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The Aspen–Amsterdam void finder comparison project

Jörg M. Colberg,^{1,2*} Frazer Pearce,³ Caroline Foster,^{4,5} Erwin Platen,⁶
 Riccardo Brunino,³ Mark Neyrinck,⁷ Spyros Basilakos,⁸ Anthony Fairall,⁹
 Hume Feldman,¹⁰ Stefan Gottlöber,¹¹ Oliver Hahn,¹² Fiona Hoyle,¹³ Volker Müller,¹¹
 Lorne Nelson,⁴ Manolis Plionis,^{14,15} Cristiano Porciani,¹² Sergei Shandarin,¹⁰
 Michael S. Vogeley¹⁶ and Rien van de Weygaert⁶

¹*Carnegie–Mellon University, 5000 Forbes Ave, Pittsburgh, PA 15213, USA*

²*Astronomy Department, University of Massachusetts, Amherst, MA 01003, USA*

³*School of Physics & Astronomy, University of Nottingham, Nottingham NG7 2LE*

⁴*Department of Physics, Bishop's University, 2600 College Street, Sherbrooke, QC J1M 0C8, Canada*

⁵*Centre for Astrophysics & Supercomputing, Swinburne University of Technology, Hawthorn, VIC 3122, Australia*

⁶*Kapteyn Institute, University of Groningen, PO Box 800, 9700 AV Groningen, the Netherlands*

⁷*Institute for Astronomy, University of Hawaii, Honolulu, HI 96822, USA*

⁸*Research Centre for Astronomy & Applied Mathematics, Academy of Athens, Soranou Efessiou 4, 11-527 Athens, Greece*

⁹*Department of Astronomy, University of Cape Town, Private Bag X3, Rondebosch 7700, South Africa*

¹⁰*Department of Physics and Astronomy, University of Kansas, Lawrence, KS 66045, USA*

¹¹*Astrophysikalisches Institut Potsdam, An der Sternwarte 16, 14482 Potsdam, Germany*

¹²*ETH Zürich, 8093 Zürich, Switzerland*

¹³*Department of Physics and Astronomy, Widener University, One University Place, Chester, PA 19013, USA*

¹⁴*Institute of Astronomy & Astrophysics, National Observatory of Athens, I. Metaxa & B. Pavlou, P. Penteli 152 36, Athens, Greece*

¹⁵*Instituto Nacional de Astrofísica, Óptica y Electrónica (INAOE) Apartado Postal 51 y 216, 72000 Puebla, Pue., Mexico*

¹⁶*Department of Physics, Drexel University, 3141 Chestnut Street, Philadelphia, PA 19104, USA*

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ABSTRACT

Despite a history that dates back at least a quarter of a century, studies of voids in the large-scale structure of the Universe are bedevilled by a major problem: there exist a large number of quite different void-finding algorithms, a fact that has so far got in the way of groups comparing their results without worrying about whether such a comparison in fact makes sense. Because of the recent increased interest in voids, both in very large galaxy surveys and in detailed simulations of cosmic structure formation, this situation is very unfortunate. We here present the first systematic comparison study of 13 different void finders constructed using particles, haloes, and semi-analytical model galaxies extracted from a subvolume of the Millennium simulation. This study includes many groups that have studied voids over the past decade. We show their results and discuss their differences and agreements. As it turns out, the basic results of the various methods agree very well with each other in that they all locate a major void near the centre of our volume. Voids have very underdense centres, reaching below 10 per cent of the mean cosmic density. In addition, those void finders that allow for void galaxies show that those galaxies follow similar trends. For example, the overdensity of void galaxies brighter than $m_B = -20$ is found to be smaller than about -0.8 by all our void finding algorithms.

Key words: methods: N -body simulations – cosmology: theory – dark matter – large-scale structure of Universe.

1 INTRODUCTION

Large regions of space that are only sparsely populated with galaxies, so-called voids, have been known as a feature of galaxy surveys

since the first of those surveys was compiled, the most well-known cases being the famous void in Boötes, discovered by Kirshner et al. (1981), and the first void sample of de Lapparent, Geller & Huchra (1986). However, due to the fact that voids occupy a large fraction of space, only recently have galaxy surveys become large enough to allow systematic studies of voids and the galaxies inside them. For recent studies of voids and void galaxies in the two-degree field

*E-mail: astro@jmcolberg.com

Galaxy Survey (2dFGRS, Colless et al. 2001) and the Sloan Digital Sky Survey (SDSS, York et al. 2000) see Hoyle & Vogeley (2004), Ceccarelli et al. (2006), Patiri et al. (2006a), Tikhonov (2007), von Benda-Beckmann & Müller (2008) and Rojas et al. (2004), Goldberg et al. (2005), Hoyle et al. (2005), Rojas et al. (2005), Patiri et al. (2006b), respectively. Also see Croton et al. (2004) for a recent, detailed study of the void probability function in the 2dF.

On the theoretical side, progress has been mirrored by vast improvements in models and simulations, with systematic studies of large numbers of voids now being common (see e.g. the early works by Regos & Geller 1991; Dubinski et al. 1993 or Van de Weygaert & Van Kampen 1993, and the more recent Arbabi-Bidgoli & Müller 2002; Mathis & White 2002; Benson et al. 2003; Gottlöber et al. 2003; Goldberg & Vogeley 2004; Sheth & Van de Weygaert 2004; Bolejko, Krasinski & Hellaby 2005; Colberg et al. 2005; Padilla, Ceccarelli & Lambas 2005; Furlanetto & Piran 2006; Hoeft et al. 2006; Lee & Park 2006; Patiri, Betancourt-Rijo & Prada 2006c; Shandarin et al. 2006; Brunino et al. 2007; Park & Lee 2007). Theory shows that voids are a real feature of large-scale structure, since initially underdense regions grow in size as overdense regions collapse under their own gravity (see e.g. Sheth & Van de Weygaert 2004). However, while the general picture appears to be well supported by the standard Λ cold dark matter (Λ CDM) cosmology, Peebles (2001) pointed out some potentially critical issues. Does the Λ CDM cosmology produce too many objects in voids that have no observational counterparts? A detailed discussion of other reasons why studies of voids are an interesting topic is beyond the scope of this paper. Briefly, their role as a prominent feature of the Megaparsec Universe means that a proper and full understanding of the formation and dynamics of the Cosmic Web is not possible without probing the structure and evolution of voids. A second rationale is that of inferring global cosmological information from the structure and geometry of and outflow from voids. The third aspect is that of providing a unique and still largely pristine environment for testing theories of the formation and evolution of galaxies.

Despite the growing interest in voids and the large number of recent studies, a fairly significant problem remains: as it turns out, almost every study uses its own void finder. There is general agreement that there are voids in the data or in the simulations, but many different ways were proposed to find them. Thus, the resulting voids are either spherical (with or without overlap), shaped like lumpy potatoes,¹ or they percolate all across the studied volume. What is more, some groups do not allow for the existence of void galaxies, whereas many others do. An added complication is that many theoretical studies use the DM distribution to find voids, whereas observational studies have to rely on galaxies. As a consequence, it is not clear how the results from studies done by different groups can be compared, especially if observational and theoretical results are brought together. What most studies so far can agree on is that (i) voids are very underdense in their centres (approaching around 5 per cent of the mean density) and that (ii) voids often have very steep edges. In other words, the number of both observed and simulated galaxies increases very rapidly when reaching the edge of a void, and the corresponding result has been found for the density of DM in studies that used DM-only simulations.

Given the disagreements in the different methods, which are in part due to the different nature of the data sets used, the aim of this work is very modest. We apply 13 different void finders, all of which have been used over the past decade to study voids, to the

same data set in order to compare the results. As our data set we use particles, haloes, and semi-analytical model galaxies (Croton et al. 2005) from a subvolume of the Millennium simulation (Springel et al. 2005) specifically selected to be underdense and therefore void-rich. That way, while the methods are as different as finding connected cells on a density grid and identifying empty regions in the model galaxy distribution by eye, a meaningful comparison is still possible, since each void finder treats a subset of the same data set.

