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Aaij, R.; Adeva, B.; Adinolfi, M.; Affolder, A.; Ajaltouni, Z.; Akar, S.; Albrecht, J.; Alessio, F.; Alexander, M.; Ali, S.

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Measurement of the ratio of B_c^+ branching fractions to $J/\psi \pi^+$ and $J/\psi \mu^+ \nu_\mu$ final states

R. Aaij et al.*

(LHCb Collaboration) (Received 8 July 2014; published 27 August 2014)

The first measurement that relates semileptonic and hadronic decay rates of the B_c^+ meson is performed using proton-proton collision data corresponding to 1.0 fb⁻¹ of integrated luminosity collected with the LHCb detector. The measured value of the ratio of branching fractions, $\mathcal{B}(B_c^+ \to J/\psi \pi^+)/\mathcal{B}(B_c^+ \to J/\psi \mu^+ \nu_{\mu}) = 0.0469 \pm 0.0028(\text{stat}) \pm 0.0046(\text{syst})$, is at the lower end of available theoretical predictions.

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I. INTRODUCTION

The B_c^+ meson is the ground state of the $\bar{b}c$ quark-pair system and is the only meson in which weak-interaction decays of both constituents compete with each other [1]. About 70% of the decay width is expected to be due to the $c \rightarrow s$ transition, favored by the Cabibbo–Kobayashi– Maskawa quark-coupling hierarchy [2]. This decay process has recently been observed in the $B_c^+ \rightarrow B_s^0 \pi^+$ mode [3]. The complementary $b \rightarrow c$ transition, which is predicted to account for 20% of the decay width, is more straightforward to observe experimentally, having a substantial probability to produce a J/ψ meson. Among such decays, semileptonic $B_c^+ \to J/\psi \ell^+ \nu_\ell (\ell = \mu, e)$ and hadronic $B_c^+ \rightarrow J/\psi \pi^+$ channels have played a special role in many measurements. The semileptonic decays were used in the discovery of the B_c^+ meson [4], the measurements of its lifetime [4–7] and the measurement of the production cross section at the Tevatron [4]. The $B_c^+ \rightarrow J/\psi \pi^+$ decays were used to measure its lifetime [8], mass [9–11], production cross section at the LHC [11] and as a reference for other hadronic branching fraction measurements [12–17]. However, there is no experimental determination of the relative size of semileptonic and hadronic decay rates. The goal of this work is a measurement of the ratio of branching fractions.

$$\mathcal{R} \equiv \frac{\mathcal{B}(B_c^+ \to J/\psi\pi^+)}{\mathcal{B}(B_c^+ \to J/\psi\mu^+\nu_{\mu})},\tag{1}$$

and to test various theoretical models of B_c^+ meson decays, for which predictions of \mathcal{R} vary over a wide range, 0.050–0.091 [18–25].

II. ANALYSIS OUTLINE

Final states containing a muon offer a distinctive experimental signature and can be triggered and reconstructed with high efficiency at LHCb. Therefore, this analysis relies on J/ψ decays to $\mu^+\mu^-$. Since the neutrino is not detected, both of the studied decay modes are reconstructed using a J/ψ candidate plus a charged track (t^+) , referred to as the *bachelor* track. The mass of $J/\psi \pi^+$ signal candidates peaks at the B_c^+ mass within the experimental resolution, allowing a straightforward signal-yield extraction in the presence of relatively small backgrounds under the signal peak. The main challenge in this analysis is the signal-yield extraction for the $B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu$ decay mode, as the $J/\psi\mu^+$ mass $(m_{J/\psi\mu})$ distribution is broad due to the undetected neutrino. To suppress the dominant backgrounds, the analysis is restricted to the $m_{J/\psi\mu} > 5.3 \text{ GeV}$ end point region and uses the mass-shape difference between the signal and the remaining background to extract the $B_c^+ \rightarrow J/\psi \mu^+ \nu_{\mu}$ signal yield [26]. In this mass region the neutrino has low energy; thus the $B_c^+ \rightarrow J/\psi \mu^+ \nu_{\mu}$ candidates are kinematically similar to the $B_c^+ \rightarrow J/\psi \pi^+$ candidates. Therefore, many reconstruction uncertainties cancel in the ratio of their rates, allowing a precise measurement of $\mathcal{R}(m_{J/\psi\mu} > 5.3 \text{ GeV})$. This end point value is then extrapolated to the full phase space using theoretical predictions. Since the B_c^+ and J/ψ are both 1S heavy quarkonia states, the form factors involved in predicting the extrapolation factor and the shape of the mass distribution at the end point have only modest model dependence.

III. DETECTOR AND DATA SAMPLE

The analysis is performed on a data sample of pp collisions at a center-of-mass energy of 7 TeV, collected during 2011 by the LHCb experiment and corresponding to an integrated luminosity of 1.0 fb⁻¹. The LHCb detector [27] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing *b* or *c* quarks. The detector includes a

^{*}Full author list given at the end of the article.

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high-precision tracking system consisting of a silicon-strip vertex detector surrounding the pp interaction region [28], a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm, and three stations of silicon-strip detectors and straw drift tubes [29] placed downstream of the magnet. The tracking system provides a measurement of momentum, p, with a relative uncertainty that varies from 0.4% at low momentum to 0.6% at 100 GeV. The minimum distance of a track to a primary vertex, the impact parameter (IP), is measured with a resolution of $(15 + 29/p_T) \mu m$, where p_T is the component of p transverse to the beam, in GeV. Different types of charged hadrons are distinguished using information from two ring-imaging Cherenkov detectors [30]. Photon, electron and hadron candidates are identified by a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic calorimeter and a hadronic calorimeter. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers [31].

Simulated event samples are generated for the signal decays and the decay modes contributing to the background. In the simulation, pp collisions are generated using PYTHIA [32] with a specific LHCb configuration [33]. The production of B_c^+ mesons, which is not adequately simulated in PYTHIA, is performed by the dedicated generator BCVEGPY [34]. Several dynamical models are used to simulate $B_c^+ \rightarrow J/\psi \mu^+ \nu_{\mu}$ decays. Decays of hadronic particles are described by EVTGEN [35], in which final-state radiation is generated using PHOTOS [36]. The interaction of the generated particles with the detector and its response are implemented using the GEANT4 toolkit [37] as described in Ref. [38].

IV. DATA SELECTION

This analysis relies on $J/\psi t^+$ candidates satisfying the trigger [39], which consists of a hardware stage, based on information from the muon system, followed by a two-level software stage, which applies a full event reconstruction. At the hardware stage, a muon with $p_{\rm T} > 1.5$ GeV, or a pair of muons with $\sqrt{p_{T1}p_{T2}} > 1.3$ GeV, is required. The subsequent lower-level software triggers require a chargedparticle track with $p_{\rm T} > 1.7 \text{ GeV}$ ($p_{\rm T} > 1.0 \text{ GeV}$ if identified as muon) and with an IP relative to any primary *pp*-interaction vertex (PV) larger than 100 μ m. A dimuon trigger, which requires a large dimuon mass, $m_{\mu^+\mu^-}$ > 2.7 GeV, and each muon to have $p_{\rm T} > 0.5$ GeV, complements the single track triggers. The final software trigger stage requires either a $J/\psi \rightarrow \mu^+\mu^-$ candidate with a J/ψ decay vertex separation from the nearest PV of at least three standard deviations, or that a two- or three-track combination, which includes a muon, is identified as a secondary vertex using a multivariate selection [39].

