Energy Time Series Forecasting Based on Pattern Sequence Similarity

Francisco Martínez-Álvarez, Alicia Troncoso, José C. Riquelme, and Jesús S. Aguilar-Ruiz

Abstract—This paper presents a new approach to forecast the behavior of time series based on similarity of pattern sequences. First, clustering techniques are used with the aim of grouping and labeling the samples from a data set. Thus, the prediction of a data point is provided as follows: first, the pattern sequence prior to the day to be predicted is extracted. Then, this sequence is searched in the historical data and the prediction is calculated by averaging all the samples immediately after the matched sequence. The main novelty is that only the labels associated with each pattern are considered to forecast the future behavior of the time series, avoiding the use of real values of the time series until the last step of the prediction process. Results from several energy time series are reported and the performance of the proposed method is compared to that of recently published techniques showing a remarkable improvement in the prediction.

Index Terms—Time series, forecasting, patterns.

1 INTRODUCTION

T HE analysis of temporal data and the prediction of future values of time series are among the most important problems that data analysts face in many fields, ranging from finance and economics, to production operations management or telecommunications.

A *forecast* is a prediction of some future event(s). Forecasting problems are often classified as short-term, medium-term, and long-term. Short-term forecasting problems involve predicting events only a few time periods (days, weeks, months) into the future. Medium-term forecasts extend from one to two years and long-term forecasting problems can extend beyond that by many years.

Time series data can be defined as a chronological sequence of observations on a variable of interest. Most forecasting problems imply the use of such data whose analysis has traditionally been done by means of classical statistical tools. Nowadays, data mining techniques are acquiring a great relevance due to the large number of samples forming the time series in multiple areas.

A new approach, called Pattern Sequence-based Forecasting (PSF), is here presented in order to forecast time series. This work can be considered a generalization of the algorithm introduced in [33], which is based on nearest neighbors techniques. Nevertheless, the new approach makes predictions using only labels generated by means of clustering techniques. This fact discretizes and simplifies the process of prediction, since during the whole process, the PSF algorithm deals with sequences of labels instead of with sets of real values. Despite that a naive use of labels to predict time series was presented in [21], the PSF includes a new methodology to automatize the obtaining of the labels providing rules to assign them to the samples of real values. The sensitivity of the key parameter involved in the selection of the number of underlying patterns is also analyzed in order to study the robustness of the method. The number of labels comprising the pattern sequence, used in each prediction process, is systematically determined in this work.

The PSF algorithm aims to be a general-purpose forecasting procedure. However, electricity-related problems are addressed in this work. To be precise, two major groups of time series are forecasted: electricity prices and electricity demand. These groups belong to three different markets: the Spanish Electricity Market Operator (OMEL), the New York Independent System Operator (NYISO), and the Australia's National Electricity Market (ANEM). Therefore, the overall experimentation consists of six independent time series showing thus the adaptability of the PSF to miscellaneous time series. Moreover, in order to facilitate the comparison of the obtained results, all the data sets analyzed are available online [19], [25], [26].

The rest of the paper is organized as follows: Section 2 presents an exhaustive revision of the state of the art on electricity prices and demand time series forecasting. Section 3 introduces the proposed methodology and the description of the PSF algorithm, which can be applied to time series of any nature. Section 4 shows the results obtained by the PSF approach in electric energy markets of Spain, Australia, and New York for the whole year 2006, including measures of the quality of them. In Section 5, comparisons between the proposed method and other techniques are provided. Finally, Section 6 summarizes the main conclusions achieved and gives clues for future work.

2 RELATED WORK

The forecasting of energy time series has been widely studied in literature, as it is described in Sections 2.1 and 2.2.

2.1 Electricity Prices Time Series Forecasting

The electric power markets have become competitive markets due to the deregulation carried out in the last years, allowing the participation of all producers, investors, traders, or qualified buyers. Thus, the price of the electricity is determined on the basis of this buying/selling system. Consequently, a will of obtaining optimized bidding strategies has arisen in the electricity-producer companies [29], needing both insight into future electricity prices and assessment of the risk of trusting in predicted prices.

Electricity prices time series presents some peculiarities such as nonconstant mean and variance as well as the presence of outliers that turns the forecasting into a specially difficult task. Due to this fact, the accomplishment of accurate forecasting has motivated research works by many authors nowadays [2], [37].

The authors in [7] used the wavelet transform and autoregressive integrated moving average (ARIMA) models to predict the day-ahead electricity price. Indeed, they first used the wavelet transform to split the available historical data into constitutive series. Then, specific ARIMA models were applied to these series and the forecasts were obtained by applying the inverse wavelet transform to the forecasts of these constitutive series. In [15], ARIMA models, selected by means of Bayesian Information Criteria, were proposed to obtain the forecasts of the prices. In addition, the work analyzed the optimal number of samples used to build the prediction models. Aggarwal et al. [3] divided each day into segments and they applied a multiple linear regression to the original series or the constitutive series obtained by the wavelet transform depending on the segment. Moreover, the regression model used different input variables for each segment.

Equally noticeable was the approach proposed by García et al. [14] in which a forecasting technique based on a generalized autoregressive conditional heteroskedasticity (GARCH) model was presented. Hence, this paper focused on day-ahead forecast of electricity prices with high volatility periods.

Transfer functions models based on past electricity prices and demand were proposed to forecast day-ahead electricity prices by Nogales and Conejo [24], but the prices of all 24 hours of the previous day were not known. They used the median as measure due to the presence of outliers and they stated that the model in which the demand was considered presented better forecasts.

Weron and Misiorek [38] presented 12 parametric and semiparametric time series models to predict electricity prices for the next day. Moreover, in this work, forecasting intervals were provided and evaluated taking into account the conditional and unconditional coverage. They concluded that the intervals obtained by semiparametric models are better than that of parametric models.

A hybrid model that combined artificial neural networks (ANN) and fuzzy logic was introduced in [4]. As regards the neural network presented, it had a feed-forward architecture and three layers, where the hidden nodes of the proposed fuzzy neural network performed the fuzzification process. Following with this technique, another neural network-based approach was introduced in [5] in which multiple combinations were considered. These combinations consisted of networks with different number of hidden layers, different number of units in each layer,

and several types of transfer functions. Recently, Pindoria et al. [28] proposed an artificial neural network in which the output of the hidden layer neurons was based on wavelets that adapted their shape to training data.

A modification of the weighted nearest neighbors (WNN) methodology is proposed in [33]. To be precise, the approach weighted the nearest neighbors in order to improve the prediction accuracy.

