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Nanoindentation Study of Buckling and Friction of Silicon Nanolines

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Nanoindentation Study of Buckling and Friction of Silicon Nanolines

By

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Dissertation

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Dedication

To my wife, Xiaoning Liu and my son, Daniel Luo

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Nanoindentation Study of Buckling and Friction of Silicon Nanolines

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Silicon-based nanostructures are essential building blocks for nanoelectronic

devices and nano-electromechanical systems (NEMS). As the silicon device size

continues to scale down, the surface to volume ratio becomes larger, rendering the

properties of surfaces and interfaces more important for improving the properties of the

nano-devices and systems. One of those properties is the friction, which is important in

controlling the functionality and reliability of the nano-device and systems. The goal of

this dissertation is to investigate the deformation and friction behaviors of single

crystalline silicon nanolines (SiNLs) using nanoindentation techniques.

Following an introduction and a summary of the theoretical background of

contact friction in Chapters 1 and 2, the results of this thesis are presented in three

chapters. In Chapter 3, the fabrication of the silicon nanolines is described. The

fabrication method yielded high-quality single-crystals with line width ranging from

30nm to 90nm and height to width aspect ratio ranging from 10 to 25. These SiNL

structures have properties and dimensions well suited for the study of the mechanical and

vi

friction behaviors at the nanoscale. In Chapter 4, we describe the study of the mechanical properties of SiNLs using the nanoindentation method. The loading-displacement curves show that the critical load to induce the buckling of the SiNLs can be correlated to the contact friction and geometry of SiNLs. A map was built as a guideline to describe the selection of buckling modes. The map was divided into three regions where different regions correlate to different buckling modes including Mode I, Mode II and slidingbending of SiNLs. In Chapter 5, we describe the study of the contact friction of the SiNL structures. The friction coefficient at the contact was extracted from the loaddisplacement curves. Subsequently, the frictional shear stress was evaluated. In addition, the effect of the interface between the indenter and SiNLs was investigated using SiNLs with surfaces coated by a thin silicon dioxide or chromium film. The material of the interface was found to influence significantly the contact friction and its behavior. Cyclic loading-unloading experiments showed the friction coefficient dramatically changed after only a few loading cycles, indicating the contact history is important in controlling the friction behaviors of SiNLs at nanoscales. This thesis is concluded with a summary of the results and proposed future studies.

Table of Contents

List of Tal	bles	X
List of Fig	ures	xi
Chapter 1:	Introduction	1
1.1	Challenges of Fabrication and Characterization of Nano-structures .	4
1.2	Mechanical Characterization of Nano-structures	7
1.3	Nanofriction of SiNLs	9
1.4	Objective and Organization of Dissertation	. 12
Chapter 2:	Contact Mechanics and Compressive Instability of Columns	. 14
2.1	Contact Mechanics of a Sphere pressed into a Half-space	. 15
	2.1.1 Adhesionless Contact Mechanics - Hertzian Model[66]	. 15
	2.1.2 Adhesive Contact Mechanics	. 17
2.2	Compressive Instability of Columns	. 22
Chapter 3:	Experimental Techniques	. 27
3.1	Fabrication of SiNL Test Structures	. 27
	3.1.1 Electron Beam Lithography Technique	. 28
	3.1.2 RIE and Pattern Transfer Process	. 32
	3.1.3 Anisotropic Wet Etching (AWE) Process	. 33
	3.1.4 SiNL Structure Design and Fabrication Results	. 34
	3.1.5 Coating of SiNLs with Silicon Dioxide and Chromium	. 40
3.2	NanoMechanical Testing System	. 41
Chapter 4:	Analysis of Buckling Behavior of SiNLs	. 45
4.1	FEM Simulation of Nanoindentation on SiNLs	. 46
	4.1.1 FEM Model	. 46
	4.1.2 FEM Simulation Results for 75nm SiNLs	. 48
4.2	Analysis of Experimental Load-Displacement Curves	. 50
4.3	Buckling Response Analysis	. 55
	4.3.1 Formulation of the Problem	. 56

	4.3.2 Buckling Modes and Critical Loads Analysis	58
	4.3.3 The Effect of Geometry and Friction on Buckling Behavior	65
4.	4 Summary	69
Chapter	5: Frictional Behaviors of SiNLs	70
5.	1 Introduction to Test Structures and Test Ambient	70
	5.1.1 Test Structures	71
	5.1.2 Impact of Test ambient on Friction at contact	73
5	2 Contact Area Evaluation	77
	5.2.1 Formulation of the problem	77
	5.2.2 Calculation of Contact Area	79
	5.2.3 Calculation of Penetration Depth by indentation Displacemen	t 82
	5.2.4 Calculation of Penetration Depth by Normal Force	
5	Friction of Bare SiNLs	86
	5.3.1 Experimental results for 90nm and 75nm SiNLs test structure	s 86
	5.3.2 Experimental results for 60nm/610nm and 30nm/720nm SiNI	
5.4	•	
5.:		
5.0		
Chapter	6: Summary and Future Work	106
6.	1 Summary	106
6	2 Future Work	108
Selected	l Publications	111
Referen	ces	112
Vita		120

List of Tables

Table 4.1 Coefficient of Friction Required for Mode II Buckling	68
Table 5.1 Specifics of 5 sets of test structures and coating layers. Test conditions are also summarized. The thickness of silicon oxide and chromium layers were around 3nm and 2nm respectively.	
Table 5.2 Critical Loads of 70nm/610nm SiNLs under dry and ambient test conditions	75
Table 5.3 Critical loads and friction coefficients of 90nm bare SiNLs	88
Table 5.4 Frictional Shear Stress of 90nm SiNLs	90
Table 5.5 Frictional Shear Stress of 75nm SiNLs	90
Table 5.6 Summary of critical loads and friction coefficient	91
Table 5.7 Average critical loads and friction coefficient of 75nm SiNLs with or without coating layers.	95
Table 5.8 Critical loads and friction coefficients of 90nm SiNLs under a 4-cycle loading experiment	99

List of Figures

Figure 1.1 Application of silicon nanowires in a dual-gate NWFET with Silicided contact
Figure 1.2 (a) Plan view SEM image of SiNWs formed by VLS process [21]. (b) Cross-sectional SEM image of lateral epitaxial SiNWs grown between microtrench by MCCVD process
Figure 1.3 (a) 12 nm wide SiNWs generated by SNAP process. Pattern was transferred into silicon using CF4+O2 plasma etching, showing line roughness due to ion bombardment. The scale bar in the inset is 150 nm. (b) SEM image of feature cross-sections of silicon lines after KOH wet etching on (110) Si wafer. The silicon nitride hard-mask caps had not been removed
Figure 1.4 Schematic of experiments setup, a) before and b) after the manipulation8
Figure 1.5 Schematic of nanoindentation experiments on hollow column at deferent stages of the indentation process and different possible buckling modes9
Figure 2.1 Geometry of the Hertzian model before contact a) and after contact b)17
Figure 2.2 Geometry of the DMT adhesive contact. The attractive interactions act outside the contact zone
Figure 2.3 Schematic illustration of JKR adhesive contact. The existing of adhesive forces changes the area of the contact zone which is shown by the formation of "necking" in a) outside of the contact zone denoted by dashed curve. In order to keep the area of contact zone constant under this case, a negative force is need to "pull out" the punch a little which is shown in b)
Figure 2.4 Beam-column structures with axial and transverse load. a) with both ends fixed; b) with one end fixed and the other end hinged; c) with both ends hinged.25
Figure 3.1 Layer stack of EBL substrate

Figure 3.2 The effect of dosage levels on the line width of SiNLs. Left, under-dosed exposure leaving more materials unremoved in the trench area (dark), and resulted in larger line width (brighter). Right, over-dosed exposure removed more materials from the trench area, and SiNLs structures with smaller line width were obtained.
Figure 3.3 Difference between anisotropic etching and isotropic etching34
Figure 3.4 a) Schematic of the mask design of SiNLs. b) A trench was formed by AWE. c) Schematic of cross-section of a trench. d) Formation of a SiNL between two trenches.
Figure 3.5 The silicon nanoline arrays fabricated by EBL and AWE. a) Grating pattern of in array element; b) SEM image of SiNLs structures after AWE. c) Pattern array for orientation alignment.
Figure 3.6 Schematic of undercut and line width control.
Figure 3.7 Cross-sectional SEM images of some Si nanoline arrays fabricated by EBL+AWE. (a) 30 nm wide lines with height of \sim 350 nm; (b) 65nm wide lines with height of \sim 1 μ m. (c) 1500 nm wide lines with height of \sim 560 nm40
Figure 3.8 Schematic of an AFM based nano-indentation process
Figure 3.9 SEM images of three types of indenters. (a) Berkovich indenter, 3-Sided pyramidal shape, 142.6° (edge to opposing face), and ~ 150 nm tip radius; (b) NorthStar indenter, 3-Sided pyramidal shape, Cube corner profile, and ~ 50 nm tip radius; (c) Conical indenter, conical shape, 60° included angle and > 1 μ m tip radius.
Figure 3.10 Schematic of indentation technique for modulus and hardness measurement. (a) Indentation on surface of materials; (b) typical load vs. displacement curve recorded in the indentation process
Figure 4.1 Layout of the 3D FEM model of indentation on silicon nanolines
Figure 4.2 FEM simulation of the silicon nanolines under indentation. The tip of the indenter is located on top of the trench center of the 75 nm silicon nanolines. (a) plots of the simulated load-displacement curve (b) and (c) show the deformation of SiNLs before and after the mode transition at the critical load, corresponding to A and B marked in (a), respectively. Since the indentation displacement was small only deformations of 6 lines are included in these plots

Figure 4.3 The dependence of critical buckling load on the friction coefficients. When the friction coefficient increases, the height of the peak of the load-displacement curves increases indicating the increasing of critical buckling load50
Figure 4.4 Indenation response of a set of SiNLs with 60 nm line width and 640 nm height and an aspect ratio 10.6. Four regions of the load-displacement curve was defined in a). The green region shows an elastic response of SiNLs, which is also shown schematically in b). The dashed green curve is the load-displacement curve predicted by the Hertzian model. The purple region shows a displacement burst. This indicates the instability of the SiNLs occurs after the applied load reaches the critical load, and the SiNLs buckles as shown in c). In the yellow region, the SiNLs slide on the surface of indenter tip as shown in d). In the final stage, the indenter was withdrawn from the SiNLs as shown by the red region of the load-displacement curve and in the inset e). Interestingly, the SiNLs fully recovered without residual deformation left after indentation54
Figure 4.5 a) A typical load-displacement curve shows the irrecoverable displacement after the withdrawal of indenter from the SiNLs structures. b) fracture of SiNLs and debris were observed in SEM images
Figure 4.6 Contact geometry of nanoindentation. The shape of the diamond indenter was conical but it was modeled as a sphere with a radius R of 3.9 μm. In the picture, two SiNLs were shown in contact with the indenter. θ is the angle that measure the relative place of the contact point on the indenter. F is the total force applied on the indenter in the vertical direction. Fn is the force on SiNLs that was normal to the indenter surface
Figure 4.7 Mode I buckling
Figure 4.8 Mode II buckling60
Figure 4.9 Effect of height to width aspect ratio of SiNLs and width to pitch ration on the buckling behaviors. When the coefficient of frictions are located in region marked by "A", Mode II buckling occurs, otherwise, Mode I buckling occurs68
Figure 5.1 SEM images of the 30nm test structures. a) top view. b) side view. The SiNLs have height of 720nm and pitch of 450nm
Figure 5.2 Image of the test system covered by a transparent cover. The test environment was enclosed and the humidity inside was measured to be nearly constant ~ 45% RH under air ambient. Additional electric power cords for the baking of the test structure were added to achieve a dry test condition. The telescope on the left was used to locate the indenter on the test structures74

heating stage is consisted of a silicon chip with copper film resistor, which is sandwiched between the test structures and the sample stage. Temperature of the test structures was controlled by the DC power source. In the experiments, temperature up to 110°C was maintained for about 10 minutes to drive out moisture on the test structures. A humidity of less than 5% was measured after 3 hours of dry nitrogen gas flush afterwards
Figure 5.4 The geometry of a diamond indenter on SiNLs structures before the indenter was brought into contact with the SiNLs. The tip of the indenter was placed at the center of the trench
Figure 5.5 Geometry configurations that are equivalent as the original contact geometry defined in Figure 5.3. Here, the system is defined as SiNLs "indenters" indent on a diamond half-space. The SiNLs originally having rectangular cross-section are now replace by SiNLs "indenters" with their top surfaces defined as spherical sectors. The spherical sectors have the same diameter as that of the original diamond indenter
Figure 5.6 SiNLs indenters before contact a), and SiNLs being pressed into the diamond half-space b), but the contact zone size a is smaller than the line width w on the x direction, i. e. the contact is incomplete
Figure 5.7 Two key points were defined in the FEM model to evaluate the elastic deformation of the SiNLs. After the SiNLs were deformed, A and B moved to points A' and B'. The elastic deformation delastic is defined by OB-OB'. The local deformation (penetration depth δ) is assumed to be AB-A'B'84
Figure 5.8 Deformation of SiNLs from FEM simulation. Pink curve shows the displacement of point A, and the red curve is for B. The blue curve is the displacement of the diamond indenter which is very close to the displacement at point A, since point A is in contact with the diamond indenter until the occurrence of buckling.
Figure 5.9 Contact area of SiNLs as a function of applied load. Two methods were used to evaluate the contact area, the force integration and displacement method.
Figure 5.10 Two sets of load-displacement curves were presented. One set of curve (green) showed two different displacement bursts, which indicated two different buckling models. One buckling occurred during the loading (marked as A), the other occurred at the unloading process (marked as B). On the other set of curve (brown), only one displacement burst was observed on the loading process88

Figure 5.11 Average friction coefficients for test structures with width/height configurations of 90nm/1400nm, 75nm/1400nm, 60nm/610nm and 30nm/720nm.
Figure 5.12 Average friction coefficients for test structures with width/height configurations of 90nm/1400nm, 75nm/1400nm, 60nm/610nm and 30nm/720nm
Figure 5.13 Typical load-displacement curve for the SiNLs of 60 nm/ 610 nm configuration. The critical load was $62~\mu N$, and corresponding friction coefficient was 0.043
Figure 5.14 Typical load-displacement curve for $30\text{nm}/720\text{nm}$ SiNLs. The critical load is $23.7\mu\text{N}$, and corresponding friction coefficient is 0.04293
Figure 5.15 Typical load-displacement curves for 75nm/1400nm test structures with or without coating layers: blue curve for bare SiNLs with the highest critical load, red curve for SiNLs with oxide and green curve for SiNLs with chromium layer
Figure 5.16 Comparison of the friction coefficients of SiNLs with different line widths and coatings
Figure 5.17 Load function of multi-cycle loading indentation. Four cycles were designed with the same maximum loading forces for each loading cycle at 150 μN. The loading and unloading rates were also designed constant for each cycle at 75μN/second and -75μN/second, respectively
Figure 5.18 Load-displacement curves of 90nm SiNLs under multi-cycle loading. The load function was defined in Figure 5.17 with four total loading cycles and maximum loading forces of 150μN for all cycles
Figure 5.19 Friction coefficients on 90nm SiNLs after two runs of 4-cycle loading indentation on the same location. Data points in blue were generated by the first 4-cycle loading and the pink data points were generate by the second 4-cycle loading. The same load function shown in Figure 5.17 was used for both runs of 4-cycle loading indentation.
Figure 5.20 Load-displacement curves for 60nm SiNLs with coatings under 4-cycle loading indentations. The critical loads of the second cycle clearly dropped from that of the first cycle. The decrease of critical load after the first cycle was more significant for bare SiNLs as shown in a), than that of SiNLs coated with silicon dioxide shown in b) and chromium shown in c). Load function shown in Figure 5.17 was used for all experiments.

Chapter 1: Introduction

With the miniaturization of semi-conductor devices into the tens of nano-meter scale, nanotechnology and nano-materials have been widely used in Nano-Electro-Mechanical systems (NEMS)[1-3], and have a significant impact on our daily life. Various applications include drug delivery, biomedicine field, chemical catalysis, solar cell systems, spintronics, ultra large-scale integrated (ULSI) circuits, etc[4-6]. For example, recently an Indian drug firm, Dabur Pharma, announced a new anti-cancer drug delivery system, which is a nano-particle based system with feature size down to a few nanometers[7]. The system allows for a more targeted treatment and avoids the unsafe and unpleasant side effects of chemotherapy. Another example is in the biomedical field. Nanopore technology can be applied to the analysis of nucleic acids converting nucleotides directly into electronic signatures. This can be employed in tissue engineering and lab-on-chip system to diagnose diseases[8]. In addition, due to the intrinsic large surface area to volume ratio of nano-structures, platinum nanoparticles are being considered as the next generation automotive catalytic converters, suggesting a great potential of their application in chemical catalysis[9]. For industrial applications, as CMOS technology is entering into the 32 nm node in 2009, nanotechnology, particularly the immersion lithography and the related patterning process[10, 11], will be of critical importance for the performance of devices. Figure 1.1 shows an application of nanowires in a nanoelectronic device[11].

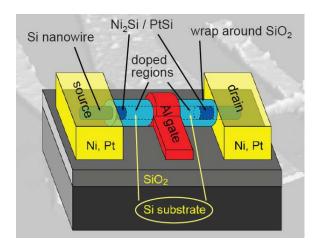


Figure 1.1 Application of silicon nanowires in a dual-gate NWFET with Silicided contact [11].

Silicon-based nanostructures are essential building blocks for nanoelectronic devices and NEMS[1-3]. During operation of nano-devices, the nano-structures are always subjected to external forces, which can enable or degrade the function of the devices. Hence, the mechanical properties of the nanostructures play an important role in controlling the functionality and reliability of the nano-devices [12-15]. However, mechanical characterization at nanoscale remains challenging for properties such as yield strength, fracture strength, contact and friction properties, which are often distinctly different at the nanoscale from their bulk properties. Thus, the investigation of the material properties of silicon-based structures at the nano-metric scale is important for both scientific understanding and practical applications.

Fabrication and the corresponding characterization metrologies of the siliconbased nano-structures are of great challenge[16]. The effort to understand the behavior of highly constrained materials (size effect) at the nanoscale has gained a lot of interests recently, particularly for feature sizes in the range of tens of nanometer[17]. In order to investigate mechanical properties of nano-structures, fabrication of well-controlled nanostructures is one of the major fields of the current research work. For mechanical characterization, Nanomechanic experiments are devoted to studying fundamental mechanical properties of physical systems at the nanoscale, such as the strain to failure, friction properties, etc[18, 19].

In this thesis work, the scaling effect on mechanical and physical properties of silicon nanolines (SiNLs) will be investigated. The mechanical responses, especially the buckling behavior and nanofriction of SiNLs[17, 20], were studied by a nanoindentation technology. For this study, we have developed an E-beam lithography and anisotropic etching process that enabled us to produce SiNLs with a width as small as 25nm and with vertical sidewalls almost atomically smooth. Using these structures, we are able to study the deformation behavior of SiNLs and to measure the contact friction as a function of materials and nanoscale dimensions. The results from this study revealed distinct deformation behavior including an elastic range approaching the theoretical limit of Si crystals and interesting buckling behaviors under nano-indentation. The thesis includes three major parts: a). fabrication process developed for the formation of well-controlled SiNLs; b). characterization of mechanical properties of silicon nanolines (SiNLs) based on the buckling behavior; and c), the nanofriction of the SiNLs.

In this introductory chapter, we will discuss the challenges of fabricating and characterizing nano-structures, objectives and a literature survey on contact mechanics and friction at the nano-scale, respectively. This chapter concludes with an overview of the dissertation.