In the offline analysis, $J/\psi \rightarrow \mu^+\mu^-$ candidates are selected with the following criteria: $p_{\rm T}(\mu) > 0.9$ GeV,

 $p_{\rm T}(J/\psi) > 1.5$ GeV, χ^2 per degree of freedom (ndf) for the two muons to form a common vertex $\chi^2_{vtx}(\mu^+\mu^-)/$ ndf < 9, and a mass consistent with the J/ψ meson. The separation of the J/ψ decay vertex from the nearest PV must be at least five standard deviations. The bachelor track, and at least one of the muons from the decay of the J/ψ meson, must not point to any PV, through the requirement $\chi^2_{\rm IP} > 9$. The quantity $\chi^2_{\rm IP}$ is defined as the difference between the χ^2 of the PV fitted with and without the considered particle. The bachelor track must not be collinear within 0.8° with either of the muons from the J/ψ meson decay and must satisfy $p_{\rm T} > 0.5 \text{ GeV}$ (> 1.0 GeV for π^+). A loose kaon veto is applied to the pion candidates, $\ln[\mathcal{L}(K)/\mathcal{L}(\pi)] < 5$, where \mathcal{L} is the particle identification likelihood [40]. The J/ψ candidates are combined with the bachelor tracks in a kinematic fit to form B_c^+ candidates with the known J/ψ mass and the B_c^+ vertex used as constraints. The B_c^+ candidate must satisfy $\chi^2_{\rm vtx}(J/\psi t^+)/$ ndf < 9 and have a pseudoproper decay time greater than 0.25 ps. The pseudoproper decay time is determined as $L \cdot m_{J/\psi t} / |\vec{p}_{J/\psi t}|$, where L is the projection of the distance between the B_c^+ production and decay vertices onto the direction of the $J/\psi t^+$ momentum $\vec{p}_{J/\psi t}$ and $m_{J/\psi t}$ is the $J/\psi t^+$ mass.

Four discriminating variables (x_i) are used in a likelihood ratio to improve the background suppression. Three of the variables are common between the two channels: $\chi^2_{\rm vtx}(J/\psi t^+)/{\rm ndf}, \chi^2_{\rm IP}(B_c^+)$, and the cosine of the angle between the J/ψ meson and the bachelor track transverse momenta. The latter quantity peaks at positive values for the signal as the B_c^+ meson has a high transverse momentum. Background events in which particles are combined from two different B decays usually peak at negative values, while those due to random combinations of particles are more uniformly distributed. The $\chi^2_{IP}(B_c^+)$ variable is small for $B_c^+ \to J/\psi \pi^+$ decays since the B_c^+ momentum points back to the PV. For $B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu$ candidates, the pointing is only approximate since the neutrino is not reconstructed. However, $\chi^2_{\rm IP}(B_c^+)$ is often smaller than for the background events because the neutrino has low momentum. The fourth variable for the $J/\psi \pi^+$ mode is $\chi^2_{\rm IP}(t^+)$, while for the $J/\psi\mu^+\nu_\mu$ mode it is the pseudoproper decay time, as $\chi^2_{\rm IP}(t^+)$ is found to be ineffective for this channel. The four one-dimensional signal probability density functions (PDFs), $\mathcal{P}_{sig}(x_i)$, are obtained from a simulated sample of signal events. The background PDFs, $\mathcal{P}_{\rm bkg}(x_i)$, are obtained from the data in the $B_c^+ \to J/\psi \pi^+$ mass sidebands (5.35-5.80 and 6.80-8.50 GeV) and from the simulation of inclusive backgrounds from $B_{u,d,s} \rightarrow$ $J/\psi X$ decays (X denotes one or more particles) for the $B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu$ candidates. The requirement $\Delta_{\text{sig/bkg}}$ $(-2 \ln \mathcal{L}) = -2 \sum_{i=1}^4 \ln[\mathcal{P}_{\text{sig}}(x_i)/\mathcal{P}_{\text{bkg}}(x_i)] < 1.0 \quad (< 0.0)$ preserves about 93% (87%) of signal events for $B_c^+ \rightarrow$ $J/\psi \pi^+$ $(B_c^+ \to J/\psi \mu^+ \nu_\mu$ with $m_{J/\psi \mu} > 5.3$ GeV) and efficiently suppresses the backgrounds. These requirements minimize the expected average statistical uncertainty on the signal yields, given the observed background levels in each channel.

V. EXTRACTION OF THE $B_c^+ \rightarrow J/\psi \pi^+$ SIGNAL

An extended maximum likelihood fit to the unbinned distribution of observed $m_{J/\psi\pi}$ values yields $N_{J/\psi\pi} = 839 \pm 40 \ B_c^+ \rightarrow J/\psi\pi^+$ signal events and is shown in Fig. 1.

The signal is represented in the fit by a double-sided Crystal Ball functionn [41]. The peak position, the Gaussian mass resolution and the peak amplitude are free parameters in the fit, while the parameters describing small non-Gaussian tails are fixed by a fit to the simulated signal distribution. Using a Gaussian function to model the signal results in a 2.3% relative change in \mathcal{R} value, and this is assigned as the systematic uncertainty. The background is smoothly distributed and modeled by an exponential function. Varying the background parametrization and the fit range results in up to a 0.6% relative change in \mathcal{R} . A small background from $B_c^+ \to J/\psi K^+$ decays, peaking 37 MeV below the signal peak, is also included in the fit with all shape parameters fixed from the simulation. Its normalization is constrained to be 1%of the fitted signal amplitude, as predicted by the measured ratio of the branching fractions [15] scaled by an efficiency ratio of 15% obtained from the simulation. The relative systematic uncertainty on \mathcal{R} related to this fit component is 0.1%.

