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1 **Pretensioned centrifugal spun high-strength concrete piles reinforced with steel**
2 **strands: flexural performances**

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1 **Abstract:** The application of pretensioned spun high-strength concrete (PHC) piles in high intensity
2 seismic areas has so far been limited by insufficient horizontal load resistance and poor deformation
3 capacity. A new type of pretensioned spun concrete pile with high strength and high elongation steel
4 strands instead of steel bars has been developed. This paper presents the flexural performance
5 evaluation of the new centrifugal spun concrete pile with steel strands (hereafter referred to as PSC
6 pile). An experimental study is presented first, including the bending tests on six full-scale pile test
7 specimens with three different pile diameters. The flexural performances of PHC and PSC piles are
8 comparatively assessed in terms of crack resistance, ultimate bearing capacity, deformation capacity
9 and failure mode. The results show that the new PSC piles have similar crack resistance, but higher
10 ultimate bearing capacity and better deformation capacity under a flexural condition. Comparing to
11 PHC piles which exhibit a brittle bending failure due to the rupture of prestressing steel bars, PSC
12 piles demonstrate a ductile bending failure with a more gradual crushing of concrete in the
13 compression zone. Following the experimental study, a theoretical model is developed to evaluate the
14 flexural strength of the piles, and a simplified calculation equation for ultimate bending moment is
15 proposed. Finally, a finite element model is also established to simulate the flexural performance of
16 the piles and the modelling results are found to be in good agreement with the experimental results.

17 **Keywords:** pretensioned spun concrete piles; prestressing strand; flexural performance; failure mode;
18 theoretical analysis; finite element model

19 **Notation**

20 A cross-section area of pile, mm^2
21 A_p total cross-section area of prestressing tendons, mm^2
22 D_1 external diameter of pile section, mm

| | | |
|----|-------------|---|
| 1 | D_2 | internal diameter of pile section, mm |
| 2 | D_p | diameter of the circle at the centre of prestressing tendons, mm |
| 3 | E_c | elastic modulus of concrete, MPa |
| 4 | E_s | elastic modulus of reinforcing bar, GPa |
| 5 | f_c | axial compressive strength of concrete, MPa |
| 6 | f_{cu} | compressive strength of 150 mm × 150 mm × 150 mm concrete cube, MPa |
| 7 | $f_{cu,10}$ | compressive strength of 100 mm × 100 mm × 100 mm concrete cube, MPa |
| 8 | f_{pt} | tensile strength of prestressing tendon, MPa |
| 9 | f_t | tensile strength of concrete, Mpa |
| 10 | f_y | yield strength of reinforcing bar, MPa |
| 11 | f_u | ultimate tensile strength of reinforcing bar, MPa |
| 12 | $f_{u,e}$ | experimental value of maximum midspan deflexion, mm |
| 13 | $f_{u,n}$ | numerical value of maximum midspan deflexion, mm |
| 14 | h | depth of neutral axis, mm |
| 15 | L | length of pile, mm |
| 16 | M_e | experimental bending moment of midspan section, kN·m |
| 17 | $M_{cr,e}$ | experimental value of cracking moment, kN·m |
| 18 | $M_{cr,n}$ | numerical value of cracking moment, kN·m |
| 19 | $M_{u,e}$ | experimental value of ultimate bending moment, kN·m |
| 20 | $M_{u,n}$ | numerical value of ultimate bending moment, kN·m |
| 21 | r_1 | external radius of pile section, mm |
| 22 | r_2 | internal radius of pile section, mm |

| | | |
|----|--------------------|--|
| 1 | r_p | radius of the circle at the centre of prestressing tendons, mm |
| 2 | t | wall thickness of pile, mm |
| 3 | W | self-weight of pile, kN |
| 4 | δ | maximum force elongation of reinforcing bar |
| 5 | ε_{cm} | peak compressive strain of concrete |
| 6 | ε_{tm} | peak tensile strain of concrete |
| 7 | ε_y | yield strain of reinforcing bar |
| 8 | ρ_s | ratio of longitudinal reinforcement |
| 9 | σ_{ce} | effective compressive pre-stress of concrete, MPa |
| 10 | σ_{con} | tensile control stress of prestressing tendon, MPa |
| 11 | σ_{cm} | peak compressive strength of concrete, MPa |
| 12 | σ_{p0} | initial stress of prestressing tendon, MPa |
| 13 | σ_{tm} | peak tensile strength of concrete, MPa |

14 **1. Introduction and research significance**

15 Pretensioned spun high-strength concrete (PHC) piles are fabricated by pretensioned prestressing
16 technology and usually using a centrifugal forming method, and have been widely used in foundation
17 engineering with the advantages of high bearing capacity, reliable quality assurance, simple
18 manufacture process and outstanding economic benefit. PHC piles are often used to support large
19 superstructures when the ground soil conditions are not strong enough, and they also need to bear
20 lateral loads caused by wind, wave and earthquake. The investigation of pile damage in 1995
21 Hyougoken-Nanbu earthquake in Japan showed that PHC piles had poor seismic performance and
22 suffered brittle failure at the pile heads under the seismic loading ([Nagae and Hayashi, 2003](#)).

1 Furthermore, the collapse incident of a 13-story building in Shanghai in 2009 raised more concerns
2 about the horizontal bearing capacity of PHC piles ([Wang et al., 2017](#)). Improving the horizontal
3 bearing capacity and deformation capacity of PHC piles becomes an urgent call.

4 PHC piles were first developed in Japan and subsequently introduced to China, which have
5 gradually become the main type of prestressed concrete piles in the two countries. In order to improve
6 the strength and ductility of PHC piles and make them suitable for application in seismic areas,
7 scholars from both countries have carried out a lot of research in the last two decades. Kishida *et al.*
8 ([2000](#)) investigated the ultimate shear behaviour of PHC piles and the influence of increasing spiral
9 reinforcement ratio and adding concrete infilling, and the results showed that using both methods
10 could improve ultimate strength and deformation behaviour but using the concrete infilling alone
11 could not prevent the brittle failure. Then, Nagae and Hayashi ([2003](#)) studied the seismic performance
12 of PHC piles under reverse cyclic loading and a constant axial load, and noted that the deformation
13 capacity was improved with a larger stirrup ratio but also affected by the axial load and the ratio of
14 the pile wall thickness to the diameter. Akiyama *et al.* ([2012](#)) conducted the flexural tests of precast
15 high-strength reinforced concrete piles with carbon-fibre sheets and concrete infilling, and
16 demonstrated that carbon-fibre sheets and concrete infilling significantly enhanced the flexural
17 capacity of prestressed reinforced concrete piles. The effect of additional non-prestressing reinforcing
18 bars has also been studied by many researchers. Ikeda *et al.* ([1982](#)) reported that the non-prestressing
19 longitudinal reinforcements could allow the ductile performance of prestressed concrete piles to
20 develop even after rupture of prestressing tendons. Wu *et al.* ([2020](#)) also showed that the failure mode
21 of PHC piles with hybrid glass fibre reinforced polymer (GFRP) bars was gradual crushing of the
22 concrete and a high degree of deformability was attained before failure. Moreover, Yang *et al.* ([2018a](#),

1 [2018b](#)) investigated the influence of deformed steel bars and concrete infilling on the seismic
2 performance of PHC piles, and pointed out that both methods could enhance the bearing capacity of
3 PHC piles while the use of deformed steel bars could also significantly improve the ductility capacity.

4 Researchers have also investigated the effects of adding steel fibre and using FRP layer to improve
5 the strength and ductility of reinforced concrete (RC) piles. Buyle-Bodin and Madhkhan ([2002](#)) noted
6 that steel fibre reinforced concrete (SFRC) piles were as efficient as RC piles in terms of strength and
7 ductility and more efficient in terms of dissipation of energy with axial load. Özden and Akdag ([2009](#),
8 [2013](#)) studied the lateral load response of SFRC piles in soil and showed that steel fibres improved
9 the horizontal bearing capacity and ductility of RC piles effectively. In recent years, fibres reinforced
10 polymer (FRP) jacketing has become popular in retrofitting existing deficient piles due to light weight,
11 high strength and excellent corrosion resistance of FRP material. Lignola *et al.* ([2017](#)) tested the
12 performance of RC hollow columns with carbon fibre reinforced polymer (CFRP) wraps subjected to
13 combined axial load and bending, and found that the FRP jacketing increased the ultimate load and
14 ductility of hollow columns. Moreover, Murugan *et al.* ([2017](#)) pointed out that both GFRP and CFRP
15 confined piles showed higher lateral bearing capacity than unconfined piles, and piles with fibres
16 oriented along the length had higher strength than along the circumference.

17 The above strengthening measures can improve the lateral load capacity and deformation capacity
18 of PHC piles effectively, but they inevitably involve the use of additional materials, a more complex
19 manufacture process and therefore significantly increased costs. As a matter of fact, some
20 experimental results ([Ikeda et al., 1982](#); [Yang et al., 2018a, 2018b](#)) have shown that the brittle failure
21 of PHC piles subjected to lateral load was mainly due to the rupture of prestressing tendons.
22 Muguruma *et al.* ([1987](#)) reported that using prestressing tendons with high elongation capacity could

1 effectively improve the flexural capacity of PHC piles. Considering that the tensile deformation
2 capacity of prestressing steel bars which are now widely used in PHC piles is not good enough, the
3 present study adopts higher elongation and higher strength prestressing steel strands to replace the
4 prestressing steel bars, and develops pretensioned centrifugal spun concrete piles with steel strands.

5 **2. Pretensioned centrifugal spun concrete piles with steel strands**

6 The prestressing tendons used in conventional PHC piles are mainly steel bars for prestressed
7 concrete ([10G409, 2010](#)). However, the elongation of prestressing steel bars is usually not good
8 enough and sometimes they show brittle fracture, which limits the deformation capacity of PHC piles
9 when subjected to lateral load. Moreover, all steel bars are fixed on the end plates (an anchoring plate
10 and a tensioning plate) of a pile with pier heads that cannot be in full contact with the plates during
11 tensioning, which leads to uneven stresses in the prestressing steel bars and affects the bearing
12 capacity of PHC piles. Therefore, changing the material of prestressing tendons and improving the
13 manufacture process are deemed to be a viable approach to enhance the horizontal bearing capacity
14 and deformation capacity of PHC piles.

15 Steel strand is a common type of prestressing tendons with high tensile strength and good tensile
16 ductility, and is used in precast and prestressed concrete structures ([Park et al., 2016](#); [Paul et al., 2017](#);
17 [Dang et al., 2018](#)). In pile foundations, particularly in solid square and octagonal prestressed concrete
18 piles, prestressing strands are also widely used ([PCI, 2017](#)). The post-tensioned hollow pipe piles,
19 which were first manufactured by the American Raymond Pile Company, were popular in port
20 engineering due to large modulus and relatively light section. However, because of the post-tensioned
21 method, a large cross-section diameter is required, and consequently the cost is also high, making it
22 uneconomical to use post-tensioned hollow pipe piles in pile foundation engineering of high-rise

1 buildings.