The aim of this paper is *not* to argue which void finder provides the best way to identify voids. We do hope, however, that this paper will allow the reader to understand the differences between the different void finders so that it will be easier to compare different studies of voids in the literature. We also hope that this paper will trigger more detailed follow-up studies to work towards a more unified view of this topic and to study properties of voids not covered here, such as for example their shapes and orientations, in detail.

This paper is organized as follows. In Section 2, we detail the simulation from which the test region was extracted and describe the procedure each group was asked to undertake. In Section 3, we briefly describe each void finding algorithm, before we undertake a comparison of the voids found in Section 4. Section 5 contains a summary and conclusions.

2 THE SIMULATION AND EXTRACTION PROCEDURE

For this work, we use the Millennium simulation (Springel et al. 2005) and a matched $z = 0$ galaxy catalogue, created using a semi-analytical galaxy formation model (Croton et al. 2005). The simulation of the concordance Λ CDM cosmology contains 2160^3 particles in a (periodic) box of size $500 h^{-1}$ Mpc in each dimension. The cosmological parameters are total matter density $\Omega_m = 0.25$, dark energy/cosmological constant $\Omega_\Lambda = 0.75$, Hubble constant $h = 0.73$, and the normalization of the power spectrum $\sigma_8 = 0.9$. With these parameters, each DM particle has a mass of $8.6 \times 10^8 h^{-1} M_\odot$.

In the Millennium simulation volume, we located a $60 h^{-1}$ Mpc region centred on a large void and extracted the coordinates of the 12 528 667 DM particles contained within it. This subvolume thus has a mean density which is lower than the cosmic mean, corresponding to an overdensity $\delta = \rho/\bar{\rho} - 1 = -0.28$.

We also extracted a list of the 17 604 galaxies together with their *BVR*IK dust-corrected magnitudes (down to $B = -10$) that are present in the semianalytic catalogue of Croton et al. (2005) within this volume and the 4006 DM haloes present in the subfind catalogue (a clean spherical overdensity based catalogue) with masses greater than $10^{11} h^{-1} M_\odot$. Note that while the small volume prohibits statistical comparisons between void finders it allows for void-by-void comparisons.

Each group was asked to run their void finder with their preferred parameters on this data base and return a void list for the voids found, tagging each of the DM particles, galaxies, and haloes with the void identifier of the void they resided in. This allowed simple plotting and analysis of each void sample. For overlapping voids, the DM particle was to be assigned to the larger void. As the region is not periodic we only requested information about voids whose centres lay within the central $40 h^{-1}$ Mpc region (i.e. the outer $10 h^{-1}$ Mpc was to be neglected).

The top left-hand and top centre panels of Fig. 1 show slices of thickness $5 h^{-1}$ Mpc through this central region. The top left-hand panel only contains the distribution of the DM, whereas the top

¹ JMC admits that this picture, while being accurate, is not very pretty.

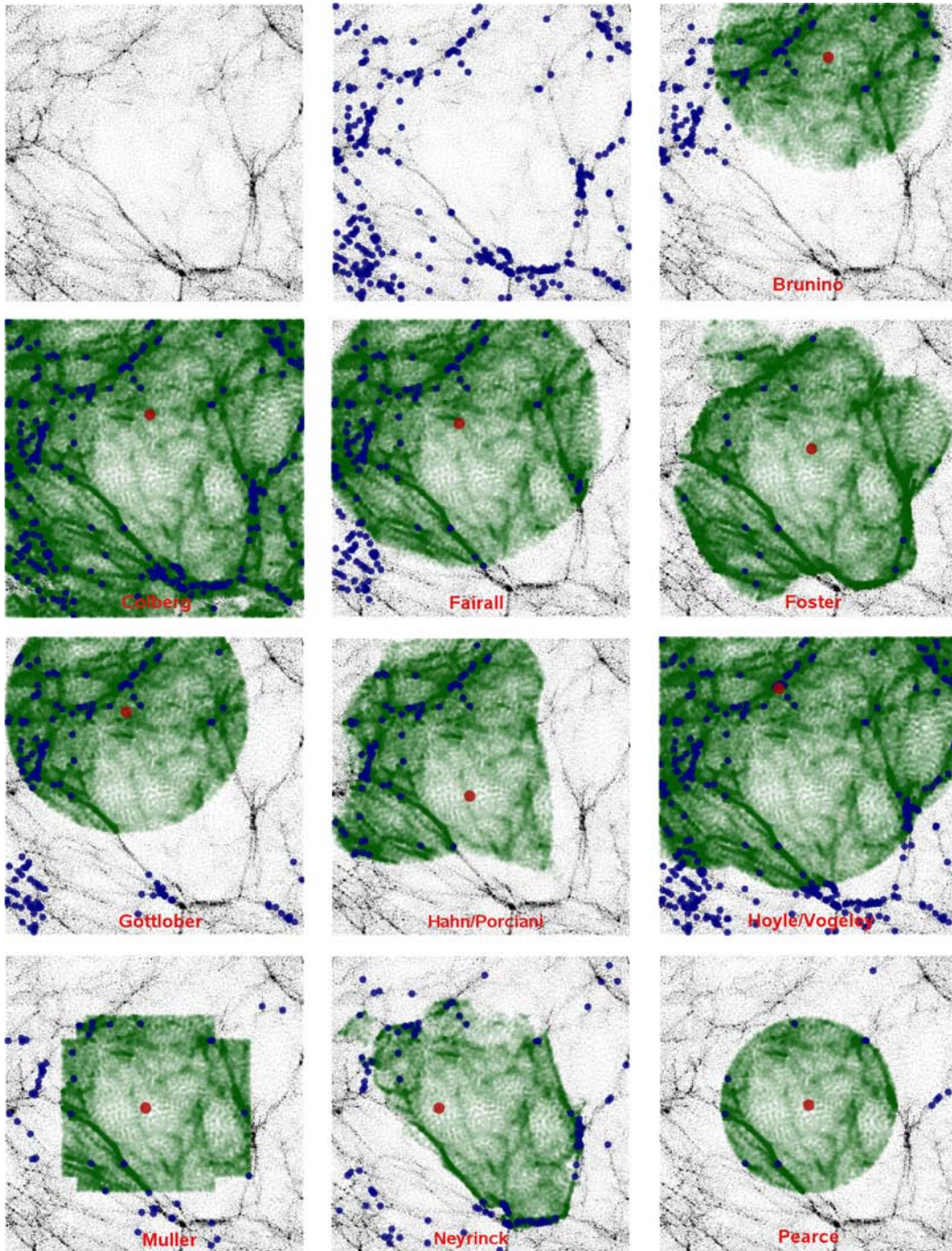


Figure 1. A slice of thickness $5 h^{-1}$ Mpc through the centre of the region extracted from the Millennium simulation. The image shows the DM distribution in the central $40 h^{-1}$ Mpc region. Void galaxies (within any void, not just the largest one) are superimposed on the DM distribution as the blue circles. The top left-hand and top centre panels show only the DM distribution and DM plus all galaxies in the slice, respectively. The other panels show the locations of the largest void (with DM particles inside the void marked green), its centre (red circle), and all void galaxies found by *Brunino* (top right-hand panel), *Colberg* (second row, left-hand column), *Fairall* (second row, centre), *Foster* (second row, right-hand column), *Gottlöber* (third row, left-hand column), *Hahn/Porciani* (third row, centre), *Hoyle/Vogeley* (third row, right-hand column), *Müller* (bottom, left-hand column), *Neyrinck* (bottom, centre), *Pearce* (bottom, right-hand column).

centre panel includes model galaxies on top of the DM distribution. The largest halo has a mass of only $1.75 \times 10^{12} h^{-1} M_{\odot}$, so filaments in these images correspond only to the less-massive filaments in standard slices through the DM distribution as seen in, for example, *Springel et al. (2005)*. Furthermore, the slice contains a total of

145 194 DM particles, equivalent to an overdensity of $\delta = -0.77$. It is important to keep these numbers in mind when studying the results obtained by the various void finders. Subsequent panels show the largest void identified by each group and those galaxies contained within all voids identified.