The occurrence of outliers (also called spike prices) or prices significantly higher than the expected values is a usual feature found in these time series. With the aim of dealing with this feature, the authors in [41] proposed a data mining framework based on both support vector machines (SVM) and a probability classifier.

Recently, a fuzzy inference system—adopted due to its *transparency and interpretability*—combined with traditional time series methods was proposed for day-ahead electricity price forecasting [18].

2.2 Electricity Demand Time Series Forecasting

The process of forecasting the quantity of electricity required for a specific geographical area during a time period is called load forecasting or demand forecasting. This process is key since current technology allows to store only little amount of electricity in batteries. Therefore, the demand forecasting plays an important role for electricity power suppliers because both excess and insufficient energy production may lead to large costs and significative reduction of benefits.

Load forecasting has been widely studied [31], [37]. The existing procedures are usually divided into two main groups [13]. The first one gathers traditional approaches such as regression, data smoothing techniques, or Box and Jenkin's models. Thus, the authors in [27] focused on the one year-ahead prediction for winter seasons by defining a new Bayesian hierarchical model. They provide the marginal posterior distributions of demand peaks. Also in [8], Bayesian models are used to forecast electricity demand. Moreover, a multiple linear regression model to forecast electricity consumption using some input variables such as the gross domestic product, the price of electricity, and the population was proposed in [23].

Taylor et al. [32] compared six univariate time series methods to forecast electricity load for Rio de Janeiro and England and Wales markets. These methods were an ARIMA model and an exponential smoothing (both for double seasonality), an artificial neural network, a regression model with a previous principal component analysis, and two naive approaches as reference methods. The best method was the proposed exponential smoothing and the regression model showed a good performance for the England and Wales demand.

With reference to the second main group, it gathers artificial intelligence techniques among which expert systems, neural networks, and fuzzy theory are the most popular [22]. In [11], the authors discussed and presented results by using an ANN to forecast the Jordanian electricity demand, which is trained by a particle swarm optimization technique. They also showed the performance obtained by using a back-propagation algorithm and autoregressive moving average (ARMA) models. An ANN-based forecasting technique can also be found in [30]. Another proposal can be found in [36], where a forecasting algorithm based

on Gray Models was introduced to predict the load of Shanghai. In the Gray model, the original data series was transformed to reduce the noise of the data series and the accuracy was improved by using Markov chains techniques. Fan et al. [12] proposed a hybrid machine learning model based on Bayesian classifiers and SVM. First, Bayesian clustering techniques were used to split the input data into 24 subsets. Then, SVM methods were applied to each subset to obtain the forecasts of the hourly electricity load. In [34], the authors proposed a methodology based on WNN techniques. The proposed approach was applied to the 24-hour load forecasting problem and they built an alternative model by means of a conventional dynamic regression (DR) technique to perform a comparative analysis. In [1], the performance of ANN, fuzzy networks, and ARIMA models was evaluated to forecast the electricity demand time series in Victoria and the results showed that the fuzzy neural network outperformed the plain ANN and ARIMA models. Finally, Wang and Wang [35] proposed a new prediction approach based on SVM techniques with a previous selection of features from data sets by using an evolutionary method. The creation of hybrid methods that highlight most of the strengths of each technique is currently the most popular work among the researchers. And, from all hybrid methods, the combination of ANN and fuzzy set theory has become a new tool to be explored.

3 THE PROPOSED METHODOLOGY

The proposed methodology is divided into two phases clearly differentiated. In a first step, a clustering technique is performed and, second, the phase of forecasting is applied by using the information provided by this clustering. The PSF algorithm is focused on predicting samples framed in a time series, either one dimensional or multidimensional, previously labeled with clustering techniques. As soon as the clustering is applied, the algorithm only processes the number of the cluster—the label associated with each pattern—assigned to the samples, ignoring if they had more than one feature.

With the PSF method, the horizon of prediction can be as long as desired. Hence, more than one sample can be predicted, making predictions of nonrestricted length. This fact is possible because it is implemented with a close loop that feeds the prediction of a sample back in the data set in order to predict the following sample. As a consequence, the PSF approach is able to insert the predicted samples in the data set with the aim of forecasting further samples. Therefore, in case the horizon of prediction was longer than one day, every predicted sample would be inserted into the data set and considered to be a regular sample. This feature is specially useful when the prediction has to cover various days or a long-term prediction is required.

Fig. 1 shows the basic idea behind the proposed methodology. All the steps composing this methodology are going to be described in subsequent sections.

3.1 Data Normalization

The first task to be completed is the normalization of data that is only used for the clustering process. It can be assumed that the prices increase all along the year following a tendency in accordance with the intra-annual inflation.



Fig. 1. Illustration of the proposed methodology. The clustering and prediction stages are further detailed.

That is, the original trend is smoothed from the initial data. The transformation applied is

$$x_j \quad \frac{x_j}{\frac{1}{N}\sum_{i=1}^N x_i},\tag{1}$$

where x_j is the price/demand of the *j*th hour of a day and N is equal to 24 since each value represents one hour of the day.

3.2 Clustering Technique

Given the database of hourly prices/demand, the clustering problem consists of identifying K groups or clusters such that the prices/demand curves of the days belonging to a cluster are similar among them and dissimilar to the curves of those days belonging to other clusters, according to a distance. Clustering is a difficult task due to the great number of possible geometric shapes for the clusters and distances that can be considered.

As a consequence, the dimensionality of the database is drastically reduced from its initial 24 features (equivalent to the 24 hours of the day) to only one dimension (the label of the cluster to which the day belongs).

To achieve this challenge, two questions should be answered: which clustering technique should be chosen? And, if appropriate, how many clusters should be created?

These two topics have widely been discussed in the literature [39]. Nevertheless, it seems that there is not a unique answer because it depends on sensitive factors.

The crisp and fuzzy clustering are the two main branches of nonsupervised classification. The discussion of choosing one technique or another can be found in [20], in which the well-known K-means algorithm was the optimal method to classify this kind of data set. For this reason, the K-means algorithm is the clustering technique used in this work during the whole process of prediction.

The K-means algorithm requires that the user provides the number of clusters to be created. However, this number is a priori unknown and its selection and later evaluations of the results obtained by the clustering are crucial for most engineering applications. Thus, the most challenging problem of the clustering realm has been to select the right number of clusters for data sets. For all these reasons, three well-known validity indices have been applied to data in order to decide how many groups the original data set has to be split into: silhouette index [16], Davies-Bouldin (DB) index [9], and the Dunn (DU) index [10]. The three of them share a common feature: the new data structure obtained by the clustering algorithm is evaluated to test the validity of the partition.