2 In the present study, a new pretensioned centrifugal spun concrete pile with steel strands is
3 developed to combine the excellent mechanical properties of prestressing strands with the advantages
4 from the well-developed technology of pretensioned spun concrete piles. Comparing to the steel bars,
5 it is more difficult to fully fix the steel strands, which are made up by a plurality of steel wires, to end
6 plates. Therefore, a new design of the end plate with an improved anchorage method has been
7 developed for the prestressing tendons ([Yu and Gao, 2016](#); [Gan et al., 2017](#)). The end plate has a
8 plurality of conical through holes, and the diameter of the holes is made to gradually increase from
9 inside towards outside and each hole hosts one individual steel strand, as depicted in Figure 1. A
10 chock assembly constituted of multiple metal clips with a toothed inner surface and a conical outer
11 surface is placed in each hole. The steel strand passes through a corresponding chock assembly and
12 is clamped tightly on the end plate. Following a series of preliminary studies and continuous
13 improvements, a reliable manufacture process of pretensioned centrifugal spun concrete piles with
14 steel strands has been established. In order to examine the flexural performance of the new pile,
15 bending tests on full-scale pile test specimens were carried out.

16 **3. Experimental programme**

17 3.1 Detail of test specimens

18 Full-scale bending tests of six pile test specimens were carried out. According to the size of PHC
19 piles commonly used in practical engineering, the test piles had external diameters of 400 mm, 500
20 mm and 600 mm, respectively. For a comparison, each diameter group consisted of two piles, namely
21 an ordinary pretensioned spun high strength concrete pile with prestressing steel bars (PHC pile) and
22 a pretensioned spun high strength concrete pile with prestressing steel strands (PSC pile). Figure 2

1 and Table 1 show the details of these piles. The three PHC pile test specimens are labelled as PHC400,
2 PHC500 and PHC600, and their counterpart PSC pile test specimens as PSC400, PSC500, and
3 PSC600, respectively.

4 The only difference between the two types of piles in each diameter group was the type of
5 prestressing tendons. The steel bars used in PHC piles were 10.7 mm in diameter (cross-section area
6 = 90 mm²) and they had a nominal tensile strength of 1420 MPa. The nominal strength of the steel
7 strands in PSC piles was higher at 1860 MPa. Because the control stresses for pretensioning of steel
8 bars and steel strands were kept at 70% of the nominal tensile strength in both PHC and PSC piles,
9 7-wire steel strand of nominal diameter of 11.1 mm, which has a smaller net cross-section area of
10 74.2 mm², was selected to ensure the effective compressive pre-stress of concrete was comparable
11 between PHC and PSC piles. For the same reason, the load-carrying capacity of the steel bars and the
12 steel strands between PHC and PSC piles was also similar.

13 3.2 Material mechanical properties

14 The design strength grade of the concrete for the pile test specimens was C105. The concrete was
15 mixed with a mass ratio of cement, water, sand and gravel as 1.00 : 0.26 : 1.12 : 2.60. In order to
16 obtain the material parameters of high-strength concrete, nine concrete cubes of size 100 mm were
17 prepared in the same curing condition as the pile test specimens for compressive tests. The average
18 value of the cubic compressive strength $f_{cu,10}$ was found to be 116.1 MPa. The standard cubic
19 compressive strength f_{cu} , axial compressive strength f_c and tensile strength f_t of the concrete material
20 may be estimated using the empirical formulas for high strength concrete such as the following ([Li](#),
21 [2004](#); [Ke, 2014](#)):

22 1.
$$f_{cu} = 0.91f_{cu,10} + 1$$

1 2. $f_c = 0.818f_{cu}$

2 3. $f_t = 0.26f_{cu}^{2/3}$

3 The test piles used low relaxation helical grooved steel bars and steel strands as prestressing
4 tendons, and grade-A cold drawn low carbon steel wires as spiral stirrups. Three samples were taken
5 from each type of reinforcing bars, including $\Phi^D10.7$ steel bars, $\Phi^S11.1$ steel strands and Φ^b6 steel
6 wires for the stirrups, and tested to measure the tensile properties. It should be noted that due to the
7 difficulty to hold Φ^b4 and Φ^b5 steel wires in the standard tensile testing machine, three samples of
8 Φ^b6 (6 mm in diameter) from the same type wires were tested instead. Figure 3 shows the measured
9 stress-strain curves, and Table 2 lists the critical material mechanical parameters of three types of
10 reinforcing bars. It can be observed that the ultimate tensile strength f_u and maximum elongation δ of
11 steel strands are much higher than those of helical grooved steel bars.

12 3.3 Test setup and loading schedule

13 The bending experiments of the pile test specimens were carried out mainly to investigate the
14 flexural performance of the piles. According to the pretensioned spun concrete piles standard ([GB](#)
15 [13476-2009, 2009](#)), the 4-point loading scheme was adopted in the experiments, and the load was
16 applied using an electro-hydraulic servo multi-functional testing machine controlled by a computer,
17 as shown in Figure 4(a). Five displacement transducers were installed to measure the displacements
18 at the middle and quarter-span points, as well as at two support locations to monitor any support
19 settlements. Nine concrete strain gauges were installed to monitor the distribution of the strain over
20 the depth of the midspan cross-section and along the bottom tensile edge at locations close to the
21 midspan.

22 The loading was terminated when rupture of prestressing tendons in the tension zone or crushing

1 of concrete in compression zone occurred. As shown in Figure 4(b), each pile test specimen was 8.0
2 m long in total, and had a net test length of 4.8 m between two supports with a 1.0 m pure bending
3 segment in the midspan. Thus, the bending moment in the midspan of pile test specimens is given by:

4 4.
$$M_e = \frac{P}{4} \left(\frac{3}{5} L - 1 \right) + \frac{1}{40} WL$$

5 where P is the total load applied via the testing machine; L and W are the length and the self-weight
6 of test specimens, respectively.

7 The cracking moment M_{cr} and the ultimate bending moment M_u of pile test specimens were first
8 estimated according to the relevant standard ([10G409, 2010](#)). The loading scheme was then stipulated
9 accordingly, as follows. Firstly, the load was applied at a 20% increment of M_{cr} , until the bending
10 moment in the midspan segment reached 80% of M_{cr} . Subsequently, a smaller load increment was
11 applied until the actual cracking of the concrete. After the first vertical crack appeared, a 5%
12 increment of M_u was applied until the bending moment in the midspan segment reached M_u .
13 Afterwards, the loading was changed to the displacement control with a displacement increment of 2
14 mm until the failure of test specimens. Each loading step was maintained about 3 minutes for the
15 stabilization of the test specimens and measurement readings.

16 4. Experimental results and analysis

17 4.1 Load-deflexion curves

18 Figure 5 shows the load-deflexion curves in the midspan of the six pile test specimens. The
19 cracking and maximum load points are marked in the diagrams, and the black and red lines represent
20 the PHC and PSC piles, respectively.

21 Combining the experimental phenomena with the load-deflexion curves, the entire loading process
22 may be described by three distinctive stages: 1) At the first stage of loading, each pile test specimen

1 exhibited an elastic behaviour and the load increased linearly with the midspan deflexion. The
2 bending stiffness of PSC piles was essentially equal to that of PHC piles of the same pile diameter. 2)
3 When the first vertical crack occurred in the midspan, the bending stiffness began to decrease
4 markedly, and the drop of the bending stiffness of PSC piles due to the cracking appeared to be more
5 than that of the corresponding PHC piles, but the degradation rate of the bending stiffness of PSC
6 piles after the cracking was slower as the load further increased. 3) Approaching failure, the steel bar
7 in the bottom of PHC piles went through a hardening phase and eventually reached its ultimate tensile
8 strength and ruptured. The main cracks in the midspan developed greatly in this process, however the
9 concrete in the compression zone of midspan did not crush. In contrast, the failure mode of PSC piles
10 was notably different. The cracks in the midspan appeared gradually with the increase of the deflexion
11 and the bearing capacity of test specimens continued to increase, until the concrete in the compression
12 zone crushed completely. Overall, the PHC piles exhibited a brittle failure mode with the rupture of
13 prestressing tendons, while the PSC piles showed a more ductile failure mode with the compressive
14 concrete eventually crushing but without the rupture of the prestressing strands. Figure 6 shows the
15 representative failure modes of PHC and PSC piles.

16 4.2 Flexural performance

17 Table 3 presents the comparison of flexural performance between PHC and PSC pile test specimens.
18 It can be observed that on average there is little difference in the cracking moment $M_{cr,e}$ between the
19 corresponding PHC and PSC piles of the same diameter. However, the difference of cracking moment
20 between PHC400 and PSC400 pile specimens is relatively large, which may be ascribed to
21 insufficient initial pre-stress of PSC400 pile specimen. Additionally, the ultimate bending moment
22 $M_{u,e}$ of PSC piles were 7%, 17% and 11% larger than that of the corresponding PHC piles, respectively.

1 Notably, the maximum midspan deflexions $f_{u,e}$ corresponding to the maximum load of PSC piles
2 were 20%, 50% and 26% greater than their respective PHC counterparts. This indicates that using the
3 steel strands instead of the steel bars as the prestressing tendons has significantly improved the
4 deformation capacity of the piles.

5 4.3 Crack distribution

6 Figure 7 shows the crack distribution of six pile test specimens before complete failure. The
7 following observations may be made: 1) In both PHC and PSC piles, the crack distributions were
8 generally uniform, and the crack extension height and distribution ranges were similar between PHC
9 and PSC piles. 2) For the two types of piles, with the increase of the pile diameter, the number of
10 cracks increased and the maximum crack width decreased. 3) When the failure of PHC piles occurred
11 in the midspan, the prestressing steel bar in the bottom tension zone ruptured and the width of the
12 main crack increased sharply. On the other hand, the failure of PSC piles was due to the crushing of
13 the concrete in the compression zone, which resulted in the bifurcation of vertical cracks in the
14 midspan.

15 4.4 Strain development

16 As described in Section 3.3, concrete strain gauges were installed on the surface of the piles to
17 measure the strain of concrete at selected critical locations, mainly for the purpose to monitor the
18 occurrence of initial cracking, as well as the crack extension along the depth of the midspan section.
19 The strain histories as measured from these strain gauges are plotted against the applied load in Figure
20 8, in which the cracking and maximum loads are represented by two vertical lines. Note that the
21 tensile strain data above $1500 \mu\epsilon$ are deemed to be meaningless due to cracking and therefore are
22 omitted in the figures. It can be observed that before the cracking in the midspan, the strain from each

1 strain gauge was small and increased linearly with the load. There was an abrupt increase in some
2 tensile strain gauges near the initiation of cracking. When the first crack appeared, the strain in the
3 tension zone increased rapidly and some strain gauges failed just after the cracking.

4 Figure 9 shows the strain distribution over the depth of the midspan section. It can be observed that
5 the concrete strain in the midspan section basically conformed to the assumption of plane section
6 before the cracking. After the cracking and with the load increasing, the neutral axis of the cross-
7 section moved upward continuously.