1.1 Challenges of Fabrication and Characterization of Nano-structures

In order to investigate the mechanical and electrical properties of nano-structures, it is necessary to fabricate good quality nanostructures with controlled microstructure and geometry. Fabrication of well-controlled silicon-based nanostructures is a significant challenge[17, 19, 21, 22]. Generally, there are two approaches to creating small scale nano-structures: bottom-up or top-down.

The first approach employs a bottom-up synthesis method, in which single crystalline nano-structures are formed through two fundamental steps: nucleation and growth by well-defined chemical or physical synthesis processes. For example, in the past decade, a vapor-liquid-solid (VLS)[21] process and metal-catalyzed chemical vapor deposition (MCCVD)[23] were successfully developed to grow single crystalline silicon nanowires with a diameter of ~ 10-100 nm[24]. Figure 1.2 shows two scanning electron microscope (SEM) images of SiNWs grown by the bottom-up approach. The feature size of the obtained nanowires can be as small as 10 nm, which was not restricted by the resolution of conventional lithography tools. However, it was difficult to precisely control the nanowire dimensions, and to form test structures with proper orientations by this fabrication process. Moreover, the placement of the nanowires for measurements can be very challenging.

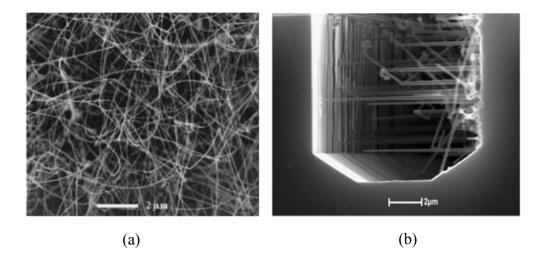


Figure 1.2 (a) Plan view SEM image of SiNWs formed by VLS process [21]. (b) Cross-sectional SEM image of lateral epitaxial SiNWs grown between microtrench by MCCVD process [22].

In the top-down approach, nano-structures are first patterned and then transferred into the bulk or film materials. Typically the pattern is formed by nano-lithography processes, e.g. E-beam lithography (EBL)[25], superlattice nanowire pattern transfer (SNAP)[26], nanoimprinting (NIL)[27], etc. The pattern is then transferred to the substrate by wet etching or dry etching processes[28]. Sub-40 nm silicon nano-structures have been successfully formed by pattern transfer into a Si substrate by reactive ion etching (RIE) processes. But the quality of the small structures is subjected to plasma damage. This can significantly affect the sidewall roughness or the uniformity of nanostructures. Another pattern transfer technique is anisotropic wet etching (AWE). It has been used to fabricate silicon nanostructures to yield vertical and smooth sidewalls without ion-bombardment and plasma induced defects[29, 30]. So far the feature size of structures processed by this method has been limited by two factors: the lithography process (e.g. optical lithography or field enhanced anodization technique), and the stringent requirement for orientation alignment under small dimensions in AWE[30].

Figure 1.3 shows two SEM images. In Figure 1.3(a), a set of 12 nm wide lines were fabricated by RIE, where line edge roughness was due to plasma damage. In Figure 1.3(b) some wide silicon lines were made by AWE, showing vertical and smooth sidewalls.

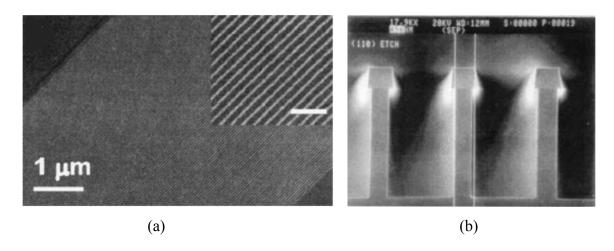


Figure 1.3 (a) 12 nm wide SiNWs generated by SNAP process. Pattern was transferred into silicon using CF_4+O_2 plasma etching, showing line roughness due to ion bombardment. The scale bar in the inset is 150 nm. (b) SEM image of feature cross-sections of silicon lines after KOH wet etching on (110) Si wafer. The silicon nitride hard-mask caps had not been removed[31].

One objective of this study is to develop a new fabrication process to further reduce the feature dimensions and to form well-controlled nano-structures. This process is based on a combination of high resolution EBL and high quality pattern transfer by AWE. The combination of these two techniques enabled us to obtain vertical and smooth single-crystal SiNLs on (110) orientated Si. This fabrication process has yielded SiNLs with potential applications for nanograting-based sensors[19] and interconnects[28]. They are also well-suited for quantitative studies of mechanical and electrical properties of silicon-based structures at the nanometer scale and are used in this thesis research.

1.2 Mechanical Characterization of Nano-structures

The scaling effect on mechanical properties is readily observed and is generally attributed to a change in the properties due to the small dimension of internal structure or in the overall sample size. Well-known examples are the improvement of the yield strength of metallic alloys through refinement of the grain size[32] and fine whiskers. For nano-structures, with dimension approaching micro- or nano-meter ranges, the sample size is expected to become an important factor for controlling their mechanical strength. Previously, single-crystal silicon (Si) beams with widths from 200 nm to 800 nm have been fabricated by field-enhanced anodization using an atomic force microscope (AFM) [33, 34]. Mechanical characterization of these Si beams by AFM bending tests showed a strong size effect on bending strength, which was defined to be the maximum tensile stress in a specimen subjected to bending up to fracture, but no size effect on Young's modulus was observed. The reported bending strength was in the range of 11 GPa to 18 GPa, significantly higher than the average strengths for microscale Si beams (4 GPa) and millimeter scale Si beams (around 500 MPa)[33].

A typical AFM based bending test has been performed by Cheng-Lun Hsin et al[35]. The mechanical response of silicon nanowires (SiNW) was analyzed under buckling and bending conditions. The single crystalline SiNW were prepared by chemical vapor deposition yielding a structure with the diameter in the range of 40-90nm and covered by a 5nm layer of native oxide on the outside. A scanning electron microscope was used to *in-situ* monitor the deflection of SiNW and to measure the force. Figure 1.4 shows the schematic of Hsin's experimental setup, before and after the operation. It was found that Hooke's law is valid over a large-displacement regime. The SiNW was found

to be able to sustain a critical strain of 1.5%, which was much larger than the 0.2%-0.5% of its bulk. The elastic modulus of the NW was determined to be 175–200 GPa, based on analysis of the force vs. displacement curves. The study indicates the superior mechanical properties of SiNWs, including the ultrahigh flexibility and the toughness.

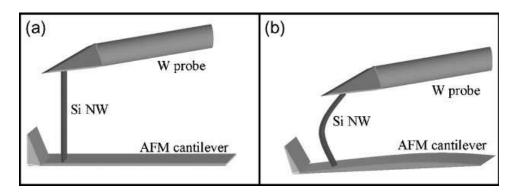


Figure 1.4 Schematic of experiments setup, a) before and b) after the manipulation[35].

In addition to the AFM bending tests, nanoindentation is a commonly used technique for material characterization of nano-structures. The nanoindentation technique is well established for measurements of elastic modulus, hardness, and fracture toughness of both bulk and thin film materials[36, 37]. The precision in both force and displacement measurements, together with easy sample preparation, have led to recent applications of this technique for the mechanical characterization of various nanomaterials. Figure 1.5 shows a typical nanoindentation study of the shell buckling behavior of hollow nanocolumns. Buckling modes of the nanocolumn were shown in Figure 1.5. A buckling strain of 7.4% was reported for an individual hollow gallium nitride nanocolumn. The Young's modulus of the nanocolumn structures was found to be close to that of bulk materials. Nanoscale mechanical behavior of individual semiconducting SnO₂ and ZnO

nanobelts have also been investigated by Mao et. al. [18]. The nanobelt is a quasi one-dimensional solid nanostructure with rectangular cross-section. This study shows the feasibility of nanoindentation technique on the study of patterned one-dimensional structures. For the nanoindentation studies, interpretation and analysis of the result is nontrivial and often requires sophisticated modeling[38, 39].

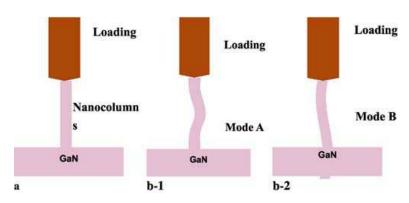


Figure 1.5 Schematic of nanoindentation experiments on hollow column at deferent stages of the indentation process and different possible buckling modes[40].

In this thesis, the nanoindentation technique and numerical simulations by finite element methods (FEM) are employed to characterize the buckling behavior of the SiNLs. We will report results on elastic modulus, strain to fracture and contact friction properties for SiNLs.

1.3 Nanofriction of SiNLs

Owing to the large surface to volume ratio, friction at contact is of fundamental importance for reliability of micro/nano systems, such as NEMS devices and high-density hard-disk drives[2, 4]. A transition of frictional shear strength has been reported, showing a decrease of about one order of magnitude as the contact radius shrank into the nanoscale range[41]. This indicated a size effect on the contact friction properties.

Friction of nanostructures is of great importance for various nano-devices. Generally, the scale of the device and the very large surface-area-to-volume ratio at the nanometer scale influences the friction and adhesion properties at the contact[41, 42]. The degradation of such properties can cause serious performance and reliability problems for nano-devices. Therefore, there is an inherent need to understand the friction phenomenon at nanoscales.

There are two major theories of friction, the classical Amontons and Coulomb's [43] laws of friction and the Bowden-Tabor Theory [44]. The classical Amontons and Coulomb's laws of friction can be expressed as

$$F = \mu N. \tag{1.1}$$

These laws can be summarized as

- 1. The force of friction is directly proportional to the applied normal load (Amontons 1st law); the coefficient is called the friction coefficient;
- 2. The force of friction is independent of the apparent area of contact (Amontons 2nd law);
- 3. The friction is independent of the sliding velocity (Coulomb's law).

These three laws have been verified by empirical observations for many years and are still being applied to many engineering problems today. However, there are examples where these laws do not apply. One example is that geckos are able to climb up vertical surfaces[45]. This fact apparently contradicts Coulomb's laws, where the nominal normal force is zero therefore the frictional force should be zero. This suggests that other mechanisms such as adhesion have to be taken into consideration in the study of mechanical behavior of contacts. The application of nano-devices requires an

understanding of the friction and contact behavior at the micro- and nanoscale.

Recent studies show that stronger adhesion will result in a larger friction force. New theories that include the frictional adhesion were developed accordingly[42, 45-58]. Bowden and Tabor, based on their work with metal-on-metal sliding, proposed that the friction force can be expressed as:

$$F = \tau A, \tag{1.2}$$

where τ is the frictional shear strength and A is the true contact area. This theory is based on a purely elastic sliding process and the Hertzian contact theory. The true contact area is taken to be a continuum representation of the number of atoms involved in the adhesive or cohesive interactions between two sliding surfaces. Explicitly, the frictional force and the frictional shear stress are independent of the applied load in this theory. However, according to the elasticity theory, the applied load plays an important role in determining the true contact area A. In addition, results from molecular dynamics simulations suggested that frictional shear stress τ is weakly depends on the normal pressure[59, 60]. It was also found that under the condition of the true contact area linearly depending on the applied normal load, the classical Coulomb laws and the Bowden-Tabor theory become the same. In this case, the Bowden-Tabor theory offers a completely different understanding of the fundamental mechanisms of friction and contact mechanics.

The complexity of the Bowden-Tabor theory originates in the fact that the friction coefficient is not an intrinsic physical property. Particularly, at a nano-scale the variation of contact area is determined by local contact details. The friction coefficient and frictional shear stress/contact area in general depend on the specific structure, chemistry

and elastic properties of contacting surfaces, the test environment and conditions, and the contact history.

Because of the complexity to evaluate the frication behavior, it is necessary to design and conduct experiments on well-defined interfaces, especially for investigation at nano-scale. One widely used metrology is the application of a single-asperity contact model, *i.e.* the contact measurement of a probe tip and a flat surface by the scanning probe microscope (SPM). With a well-defined geometry, the SiNLs is a good candidate for the study of contact measurements. The associated contact mechanics will be discussed in Chapter 2. The general models of contact mechanics are based on the Hertzian contact theory. The details of the contact area evaluation as well as the nano-friction study will be discussed in Chapter 5, with the assumption of a single-asperity model.

1.4 Objective and Organization of Dissertation

The purpose of the present work is to study the mechanical response and friction behavior of the Silicon Nanolines (SiNLs) structures by a nanoindentation technique, based on the analysis of the buckling behaviors of SiNLs. The friction coefficients were evaluated based on the classical Amontons using Coulomb's laws of frictions and Finite Element Simulation. For comparison, frictional shear stresses in the Bowden-Tabor theory will be calculated. The area of contacting surfaces between a diamond indenter and SiNLs structures will be evaluated based on the Hertzian contact theory. The impact of contact history on the frictional behavior of SiNLs will be studied by a set of cyclic-loading nanoindentation experiments.

Following this introductory chapter, Chapter 2 will review in the theoretical background of the buckling behaviors of column structures and contact mechanics between a sphere and a flat half-space. In Chapter 3, the experimental techniques, including the fabrication methods developed to fabricate SiNLs test structures and the nanoindentation technique, will be presented. In Chapter 4, the mechanical response of SiNLs under nanoindentation will be described. The loading-displacement indentation curves show that the critical load to induce the buckling of the SiNLs can be correlated to the contact friction of the nano-indenter and the geometry of SiNLs. The mapping of buckling mode selection with the geometry, applied load and friction is developed. Chapter 5 will begin with details of contact area calculations for the SiNLs geometry, which is followed by discussion of the results from experiments and nanofriction model analysis. Finally, in Chapter 6 we will present a summary of the dissertation and some suggestions for future work.

Chapter 2: Contact Mechanics and Compressive Instability of Columns

In this chapter, the first section is an introduction to the contact mechanics for a single asperity contact. Then, it is followed by a discussion about the buckling behavior of column structures.

In the nanoindentation experiment, the contact between the nanoindenter and SiNLs can be approximated as a single asperity contact. In order to evaluate the frictional shear stress, the true contact area has to be determined. In some cases, the contact area can be determined by experimental techniques. For example, with a surface force apparatus (SFA), the contact area can be directly evaluated by interference fringes[61, 62]; and if both materials in contact are electrically conductive, the contact area can be estimated by the variation of electrical current passing through the contact zone[63, 64]. However in AFM or MFT, it is impossible to directly measure the contact area, several methods and models have been developed to evaluate the contact area indirectly[65-67]. These methods and models are based on contact mechanics theories, and the corresponding results are consistent with the experimental data. In the first section, classical contact mechanics will be reviewed; then, contact mechanics theories that include adhesion between contacting surfaces will be discussed.

In the nanoindentation experiments, the indenter imposed vertical forces on SiNLs and a sudden displacement burst was observed during the loading and unloading cycle. Such a displacement burst was characterized as buckling behavior of SiNLs. When

a column structure is subjected to compressive forces, buckling may occur [65]. Buckling is a failure mode where a strut, rod, plate, or column reaches an unstable state under compressive stress and laterally deflects. In the second section of this chapter, SiNL structures were modeled as a column structure with one end fixed and the other end free or pinned. The buckling behaviors of column under such boundary conditions will be analyzed in Section 2.2.

2.1 Contact Mechanics of a Sphere pressed into a Half-space

It is complicated to evaluate the contact areas between surfaces of arbitrary profiles. One of the simplest models is the classical Hertzian contact model between a sphere and half-space. In the Hertzian model, the mating parts are assumed to be elastic and have no adhesive force attraction[66]. When adhesion is considered, the classical Hertzian model has to be modified. The DMT[67], JKR[68], and Maugis[69] models include the effect of adhesive attraction, and cover a wide range of the adhesion spectrum.

In this thesis work, the feature sizes of the test structures, SiNLs, scale down to 30nm and into the regime of nano-contact where the adhesion may play an important role in the nano-devices and nano-materials. Although eventually we will find out that the adhesion is not the key factor to determine buckling behavior of SiNLs, several classic contact mechanics, the Hertzian model, DMT, JKR, and Maugis models, will be reviewed here to give a whole background of the contact mechanics.

2.1.1 Adhesionless Contact Mechanics - Hertzian Model[66]

The geometry of the Hertzian model is shown in Figure 2.1 a) before contact is

made. The spherical punch has a radius of R, which is pressed into the half-space. It is assumed that the punch is rigid, and the half-space is elastic. In reality, the punch and the half-space both possess finite modulus, which can be modeled that the punch is rigid but the half-space has a reduced modulus of,

$$\frac{1}{E_r} = \frac{1 - v_1^2}{E_1} + \frac{1 - v_2^2}{E_2},$$

where E_1 and E_2 are the Young's modulus of the punch and half-space, and v_1 and v_2 are their Poisson ratio, respectively. When the contact zone is small compared to the size of the punch, the shape profile of the punch can be approximated as

$$f(r) = \frac{r^2}{2R},$$

where r is the lateral distance measured from the apex of the punch. When the punch is pushed a distance Δ into the half-space, a contact zone of circular shape with radius a will form. Δ is also called penetration depth. The relation between Δ and a is

$$\Delta = \frac{a^2}{R} \, .$$

The stress distribution inside the contact zone was demonstrated by Hertz to be,

$$p = p_0 (1 - \frac{r^2}{a^2})^{1/2},$$

where p_0 is the maximum stress at the center of the contact zone. The total force is calculated by integrating the stress p over the contact area, and found to be

$$F_H(a) = \frac{4E_r a^3}{3R} .$$

Therefore, once given the material properties of the interacting objects and the

penetration depth, one can calculate the area of the contact zone and the total force. In actual experiments, the total force F was measured, and the material properties of the indenter and SiNLs were assumed to be those of bulk materials. Therefore, the contact area can be calculated. However, considering the geometry properties of SiNLs patterns, a more careful calculation is needed and will be discussed in Chapter 5.

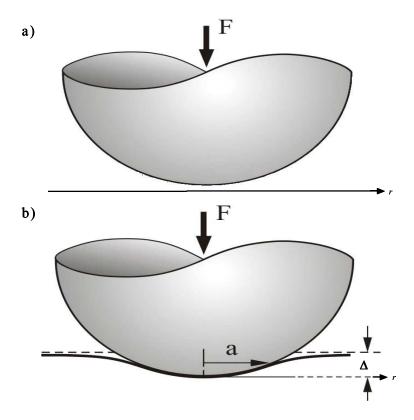


Figure 2.1 Geometry of the Hertzian model a) before contact, and b) after contact.

2.1.2 Adhesive Contact Mechanics

The effect of adhesion on the contact mechanics of a simple model will be discussed at first. When adhesive energy between the contacting surfaces is considered, the total energy of the system is the sum of the adhesive energy and the elastic energy which is stored in the punch due to the elastic deformation. By assuming the elastic

energy only exists inside the contact zone, and denoting the elastic energy as $\varepsilon_H(\Delta)$ and the adhesive energy per unit area as ω , the total energy would be

$$\varepsilon(\Delta) = \varepsilon_H(\Delta) + \omega A,$$

where A is the area of the contact zone. The total force is calculated as

$$F = \frac{d\varepsilon}{d\Delta} = \frac{d\varepsilon_H}{d\Delta} + \omega \frac{dA}{d\Delta} .$$

The first term is the Hertzian force and the second term is the adhesive force, which can be calculated in this simple model to be $-\pi R \varpi$. Therefore the effect of adhesion is an offset of the Hertzian force by a constant $-\pi R \varpi$.

More complicated models consider the material properties and the nature of adhesion[45, 56, 70-73]. One famous model is the DMT model developed by Derjaguin and coworkers. Another famous model called JKR was developed by Johnson et. al. In these two theories, the contact problem is modeled in two different elastic regimes.

