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Citation: *Journal of Applied Physics* **103**, 116101 (2008); doi: 10.1063/1.2913166

View online: <http://dx.doi.org/10.1063/1.2913166>

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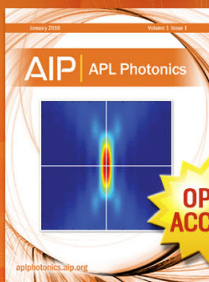
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A phenomenological fitting curve for the magnetocaloric effect of materials with a second-order phase transition

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(Received 22 November 2007; accepted 3 March 2008; published online 2 June 2008)

The magnetic entropy change of polycrystalline samples Gd, La(Fe_{0.92}Co_{0.08})_{11.83}Al_{1.17}, LaFe_{10.8}Si_{2.2}, Mn₅Ge_{2.7}Ga_{0.3}, Nd₂AlFe₁₃Mn₃, and TbCo₂ with a second-order phase transition has been investigated. A uniform phenomenological function that describes the magnetic entropy change is found for these materials. This could be of great benefit for the design of magnetic refrigerators. The field dependence of the critical exponent for the variation in the maximum entropy change with field is studied. The critical exponent value of 2/3, which is predicted by the mean field theory, is only satisfied for moderate field values. The refrigerant capacity is analyzed and compared to the predictions of the fitting function. © 2008 American Institute of Physics. [DOI: 10.1063/1.2913166]

Since the discovery of the giant magnetocaloric effect (MCE) in Gd₅Si₂Ge₂,¹ much interest has been focused on the magnetic refrigeration near room temperature due to its numerous potential advantages over vapor-compression refrigeration.²⁻⁴ The isothermal magnetic entropy change (ΔS_M) is an important parameter for evaluating the refrigerant properties.⁵ Currently, large ΔS_M has been found in materials with a magnetostructural first-order phase transition. However, some problems such as hysteresis and time dependence should be overcome before using those materials as magnetic refrigerants. In fact, the cooling power of a magnetic refrigerator is a product of the operation frequency and the relative cooling power of the refrigerant. Therefore, although materials with a second-order phase transition may have a lower peak entropy change, this can be compensated by their faster response, which can facilitate the increase in the operation frequency in refrigerator appliances.⁶

Recently, the investigation of the magnetic field (H) dependence of ΔS_M has been renewed in materials with a second-order phase transition. The critical exponent n for the variation in the maximum ΔS_M (ΔS_M^{pk}) with H has been studied in detail.⁷⁻¹² Furthermore, a universal behavior is fulfilled for ΔS_M curves measured for various field changes in amorphous alloys.⁹⁻¹¹ Later on, it was evidenced for lanthanide-based materials such as Gd and (Er_{1-x}Dy_x)Al₂.¹² However, up until now, no exact analytical form of this universal curve has been given because in a general case, the $\Delta S_M(H, T)$ curve involves the hypergeometric function, where T is the temperature. In this work, a uniform phenomenological function is found to describe the variation in ΔS_M with H and T for some different samples. As a consequence, the $\Delta S_M(H, T)$ curve for any of these materials can be determined by knowing its Curie temperature (T_C), peak entropy change ΔS_M^{pk} , and two additional reference temperatures. Meanwhile, the

variation in the critical exponent n with field has been obtained, which is necessary to obtain $\Delta S_M^{\text{pk}}(H)$. Although it is usually assumed that the value of n corresponds to the mean field approach ($\Delta S_M^{\text{pk}} \sim H^{2/3}$), using the actual value for each particular sample can solve the negative intercept problem in fitting the experimental data of these materials in Ref. 8. The clarification of this problem can provide directions for the design of a magnetic refrigerator.

The preparation, x-ray diffraction analyses, and magnetic measurements of the polycrystalline samples Gd, La(Fe_{0.92}Co_{0.08})_{11.83}Al_{1.17}, LaFe_{10.8}Si_{2.2}, Mn₅Ge_{2.7}Ga_{0.3}, Nd₂AlFe₁₃Mn₃, and TbCo₂ are described elsewhere.⁸ The value of ΔS_M was calculated from magnetization data by using the integrated Maxwell relations.