8 The initial concrete strain of each test specimen before applying external loading was not available
9 but it may be estimated based on the effective compressive pre-stress and the elastic modulus of
10 concrete. Adding the so calculated initial strain values to the maximum readings of concrete strain
11 gauges in the compression zone, the maximum compressive strain of the concrete for all test
12 specimens can be obtained. The average values are found to be about 2300 $\mu\epsilon$ in PHC piles and 2800
13 $\mu\epsilon$ in PSC piles. These values tend to suggest that the compressive performance of the high strength
14 concrete was better attained in PSC piles as compared to PHC piles, possibly because of an improved
15 interaction between the prestressing strands and concrete as compared to the more rigid prestressing
16 steel bars.

17 **5. Theoretical analysis of flexural strength**

18 This section presents a theoretical analysis of the flexural strength of the pile test specimens. The
19 flexural strength of prestressed circular hollow section piles is affected by several inter-connected
20 factors such as the prestressing level and the circular arrangement of the reinforcements, therefore
21 the theoretical analysis is not straightforward. The present experiments on full-scale pile test
22 specimens provide a unique opportunity to verify the accuracy of theoretical calculations concerning

1 the flexural strength. The theoretical analysis is carried out at a cross-section level and is based on
2 the strain compatibility, force equilibrium, and constitutive relationships for the reinforcing bars and
3 the concrete.

4 5.1 General calculation method

5 Similar to the calculation of the bearing capacity of ordinary flexural members, it is assumed that
6 a cross-section of piles remains plane at all loading stages and perfect bonding exists between the
7 prestressing tendons and the concrete ([Qiao et al., 2018](#)). However, the analysis of an annular section
8 is much more complicated than rectangular section and the prestressing tendons are distributed in a
9 circle, which requires to a more sophisticated calculation. Referring to the recommendations in the
10 literature ([Joen and Park, 1990](#); [GB 50010-2010, 2010](#)), herein the pile cross-section is divided into
11 a number of discrete strips, as shown in Figure 10, and each strip is calculated as an approximate
12 rectangle and the stress within a strip is assumed to be constant.

13 To calculate the theoretical ultimate bending moment, the maximum compressive strain of concrete
14 in the current PHC and PSC piles is assumed to be $2300 \mu\epsilon$ and $2800 \mu\epsilon$, respectively, based on the
15 experimental data as mentioned in Section 4.4. The calculation procedure is summarized into the
16 following steps ([Qiao et al., 2018](#)):

- 17 1. Select appropriate constitutive relationships of concrete and prestressing tendons, and determine
18 the initial strain of concrete and prestressing tendons. Details will be described in Section 5.2.
- 19 2. Assume an initial value for the neutral axis depth h .
- 20 3. According to the difference between the maximum compressive strain and the initial strain of
21 concrete in the upper edge strip and the plane section assumption, the strain increments of concrete
22 in the other strips are calculated, and subsequently the strain and the stress are obtained. The

1 compressive force of concrete F_c can be determined as follows:

2 5.
$$F_c = \sum_{i=1}^{n_c} f_{ci} A_{ci}$$

3 where f_{ci} is the stress in the i -th concrete strip (positive if compression); A_{ci} is the area of the i -th
4 concrete strip.

5 4. Based on the assumption that perfect bonding exists between the prestressing tendons and the
6 concrete, the strain of prestressing tendons is comprised of the initial strain and strain increment
7 which is assumed to be the same as that of surrounding concrete. The stress of the prestressing tendons
8 is then calculated from the constitutive relationship, and from there the tensile force of prestressing
9 tendons F_p can be determined as follows:

10 6.
$$F_p = \sum_{j=1}^{n_p} f_{pj} A_{pj}$$

11 where f_{pj} is the stress in the j -th prestressing tendon (positive if compression); A_{pj} is the area of the j -
12 th prestressing tendon.

13 5. Check the force equilibrium of section by satisfying that the absolute value of the sum of
14 compressive force F_c and tensile force F_p is less than a certain allowable tolerance ζ .

15 7.
$$|F_c + F_p| \leq \zeta$$

16 6. If the force equilibrium is not satisfied, revise the value h and repeat from step 2 until the force
17 equilibrium is achieved.

18 7. When force equilibrium is satisfied, the section bending moment M can be determined as follows:

19 8.
$$M = \sum_{i=1}^{n_c} f_{ci} A_{ci} y_{ci} + \sum_{j=1}^{n_p} f_{pj} A_{pj} y_{pj}$$

20 where y_{ci} is the distance from the centroid of the i -th concrete strip to the central axis of the pile
21 section; y_{pj} is the distance from the centroid of the j -th prestressing tendon to the central axis of the

1 pile section.

2 5.2 Constitutive relationships

3 In the above calculations, the constitutive relationships of concrete and prestressing tendons are
 4 needed. There are many stress-strain relationships for concrete in the literature, and the material
 5 model proposed by Velasco (2008) about uniaxial compression and tension stress-strain curves is
 6 adopted herein for the constitutive relationship of the high strength concrete.

7 The uniaxial compression stress-strain curve of concrete is composed by three sections: initial
 8 elastic section, damage-based plastic rising section and damage-based plastic descending section, as
 9 illustrated in Figure 11(a). The constitutive relationship is given by the following equations:

$$10 \quad 9. \quad \sigma_c = \begin{cases} E_c \varepsilon_c & \varepsilon_c \in [0, \varepsilon_{c0}] \\ \sigma_{cm} \left[1 - \left(1 - \frac{\varepsilon_c}{\varepsilon_{cm}} \right)^{\eta_1} \right] & \varepsilon_c \in (\varepsilon_{c0}, \varepsilon_{cm}] \\ \sigma_{cm} \left[1 - \left(\frac{\varepsilon_c - \varepsilon_{cm}}{\varepsilon_{cf} - \varepsilon_{cm}} \right)^{\eta_2} \right] & \varepsilon_c \in (\varepsilon_{cm}, \varepsilon_{cf}] \end{cases}$$

11 where E_c is the elastic modulus of concrete and can be calculated by $E_c = 10200 f_c^{1/3}$ (Wee et al.,
 12 1996); σ_{cm} is the peak compressive stress, which is taken as equal to the axial compressive strength
 13 of concrete; ε_{c0} is the elastic compressive strain, the value is 0.001; ε_{cm} is the peak compressive strain
 14 and can be calculated by $\varepsilon_{cm} = 0.00078 f_c^{1/4}$ (Wee et al., 1996); ε_{cf} is the final compressive strain, the
 15 value is taken as 0.0045 based on the compression test; η_1 and η_2 are the empirical parameters related
 16 to smoothness of the curve, the values are 1.434 and 1.650, respectively.

17 The uniaxial tension stress-strain curve of concrete can be described by a piece-wise linear line
 18 consisting of four segments, as shown in Figure 11(b). The rising section of the curve is a linear elastic

1 section and the descending section of the curve is composed by three segments, passing through three
 2 points $(\varepsilon_{t1}, \sigma_{t1})$, $(\varepsilon_{t2}, \sigma_{t2})$, $(\varepsilon_{tf}, 0)$ in turn. The coordinates of the controlling points are obtained by the
 3 following expressions: $\sigma_{t1} = b_1 \sigma_{tm}$, $\sigma_{t2} = b_2 \sigma_{tm}$, $\varepsilon_{t1} = (\varepsilon_{tf} - \varepsilon_{tm}) / c_1$, $\varepsilon_{t2} = (\varepsilon_{tf} - \varepsilon_{tm}) / c_2$, and
 4 the constitutive relationship is given by the following equations:

$$10. \quad \sigma_t = \begin{cases} E_c \varepsilon_t & \varepsilon_t \in [0, \varepsilon_{tm}] \\ \frac{\sigma_{tm} - \sigma_{t1}}{\varepsilon_{tm} - \varepsilon_{t1}} (\varepsilon_t - \varepsilon_{tm}) + \sigma_{tm} & \varepsilon_t \in (\varepsilon_{tm}, \varepsilon_{t1}] \\ \frac{\sigma_{t1} - \sigma_{t2}}{\varepsilon_{t1} - \varepsilon_{t2}} (\varepsilon_t - \varepsilon_{t1}) + \sigma_{t1} & \varepsilon_t \in (\varepsilon_{t1}, \varepsilon_{t2}] \\ \frac{\sigma_{t2}}{\varepsilon_{t2} - \varepsilon_{tf}} (\varepsilon_t - \varepsilon_{tf}) & \varepsilon_t \in (\varepsilon_{t2}, \varepsilon_{tf}] \end{cases}$$

6 where σ_{tm} is the peak tensile stress, which is taken as equal to the tensile strength of concrete; ε_{tm} and
 7 ε_{tf} are the peak tensile strain and the final tensile strain, respectively; b_1 and b_2 are the empirical
 8 parameters that can better describe the softening behaviour in uniaxial tension test, the values are 0.33
 9 and 0.1, respectively; c_1 and c_2 are the constants, and the values are 10 and 1.5, respectively.

10 As shown earlier in Figure 3, the shapes of the stress-strain curves of the prestressing steel bar and
 11 prestressing strand are similar, and both exhibit a linear elastic stage that is followed immediately by
 12 a hardening stage, without obvious yield plateau. Therefore, the model proposed by Esmaily and
 13 Xiao (2005) is adopted to describe the stress-strain curve, as shown in Figure 12, according to the
 14 following expressions:

$$15. \quad \sigma = \begin{cases} E_s \varepsilon & \varepsilon \in [0, \varepsilon_y] \\ k_3 f_y + \frac{E_s (1 - k_3)}{\varepsilon_y (k_1 - 1)^2} (\varepsilon - k_1 \varepsilon_y)^2 & \varepsilon \in (\varepsilon_y, k_2 \varepsilon_y] \end{cases}$$

16 where E_s and ε_y are the elastic modulus and the yield strain of reinforcing bars respectively, which

1 are obtained from the tensile test; k_1 is the ratio of the peak strain to the yield strain, k_2 is the ratio of
 2 the ultimate strain to the yield strain, and k_3 is the ratio of the peak stress to the yield stress.

3 5.3 Simplified calculation method

4 The general calculation method described in Section 5.1 requires iteration and so needs to be
 5 implemented through a computer programme. For practical calculations, a further simplified
 6 formulation is proposed in this section, using an arc analogy with a polar coordinate system. For a
 7 simple calculation of the area of the concrete in the compression zone, it is assumed that the
 8 compression zone is distributed as an annular segment, as shown in Figure 13, and the equivalent
 9 height of compression zone concrete is taken as the average value of the heights of the outer arc and
 10 the inner arc ([Zhang et al., 2019](#)). In addition, a thin steel arc is used to replace the discrete
 11 prestressing tendons, and through the total steel area equivalence the wall thickness of the arc can be
 12 found as $\delta_p = A_p / 2\pi r_p$.

13 The distribution of the stresses in the prestressing strands at the ultimate state under bending is
 14 complicated. For simplicity and by reference to the numerical results using the finite element
 15 simulation as will be described in section 6.3, it is assumed that at the ultimate state the stress
 16 distributions of the prestressing tendons in the upper and lower parts of the pile cross-section
 17 (bounded by the central axis) are both linear, as shown in Figure 13. The stress of the prestressing
 18 tendon at the central axis reaches the yield strength, and the stress of the bottom prestressing tendon
 19 reaches the ultimate tensile strength.