The DMT model assumes that the elastic deformation occurs inside the contact zone, and the Hertzian stress distribution and penetration fields only apply inside the contact zone as well. However the adhesive interaction only applies outside of the contact zone, as shown in Figure 2.2. The model gives an offset of the Hertzian force by a constant of $-2\pi R\varpi$, instead of $-\pi R\varpi$ which is given by the simple estimation of the previous model. The DMT model is a good approximation for cases where the adhesive interactions are weak, and the elastic stress inside the contact zone are very strong compared to stresses due to adhesion. For most solid-solid contacts, this model applies.

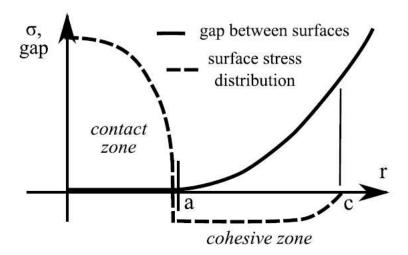


Figure 2.2 Geometry of the DMT adhesive contact. The attractive interactions act outside the contact zone.

The JKR model assumes that adhesive forces act both inside and outside the contact zone. The existence of the adhesive forces inside the contact zone causes the formation of a "necking" effect on the punch, which is shown in Figure 2.3 a). The "necking" will introduce additional deformation of the punch and therefore changes the area of contact or the penetration depth if the applied force is kept constant as shown in b). This model give the Hertzian forces an offset of $-\frac{3}{2}\pi R\omega$, compared to $-2\pi R\omega$ for the DMT model. The JKR model, as shown in Figure 2.3 a), requires significant local deformation of the punch to develop by the adhesive forces. This applies to cases where the punch is compliant and the elastic interaction inside the contact zone is comparable to the stress induced by adhesion. For example, in the case of rubber-rubber interaction, the JKR model is better suited than the DMT model.

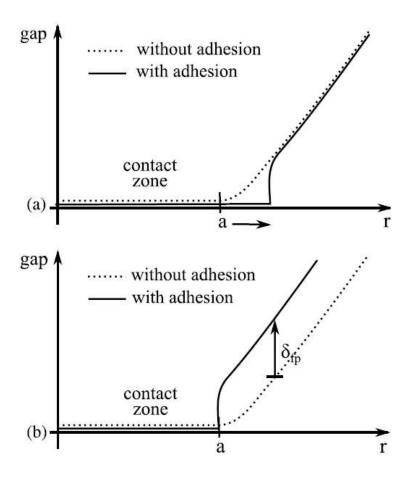


Figure 2.3 Schematic illustration of JKR adhesive contact. The existing of adhesive forces changes the area of the contact zone which is shown by the formation of "necking" in a) outside of the contact zone denoted by dashed curve. In order to keep the area of contact zone constant under this case, a negative force is need to "pull out" the punch a little which is shown in b).

However, the DMT and JKR models together do not cover all cases. There are cases where the adhesive interactions are in an intermediate range, and the adhesion induced deformation is comparable to the punch displacement. The adhesive forces contribute to the deformation of the punch by an extent that is not fully in the JKR regime. The interactions have to be considered both inside and outside of the contact zone. One method is a superposition of JKR and DMT terms for the penetration depth and forces,

$$\Delta(a) = \Delta_H(a) + \Delta_{JKR}$$

$$F(a) = F_H(a) + F_{JKR}(a) + F_{DMT}(a)$$

where Δ_{JKR} is the offset of penetration depth by the JKR model, and F_{JKR} and F_{DMT} are the offset of forces by JKR and DMT models, respectively. The F_{JKR} and F_{DMT} can not be simply evaluated by the JKR or DMT model, and elaborate calculations are needed. Maugis developed a quasi-analytical method that is now generally called the Maugis model to circumvent the difficulties[69]. The calculation is complicated but, as expected, this model gives an offset of the Hertzian forces by $-n\pi R\varpi$, where 1.5 < n < 2.

For each model, the penetration depth and contact radius can also be calculated if the adhesive energy is measured or calculated. This gives us the capabilities to calculate the area of the contact which is important to evaluate frictional shear stresses. It is noted that these three models cover a large spectrum of adhesive interactions. An important problem is the selection of an appropriate model under specific experimental condition. Tabor first defined a non-dimensional parameter [74],

$$\mu_T = (\frac{16R\omega}{9K^2z_0^3})^{1/3},$$

where K is the effective modulus and $K = \frac{4}{3}E_r$, z_0 is the interatomic equilibrium distance in a Lennard-Jones potential. This parameter was used to characterize the adhesion spectrum and determine which model, DMT, JKR, or Maugis, is appropriate. The Tabor parameter is defined by the ratio of the penetration depth versus the decay length of the adhesive interactions. The parameter measures the impact of the interaction stresses on the deformation of the punch. There are some variations of this parameter

when the existence of moisture interlayer and capillary forces are considered, however the selection of models generally falls within the following rule,

 $\mu_T > 5$, JKR model $\mu_T < 0.1$ DMT model . $0.1 < \mu_T < 5$ Maugis model

When the deformation due to adhesion is small and the interaction has long range forces, the value of the parameter is small, and the DMT model is a good choice. DMT normally works well for solid-solid interactions with small adhesion and small punch compliance. On the other hand, if the deformation is large due to adhesion with a short range interaction force, the JKR model is better.

2.2 Compressive Instability of Columns

In this section, the fundamental of buckling mechanics will be reviewed. Although all three cases reviewed below are classic cases with simple boundary conditions, they provide a good starting point to understand the buckling behaviors and the conditions that determine buckling modes. Specific boundary conditions and more complicated cases related to the SiNLs nanoindentation experiments will be discussed in Chapter 4 and Chapter 5.

When an elastic beam or column structure is subjected to a compressive load, the structure undergoes elastic response. But as the compressive load further increases to some critical load, the column becomes unable to support the load and reaches an unstable state[65, 75]. At the critical load, any other transverse force, no matter how small it is, can cause the deflection of the structure to mathematically reach infinity. Such

an elastic instability under a compressive load is called buckling. There are several other common types of elastic instability such as lateral buckling. Reviewed here is the compressive instability of beam-column structures, which will be applied to simulate the SiNLs structures in Chapter 4.

The basic differential equation of a beam-column deformation is

$$EI\frac{d^4x}{dz^4} + F\frac{d^2x}{dz^2} = Q,$$
 (2.2.1)

where x(z) is the deflection of the beam-column at any position z, E is the Young's Modulus and I is the second moment of inertia of the beam's cross section, Q(x) is the transverse load acting on the beam, and F is the applied load. When Q(x) is negligible, the beam-column structure becomes a column structure.

Three common cases are considered as shown in Figure 2.4. Case one, both ends of the beam-column are fixed, for which the boundary conditions are

$$x(0) = x'(0) = x(h) = x'(h) = 0 (2.2.2)$$

where x(0)=0 indicates that the deflection is zero, and x'(0)=0 indicates that the slope is zero.

Case two, one end (z=0) is fixed, and the other end (z=h) is hinged and allowed to rotate. The corresponding boundary conditions are

$$x(0) = x'(0) = x(h) = x''(h) = 0 (2.2.3)$$

where x''(h)=0 indicates the moment at the end is zero.

Case three, both ends of the beam-column are hinged and allowed to rotate. The boundary conditions are

$$x(0) = x''(0) = x(h) = x''(h) = 0 (2.2.4)$$

The general solution of equation 2.2.1 is

$$x(z) = A\cos kz + B\sin kz + Cz + D + \frac{Q}{2F}z^{2},$$

where k satisfies $k^2 = \frac{F}{EI}$.

Considering the boundary conditions of Case one as expressed in equation 2.2.2, the solution for the deflection of the beam gives

$$x(z) = ((z-h)kz + h(\cos kz - 1)\cot(\frac{kh}{2}) + h\sin kz)\frac{Q}{2kF}.$$

As mentioned previously, at the critical load, the deflection of the beam reaches infinite mathematically, which indicates that $\cot(\frac{kh}{2}) = \infty$, and kh satisfies $kh = 2n\pi$ with n=1, 2, 3.... Recall that k is defined as $k^2 = \frac{F}{EI}$, and the critical load is determined by setting n=1, therefore the buckling occurs at $F_{cr} = \frac{4\pi^2 EI}{h^2}$.

Similarly, Case two gives the solution of deflection,

$$x(z) = \frac{2k(h-z) + kz(2 + (h-z)k^2h)\cos kh - k^2(h^2 - z^2)\sin kh + (2 + k^2h^2)\sin k(h-z) + 2\sin kz - 2kh\cos kz}{kh\cos kh - \sin kh} \frac{Q}{2k^2F}$$

and the critical load can be found by solving $kh\cos kh - \sin kh = 0$, that is $\tanh = kh$ which can be solved numerically to be kh = 4.493, and critical load $F_{cr} = \frac{4.493^2 EI}{h^2}$.

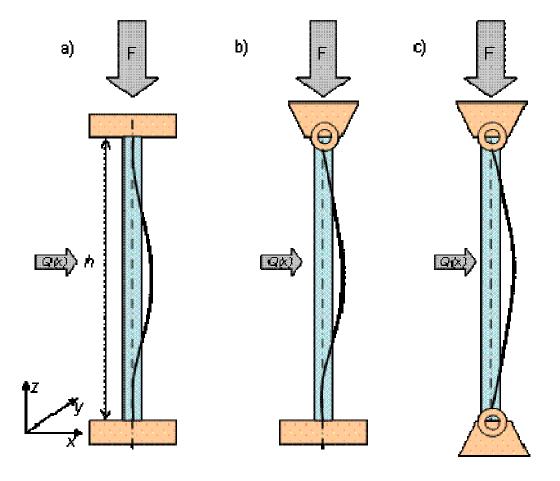


Figure 2.4 Beam-column structures with axial and transverse load. a) with both ends fixed; b) with one end fixed and the other end hinged; c) with both ends hinged.

For Case three, where both ends of the beam-column are hinged, the deflection can be found from equations 2.2.1 and 2.2.4,

$$x(z) = \left(\frac{k^2 z (h - z)}{4} - \frac{\sin \frac{kz}{2}}{\cos \frac{kh}{2}} \sin \frac{k(h - z)}{2}\right) \frac{Q}{k^2 F}.$$

From $\cos \frac{kh}{2} = 0$, $kh = (2n+1)\pi$, and the critical load is found to be $F_{cr} = \frac{\pi^2 EI}{h^2}$.

In the experiments, SiNLs was simulated as a column structure with the bottom end fixed but the top end hinged or free, depending on the buckling modes. When the top end is free, the analysis is analogous to Case three with its height being assigned in half. More details on the buckling behaviors of SiNLs will be presented in Chapter 4. The solution of buckling response under eccentric loading condition will also be discussed in Chapter 4.

Chapter 3: Experimental Techniques

In this chapter, a fabrication process was developed to prepare nanoindentation test structures. The SiNL test structures were fabricated on a single crystalline [110] silicon wafer. To achieve test structures with well-controlled micro-structure and geometry at nanoscale, anisotropic wet etching (AWE) was employed for pattern formation. Other major fabrication techniques involved were electron-beam lithography, reactive plasma etching, and chemical etching. Generally, patterns were formed by the electron-beam lithography (EBL). EBL has the capability to generate patterns with feature sizes down to tens of nanometers. Then patterns are transferred into the silicon substrate by selective etching process, *i. e.* reactive ion etching (RIE) or AWE.

3.1 Fabrication of SiNL Test Structures

For mechanical characterization at nano-scale, it is of critical importance to form well-control test structures, *i.e.* uniform feature size, smooth sidewalls, etc. In this section, the fabrication process to obtain single crystalline silicon nano-line structures, having nearly atomic flat sidewalls and uniform linewidths, will be introduced. The general fabrication process flow will be briefly reviewed, followed by a detailed introduction to some key process steps and challenges. The quality of the fabricated SiNLs will be discussed, based on SEM images of them.

The fabrication process began with a chromium coating by an e-beam evaporator on (110) silicon wafers already having an oxide layer deposited on their upper surfaces by low pressure chemical vapor deposition (LPCVD). After chromium evaporation, a

positive-tone resist was spun on the wafer. The resist was imaged on an electron-beam exposure system operating at 50 kV. Pattern transfer from the resist to chromium lines was performed by reactive plasma etching (RIE) through the oxide layer down to the silicon surface using the chromium lines as the etch mask. Subsequently, the residual resist was removed and tetra-methyl-ammonium hydroxide (TMAH) was used for anisotropic wet etching (AWE) of silicon along the (111) planes. Finally, chromium and oxide hard masks were removed by chromium etchant and buffered oxide etchant dip.

In Section 3.1.1 the EBL process will be introduced. The RIE and some details of the associated pattern transfer will be further introduced in section 3.1.2. The AWE technique, which is the critical process for pattern transferring into silicon wafers, will be discussed in detail on section 3.1.3. Section 3.1.4 is about the integration of the fabrication process and the corresponding challenges.

3.1.1 Electron Beam Lithography Technique

Electron beam lithography (EBL) is one of the premier techniques for defining structures with nanometer dimensions [76]. The electron beam has much shorter wavelength compared with that of the conventional optical lithography techniques, which gives the capability to overcome the diffraction limit of light. The electron beam also changes the properties of the resist, which makes the resist either more soluble or less soluble after the resist is exposed to the electron beam. Positive resist will be more soluble after being subjected to electron beam exposure and the exposed materials will be removed by the developer. While negative resist will be less soluble after electron beam exposure and the un-exposed materials will be removed.

There are a few advantages of using EBL technique in the study. First, EBL provides the flexibility of a design change and does not require a mask like a conventional optical lithography. Second, much better dimension resolution is achievable by EBL, which enables nano-structures to be fabricated with feature sizes as small as 20 nm. EBL writing is a serial process that requires much longer writing time than conventional optical lithography, but it is not a significant issue in the experiments, since massive productivity is not an important issue in a laboratory research. EBL writing is widely used in the industry for mask writing due to its flexibility of design change.

In the EBL exposure, the selection of wafer stack is important. A typical layer stack for the experiments is shown in Figure 3.1. First, a piece of silicon wafer was prepared with a 15nm thick of chromium deposited on top of a 25nm thick layer of SiO2. Then, a positive EBL resist layer was spin-coated on top. The thickness of the EBL resist was around 145nm. The purpose of a SiO2 layer was to serve as a hard mask for the pattern transfer, and prevent formation of silicide layer between chromium and silicon. The chromium layer is conductive and was used to change the charging nature of the substrate during EBL exposure. Without a conductive layer, an insulating substrate surface will charge up during an EBL exposure and may cause the distortion of the patterns. Even on semiconductor substrate, the conductive layer will help distribute electron charging. Another advantage of the chromium layer is the high selectivity during the pattern transfer where a chromium layer serves as a hard mask layer to transfer patterns into oxide layer.

The thickness of the EBL resist layer is important. A thinner resist layer is desired to achieve ultra-fine nano-structures. However, EBL resist layer serves as a mask layer for the pattern transfer, from EBL resist layer into the chromium layer. An EBL resist layer must have sufficient thickness to protect patterns during RIE etching. An EBL resist film of 145nm was used to achieve patterns with feature sizes less than 100nm and transfer them into a chromium layer of 15nm.

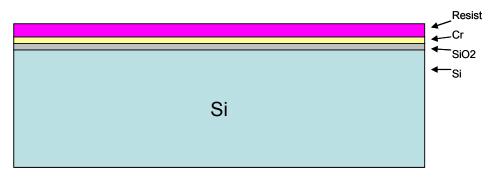


Figure 3.1 Layer stack of EBL substrate.

The EBL writer was a JEOL JBX6000 system at The University of Texas at Austin, Microelectronic Research Center. The EBL resist used was ZEP-520a, which was diluted by a solvent ZEP-A with a ratio of 1:1. With a spin-coating speed of 3500rpm for 60 seconds, an EBL resist film with thickness of 145nm was obtained. Then, the resist was baked at 180°C for 120 seconds. Afterwards, the EBL resist was exposed to a 50KeV electron beam with an appropriate dosage, before the substrate was immersed into the developer (Zed-N50) for 90 seconds to remove the exposed materials. Finally the substrate was rinsed in IPA for 50 seconds to remove residues.

A series of dosage tests were performed, which was necessary due to the following reasons. First, an appropriate dosage level is critical in EBL writing, because the feature size is directly affected by the exposure dosage. Second, the EBL system

condition may change after a period of time. Third, the required dosage level may be different to achieve the same patterns if the substrate is changed. For example, the thickness difference in the conductive layer (chromium in the current experiments) may cause different feature sizes of the final patterns. Normally, an over-dosed exposure will cause an over-exposure of the patterns, which means more materials on the line areas of the patterns are exposed. As a result, over-dosed exposure will increase the width of a trench if positive-tone EBL resist is used.

In the experiments, positive-tone resist was used, and the test structures were defined by un-exposed material as shown in Figure 3.2. Based on the description in the last paragraph, an over-dosed exposure was desired to effectively decrease the feature sizes of SiNL structures as demonstrated in Figure 3.2. An over-dose exposure will effectively reduce the line width of SiNLs structures.

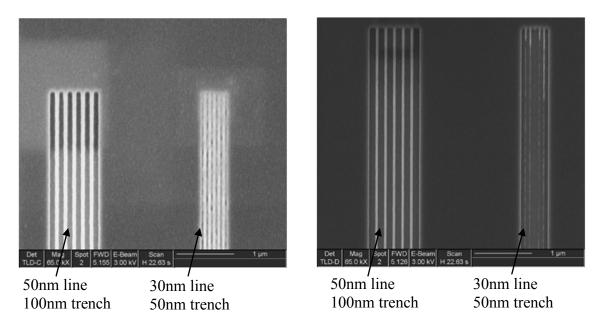


Figure 3.2 The effect of dosage levels on the line width of SiNLs. Left, under-dosed exposure leaving more materials unremoved in the trench area (dark), and resulted in larger line width (brighter). Right, over-dosed exposure removed more materials from the trench area, and SiNLs structures with smaller line width were obtained.

3.1.2 RIE and Pattern Transfer Process

After EBL exposure and subsequent developing processes, the designed patterns were formed on the resist layer. The next task was to transfer patterns into the layers below the EBL resist in the stack on silicon substrate. The patterns were first transferred into the chromium layer then into the silicon dioxide layer, as shown in Figure 3.1. The pattern transfer was done by two steps of reactive ion etching (RIE), and then followed by anisotropic wet etching (AWE). The RIE process is further discussed below, and the AWE process in section 3.1.3.

RIE is a common technique in the semiconductor industry and research labs. Neutral or charged particles are generated by plasma in the RIE chamber [77]. Particles that bombard with the substrate will either chemically react with the substrate materials or physically liberate the substrate atoms. Typical reaction gases to generate a plasma include oxygen, fluorine-based gases (such as CF₄ or CHF₃), and chlorine and bromine based gases (such as Cl₂ or HBr). The selection of reaction gases depends on their etching rate and selectivity, as well as on the feature sizes of the structures and composition of the substrate materials. Other parameters of importance for the selection of reaction gases include the power and design of the plasma chamber. All the factors mentioned can have an effect on developing an etching recipe. For example, O₂ plasma is normally chosen for ashing or cleaning of the organic contaminants since it has good etching rate and selectivity on polymers.

The etching recipes used in the processes are summarized next. According to the layer stack of the EBL substrate shown in Figure 3.1, as a first step, the pattern written by

EBL was transferred into the chromium layer. The EBL resist served as the etching mask in this step. A good etching recipe for this step is characterized by an enough etching rate on chromium, while the etching rate on EBL resist is small enough that the EBL resist can survive this step. Such a recipe had been developed using the reaction gases of Cl₂ and O₂ with a flow rate of 9.7sccm and 2.25sccm, respectively. The base pressure was set to be 80mTorr and the RF power to be 75W. The etching rate for chromium was 15nm/minute, and 50nm/minute for EBL resist. Normally, the thickness of the mask layer has to ensure a 100% over-etching of the chromium layer; therefore, at least 100nm of thickness for the EBL resist was required. As mentioned before, the spin-coated EBL resist thickness was about 145nm. The second etching step was to transfer patterns into the silicon dioxide layer where chromium layer served as the hard mask. One of two etching recipes was chosen in this etching step: one recipe with CF₄+O₂ and the other recipe with CHF₃+O₂ reaction gases. Normally, at least 100% over-etching was desired at this step to make sure there was no oxide residue in the trench area.