The procedure to select the number of clusters to be generated, K, is now discussed. From the application of these three indices (see Sections 3.2.1, 3.2.2, and 3.2.3), two possible situations can appear: at least two indices—the majority—coincide in selecting the same K (the K eventually chosen) or none of them coincide. When the second situation occurs, the second best values of the three indices are also considered (together with the first best values). The K selected is, then, the one pointed by the majority of all the cases. Further, best values will be included and analyzed until one K had more votes than the others.

3.2.1 The Silhouette Index

The *silhouette function* provides a quality measure of separation among the clusters obtained by using a clustering technique. The average distance of the object *i* belonging to the cluster *A* to all the objects in *A* is denoted by a(i) and the average distance of *i* to all objects of the cluster $C \neq A$ is called d(i, C). For every cluster $C \neq A$, d(i, C) is computed and the smallest one is selected as follows:

$$b(i) = \min_{C \neq A} d(i, C) \text{ with } i \in A.$$
(2)

The value b(i) represents the dissimilarity of the object i to its nearest neighbor cluster. Thus, the silhouette values, silh(i) are given by the following equation:

$$silh(i) = \frac{a(i) - b(i)}{max\{a(i), b(i)\}}.$$
 (3)

The silh(i) can range from -1 to +1, where +1 and -1 mean that the object i belongs to an adequate and inadequate cluster, respectively. If the silhouette value of the object i belonging to the cluster A is close to zero, it means that the object i can also be in the nearest neighbor cluster to A. If cluster A is a set with only one element, the silhouette value of the object i is not defined and in this case, it is concerted to be equal to zero. The objective function is the average of silh(i) over the number of objects to be classified, and the best clustering is reached when this function is maximized.

3.2.2 The Dunn Index

One of the most cited indices was proposed in [10]. The Dunn index aims to identify clusters with high intercluster distance and low intracluster distance. The Dunn index for K clusters C_i with i = 1, ..., K is defined by

$$DU_K = \min_i \min_{j \neq i} f_{i,j}, \tag{4}$$

where

$$f_{i,j} = \frac{d(C_i, C_j)}{max_m \, diam(C_m)}.$$
(5)

 $d(C_i, C_j)$ is the dissimilarity between clusters C_i and C_j defined by

$$d(C_i, C_j) = \min_{x \in C_i \atop y \in C_j} ||x - y||,$$
(6)

and diam(C) is the intracluster function or diameter of the cluster defined by this equation

$$diam(C) = \max_{\substack{x,y \in C}} ||x - y||, \tag{7}$$

where $\|\cdot\|$ represents a norm.

In short, the existence of compact and well separated clusters is guaranteed if the Dunn index reaches high values. Therefore, the maximum is observed for the most probable number of clusters in the data set.

3.2.3 The Davies-Bouldin Index

The Davies-Bouldin index identifies as good clusters those compact clusters which are far from each other. Davies-Bouldin index for K clusters C_i with i = 1, ..., K is defined according to

$$DB_{K} = \frac{1}{K} \sum_{i=1}^{K} \max_{j \neq i} f_{i,j},$$
(8)

where

$$f_{i,j} = \frac{diam(C_i) + diam(C_j)}{d(C_i, C_j)},\tag{9}$$

and, in this case, the diameter of a cluster is defined as

$$diam(C_i) = \frac{1}{n_i} \sum_{x \in C_i} ||x - z_i||^2 \Big)^{\frac{1}{2}},$$
(10)

with n_i the number of points and z_i the centroid of cluster C_i .

The existence of high-quality clusters is guaranteed if the Davies-Bouldin index reaches small values. Therefore, the optimal number of clusters is found when this index is minimized for the data set.

3.3 The PSF Algorithm

Given the hourly prices/demand recorded in the past, up to day d - 1, the forecasting problem aims at predicting the 24-hourly prices/demand corresponding to day d.

Let $X(i) \in \mathrm{IR}^{24}$ be a vector composed of the 24-hourly energy prices/demand corresponding to a certain day *i*

$$X(i) = [x_1, x_2, \dots, x_{24}].$$
 (11)

Let $L_i \in \{1, ..., K\}$ be the label of the prices/demand of the day *i* obtained as a previous step to the forecasting by using a clustering technique, where *K* is the number of clusters. Let S_W^i be the sequence of labels of the prices/demand of the *W* consecutive days, from day *i* backward, as follows:

$$S_W^i = [L_{i-W+1}, L_{i-W+2}, \dots, L_{i-1}, L_i],$$
(12)

where the length of the window, *W*, is a parameter to be determined (see Section 3.4).

The PSF algorithm for the prediction of the hourly prices/ demand of the day d first searches for the sequences of labels



Fig. 2. PSF algorithm.

which are exactly equal to S_W^{d-1} in the database, providing the equal subsequences set, ES_d , defined by this equation

$$ES_d = \left\{ j \text{ such that } S_W^j = S_W^{d-1} \right\}.$$
(13)

In case of finding no sequences in database equal to S_W^{d-1} , the procedure searches for the sequences of labels which are exactly equal to S_{W-1}^{d-1} and thus successively. That is, the length of the window composed of the sequence of labels is decreased in one unit. This strategy guaranties that at least some sequences will be found when W is equal to 1.

According to the PSF approach, the 24-hourly values of the time series for the day d are predicted by averaging the values of the days following those in ES_d

$$\widehat{X}(d) = \frac{1}{\text{size } (ES_d)} \cdot \sum_{j \in ES_d} X(j+1), \tag{14}$$

where size(ES_d) is the number of elements that belong to the set ES_d .

The full procedure of the PSF algorithm is detailed in Fig. 2 and a general scheme is presented in Fig. 3. The symbol \triangleright stands for "*append*" (insert at the end).

In case of a medium- or long-term prediction, in which the forecasting of more than one sample is required, the following tasks have to be carried out. First of all, the values of the predicted sample are linked to the whole data set. Second, the clustering process is repeated with the enlarged data set and, finally, the prediction step is performed (see Fig. 1).

3.4 Determining the Size of the Window

The previous clustering generates a sequence of labels associated with every day (in Fig. 2, the sequence of numbers are these labels). Now, a sequence of labels is taken into consideration for further steps; concretely, if the day *d* has to be predicted, the sequence of labels $S_W^{d-1} = [L_{d-W}, L_{d-W+1}, \ldots, L_{d-2}, L_{d-1}]$ is extracted from the data set

and is used as a pattern of search, where W is the length of this sequence (or window).