VI. EXTRACTION OF THE $B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu$ SIGNAL

To measure the $B_c^+ \to J/\psi \mu^+ \nu_\mu$ rate, feed down from other $B_c^+ \to f$, $f \to J/\psi \mu^+ \nu_\mu X$ decays must be accounted for. Decays to excited charmonium states $[f = \psi_f \mu^+ \nu_\mu,$



FIG. 1 (color online). Invariant-mass distribution of $B_c^+ \rightarrow J/\psi \pi^+$ candidates (black data points). The maximum likelihood fit of the B_c^+ signal is superimposed (blue solid line). Individual fit components are also shown: (dashed blue line) the signal, (red long-dashed line) the background and (green dotted line) $B_c^+ \rightarrow J/\psi K^+$ feed down.

with $\psi_f = \chi_{cJ}$ or $\psi(2S)$] and states containing τ leptons $(f = J/\psi \tau^+ \nu_\tau)$ are the dominant contributions. Since the rates for such decays have not been measured, we rely on theoretical predictions for

$$R_f \equiv \frac{\mathcal{B}(B_c^+ \to f)}{\mathcal{B}(B_c^+ \to J/\psi\mu^+\nu_\mu)}.$$
 (2)

Although the spread in R_f predictions is large (see below), the related systematic uncertainty is minimized by restricting the analysis to the high $J/\psi\mu^+$ mass region. Unreconstructed decay products in the $\psi_f \rightarrow J/\psi X$ transitions $(X = \gamma, \pi\pi, \pi^0, \eta, \gamma\gamma)$ or $\tau^+ \to \mu^+ \nu_\mu \bar{\nu}_\tau$ decays carry energy away, lowering the $J/\psi\mu^+$ mass relative to that from direct $B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu$ decays, as illustrated in Fig. 2. The selection requirement in $m_{J/\psi\mu}$ is chosen to eliminate the backgrounds from $B_{u,d,s}$ decays to J/ψ mesons associated with hadrons, with one of the hadrons misidentified as a muon. These backgrounds are large because the $B_{u,d,s}$ production rates are orders of magnitude higher than for B_c^+ . Since many exclusive decay modes with various hadron multiplicities and unknown branching ratios contribute, the $m_{J/\psi\mu}$ shape of such backgrounds is difficult to predict. The 5.3 GeV lower limit on $m_{J/\psi\mu}$ is above the kinematic limit for $B_u^+ \to J/\psi h^+$ decays, with h^+ denoting a charged kaon or pion, as illustrated in Fig. 2. The $B_{u,d,s}$ backgrounds in the selected region are much smaller, and are from $B_{u,d,s} \rightarrow J/\psi X$ decays paired with a bachelor μ^+ originating from a semileptonic decay of the companion bquark in the produced bb pair. Simulation of b-baryon decays to final states involving a J/ψ meson shows that they also contribute via this mechanism. The shape of such



FIG. 2 (color online). Distribution of $m_{J/\psi\mu}$ for $B_c^+ \rightarrow J/\psi\mu^+\nu_{\mu}$ candidates selected in simulated event samples of (blue filled points) the signal, (green filled points) the B_c^+ feed down and (red filled squares) the $B_{u,d,s}$ backgrounds. Relative normalization is derived from the fit to the data described later in the text. The part of the spectrum included in the fit is indicated with a vertical dashed black line. The B_c^+ feed down distribution is also shown after magnifying its normalization by a factor of 10 (green dashed histogram).

combinatorial backgrounds is less sensitive to the details of the composition of *b*-hadron decay modes, and thus is easier to predict. Since the combinatorial backgrounds are dominated by genuine muons, the analysis is not sensitive to the estimation of muon misidentification rates and associated systematic uncertainties.

The $m_{J/\psi\mu}$ signal shape is dominated by the end point kinematics, whereas the combinatorial background is smooth and extends beyond the kinematic limit for the $B_c^+ \rightarrow J/\psi\mu^+\nu_\mu$ decays. The signal yield is determined by a fit to the $m_{J/\psi\mu}$ distribution. The feed down background is small as discussed in detail below. Its shape is constrained by simulation, while its normalization is related to the signal yield via theoretical predictions. The unbinned maximum likelihood fit is performed simultaneously to the $m_{J/\psi\mu}$ distribution in data and the signal and background distributions from simulation, in the range of 5.3 to 8.0 GeV, and gives $N_{J/\psi\mu} = 3537 \pm 125$ signal events. The $m_{J/\psi\mu}$ distributions and the fit results are displayed in Fig. 3. The fit is described in detail below.

The total PDF used in the fit is the sum of the signal PDF (\mathcal{P}_{sig}) , the feed down background PDF (\mathcal{P}_{fd}) and the combinatorial background PDF (\mathcal{P}_{bkg}) ,

$$\mathcal{P}(m_{J/\psi\mu}) \propto N_{J/\psi\mu} (\mathcal{P}_{\text{sig}}(m_{J/\psi\mu}) + \alpha \mathcal{P}_{\text{fd}}(m_{J/\psi\mu})) + N_{\text{bkg}} \mathcal{P}_{\text{bkg}}(m_{J/\psi\mu}),$$
(3)

where α is the feed-down-to-signal yield ratio and $N_{\rm bkg}$ is the combinatorial background yield. The signal shape is dominated by the end point kinematics; thus it is modeled as

$$\mathcal{P}_{sig}(m_{J/\psi\mu}) \propto PS(m_{J/\psi\mu})(1 + s_1 \bar{m}_{J/\psi\mu}),$$
 (4)

where $\bar{m}_{J/\psi\mu} = m_{J/\psi\mu} - 5.3 \text{ GeV}$ and $PS(m_{J/\psi\mu})$ corresponds to the uniform distribution in the $B_c^+ \rightarrow J/\psi\mu^+\nu_\mu$ three-body phase-space,

$$PS(m_{J/\psi\mu}) = \frac{M_{B_c}^2 - m_{J/\psi\mu}^2}{m_{J/\psi\mu}} \times \sqrt{m_{J/\psi\mu}^2 - (M_{J/\psi} + M_{\mu})^2} \times \sqrt{m_{J/\psi\mu}^2 - (M_{J/\psi} - M_{\mu})^2}, \quad (5)$$

with the J/ψ and μ masses $(M_{J/\psi}$ and $M_{\mu})$ set to their known values [42] and M_{B_c} set to an effective value, which



FIG. 3 (color online). Invariant-mass distribution of $J/\psi\mu^+$ pairs from $B_c^+ \rightarrow J/\psi\mu^+\nu_\mu$ candidates (black data points) for (top left) the data, (bottom left) $B_c^+ \rightarrow J/\psi\mu^+\nu_\mu$ signal simulation, (top right) $B_{u,d,s} \rightarrow J/\psi X$ background simulation and (bottom right) B_c^+ feed down simulation. The unbinned maximum likelihood fit of the B_c^+ signal is superimposed (blue solid line). Individual fit components are also shown: (blue short-dashed line) the signal, (red long-dashed line) the background and (green dotted line) B_c^+ feed down.

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is slightly higher than the B_c^+ mass to account for detector resolution effects. Setting M_{B_c} to the known B_c^+ mass [42] changes the signal yield by a negligible amount. Deviations from the uniform distribution are allowed by the linear term, with the s_1 coefficient determined by the simultaneous fit to the simulated signal distribution and the data. The simulation based on the Kiselev *et al.* QCD sum rules model [22] is used in the default fit. The models of Ebert *et al.* [23], based on a relativistic quasipotential Schrödinger approach, and ISGW2 [43], based on a nonrelativistic constituent quark model with relativistic corrections, alter the determined signal yield by +0.2% and -0.4%, respectively. Relying on the data themselves to determine the signal shape changes the signal yield by +0.7%. The latter value is taken as a systematic error.

