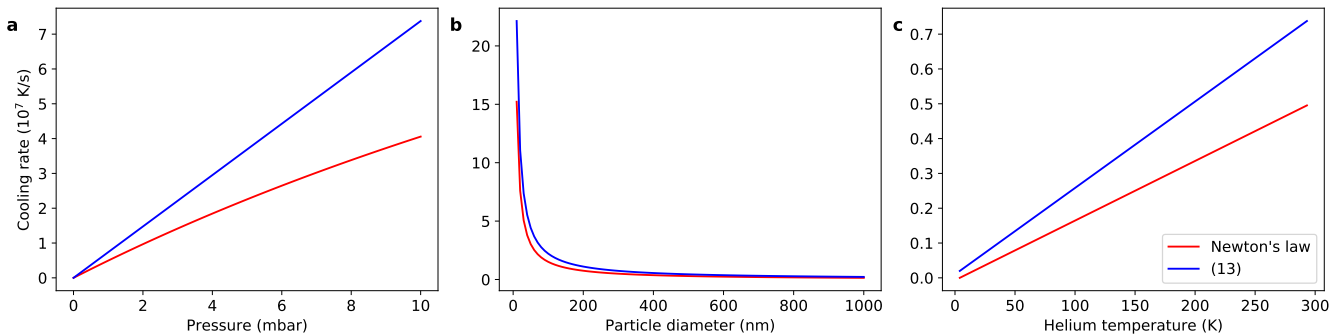


FIG. 2. Calculated values of the cooling rate (13) compared to Newton's law of cooling and its dependence on (a) pressure, (b) particle diameter, and (c) initial temperature of the particle for a polystyrene sphere in helium at 4 K. While one of the parameters is varied the others are fixed at 1 mbar, 300 nm., 293.15 K and 0.1 m/s.

The calculations of cooling rates using Newton's law of cooling involve several empirical approximations in the calculation of the Nusselt number and the heat transfer coefficients for forced convection [10]. In addition, another empirical parameter is needed to correct for the rarefied gas regime. The only empirical value in the new model (13) is the specific heat of the particle. Thus, it comes by no surprise, the two models do not produce identical quantitative results and the agreement we can see in Fig. 2 a–c is pretty good, with (13) being a much clearer, hence more trustworthy, model.

Fig. 3 shows calculated cooling rates using the full model (11) and the approximation for small velocities (12) for the change in energy. Up to relative velocities of 100 m/s the calculated cooling rate does not strongly depend on velocity and the approximation of small velocities is applicable. Hence, depending on the system of interest, it is a valid approach to use this assumption for the sake of computational speed.

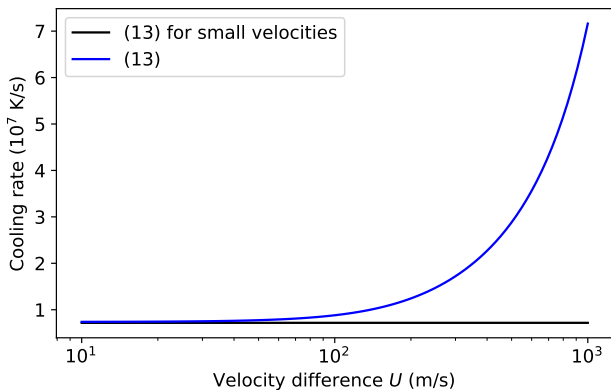


FIG. 3. Cooling rate as a function of the velocity difference U for a 300 nm polystyrene sphere in helium at 4 K and 1 mbar, calculated with (blue) the full model (13) and (black) the approximation for small velocity differences between particle and gas.

C. Comparison to experimental Results

We compared our model against recent experimental and computational results for the focusing of polystyrene spheres of diameter 220 nm in a helium buffer gas cell at 4 K [10]. Fig. 4 shows the full width at half maximum (FWHM) of the particle beams 10 mm behind the outlet of a cryogenic buffer-gas cell as a function of the helium flow rate, i. e., differing pressures and velocities.

As expected, Stokes' drag force, even with a temperature dependent slip correction, does not reproduce the experimental results at all, because it overestimates the force (*vide supra*). Only by scaling it down by a factor of 4 as in Fig. 4 of [10] comparable results can be achieved.

The microscopic drag force (10) derived here reproduces these experimental result very well, validating our simulation framework.