The selection of W depends on the case under study but it can be systematically tuned. Thus, it is compulsory to perform a training phase to find an adequate value of Wbefore applying the PSF approach.

The optimal number of labels comprising the window (parameter *W*)—that will be used as a pattern of search to find all equal sequences of labels in data set—is determined by minimizing the forecasting error when the PSF method is applied to a training set.

Mathematically, that means to find the value of W that minimizes the following function:

$$\sum_{d \in TS} \|\widehat{X}(d) - X(d)\|,\tag{15}$$

where $\hat{X}(d)$ are forecasted prices/demand for day d, according to the PSF method, X(d) are actual recorded prices/demand, and TS refers to the training set. Notice that, according to (14), $\hat{X}(d)$ is an implicit function of the discrete variable W. Hence, the application of standard mathematical programming methods is not possible when searching for W.

In practice, *W* is calculated by means of cross validation. The cross validation was originally defined as: "the statistical practice of partitioning a sample of data into subsets such that the analysis is initially performed on a single subset, while the other subsets are retained for subsequent use in confirming and validating the initial analysis" [17].

In this work, the *n*-fold cross validation is used to obtain the optimal value of *W*. In *n*-fold cross validation, the original data set is split into *n* subsets. From all the *n* subsets, one subset is used to validate the model, which is generated by the remaining n - 1 subsets. Thus, this process is repeated *n* times, using each of the *n* subsets exactly once to validate. The *n* results are then combined—usually averaged—in Input: Dataset D, number of clusters K, labeled dataset $[L_1, L_2, ..., L_{d-2}, L_{d-1}]$, length of the window W and Test Set T **Output:** Forecasts $\widehat{X}(d)$ for all days of T $\mathbf{PSF}()$ $ES_d \leftarrow \{\}$ $\widehat{X}(d) \leftarrow 0$ for each day $d \in T$ $S_W^{d-1} \leftarrow [L_{d-W}, L_{d-W+1}, \dots, L_{d-2}, L_{d-1}]$ for each j such as $X(j) \in D$ $S_W^j \leftarrow \left[L_{j-W+1}, L_{j-W+2}, \dots, L_{j-1}, L_j \right]$ $\mathbf{if}(S_W^j = S_W^{d-1}) \\ ES_d \leftarrow ES_d \bigcup j$ for each $j \in ES_d$ $\hat{X}(d) \leftarrow \hat{X}(d) + X(j+1)$ $\widehat{X}(d) \leftarrow \widehat{X}(d) / size(ES_d)$ $D \leftarrow D \triangleright \widehat{X}(d)$ $[L_1, L_2, ..., L_{d-1}, L_d] \leftarrow \text{clustering}(D, K)$ $d \leftarrow d + 1$ **return** $\widehat{X}(d)$ for all days of T

Fig. 3. A general scheme of the algorithm PSF.

order to generate the final estimation. The advantage of this method lies on the use of all samples for both training and validation.

For the training phase, 12 folds have been used in this work (n = 12), where each fold represents a month of the year under study. The 12-fold cross validation is then evaluated. The forecasting errors are calculated in every fold by varying the length of W. These monthly errors are denoted by $e_{month}\{W = j\}$ for $j = 1...W_{max}$, where $W_{max} = 10$ —as empirically is shown in Section 4.2.2. Then, the average errors are calculated for each window size as follows:

$$\mathbf{e}_{j} = \frac{1}{n} \sum_{i=1}^{n} e_{month} \{ W = j \},$$
 (16)

where n = 12 and $month = \{Jan, \dots, Dec\}$.

The W selected is the one that minimizes the average error corresponding to the 12 folds (months) evaluated.

$$W = \arg\min\{\mathbf{e}_j\} \text{ with } j = 1, \dots, W_{max}.$$
(17)

4 RESULTS

The above described methodology has been applied to the electricity prices and demand of Spanish [25], Australian [19], and New York [26] markets. These six data sets have been selected due to the great amount of forecasting results published in the literature. These results will be used to establish a comparison with that of the proposed method in this work.

This section is structured as follows: first, the accuracy of the predictions is validated. Thus, the usual quality parameters are presented. Second, the PSF approach is trained in order to produce accurate predictions and, for this reason, the election of both W and K is discussed here. Third, the prediction of the year 2006 is provided. Finally, a sensitivity analysis of the proposed method with regard to the number of clusters is presented.

4.1 Parameters of Quality

In order to assess the performance of the PSF approach, several measures have been considered:

TABLE 1 Number of Clusters Selected for All the Markets

	Market	Silhouette	DU	DB	Selection
	OMEL	4 (3)	6(4)	5(4)	4
prices	NYISO	5	5	5	5
	ANEM	3	4	3	3
	OMEL	8	8	7	8
demand	NYISO	4	4	3	4
	ANEM	5	5	5	5

• Mean error relative to \bar{x} (MER).

$$MER = 100 \cdot \frac{1}{N} \sum_{h=1}^{N} \frac{|\hat{x}_h - x_h|}{\bar{x}}, \qquad (18)$$

where \hat{x}_h and x_h are the predicted and current prices/demand at hour *h*, respectively, \bar{x} is the mean price/demand for the period of interest (a day or a week in this work), and *N* is the number of predicted hours. Note that, the mean price/demand is used in the denominator of (18) to avoid the effect of prices close to zero.

• Mean absolute error (MAE).

$$MAE = \frac{1}{N} \sum_{h=1}^{N} |\hat{x}_h - x_h|.$$
 (19)

• Standard deviation of MER/MAE (σ).

$$\sigma = \sqrt{\frac{1}{N} \sum_{h=1}^{N} (e_h - \bar{e})^2},\tag{20}$$

where

$$e_h = \frac{\hat{x}_h - x_h}{\bar{x}},\tag{21}$$

and \bar{e} is the mean of the hourly errors.

4.2 Training the PSF Algorithm

In this section, the number of clusters to be generated, as well as the length of the window comprising the sequence of labels that has to be searched along the time series, are presented.

4.2.1 Selecting the Number of Clusters

First of all, the number of clusters K has to be chosen and, for this purpose, the 12 months of the year 2005 are considered for training the algorithm.

In order to validate the quality of the clusters produced by K-means algorithm, the silhouette, Dunn, and Davies-Bouldin three indices have been used in the experiments. Thus, the optimal value of K is selected from a system based on majority votes.