The feed down includes contributions from the following B_c^+ decay modes $f = \psi(2S)\mu^+\nu_\mu$, $\chi_{cJ}\mu^+\nu_\mu$ and $J/\psi\tau^+\nu_\tau$. Feed down from $B_c^+ \to B_{d,s}\mu^+\nu_\mu$ and $B_c^+ \to J/\psi$ plus hadrons is also investigated and found negligible. Their individual proportions with respect to the signal yield are determined as

$$\alpha_f = R_f \mathcal{B}_{\operatorname{casc} f} R_{ef},\tag{6}$$

and then added, $\alpha = \sum_{f} \alpha_{f}$, where $\mathcal{B}_{casc f}$ is the sum of the measured branching fractions [42] for the ψ_f state to decay to a J/ψ meson by emission of unreconstructed photons or light hadrons, and R_{ef} is the ratio of the feed down and the signal reconstruction efficiencies [44]. This quantity is small because of the $m_{J/\psi\mu} > 5.3$ GeV requirement. For χ_{cJ} states the sum extends over the three J values, $R_f \mathcal{B}_{casc f} =$ $\sum_{J=0,1,2} R_{fJ} \mathcal{B}_{\text{casc } fJ}$. The values of the parameters affecting the estimate of the feed down fraction are summarized in Table I. Theoretical predictions for R_f for the $B_c^+ \rightarrow$ $\psi(2S)\mu^+\nu_\mu$ feed down mode vary over a wide range, 0.009–0.185 [18,21–23,25,43,45]. An average of the highest and the lowest prediction is taken for the nominal estimate, and half of the difference is taken for the systematic error. The theoretical uncertainties in the $R_f \mathcal{B}_{casc f}$ values for the dominant $B_c^+ \rightarrow \chi_{cJ} \mu^+ \nu_{\mu}$ feed down mode are smaller, 0.032-0.038 [24,46,47]. The spread is also limited for theoretical predictions of R_f for the $B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau$ decay, 0.237–0.283 [19,22,24,47]. The simulated distributions for the individual feed down modes are mixed according to the proportions resulting from the $R_f \mathcal{B}_{casc f}$ values and then parametrized as

$$\mathcal{P}_{\rm fd}(m_{J/\psi\mu}) \propto {\rm PS}(m_{J/\psi\mu})(1 + f_1 \bar{m}_{J/\psi\mu} + f_2 \bar{m}_{J/\psi\mu}^2), \ (7)$$

where f_1 and f_2 are parameters determined by the fit. The effect of the unreconstructed decay products X is to lower the effective M_{B_c} value in Eq. (5). Varying the feed down fraction within its uncertainty changes the signal yield by up to 0.6%.

The combinatorial $B_{u,d,s}$ background is parametrized with an exponential function. The tail of the $B_u^+ \rightarrow J/\psi h^+$ distribution, with the light hadron misidentified as a muon, may enter the signal region because of detector resolution. We parametrize it with a Gaussian function, $G(m_{J/\psi\mu})$, with a mean value and width fixed to the results of the fit to the simulated $B_u^+ \rightarrow J/\psi h^+$ distribution. The exponential and $G(m_{J/\psi\mu})$ functions together define $\mathcal{P}_{bkg}(m_{J/\psi\mu})$,

$$\mathcal{P}_{\rm bkg}(m_{J/\psi\mu}) \propto c \, N_e e^{b_1 \bar{m}_{J/\psi\mu} + b_2 \bar{m}_{J/\psi\mu}^2} + (1-c) G(m_{J/\psi\mu}),$$

where N_e normalizes the exponential function to 1. The combinatorial background fraction c and the polynomial coefficients b_1 and b_2 are free parameters in the simultaneous fit to the simulated $B_{u,d,s} \rightarrow J/\psi X$ distribution and to the distribution in the data. To avoid relying on simulation for the absolute values of the muon misidentification rates, c is allowed to vary independently in the fit to the simulated and the observed distributions. A systematic uncertainty of 1.8% is assigned to this background parametrization based on fit results in which either the Gaussian term is neglected or the exponential function is replaced by a sum of two exponential functions.

Varying the upper limit of the mass range used in the fit from 8.0 down to 6.75 GeV results in a signal-yield change of up to 1.5%. Varying the corresponding lower limit from its default value of 5.3 to 5.1 GeV, thus including the peak of the $B_u^+ \rightarrow J/\psi h^+$ component (see Fig. 2), or to 5.5 GeV, thus avoiding the tail of that component, results in a relative change in the \mathcal{R} value of up to 1.6%.

The default method of the $B_c^+ \rightarrow J/\psi\mu^+\nu_\mu$ signal-yield determination relies on simulation to predict the signal and background shapes in the $m_{J/\psi\mu}$ distribution. An alternative approach relies on simulation to predict the signal and background shapes of the $\Delta_{\text{sig/bkg}}(-2 \ln \mathcal{L})$ distribution. Correlations between $m_{J/\psi\mu}$ and $\Delta_{\text{sig/bkg}}(-2 \ln \mathcal{L})$ variables are small. The requirement on the $\Delta_{\text{sig/bkg}}(-2 \ln \mathcal{L})$ value is removed. The $m_{J/\psi\mu}$ range is restricted to 5.3–6.1 GeV to exclude the backgrounds above the B_c^+ kinematic limit.

TABLE I. Values of the parameters affecting the estimate of the feed down fraction in the fit to the $m_{J/\psi\mu}$ distribution. For $B_c^+ \rightarrow \chi_{cJ} \mu^+ \nu_{\mu}$, $\sum_{J=0,1,2} R_{fJ} \mathcal{B}_{casc fJ}$ is listed.

Feed down mode	R_{f}	$\mathcal{B}_{\operatorname{casc} f}$	R_{ef}	$lpha_{f}$
$B_c^+ \rightarrow \psi(2S)\mu^+\nu_\mu$	0.009-0.185	0.598 ± 0.006	0.118 ± 0.004	0.0069 ± 0.0062
$B_c^+ \rightarrow \chi_{cJ} \mu^+ \nu_{\mu}$	0.032-0.038		0.364 ± 0.009	0.0127 ± 0.0011
$B_c^+ \to J/\psi \tau^+ \nu_{\tau}$	0.237-0.283	0.1741 ± 0.0004	0.014 ± 0.001	0.0006 ± 0.0001
Total α				0.0202 ± 0.0063

The signal and combinatorial background yields are determined by a fit to the $\Delta_{sig/bkg}(-2 \ln \mathcal{L})$ distribution in the data. The B_c^+ feed down simulation predicts a similar $\Delta_{sig/bkg}(-2 \ln \mathcal{L})$ shape as for the $B_c^+ \rightarrow J/\psi \mu^+ \nu_{\mu}$ signal. Therefore, this contribution is not represented explicitly in the fit to the $\Delta_{sig/bkg}(-2 \ln \mathcal{L})$ distribution, but is subtracted from the fitted signal yield according to the feed down fraction α . Taking into account the differences in signal efficiency, the $B_c^+ \rightarrow J/\psi \mu^+ \nu_{\mu}$ signal yield is consistent with that resulting from the $m_{J/\psi\mu}$ fit method within 0.5%, which is included as an additional systematic uncertainty due to the $\Delta_{sig/bkg}(-2 \ln \mathcal{L})$ requirement in the nominal approach.