3.1.3 Anisotropic Wet Etching (AWE) Process

Wet etching is a simple etching technique where the material dissolves when immersed into a chemical solution. To generate patterns and structures of interest, an etching mask is required to selectively etch the material. The mask material must have a much lower etching rate compared to the material to be etched. Either silicon dioxide or chromium is a good mask material for the AWE etching of silicon in TMAH solutions. Some materials, such as silicon, exhibit anisotropic etching properties in certain etchants [30, 31, 78]. For example, silicon has a different etching rate in different crystalline

directions in TMAH and KOH solutions. The etching rate for the silicon (110) plane is $0.532\mu m/min$, while it is only $0.009\mu m/min$ for the silicon (111) plane in the 70°C 25% TMAH solution. The anisotropic etching results in shaped holes with flat sidewalls, while the isotropic etching results in rounded holes, as shown in Figure 3.3.

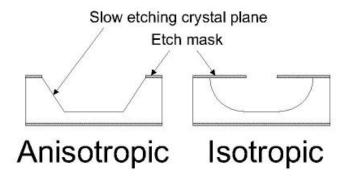


Figure 3.3 Difference between anisotropic etching and isotropic etching.

By taking advantage of the characteristics of anisotropic etching and carefully designing the masks, unique structures can be fabricated. These arrangements resulted in fabricating the SiNL structures with a rectangular cross-section and nearly atomically flat sidewalls. Compared with the SiNLs obtained by RIE etching, the SiNLs obtained by AWE had a much improved quality. The design of mask structures and the specifics of fabricated SiNLs will be discussed in detail in the next section.

3.1.4 SiNL Structure Design and Fabrication Results

As mentioned in the last section, careful design of the mask structure was needed to obtain the desired SiNL structures. Here, the mask structure was the pattern that was first written by an EBL system and then transferred into the chromium and silicon

dioxide layers. In the design of SiNL structures, the major goals were to obtain structures with vertical sidewalls, nearly atomically flat sidewalls, rectangular cross-sections, and the length up to 30µm, and the width down to 30nm. All the design goals could be fulfilled by aligning the trenches along the <112> crystalline direction of a {110} silicon wafer, as shown in the schematic in Figure 3.4 a). The line structures were defined by a series of closely placed trench structures. When the material in the trench structures was removed by AWE etching, the line structures were formed by the remaining material between the trenches. When a trench was designed and aligned to the <112> direction as shown in Figure 3.4 a), a trench with the flat, vertical sidewalls were obtained after the AWE etching as shown in Figure 3.4 b). Its cross-section is shown in Figure 3.4 c) where the arrows indicate the normal directions of the sidewalls in <111> orientation. When two or more parallel trenches were closely placed, SiNLs structures were formed as shown in Figure 3.4 d).

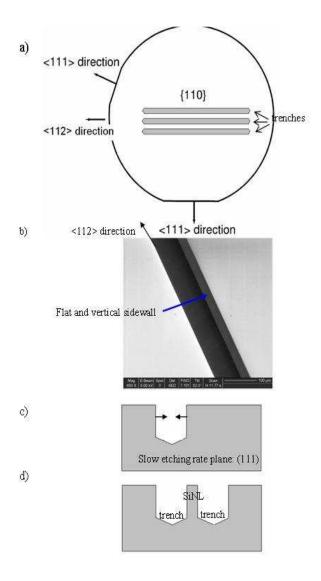


Figure 3.4 a) Schematic of the mask design of SiNLs. b) A trench was formed by AWE. c) Schematic of cross-section of a trench. d) Formation of a SiNL between two trenches.

The key point of the design was to align the sidewalls of SiNLs to the <112> direction of the {110} wafer. This problem was solved by two methods. The first method was to find out the exact crystalline orientation of the silicon wafer. By this method, a set of alignment marks were needed to be generated first, followed by writing a set of orientation test structures. After the orientation test structures were carefully inspected

and the exact crystalline orientation was determined, an EBL alignment was performed and the SiNLs structures were written. Although, by this method, all SiNLs were close to the exact crystalline orientation and the product yield was much higher than the other method, it required much more EBL writing and extra process steps. Therefore, the second method discussed below was adopted for the research work in the laboratory.

In the second method, the fabrication process was simplified by designing a 10 by 10 structure array, which is shown in Figure 3.5 c). On each element of the array, the SiNLs structures had the same orientation as shown in Figure 3.5 a). But there was an orientation change between each element, starting from the lower-left corner at an angle of -0.5° to the upper-right corner at an angle of +0.5°. In order to avoid the stitching effect, the size of each element was 30μm X 30μm, smaller than the field size of the EBL system, and the distance between the nearest neighbors was 160μm which was twice the field size (80μm). This design ensured the writing of each element to be done in a single field.

After all the RIE and pattern transfer steps and the AWE process, the element that had the best orientation alignment to the intrinsic crystalline orientation of silicon wafer was determined by SEM inspection. It is known that misalignment would cause bending, distortion, and even cracking of the SiNL structures. The SiNLs with the best orientation alignment had the best quality. Figure 3.5 b) shows an SEM image of a "good" SiNL structure after the AWE process. Those SiNLs on the elements with the best orientation alignment were selected for the nanoindentation experiments.

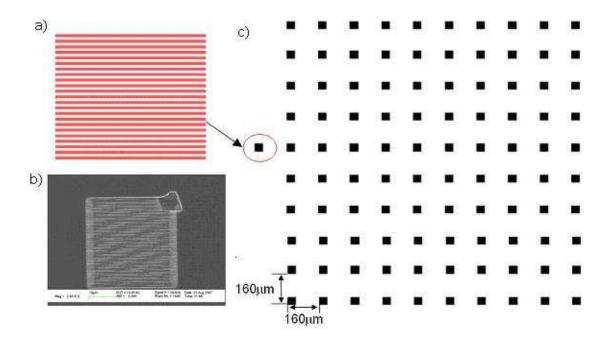


Figure 3.5 The silicon nanoline arrays fabricated by EBL and AWE. a) Grating pattern of an array element; b) SEM image of SiNLs structures after AWE. c) Pattern array for orientation alignment.

The uniformity of the line width may be very good for SiNLs within a single array element. Yet, there are two key parameters dictating the entire SiNLs[79, 80]. One is the line width, the other is the height. The height can be roughly controlled by the AWE etching time and the working temperature of the TMAH/KOH solution. SiNLs structures with a wide range of heights from 300nm to 1.5µm were fabricated. As for the line width, there are two ways to control its dimension. One is the dosage level of EBL exposure. As already mentioned, the dosage level directly determines how much EBL resist is exposed to electrons. The more material exposed, the wider trenches were obtained, therefore the narrower line width of SiNLs. In the EBL exposure process, this was done by repeating the writing of 10 X 10 arrays at different dosage levels. The other

way to control line the width is to control the dimension of the AWE etching mask, as demonstrated in Figure 3.6. The AWE etching mask was the silicon dioxide layer, and the line width of SiNLs was directly determined by the dimension of the silicon dioxide layer. When hydrofluoric acid (HF) was used to selectively etch the silicon dioxide, the critical dimension under the mask changed due to the undercut effect and subsequently decreased the line width of SiNLs. SEM images showing SiNLs structures with different line widths and heights are shown in Figure 3.7.

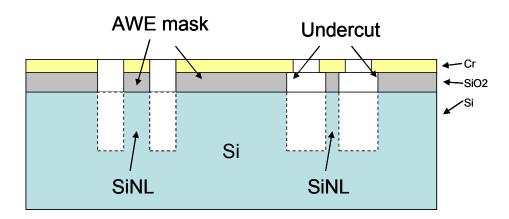


Figure 3.6 Schematic of undercut and line width control.

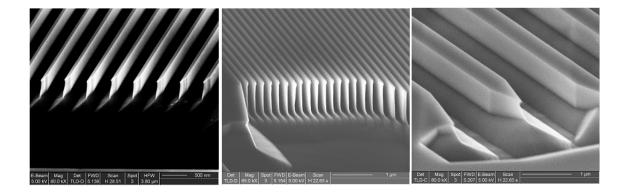


Figure 3.7 Cross-sectional SEM images of some Si nanoline arrays fabricated by EBL+AWE. (a) 30 nm wide lines with height of \sim 350 nm; (b) 65nm wide lines with height of \sim 1 μ m. (c) 1500 nm wide lines with height of \sim 560 nm.

3.1.5 Coating of SiNLs with Silicon Dioxide and Chromium

To study the impact of surface modification on friction, some SiNLs test structures were coated with silicon oxide or chromium layers. For the oxide formation, the fabricated bare SiNLs structures were cleaned by Piranha cleaning (Hydrogen Peroxide: Surlfic Acid=1:2). Then a 3nm layer of thermal silicon dioxide was formed on SiNLs surface by low pressure chemical vapor deposition technique. Since a thin layer of silicon material would be consumed by the growth of silicon oxide, and the growth not only occurred on the top but also on the sidewall of SiNLs. The actual line widths of these structures after oxidation would be slightly smaller than those of bare SiNLs. The effect of oxidation on the mechanical response of SiNLs was taken into account by adjusting the effective line width for FEM simulation and friction coefficient calculations.

After finishing the nanoindentation experiments on SiO_2 coated SiNLs structures, a 2nm layer of chromium was deposited on the SiNLs by the electron-beam evaporation system. The chromium layer was deposited mostly on top of the SiNLs.

3.2 NanoMechanical Testing System

The NanoMechanical Testing System was based on a multi-mode AFM system. Equipped with a 2D-Transducer, this system had both the capabilities of nanoindentation tests and nanoscratching tests. The nanoindentation technique was extensively employed for the study of SiNLs and will be reviewed here.

Compared with other methods such as microbeam cantilever tests or bulge tests, nanoindentation is a more convenient technique, because there is less stringent requirement for sample preparation. Figure 3.8 shows a schematic of the nanoindentation process. First, the sample surface was imaged in conventional AFM mode with a diamond indenter and the positions for the indentation were selected. Then, the loading and unloading process, with the simultaneous force and displacement measurement, was monitored and recorded using a transducer. A second AFM image of the surface may be used to examine the shape of the indent after the indentation. Since the depth resolution was on the order of nanometers, it was possible to indent the thin, low-k films with submicron thickness. Figure 3.9 shows SEM images of three types of indenters. Among these, the Berkovich indenter is the most widely used to extract both elastic modulus and hardness from the force vs. displacement curves.

Oliver and Pharr proposed an analysis method, with which the elastic modulus, E, and hardness, H, can be derived directly from the analysis of the unloading force vs.

displacement curve. The process is shown schematically in Figure 3.10. As the indenter is driven into a thin film, both elastic and plastic deformation occurs. The assumption of this analysis is that after the indenter is withdrawn, only the elastic displacements are recovered. The initial unloading contact stiffness S, which is determined by the slope of the unloading curve, is related to the reduced modulus (E_{Γ}) by:

$$S = \frac{dP}{dh} = \frac{2}{\sqrt{\pi}} E_r \sqrt{A} , \qquad (3.1)$$

where P is the load and h is the indentation displacement. A is the projected contact area, which is a function of displacement and could be deduced by the geometry of the indenter and the displacement h. After acquiring the contact stiffness, S, and the contact area, A, from the unloading curve, the reduced modulus E_r could be calculated from Eqs. 3.1. E_r is directly related to elastic modulus of materials and is given by

$$\frac{1}{E_r} = \frac{1 - v_f^2}{E_f} + \frac{1 - v_i^2}{E_i},\tag{3.2}$$

where E_f and v_f are the elastic modulus and Poisson's ratio for the film, and E_i and v_i are the elastic modulus and Poisson's ratio for the indenter. (For diamond tip, E_i =1141 GPa and v_i =0.07). The hardness H of the thin film could be estimated by:

$$H = \frac{P_{\text{max}}}{A} \,, \tag{3.3}$$

where P_{max} is the maximum load and A is the projected contact area.

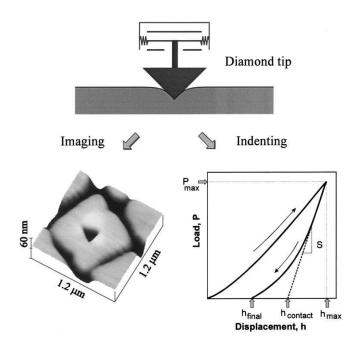


Figure 3.8 Schematic of an AFM based nano-indentation process

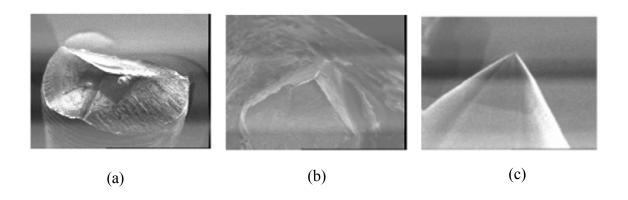


Figure 3.9 SEM images of three types of indenters. (a) Berkovich indenter, 3-Sided pyramidal shape, 142.6° (edge to opposing face), and ~ 150 nm tip radius; (b) NorthStar indenter, 3-Sided pyramidal shape, Cube corner profile, and ~ 50 nm tip radius; (c) Conical indenter, conical shape, 60° included angle and > 1 μ m tip radius [81].

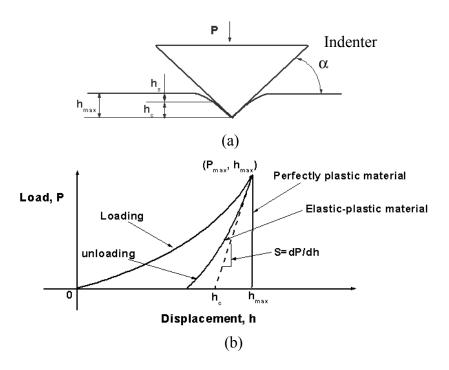


Figure 3.10 Schematic of indentation technique for modulus and hardness measurement. (a) Indentation on surface of materials; (b) typical load vs. displacement curve recorded in the indentation process.

Chapter 4: Analysis of Buckling Behavior of SiNLs

In this chapter, the focus is on the mechanical response of high aspect ratio SiNLs under nanoindentation. The Nano-indentation technique was combined with finite element method (FEM) with the latter to simulate the indentation process. Material properties of SiNLs, *e.g.* elastic modulus and strain to failure, were extracted from the simulation. The metrology was also used to evaluate friction between indenter and SiNLs, and the results indicated that this approach can be used to study friction behavior at nano-metric scale.

This chapter starts with an analysis of a set of typical experimental load-displacement curves. During indentation, a buckling instability was observed at a critical load, followed by a displacement burst without a load increase, then a fully recoverable deformation upon unloading. For experiments with larger indentation displacements, irrecoverable indentation displacements were observed due to fracture of Si nanolines. The strain to failure was estimated by FEM simulation to be as high as 7%[79], which is much larger than 0.25-0.5% of its bulk[37]. An analytical model is also developed for further understanding of the buckling behavior, *e.g.* post-buckling modes, critical buckling load, etc, of a set of SiNLs. These analyses indicated that the buckling behavior of SiNLs depends on the combined effects of load, line geometry such as height to width aspect ratio, the width to pitch ratio, etc, and the friction at contact.

4.1 FEM Simulation of Nanoindentation on SiNLs

The friction force, if exists, provides additional constraints to the SiNLs at the contacting surfaces and changes the boundary conditions of the bending and buckling problems we formulated in Chapter 2. As it can be predicted, the existence of friction may change the mechanical responses of SiNLs under nanoindentation. Specifically, the friction may change the buckling behavior of SiNLs in our experiments. To evaluate the friction effect in the buckling behavior of SiNLs, an FEM model was developed by *Li et. al.*[79].

FEM is widely used for the simulation analysis of experimental results for the study of material properties under indentation[36, 38, 82]. The unknown material properties are determined by first using them as input parameters in FEM model until best fit to the experimental load-displacement curves is obtained. Then the indentation process details could be examined accordingly.

In this section, the FEM model for the 75nm SiNLs test structures will be discussed. The normal procedures to extract the friction coefficient for the experimental load-displacement curves will be demonstrated. These procedures will be followed in our data analysis for other SiNLs test structures.

4.1.1 FEM Model

The FEM model of nanoindentation on SiNLs is shown in Figure 4.1. Twelve parallel lines were modeled as SiNLs. The tip of the indenter was located at the trench center. The diamond indenter is simulated as a rigid sphere, since it has much higher modulus (1140 GPa) than silicon (163 GPa). The modulus of silicon is assumed to be the

reduced modulus of the two, which is defined by Equation 2.2.1. The support of SiNLs, which is the bulk silicon, is assumed to be rigid as well.

The process of the nanoindentation experiments is simulated by a vertical displacement applied to the reference node of the indenter. The indenter will withdraw from the SiNLs when the maximum indentation depth is reached. The indentation force was obtained by the reaction force at the reference node of the rigid body.

The Coulomb's Law was used to simulate the friction forces. The friction coefficient was varied to generate a series of load-displacement curves. The FEM generated load-displacement curve will be compared to the experimental load-displacement curves. The coefficient of friction, which gives the FEM curves the best fit to experimental curves, will be taken as the friction coefficient of the diamond indenter and SiNLs contacting surfaces.

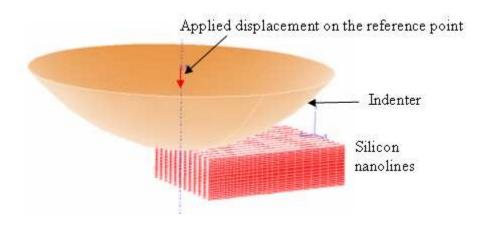


Figure 4.1 Layout of the 3D FEM model of indentation on silicon nanolines.

4.1.2 FEM Simulation Results for 75nm SiNLs

Figure 4.2 shows one load-displacement curve generated by the FEM simulation for the 75nm SiNLs test structures. A buckling was predicted at point A, where a quick drop of load is observed. In our experiments, the indentation was force controlled, and the force on SiNLs by the force controller was applied at a constant rate. Therefore when the buckling occurred, a displacement burst was observed in experiments, while the FEM simulation predicts a force drop. The critical load for the displacement burst can be determined from the first peak of the simulated curve. Figure 4.2(b) and (c) show the simulated deformation of the nanolines immediately before and after the critical load. Below the critical load, the two center lines were bent symmetrically into a half-wave mode with the top nearly perpendicular to the surface of the indenter. Once after the buckling occurred, the SiNLs bent into a quarter wave or half wave, and became softer.

FEM Simulation proved that the critical load increased as the friction coefficient of the contacting surfaces increased. Figure 4.3 shows the dependence of critical buckling load on the coefficient of friction. Without friction, the Si lines slided freely along the surface of the indenter. With friction, the sliding of Si lines was suppressed and the SiNLs were confined on the indenter surface, leading to a delay of transition of the buckling mode as well as a higher critical load. Therefore the critical buckling load offers an indirect measurement of the friction coefficient of nano-contact. The behavior will be discussed further in next section.