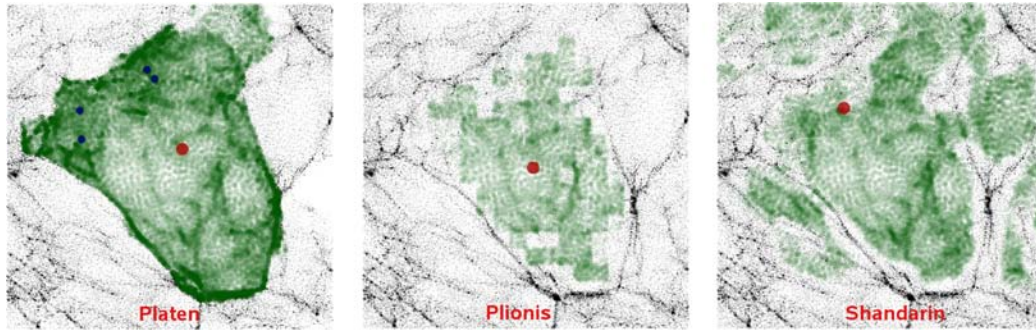


Figure 2. Same as and continued from Fig. 1. *Platen/Weygaert* (left-hand column), *Plionis/Basilakos* (centre), and *Shandarin/Feldman* (right-hand column). Note that both *Plionis/Basilakos* and *Shandarin/Feldman* find no void galaxies.

Table 1. An overview of the void finders used in this study.

Author	Base	Method
Brunino	Haloes	Spherical regions in halo distribution
Colberg	DM density field	Irregularly shaped underdense regions around local density minima
Fairall	Galaxies	Empty regions in galaxy distribution
Foster/Nelson	Galaxies	Empty regions in galaxy distribution
Gottlöber	Haloes/galaxies	Spherical empty regions in point set
Hahn/Porciani	DM density field	Tidal instability in smoothed density field
Hoyle/Vogeley	Galaxies	Empty regions in galaxy distribution
Müller	Halos/galaxies	Empty convex regions in point set
Neyrinck	DM density field	ZOBOV, depressions in unsmoothed DM field
Pearce	DM	Local density minima spheres
Platen/Weygaert	DM density field	Watershed DTFE
Plionis/Basilakos	DM density field	Connected underdense density grid cells
Shandarin/Feldman	DM density field	Connected underdense density grid cells

3 VOID FINDERS

This section gives a brief outline of the void finders used for this study, grouped into those which rely on the DM distribution and those which rely on the sparser galaxy or halo distributions (also see Table 1 for a general overview). For more details, the interested reader is referred to the individual studies by the different groups. Anyone simply interested in the results can skip to the next section. Please note that in this study, all group finders use real-space data.

3.1 Finders based on the DM distribution

3.1.1 Colberg: irregularly shaped underdense regions around local density minima

This method was introduced in Colberg et al. (2005), where it was used to study voids in the DM distribution of a suite of large N -body simulations. The starting point for Colberg et al.'s void finder is the adaptively smoothed distribution of the full DM distribution in a simulation. Proto-voids are constructed in a fashion quite similar to Hoyle & Vogeley's void finder, the difference being that Colberg's halo finder uses local minima in the density field as the centres of voids, and the mean density of the spherical proto-voids is required to be smaller or equal to an input threshold which, following a simple linear theory argument, is taken to be $\delta = -0.8$ (Blumenthal et al. 1992). Proto-voids are then merged according to a set of criteria, which allow for the construction of voids that can have any shape, as long as two large regions are not connected by a thin tunnel (which

would make the final void look like a dumbbell). The voids thus can have arbitrary shapes, but they typically look like lumpy potatoes.

For this study, a grid of size 480^3 and a minimum void radius of $r_{\min} = 2.0 h^{-1}$ Mpc were used. In the following, this void finder and its results are referred to as *Colberg*.

3.1.2 Pearce: spheres around local density minima

For every particle in the Millennium simulation, local densities were calculated by smoothing over the nearest 32 neighbours using a beta spline kernel (Monaghan & Lattanzio 1985). This list was then ranked in order of density (starting from the most underdense particle), and independent initial void centres were chosen such that they were more than $2 h^{-1}$ Mpc away from a previously selected centre (up to $\delta = -0.965$). The radial distribution of particles about these trial centres was then used to calculate the first up-crossing above $\delta = -0.9$. These radii were then sorted in order of size, and the resulting list was cleaned by removing voids whose centres lie within an already found void. The 3024 voids found by this procedure were used as the starting points for the more traditional halo based group finder used by Brunino et al. (2007). In the following, this void finder and its results are referred to as *Pearce*.

3.1.3 Hahn/Porciani: equation of motion in smoothed density field

A stability criterion for test-particle orbits is used to discriminate four environments with different dynamics (Hahn et al. 2006). The classification scheme is based on a series expansion of the equation of motion for a test particle in the smoothed matter distribution.

The series expansion yields a zero-order term, the acceleration, and a second order term, the tidal field T_{ij} (Hessian of the potential). The eigenvalues of T_{ij} characterize the triaxial deformation of an infinitesimal sphere due to the gravitational forces. Voids are classified as those regions of space where T_{ij} has no positive eigenvalues (tidally unstable).

The method has one free parameter, the size of the Gaussian filter used to smooth the potential. This parameter is set to $R_s = 2.09 h^{-1} \text{Mpc}$, which corresponds to a mass of $10^{13} h^{-1} M_\odot$ contained in the filter at mean density. This choice gives excellent agreement with a visual classification (see the discussion in Hahn et al. 2006). This mass scale corresponds to about $2M_*$ at $z = 0$.

The tidal field eigenvalues are evaluated on a grid. Contiguous regions classified as voids are then linked together. Voids can thus have arbitrary shapes, and their volumes are proportional to the number of cells linked together. In the following, this void finder and its results are referred to as *Hahn/Porciani*.

3.1.4 Neyrinck: ZOBOV

ZOBOV (ZONES Bordering On Voidness, Neyrinck 2008) is an inversion of a publicly available halo-finder, VOBOZ² (Neyrinck, Gnedin & Hamilton 2005). ZOBOV differs from VOBOZ in that ZOBOV looks for density minima instead of maxima, and does not consider gravitational binding. ZOBOV has some unique features: it is entirely parameter-free, working directly on the unsmoothed particle distribution; and, it returns all (even possibly spurious) depressions surrounding density minima, along with estimates of the probability that each arises from Poisson noise.

The first step is density estimation and neighbour identification for each DM particle, using what Schaap (2007) calls the Voronoi Tessellation Field Estimator. ZOBOV then partitions the particles into zones (depressions) around each minimum. Each particle jumps to its lowest density neighbour, repeating until it reaches a minimum. A minimum's *zone* is the set of particles which flow downward into it. Zones resemble voids, but because of unsmoothed discreteness noise, many zones are spurious, and others are only cores of voids detected by eye. Thus, ZOBOV must join some zones together to form voids. Voids around each zone grow by analogy with a flooding landscape (representing the density field): water flows into neighbouring zones, adding them to the original zone's void. The zone's void stops growing when the water spills into a zone deeper than the original zone, or the whole field is submerged. The probability that a void is real is judged by the ratio of the density at which this happens to the void's minimum density.