20 According to the geometric relationship shown in Figure 13, the depth of the equivalent concrete
 21 compression zone h_c and the depth of neutral axis h can be calculated as follows:

$$22 \quad 12. \quad h_c = r_1 - r_c \cos \pi \alpha$$

1 13. $h = h_c / \beta_1$

2 where r_c is the average radius of the cross-section. The value of r_c should be very close to the radius
 3 r_p of the circle along which the prestressing tendons are distributed, and for simplicity take $r_c = r_p \cdot \beta_1$
 4 is the ratio of the depth of equivalent rectangular stress block to the depth of neutral axis, the value
 5 can be taken as 0.65 (ACI, 2019).

6 Above the central axis, the stress of prestressing tendons σ at any height y can be calculated as
 7 follows:

8 14.
$$\sigma = \frac{r_1 - h - y}{r_1 - h} (f_y - \sigma_{p0}) + \sigma_{p0}$$

9 where f_y is the yield strength of prestressing tendons; σ_{p0} is the initial stress of prestressing tendons.

10 The stress of prestressing tendons below the central axis can be calculated as follows:

11 15.
$$\sigma = f_y - \frac{y}{r_p} (f_{pt} - f_y)$$

12 where f_{pt} is the tensile strength of prestressing tendons.

13 The tensile force of the prestressing tendons F_p can be calculated as:

14 16.
$$F_p = 2 \int_{-\pi/2}^{\pi/2} \sigma \delta_p r_p d\theta = \frac{f_{pt} - f_y}{\pi} A_p - \frac{\beta_1 r_p (f_y - \sigma_{p0})}{\pi [(\beta_1 - 1) r_1 + r_p \cos \pi \alpha]} A_p + f_y A_p$$

15 On the other hand, the compressive force of concrete F_c can be calculated as:

16 17.
$$F_c = \alpha_1 \alpha A f_c$$

17 where α_1 is the ratio of stress of equivalent rectangular concrete block in the compression zone to
 18 axial compressive strength of concrete, the value can be taken as 0.85 (ACI, 2019); A is the cross-
 19 section area of the pile.

20 Based on the axial force equilibrium, the value of α can be obtained by an iterative calculation to
 21 satisfy:

$$18. \quad \alpha_1 \alpha f_c = \frac{f_{pt} - f_y}{\pi} A_p - \frac{\beta_1 r_p (f_y - \sigma_{p0})}{\pi [(\beta_1 - 1) r_1 + r_p \cos \pi \alpha]} A_p + f_y A_p$$

The total bending moment of the section is the sum of the moments produced by the compression zone concrete and the tensile prestressing tendons, which can be obtained by multiplying F_c and F_p by their respective distances to the central axis x . Then the resultant (total) moment can be calculated as follows:

$$19. \quad \begin{aligned} M &= \alpha_1 f_c \int_{\pi/2-\pi\alpha}^{\pi/2+\pi\alpha} r_c \sin \theta \frac{A}{2\pi} d\theta + 2 \int_{-\pi/2}^{\pi/2} -\sigma \delta_p r_p d\theta r_p \sin \theta \\ &= \alpha_1 f_c \frac{\sin \pi \alpha}{\pi} r_p + \frac{(f_{pt} - f_y) r_p A_p}{4} + \frac{(f_y - \sigma_{p0}) \beta_1 r_p^2 A_p}{4 [(\beta_1 - 1) r_1 + r_p \cos \pi \alpha]} \end{aligned}$$

5.4 Theoretical bending moment capacities and comparison with experimental results

The bending moment strengths for the pile test specimens are calculated using both the general method described in Section 5.1 and the simplified method in Section 5.3, and the results are compared with the experimental results in Table 4. Note that h_g and h_s in the table denote the depth of the neutral axis of the cross-section obtained by the two methods, respectively. It can be observed that the bending moment capacities and the depth of neutral axis calculated using the general and simplified methods match closely with each other, indicating that the simplification using the arc analogy is effective. The two groups of calculated values compare reasonably well with the experimental results; however, the predicted values are generally lower than the experimental results by a margin of less than 15%.

The above comparisons indicate that the two calculation methods can predict the flexural capacity of the pile test specimens with reasonable accuracy, and therefore may be used to evaluate the flexural strength of prestressed concrete piles in practical applications.

1 **6. Finite element analysis**

2 Using the above theoretical methods, the bending strength of different type of prestressed concrete
3 piles can be estimated with reasonable accuracy. In order to assist in further evaluation of the damage
4 process and facilitate the parametric investigations, a finite element model has been developed for
5 prestressed concrete piles and verified against the experimental results.

6 6.1 Finite element model

7 The finite element analysis is carried out using the software ABAQUS to simulate the flexural
8 performance of the pile test specimens. Figure 14 shows the configuration of the finite element model.
9 The geometric dimensions and loading condition of the model are the same as the experiments. In
10 order to avoid artificial stress concentration and numerical singularity at the loading points, two
11 elastic loading blocks similar to the experiments are added onto the pile model. An eight-node three-
12 dimensional solid element with reduced integration (C3D8R) is chosen for concrete and a two-node
13 three-dimensional truss element (T3D2) is used for reinforcing bars which are embedded into the
14 concrete. The initial pre-stress of the concrete is applied with an equivalent method of decreasing the
15 temperature of prestressing tendons. In order to ensure the convergence of the solution process, the
16 displacement loading is adopted.

17 On the basis of sensitivity analysis of mesh size, the cross-section of the pile models is meshed into
18 4 layers through the thickness and 36 divisions in the circumferential direction. In the length direction,
19 the mesh density gradually becomes coarser from the midspan segment to two sides of overhanging
20 segments, and the mesh length in the pure bending part is 25 mm, as shown in Figure 14.

21 6.2 Material parameters

22 The concrete damage plasticity (CDP) model in ABAQUS is used for the high strength concrete.

1 The CDP model is based on isotropic damage combined with isotropic tensile and compressive
2 plasticity to describe the inelastic behaviour of concrete, which can simulate the cumulative damage
3 in concrete. The uniaxial compression and tension stress-strain curves mentioned in Section 5.2 are
4 employed to define the constitutive relationships of the high strength concrete under consideration.
5 Other parameters of CDP model are determined by referring to relevant studies ([An et al., 2012](#);
6 [Genikomsou and Polak, 2015](#); [Yilmaz et al., 2019](#)) and trial calculations as follows: dilation angle ψ
7 = 45° , eccentricity $\epsilon = 0.1$, $\sigma_{bo} / \sigma_{co} = 1.16$, $K = 0.6667$, and viscosity parameter $\mu = 0.001$.

8 The mechanical properties of reinforcing bars are modeled by the standard plastic model, and a
9 thermal expansion coefficient is defined to generate the initial pre-stress of the concrete resulting
10 from the initial prestressing condition. The stress-strain relationship for reinforcing bars mentioned
11 in Section 5.2 is adopted to define the basic constitutive properties. The detailed parameter values of
12 reinforcing bars are shown in Table 5.

13 6.3 Numerical results

14 Using the above finite element model, numerical simulations of PHC and PSC piles have been
15 performed. Figure 15 shows the comparison of the load-deflexion curves between the numerical and
16 experimental results. It should be noted that for PHC piles, the failure limit is considered to have been
17 reached when the tensile strain of the prestressing steel bar in the lowest layer reaches the
18 experimental rupture strain of 0.034. It can be observed that the simulated curves match closely the
19 experimental curves before the cracking, and show good agreement after the cracking and throughout
20 the inelastic response range.

21 A comparison of the flexural performance parameters of the pile test specimens between numerical
22 and experimental results is shown in Table 6. It can be seen that the cracking bending moment $M_{cr,n}$

1 obtained by the numerical simulation are in good agreement with the experimental results besides the
2 pile specimen PSC400 due to insufficient initial pre-stress. In addition, the simulated values of
3 ultimate bending moment $M_{u,n}$ for all pile specimens are generally lower but within a margin of 10%.
4 The deflexions obtained from the numerical simulation are also consistent with the experimental
5 results, but the margin of errors is slightly larger than that for the bending strength. These comparisons
6 suggest that the finite element modelling scheme used in this analysis is adequate for the evaluation
7 of the flexural performance of PHC and PSC piles.

8 The finite element simulation allows a detailed examination of the strain distribution in the
9 prestressing tendons. Figure 16 shows the strain distribution of the prestressing tendons in the
10 midspan section at some key loading stages, including concrete cracking, yield of prestressing
11 tendons at different depths of the cross-section, and final failure. The yield sequence shown in Figure
12 16 corresponds to the yield of prestressing tendons layer by layer from the bottom to the top. The
13 arrangement of prestressing tendons in the pile cross-section is shown in Figure 17.

14 It can be observed that before the yield of the bottom prestressing tendon, the strain of prestressing
15 tendons is linearly distributed over the depth of the cross-section, which satisfies the assumption of
16 plane section. With the cracking of concrete and yielding of the prestressing tendons from the bottom
17 layer, the increase of strain in the lower prestressing tendons (i.e. the flexural tension side) accelerates.
18 The strain distribution may still be regarded as following approximately a linear distribution, until
19 the prestressing tendons below the central axis of the section all reach yield strength. After about half
20 of the prestressing tendons in the cross-section have yielded, the strain of prestressing tendons below
21 the central axis increases significantly, suggesting that the assumption of plane section is no longer
22 applicable.

1 Figure 17 shows the stress distribution of prestressing tendons at the failure stage. It can be found
2 that the stress distribution of prestressing tendons over the depth of the cross-section is approximately
3 a two-fold linear distribution. The turning point is above the central axis of the cross-section, and the
4 stress at this point is close to the yield strength. The stresses of the prestressing tendons at and below
5 the central axis all exceed the yield strength, and the stress of the prestressing tendon at the lowest
6 layer approaches the ultimate tensile strength.

7 From the finite element results, the crack distribution of concrete can be observed by the maximum
8 principal plastic strain. In the CDP model, it is assumed that the cracking occurs when the maximum
9 principal plastic strain of concrete is positive and the crack direction is perpendicular to the maximum
10 principal plastic strain ([Genikomsou and Polak, 2015](#)). Figure 18 shows the comparison of crack
11 distribution in the pile when the ultimate bending moment is reached between numerical and
12 experiment results. As can be seen, the patterns of the cracks from the numerical model generally
13 resemble the crack distribution from the experimental results.