Table 1 summarizes the results obtained by the three indices of cluster validity, in which the numbers in brackets represent the second best values, as described in Section 3.2. A further study about the influence of the number of clusters on the results of the prediction is made in the Section 4.4.

The values of the indices when *K* varies from 2 to 20 are depicted in Figs. 4, 5, and 6. Fig. 4a shows the results of all



Fig. 4. Selecting the optimal number of clusters in OMEL time series. (a) OMEL—price. (b) OMEL—demand.

the three indices when varying K in the Spanish electricity price market. Apparently, all of them have different optimum values since the silhouette and the Dunn indices reach the maximum values in K = 4 and K = 6 (0.3536 and 0.0010, respectively), while the Davies-Bouldin index reaches its optimum value when K = 5 (0.7417). Nevertheless, a thorough analysis of all the values reveals that for K = 4, both Dunn and Davies-Bouldin indices have the second best result (0.0010 and 0.7703), with values really close to the optimum values. For these reasons, the number of clusters selected for this time series is K = 4. On the other hand, Fig. 4b illustrates the results of the Spanish demand market. As can be appreciated, both silhouette and Dunn indices select K = 8—reaching the maximum values in 0.5872 and 1.964E-06, respectively. On the contrary, the Davies-Bouldin index reaches its minimum and, consequently, its optimum value when K = 7. However, when K = 8, this index also presents a low value close to its global minimum (0.8983 versus 0.8208, respectively).

With reference to the New York electricity prices, the situation shown in Fig. 5a reveals an easy selection of the number of clusters. Actually, the three methods select K = 5 since both silhouette and Dunn indices reach the maximum values (0.5324 and 0.0004, respectively) while the Davies-Bouldin index reaches its minimum value (0.6602). The selection of K for the New York electricity demand time series is shown in Fig. 5b. It can be noticed, both silhouette and Dunn indices reach the optimum values in K = 4 (0.7895 and 0.0002, respectively), but the Davies-Bouldin index reaches its minimum when K = 3 (0.8193). Even if the value in K = 4 is not specially low (0.9739), it can be considered a globally low value since this index reaches values such as 1.3125 in K = 6.

Fig. 6a shows the results obtained in the Australian electricity price market. As it can be noticed, both silhouette

and Davies-Bouldin indices reach the maximum and minimum values (0.4858 and 0.6931, respectively) in K = 3. Oppositely, the Dunn index reaches its maximum and, consequently, its optimum value when K = 4. However, when K = 3, this index also presents a high value verging on its global maximum (0.0003 and 0.0002, respectively). With regard to the Australian electricity demand, the situation shown in Fig. 6b is conclusive. Hence, the three methods agree in selecting K = 5 since both silhouette and Dunn indices reach the maximum values (0.5673 and 0.0178, respectively) while the Davies-Bouldin index reaches its minimum value (0.9800).

4.2.2 Selecting the Length of the Window

Once the number of clusters is already decided, the next step is to select the optimal length of the window W. Thus, this step is focused on finding the W that obtains the minimum prediction error in the training set.

Therefore, it is required to evaluate the performance of the PSF algorithm when *W* varies according to the methodology presented in Section 3.4.

Table 2 shows how the prediction error varies in accordance with the number of patterns considered in the window. Note that the symbol "-" means that similar sequences of length W were not found when K clusters were considered in the training set. Finally, the W that allows a lower prediction error is the value chosen for further forecasting on real data. It can be concluded that the optimal lengths of the windows that have to be used are W = 5, W = 3, and W = 6 for the OMEL, NYISO, and ANEM price time series since they reach the lower prediction errors (2.23, 3.27, and 5.81 percent, respectively) and W = 2, W = 5, and W = 3 for the OMEL, NYISO, and ANEM demand time series (2.87, 4.99, and 3.43 percent, respectively).



Fig. 5. Selecting the optimal number of clusters in NYISO time series. (a) NYISO-price. (b) NYISO-demand.

4.3 Forecasting Results

In this section, the results obtained from the three different markets are provided. Precisely, Tables 3, 4, and 5 show the MER and the MAE (and the standard deviations σ in brackets) in the Spanish, Australian, and New York electricity time series—both for prices and demand—for the whole year 2006. In spite of the average of the MER for the year 2006 in the OMEL prices time series is greater than that corresponding to NYISO (6.15 percent versus

5.53 percent), it can be noticed that the mean of standard deviation of MER in the Spanish market is lower than that of the New York market (0.27 percent versus 1.94 percent). This fact means that the maximum errors in the OMEL prices time series are closer to the average errors than the maximum errors obtained when the prices are predicted in the NYISO market. The standard deviation for the Australian market is the highest (4.40 percent) due to the



Fig. 6. Selecting the optimal number of clusters in ANEM time series. (a) ANEM—price. (b) ANEM—demand.

TABLE 2 MER Obtained with the PSF Algorithm on All the Markets

Market	W=1	W=2	W=3	W=4	W=5	W=6	W=7	W=8	W=9	W=10	Selected W
OMEL – price $(K = 4)$	10.32%	8.44%	8.21%	4.39%	2.23%	2.89%				-	5
$OMEL - demand \ (K = 8)$	3.11%	2.87%	-	-	-	-	-	-	-	-	2
NYISO – price $(K = 5)$	7.09%	5.98%	3.27%	6.98%	4.45%	13.20%	10.31%	-	-	-	3
NYISO – demand $(K = 4)$	5.16%	6.21%	5.68%	5.02%	4.99%	6.23%	7.14%	6.90%	8.91%		5
ANEM – price $(K = 3)$	9.58%	7.91%	6.26%	6.17%	7.33%	5.81%	6.04%	9.12%	-	_	6
ANEM – demand $(K = 5)$	3.45%	4.17%	3.43%	6.10%	5.89%	4.02%	7.11%	_	<u> </u>	<u> </u>	3

many peak prices—considered as outliers—that occur in this prices time series.

Fig. 7 illustrates several prediction curves obtained for the Spanish market for the year 2006. Concretely, Fig. 7a shows the best and worst predictions generated by the PSF algorithm when electricity price curves were considered. With regard to the prices, the best prediction occurred on June 23rd in which the MER was 3.10 percent and the MAE 0.12cE/KWHr, while the worst took place on May 8th in which the MER was 9.39 percent and the MAE 0.80cE/ KWHr. Note that these curves are expressed in cents of Euro per kilowatts per hour (cE/KWHr). Fig. 7b presents the best and worst predictions when the electricity demand was analyzed. The best one took place on May 16th in which the MER was 1.16 percent and the MAE 253.49 MW. On the other side, the worst prediction had an MER of 8.67 percent and an MAE equal to 1759.03 MW and it took place on December 12th. Note that these curves are expressed in megawatts (MW).