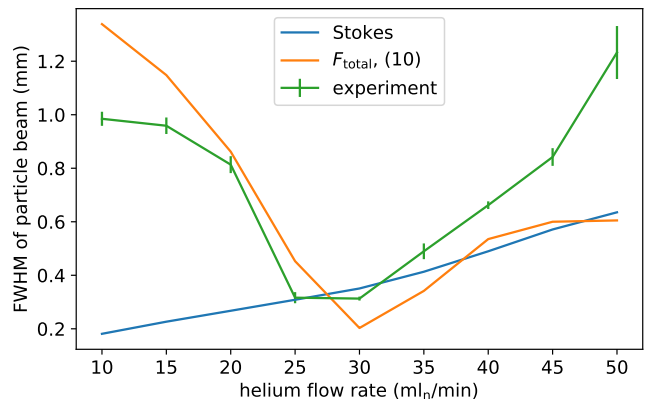


FIG. 4. The full width at half maximum (FWHM) of the particle beam transverse position 1 cm after the buffer gas cell for different helium mass flows, simulated using the temperature-dependent Stokes' drag force [20], simulated using (10), and experimentally measured.

IV. CONCLUSION

We have developed a new description of the flow of nanoparticles through a fluid, or the flow of a fluid past an object, which works over a large range of pressures, relative velocities, particle sizes, and temperatures. The model follows the ideas of Epstein’s formulation of the drag force and does not require additional empirical adjustments of the force. We have verified the model against Stokes’ drag force in the regime where the latter is valid and against experimental results for nanoparticles at cryogenic temperatures. Our new description works very well over this wide range of conditions.

The accurate descriptions enabled by our model are an important ingredient, for instance, for optimized sample injection in single-particle diffraction experiments: Hit rates can be significantly improved through reliable predictions of injection parameters before the actual measurement campaign at the large-scale facility. This does not only improve data quality, but allows to make much better use of the expensive x-ray pulses and thus enables better science.

As another benefit, the new model directly provides the particles’ temperatures and thus the cooling rate in the gas, which is important, for instance, for the shockfreezing of biological samples.

However, while our model is a good description for the conditions in current SPI experiments, the envisioned advances to single-molecule samples, i. e., proteins or other macromolecules with sizes of a few nanometers, will necessitate an advanced description of the nanoparticle-gas collisions, see the Introduction.

The model is implemented in our larger CMInject software package for the simulation of generic aerosol injectors, which we currently prepare for publication.