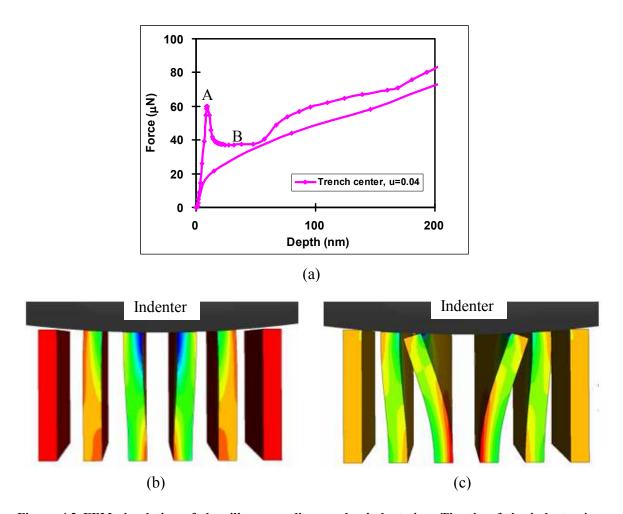


Figure 4.2 FEM simulation of the silicon nanolines under indentation. The tip of the indenter is located on top of the trench center of the 75 nm silicon nanolines. (a) plots of the simulated load-displacement curve (b) and (c) show the deformation of SiNLs before and after the mode transition at the critical load, corresponding to A and B marked in (a), respectively. Since the indentation displacement was small, only deformations of 6 lines are included in these plots.

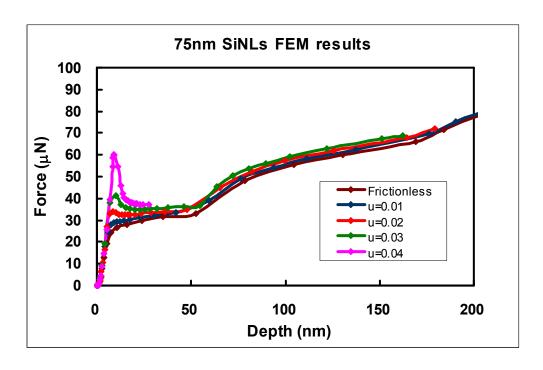


Figure 4.3 The dependence of critical buckling load on the friction coefficients. When the friction coefficient increases, the height of the peak of the load-displacement curves increases indicating the increasing of critical buckling load.

4.2 Analysis of Experimental Load-Displacement Curves

In this section, the analysis is based on a set of load vs. displacement curve, which was obtained by nanoindentation of SiNLs. The load-displacement curve shows a typical buckling behavior of the high aspect ratio SiNLs under indentation.

After the test structures were prepared and mounted on the sample stage, as the first step it is necessary to calibrate the nanoindentation system. The indenter was then positioned slightly above the SiNLs structures. The tip of the indenter was aligned at the center of the trench of two adjacent SiNLs, by AFM imaging of SiNLs scanned by the conical indenter before indentation. This generates a symmetric loading configuration, avoiding the horizontal reaction forces from SiNLs. The indenter was pushed towards

sample surface vertically until a contact between indenter and SiNLs was initiated. As the indention continued, the SiNLs structures deformed until a designated maximum indentation force was reached. Finally, after withdraw of the indenter, SiNLs were separated from indenter. The reaction forces of the SiNLs were recorded to generate a load vs. displacement curve. The first contact occurred between the indenter and the two adjacent SiNLs leading to an increase of the reaction force as the indentation depth advanced, which is shown in a typical load vs. displacement curve (before mark "a") in Figure 4.4 a). This set of load-displacement curve was obtained from the indentation test on a set of SiNLs, having 60 nm linewidth and 640 nm line height with an aspect ratio as high as 10.6. At the initial stage of deformation, the two SiNLs in contact with the indenter were elastically deformed. The SiNLs were pinned on the surface of indenter if frictional force is strong enough. The reaction force increased with further increase of displacement, until a displacement burst was observed, which was attributed to the onset of buckling instability (Marked "a" in Figure 4.4a). The reaction force at point "a" is defined as the critical load for the buckling of SiNLs, or critical buckling load.

The load-displacement curve is divided into four different regions, corresponding to four different stages of the FEM model which are shown in Figure 4.4b)-e). At the first stage, when the applied load was small, the SiNLs structures exhibited an elastic response, as shown by the green segment of the curve. This elastic response was correlated to the FEM model in Figure 4.4b). As the applied load increased, a displacement burst occurred. The displacement burst reflects a structural instability of the SiNLs when subjected to a sufficiently large applied load. At this point, the high aspect ratio SiNLs usually demonstrated a buckling behavior, with one of the possible buckling

modes as shown schematically in Figure 4.4 c). After buckling, the SiNLs may regain some structure strength, and the applied load increases gradually. This corresponds to the load-displacement curve marked by yellow and the deformation behavior in Figure 4.4d), showing that the two SiNLs bent outwards to the indenter and slided on the indenter surface. In the final stage, the indenter was withdrawn as indicated in the red region of the load-displacement curve, which corresponded to deformation behavior in Figure 4.4e). In this case, it was found that the displacement of SiNLs could fully recover without a residual deformation. It is also observed that further increase of the applied load would eventually lead to fracture of SiNLs. A typical indentation curve showing residual deformation left after indentation, and the corresponding SEM image revealing the fracture of SiNLs and debris of broken pieces, are shown in Figure 4.5 (a) and Figure 4.5(b), respectively.

The two possible buckling modes, Mode I and Mode II, are schematically demonstrated in Figure 4.7 and Figure 4.8. At the critical buckling load, softening of the nanolines under the indentation would lead to a displacement burst during a load-control experiment. In the Figure 4.7, the SiNLs are bent into a quarter-wave mode, due to a lack of constraint on the top ends of lines. In Figure 4.8, the center two lines are bent symmetrically into a half-wave mode with the top nearly perpendicular to the surface of the indenter, which is structurally stiffer than the half-wave Mode I and should have a higher critical load under the same geometry condition. It is shown that the buckling mode selection is close related to constraint boundary condition, which is determined by the line geometry and friction properties at the contact.

The impact of geometry and friction on the structure buckling mode will be further discussed in Section 4.3. The predicted mapping of line geometry, friction at contact vs. buckling mode, matches well with the experimental results, showing the validity of the buckling analysis.

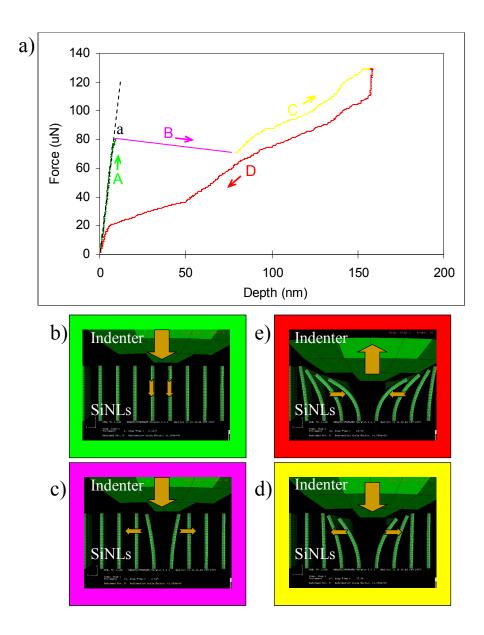


Figure 4.4 Indenation response of a set of SiNLs with 60 nm line width and 640 nm height and an aspect ratio 10.6. Four regions of the load-displacement curve was defined in a). The green region shows an elastic response of SiNLs, which is also shown schematically in b). The dashed green curve is the load-displacement curve predicted by the Hertzian model. The purple region shows a displacement burst. This indicates the instability of the SiNLs occurs after the applied load reaches the critical load, and the SiNLs buckles as shown in c). In the yellow region, the SiNLs slide on the surface of indenter tip as shown in d). In the final stage, the indenter was withdrawn from the SiNLs as shown by the red region of the load-displacement curve and in the inset e). Interestingly, the SiNLs fully recovered without residual deformation left after indentation.

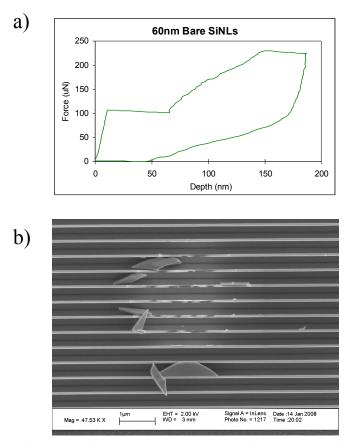


Figure 4.5 a) A typical load-displacement curve shows the irrecoverable displacement after the withdrawal of indenter from the SiNLs structures. b) fracture of SiNLs and debris were observed in SEM images.

4.3 Buckling Response Analysis

In this section, a simple mode is developed to analyze buckling behavior of SiNLs. The effect of SiNLs geometry, friction, and applied load will be discussed and a map will be created as a guideline for the buckling mode selection.

4.3.1 Formulation of the Problem

In this section, a simplified contact geometry is used to analyze the mechanical response of SiNLs structures under nanoindentation, which is shown in Figure 4.6 a) where the contact is frictionless. The indenter used in the experiments was a diamond indenter with a conical shape. The tip of the indenter was approximately spherical with a tip of radius of $R=3.9 \mu m$. In our experiments generally the contact zone was smaller than 1.5 μm . The pitch of SiNLs structures was 450nm and normally only one or two pairs of SiNLs were in contact with the indenter. In Figure 4.6 a), two SiNLs are in contact with the indenter where θ is the angle between the contact point on the indenter surface and the indenter apex. Here θ could be deduced as:

$$\theta = \arcsin(\frac{p-w}{2R}) \approx \frac{p-w}{2R},$$
(4.1)

Where p is the pitch of the SiNLs structures and w is the line width. For the force applied on the indenter, since the sum of vertical components acting on the indenter is balanced, there is:

Where F is the total force applied to the indenter in the vertical direction, and F_n is the normal force acting on SiNLs by the indenter. From the force balance in other directions, the relation between force components on the SiNLs, F_z and F_x , are given by

$$F_z = F_n \cos \theta = \frac{F}{2}$$

$$F_x = F_n \sin \theta = \frac{F}{2} \tan \theta$$
(4.3)

where the *xyz* coordinate system is defined as shown in the lower-left inset of Figure 4.6 a).

Consider under the condition of existence of frictional forces at the contact surfaces, the force components are to be modified as:

$$F_z = F_n \cos \theta + F_f \sin \theta = \frac{F}{2} ,$$

$$F_x = F_n \sin \theta - F_f \cos \theta$$
(4.4)

where F_f is the frictional force which is tangent to the diamond surface at the contact. Rearranging Equation 4.4 and defining $F_f = \mu \times F_n$, according to the Coulomb's Law, we have

$$F_{z} = \frac{F}{2}$$

$$F_{x} = \frac{F}{2} \frac{\tan \theta - \mu}{1 + \mu \tan \theta}$$

$$\approx \frac{F}{2} (\tan \theta - \mu) \quad \text{with } \theta << 1 \text{ and } \mu \tan \theta << 1$$

$$(4.5)$$

In the following text, the coefficient $\frac{\tan\theta-\mu}{1+\mu\tan\theta}$ will be denoted as Q for convenience.

For clarification, the details of the undeformed line geometry are shown in Figure 4.6 b). The SiNLs is eccentrically loaded at the upper-left corner with F_z acting at a distance w/2 away from the axis of SiNLs. It should be noted that the "friction coefficient" μ as defined is only a static friction coefficient assuming that the SiNLs were not sliding on the indenter surface. Once sliding occurs, the friction coefficient μ will become smaller than the static friction coefficient, which is determined by the lateral

forces. Therefore this "friction coefficient" represents the static friction coefficient before transition to sliding friction from static state.

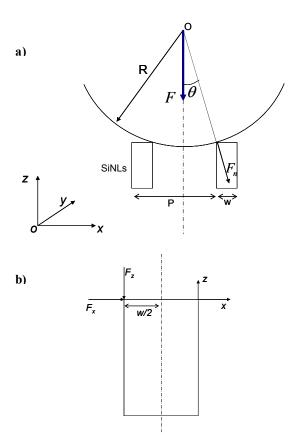


Figure 4.6 Contact geometry of nanoindentation. The shape of the diamond indenter was conical but it was modeled as a sphere with a radius R of 3.9 μ m. In the picture, two SiNLs were shown in contact with the indenter. θ is the angle that measure the relative place of the contact point on the indenter. F is the total force applied on the indenter in the vertical direction. F_n is the force on SiNLs that was normal to the indenter surface.

4.3.2 Buckling Modes and Critical Loads Analysis

The two buckling modes are determined by different the boundary conditions. The first buckling mode (denoted as Mode I) shows the sliding of SiNLs on the indenter surface after buckling (in Figure 4.7). Under this buckling mode, the bottom of SiNLs is fixed on the substrate and the top end is normally simulated as a free end. The second buckling mode (denoted as Mode II) is shown in Figure 4.8. The top end of SiNLs is pinned on the indenter surface and allowed to move vertically and rotate, but is confined laterally.

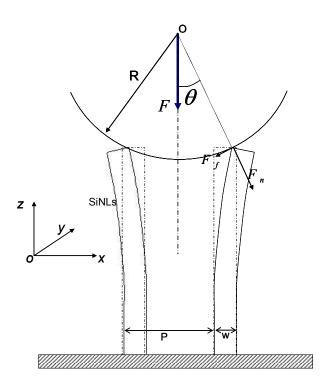


Figure 4.7 Mode I buckling

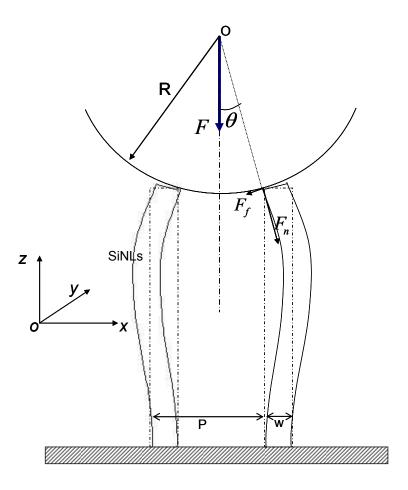


Figure 4.8 Mode II buckling

For Mode II buckling, the bending moment at the top of SiNLs is

$$M = F_z(e+x) + F_x z , (4.6)$$

where e=-w/2 is eccentricity of applied load (Figure 4.6b). Here F_x depends on the deflection of SiNLs, the applied force by the indenter and the frictional force. According to the definition of moment, $M = -EI\frac{d^2x}{dz^2}$, the equation of deflection can be written as

$$EI\frac{d^2x}{dz^2} = -M = -F_z(e+x) - F_x z.$$
 (4.7)

The general solution to the equation of deflection is

$$x = A\sin kz + B\cos kz + Cz + D, \qquad (4.8)$$

where $k = \sqrt{\frac{F_z}{EI}}$, and the constants A, B, C and D are determined by the boundary conditions.

The bottom end (where z=0) of SiNL is fixed, therefore both the deflection and the angle of deflection are always zero, which corresponds to x=0 and $\frac{dx}{dz} = 0$. Under these boundary conditions, the solution of deflection x is

$$x = \frac{Q}{k}(\sin kz - kz) + e(\cos kz - 1). \tag{4.9}$$

Since for Mode II buckling the top end is pinned, which indicates that two boundary conditions have to be satisfied

$$x(z = h) = 0$$

$$\frac{d^2x}{dz^2}\Big|_{z=h} = 0$$
(4.10)

where the first equation reflects the fact that there is no significant deflection; and the second equation indicates that the total moment is zero at the top end. The moment due to externally applied forces have to be offset by the moment generated by reactive force of SiNL. Applying boundary conditions (4.9) to the solution of deflection x in equation (4.8), we have

$$\frac{Q}{k}(\sin kh - kh) + e(\cos kh - 1) = 0$$

$$\frac{Q}{k}(-k^2)\sin kh + e(-k^2)\cos kh = 0$$
(4.11)

After simplifying the above equations, we obtain

$$\tan kh = kh$$

$$Q = \frac{e}{h}$$
(4.12)

where the first equation can be solved numerically and the smallest positive solution for *kh* is found to be 4.493, therefore the critical buckling load is

$$F_{z_{-}cr} = \frac{4.493^2 EI}{h^2} \,. \tag{4.13}$$

According to the definition of $k = \sqrt{\frac{F_z}{EI}}$. This critical buckling load has the same value as that given in Chapter 2, where there is no external lateral load F_x and the eccentricity of applied load is zero, but in both cases, the boundary conditions are the same because the top end of SiNLs is pinned.

The second equation, $Q = \frac{e}{h}$, provides the requirement for the frictional force to satisfy the boundary conditions. Recall that we defined $Q = \frac{\tan \theta - \mu}{1 + \mu \tan \theta} \approx \tan \theta - \mu$ in

Equation (4.4), and $e = -\frac{w}{2}$, therefore

$$\mu = \frac{w}{2h} + \tan \theta \approx \frac{w}{2h} + \frac{p - w}{2R} \quad . \tag{4.14}$$

Only when the friction coefficient μ is larger than this value can the frictional force provide enough constraint to pin the SiNLs on the indenter surface before the initiation of Mode II buckling. When μ is smaller than equation 4.14, sliding may occur before the occurrence of Mode II buckling.

For Mode I buckling, since the system is eccentrically loaded and a lateral force exists, there is a deflection of the top of SiNL even before the occurrence of buckling. As shown in Figure 4.4, a deflection, δ , is assumed at the top of SiNLs. By considering the deflection, the bending moment in equation 4.6 is:

$$M = F_z(-\delta + e + x) + F_x z$$

Following the same procedure and boundary conditions for the bottom end of SiNLs, the solution of the equation of deflection (equation 4.7) is solved to be

$$x = \frac{Q}{k}(\sin kz - kz) + (-\delta + e)(\cos kz - 1), \tag{4.15}$$

which is very similar to equation 4.9. Equation 4.15 need to satisfy the assumption that the deflection of SiNL at the top end is δ , therefore,

$$x(h) = \frac{Q}{k}(\sin kh - kh) + (-\delta + e)(\cos kh - 1) = \delta, \qquad (4.16)$$

from which the deflection δ can be solved as

$$\delta = e^{\frac{\cos kh - 1}{\cos kh}} + \frac{Q}{k} \frac{\sin kh - kh}{\cos kh} \,. \tag{4.17}$$

Equation 4.17 is derived as a superposition of solutions for a purely eccentrically loaded beam and purely laterally loaded buckling beam. From equation 4.17, it is clear that when $\cos kh=0$, the deflection mathematically reaches infinite which indicates the unstable state where buckling occurs. The critical buckling load can be solved from $\cos kh=0$,

$$F_{z_{-}cr} = \frac{\pi^2 EI}{4h^2} , (4.18)$$

which is the same as given solved in Chapter 2 under the condition of no eccentric or lateral load.

For the boundary conditions in Mode I buckling are applied, the top end of the SiNL is free and the total force and total moment is zero. These conditions lead to the following equation for the deflection along the x direction when, z=h:

$$\frac{d^2x}{dz^2} = \frac{d^3x}{dz^3} = 0.$$

The solutions of this equation are defined by the following conditions:

$$Q\sin kh + (e - \delta)k\cos kh = 0$$

$$Q\cos kh - (e - \delta)k\sin kh = 0$$

These two equations are true only when Q=0, indicating $F_x=0$. This corresponds to the condition where the top end of the SiNL is considered to be "free". When Q=0, we deduce the friction coefficient µ to be:

$$\mu \approx \tan \theta \approx \frac{p-w}{2R}$$
.

Accordingly, the friction behavior at the contact can be divided into three regions with

$$\mu \ge \frac{w}{2h} + \frac{p - w}{2R} \tag{4.19a}$$

$$\begin{cases}
\frac{p-w}{2R} \le \mu \le \frac{w}{2h} + \frac{p-w}{2R} \\
\mu \le \frac{p-w}{2R}
\end{cases} \tag{4.19b}$$

$$\mu \le \frac{p - w}{2R} \tag{4.19c}$$

Different buckling behaviors will occur depending on in which regime the friction coefficient belongs. These regions are defined according to the geometry of the SiNLs, e.g. height to width aspect ratio, and the width to pitch ratio, etc. The effect of geometry on the buckling behavior is further discussed in the following section.