This density contrast r is converted to a probability through comparison with a Poisson point distribution; see Neyrinck et al. (2005) for details. The ZOBOV catalogue used for comparison with other void-finders includes only voids exceeding a 5σ probability threshold, which corresponds to a density contrast of 2.89. Also, subvoids exceeding this threshold have been removed from parent voids. In the following, this void finder and its results are referred to as *Neyrinck*.

3.1.5 Platen/Weygaert: watershed void finder

The Watershed Void Finder is an implementation of the Watershed Transform (WST) for image segmentation towards the analysis of

the Cosmic Web. The WST is a familiar concept in mathematical morphology and was first introduced by Beucher & Lantuejoul (1979, also see Beucher & Meyer 1993).

The WST delineates the boundaries of separate domains, that is, the *basins*, into which the yields of, for example, rainfall will collect. The analogy with the cosmological context is straightforward: *voids* are to be identified with the *basins*, while the *filaments* and *walls* of the Cosmic Web are the ridges separating the voids from each other.

The voids are computed by an algorithm that mimics the flooding process. First, the cosmological point distribution is transformed by the Delaunay Tessellation Field Estimator (DTFE) technique into a density field. DTFE (Schaap & van de Weygaert 2000; Schaap 2007) assures an optimal rendering of the hierarchical, anisotropic and void-like nature and aspects of the web-like cosmic matter distribution. The density field is adaptively smoothed by *nearest neighbour median filtering* (Platen, Van de Weygaert & Jones 2007). Minima are selected from the smoothed field and marked as the sources of flooding. While the 'watershed' level rises, a growing fraction of the 'landscape' will be flooded: the basins expand. Ultimately, basins will meet at the ridges, saddlepoints in the density field. These ridges define their boundaries, and are marked as edges separating the two basins. The procedure is continued until the density field is completely immersed, leaving a division of the landscape into individual segments separated by *edges*. The edges delineate the skeleton of the field and outline the *voids* in the density field.

The voids in the watershed procedure have no shape constraints. By definition the voids fill space completely. Nearly without exception galaxies and dark haloes are located on the ridges of the Cosmic Web, implying a minimal amount of galaxies to be located in the watershed void segments.

3.1.6 Plionis/Basilakos: connected underdense density grid cells

This void finder is applied on a regular 3D grid of the DM particle distribution or of a smoothed galaxy distribution, and it is based in identifying those grid cells (which we call 'void cells') whose density contrast lies below a specific threshold. Then all neighbouring (touching) 'void cells' are connected to form candidate voids (see also Plionis & Basilakos 2002). Therefore, by construction, voids do not overlap, and they can have an arbitrary shape, which is approximated by an ellipsoidal configuration (see Plionis & Basilakos 2002). Of course, increasing the threshold one tends to percolate through the available volume by connecting voids. The threshold below which the 'void cells' are identified is chosen so that a specific fraction of the probability density function (PDF) is used. For example, the voids presented here are based on the lowest 12.5 per cent density 'void cells', which corresponds to $\delta\rho/\rho \simeq -0.92$.

In order to identify significant voids from our candidate list, we compare with voids found in 1000 realizations of the DM particle distribution, using again the lowest 12.5 per cent density void cells of each 'random-realization' PDF. Now a probability curve as a function of void size can be built. Smaller voids appear with a large frequency in the random realizations and thus a candidate void is considered as significant only if its probability of appearing in a random distribution is <0.05 .

There are two free parameters in this void identification procedure: (i) the grid cell size and (ii) the threshold below which void cells are identified. The first is selected arbitrarily in this work such that it roughly encloses the volume of a typical cluster of galaxies, $(2 \text{Mpc})^3$, while the second is selected such that it maximizes the number of significant voids. In the following, this void finder and its results are referred to as *Plionis/Basilakos*.

² Available at <http://ifa.hawaii.edu/~neyrinck/VOBOZ>.

3.1.7 Shandarin/Feldman: connected underdense density grid cells

Voids are defined as the individual 3D regions of the low-density excursion set fully enclosed with the isodensity surfaces (for more details see Shandarin et al. 2006). Here, we first generate the density field on a uniform rectangular grid using the cloud-in-cell (CIC) technique. The grid parameter is chosen to be equal to the mean separation of particles in the whole simulation $d = (500/2160) h^{-1}$ Mpc. The CIC algorithm uses particles of the same size. The density field is then smoothed with a spherical Gaussian filter with $R_G = 1 h^{-1}$ Mpc, assuming non-periodic boundary conditions and empty space beyond the boundaries. In the analysis, we use only the central part of the cube, slicing 4.5 d from every face of the initial cube affected by smoothing. The final cube consists of 250^3 grid sites with the volume of about 91 per cent of the initial cube. Non-percolating voids reach maximum sizes at the percolation transition (Shandarin, Sheth & Sahni 2004). The technique makes no assumptions about the shapes of voids that generally are highly non-spherical. At higher thresholds, the total volume in all but the percolating void drops off precipitously and the excursion set practically becomes a single percolating void. Our voids are identified at the percolation threshold $\delta \approx -0.88$ (filling fraction of the voids, $FF_v = 20$ per cent). We find 19 voids larger than $5 h^{-3} \text{ Mpc}^3$. The largest void is of irregular shape and its volume is $V = 2.1 \times 10^4 h^{-3} \text{ Mpc}^3$. There are neither haloes nor galaxies inside these voids. Galaxies start to appear in the percolating void at $\delta > -0.86$ ($FF_v > 27$ per cent) and haloes at $\delta > -0.63$ ($FF_v > 66$ per cent). In the following, this void finder and its results are referred to as *Shandarin/Feldman*.

3.2 Finders based on the galaxy or halo distribution

3.2.1 Brunino: spherical voids in halo catalogue

This void finder algorithm uses the void centres provided by *Pearce's* algorithm as an initial guess for the location of the underdense regions. These positions are then used to search for the maximum spheres that are empty of haloes with masses larger than $8.6 \times 10^{11} h^{-1} M_\odot$, or 1000 particles. To characterize the final position of the void centres and their radii, we populate a sphere of radius $R = 5 h^{-1}$ Mpc, centred on each initial position, with 2000 random points (the choice of these quantities has proved to be the most convenient in order to obtain a stable result). For every point in this sphere, the position of the closest four haloes lying in geometrically 'independent' octants is found. The sphere defined by these four haloes is then built. This is repeated for all the 2000 random points. As a characterization (position and radius) of the void, the biggest empty spherical region generated in the previous step is chosen.

It is important to stress that the position of the void defined in this way normally does not match the position of the initial guess. Furthermore, in this work, voids whose centre turned out to lie inside a larger void have been discarded. A total of six void regions have been found in the volume of interest, three of which have been neglected applying this criteria. This algorithm is a variant of the one described in Patiri et al. (2006a) which has been developed to resemble the observational technique used to detect voids to enable a more direct comparison with simulations (e.g. Trujillo, Carretero & Patiri 2006; Brunino et al. 2007) In the following, this void finder and its results are referred to as *Brunino*.

3.2.2 Fairall: voids in the galaxy distribution

Voids have been located manually by inspection of slice visualizations: a moving slice, in x and y with thickness $\Delta z = 5 h^{-1}$ Mpc, has been passed through the data in steps of $2.5 h^{-1}$ Mpc. Its progress has been visualized by a software that shows both individual galaxies and large-scale structures, the latter based on minimal spanning trees with percolations of $1 h^{-1}$ Mpc or less (effectively 'friends of friends'). The voids are conspicuous cavities, approximately spherical, empty or almost empty of galaxies, visible in consecutive slices, with sharply defined walls formed by large-scale structures. Since the voids interconnect with one another, the large-scale structures do not necessarily completely enclose each void. If a void departs from sphericity, an average radius is estimated. Where the data allow, distinct voids as small as $2.5 h^{-1}$ Mpc (radius) are identified. In the following, this void finder and its results are referred to as *Fairall*.