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- [1] R. Neutze, R. Wouts, D. van der Spoel, E. Weckert, and J. Hajdu, Potential for biomolecular imaging with femtosecond x-ray pulses, *Nature* **406**, 752 (2000).
 - [2] M. J. Bogan, W. H. Benner, S. Boutet, U. Rohner, M. Frank, A. Barty, M. M. Seibert, F. Maia, S. Marchesini, S. Bajt, B. Woods, V. Riot, S. P. Hau-Riege, M. Svenda, E. Marklund, E. Spiller, J. Hajdu, and H. N. Chapman, Single particle x-ray diffractive imaging, *Nano Lett.* **8**, 310 (2008).
 - [3] M. M. Seibert, T. Ekeberg, F. R. N. C. Maia, M. Svenda, J. Andreasson, O. Jönsson, D. Odić, B. Iwan, A. Rocker, D. Westphal, M. Hantke, D. P. Deponte, A. Barty, J. Schulz, L. Gumprecht, N. Coppola, A. Aquila, M. Liang, T. A. White, A. Martin, C. Caleman, S. Stern, C. Abergel, V. Seltzer, J.-M. Claverie, C. Bostedt, J. D. Bozek, S. Boutet, A. A. Miahnahri, M. Messerschmidt, J. Krzywinski, G. Williams, K. O. Hodgson, M. J. Bogan, C. Y. Hampton, R. G. Sierra, D. Starodub, I. Andersson, S. Bajt, M. Barthelmeß, J. C. H. Spence, P. Fromme, U. Weierstall, R. Kirian, M. Hunter, R. B. Doak, S. Marchesini, S. P. Hau-Riege, M. Frank, R. L. Shoeman, L. Lomb, S. W. Epp, R. Hartmann, D. Rolles, A. Rudenko, C. Schmidt, L. Foucar, N. Kimmel, P. Holl, B. Rudek, B. Erk, A. Hömke, C. Reich, D. Pietschner, G. Weidenspointner, L. Strüder, G. Hauser, H. Gorke, J. Ullrich, I. Schlichting, S. Herrmann, G. Schaller, F. Schopper, H. Soltau, K.-U. Kühnel, R. Andritschke, C.-D. Schröter, F. Krasnqi, M. Bott, S. Schorb, D. Rupp, M. Adolph, T. Gorkhovev, H. Hirsemann, G. Potdevin, H. Graafsma, B. Nilsson, H. N. Chapman, and J. Hajdu, Single mimivirus particles intercepted and imaged with an X-ray laser, *Nature* **470**, 78 (2011).
 - [4] A. Barty, J. Küpper, and H. N. Chapman, Molecular imaging using x-ray free-electron lasers, *Annu. Rev. Phys. Chem.* **64**, 415 (2013).
 - [5] E. Sobolev, S. Zolotarev, K. Giewekemeyer, J. Bielecki, K. Okamoto, H. K. N. Reddy, J. Andreasson, K. Ayyer, I. Barak, S. Bari, A. Barty, R. Bean, S. Bobkov, H. N. Chapman, G. Chojnowski, B. J. Daurer, K. Dörner, T. Ekeberg, L. Flückiger, O. Galzitskaya, L. Gelisio, S. Hauf, B. G. Hogue, D. A. Horke, A. Hosseinizadeh, V. Ilyin, C. Jung, C. Kim, Y. Kim, R. A. Kirian, H. Kirkwood, O. Kulyk, R. Letrun, D. Loh, M. Messerschmidt, K. Mühlig, A. Ourmazd, N. Raab, A. V. Rode, M. Rose, A. Round, T. Sato, R. Schubert, P. Schwander, J. A. Sellberg, M. Sikorski, A. Silenzi, C. Song, J. C. H. Spence, S. Stern, J. Sztuk-Dambietz, A. Teslyuk, N. Timneanu, M. Trebbin, C. Uetrecht, B. Weinhausen, G. J. Williams, P. L. Xavier, C. Xu, I. Vartanyants, V. Lamzin, A. Mancuso, and F. R. N. C. Maia, Megahertz single-particle imaging at the european XFEL, *Comm. Phys* **3**, 97 (2020), arXiv:1912.10796 [physics].
 - [6] Y. Shi, A glimpse of structural biology through x-ray crystallography, *Cell* **159**, 995 (2014).
 - [7] R. Fernandez and S. H. W. Scheres, Unravelling biological macromolecules with cryo-electron microscopy, *Nature* **537**, 339 (2016).
 - [8] Y. Sugita, H. Matsunami, Y. Kawaoka, T. Noda, and M. Wolf, Cryo-em structure of the ebola virus nucleoprotein-rna complex at 3.6 Å resolution, *Nature* **563**, 137 (2018).
 - [9] J. Bielecki, M. F. Hantke, B. J. Daurer, H. K. N. Reddy, D. Hasse, D. S. D. Larsson, L. H. Gunn, M. Svenda, A. Munke, J. A. Sellberg, L. Flueckiger, A. Pietrini, C. Nettelblad, I. Lundholm, G. Carlsson, K. Okamoto,