The phenomenological universal curve can be constructed by⁹ (1) normalizing all the $\Delta S_M(T)$ curves by using their respective maximum value ΔS_M^{pk} , namely, $\Delta S' = \Delta S_M(T) / \Delta S_M^{\text{pk}}$, and (2) rescaling the temperature axis below and above T_C , as defined in Eq. (1) with an imposed constraint that the position of two additional reference points in the curve corresponds to $\theta = \pm 1$,

$$\theta = \begin{cases} -(T - T_C) / (T_{r1} - T_C), & T \leq T_C, \\ (T - T_C) / (T_{r2} - T_C), & T > T_C, \end{cases} \quad (1)$$

where T_{r1} and T_{r2} are the temperature of the two reference points that, for the present study, have been selected as those corresponding to $\Delta S_M(T_{r1,2}) = 1/2 \Delta S_M^{\text{pk}}$. Figure 1 shows the $\Delta S'$ dependence of $\Delta S'$ for typical field changes for all of the studied samples. One can clearly find that all the experimental points distribute on one universal curve. The universal curve can be well fitted by a Lorentz function,

$$\Delta S' = \frac{a}{b + (\theta - c)^2}, \quad (2)$$

where a , b , and c are the free parameters. By taking into account the asymmetry of the curve, two different set of constants have to be used: for $T \leq T_C$, $a = 1.69 \pm 0.06$, b

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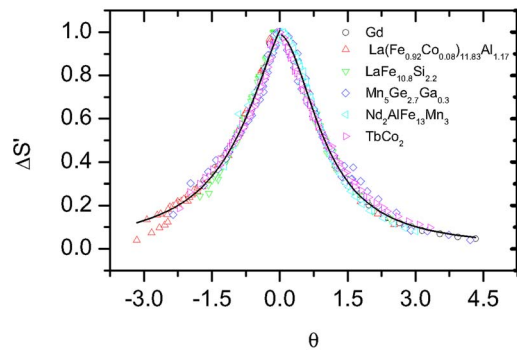


FIG. 1. (Color online) θ dependence of $\Delta S'$ for the studied samples for typical field changes (0–1, 2, 3, 4, and 5 T); the solid line is the fit to Eq. (2).

$= 1.54 \pm 0.03$, $c = 0.38 \pm 0.03$; and for $T > T_C$, $a = 1.05 \pm 0.02$, $b = 1.06 \pm 0.02$, $c = -0.03 \pm 0.01$. In the present cases, a , b , and c are common for these materials. Recently, it was demonstrated that a single reference temperature should be enough for constructing the universal curve.^{13,14} Although this alternative approach works well for most of the present materials, the data for $\text{La}(\text{Fe}_{0.92}\text{Co}_{0.08})_{11.83}\text{Al}_{1.17}$ and $\text{LaFe}_{10.8}\text{Si}_{2.2}$ alloys fail to collapse on one universal curve when only a single reference temperature is used. This peculiarity is being currently investigated in more detail.¹⁵

According to Eq. (2), only the position and magnitude of the peak, namely, $(T_C, \Delta S_M^{\text{pk}})$, and two reference temperatures T_{r1} and T_{r2} , are needed to characterize the entropy change, where $T_{r1} < T_C$ and $T_{r2} > T_C$. That is to say, to translate $\Delta S'(\theta)$ into the “real” $\Delta S_M(T)$, you need only these values that are determined by the properties of the materials. Thus, incomplete $\Delta S_M(T)$ curves, which are experimentally determined from a small temperature span in the vicinity of T_C for the isothermal magnetization measurements, can be easily transformed into the complete curves, which is a helpful tool for the evaluation of material properties such as the refrigerant capacity (RC). Furthermore, engineers can use this function to analyze the influence of material parameters on the design of a magnetic refrigerator. Certainly, the extension of Eq. (2) obtained from the present materials to other compositions needs to be verified experimentally and theoretically in the future.

Among the three points mentioned above, the point $(T_C, \Delta S_M^{\text{pk}})$ is the most important. So, we check the field dependence of ΔS_M^{pk} in detail. First, to determine the field dependence of the experimental $|\Delta S_M|$ of the studied materials, a local exponent¹⁶ is calculated as

$$n = \frac{d \ln |\Delta S_M|}{d \ln H}. \quad (3)$$

The value of n depends on the values of field and temperature. On the basis of a mean field approach, the field dependence of the magnetic entropy change at T_C , ΔS_M^{pk} , has been predicted by $n=2/3$.^{7–9} In a general case, n is related to the critical exponents of the material.⁹ Figure 2 shows the θ dependence of the local exponent n for the studied samples for typical field changes (not larger than 5 T). At T_C , an increase in n is observed with the decrease in the field change. This can be associated to the nonsaturation of the