14 **7. Conclusions**

15 A new type of pretensioned spun concrete piles with high strength and high elongation steel strands
16 has been developed for use in high intensity seismic areas. To evaluate the flexural performance of
17 the new type of piles, bending tests have been conducted on six full-size pile test specimens with
18 three different cross-section diameters. In conjunction with the experiments, theoretical analysis and
19 finite element modelling of the pile test specimens have also been carried out. The differences in the
20 crack resistance, flexural capacity, deformation capacity and failure mode between the PHC and PSC
21 piles are compared and analyzed. The main conclusions can be summarized as follows:

22 1. With the use of high strength and high elongation prestressing strands instead of prestressing steel

- 1 bars as longitudinal reinforcements, the new PSC piles achieved significant improvement in the
2 lateral deformation capacity. The special end plate design ensured sufficient anchorage and a
3 uniform pre-stress distribution of steel strands in the piles.
- 4 2. Because a higher tensile control stress with the use of prestressing strands, less longitudinal
5 reinforcement ratio can achieve the same effective compressive pre-stress of concrete. In the pile
6 test specimens, the quantity of longitudinal reinforcement of PSC piles was about 17.6% lower
7 than that of PHC piles of the same cross-section diameter. The experimental cracking moments
8 of the PSC piles were similar to those of the corresponding PHC piles, and the ultimate bending
9 moments of the PSC piles were on average about 11% larger than those of the PHC piles. The
10 new PSC piles exhibited comparatively better flexural capacity.
- 11 3. The new PSC piles showed markedly increased deformation capacity comparing to their
12 traditional PHC counterparts. The maximum midspan deflexions of the PSC pile test specimens
13 were observed to increase by 20%, 50% and 26% from those of the corresponding PHC pile test
14 specimens, respectively.
- 15 4. The failure mode of the PHC pile test specimens was brittle bending failure with the rupture of
16 prestressing steel bars, while the failure mode of PSC pile test specimens was governed by the
17 eventual crushing of concrete in the compression zone, without rupture of prestressing strands.
18 The failure process of the PSC piles was more gradual and it exhibited the characteristic of ductile
19 failure, indicating that the PSC piles can be suitable in seismic areas.
- 20 5. The theoretical method is able to predict the flexural strength of prestressed concrete piles
21 reasonably well. The predicted values tend to be slightly lower, and hence on the conservative
22 side, than the experimental results by a margin of less than 15%. The simplified version of the

1 method enables hand calculations and is therefore convenient for practical application.

2 6. Using a general-purpose finite element approach (with ABAQUS herein), the behaviour of the
3 prestressed concrete piles can be simulated satisfactorily. The simulated load-deflexion curves
4 compare well with the experimental curves, including key stages of cracking, maximum bending
5 moment and ultimate midspan deflexion. The finite element model also can capture the strain
6 distribution of prestressing tendons in the midspan section at any critical moment and the
7 development of cracks in the piles through the plastic strain distribution.

8 In future research, more parametric studies may be conducted to cover a wider range of design
9 parameters for the PSC piles, and the parametric study can be assisted by the finite element model as
10 verified in the present paper. Furthermore, for the general application of PSC piles in seismic regions,
11 the behaviour of PSC piles under combined bending and shear, as well as lateral and axial loading,
12 will need to be evaluated. Studies in this direction are underway and the results will be reported
13 subsequently.

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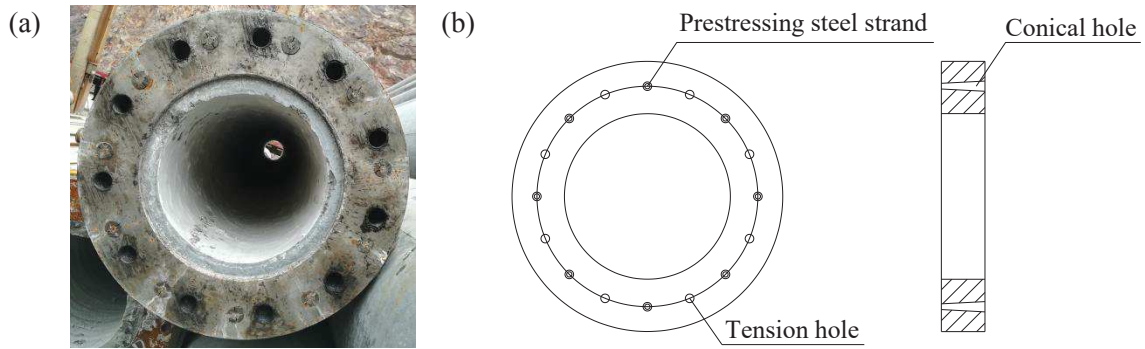


Figure 1. End plate for anchorage of pretensioned steel strands: (a) photo of end plate; (b) schematic diagram

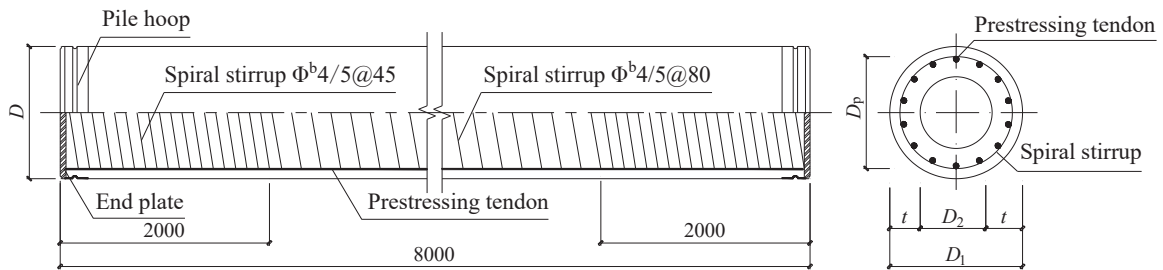


Figure 2. Schematic diagram of reinforcements in test specimens (Unit: mm)

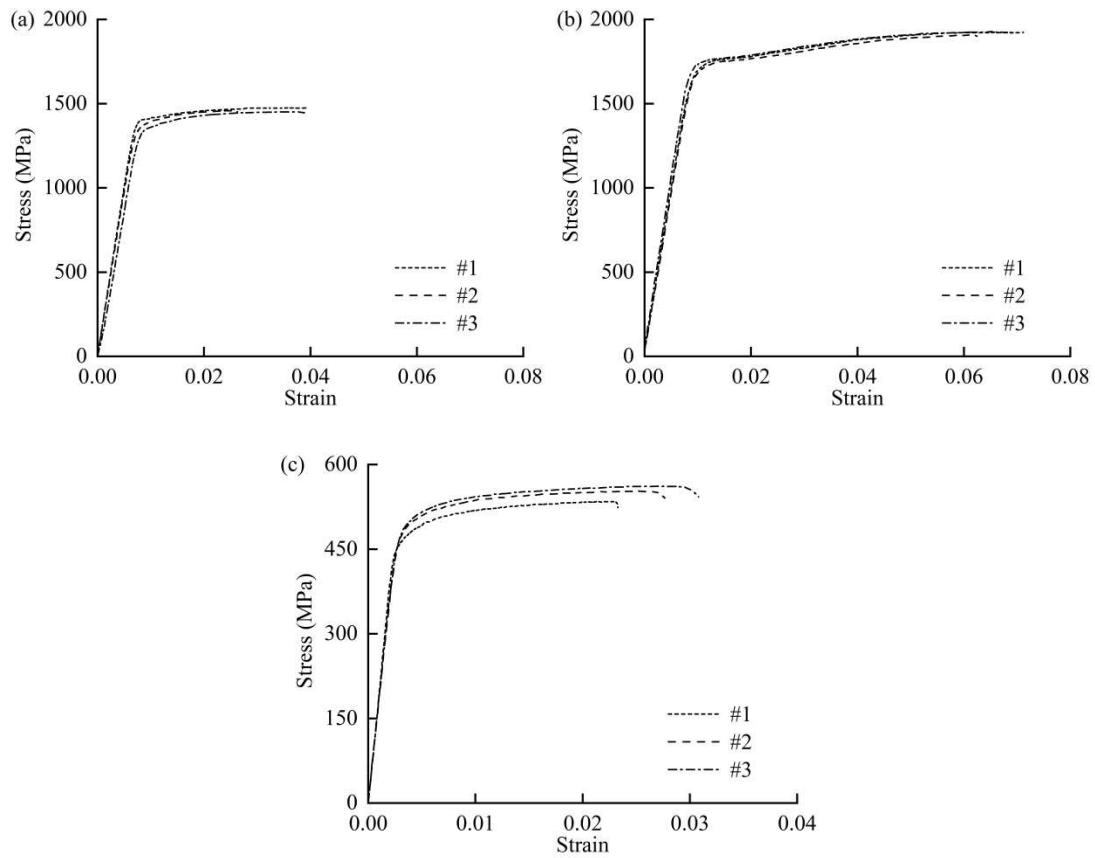


Figure 3. Measured stress-strain curves of reinforcing bars: (a) $\Phi^D10.7$; (b) $\Phi^S11.1$; (c) Φ^b6

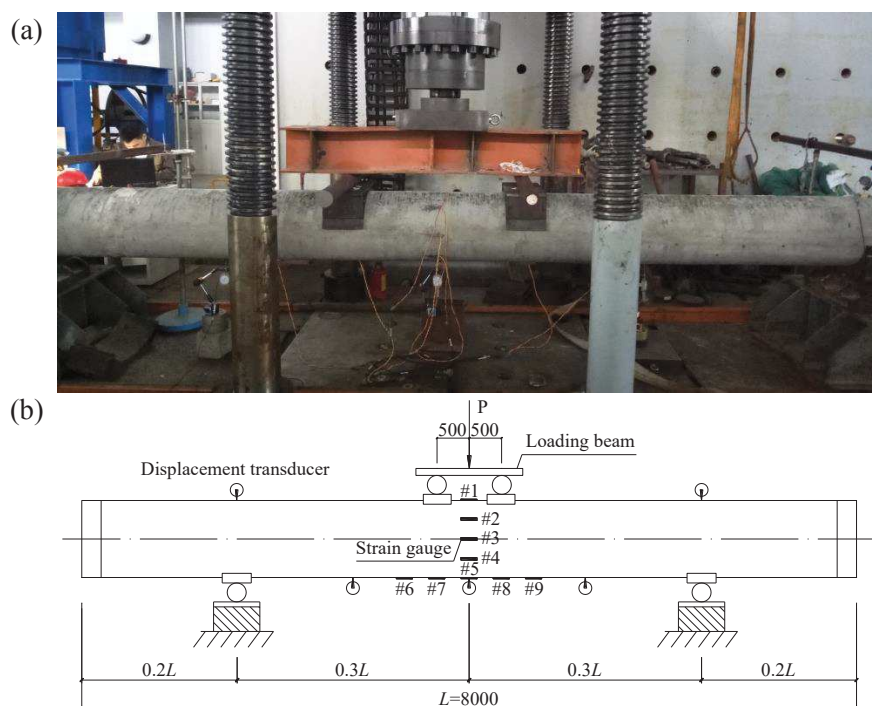


Figure 4. Bending test setup and loading scheme: (a) setup photo; (b) schematic diagram (Unit: mm)