VII. RESULTS

The ratio of the reconstruction efficiencies between the two B_c^+ signal modes, as determined from simulation, is $\epsilon(B_c^+ \to J/\psi \mu^+ \nu_\mu)/\epsilon(B_c^+ \to J/\psi \pi^+) = 1.14 \pm 0.01$ (statistical error) for $B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu$ events generated in the end point region. Using different $B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu$ form factor models changes this efficiency ratio by up to 1.3%. Efficiencies of the pion and muon particle identification (PID) requirements have systematic uncertainties of 0.8% and 1.9%, respectively. The efficiency-ratio systematic uncertainties from the B_c^+ lifetime assumed in the simulation is 0.2% due to the cancelations between the two decay modes. The fraction of multiple signal candidates per event is 0.1% for $B_c^+ \to J/\psi \pi^+$ and 1.9% for $B_c^+ \to$ $J/\psi\mu^+\nu_\mu$ decays. To check for possible biases due to the neglected correlations between multiple candidates, one candidate is randomly chosen, which changes the \mathcal{R} result by 0.4%. The systematic uncertainty associated with the limited knowledge of the efficiency of the $\Delta_{\text{sig/bkg}}(-2 \ln \mathcal{L})$ requirement for $B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu$ decays is included using the results of the $\Delta_{sig/bkg}(-2\ln\mathcal{L})$ fit. To study the corresponding uncertainty for $B_c^+ \rightarrow J/\psi \pi^+$ decays, the $\Delta_{\text{sig/bkg}}(-2\ln \mathcal{L})$ requirement is varied, resulting in a 2% variation. The systematic uncertainty associated with the trigger simulation is 3.4%, as estimated by modifying the trigger requirements. The systematic errors are summarized in Table II. The total relative systematic uncertainty on $\mathcal{R}(m_{J/wu} > 5.3 \text{ GeV})$ is 6%.

The result for the ratio of the branching fractions restricted to decays with $m_{J/\psi\mu} > 5.3$ GeV is

$$\mathcal{R}(m_{J/wu} > 5.3 \text{ GeV}) = 0.271 \pm 0.016 \pm 0.016,$$
 (8)

where the first uncertainty is statistical and the second is systematic. This ratio is extrapolated to the full phase space using the predictions of the phenomenological models [22,23,25,43,48,49]. No correlation pattern is observed between the predicted values of \mathcal{R} and of the extrapolation factor; thus equal weight is given to all models. The model of Kiselev *et al.* [22] predicts the fraction of the $B_c^+ \rightarrow J/\psi\mu^+\nu_\mu$ rate with $m_{J/\psi\mu}$ above 5.3 GeV to be 0.173,

TABLE II. Summary of systematic uncertainties. The total systematic errors are obtained by adding in quadrature the individual contributions.

Contribution	Relative error
$m_{J/w\pi}$ signal shape	2.3%
$m_{J/\psi\pi}$ background shape	0.2%
$B_c^+ \rightarrow J/\psi K^+$ component	0.1%
$m_{J/w\mu}$ signal shape	0.7%
$m_{J/\psi\mu}$ background shape	1.8%
B_c^+ feed down	0.6%
Lower $m_{I/wu}$ fit range limit	1.6%
Upper $m_{I/\mu\mu}$ fit range limit	1.5%
$B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu$ model dependence of efficiency	1.3%
Pion PID	0.8%
Muon PID	1.9%
Lifetime	0.2%
Multiple candidates	0.4%
$\Delta_{\text{sig/bkg}}(-2\ln\mathcal{L})$ requirement for $B_c^+ \to J/\psi\pi^+$	2.0%
$\Delta_{\rm sig/bkg}(-2\ln \mathcal{L})$ requirement for $B_c^+ \to J/\psi \mu^+ \nu_\mu$	0.5%
Trigger simulation	3.4%
Total within selected $m_{I/wu}$ range	6.0%
$m_{J/w\mu}$ extrapolation	7.9%
Total	9.9%

which is close to the average over all models. The largest deviation from this prediction is 7.9%, which is taken as an estimate of the extrapolation systematic error. This increases the systematic uncertainty on \mathcal{R} , when extrapolated to the full mass range, to 9.9% yielding



FIG. 4 (color online). The measured value of \mathcal{R} (horizontal solid line) and its $\pm 1\sigma$ uncertainty band (dashed lines) compared to the predictions (diamonds). A nonrelativistic reduction of the Bethe–Salpeter equation is used in the predictions of Chang *et al.* [18], El-Hady *et al.* [20] and Colangelo *et al.* [21], while the latter also utilizes heavy quark symmetry. A light-front constituent quark model is used by Anisimov *et al.* [19] and Ke *et al.* [25]. QCD sum rules are used by Kiselev *et al.* [22], a relativistic quasipotential Schrödinger model is used by Ebert *et al.* [23], and a relativistic constituent quark model is used by Ivanov *et al.* [24].

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$$\mathcal{R} = 0.0469 \pm 0.0028 \pm 0.0046. \tag{9}$$

A comparison between the measured and the predicted values of \mathcal{R} is shown in Fig. 4. The measured value is slightly below the lowest predicted value. The predictions by the relativistic quasipotential Schrödinger model of Ebert *et al.* [23] and the model of El-Hady *et al.*, based on a nonrelativistic reduction of the Bethe–Salpeter equation [20], are in good agreement with the experimental value. The model of Ke *et al.* [25], based on the modified harmonic oscillator wave function in light-front quark model, is also consistent with the data. The other models [18,19,21,22,24] significantly overestimate \mathcal{R} .

VIII. SUMMARY

The ratio of hadronic and semileptonic decay branching fractions of the B_c^+ meson is measured for the first time. Within the observed mass range, $m_{J/\psi\mu} > 5.3$ GeV, the measured value of $\mathcal{B}(B_c^+ \to J/\psi\pi^+)/\mathcal{B}(B_c^+ \to J/\psi\mu^+\nu_{\mu})$ is found to be $0.271 \pm 0.016(\text{stat}) \pm 0.016(\text{syst})$. Extrapolating to the full mass range, we obtain a value of $\mathcal{B}(B_c^+ \to J/\psi\pi^+)/\mathcal{B}(B_c^+ \to J/\psi\mu^+\nu_{\mu}) = 0.0469 \pm 0.0028(\text{stat}) \pm 0.0046(\text{syst})$, which is in good agreement with the theoretical predictions by Ebert *et al.* [23] and El-Hady *et al.* [20], and consistent with the prediction by Ke *et al.* [25]. All other currently available models [18,19,21,22,24] overestimate this ratio.