The Effect of Geometry and Friction on Buckling Behavior

For convenience, the height to width aspect ratio is denoted as AR, and the width to pitch ratio is denoted as WP, we have:

$$AR = \frac{h}{w}$$

$$WP = \frac{w}{p}$$

Then the regions of friction coefficient can be expressed as

$$\mu \ge \frac{1}{2AR} + \frac{p(1 - WP)}{2R} \tag{4.20a}$$

$$\begin{cases} \mu \ge \frac{1}{2AR} + \frac{p(1 - WP)}{2R} \\ \frac{p(1 - WP)}{2R} \le \mu \le \frac{1}{2AR} + \frac{p(1 - WP)}{2R} \\ \mu \le \frac{p(1 - WP)}{2R} \end{cases}$$
(4.20a)
$$(4.20b)$$

$$(4.20c)$$

$$\mu \le \frac{p(1 - WP)}{2R} \tag{4.20c}$$

Equation 4.20a expresses the conditions for Mode II buckling to occur. The effect of AR and WP is plotted in Figure 4.9. There are two sets of curves in Figure 4.9, which divide the area of the graph into three regions, as marked by A, B and C. The set of straight lines corresponds to the condition that Q=0 and with the top end of SiNL being free, where $\mu = \frac{p(1-WP)}{2R}$. The other set of curves corresponds to the condition that the

top end of SiNL is pinned on the indenter surface, and $\mu = \frac{w}{2h} + \tan \theta \approx \frac{w}{2h} + \frac{p-w}{2R}$.

As the height to width aspect ratio (AR) increases, the required coefficient of friction to initiate the Mode II buckling becomes smaller. This can be seen from the result of the 70nm test structures which has an AR=8.7, the coefficient of friction required for Mode II buckling to occur for this structure is 0.107. In comparison, with the AR of the 90nm test structure increasing to 15.5, the required coefficient of friction for Mode II buckling decreases to 0.078. If the actual coefficient of friction is smaller than this value, it is highly probable that the Mode II buckling will not be observed for the 90nm test structure. Accordingly, Mode II buckling would be less probable to occur for the 70nm and 60nm test structures, considering the coefficient of friction between diamond and silicon is low and may not reach a value of 0.1. Table 4.1 summarizes the required coefficients of friction for Mode II buckling for all test structures on which nanoindentation experiments were performed. The results were confirmed by the experimental observation, which shows that Mode II buckling was only observed for 90nm and 75nm test structures.

Based on this analysis, the required coefficient of friction for 30nm test structures for Mode II is the smallest. However, Mode II buckling was not experimentally observed. This indicates that the actual coefficient of friction for this set of test structures is smaller than 0.075. In Chapter 5, this phenomenon is further analyzed, which indicates that the coefficient of friction for 30nm test structures is smaller than those of other test structures.

The width to pitch ratio (WP) will also affect the buckling behavior. Based on above analysis, if the height to width aspect ratio is kept constant while the dimension of SiNL is scaled down, Mode II buckling would be less likely to be observed. When the

dimension of SiNL is scaled down, the eccentricity of applied load (e=-w/2) decreases. An eccentric load has similar effect as friction force because it applies a bending moment on SiNL to cause the SiNL to bend inwards.

So far we have focused on coefficient of friction in region A, where SiNL most likely buckles in Mode II. Next the buckling modes in regions B and C will be discussed. The buckling mode in region B and C is most likely to be Mode I, but SiNL may behave differently. In region C, the frictional force is smaller than the lateral force applied by the indenter. Therefore there is always a positive force in the *x-axis* direction for the right SiNL in Figure 4.7. When the indenter makes contact with SiNL and a force is applied, the SiNL will bend outward, regardless of the magnitude of the force. When buckling occurs, the indenter surface will not provide enough force to pin the SiNL and Mode I buckling occurs. In region B, the SiNL is pinned, but the pinning force will not be strong enough to hold the SiNL until the Mode II buckling occurs. Therefore, in this region, either Mode I buckling or bending-sliding will occur.

It must be noted that the coefficients of friction calculated in this simple model are generally larger than the values evaluated by FEM simulation. This discrepancy is due to the fact that, in this simple model, it is assumed that the load is applied uniformly. The SiNLs, therefore, deformed uniformly. In our experiments, the indenter is a conical shape, and the deformation of SiNLs is localized. Therefore this simple model overestimated the lateral force.

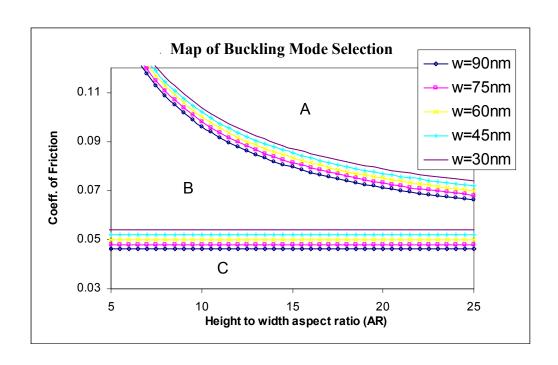


Figure 4.9 Effect of height to width aspect ratio of SiNLs and width to pitch ration on the buckling behaviors. When the coefficient of frictions are located in region marked by "A", Mode II buckling occurs, otherwise, Mode I buckling occurs.

Table 4.1 Coefficient of Friction Required for Mode II Buckling

Width	Height	Pitch	AR	WP	μ_{ModeII}	Mode II
90nm	1400nm	450nm	15.55	0.2	0.078	Observed
75nm	1400nm	450nm	18.67	0.17	0.075	Observed
70nm	610nm	450nm	8.71	0.16	0.107	No
60nm	610nm	450nm	10.17	0.13	0.099	No
30nm	720nm	450nm	24	0.067	0.075	No

4.4 Summary

In Chapter 4, the results obtained from the study of the mechanical behavior and friction properties of SiNLs using a nanoindentation technique was represented. The SiNLs test structures used in the experiments had height to width ratio from 10 to 20, making it well suitable for the study of buckling behaviors. The loading-displacement indentation curves showed that the critical load to induce the buckling of the SiNLs can be correlated to the contact friction of the nano-indenter, the geometry of SiNLs, and the eccentricity of the applied load. A map was built as a guideline to describe the buckling modes observed. The map was divided into three regions where different regions correlate to different buckling modes including Mode I, Mode II and sliding-bending of SiNLs. This map agrees very well with the experimental observations.

Chapter 5: Frictional Behaviors of SiNLs

In this chapter, nanoindentation experiments were performed on multiple SiNLs samples, and the focus is on the friction behaviors of SiNLs at the contact interface. The SiNLs were prepared with the fabrication methods as described in Chapter 3, using EBL for pattern defining and anisotropic wet etching for pattern transferring. The high quality SiNLs, having nearly perfect rectangular cross sections, smooth sidewalls, and high ARs, are well suited to the frication at nano-metric scale.

The first part of this chapter is a description of the indentation experimental details, including an introduction to the test structures fabricated, indentation procedure details, experimental environment selection, etc. To evaluate friction properties at nanoscale, a model is developed afterwards, to extract contact area, penetration depth, and the frictional shear stress for the contact situation between SiNLs and the indenter. The model is then applied to the experimental results of nanoindentation of SiNLs under various conditions, *e.g.* indentation of bare SiNLs with various line geometry, indentation of SiNLs with different coating layers for modification of contact surface properties, and the indentation under cyclic loading conditions for a study of contact history. The contact area and the frictional shear stress are evaluated, and their impact on the buckling behavior of SiNLs is analyzed.

5.1 Introduction to Test Structures and Test Ambient

This section starts with an introduction to the SiNLs test structures prepared. Since friction properties, particularly the friction at nano-scale, are directly affected by localized contact interface details; various test conditions were employed, e.g. SiNLs with oxide or chromium coatings, indentation under air or N_2 ambient, etc, for the assessment of the impact of the modification of the contact conditions on friction properties. The second part of this section is about the influence of test ambient on friction of SiNLs. It was found that the impact on friction coefficient is not apparent if the only change of test conditions is changing from air to dry N_2 . The results and the associate analysis are presented.

5.1.1 Test Structures

A series of test structures were fabricated on [110] silicon wafers, based on the proposed fabrication process in Chapter 3. The line widths and heights were varied, and the line pitch was kept constant at 450nm. The details of the test structures are summarized in Table 5.1. Nanoindentation tests were performed on these 5 sets of test structures, with the smallest feature size reaching a 30 nm range. The height to width ARs of the SiNLs varied from 10 to 24, indicating a large range of ARs for the nanostructures that are well-suited for investigation of buckling behavior.

Figure 5.1 shows the SEM images of the 30nm SiNLs test structures. The SiNLs have single crystalline structures, nearly atomically flat sidewalls and rectangular cross sections. The uniformity of line widths and height, along with the well-defined geometry, make these SiNLs almost perfect test structures for friction characterization as well as numerical evaluation.

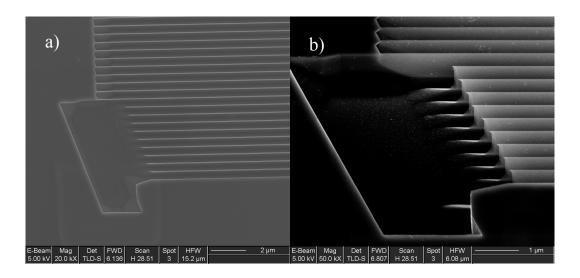


Figure 5.1 SEM images of the 30nm test structures. a) top view. b) side view. The SiNLs have height of 720nm and pitch of 450nm.

Table 5.1 Specifics of 5 sets of test structures and coating layers. Test conditions are also summarized. The thickness of silicon oxide and chromium layers were around 3nm and 2nm respectively.

Sample	-	Dimension	S	Coatings			Test Conditions	
set #	Width	Height	AR	Bare Si	Oxide	Cr	Air	Dry N2
1	90nm	1400nm	450nm	Performed	Performed	Performed	Performed	N/A
2	75nm	1400nm	450nm	Performed	Performed	Performed	Performed	N/A
3	70nm	610nm	450nm	Performed	Performed	Performed	Performed	Performed
4	60nm	610nm	450nm	Performed	Performed	Performed	Performed	Performed
5	30nm	720nm	450nm	Performed	Performed	Performed	Performed	Performed

Since details at contact interface may pose significant impact on nanoscale friction properties, the surface of SiNLs was modified, by coating of thin layers of silicon oxide or chromium in order to assess the influence of interface modification on friction. Meanwhile, it was reported that test ambient may also affect interface properties[57],

owing to whether there is an existence of water layer between contact interfaces or not. The experiments performed are summarized in Table 5.1. The impact of test ambient was investigated at first, by conducting nanoindentation in both N_2 and air ambient on a set of SiNLs with feature size of 70 nm. The associated background and results are discussed in the following section.

5.1.2 Impact of Test ambient on Friction at contact

At nanoscale, the existence of a layer of water molecules between the indenter and SiNLs surface may change the contact nature. When a lubricant layer exists, such as a water intermediate layer, the friction coefficient may be significantly reduced. Without the water molecules or other intermediate layers, intimate contact normally occurs. To assess the impact of test ambient on the contact interface modes, Nanoindentation tests were conducted both in N₂ and air ambient. It was noted that at air ambient, the relative humidity is roughly constant of ~45% RH, while in a dry N₂ ambient the humidity is much lower and is smaller than 5% RH. It is expected under such a low humidity, the contact friction forces should be larger than that in air ambient, leading to a higher critical buckling load under indentation test. All the experiments were performed at room temperature.

The air ambient test condition was just carrying out the experiments in regular lab environment. The test system was covered by a transparent cover to reduce the influence of air flow, which is shown in Figure 5.2. The humidity inside the enclosure was measured to be around 45% RH during of the indentations. In order to achieve a dry ambient test condition, two steps were needed. The first step was to bake out the trapped

moisture from the SiNLs samples, and the second step was to maintain the low humidity condition by filling dry N_2 into the enclosure.

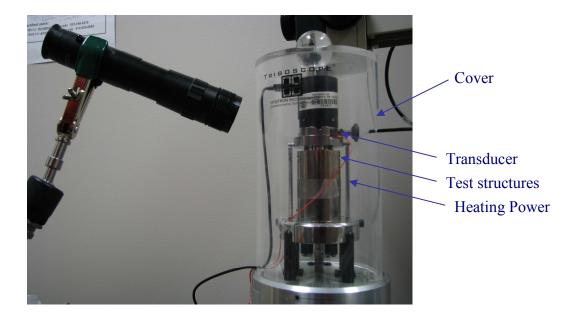


Figure 5.2 Image of the test system covered by a transparent cover. The test environment was enclosed and the humidity inside was measured to be nearly constant $\sim 45\%$ RH under air ambient. Additional electric power cords for the baking of the test structure were added to achieve a dry test condition. The telescope on the left was used to locate the indenter on the test structures.

For the purpose of baking out absorbed water molecule layers, a heating chip was designed and incorporated into the test system, which is shown in Figure 5.3. The heating chip was a piece of silicon chip coated with copper film. The temperature control was achieved by passing electrical current through the conductive film. The heating chip was sandwiched between the SiNLs test structure and the sample stage of indentation system. The test structures were heated up to about 110°C for 10 minutes. N₂ gas was kept flushing into the enclosure for at least three hours, two hours before heating plus one hour after heating. The nano-indentation experiments were performed immediately after

turning off the nitrogen gas for stabilizing the censoring system. The purpose of this setup is to avoid any additional moisture uptake before and during the indentation test.

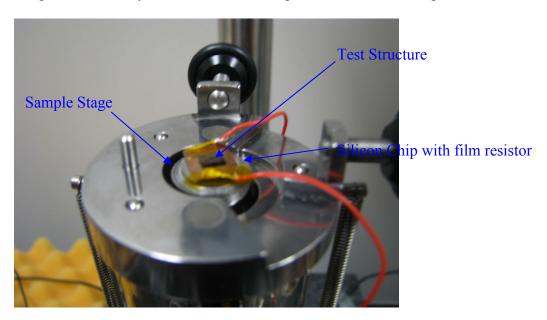


Figure 5.3 Image of the heating chip, sample stage, and the SiNLs test structures. The heating stage is consisted of a silicon chip with copper film resistor, which is sandwiched between the test structures and the sample stage. Temperature of the test structures was controlled by the DC power source. In the experiments, temperature up to 110°C was maintained for about 10 minutes to drive out moisture on the test structures. A humidity of less than 5% was measured after 3 hours of dry nitrogen gas flush afterwards.

Table 5.2 Critical Loads of 70nm/610nm SiNLs under dry and ambient test conditions

Test condition	Average critical load (μN)	Standard Deviation (μN)
Dry Nitrogen	69.0	10.4
Air Ambient	66.9	12.2

Table 5.2 shows the experimental results of nanoindentation on the SiNLs with 70 nm linewidth. Interestingly, it was found that statistically the critical buckling load of SiNLs did not show significant differences between the two humidity conditions. The results at the first glance is sort of in contradiction with the contact theory presented in Chapter 2, which suggested that the water intermediate layer under a humid condition may change the contact nature and greatly affect the contact friction. However in our experimental conditions, this is reasonable and it will be addressed in detail next.

As it is mentioned before, the water intermediate layer, particularly under a high humidity ambient, may serve as a lubricating layer for the contact, thus significantly reduce the friction force. When there is no intermediate layer existing, intimate contact may establish and the friction force increases. One possible explanation of our nanoindentation phenomenon is the effect of high contact pressure.

It was reported that high contact pressure of a few hundreds of MPa will squeeze out water layers between contacting surfaces. In nanoindentation tests, generally the force applied on the SiNLs is in the range of $10\sim200\mu N$. Since the size of the contact zone should be at the same order of the width of SiNLs, which gives a contact area of $\sim10^{-14}m^2$, the contact pressure in the nanoindentation test is estimated to be of $10\sim20$ GPa. This high contact pressure can initiate an intimate contact between the indenter and SiNLs, even with the existence of a water molecular intermediate layer.

Another perspective to look into this issue, is to understand the boundary conditions of the water intermediate layer posing effect on the contact friction. In Chapter

2 it is shown that the adhesion between the two contact surfaces generates an offset to the Hertzian force. The offset is in the range of

$$F_{adhesive} \sim n \pi R \gamma$$
,

where n is a number in the range of 1.5~2, and γ is the surface tension of contacting surface which is normally on the order of $0.1J/m^2$ for solid-solid contact, and $0.073J/m^2$ for water. Assuming R is the line width of SiNLs, the offset force is found to be less than $0.1\mu N$. Considering under the condition of the applied indentation force is generally about $10\sim200\mu N$, the effect of the adhesion force with a water intermediate layer on the contact friction is less than 1% here.

From the above analysis, it is concluded that due to a high elastic pressure between the contact surfaces in the nanoindentation tests, the moisture effect on the change of contact nature was not likely to be observed in experiments. Nevertheless, it is also mean that the adhesion force contributes little to the contact area, the friction force, and the buckling behavior of SiNLs. Thus Hertzian contact model is still a valid approximation to evaluate the contact area at nano-scale. An analysis model is developed in the next section, which is based on the Hertzian contact model and the fact that the effect of adhesion force can be neglected, to deduce penetration depth, contact area, and the friction shear stress at the nano-contact. The model results will be compared with experimental results, which are mainly under air ambient test condition.

5.2 Contact Area Evaluation

5.2.1 Formulation of the problem

The geometry of our experiments consists of a conical diamond indenter indenting on SiNLs with rectangular cross sections, as shown in the Figure 5.4. The pitch of SiNLs structures was much smaller than the diameter of the indenter, therefore the shape of the indenter can be approximated as a sphere.

Instead of formulating the problem as a diamond indenter with relatively large size being pressed into SiNLs structures with relatively small size, this problem is equivalent to silicon "indenters" with a shape of spherical sector indent on a flat diamond surface, as shown in the schematic of Figure 5.5. The SiNLs "indenters" have a tip shape of spherical sector with radius of R which is the radius of the original diamond indenter. Other geometry parameters of the SiNLs indenters are set to be the same as the SiNLs, such as height and pitch.

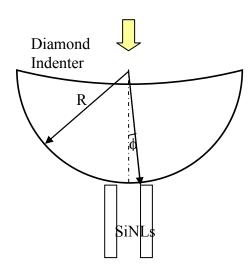


Figure 5.4 The geometry of a diamond indenter on SiNLs structures before the indenter was brought into contact with the SiNLs. The tip of the indenter was placed at the center of the trench.

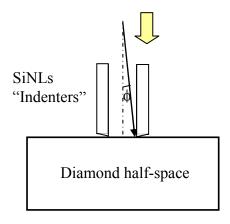


Figure 5.5 Geometry configurations that are equivalent as the original contact geometry defined in Figure 5.3. Here, the system is defined as SiNLs "indenters" indent on a diamond half-space. The SiNLs originally having rectangular cross-section are now replace by SiNLs "indenters" with their top surfaces defined as spherical sectors. The spherical sectors have the same diameter as that of the original diamond indenter.

5.2.2 Calculation of Contact Area

The details of the contact surfaces before the contact is made are shown in the schematic Figure 5.6a). The profile of the surface of the un-deformed silicon "indenter" can be described as

$$f(x) = \frac{\left(x - \frac{p - w}{2}\right)^2}{2R} - \frac{\left(\frac{p - w}{2}\right)^2}{2R},\tag{5.1}$$

where p and w are the pitch and width of the SiNLs structures. This profile is actually an approximation of a sphere when the contact area is small compared with the indenter size, i. e. x << R, where R is the diameter of the diamond indenter. In our experiments, pitch and width or SiNLs are 450nm and less than 100nm respectively but R is 3900nm. The approximation of the profile is good enough considering the contact size of our

experiments are actually even smaller. The second term on the right hand side is a constant, which is a compensation of area due to the fact that the indentation was performed at the trench center instead of right on the SiNLs. For the same reason, the coordinate x has an offset of (p-w)/2.