- N. Timneanu, D. Westphal, O. Kulyk, A. Higashiura, G. van der Schot, N.-T. D. Loh, T. E. Wysong, C. Bostedt, T. Gorkhover, B. Iwan, M. M. Seibert, T. Osipov, P. Walter, P. Hart, M. Bucher, A. Ulmer, D. Ray, G. Carini, K. R. Ferguson, I. Andersson, J. Andreasson, J. Hajdu, and F. R. N. C. Maia, Electrospray sample injection for single-particle imaging with x-ray lasers, *Science Advances* **5**, 10.1126/sciadv.aav8801 (2019).
- [10] A. K. Samanta, M. Amin, A. D. Estillore, N. Roth, L. Worbs, D. A. Horke, and J. Küpper, Controlled beams of shockfrozen, isolated, biological and artificial nanoparticles, *Struct. Dyn.* **7**, 024304 (2020), arXiv:1910.12606 [physics].
- [11] N. Eckerskorn, R. Bowman, R. A. Kirian, S. Awel, M. Wiedorn, J. Küpper, M. J. Padgett, H. N. Chapman, and A. V. Rode, Optically induced forces imposed in an optical funnel on a stream of particles in air and in vacuum, *Phys. Rev. Appl.* **4**, 064001 (2015).
- [12] Z. Li, L. Shi, L. Cao, Z. Liu, and J. Küpper, Acoustic funnel and buncher for nanoparticle injection, *Phys. Rev. Appl.* **11**, 064036 (2019), arXiv:1803.07472 [physics].
- [13] Y.-P. Chang, D. A. Horke, S. Trippel, and J. Küpper, Spatially-controlled complex molecules and their applications, *Int. Rev. Phys. Chem.* **34**, 557 (2015), arXiv:1505.05632 [physics].
- [14] N. Roth, S. Awel, D. A. Horke, and J. Küpper, Optimizing aerodynamic lenses for single-particle imaging, *J. Aerosol. Sci.* **124**, 17 (2018), arXiv:1712.01795 [physics].
- [15] E. Cunningham and J. Larmor, On the velocity of steady fall of spherical particles through fluid medium, *Proc. Royal Soc. London A* **83**, 357 (1910).
- [16] M. Knudsen and S. Weber, Luftwiderstand gegen die langsame Bewegung kleiner Kugeln, *Ann. Phys.* **341**, 981 (1911).
- [17] R. A. Millikan, The isolation of an ion, a precision measurement of its charge, and the correction of Stokes's law, *Science* **32**, 436 (1910).
- [18] R. A. Millikan, The general law of fall of a small spherical body through a gas, and its bearing upon the nature of molecular reflection from surfaces, *Phys. Rev.* **22**, 1 (1923).
- [19] Z. Li and H. Wang, Drag force, diffusion coefficient, and electric mobility of small particles. I. Theory applicable to the free-molecule regime, *Phys. Rev. E* **68**, 061206 (2003).
- [20] K. Willeke, Temperature dependence of particle slip in a gaseous medium, *J. Aerosol. Sci.* **7**, 381 (1976).
- [21] P. S. Epstein, On the resistance experienced by spheres in their motion through gases, *Phys. Rev.* **23**, 710 (1924).
- [22] I. Akhatov, J. Hoey, O. Swenson, and D. Schulz, Aerosol focusing in micro-capillaries: Theory and experiment, *J. Aerosol. Sci.* **39**, 691 (2008).
- [23] H. Tammert, Size and mobility of nanometer particles, clusters and ions, *J. Aerosol. Sci.* **26**, 459 (1995).
- [24] D. Drosdoff, A. Widom, and Y. Srivastava, Quantum drag forces on a sphere moving through a rarefied gas, *Phys. Rev. E* **71**, 051202 (2005).
- [25] F. L. Wiseman, An expression for the drag force of small spherical particles in an ideal-gas media analyzed using configuration-specific kinetic molecular theory, *Chem. Phys. Lett.* **465**, 175 (2008).
- [26] C. Liu and H. Wang, Nanoparticles in dilute gases: Fundamental equivalence between momentum accommodation and surface adsorption, *Phys. Rev. E* **99**, 042127 (2019).
- [27] Z. Li and H. Wang, Gas-nanoparticle scattering: A molecular view of momentum accommodation function, *Phys. Rev. Lett.* **95**, 014502 (2005).
- [28] H. Wang, Transport properties of small spherical particles, *Ann. N.Y. Acad. Sci.* **1161**, 484 (2009).
- [29] Z. Li and H. Wang, Thermophoretic force and velocity of nanoparticles in the free molecule regime, *Phys. Rev. E* **70**, 021205 (2004).
- [30] J. Wang and Z. Li, Thermophoretic force on micro- and nanoparticles in dilute binary gas mixtures, *Phys. Rev. E* **84**, 021201 (2011).
- [31] I. S. Akhatov, J. M. Hoey, O. F. Swenson, and D. L. Schulz, Aerosol flow through a long micro-capillary: collimated aerosol beam, *Microfluid. Nanofluid.* **5**, 215 (2007).
- [32] N. Liu and D. B. Bogy, Forces on a spherical particle with an arbitrary axis of rotation in a weak shear flow of a highly rarefied gas, *Phys. Fluids* **21**, 047102 (2009).
- [33] D. S. Lemons and A. Gythiel, Paul Langevin's 1908 paper "On the theory of Brownian motion", *Am. J. Phys.* **65**, 1079 (1997), translation of "Sur la théorie du mouvement brownien" in *C. R. Acad. Sci. (Paris)* **146**, 530–533 (1908).
- [34] G. G. Stokes, On the effect of the internal friction of fluids on the motion of pendulums, *Trans. Cambridge Phil. Soc.* **9**, 8 (1851).