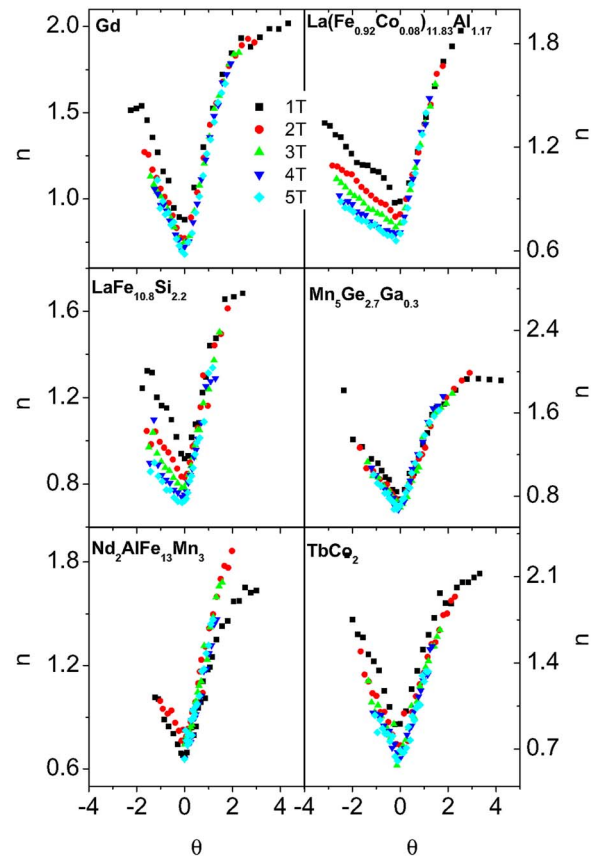


FIG. 2. (Color online) θ dependence of the local exponent n for the studied samples for typical field changes.

sample. Thus, due to the local exponent n being larger than $2/3$ for small field changes, the negative intercept can be eliminated in fitting the relationship of $|\Delta S_M|$ and $H^{2/3}$ at T_C in Ref. 8. Apart from the lowest field data, all of the $n(\theta)$ curves in Fig. 2 collapse, within the experimental error, onto a single one. There are two remarkable exceptions: $\text{La}(\text{Fe}_{0.92}\text{Co}_{0.08})_{11.83}\text{Al}_{1.17}$ and $\text{LaFe}_{10.8}\text{Si}_{2.2}$ compounds, wherein a continuous decrease in n with increasing field is found below T_C . This can be related to the previously mentioned failure in obtaining a universal curve for these two alloys when a single reference temperature is used.¹⁵ As an example, Fig. 3 shows the field change dependence of n in the vicinity of T_C ($=241$ K) for $\text{LaFe}_{10.8}\text{Si}_{2.2}$ compound. As

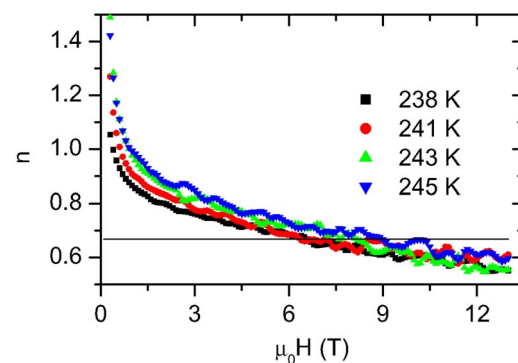


FIG. 3. (Color online) Field change dependence of n in the vicinity of T_C for $\text{LaFe}_{10.8}\text{Si}_{2.2}$ compound; the solid line is the $n=2/3$ reference.