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Kandybei,⁴³ W. Kanso,⁶ M. Karacson,³⁸ T. M. Karbach,³⁸ S. Karodia,⁵¹ M. Kelsey,⁵⁹ I. R. Kenyon,⁴⁵ T. Ketel,⁴² B. Khanji,²⁰ C. Khurewathanakul,³⁹ S. Klaver,⁵⁴ K. Klimaszewski,²⁸ O. Kochebina,⁷ M. Kolpin,¹¹ I. Komarov,³⁹ R. F. Koopman,⁴² P. Koppenburg,^{41,38} M. Korolev,³² A. Kozlinskiy,⁴¹ L. Kravchuk,³³ K. Kreplin,¹¹ M. Kreps,⁴⁸ G. Krocker,¹¹ P. Krokovny,³⁴ F. Kruse,⁹ W. Kucewicz,^{26,1} M. Kucharczyk,^{20,26,38,f} V. Kudryavtsev,³⁴ K. Kurek,²⁸ T. Kvaratskheliya,³¹ V. N. La Thi,³⁹ D. Lacarrere,³⁸ G. Lafferty,⁵⁴ A. Lai,¹⁵ D. Lambert,⁵⁰ R. W. Lambert,⁴² G. Lanfranchi,¹⁸ C. Langenbruch,⁴⁸ B. Langhans,³⁸ T. Latham,⁴⁸ C. Lazzeroni,⁴⁵ R. Le Gac,⁶ J. van Leerdam,⁴¹ J.-P. Lees,⁴ R. Lefèvre,⁵ A. Leflat,³² J. Lefrançois,⁷ S. Leo,²³ O. Leroy,⁶ T. Lesiak,²⁶ B. Leverington,¹¹ Y. Li,³ T. Likhomanenko,⁶³ M. Liles,⁵² R. Lindner,³⁸ C. Linn,³⁸ F. Lionetto,⁴⁰ B. Liu,¹⁵ G. Liu,³⁸ S. Lohn,³⁸ I. Longstaff,⁵¹ J. H. Lopes,² N. Lopez-March,³⁹ P. Lowdon,⁴⁰ H. Lu,³ D. Lucchesi,^{22,e} H. Luo,⁵⁰ A. Lupato,²² E. Luppi,^{16,b} O. Lupton,⁵⁵ F. Machefert,⁷ I. V. Machikhiliyan,³¹ F. Maciuc,²⁹ O. Maev,³⁰ S. Malde,⁵⁵ G. Manca,^{15,m} G. Mancinelli,⁶ J. Maratas,⁵ J. F. Marchand,⁴ U. Marconi,¹⁴ C. Marin Benito,³⁶ P. Marino,^{23,n} R. Märki,³⁹ J. Marks,¹¹ G. Martellotti,²⁵ A. Martens,⁸ A. Martín Sánchez,⁷ M. Martinelli,⁴¹ D. Martinez Santos,⁴² F. Martinez Vidal,⁶⁴ D. Martins Tostes,² A. Massafferri,¹ R. Matev,³⁸ Z. Mathe,³⁸ C. Matteuzzi,²⁰ A. Mazurov,^{16,b} M. McCann,⁵³ J. McCarthy,⁴⁵ A. McNab,⁵⁴ R. McNulty,¹² B. McSkelly,⁵² B. Meadows,⁵⁷ F. Meier,⁹ M. Meissner,¹¹ M. Merk,⁴¹ D. A. Milanes,⁸ M.-N. Minard,⁴ N. Moggi,¹⁴ J. Molina Rodriguez,⁶⁰ S. Monteil,⁵ M. Morandin,²² P. Morawski,²⁷ A. Mordà,⁶ M. J. Morello,^{23,n} J. Moron,²⁷ A.-B. Morris,⁵⁰ R. Mountain,⁵⁹ F. Muheim,⁵⁰ K. Müller,⁴⁰ M. Mussini,¹⁴ B. Muster,³⁹ P. Naik,⁴⁶ T. Nakada,³⁹ R. Nandakumar,⁴⁹ I. Nasteva,² M. Needham,⁵⁰ N. Neri,²¹ S. Neubert,³⁸ N. Neufeld,³⁸ M. Neuner,¹¹ A. D. Nguyen,³⁹ T. D. Nguyen,³⁹ C. Nguyen-Mau,^{39,0} M. Nicol,⁷ V. Niess,⁵ R. Niet,⁹ N. Nikitin,³² T. Nikodem,¹¹ A. Novoselov,³⁵ D. P. O'Hanlon,⁴⁸ A. Oblakowska-Mucha,²⁷ V. Obraztsov,³⁵ S. Oggero,⁴¹ S. Ogilvy,⁵¹ O. Okhrimenko,⁴⁴ R. Oldeman,^{15,m} G. Onderwater,⁶⁵ M. Orlandea,²⁹ J. M. Otalora Goicochea,² P. Owen,⁵³ A. Oyanguren,⁶⁴ B. K. Pal,⁵⁹ A. Palano,^{13,p} F. Palombo,^{21,q} M. Palutan,¹⁸ J. Panman,³⁸ A. Papanestis,^{49,38} M. Pappagallo,⁵¹ C. Parkes,⁵⁴ C. J. Parkinson,^{9,45} G. Passaleva,¹⁷ G. D. Patel,⁵² M. Patel,⁵³ C. Patrignani,^{19,j} A. Pazos Alvarez,³⁷ A. Pearce,⁵⁴ A. Pellegrino,⁴¹ M. Pepe Altarelli,³⁸ S. Perazzini,^{14,h} E. Perez Trigo,³⁷ P. Perret,⁵ M. Perrin-Terrin,⁶ L. Pescatore,⁴⁵ E. Pesen,⁶⁶ K. Petridis,⁵³ A. Petrolini,^{19,j} E. Picatoste Olloqui,³⁶ B. Pietrzyk,⁴ T. Pilař,⁴⁸ D. Pinci,²⁵ A. Pistone,¹⁹ S. Playfer,⁵⁰ M. Plo Casasus,³⁷ F. Polci,⁸ A. Poluektov,^{48,34} E. Polycarpo,² A. Popov,³⁵ D. Popov,¹⁰ B. Popovici,²⁹ C. Potterat,² E. Price,⁴⁶ J. Prisciandaro,³⁹ A. Pritchard,⁵² C. Prouve,⁴⁶ V. Pugatch,⁴⁴ A. Puig Navarro,³⁹ G. Punzi,^{23,r} W. Qian,⁴ B. Rachwal,²⁶ J. H. Rademacker,⁴⁶ B. Rakotomiaramanana,³⁹ M. Rama,¹⁸ M. S. Rangel,² I. Raniuk,⁴³ N. Rauschmayr,³⁸ G. Raven,⁴² S. Reichert,⁵⁴ M. M. Reid,⁴⁸ A. C. dos Reis,¹ S. Ricciardi,⁴⁹ S. Richards,⁴⁶ M. Rihl,³⁸ K. Rinnert,⁵² V. Rives Molina,³⁶ D. A. Roa Romero,⁵ P. Robbe,⁷ A. B. Rodrigues,¹ E. Rodrigues,⁵⁴ P. Rodriguez Perez,⁵⁴ S. Roiser,³⁸ V. Romanovsky,³⁵ A. Romero Vidal,³⁷ M. Rotondo,²² J. Rouvinet,³⁹ T. Ruf,³⁸ F. Ruffini,²³ H. Ruiz,³⁶ P. Ruiz Valls,⁶⁴ J. J. Saborido Silva,³⁷ N. Sagidova,³⁰ P. Sail,⁵¹ B. Saitta,^{15,m} V. Salustino Guimaraes,² C. Sanchez Mayordomo,⁶⁴ B. Sanmartin Sedes,³⁷ R. Santacesaria,²⁵ C. Santamarina Rios,³⁷ E. Santovetti,^{24,i} A. Sarti,^{18,s} C. Satriano,^{25,c} A. Satta,²⁴ D. M. Saunders,⁴⁶ M. Savrie,^{16,b} D. Savrina,^{31,32} M. Schiller,⁴² H. Schindler,³⁸ M. Schlupp,⁹ M. Schmelling,¹⁰ B. Schmidt,³⁸ O. Schneider,³⁹ A. Schopper,³⁸ M.-H. Schune,⁷ R. Schwemmer,³⁸ B. Sciascia,¹⁸ A. Sciubba,²⁵ M. Seco,³⁷ A. Semennikov,³¹ I. Sepp,⁵³ N. Serra,⁴⁰ J. Serrano,⁶ L. Sestini,²² P. Seyfert,¹¹ M. Shapkin,³⁵ I. Shapoval,^{16,43,b} Y. Shcheglov,³⁰ T. Shears,⁵² L. Shekhtman,³⁴ V. Shevchenko,⁶³ A. Shires,⁹ R. Silva Coutinho,⁴⁸ G. Simi,²² M. Sirendi,⁴⁷ N. Skidmore,⁴⁶ T. Skwarnicki,⁵⁹ N. A. Smith,⁵² E. Smith,^{55,49} E. Smith,⁵³ J. Smith,⁴⁷ M. Smith,⁵⁴ H. Snoek,⁴¹ M. D. Sokoloff,⁵⁷ F. J. P. Soler,⁵¹ F. Soomro,³⁹ D. Souza,⁴⁶ B. Souza De Paula,² B. Spaan,⁹ A. Sparkes,⁵⁰ P. Spradlin,⁵¹ S. Sridharan,³⁸ F. Stagni,³⁸ M. Stahl,¹¹ S. Stahl,¹¹ O. Steinkamp,⁴⁰ O. Stenyakin,³⁵ S. Stevenson,⁵⁵ S. Stoica,²⁹ S. Stone,⁵⁹ B. Storaci,⁴⁰ S. Stracka,^{23,38} M. Straticiuc,²⁹ U. Straumann,⁴⁰ R. Stroili,²² V. K. Subbiah,³⁸ L. Sun,⁵⁷ W. Sutcliffe,⁵³ K. Swientek,²⁷ S. Swientek,⁹ V. Syropoulos,⁴² M. Szczekowski,²⁸ P. Szczypka,^{39,38} D. Szilard,² T. Szumlak,²⁷ S. T'Jampens,⁴ M. Teklishyn,⁷ G. Tellarini,^{16,b} F. Teubert,³⁸