The results obtained for the New York market are illustrated in Fig. 8. Fig. 8a presents the best and worst prediction curves obtained for the New York electricity prices, which took place on July 8th (with an MER of 2.76 percent and an MAE of 1.41\$/MWHr) and on May 12th (its MER was 8.89 percent and the MAE was equal to 6.89\$/ MWHr), respectively. Note that these curves are expressed in dollars per MWHr (\$/MWHr). Alternatively, Fig. 8b references to the best—December 10th with an MER and MAE equal to 2.67 percent and 28.47 MW, respectively—and the worst—February 15th with an MER and MAE equal to 10.56 percent and 97.89 MW, respectively—predictions in the demand time series.

With respect to the Australian market, it is important to remark that it shows the information structured in different areas. Thus, the National Electricity Market in Australia is comprised of five jurisdictions: Queensland, New South

TABLE 3 Performance of the PSF Algorithm for the Year 2006 in OMEL Time Series

	PRIC	CES	DE	EMAND
Month	MER (σ)	MAE (σ)	MER (σ)	MAE (σ) in MW
Jan.	7.26% (0.25)	0.53(0.07)	3.12% (1.86)	744.32 (82.12)
Feb.	4.93% (0.19)	0.36(0.04)	4.21% (2.26)	1033.97 (109.21)
Mar.	5.88% (0.22)	0.43(0.05)	5.07% (4.17)	1001.71 (98.85)
Apr.	3.62% (0.18)	0.28(0.03)	4.18% (1.28)	1006.30 (107.58)
May	8.11% (0.21)	0.64(0.05)	5.90% (2.33)	1129.76 (96.37)
Jun.	3.76% (0.24)	0.29(0.05)	2.89% (1.81)	693.60 (84.60)
Jul.	4.30% (0.23)	0.33(0.04)	2.34% (1.19)	585.88 (63.17)
Aug.	5.37% (0.34)	0.42(0.06)	3.61%(2.17)	792.21 (86.94)
Sep.	6.41% (0.31)	0.50(0.06)	3.15% (1.55)	757.02 (75.39)
Oct.	7.89% (0.29)	0.58(0.08)	2.89% (3.40)	1121.43 (149.75)
Nov.	8.30% (0.40)	0.64(0.05)	4.72% (2.39)	982.19 (120.52)
Dec.	8.02% (0.36)	0.59(0.07)	6.21% (3.82)	1503.44 (198.49)
Mean	6.15% (0.27)	0.47(0.05)	4.02% (2.35)	945.99 (106.08)

Wales, Victoria, Tasmania, and South Australia. The results in Table 5 refer to the Queensland market.

Fig. 9 shows the best and worst prediction curves obtained for the Australian market in the year 2006 for both electricity prices and demand markets. Fig. 9a illustrates the best and worst prediction curves obtained for the electricity prices, which took place on May 12th (with associated MER and MAE of 3.66 percent and 0.98\$/MWHr, respectively) and on July 20th (with associated MER and MAE of 65.60 percent and 28.39\$/ MWHr, respectively). The Australian electricity price market is characterized by the existence of many spike prices during the year. Indeed, many authors have studied how to perform accurate predictions in that market [41]. The PSF algorithm, even if it is not able to find the real magnitude of such peaks, it is able to forecast the existence of them. This fact justifies the higher value of the MER obtained for that day. It can be observed how the proposed algorithm captures the trend of the prices time series in the Australian market detecting a peak-an outlier-at 7:00 pm. Note that all the curves are expressed in Australian dollars per MWHr.

TABLE 4 Performance of the PSF Algorithm for the Year 2006 in NYISO Time Series

	PRIC	CES	DE	EMAND
Month	MER (σ)	MAE (σ)	MER (σ)	MAE (σ) in MW
Jan.	4.45% (2.07)	2.25(0.34)	5.05% (1.95)	53.21(6.03)
Feb.	5.53% (1.52)	3.02(0.28)	6.88% (2.62)	83.76 (9.19)
Mar.	6.30% (2.52)	3.97(0.43)	5.31% (2.42)	59.63 (6.13)
Apr.	4.94% (1.47)	3.51(0.61)	4.97% (2.22)	52.18(7.21)
May	7.59% (2.13)	4.63(0.43)	6.18% (2.39)	61.12(5.74)
Jun.	3.34% (1.92)	2.31(0.29)	3.75%(2.06)	44.17 (4.86)
Jul.	3.93% (1.68)	2.28(0.20)	3.41% (1.78)	37.54(4.01)
Aug.	5.37%(1.87)	3.49(0.41)	3.99%(2.13)	39.86 (5.52)
Sep.	6.24% (1.74)	4.49(0.53)	4.83% (2.16)	54.14(6.87)
Oct.	7.43% (2.33)	4.23(0.49)	5.37% (2.25)	65.08 (8.01)
Nov.	5.19% (2.09)	3.53(0.30)	4.86% (1.99)	50.25(5.11)
Dec.	6.04% (1.99)	3.08 (0.33)	6.80% (2.40)	82.55 (9.97)
Mean	5.53% (1.94)	3.40(0.39)	5.97% (2.20)	56.96(6.55)

TABLE 5 Performance of the PSF Algorithm for the Year 2006 in ANEM Time Series

	PRICI	ES	DE	EMAND
Month	MER (σ)	MAE (σ)	MER (σ)	MAE (σ) in MW
Jan.	5.58% (1.34)	1.51 (0.52)	4.74% (3.54)	412.38 (58.02)
Feb.	8.59% (3.24)	5.15(2.21)	4.98% (2.98)	445.12 (43.29)
Mar.	7.84% (2.98)	1.73(0.34)	5.02% (5.27)	430.00 (38.90)
Apr.	9.92% (3.90)	1.98(0.63)	6.03% (7.46)	519.73 (57.71)
May	12.85% (4.03)	3.21(1.02)	4.17% (2.72)	373.22 (43.28)
Jun.	22.04% (12.34)	6.81(2.89)	5.67% (3.84)	561.44 (60.32)
Jul.	17.11% (10.58)	8.16(3.42)	4.91% (5.84)	481.18 (53.67)
Aug.	11.71% (5.08)	3.32(0.40)	5.88% (6.01)	555.07 (65.05)
Sep.	8.23% (2.45)	2.34(0.23)	3.99% (2.74)	350.88 (32.41)
Oct.	7.66% (2.89)	1.92(0.11)	4.04% (3.34)	340.73(48.91)
Nov.	6.76% (1.94)	2.09(0.34)	6.12% (5.90)	504.16 (70.42)
Dec.	6.42% (2.01)	1.41(0.28)	3.91% (3.22)	329.26 (33.81)
Mean	10.39% (4.40)	3.30(1.03)	4.96% (4.41)	441.93 (50.48)



Fig. 7. Best and worst predictions for the Spanish electricity market in 2006. (a) Spanish electricity price market. (b) Spanish electricity demand.

