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# The arithmetic of maximal curves, the Hesse pencil and Mestre curve <br> Anema, Ane Schelte Izaäk 

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## Propositions accompanying the PhD thesis

# The arithmetic of maximal curves, the Hesse pencil and the Mestre curve 

by Ane Anema

1. Let $C$ be a curve of genus $g$ over $\mathbb{F}_{q}$ with non-supersingular Jacobian variety. The upper bounds presented in Chapter 1 of the thesis for the case $g=1$ on the degree of $k / \mathbb{F}_{q}$ such that $C$ is maximal over $k$ generalize to the case $g>1$.
2. For infinitely many primes $p$ there exists a genus 2 curve $C$ over $\mathbb{F}_{p}$ such that $C$ is maximal over $\mathbb{F}_{p^{3}}$.
3. The hyperelliptic curve $C$ over $\mathbb{F}_{17}$ defined as $y^{2}=x^{9}+7 x^{5}-x$ is maximal over $\mathbb{F}_{17^{3}}$ and the twist of $C$ defined as $y^{2}=x^{9}+11 x^{5}+x$ is minimal over $\mathbb{F}_{17^{3}}$.
4. The work of Katz on Frobenius trace ratios in the Legendre family of elliptic curves over finite fields does not carry over in a natural way to the Hesse pencil.
5. There are at most countably many $j \in \mathbb{C}$ such that the Jacobian variety of the curve $D_{a, b}$ is isogeneous to a product of elliptic curves, where $a, b \in \mathbb{C}$ satisfy $j=1728 \frac{4 a^{3}}{4 a^{3}+27 b^{2}}$ and $D_{a, b}$ is defined as

$$
y^{2}=\left(x^{3}+a x+b\right)(a x+b)(a x-3 b) .
$$

The following two propositions are related to Chapter 6 of the thesis:
6. The maximal exponent 4 extension of $\mathbb{Q}$ unramified outside 2,5 and $\infty$ has degree $2^{14}$ over $\mathbb{Q}$ and is the splitting field of

$$
\begin{aligned}
& \left(x^{8}+4 x^{6}+4 x^{4}-2\right) \cdot\left(x^{8}+4 x^{6}+4 x^{4}-5\right) \cdot\left(x^{8}+4 x^{6}+4 x^{4}-10\right) \\
& \quad \cdot\left(x^{16}+6 x^{12}-4 x^{10}+8 x^{8}+8 x^{6}-4 x^{4}-8 x^{2}+4\right) .
\end{aligned}
$$

7. The number of isogeny classes of abelian surfaces $A$ over $\mathbb{Q}$ with good reduction at every prime $p \neq 2,5$ and $\mathbb{Q}(A[2]) / \mathbb{Q}$ a 2 -extension is at most $2.1 \cdot 10^{1435}$.
8. The scientific community would benefit from a professionally maintained collection of errata of scientific publications.