C. Thomas,⁵⁵ E. Thomas,³⁸ J. van Tilburg,⁴¹ V. Tisserand,⁴ M. Tobin,³⁹ S. Tolk,⁴² L. Tomassetti,^{16,b} D. Tonelli,³⁸ S. Topp-Joergensen,⁵⁵ N. Torr,⁵⁵ E. Tournefier,⁴ S. Tourneur,³⁹ M. T. Tran,³⁹ M. Tresch,⁴⁰ A. Tsaregorodtsev,⁶ P. Tsopelas,⁴¹ N. Tuning,⁴¹ M. Ubeda Garcia,³⁸ A. Ukleja,²⁸ A. Ustyuzhanin,⁶³ U. Uwer,¹¹ V. Vagnoni,¹⁴ G. Valenti,¹⁴ A. Vallier,⁷ R. Vazquez Gomez,¹⁸ P. Vazquez Regueiro,³⁷ C. Vázquez Sierra,³⁷ S. Vecchi,¹⁶ J. J. Velthuis,⁴⁶ M. Veltri,^{17,1} G. Veneziano,³⁹ M. Vesterinen,¹¹ B. Viaud,⁷ D. Vieira,² M. Vieites Diaz,³⁷ X. Vilasis-Cardona,^{36,g} A. Vollhardt,⁴⁰ D. Volyanskyy,¹⁰ D. Voong,⁴⁶ A. Vorobyev,³⁰ V. Vorobyev,³⁴ C. Voß,⁶² H. Voss,¹⁰ J. A. de Vries,⁴¹ R. Waldi,⁶² C. Wallace,⁴⁸ R. Wallace,¹² J. Walsh,²³ S. Wandernoth,¹¹ J. Wang,⁵⁹ D. R. Ward,⁴⁷ N. K. Watson,⁴⁵ D. Websdale,⁵³ M. Whitehead,⁴⁸ J. Wicht,³⁸ D. Wiedner,¹¹ G. Wilkinson,⁵⁵ M. P. Williams,⁴⁵ M. Williams,⁵⁶ F. F. Wilson,⁴⁹ J. Wimberley,⁵⁸ J. Wishahi,⁹ W. Wislicki,²⁸ M. Witek,²⁶ G. Wormser,⁷ S. A. Wotton,⁴⁷ S. Wright,⁴⁷ S. Wu,³ K. Wyllie,³⁸ Y. Xie,⁶¹ Z. Xing,⁵⁹ Z. Xu,³⁹ Z. Yang,³ X. Yuan,³ O. Yushchenko,³⁵ M. Zangoli,¹⁴ M. Zavertyaev,^{10,u} L. Zhang,⁵⁹ W. C. Zhang,¹² Y. Zhang,³ A. Zhelezov,¹¹ A. Zhokhov,³¹ L. Zhong,³ and A. Zvyagin³⁸

(LHCb Collaboration)

¹Centro Brasileiro de Pesquisas Físicas (CBPF), Rio de Janeiro, Brazil

²Universidade Federal do Rio de Janeiro (UFRJ), Rio de Janeiro, Brazil

³Center for High Energy Physics, Tsinghua University, Beijing, China

⁴LAPP, Université de Savoie, CNRS/IN2P3, Annecy-Le-Vieux, France

⁵Clermont Université, Université Blaise Pascal, CNRS/IN2P3, LPC, Clermont-Ferrand, France

⁶CPPM, Aix-Marseille Université, CNRS/IN2P3, Marseille, France

⁷LAL, Université Paris-Sud, CNRS/IN2P3, Orsay, France

⁸LPNHE, Université Pierre et Marie Curie, Université Paris Diderot, CNRS/IN2P3, Paris, France