If the SiNLs "indenters" was pressed "into" the diamond half-space by a penetration of δ , the "indenter" will be deformed. The geometry of the indenter and diamond half-space after the contact is schematically shown in Figure 5.6 b). In the next of this section, the terminology indenter will be used to refer the SiNLs indenter with spherical sector surface, if not stated otherwise; and the original diamond indenter will be referred as diamond indenter. Here, the diamond half-space was modeled as a rigid body, and the modulus of SiNLs indenter was defined by the reduced modulus E_r ,

$$\frac{1}{E_r} = \frac{1 - v_1^2}{E_1} + \frac{1 - v_2^2}{E_2} \quad . \tag{5.2}$$

The profile of the indenter with deformation can de described as

$$v(x) = 0 \qquad \text{when } x < a$$

$$v(x) = \frac{x^2}{2R} - \delta \qquad \text{when } x > a \qquad (5.3)$$

where a is contact length along the x-direction as shown in Figure 5.3b. For a given penetration depth δ , a can be determined by the following relationship, $f(a) = \delta$. To be explicit, when a < w, a can be found by

$$2R\delta = a^2 + (p - w)a \quad . \tag{5.4}$$

The condition a < w indicates the contact is incomplete, and the scenario is shown in Figure 5.6 a).

With the increase of the applied force, the contact area also increases. When a=w, the contact becomes complete, then the contact length along line width direction a is constant. However, the contact length along line length direction, which is denoted as b, changes as the penetration depth changes. The relation between b and δ is

$$b = \sqrt{2R\delta} \ . \tag{5.5}$$

In both cases, the area of contact is calculated as

$$A = \begin{cases} c^{2} \left(\frac{\pi}{2} - \arcsin(\frac{p-w}{2c}) - \sqrt{1 - (\frac{p-w}{2c})^{2}} (\frac{p-w}{2c}) \right) & (a < w) \\ c^{2} \left(\arcsin(\frac{p+w}{2c}) + \sqrt{1 - (\frac{p+w}{2c})^{2}} (\frac{p+w}{2c}) - \arcsin(\frac{p-w}{2c}) - \sqrt{1 - (\frac{p-w}{2c})^{2}} (\frac{p-w}{2c}) \right) & (a = w) \end{cases}$$

where

$$c = \begin{cases} \frac{p - w}{2} + a & (a < w) \\ \sqrt{\left(\frac{p - w}{2}\right)^2 + b^2} & (a = w) \end{cases}$$
 (5.7)

Therefore, once the penetration depth δ is determined, the parameters of contact length a or b can be calculated by equations 5.4 and 5.5, respectively. Then the contact area can be calculated according to equation 5.7.

However, the challenge is that the penetration depth δ is not a quantity that is directly measured or monitored by experiments. To address this issue, there are two possible methods tackling this problem. The first method is to calculate δ from the displacements of indenter that were experimentally measured by the displacement transducer. The second method is to calculate δ from the indentation forces. The

following sections will discuss the evaluation of penetration depth δ using these two methods, respectively.

5.2.3 Calculation of Penetration Depth by indentation Displacement

The displacement of indenter consists of the local deformation of SiNL (penetration depth δ) and the elastic deformation of the SiNL under compressive force. A simple model is used to express the relation between displacement and penetration depth

$$d = \delta + d_{elastic} , \qquad (5.8)$$

where d is the experimentally measured displacement of indenter. d is around 10 nm to 20 nm before buckling of SiNLs. $d_{elastic}$ is the global deformation of the SiNL when it is subjected to compressive forces. It is noted that only localized deformation at the contact, which represents the penetration depth of indenter, contributes to the contact area estimation.

It is difficult to derive an analytical solution for $d_{elastic}$, since the compression stress on the SiNLs was not uniform, and the deformation of SiNLs is also subjected to the confinement in the y-direction. FEM simulation was employed to get an approximate solution of $d_{elastic}$ as a function of applied forces. A schematic of the FEM model is shown in Figure 5.7 a) where two key points were defined as A and B. Point A was on the upper-left corner of the SiNL, and Point B was on the sidewall of SiNL with a distance of 50 nm below point A. In the indentation, SiNL was only subjected to compressive global elastic deformation at OB; and the localized deformation only occurred at BA. These assumptions were based on the fact that the total deformation

before buckling was measured to be around 20 nm, plus the penetration or localized deformation is only a fraction of the total deformation. In Figure 5.7 b), points A and B moved down to points A' and B' when the SiNL was deformed. As an example, Figure 5.8 plots the displacements of the diamond indenter, point A and point B, respectively, of nanoindentation on for a set of 90 nm SiNLs. The penetration depth can be evaluated as

$$\delta = OA' - \frac{OB'}{OB}OA. \tag{5.9}$$

The second term on the right side of equation 5.9 is the height OB' prorated into the line height of SiNL OA.

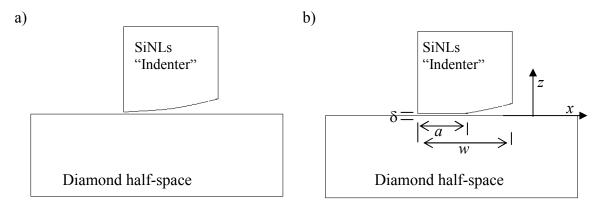


Figure 5.6 SiNLs indenters before contact a), and SiNLs being pressed into the diamond half-space b), but the contact zone size a is smaller than the line width w on the x direction, i. e. the contact is incomplete.

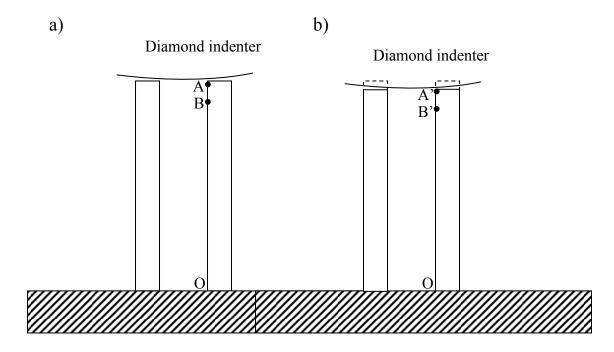


Figure 5.7 Two key points were defined in the FEM model to evaluate the elastic deformation of the SiNLs. After the SiNLs were deformed, A and B moved to points A' and B'. The elastic deformation $d_{elastic}$ is defined by OB-OB'. The local deformation (penetration depth δ) is assumed to be AB-A'B'.

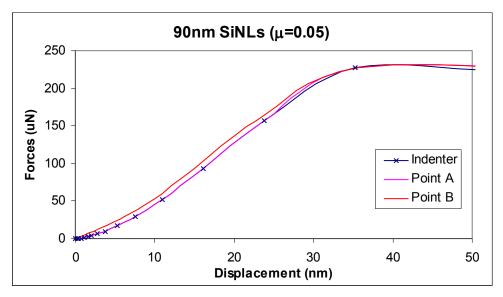


Figure 5.8 Deformation of SiNLs from FEM simulation. Pink curve shows the displacement of point A, and the red curve is for B. The blue curve is the displacement of the diamond indenter which is very close to the displacement at point A, since point A is in contact with the diamond indenter until the occurrence of buckling.

5.2.4 Calculation of Penetration Depth by Normal Force

The second method to evaluate penetration depth δ is from indentation force. Once the contact is made, the silicon "indenter" is subjected to deformation. Consequently, elastic stress is built up around the contact zone. If the distribution of elastic stress is known, the total reactive force can be estimated by integrating the stress over the area of contact zone

$$F = \int_{\text{ContactZone}} \sigma dA = \int_0^{\delta} \sigma \frac{dA}{d\delta} d\delta \quad , \tag{5.10}$$

where σ is the distribution of stress; and A is the contact area which is a function of penetration depth δ according to equation 5.6. In Hertzian contact model, a spherical indenter is studied; and the stress distribution is assumed to be in the form of a parabolic function:

$$\sigma = \sigma_0 \sqrt{1 - \left(\frac{r}{c}\right)^2} \qquad , \tag{5.11}$$

where c is defined by equation 5.7; σ_0 is the maximum stress under the indenter which could be approximated to be

$$\sigma_0 = \frac{3F}{2A} \qquad . \tag{5.12}$$

Therefore σ_0 is 1.5 times of the average stress. In the calculation, the "solver" function of Microsoft Excel program was used to carry out the integral numerically for equation 5.10, and relations between the total force F and the penetration depth δ was solved. Subsequently, the total force F as a function of contact area A can be obtained.

Figure 5.8 plots the curves of contact area change in the elastic range of nanoindentation, which were evaluated by the proposed methods based on the analysis of displacement and force, respectively, for a indentation test on a set of 90 nm wide SiNLs. The results show a reasonable agreement to each other, between these two methods. With the extraction of relationship between force and contact area, frictional shear stress can be evaluated based on the Bowden Tabor's Theory, and the results are shown in the following sections.

5.3 Friction of Bare SiNLs

In this section, the experimental data on bare SiNLs with various geometrical configurations are presented. Mechanical responses and friction behaviors at nanocontact are analyzed based on the FEM simulation and Coulomb's friction theory. The geometries of SiNLs were summarized in Table 5.1

5.3.1 Experimental results for 90nm and 75nm SiNLs test structures

Nanoindentation results on 90nm and 75nm SiNLs test structures are presented and analyzed. The experiments were performed in air ambient. Experimental results under other loading conditions and coating layers will be reported in the following sections.

Figure 5.10 shows the typical load-displacement curves of this set of experiments. There are two sets of curves representing two kinds of distinct buckling behavior occurred. On the green curve, two displacement bursts were observed, which indicates

two different buckling modes. One buckling mode occurred during the loading (marked as A), the other occurred at the unloading process (marked as B). We defined the process that a buckling occurred on the unloading process as a buckling mode transfer, because initially there was a different buckling mode occurred then the buckling mode transferred to another. We define the buckling mode occurred on the unloading process as Mode I, while the other as Mode II. On the other curve (brown), only one displacement burst was observed which occurred on the loading process only. The critical load of the brown curve was almost identical as the critical load of the Mode I buckling of the green curve, indicating that they were subjected to the same buckling mode.

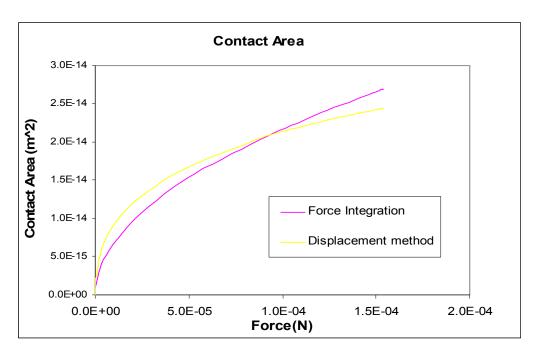


Figure 5.9 Contact area of SiNLs as a function of applied load. Two methods were used to evaluate the contact area, the force integration and displacement method.

The critical buckling loads of each set of the experiment data were recorded, and summarized in

Table 5.3. The critical loads of different buckling modes were recorded separately, as indicated by Mode I and Mode II. The average critical load of Mode II, occurred at point A marked in Figure 5.10 was significantly larger than that of Mode I occurred at point B, namely $194\mu N\pm 16\mu N$ as compared to $123\mu N\pm 5\mu N$.

Table 5.3 Critical loads and friction coefficients of 90nm bare SiNLs

	Average Critical Load (uN)	Standard Deviation (uN)	Average Friction Coefficient	Standard Deviation
Mode II	194	16	0.051	0.002
Mode I	123	5	0.041	0.001

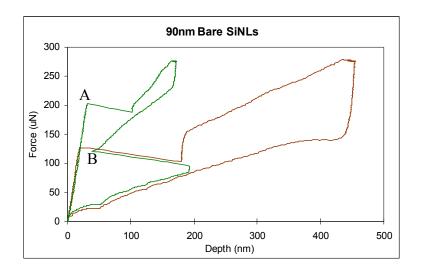


Figure 5.10Two sets of load-displacement curves were presented. One set of curve (green) showed two different displacement bursts, which indicated two different buckling models. One buckling occurred during the loading (marked as A), the other occurred at the unloading process (marked as B). On the other set of curve (brown), only one displacement burst was observed on the loading process.

The friction coefficients μ were determined based on FEM simulation by comparing the critical loads of simulated load-displacement curve and experimental load-displacement curve. The friction coefficients results were also summarized in

Table 5.3. The Mode II buckling mode yielded an average friction coefficient of 0.051 which is slightly larger than that of Mode I buckling mode at 0.041.

Next the frictional shear stress will be evaluated. In Chapter 1, the frictional shear stress τ was defined as

$$F_f = \tau A$$
,

where the contact area is evaluated in Section 2. The friction force F_f can be calculated according to the geometry and Equation 4.4,

$$F_f = \frac{\mu}{\cos\theta + \mu\sin\theta} \frac{F}{2} \approx \frac{\mu}{\cos\theta} \frac{F}{2}.$$

Therefore the frictional shear stress is

$$\tau = \frac{F_f}{A} = \frac{\mu}{A\cos\theta} \frac{F}{2},$$

where F is the experimentally measured critical buckling load. The frictional shear stress data are summarized in Table 5.4. The data show that the difference between shear stresses of Mode I and Mode II buckling is significant. In the case when there is a buckling mode transition, the initial buckling is Mode II buckling with high frictional shear stress but after experiencing the postbuckling loading process, a Mode I buckling occurs during the unloading process. The frictional shear stress reduced significantly in this process, indicating the contact history had a significant effect on friction. The contact

history effect is confirmed by nanoindentation experiments under cyclic loading which will be discussed in Section 5.

Table 5.4 Frictional Shear Stress of 90nm SiNLs

	Average	Average	Contact Area		Average Shear Stress	
	Critical	Friction	(10^{-14} m^2)		(MPa)	
	Load(μN)	Coefficient	Force	Disp	Force	Disp
			method	method	method	method
Mode II	194	0.051	2.2	2.17	225	228
Mode I	123	0.041	1.83	1.72	138	147

The buckling behavior for the 75nm SiNLs test structures was similar to the 90nm test structure. A buckling mode transition from Mode II to Mode I was observed in the nanoindentation experiments. The friction coefficient and frictional shear stress results are summarized in Table 5.5. Similarly, the Mode II buckling is due to high shear stress.

Table 5.5Frictional Shear Stress of 75nm SiNLs

	Average	Average	Contact Area		Average Shear Stress	
	Critical	Friction	(10^{-14} m^2)		(MPa)	
	Load(μN)	Coefficient	Force	Disp	Force	Disp
			method	method	method	method
Mode II	95	0.049	0.89	0.81	285	265
Mode I	64	0.041	1.12	0.95	138	117

5.3.2 Experimental results for 60nm/610nm and 30nm/720nm SiNLs

The same experimental protocols were repeated on SiNLs test structures of 60nm/610nm, and 30nm/720nm. Besides the difference of line widths, these two sets of test structures have different heights compared to test structures of 90nm/1400nm and 75nm/1400nm. According to analysis in Chapter 4, the chance to observe Mode II buckling for the 60nm test structures is much less because of the small aspect ratio. This is agreed by the experimental observation. However, models in Chapter 4 predicted a buckling mode transition for the 30nm test structures because they have the largest aspect ratio among all test structures. In experiments no significant buckling mode transition was observed. This may suggest that the friction force is not strong enough to initiate Mode II buckling, although the aspect ratio is larger. All the critical loads and friction coefficients are summarized in Table 5.6 and Figure 5.11 for bare SiNLs. Figure 5.12 shows the corresponding frictional shear stress. Some typical load-displacement curves are shown in Figure 5.13 and Figure 5.14.

It is interesting to note that the variations of critical loads and friction coefficients of the 30nm/720nm test structures were very large compared to other sets of test structures. Although the transfer of buckling modes was not observed, some of the friction coefficients were as large as 0.05 which is close to the average of friction coefficients of the Mode II buckling for the 90nm/1400nm and 75nm/1400nm test structures. For those buckling with large friction coefficients, Mode II buckling might have occurred as well, except that Mode I buckling did not occur during the unloading

process. Similar behaviors were observed by Bin Li in his buckling studies of the 24nm/380nm test structures.

Table 5.6 Summary of critical loads and friction coefficient

Linewidth	Buckling Mode	Average Critical Load (uN)	Standard Deviation (uN)	Average Friction Coefficient	Standard Deviation
90nm	Mode I	194	16	0.051	0.0019
	Mode II	123	5	0.041	0.0011
75nm	Mode I	95	6	0.049	0.0013
	Mode II	64	5	0.041	0.0013
60nm	Mode I	56	9	0.036	0.0055
30nm	Mode I	17	4	0.031	0.0098

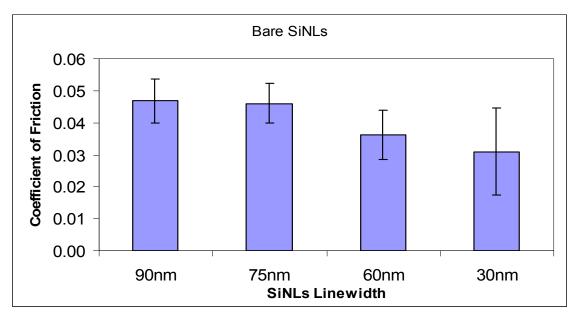


Figure 5.11 Average friction coefficients for test structures with width/height configurations of 90nm/1400nm, 75nm/1400nm, 60nm/610nm and 30nm/720nm.

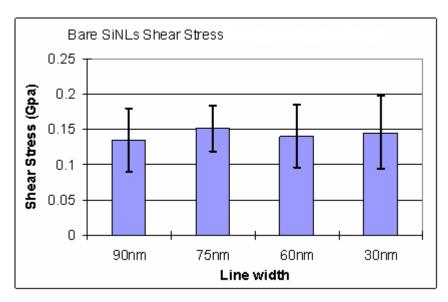


Figure 5.12 Average friction coefficients for test structures with width/height configurations of 90nm/1400nm, 75nm/1400nm, 60nm/610nm and 30nm/720nm.

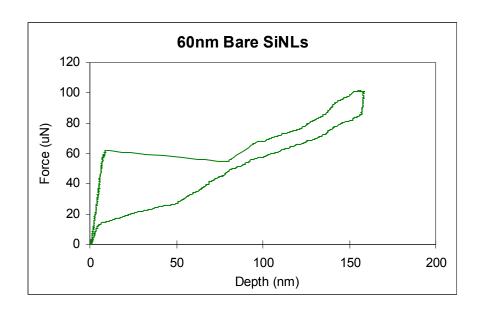


Figure 5.13 Typical load-displacement curve for the SiNLs of 60nm/610nm configuration. The critical load was 62 μ N, and corresponding friction coefficient was 0.043.

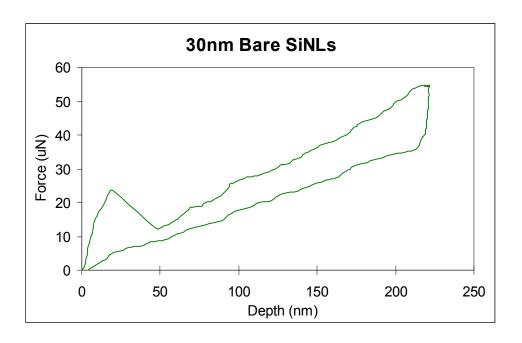


Figure 5.14 Typical load-displacement curve for 30nm/720nm SiNLs. The critical load is 23.7μ N, and corresponding friction coefficient is 0.042.