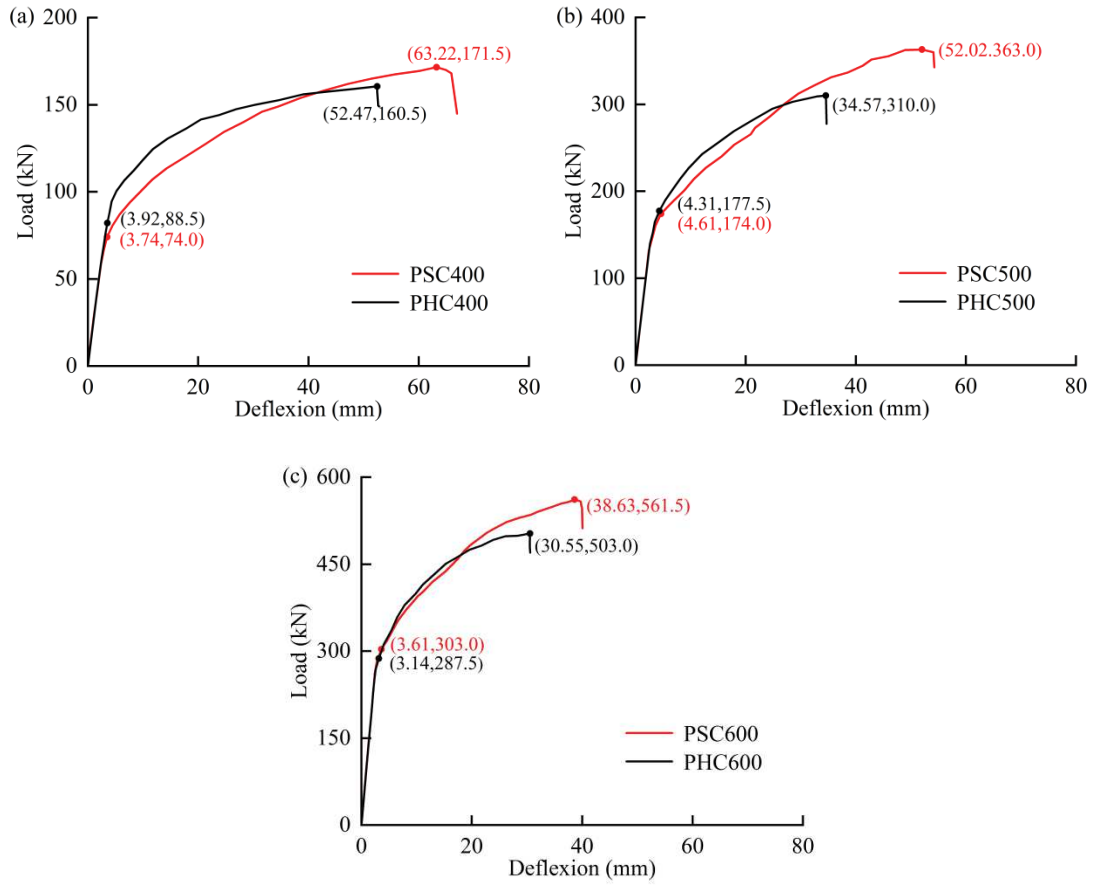


Figure 5. Load vs. midspan deflection curves of test specimens

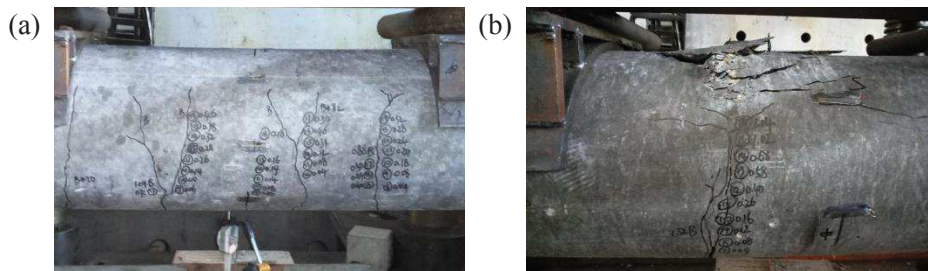


Figure 6. Failure modes of test specimens: (a) PHC400; (b) PSC400

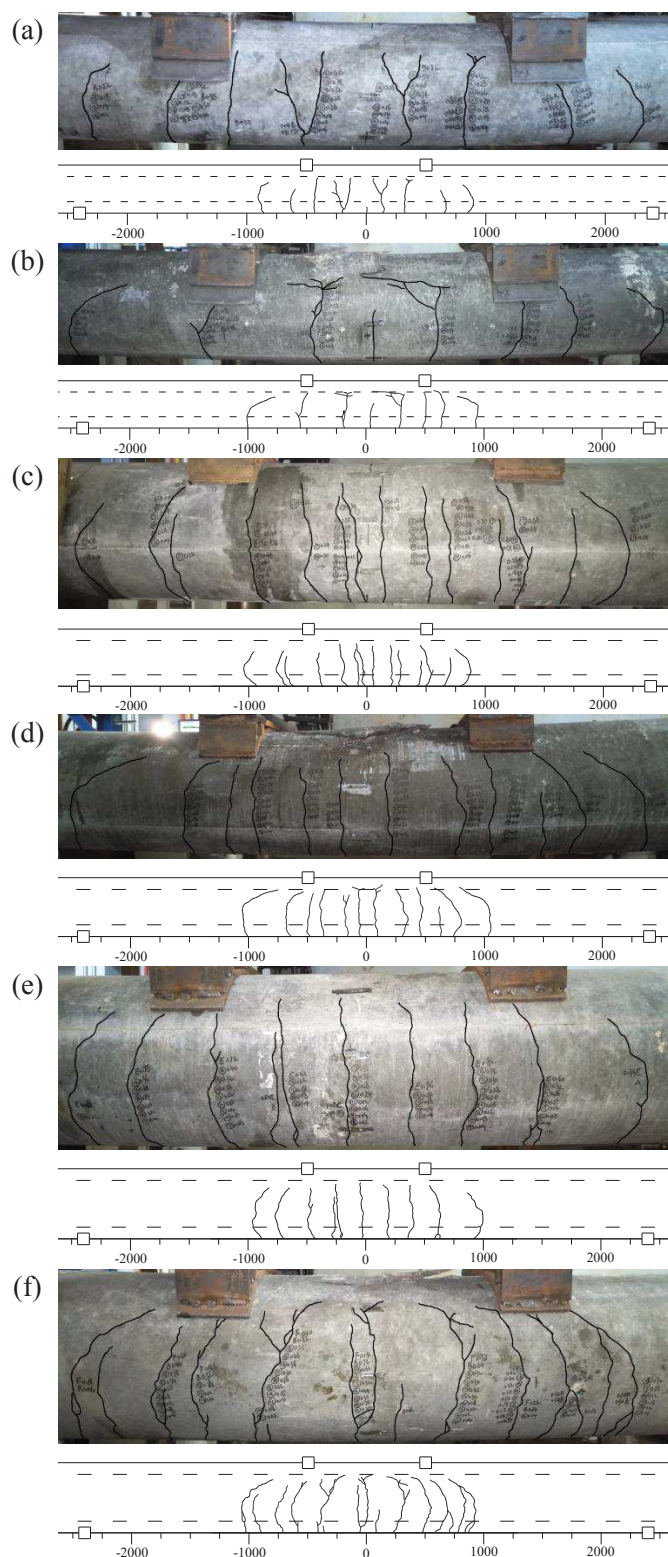


Figure 7. Crack distribution of test specimens: (a) PHC400; (b) PSC400; (c) PHC500; (d) PSC500; (e) PHC600; (f) PSC600

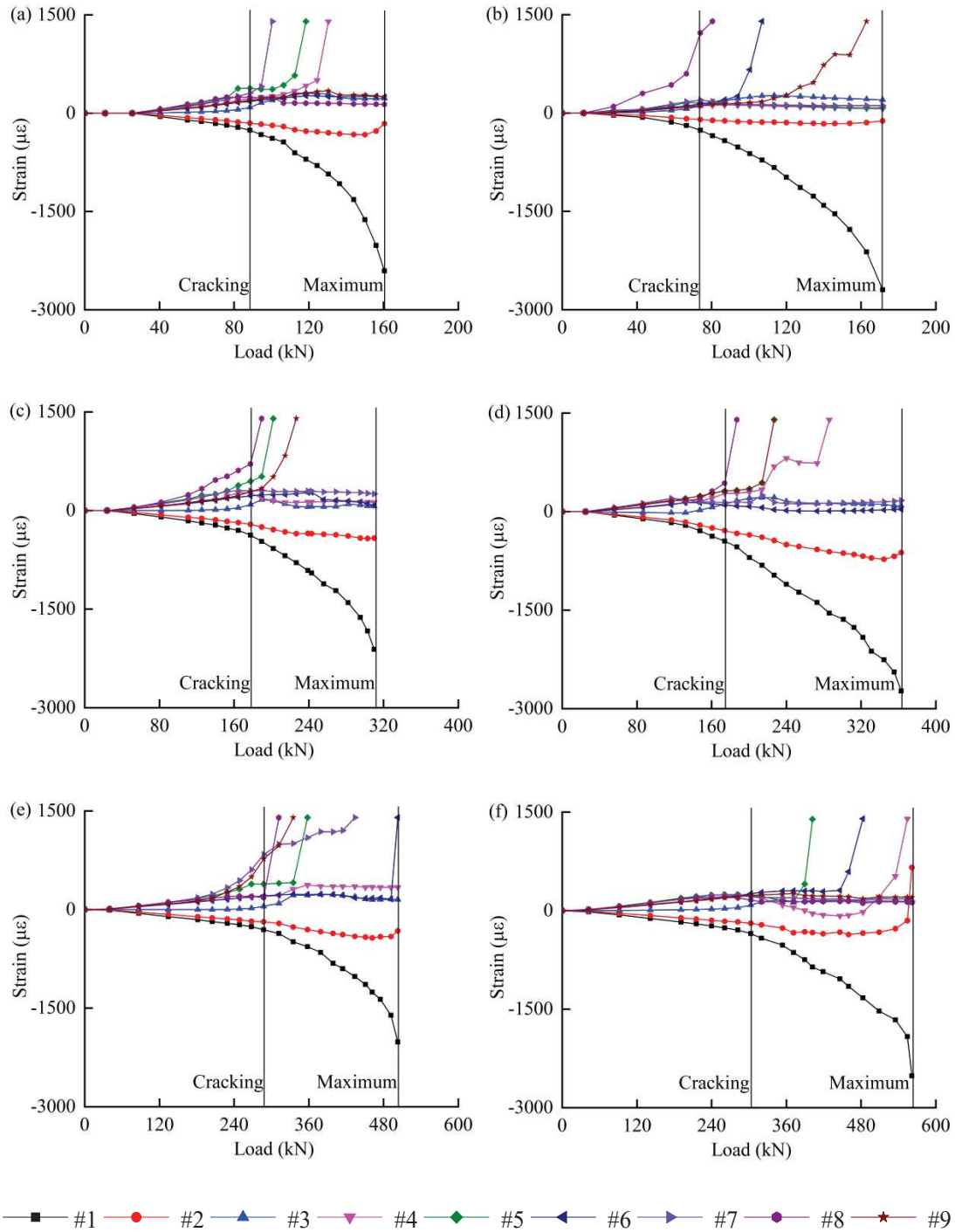


Figure 8. Concrete strain development of test specimens: (a) PHC400; (b) PSC400; (c) PHC500; (d) PSC500; (e) PHC600; (f) PSC600