⁹Fakultät Physik, Technische Universität Dortmund, Dortmund, Germany

¹⁰Max-Planck-Institut für Kernphysik (MPIK), Heidelberg, Germany

¹¹Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany

¹²School of Physics, University College Dublin, Dublin, Ireland

¹³Sezione INFN di Bari, Bari, Italy

¹⁴Sezione INFN di Bologna, Bologna, Italy

¹⁵Sezione INFN di Cagliari, Cagliari, Italy

¹⁶Sezione INFN di Ferrara, Ferrara, Italy

¹⁷Sezione INFN di Firenze, Firenze, Italy

¹⁸Laboratori Nazionali dell'INFN di Frascati, Frascati, Italy

¹⁹Sezione INFN di Genova, Genova, Italy

²⁰Sezione INFN di Milano Bicocca, Milano, Italy

²¹Sezione INFN di Milano, Milano, Italy

²²Sezione INFN di Padova, Padova, Italy

²³Sezione INFN di Pisa, Pisa, Italy

²⁴Sezione INFN di Roma Tor Vergata, Roma, Italy

²⁵Sezione INFN di Roma La Sapienza, Roma, Italy

²⁶Henrvk Niewodniczanski Institute of Nuclear Physics Polish Academy of Sciences,

Kraków, Poland

²⁷AGH–University of Science and Technology, Faculty of Physics and Applied Computer Science,

Kraków, Poland

²⁸National Center for Nuclear Research (NCBJ), Warsaw, Poland

²⁹Horia Hulubei National Institute of Physics and Nuclear Engineering, Bucharest-Magurele, Romania

³⁰Petersburg Nuclear Physics Institute (PNPI), Gatchina, Russia

³¹Institute of Theoretical and Experimental Physics (ITEP), Moscow, Russia

³²Institute of Nuclear Physics, Moscow State University (SINP MSU), Moscow, Russia

³³Institute for Nuclear Research of the Russian Academy of Sciences (INR RAN), Moscow, Russia

³⁴Budker Institute of Nuclear Physics (SB RAS) and Novosibirsk State University, Novosibirsk, Russia ³⁵Institute for High Energy Physics (IHEP), Protvino, Russia

³⁶Universitat de Barcelona, Barcelona, Spain

³⁷Universidad de Santiago de Compostela, Santiago de Compostela, Spain

³⁸European Organization for Nuclear Research (CERN), Geneva, Switzerland

³⁹Ecole Polytechnique Fédérale de Lausanne (EPFL), Lausanne, Switzerland

⁴⁰Physik-Institut, Universität Zürich, Zürich, Switzerland

⁴¹Nikhef National Institute for Subatomic Physics, Amsterdam, The Netherlands

⁴²Nikhef National Institute for Subatomic Physics and VU University Amsterdam, Amsterdam,

The Netherlands

⁴³NSC Kharkiv Institute of Physics and Technology (NSC KIPT), Kharkiv, Ukraine

⁴⁴Institute for Nuclear Research of the National Academy of Sciences (KINR), Kyiv, Ukraine

⁴⁵University of Birmingham, Birmingham, United Kingdom

⁴⁶H.H. Wills Physics Laboratory, University of Bristol, Bristol, United Kingdom

⁴⁷Cavendish Laboratory, University of Cambridge, Cambridge, United Kingdom

⁴⁸Department of Physics, University of Warwick, Coventry, United Kingdom

⁴⁹STFC Rutherford Appleton Laboratory, Didcot, United Kingdom

⁵⁰School of Physics and Astronomy, University of Edinburgh, Edinburgh, United Kingdom

¹School of Physics and Astronomy, University of Glasgow, Glasgow, United Kingdom

²Oliver Lodge Laboratory, University of Liverpool, Liverpool, United Kingdom

⁵³Imperial College London, London, United Kingdom

⁵⁴School of Physics and Astronomy, University of Manchester, Manchester, United Kingdom

⁵⁵Department of Physics, University of Oxford, Oxford, United Kingdom

⁵⁶Massachusetts Institute of Technology, Cambridge, Massachusetts, United States

⁵⁷University of Cincinnati, Cincinnati, Ohio, United States

⁵⁸University of Maryland, College Park, Maryland, United States

⁵⁹Syracuse University, Syracuse, New York, United States

⁶⁰Pontifícia Universidade Católica do Rio de Janeiro (PUC-Rio), Rio de Janeiro, Brazil (associated with

Universidade Federal do Rio de Janeiro (UFRJ), Rio de Janeiro, Brazil)

⁶¹Institute of Particle Physics, Central China Normal University, Wuhan, Hubei, China (associated with

Center for High Energy Physics, Tsinghua University, Beijing, China)

⁶²Institut für Physik, Universität Rostock, Rostock, Germany (associated with Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany)

⁶³National Research Centre Kurchatov Institute, Moscow, Russia (associated with Institute of Theoretical and Experimental Physics (ITEP), Moscow, Russia)

⁶⁴Instituto de Fisica Corpuscular (IFIC), Universitat de Valencia-CSIC, Valencia, Spain (associated with Universitat de Barcelona, Barcelona, Spain)

⁶⁵KVI–University of Groningen, Groningen, The Netherlands (associated with Nikhef National Institute for

Subatomic Physics, Amsterdam, The Netherlands)

⁶⁶Celal Bayar University, Manisa, Turkey (associated with European Organization for Nuclear Research (CERN), Geneva, Switzerland)

^aAlso at Università di Firenze, Firenze, Italy.

^bAlso at Università di Ferrara, Ferrara, Italy.

^cAlso at Università della Basilicata, Potenza, Italy.

^dAlso at Università di Modena e Reggio Emilia, Modena, Italy.

^eAlso at Università di Padova, Padova, Italy.

^fAlso at Università di Milano Bicocca, Milano, Italy.

^gAlso at LIFAELS, La Salle, Universitat Ramon Llull, Barcelona, Spain.

^hAlso at Università di Bologna, Bologna, Italy.

¹Also at Università di Roma Tor Vergata, Roma, Italy.

^JAlso at Università di Genova, Genova, Italy.

^kAlso at Universidade Federal do Triângulo Mineiro (UFTM), Uberaba-MG, Brazil.

¹Also at AGH–University of Science and Technology, Faculty of Computer Science, Electronics and Telecommunications, Kraków, Poland.

^mAlso at Università di Cagliari, Cagliari, Italy.

ⁿAlso at Scuola Normale Superiore, Pisa, Italy.

^oAlso at Hanoi University of Science, Hanoi, Viet Nam.

^pAlso at Università di Bari, Bari, Italy.

^qAlso at Università degli Studi di Milano, Milano, Italy.

^rAlso at Università di Pisa, Pisa, Italy.

^sAlso at Università di Roma La Sapienza, Roma, Italy.

^tAlso at Università di Urbino, Urbino, Italy.

^uAlso at P.N. Lebedev Physical Institute, Russian Academy of Science (LPI RAS), Moscow, Russia.