3.2.3 Foster/Nelson: voids in the galaxy distribution

The identification of voids is calculated using a prescription similar to that of Hoyle & Vogeley (2002). The algorithm has been extensively employed to analyse void structure and distribution using the results from the recently published Data Release 5 (DR5) of the Sloan Digital Sky Survey (SDSS) (see, Foster & Nelson 2007). The average distance to the third nearest neighbour (d) in the sample and its standard deviation (σ) are calculated. In order to ensure a high degree of confidence in identifying bona fide voids, we use the parameter $R_3 = d + \lambda \sigma$ to distinguish wall galaxies from field galaxies and set $\lambda = 2$. Wall galaxies are defined as those galaxies whose third nearest neighbour is closer than R_3 . All other galaxies are field galaxies. The wall galaxies are placed in a grid whose basic cell geometry is cubic having a side of length $R_3/2$. The empty cells are then identified and each empty cell acts as a seed from which holes are grown. A hole is defined as a sphere that is entirely devoid of wall galaxies. Its radius and centre are computed such that there are exactly three wall galaxies on its surface. Voids are then formed by amalgamating the overlapping holes starting with the largest holes. Only holes whose radius exceeds a certain threshold value ($R_{\min} = 7.5 h^{-1}$ Mpc for this analysis) can form voids; those that are smaller are used to map out the boundary surface of a pre-existing void. Thus, if there are no holes whose size exceeds the threshold, no voids will be identified. The position of the centre of each void is calculated by finding the 'centre of volume'. The position of the centre and the volume are calculated using Monte Carlo methods and the equivalent spherical radius is determined. In the following, this void finder and its results are referred to as *Foster/Nelson*.

3.2.4 Gottlöber: empty spheres in point set

The void finder starts with a selection of point-like objects in 3D space. These objects can be haloes above some mass (or circular velocity) or galaxies above some luminosity. Thus, voids are characterized by the threshold mass or luminosity.

For the data used here, $N_g = 380$ grid cells in each dimension were used, which corresponds to a grid cell size of $158 h^{-1}$ kpc. On this grid, the point is found, which has the largest distance to the set of points defined above. This grid point is the centre of the largest void. This void is then excluded, and the procedure is repeated by searching for a point with the largest distance to the set. Iterating this procedure thus yields the full sample of voids

Table 2. An overview of some of the main results of this study: for each void finder, we give the total number of voids, N_V , in the volume considered here, the volume filling fraction, FF_V , the average DM overdensity, δ_{DM} , of the voids, the total number of galaxies, N_g , found in voids, the average galaxy overdensity δ_g , the number of galaxies brighter than $m_B = -20$, $N_{g,20}$, found in voids, the average galaxy overdensity using only galaxies brighter than $m_B = -20$, $\delta_{g,20}$, and positions of the centres of the largest void and their radii. We also classify the void finders into those using the DM (smoothed or not – DM) and those using points (galaxies or haloes – P).

Author		N_V	FF_V	δ_{DM}	N_g	δ_g	$N_{g,20}$	$\delta_{g,20}$	$(x_{\max}, y_{\max}, z_{\max})$ (Mpc h^{-1})	r (Mpc h^{-1})
Brunino	P	3	0.37	-0.78	754	-0.71	7	-0.93	(38.6, 46.8, 199.5)	16.0
Colberg ^a	DM	21	0.92	-0.74	2258	-0.65	35	-0.85	(35.3, 41.2, 193.9)	29.9
Fairall	P	18	0.59	-0.73	1376	-0.67	25	-0.83	(33.0, 40.0, 200.0)	20.0
Foster/Nelson	P	3	0.41	-0.82	114	-0.96	0	-1.00	(36.3, 36.6, 192.4)	18.0
Gottlöber ^b	P	9	0.35	-0.77	733	-0.70	0	-1.00	(32.1, 44.0, 192.0)	16.4
Hahn/Porciani ^{a,c}	DM	14	0.29	-0.73	248	-0.92	0	-1.00	(30.5, 33.6, 191.8)	17.2
Hoyle/Vogeley ^{a,b}	P	4	0.84	-0.68	2166	-0.56	40	-0.79	(31.9, 47.1, 193.2)	24.6
Müller ^b	P	24	0.58	-0.76	1469	-0.65	0	-1.00	(30.7, 42.7, 189.1)	25.6
Neyrinck ^{a,c,d}	DM	29	0.32	-0.68	834	-0.63	14	-0.83	(30.3, 33.5, 194.9)	11.3
Pearce	DM	5	0.15	-0.90	51	-0.95	0	-1.00	(35.9, 33.8, 193.5)	11.9
Platen/Weygaert ^a	DM	167	1.0	-0.91	18	-1.00	0	-1.00	(37.5, 36.2, 194.3)	14.3
Plionis/Basilakos	DM	15	0.13	-0.92	0	-1.00	0	-1.00	(37.1, 33.8, 192.7)	10.0
Shandarin/Feldman	DM	19	0.23	-0.88	0	-1.00	0	-1.00	(31.5, 41.1, 192.7)	17.1

Notes. ^aThe voids are non-spherical, so the quoted radius is an approximation, assuming a spherical void. ^bUsing the $B < -20$ galaxy sample. ^cThe quoted centre of the void is actually the position of lowest density. ^d9308 voids found; out of them 2362, 525, 164, 64, 29, 13 and 5 exceed 1, 2, 3, 4, 5, 6 and 7 σ probability thresholds, respectively. We use the 5 σ results for comparisons.

In principle, the algorithm allows to have a certain number of points (objects above the threshold mass or luminosity) inside the void. Here, this number is set to zero, i.e. the voids are completely empty with respect to the defined sample. Of course, they may contain objects with smaller masses or lower luminosities than the assumed threshold.

In principle, the algorithm allows for the construction of voids with arbitrary shape. The starting point is the spherical void described above. It can be extended by spheres of lower radius which grow from the surface of the void into all possible directions. However, in this test case this feature was switched off, and the search was restricted to spherical voids to avoid ambiguities of the definition of allowed deviations from spherical shape. In the following, this void finder and its results are referred to as *Gottlöber*.

3.2.5 Hoyle/Vogeley: void finder

Void finder was introduced in Hoyle & Vogeley (2002; *HV02*) and has been used frequently to locate voids in galaxy surveys (Hoyle & Vogeley 2004; Hoyle et al. 2005). Full details of how *void finder* works can be found in Hoyle & Vogeley (2002), so here we will only briefly summarize the algorithm. *Void finder* operates on samples of galaxies and is based on the ideas discussed in El-Ad & Piran (1997) and El-Ad, Piran & Costa (1997). In a volume-limited galaxy catalogue (with a typical limit just fainter than M^*), galaxies are first pre-categorized into wall or void galaxies, depending on the distances to the galaxies' third-nearest neighbours. Wall galaxies are then binned into cells of a cubic grid. Around the centres of all empty grid cells, the largest possible spheres that are also empty are found. Finally, the set of unique voids is constructed by determining maximal spheres and their overlaps. *Void finder* voids are non-spherical. A minimum void size of 10 h^{-1} Mpc is set to only select the largest, statistically most significant voids. For tests of *void finder* using simulation data, see Benson et al. (2003). In the following, this void finder and its results are referred to as *Hoyle/Vogeley*.