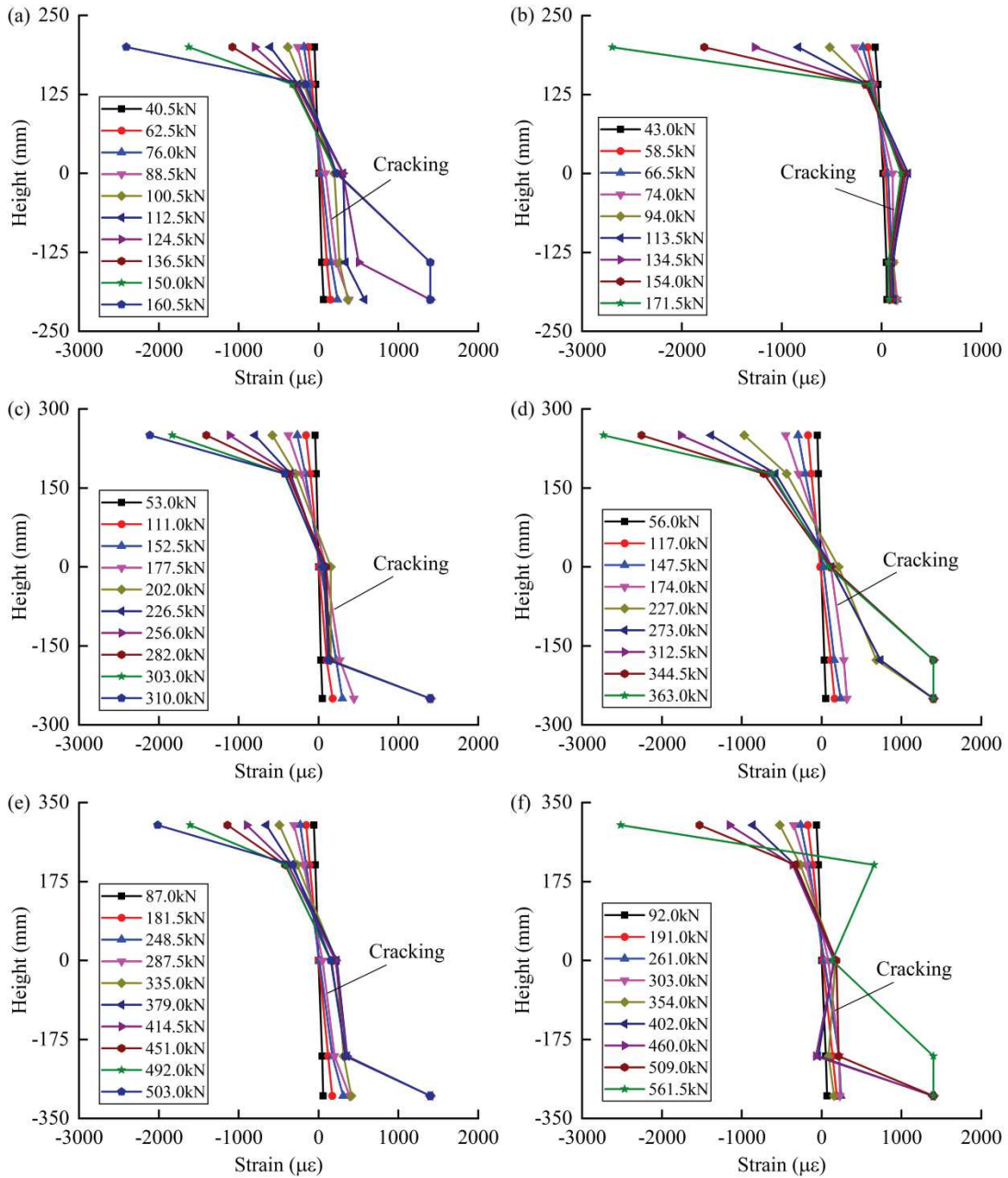


Figure 9. Concrete strain distribution over the depth of the midspan section: (a) PHC400; (b) PSC400; (c) PHC500; (d) PSC500; (e) PHC600; (f) PSC600

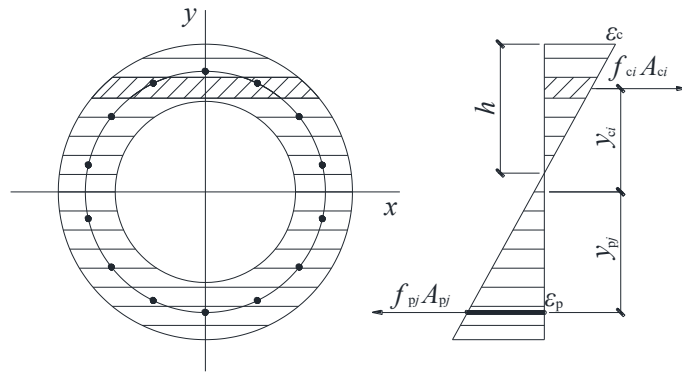


Figure 10. Pile cross-section and strain distribution for the general bending analysis

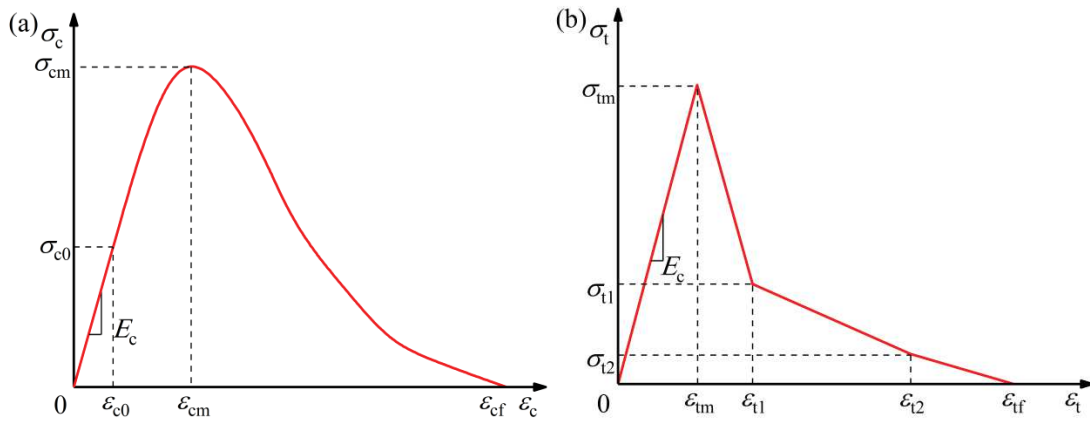


Figure 11. Stress-strain curves of concrete: (a) uniaxial compression; (b) uniaxial tension

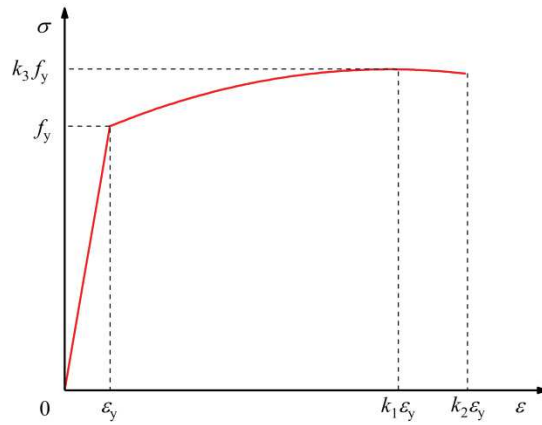


Figure 12. Stress-strain curve of reinforcing bar under uniaxial tension

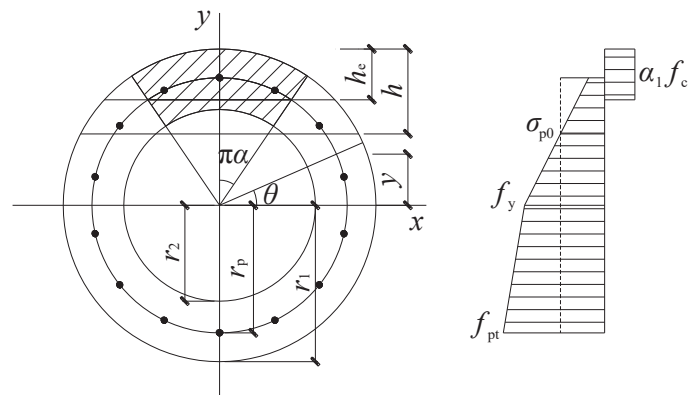


Figure 13. Cross-section stress distribution for the simplified calculation method

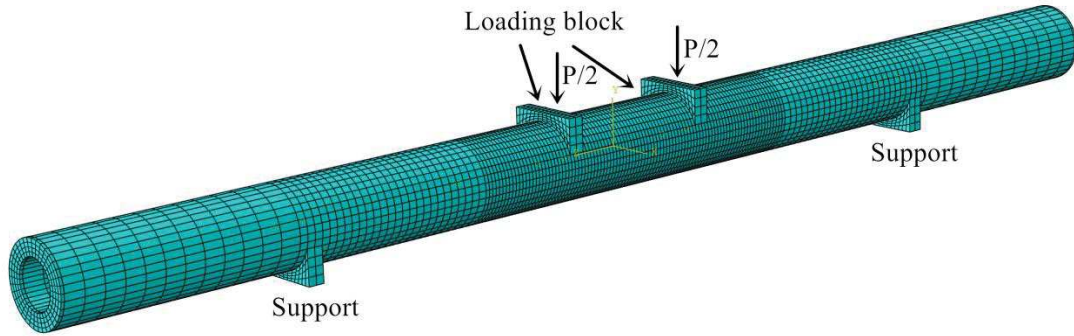


Figure 14. Schematic diagram of finite element model

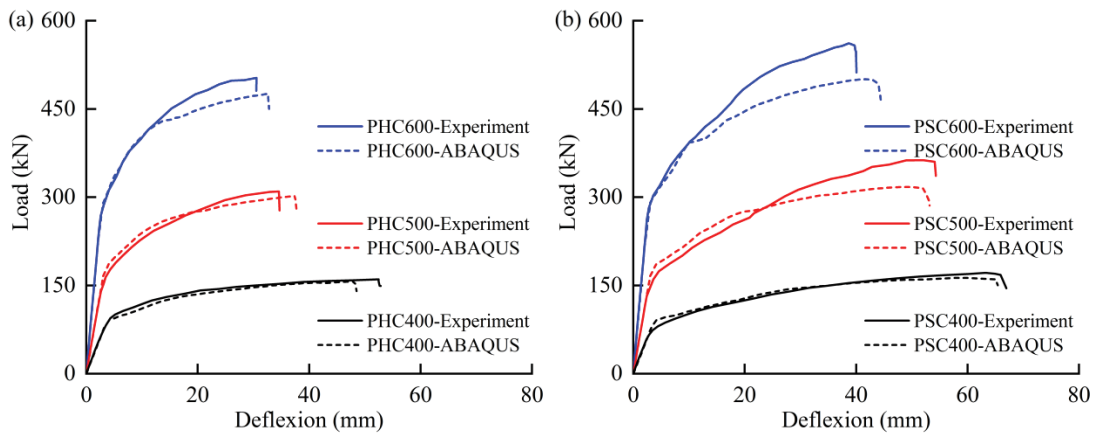


Figure 15. Comparison of load-deflection curves between numerical and experimental results