Finally, Fig. 9b references to the best—December 8th with an MER and MAE equal to 2.67 percent and 322.82 MW, respectively—and the worst—November 19th with an MER and MAE equal to 10.56 percent and 638.92 MW, respectively —predictions in the demand time series.





Fig. 8. Best and worst predictions for the New York electricity market in 2006. (a) New York electricity price market. (b) New York electricity demand.



Fig. 9. Best and worst predictions for the Australian electricity market in 2006. (a) Australian electricity price market. (b) Australian electricity demand.

4.4 Sensitivity to the Parameter K

In this section, a posteriori analysis of sensitivity to the parameter K is carried out in order to show the good performance of the three indices of cluster validity presented for these six time series and the robustness of the proposed method with regard to this parameter.

Fig. 10 shows the MER provided by the PSF algorithm in 2006 for the prices and demand time series when the number of clusters K ranges from 2 to 15.

From Table 1 and Fig. 10, the following can be stated:

- **Remark 1.** The MER is minimum when five clusters (K = 5) are considered for both prices and demand in New York and Australia, respectively. All indices—silhouette, DU, and DB—coincided in the optimal selection of this parameter for the aforementioned markets.
- **Remark 2.** The indices silhouette and DU selected the same number of clusters for the demand time series of the Spanish and New York markets (K = 8 and K = 4, respectively) and for the prices time series of the Australian market (K = 4). Indeed, the global minima



Fig. 10. Sensitivity of the PSF approach to the K parameter.

 TABLE 6

 MER for Some Weeks of the Year 2002 (OMEL—Price)

Week	Naive	ANN	ARIMA	Mixed models	WNN	\mathbf{PSF}
$18^{th} - 24^{th}$ Feb 2002	7.68%	5.23%	6.32%	6.15%	5.15%	5.98%
$20^{th} - 26^{th}$ May 2002	7.27%	6.36%	6.36%	4.46%	4.34%	4.51%
$19^{th} - 25^{th}$ Aug 2002	27.30%	11.40%	13.39%	14.90%	10.89%	9.11%
$18^{th} - 24^{th}$ Nov 2002	19.98%	13.65%	13.78%	11.68%	11.83%	10.07%
Average	15.56%	9.16%	9.96%	9.30%	8.05%	7.42%

of the MER for these three time series are reached in these values.

Remark 3. The three indices of cluster validity provided different values of the parameter K for the OMEL prices time series (K = 4, K = 6, and K = 5 for silhouette, DU, and DB indices, respectively). However, the MER obtained for these three values does not present significative differences. Nevertheless, for this time series, the global minimum is reached in the selected number of clusters from the proposed system based on majority votes.

This analysis highlights the validity of the methodology followed in order to select K, since it reveals that the MER is minimized when the three indices agreed, that the optimality is guaranteed when two of them—a majority—agreed and, finally, that the MER does not vary significantly when all of them are different and K is selected as described in Section 3.2.

5 COMPARATIVE ANALYSIS OF PSF

A comparison between the results obtained by the PSF method and the most representative approaches reported in the literature is provided in this section, showing that the proposed approach improves the aforementioned techniques. Thus, in order to validate the accuracy of the proposed algorithm, it has been applied to specific periods of time in which other authors evaluated their own approaches.

Furthermore, this section is divided into two sections. The first one gathers the forecasting results related to the electricity price markets, while the second one points out the enhancements achieved in the electricity demand forecasting with the proposed methodology.

5.1 Electricity Prices Time Series

5.1.1 The Spanish Electricity Prices Market

The *Spanish electricity prices market* has been widely analyzed. Many authors have evaluated their own approaches over the time series for the year 2002 and, as a consequence, the literature offers multiple results for this year. The PSF algorithm is compared to four published approaches: ARIMA [7], ANN [5], mixed models [15], and WNN [33]. Finally, it is also compared to the naive Bayes classifier as a reference method.

As it can be observed in Table 6, the proposed method has improved most of the MER rates. However, there are some exceptions, such as for the week of February 18th–24th, in which the ANN obtained an error of 5.23 and 5.15 percent for the WNN versus the 5.98 percent

provided by the PSF method. The mixed models and the WNN method also obtained lower errors in the week of May 20th-26th (4.46 and 4.34 percent versus 4.51 percent, respectively). Apart from these two weeks, the PSF algorithm was much more efficient than the others. The mean errors improved by more than 0.5 percent the best method compared to (7.42 percent for the PSF versus 8.05 percent for the WNN).

The authors in [15] also forecasted a week of the year 2000. The comparative of the MER rates is shown in Table 7. The average of the MER for this week is 5.46 percent when the PSF method was applied, whereas the mixed models and ARIMA models yield an average of 7.04 and 8.17 percent, respectively. For this week, the average results are 1.5 percent better than those obtained by the other methods. Therefore, the improvement reached by the proposed algorithm is considered successful.

5.1.2 The New York Electricity Prices Market

As for the *New York electricity prices time series*, the authors in [6] compared some forecasting algorithms with their own approach called STR. They applied manifold-based dimensionality reduction to electricity prices curve modeling. Hence, they showed that there exists a low-dimensional manifold representation for the price curve in the New York electricity market. They compared with an ARIMA model and a naive Bayes as reference method.