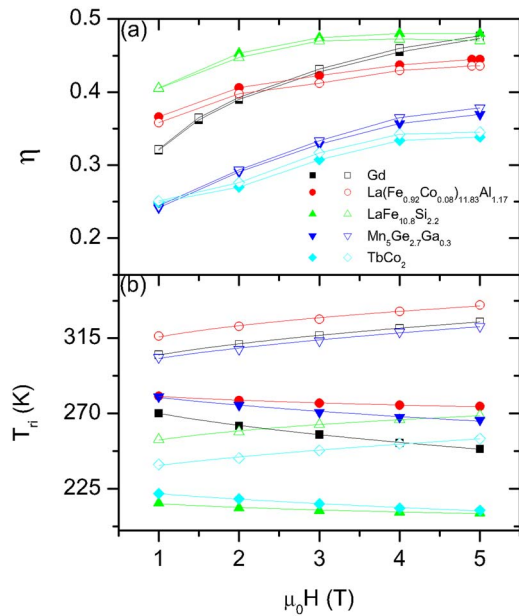


FIG. 4. (Color online) Field change dependence of (a) η [the closed symbols are for experimental data and the open symbols for the results of Eq. (2); the lines are a guide for the eye] and (b) T_{ri} ($i=1, 2$) (the closed symbols are for T_{r1} and the open symbols are for T_{r2} ; the lines are a fit to a power law of the field).

shown in Fig. 3, n initially decreases with increasing field changes. Then, it slowly changes with further increasing field changes, but it is not saturating even for a field change of 0–13 T at T_C .

Besides the ΔS_M^{pk} , the RC is another important parameter in characterizing the MCE. The numerical integration of the area under the $|\Delta S_M|$ curve between T_{r1} and T_{r2} is used as $\text{RC} = -\int_{T_{r1}}^{T_{r2}} \Delta S_M(T) dT$.⁴ We can obtain RC not only from the experimental $\Delta S_M(T)$ curves but also from the curves given by Eq. (2). The former is labeled as RC_{expt} , and the latter as RC_{calc} . Now, we define the utilization ratio of a given magnetic refrigerant as $\eta = \text{RC}/A$, where A is the RC between 0 K and infinite. According to the Maxwell relations, A equals to $-\int_0^\infty \Delta S_M(T) dT = \Delta H M_s$,¹⁷ where M_s is the saturation magnetization at 0 K. Similarly, we have $\eta_{\text{expt}} = \text{RC}_{\text{expt}}/A$ and $\eta_{\text{calc}} = \text{RC}_{\text{calc}}/A$. Figure 4(a) shows the field change dependence of η for the present materials. The value of M_s for the present materials refers to Ref. 8. As shown in Fig. 4(a), η_{calc} is consistent with η_{expt} , which further confirms the validity of Eq. (2). Both η_{calc} and η_{expt} increase with increasing field and reach about 0.48 for a field change of 5 T for Gd and $\text{LaFe}_{10.8}\text{Si}_{2.2}$. Figure 4(b) shows the variation in T_{ri} ($i=1, 2$) with the magnetic field change, which can guide the design of a magnetic refrigerant. In Fig. 4(b), the lines correspond to the fitting of the reference temperature data to a power law of the field, as was recently predicted.^{13,14} For a low field change (0–1.5 T), which can be supplied by a NdFeB per-

manent magnet, the value of $\Delta T (=T_{r2} - T_{r1})$ is larger than 40 K for Gd, $\text{La}(\text{Fe}_{0.92}\text{Co}_{0.08})_{11.83}\text{Al}_{1.17}$, and $\text{LaFe}_{10.8}\text{Si}_{2.2}$. This is also beneficial for future applications in magnetic refrigeration.

In summary, the magnetic entropy change can be characterized by one universal curve for all of the studied materials. The universal curve can be fitted by a Lorentz function, $\Delta S' = a/[b + (\theta - c)^2]$, where $a = 1.69 \pm 0.06$, $b = 1.54 \pm 0.03$, and $c = 0.38 \pm 0.03$ for $T \leq T_C$; and $a = 1.05 \pm 0.02$, $b = 1.06 \pm 0.02$, and $c = -0.03 \pm 0.01$ for $T > T_C$. Based on this function, only the coordinates of the peak ($T_C, \Delta S_M^{\text{pk}}$) and the two reference temperatures T_{r1} and T_{r2} are needed to describe the whole entropy change curves. The exponent n initially rapidly decreases with increasing field changes and then slowly for 0–13 T field change for $\text{La}(\text{Fe}_{0.92}\text{Co}_{0.08})_{11.83}\text{Al}_{1.17}$ and $\text{LaFe}_{10.8}\text{Si}_{2.2}$ compounds. In 0–5 T, the value of the utilization ratio η reaches about 0.48 for Gd and $\text{LaFe}_{10.8}\text{Si}_{2.2}$, being smaller for the other studied compositions.

This work was supported by the State Key Project of Fundamental Research and the National Natural Science Foundation of China (Grant No. 10774178). V.F. acknowledges the financial support of the Spanish Government and EU FEDER (Project MAT 2007-65227).

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