3.2.6 Müller: empty convex regions in point set

This grid based void finder looks first for empty base voids in the halo/galaxy sample, and then it adds extensions to approximate spherical voids. It was run first with only a base void search and then with extensions. The idea of the void finder is to look for empty nearly convex regions in the galaxy distribution. It is based on a grid on the survey volume where cells with galaxies are marked as occupied. In the next step, it looks for maximum cubes on the grid that are empty of galaxies and previously found voids. We call this a base voids, and get a first catalogue of cube voids, the most simple algorithm, but it produces a void catalogue with similar sizes as assuming a spherical base volume. A slightly more refined method is to extend the base voids along the faces with adding square sheets empty of galaxies and not contained in previously found voids. This extension procedure is iterated. To avoid extended fingers or bridges between voids, we require the extension to have a surface bigger than two-thirds (an arbitrary parameter) of the previous one. These extended voids have on average the same volume in the extensions as in the base voids. We measure the size by the effective cube size, that is, a cube of the same volume as the base plus extensions. Such voids are in general larger than selecting square voids. This void finder is based on the prescription of Kauffmann & Fairall (1991), which was further developed and tested by Müller et al. (2000) and Arbabi-Bidgoli & Müller (2002). It uses a 300³ grid and includes voids with a minimum effective radius of 3 h^{-1} Mpc. In the following, this void finder and its results are referred to as *Müller*.

4 RESULTS–COMPARISON

4.1 Basic numbers

In Table 2, we provide an overview of the results obtained with the different void finders. In particular, for each void finder, we list the total number of voids, N_V , the volume filling fraction,³

³ The volume filling fraction is the fraction of the volume that is contained in voids, FF , where the sum is over all voids in the sample, and V_{total} is the total volume; so, for example, $FF_V = 0.5$ means that voids fill half the volume.

FF_v , the average DM overdensity, δ_{DM} , of the voids, the total number of galaxies, N_g , found in voids, the corresponding average galaxy overdensity, δ_g , the number of galaxies brighter than $m_B = -20$, $N_{g,20}$, found in voids, the corresponding average galaxy overdensity using only those galaxies, $\delta_{g,20}$, and positions of the centres of the largest void and their radii.

When comparing these numbers it is important to keep the differences in the void finders in mind. For example, some void finders construct strictly spherical voids, whereas others build larger ones out of spherical proto-voids. In addition, there are differences in the spatial resolutions. The numbers of voids found in the volume thus can be expected to be different, and they should merely be treated as illustrative quantities.

If the different results strictly reflected the density field in the simulation, that is, if all the void samples were centred on the most underdense regions and then extended out to higher density regions, there would be a simple relationship between the volume filling fraction FF_v and the average DM overdensity δ_{DM} . To a certain degree such a correlation does exist. For example, the *Pearce* voids are centred on the particles with the lowest local densities and are cut off at an overdensity of $\delta = -0.9$, whereas *Colberg* voids are constructed around proto-voids with $\delta = -0.8$. This results in a much lower value of FF_v for *Pearce*, whereas *Colberg*'s voids fill almost the entire volume.⁴

A more detailed examination of Table 2 reveals the key difference between the void finders we have employed: they effectively target different mean overdensities. Those which correspond to a low mean overdensity (*Pearce*, *Platen/Weygaert*, *Plionis/Basilakos* & *Shandarin*, all with $\delta \sim -0.9$) naturally contain very few galaxies as they pick out the deepest parts of the voids. At the other extreme, those finders which effectively employ higher overdensity thresholds (for instance, *Colberg* and *Hoyle/Vogeley* with $\delta \sim -0.7$) pick out much larger regions and naturally enclose far more galaxies. There is nothing intrinsically wrong with different void finders targeting different overdensities, in fact in some sense pretty much the whole region could be classed as a ‘void’, in that it has far less DM than expected and consequently is depleted of galaxies. As a result secondary characteristics such as the void radius or the number density of void galaxies need to be calibrated against this effective threshold before techniques can be compared in detail. Such a study is beyond the scope of this paper but should be borne in mind when examining such measures as the largest void in any particular dataset.

Given that not all void finders are density-based, there also is no direct relationship between FF_v and the number of galaxies inside the voids, N_g . There is a clear difference in N_g between the different models, with *Plionis/Basilakos* and *Shandarin/Feldman* finding no void galaxies whatsoever,⁵ and the most extreme cases with several thousand void galaxies. Given the fact that the volume studied here has a mean overdensity of $\delta = -0.28$, finding lots of void galaxies is maybe not all that surprising – provided one is happy with the existence of such objects. The number of galaxies brighter than $m_B = -20$, $N_{g,20}$, is either zero or very small for all void finders. This is an important agreement for void finders which accept the

⁴ Recall that the subvolume studied here has a mean overdensity of $\delta = -0.28$. Thus, *Colberg*'s result is not all that surprising, given the procedure it uses and the fact that the whole region is quite underdense.

⁵ Note, though that for *Plionis/Basilakos* a change in the PDF fraction, below which ‘void cells’ are considered, to the lowest 30 per cent of the PDF, results in finding void galaxies.

existence of galaxies in voids: The overdensity of such galaxies, $\delta_{g,20}$, is smaller than about -0.8 , regardless of how voids are found.

There are also interesting agreements for quite different void finders. For example, *Plionis/Basilakos* and *Pearce* find very similar results (FF_v , δ_{DM} , and especially the position of the largest void, but not N_g).

In Table 2, we also give the position of the centre of the largest void and its radius, as provided by the different groups. Note that some void finders build non-spherical voids, so the quoted radius merely reflects the total size of the void. While all the finders indeed locate a large void within the central region, it is perhaps a little surprising that some centres are not within the central structure that is so clearly visible in the top left-hand panel. This is in fact another consequence of the varying density thresholds employed in that those finders with effectively lower thresholds rely on larger scale structures than those that employ very low density thresholds. In addition, some methods (such as those of *Brunino* and *Gottlöber*) find several voids of nearly equal size in this region, as evidenced by the number of marked blue galaxies in Fig. 1 that are not within the marked green void. The key point is that the filamentary structures visible in the top left-hand panel of Fig. 1 are not very massive. Again it is clear that *void sizes depend quite strongly on how voids are found*, so one has to be very careful about using void sizes to make statements about large-scale structure.

In Figs 1 and 2, we show void galaxies found by the different groups. As noted above, the top left-hand and top centre panels of Fig. 1 give only the DM distribution and the DM plus all model galaxies, respectively. All other panels superimpose all the recovered void galaxies on top of the DM distribution. In addition, for each group, we also show the largest void in green. The void centre is marked with a large red dot.

As is clearly visible, there are quite large variations between the different groups, a direct consequence of the wide variety of techniques and limits employed. Hopefully, these figures shed some light on the question of what each group actually means when they refer to a ‘void’ and illustrate the inherent difficulty of comparing results obtained using different void finders. Individually, the results of each group make perfect sense, when seen in the light of how voids are identified. For example, the *Pearce* voids are some of the most underdense spheres in the volume, centred on the particles with the lowest density. Conversely, at first glance, the *Colberg* void does not appear void at all and spans the entire figure, but this is a natural consequence of the very low density of the entire region.

Thus, unless agreement has been reached on how to define what a void really is – or should be – it is not straightforward to argue which void finder does the best job, at least when comparing images.

4.2 Void density profiles

Despite the differences in the void-finding methods employed in earlier studies, there has been broad agreement on two facts, namely that voids are very empty in their centres and that they have very sharp edges (see e.g. Benson et al. 2003; Colberg et al. 2005, or Patiri et al. 2006b). Given the differences in the void finders, ‘very empty’ might mean different things. It might mean that the voids are literally empty of the objects used as data – such as galaxies below some given luminosity, say – or that voids do contain some material (e.g. DM), but very little of it.