Table 8 presents the MER obtained for the one weekahead electricity price forecasting for each second week for every month of the year 2005. The last row shows the average errors when the horizon of prediction is 24 hours. It can be noticed that the PSF approach provides better predictions in most months. There are just two cases in which the STR overcomes the PSF algorithm: February 2005 and May 2005 (7.65 and 7.53 percent for STR versus 7.89 and 7.58 percent for PSF, respectively). Note that in these two cases, the MER obtained by the PSF is not significantly high. In addition, when the average error is evaluated, all the

TABLE 7 MER for One Week of the Year 2000 (OMEL—Price)

Day	ARIMA	Mixed Models	\mathbf{PSF}
Day 1	4.30%	4.80%	3.74%
Day 2	7.99%	7.30%	6.91%
Day 3	4.57%	5.40%	3.45%
Day 4	10.81%	4.60%	5.21%
Day 5	6.12%	5.10%	4.48%
Day 6	17.34%	14.90%	9.63%
Day 7	6.05%	7.20%	4.81%
Average	8.17%	7.04%	5.46%

TABLE 8 MER for the Year 2005 (NYISO—Price)

Month	ARIMA	Naive	STR	\mathbf{PSF}
Feb 2005	14.57%	12.19%	7.65%	7.89%
Mar 2005	13.28%	12.33%	10.19%	9.12%
Apr 2005	10.68%	14.59%	10.53%	8.23%
May 2005	14.21%	6.71%	7.53%	7.58%
Jun 2005	21.64%	26.68%	13.88%	8.85%
Jul 2005	14.63%	14.44%	10.41%	9.21%
Aug 2005	9.49%	10.28%	6.42%	5.56%
Sep 2005	10.36%	13.17%	7.31%	6.59%
Oct 2005	11.84%	11.57%	10.11%	8.03%
Nov 2005	11.24%	15.18%	8.99%	7.89%
Dec 2005	21.78%	23.94%	13.30%	11.21%
Jan 2006	26.01%	11.52%	13.28%	10.77%
Average	14.98%	14.38%	9.95%	8.41%
Average (one-day-ahead)	7.39%	16.07%	7.10%	6.11%

approaches obtained worse results than those of the PSF algorithm, which improves 1.5 percent the result of STR. An increment of 2 percent approximately can be observed when the horizon of prediction is one week instead of one day.

5.1.3 The Australian Electricity Prices Market

The prices in the *Australia's National Electricity Market* have also been predicted in [41]. It is remarkable that this market presents an especial behavior since many spike prices are observed. Despite the authors in [41] have developed techniques based on SVM in order to deal with this particular days, the PSF algorithm does not make any assumption about the nature of the days to be predicted, insofar it uses unsupervised learning and, consequently, no a priori information is known about data.

Table 9 shows the MER obtained for, precisely, these days of the year 2004 with peak prices. It can be observed that the proposed method outperforms all the predictions produced by both ARIMA and SVM approaches.

According to [40], four weeks were predicted with different methods: a discrete wavelet transform (DWT), a multilayer perceptron (MLP), and an SMV approach. Table 10 presents the MER provided by the PSF method and the aforementioned techniques when the horizon of prediction is one week. The PSF algorithm outperforms the average MER provided by all these methods.

5.2 Electricity Demand Time Series

5.2.1 The Spanish Electricity Demand

In order to compare the performance of the proposed approach in the Spanish electricity demand time series, the results provided in [34] are analyzed.

Table 11 shows the comparison between a dynamic regression, a method based on nearest neighbors techniques (kNN), and the PSF algorithm for the period from June to

TABLE 9 MER for Some Days of the Year 2004 (ANEM—Price)

Day (2004)	ARIMA	SVM	\mathbf{PSF}
5^{th} June	32.31%	18.09%	16.72%
17 th June	29.09%	13.31%	8.31%
20^{th} June	33.73%	17.11%	14.23%
21^{st} June	24.18%	19.20%	18.93%
Average	29.82%	16.93%	14.55%

TABLE 10 MER for Some Weeks of the Year 2004 (ANEM—Price)

Week	DWT	MLP	SVM	PSF
Second of January	12.94%	25.81%	23.37%	15.62%
First of July	12.23%	8.36%	15.03%	9.12%
First of August	16.17%	15.85%	36.18%	13.98%
Third of December	10.01%	47.41%	33.74%	10.23%
Average	12.84%	24.36%	27.08%	12.23%

TABLE 11 MER, MAE, and σ_{MER} for Several Months of the Year 2001 (OMEL—Demand)

Parameter	DR	kNN-based	PSF
MER	2.82%	2.30%	1.89%
σ_{MER}	0.019	0.015	0.014
MAE (MW)	572	471	454

November of the year 2001. As it can be noticed, the proposed algorithm obtained better predictions—not only for MER but also for MAE—when it was compared to the other methods considered in the literature.

Although the kNN had a good performance, the PSF was able to reduce from 2.30 to 1.89 percent.

5.2.2 The New York Electricity Demand

The authors in [12] used a model of machine learning called MLF to predict the electricity demand for the next day. The forecasted period was January of the year 2004. Moreover, two methods were used in order to validate the forecasting: an SVM-based model and the prediction itself provided by the New York Independent System Operator.

Table 12 shows the results of comparing PSF and the aforementioned methods in the same period. Given the difficulty of predicting demand time series, an improvement of about 5 percent (2.39 percent for PSF versus 2.51 percent for MLF), it can be considered a remarkable enhancement.

5.2.3 The Australian Electricity Demand

To compare the results provided by the proposed method for the Australian market, the work in [1] was considered. Two days were predicted—October 1st and 2nd of the year 1998—and three methods were used: fuzzy and plain neural networks, and an ARIMA model.

As it can be observed in Table 13, the PSF algorithm improves the prediction error with respect to the other methods, including the very accurate fuzzy neural network.

TABLE 12 MER and MAE for January of the Year 2004 (NYISO—Demand)

Parameter	NYISO	SVM	MLF	PSF
MAE (MW)	214.40	226.87	178.21	176.03
MER	3.16%	3.27%	2.51%	2.39%

TABLE 13 MER for Some Days of the Year 1998 (ANEM—Demand)

Parameter	ARIMA	ANN	Fuzzy-ANN	PSF
MER	4.23%	3.23%	0.92%	0.90%

6 CONCLUSIONS

In this paper, a new forecasting algorithm has been proposed to predict real-world time series. As previous step to the prediction, a clustering technique to label 24dimensional time series has been used and the main novelty lies on the exclusive use of the labels obtained by the clustering to forecast the future behavior of the time series, avoiding the use of the real values of the time series until the last step of the prediction process. Moreover, an automatization of the selection of the critical parameters—K and W—has been proposed.

The algorithm has been successfully applied in electricity prices and demand time series of Spanish, Australian, and New York markets providing very competitive results. The performance was accurate in all of them, showing thus the robustness and adaptability of the proposed approach for time series of different nature. This fact is specially remarkable since the approaches found in literature are usually focused on only one specific time series.

Future work is focused on adjusting the model with dynamical lengths of window and on smoothing the matching sequence criterion.

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