5.4 Friction of Coated SiNLs

In this section, the experimental data on SiNLs coated with thin layers of chromium and silicon dioxide are presented. Similarly, the friction behaviors of the nanocontact are analyzed based on the FEM simulation and the Coulomb's friction theory. Since the contact area is determined by the contact geometry for uniform materials, the contact area for SiNLs will be a constant with different coatings. Here the coating of Chromium and silicon dioxide was assumed to be uniform. Therefore, the frictional shear stress will have the same scaling trend as the friction coefficient. Consequently the frictional shear stress will not be discussed and presented in this section. But the discussion on friction coefficient applies to the frictional shear stress.

The bare SiNL test structures were reprocessed and coated with silicon dioxide or chromium for the studying of coating effect. The coating process was briefly discussed in Chapter 3. The coating layer were 3nm silicon dioxide and 2nm chromium.

The selection of indentation locations is important since there probably were some fractures or surface topography changes left on the structures that were indented in previous studies. We will show that the indentation history has significant effect on the buckling behavior and friction coefficients. Therefore, repeating nanoindentation on the previously indented structures is not desired. Our test structures were an array of SiNLs patterns arranged in a way that the patterns on one location were very similar in geometry and consequently mechanical properties to their nearest neighbors. Actually, dimensions measured by SEM images were almost identical for two patterns in the same neighborhood. For indentation experiments on the bare SiNLs, the patterns with best quality (whose line directions are supposed to be the closest to the intrinsic crystalline direction [112] of the (110) silicon wafer) were selected, and two patterns nearest to it were selected for subsequent studies for nanoindentation on SiNLs with chromium or silicon dioxide coatings.

Typical load-displacement curves are shown in Figure 5.15 or the 75nm/1400nm test structures where the blue curve is for bare SiNLs with the highest critical load, the red curve for SiNLs with oxide coating and the green curve for SiNLs with chromium layer. The average critical loads and corresponding friction coefficients are shown in Table 5.7.

Table 5.7 Average critical loads and friction coefficient of 75nm SiNLs

Coatings	Average Critical Load (uN)	Standard Deviation_(uN)	Average Friction Coefficient	Standard Deviation
Bare SiNLs	83	17	0.046	0.0062
SiNLs w/ Ox	46	9	0.031	0.0084
SiNLs w/ Cr	39	3	0.022	0.0062

These experiments provided a number of interesting observations regarding the effect of overcoating on the buckling and fracture behavior of SiNL test structures. The average critical loads therefore the friction coefficients of bare SiNLs were clearly higher than that of SiNLs with coatings. Also, the load-displacement curves overlap with each other before buckling occurs, which indicates the elastic response of SiNLs is determined by the geometry and mechanical properties of SiNLs instead of the contact surfaces. The unloading curves are very close to each other indicating that the coating and the small line width changes due to coating had small effect on the compliance of SiNLs structures too. Therefore, the change of critical loads can be attributed to the change of contact surfaces where the coatings of silicon dioxide and chromium layers could be viewed as lubricant layers, and the surface roughness and the contact singularities of the SiNLs might have been significantly altered by the coatings. The transfer of buckling mode II to mode I was not observed for either set of test structures coated with oxide or chromium layers. This is the direct evidence of smaller friction forces between coated SiNLs and indenter. The friction coefficients are summarized in

Figure 5.16, and it is clear from the figure that coating layers significantly decreased the friction forces.

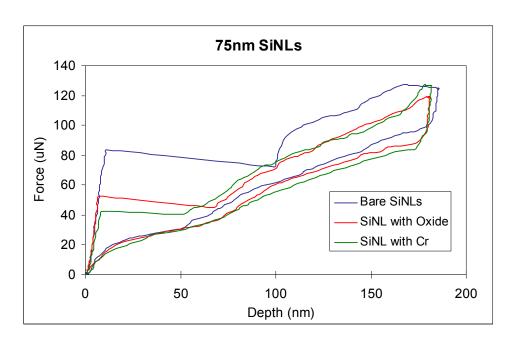


Figure 5.15 Typical load-displacement curves for 75nm/1400nm test structures with or without coating layers: blue curve for bare SiNLs with the highest critical load, red curve for SiNLs with oxide and green curve for SiNLs with chromium layer.

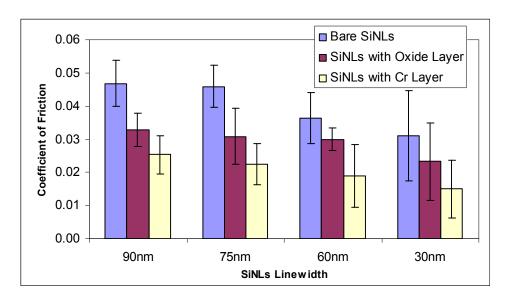


Figure 5.16 Comparison of the friction coefficients of SiNLs with different line widths and coatings.

5.5 Friction of SiNLs under cyclic loading

It has been widely agreed that friction will change the surface of contact. For example, friction activates the surface reaction sites by bond stretching, breaking and reformation. Friction welding and doping have already been implemented in industry or laboratory as standard manufacturing processes. It was also found that contact pressure on silicon could induce brittle-to-ductile solid phase transitions at room temperature. In previous sections, we have presented the indentation results of SiNLs under single-cycle loading condition. In this section, multi-cycle loading nanoindentation experiments were designed to investigate the effect of indentation history on the buckling responses and frictional behaviors of SiNLs, which can help us to understand the physical process that occurred at the SiNLs surface due to friction and contact pressure.

We performed multi-cyclic nanoindentation experiments following the same experimental steps as the single-cycle loading indentation. The load functions were defined to control the system to perform cyclic loading-unloading indentation automatically. Figure 5.17 shows a typical and generally used load function in our multi-cycle loading experiments. First, the load increases at a constant rate of 75µN/second to reach the maximum loading force. Then the load was held at constant at the maximum loading forces for one second before the load started to decrease at a constant rate of 75µN/second until the loading force reaches zero. After the first loading-unloading cycle, the indenter was allowed to rest for one second before the second loading cycle was started to repeat the same process as the first loading cycle. A total of four loading cycles

were designed. More cycles can be designed but longer time is required to finish the experiments, which is not desired especially when signal drifting existing.

Figure 5.18 shows the load-displacement curve for 90nm bare SiNLs under multicycle loading. The load function used was defined as shown in Figure 5.17 with four total loading cycles and maximum loading forces of $150\mu N$ for all cycles. The load-displacement of first loading cycle was marked by the green in the figure, having a critical load of $128\mu N$. The second loading cycle was marked by pink with a critical load of $96\mu N$. The third loading cycle (yellow curve) gave a critical load of $87\mu N$. And the last loading cycle was the blue curve having a critical load of 84. The critical loads and corresponding friction coefficients for this set of data was summarized in Table 5.8.

Table 5.8 Critical loads and friction coefficients of 90nm SiNLs under a 4-cycle loading experiment

	1 st cycle	2 nd cycle	3 rd cycle	4 th cycle
Critical loads (μN)	128	96	87	84
Friction coefficients	0.042	0.035	0.031	0.030

It is noted interesting that in the load-displacement curves, the elastic response of each loading cycle is consistent with each other. As we mentioned before, when the maximum loading forces were not large enough for the occurrence of fracture, the displacement of SiNLs fully recovered after the indenter withdrawal, and the strain of failure of SiNLs were as large as \sim 7%, indicating a superior mechanical strength of the structures[79]. Here, under multi-cycle loading indentation, we found that not only the displacement of SiNLs fully recovered after each cycle but the stiffness of the elastic

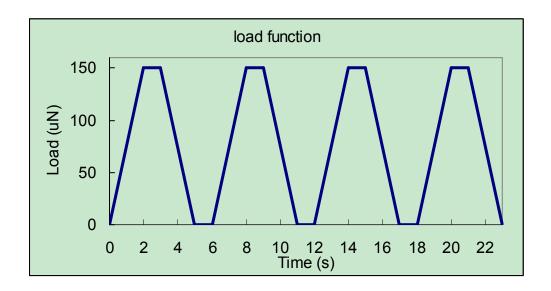


Figure 5.17 Load function of multi-cycle loading indentation. Four cycles were designed with the same maximum loading forces for each loading cycle at 150 μ N. The loading and unloading rates were also designed constant for each cycle at 75 μ N/second and -75 μ N/second, respectively.

response of SiNLs remained the same. Interestingly, it was found that the critical buckling loads dropped significantly after the first indentation cycle. For the second and third cycles, averagely critical loads dropped slightly. The phenomena suggest that the indentation history poses significant impact on the contact surfaces; however the impact on the mechanical strength of SiNLs is small.

We repeated the data acquisition by shifting the indenter to different locations on the SiNLs structures. The results showed very good repeatability. By comparison, we repeated the multi-cycle loading experiment one more time on the same location as the previous multi-cycle loading experiment; the critical loads were pretty close to smallest critical load in the previous experiment, as shown in Figure 5.19 where friction coefficients of the second 4-cycle loading were colored by pink. Those results implied that, the impact of the indentation was mainly on the contact surfaces of SiNLs, instead of the indenter surface which is made of diamond with much higher modulus.

Similar results were obtained on different sets of SiNLs test structures with different coatings. As an example, representative load-displacement curves for multicycle loading experiments on 60nm SiNLs without coating (bare SiNLs) and with coating of silicon dioxide or chromium layers are shown in Figure 5.20.

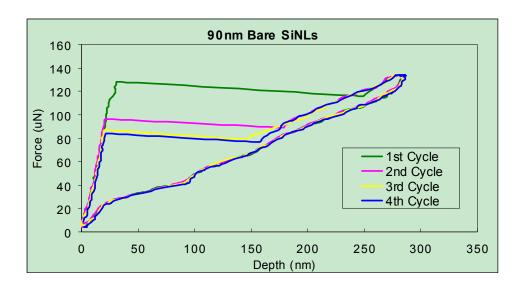


Figure 5.18 Load-displacement curves of 90nm SiNLs under multi-cycle loading. The load function was defined in Figure 5.17 with four total loading cycles and maximum loading forces of $150\mu N$ for all cycles.

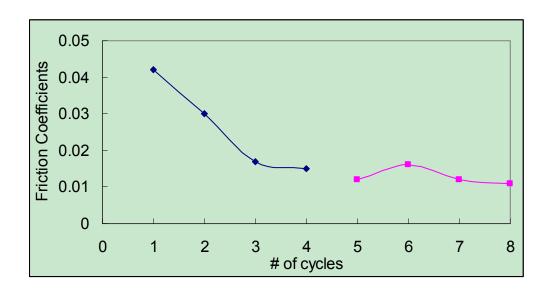


Figure 5.19 Friction coefficients on 90nm SiNLs after two runs of 4-cycle loading indentation on the same location. Data points in blue were generated by the first 4-cycle loading and the pink data points were generate by the second 4-cycle loading. The same load function shown in Figure 5.17 was used for both runs of 4-cycle loading indentation.

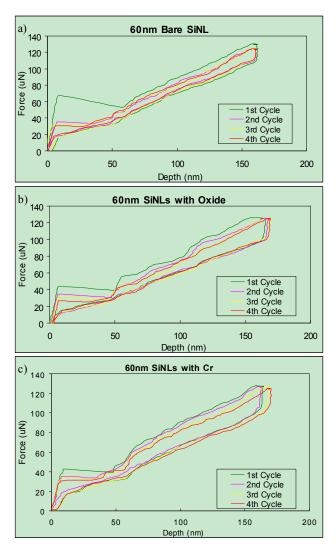


Figure 5.20 Load-displacement curves for 60nm SiNLs with coatings under 4-cycle loading indentations. The critical loads of the second cycle clearly dropped from that of the first cycle. The decrease of critical load after the first cycle was more significant for bare SiNLs as shown in a), than that of SiNLs coated with silicon dioxide shown in b) and chromium shown in c). Load function shown in Figure 5.17 was used for all experiments.

As one can notice that the critical load decreased more significantly for bare SiNLs than that did for SiNLs with silicon dioxide coatings or chromium coatings. In this case, the coatings served not only as lubricating layer but also as a passivation layer to

protect the silicon surface from morphology changes such as plasticity and phase transitions.

Another interesting phenomenon is that the unloading curves match very nicely for each loading cycle, which may indicate the cyclic loading has little effect on the sliding friction. More understanding are needed for future study of the mechanics responses and friction behaviors after the buckling occurrences.

Since no residual deformation left after indentation, it could be concluded that the contact history did not cause significant geometry change of SiNLs. Therefore, based on the same discussion in Section 5.4, the frictional shear stress should follow the same trend as the friction coefficient. Thus the contact history should significantly decrease the frictional shear stress of SiNLs, particularly after the first indentation cycle.

5.6 Summary

In Chapter 5, we investigated the effects due to the test environment and the contact materials. The study on the environmental effect showed that humidity did not have an apparent effect on the buckling behavior. The reason can be attributed to the high contact pressure between the indenter and SiNLs surface, which squeezed out the water layer. This led to the building up of an intimate contact where the reactive stress overwhelmed the stress due to water adhesion.

This justified the selection of the Hertzian contact model over the DMT, JKR or Maugis models to evaluate the contact area and the friction coefficient. On this basis, the frictional shear stress was calculated for all test structures. The results showed that the

shear stress was independent on the line width of SiNLs and thus provided a better description of the friction properties of the contact materials.

The critical buckling load was found to decrease when the surface was coated with a silicon dioxide or chromium layer. This can be attributed to the change of contact surfaces due to overlayer coatings. The coating may minimize the surface roughness and the contact singularities of the SiNLs, resulting in a reduction of the critical load for buckling. This was evidenced by the fact that the transfer of buckling mode II to mode I was not observed for either set of test structures with oxide or chromium coating.

Under multi-cycle loading conditions, the critical buckling loads dropped significantly after the first loading cycle. However, the mechanical strength of the SiNLs test structures remained the consistent for each loading cycle. The contact history therefore has significant impact on the contact surface but little impact on the SiNLs.

Chapter 6: Summary and Future Work

6.1 Summary

In this thesis work, we report a study of the mechanical behavior and contact friction of silicon nanolines (SiNLs). The mechanical responses, especially the buckling behavior and nanofriction of SiNLs, were studied by a nanoindentation technique. For this study, we have developed a process based on e-beam lithography and anisotropic etching which yielded SiNLs with line width as small as 25nm and with vertical sidewalls almost atomically smooth. Using such structures, we have investigated the deformation behavior of SiNLs and to measure the contact friction as a function of materials and nanoline dimensions. The results of this study are presented in three chapters: in Chapter 3, the fabrication process of SiNLs; in Chapter 4, the buckling behavior of the silicon nanolines and in Chapter 5, the nanofriction of the SiNLs.

The process developed to fabricate SiNLs test structures was described in Chapter 3. This process was based on a combination of high resolution EBL and high quality pattern transfer by AWE. The combination of these two techniques enabled us to obtain vertical and smooth single-crystal SiNLs on (110) orientated Si. This fabrication process yielded SiNLs with potential applications for nanograting-based sensors and interconnects. They were well-suited for quantitative studies of mechanical and friction properties of silicon-based structures at the nanoscale.

In Chapter 4, we report the results obtained from the study of the mechanical behavior and friction properties of SiNLs using a nanoindentation technique. The SiNLs test structures used in our experiments had height to width ratio from 10 to 20, making it well suitable for the study of buckling behaviors. The loading-displacement indentation curves showed that the critical load to induce the buckling of the SiNLs can be correlated to the contact friction of the nano-indenter, the geometry of SiNLs, and the eccentricity of the applied load. A map was built as a guideline to describe the buckling modes observed. The map was divided into three regions where different regions correlate to different buckling modes including Mode I, Mode II and sliding-bending of SiNLs. This map agreed very well with the indentation results observed experimentally.

In Chapter 5, we investigated the effects due to the test environment and the contact materials. The study on the environmental effect showed that the water intermediate layer did not have an apparent effect on the buckling behavior. The reason can be attributed to the high contact pressure between the indenter and SiNLs surface which squeezed out the water layer. This led to the building up of an intimate contact where the reactive stress overwhelmed the stress due to water adhesion. This verified the use of a Hertzian contact model to evaluate the contact area and the friction coefficient. On this basis, the frictional shear stress was calculated for all test structures. The results showed that the shear stress was independent on the line width of SiNLs and thus provided a better description of the friction properties of the contact materials.

The critical buckling load was found to decrease when the surface was coated with a silicon dioxide or chromium layer. This can be attributed to the change of contact surfaces due to the oxide or the chromium coating which apparently served as a lubricant layer. The coating minimized the surface roughness and the contact singularities of the SiNLs resulting in a reduction of the critical load for buckling. This was evidenced by the

fact that the transfer of buckling mode II to mode I was not observed for either set of test structures with oxide or chromium coating.

Under multi-cycle loading conditions, the critical buckling loads dropped significantly after the first loading cycle. However, the mechanical strength of the SiNLs test structures remained the consistent for each loading cycle. The contact history therefore has significant impact on the contact surface but little impact on the SiNLs.

6.2 Future Work

The average contact pressure on the SiNLs is on the order of 10GPa. Considering the maximum contact pressure on asperities could be even higher than 10GPa, the local contact pressure could be higher than 12GPa, which is around the contact pressure that induces phase transformation of single-crystalline silicon. If phase transformation occurs for the SiNLs in the nanoindentation experiments, the friction bonding nature could be changed. Other probable changes of SiNLs under the nanoindentation include the initiation of dislocations or micro-cracks. A closer look at the interfaces of contact and perimeters are needed to understand the mechanisms of the effect of contact history on friction. We have performed TEM imaging experiments on the sidewalls of SiNLs. From the TEM images, a 10nm band was discovered which has apparently different contrast compared to other regions of the images. There might have micro-structural changes or dislocations in the regions which are 10nm away from the contact interface. More systematic studies and TEM imaging could help to understand the mechanisms of contact history.

The thickness of the coated silicon dioxide was 3nm, and the effect of surface coating was significant on friction compared with bare SiNLs. Considering the thickness

of native oxide is around 1nm on the bare SiNLs, it is interesting to study the friction behavior as a function of coating thickness. The results of this study could reveal the effective friction bonding distance between silicon and diamond. The effect of contact history could be very interesting if the thickness of the coating layer is around a critical thickness.

The friction coefficients of 30nm SiNLs exhibited the largest variation. This observation was similar to the 24nm SiNLs study by Bin Li. And we argued that Mode II buckling actually did occur but we did not observe the second displacement burst on the load-displacement curves, which means a transition of Mode II buckling to Mode I buckling was not observed on the unloading process. The mechanism that determines the transition of buckling mode is still not clear.

To derive an analytical solution of the buckling modes, 2D modes were employed in current study. The confinement effect of SiNLs due the length and the spherical shape of indenter were not studied. More accurate modes considering the 3D effect could help to build a better map of buckling mode and solve the problem of transition of buckling mode.

Diamond indenter was used in this study, and the SiNLs was coated with silicon dioxide or chromium. Another way of changing the contact material is using another indenter with different material, such as tungsten or silicon carbide.

Our nanoindenter system has the capabilities to perform nanoscratching test. The nanoscratching test measures the lateral forces directly and it could provide a great complimentary study to the nanoindentation. Actually, preliminary studies showed consistent results with those two methods. To perform nanoscratching test, new test structures with larger pitches and larger linewidth might be helpful at the starting point to understand the mechanical behaviors of SiNLs. The lateral forces with current test

structures were in range of $0.5\mu N$ to $2\mu N$. With larger linewidth, the lateral forces will increase. With larger pitches, the interaction between SiNLs can be disentangled.

Selected Publications

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120