With the large variety of void finders used here, it is an interesting and important point to study the internal structure of a void. With the volume under consideration relatively small and underdense, most of the void finders find one very large void, at about the same

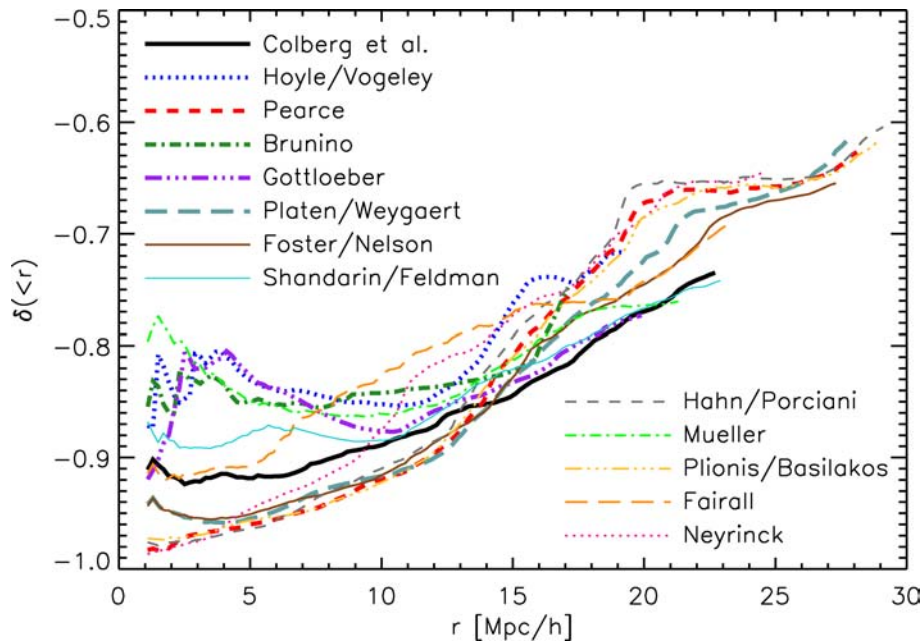


Figure 3. Radially averaged DM density profiles of the largest void in each of the void catalogues found by the groups involved in this study. For each void finder, the profile extends out to the largest radius that can be studied, given the size of the volume. See the main text for more details.

location. We are thus limited to studying the structure of the largest void in each catalogue.

Fig. 3 shows the radially averaged enclosed DM density as a function of radius for each of the catalogues, using the void centres given in Table 2 and shown visually on Figs 1 and 2 as a red point. It is quite important to note that such a radial average is not ideal for void finders that produce non-spherical voids. Also, for each void finder the profile extends out to the largest radius that can be studied, given the size of the volume, so only the profiles of voids that lie close to the centre of the volume extend beyond $25 h^{-1}$ Mpc. Note that these radially averaged density profiles cannot be easily compared with the average overdensities quoted in Table 2. The values quoted in Table 2 were computed using only the total void volume. However, radially averaging as in Fig. 3 for voids that are not perfectly spherical will include material that does not lie inside a void.

It appears that the void finders fall into three broad categories, namely those which have central densities well below $\delta = -0.9$ (*Foster/Nelson, Hahn/Porciani, Neyrinck, Platen/Weygaert, Plionis/Basilakos, Pearce*), those with much higher, flat, central densities (*Brunino, Gottlöber, Hoyle/Vogeley, Müller*) and a third set with intermediate central densities (*Colberg, Fairall, Shandarin/Feldman*). Void finders with very low central densities all use the DM density field in order to identify voids in combination with a low effective overdensity threshold which restricts the size of the voids. The void finders that use (model) galaxies or haloes all have somewhat higher central densities, and much flatter central profiles. This effect is partly due to the inclusion of small haloes near the void centres as well as the difficulty of defining a void from a sparse sample of points. Nevertheless, it is clear that voids selected using the sparse tracers available from galaxies or haloes typically have central overdensities around $\delta = -0.85$ whereas those selected from the richer DM distribution have typically lower central density limits. Fig. 3 further illustrates the role of the effective overdensity threshold driving void choice: in the central region the method of *Colberg*

does not recover a particularly deep void; however, between 15 and $20 h^{-1}$ Mpc, this method has found the most underdense region of all the finders.

Up to a radius of around $15 h^{-1}$ Mpc, the largest void in each catalogue has an average density of $\delta \approx -0.85$ and at larger radii the radially averaged densities are all rising. However, the entire volume studied here has a mean $\delta = -0.28$ so none of the voids runs into the very steep edges seen in earlier work as we are still well below the mean cosmic density.

Despite the differences in the central densities, we can conclude that regardless of how voids are found, their interiors are very underdense and they contain mean densities between 5 per cent and 20 per cent of the cosmic mean. The central regions of voids also tend to have a rather flat profile which means that regardless of how voids are found in observational surveys, follow-up work of their interiors – such as, for example, searches for hydrogen (see, for example, Giovanelli et al. 2005) – should expect very low densities of material, provided, of course, that the current model of structure formation used in the simulation is correct.

4.3 Luminosity function

Fig. 4 shows the luminosity functions of galaxies in the entire Millennium simulation (solid red line), that of the volume under consideration (solid black line) and in each of the catalogues of those void finders which identify galaxies inside voids, colour-coded as shown in the figure.

We present this plot mostly for illustrative purposes, since the volume under consideration here is quite small. The key difference between the full simulation and our selected subvolume is that the galaxy formation efficiency across this entire region has been suppressed. In the full Millennium volume, there are 7151 282 galaxies with M_B between -16 and -22 . If the central $40 h^{-1}$ Mpc of our subvolume was a random section of the full box, you would expect to find 3661 galaxies. In practice, our region has 707, or less

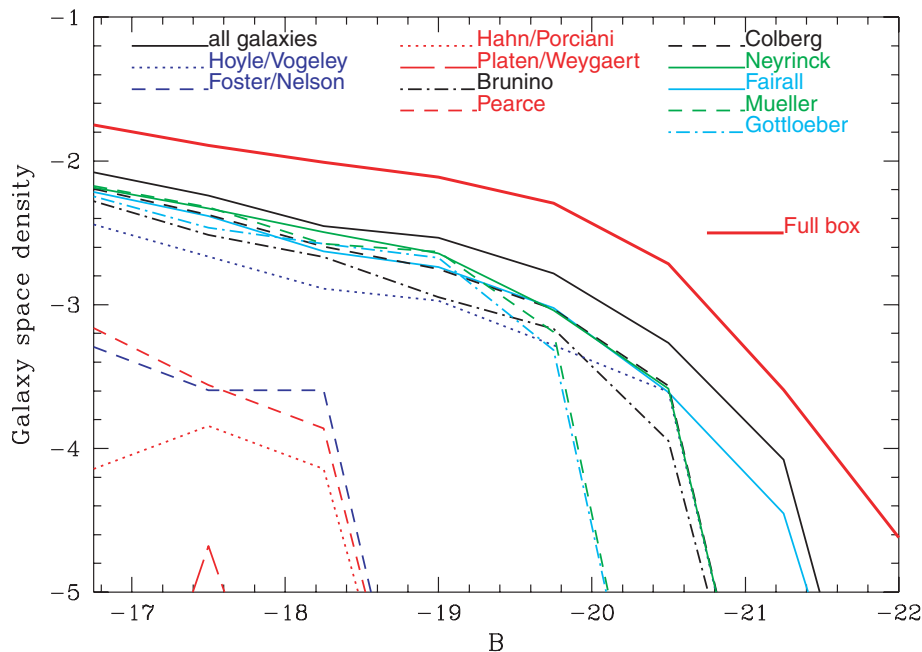


Figure 4. Space density of galaxies ($h^3 \text{Mpc}^{-3} \text{mag}^{-1}$) as a function of dust-corrected M_B for galaxies in the volume under consideration and in the catalogues of those void finders which identify galaxies inside voids. For purposes of comparison, the luminosity function of the full simulation volume is also given. Each void finder luminosity function is corrected for the volume occupied by the relevant void sample.

than one-fifth of the expected number. As well as this overall normalization, compared with the full volume of the simulation, the luminosity function of the subvolume is very slightly steeper at the faint end and is deficient in bright galaxies. As mentioned before, the subvolume is underdense, so we do not expect to find many bright galaxies.

The luminosity functions of the samples that contain significant numbers of galaxies (with the exception of *Fairall*) show an even greater deficiency of bright galaxies, as evidenced earlier by the very low overdensity of bright galaxies in voids (Section 4.1). Although it is difficult to tell, it looks as if at the fainter end, the luminosity functions of the void samples all are just very slightly steeper than the subvolume ones and slightly steeper than the full simulation volume ones. This could be seen as a trend towards the most isolated galaxies being fainter than expected, as would be suggested from theoretical arguments. Those galaxies residing in the most underdense regions (although there aren't very many) are certainly faint. The limit of this effect, no galaxies in the voids, is achieved by two finders, those of *Plonis/Basilakos* and *Shandarini/Feldman*.

4.4 Void galaxies and local environments

Given that we are interested in comparing results from different void finders, it is worthwhile to look at which galaxies void finders identify as belonging to a void. Apart from a galaxy's brightness, its environment, expressed through some measure of the local density, provides a useful descriptor. In order to quantify the local density, for each galaxy we compute r_{14} , the radius of the sphere that contains a mass of $10^{14} h^{-1} M_{\odot}$, roughly the mass of a small galaxy cluster.

In Fig. 5, we show the distribution of the values of r_{14} , for both the complete subsample and the individual void galaxy sets. Large (small) values of r_{14} correspond to regions of low (high) density. The distribution reflects the fact that the subvolume considered here

is underdense, since most galaxies reside in the low-density part of the distribution.

One would naively expect that void finders would pick up the galaxies in the lowest density regions first and then move towards the higher density regions. However, while this is true for some of the void finders, it is not true for all of them. This fact should be an important criterion for future discussions of void finders: if a void finder locates galaxies inside voids, should these be those in the most underdense environments?

Interestingly enough, the purely visual *Fairall* void-finding results in a distribution that is quite similar to *Colberg's*, and also to *Neyrinck's* and *Müller's*. Given the large differences in the methods, these similarities are quite interesting, and they merit to be taken into account in future discussions of how to find voids.

5 SUMMARY AND DISCUSSION

This study represents the first systematic study of 13 void finders, all of which have been used over the past decade to study voids, using the same data set to compare results. For the data we used real-space coordinates of particles, haloes, and semi-analytical model galaxies (Croton et al. 2005) from a subvolume of the Millennium simulation (Springel et al. 2005). The goal of this paper was *not* to argue about the best way to define or identify voids. Instead, we aimed at allowing the reader to understand the differences between the methods to allow easier comparison of studies of voids in the literature.

As outlined in Table 1, the void finders in this study range from studies of the smoothed DM density field to identifying empty spheres in the distribution of model galaxies, the latter either using sophisticated algorithms or simply the human eye. Given the vastly different assumption of what a void actually is, it is not surprising to see large differences between some of the void finders. However,

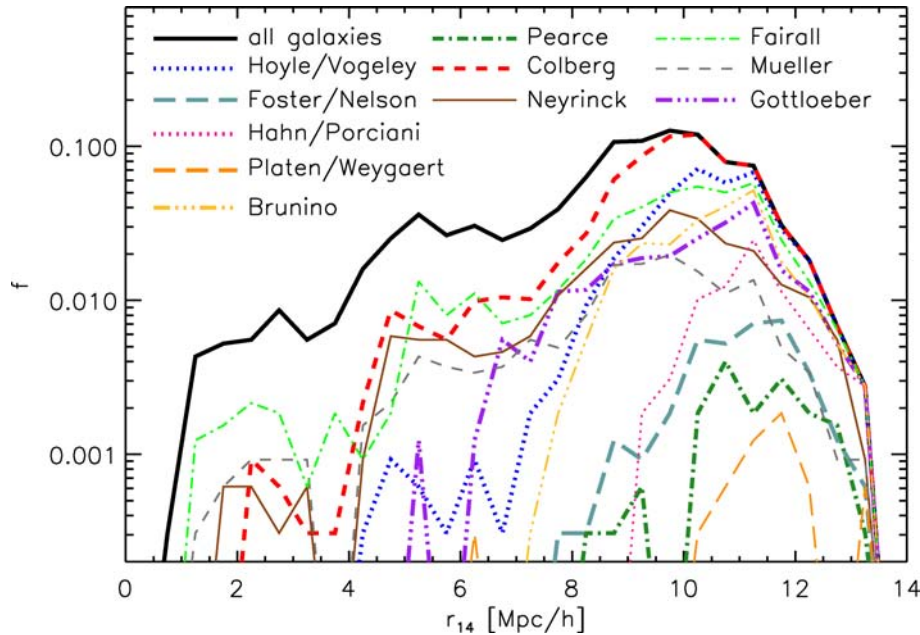


Figure 5. Distributions of the local densities of the galaxies in the results of those void finders that identify void galaxies. The local density is expressed via r_{14} , which for each galaxy gives the radius of the sphere around the galaxy that contains $10^{14} h^{-1} M_{\odot}$. For comparison purposes, the distribution of the full galaxy sample is also shown.

there are also some quite encouraging agreements between methods that are quite different.

Not surprisingly, the different methods result in a large spread in basic numbers such as the number of voids, the size of the largest voids (see Table 2), or their basic appearance (see Figs 1 and 2). We caution against putting too much emphasis on this fact. If one void finder constructs spherical voids with mean overdensities of $\delta = -0.9$ and another one builds large, irregularly shaped voids from spherical proto-voids in a distribution of galaxies, then the numbers and sizes of voids can be expected to be quite different. Likewise, the fraction of volume filled by the voids will be different. Regardless of these differences, it is quite interesting to see that the locations of the largest voids found by most of the groups agree quite well with each other. The eye finds a large void in the centre of the region studied, and the void finders do the same!

For a more detailed comparison, the effective overdensity proves to be most interesting. Here, the spread is not quite as extreme as expected (see the values of δ_{DM} in Table 2), and the agreement in the overdensities of bright galaxies is quite impressive. The void finders in this study agree that there should be no or just a very small number of bright galaxies in voids. In other words, regardless of how one defines voids, there are almost no bright galaxies in them.

As Section 4.2 shows, the differences in the (radially averaged) density profiles of the largest void are also not very large, with the void centres containing only between 5 and 20 per cent of the mean density. This means that regardless of how voids are found, their centres contain very little mass – unless, of course, our model of cosmic structure formation, which forms the basis of the simulation, is wrong. With searches for H I emission in voids under way (see Giovanelli et al. 2005 or Basilakos et al. 2007), there should soon exist additional data points, which makes it all the more pressing to move towards a more unified picture of voids.

As just mentioned, voids contain very few bright galaxies, and they contain relatively more dim galaxies, something that those

void finders that identify void galaxies appear to agree on, too (see Section 4.3). Given the small number statistics in our sample, it is impossible to make stronger comments about this. What appears clear, though, is that this is an important topic to study, both observationally and theoretically, in particular, since current models of galaxy formation and evolution have to account for the observed relation. For these studies to be successful, more common ground is needed as far as defining and finding voids is concerned.

We hope that this paper will trigger more detailed follow-up studies to work towards a more unified view of how to define and find voids. We believe that studies like this one, which make use of high-resolution simulations of large-scale structure, provide invaluable tools to this end, since they contain full information about the distribution of model galaxies and of the underlying density field. In the end, the model could then still be entirely wrong – a possibility that, in the light of the recent development of a standard cosmological model, appears to be somewhat unlikely – but it will still be able to provide a sound basis for calibrations of methods and ideas. This point is of particular interest since observationally (at present) only galaxies can be used to find voids. The distribution of galaxies is much harder to model, though, than the cosmic density field – the latter can be described quite well using linear theory. For studies of voids to be useful, a link needs to be forged between theory and observation. We hope that this work will provide a basis for resolving this situation. Ultimately, as one of the most extreme cosmic environments, voids possess the potential to constrain models of galaxy formation. However, for that to be the case, we need to agree on what they really are and how to find them.

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