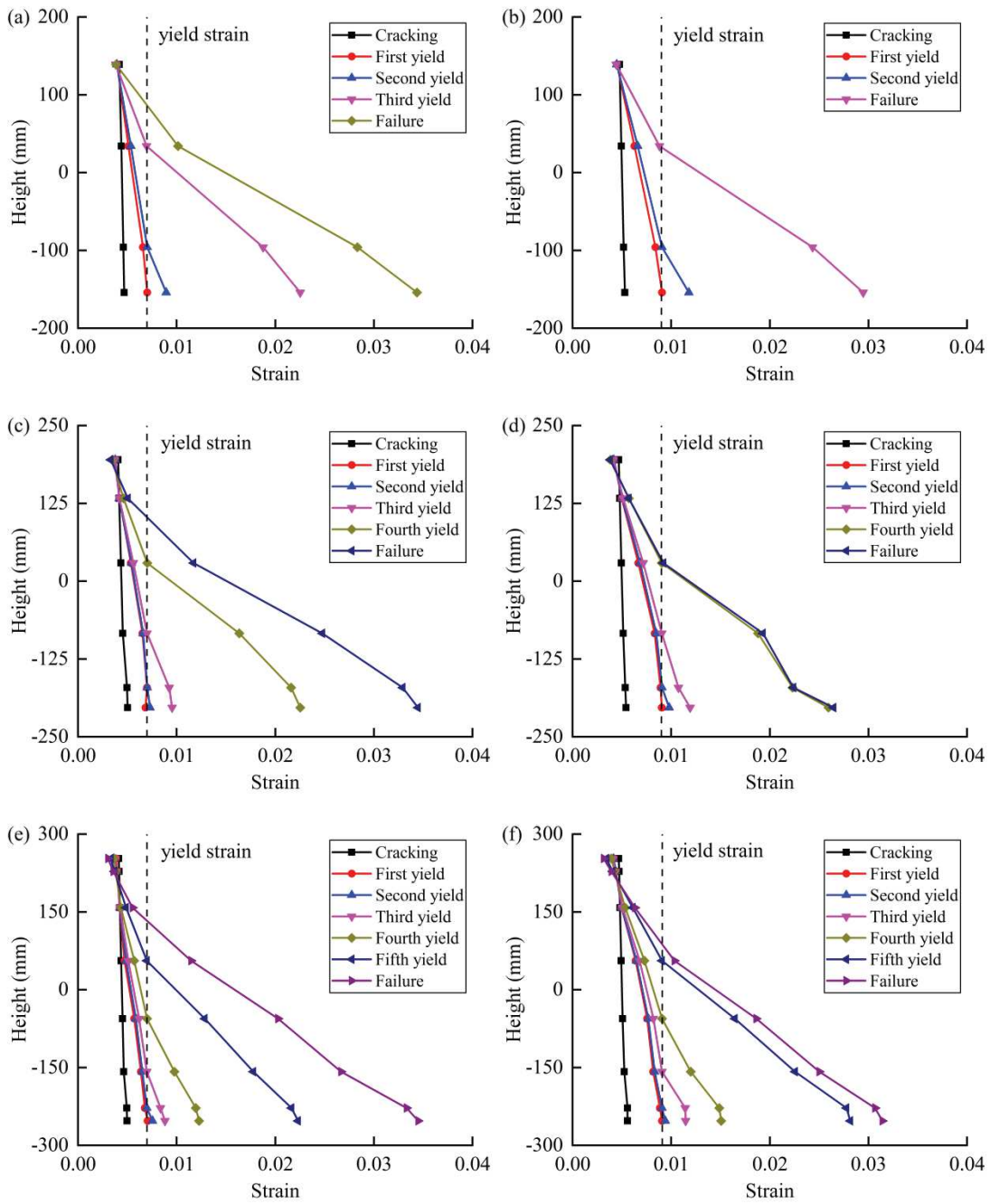


Figure 16. Strain distribution of prestressing tendons over the cross-section depth in the midspan

section: (a) PHC400; (b) PSC400; (c) PHC500; (d) PSC500; (e) PHC600; (f) PSC600

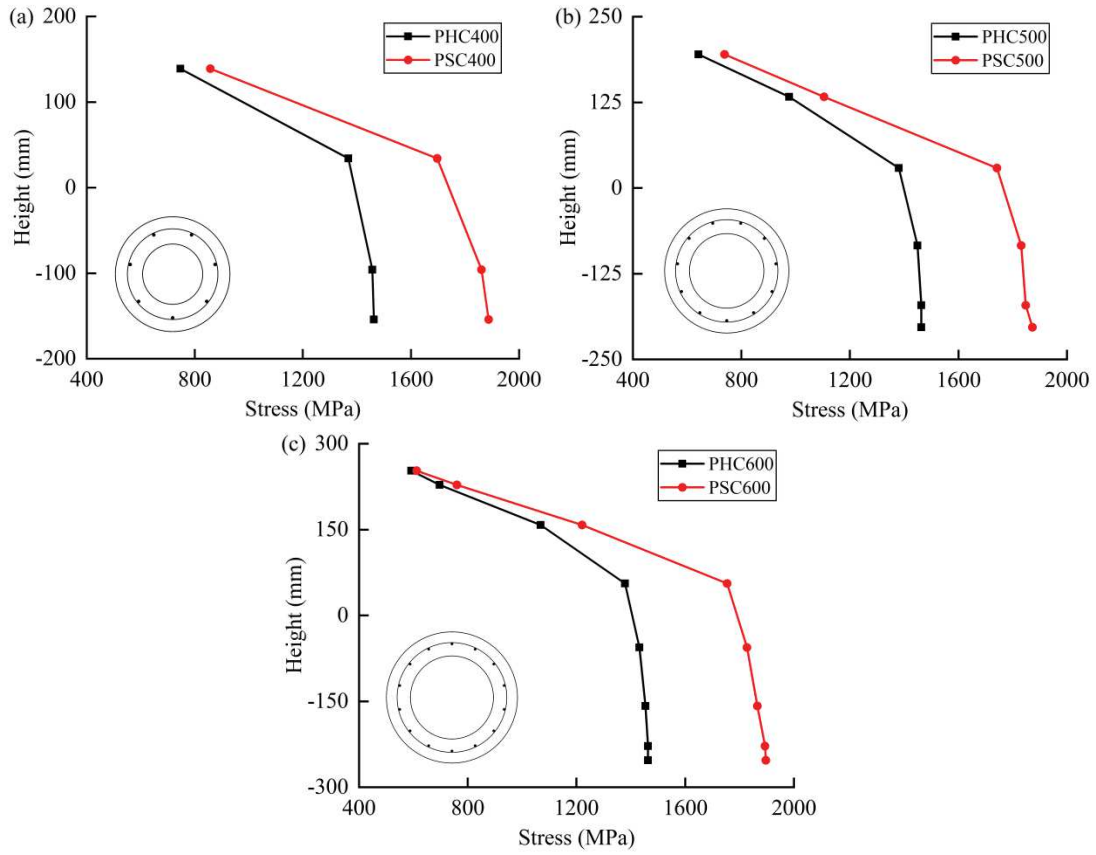


Figure 17. Stress distribution of prestressing tendons along the height of the midspan cross-section at failure

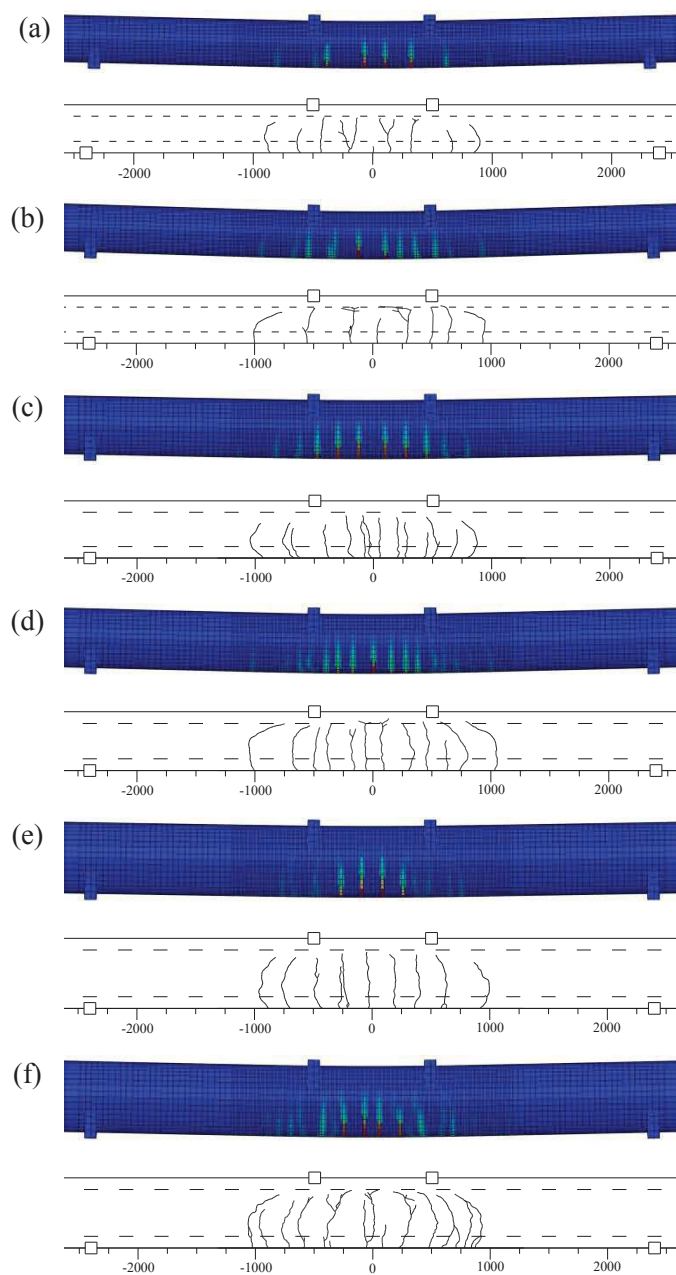


Figure 18. Crack distribution of numerical and experimental results for test specimens: (a) PHC400; (b) PSC400; (c) PHC500; (d) PSC500; (e) PHC600; (f) PSC600

Table 1. Geometric dimensions and reinforcement specifications of test specimens

| Pile type | D_1 (mm) | D_p (mm) | t (mm) | Longitudinal reinforcement | ρ_s (%) | Stirrup | σ_{con} (MPa) | σ_{ce} (MPa) |
|-----------|------------|------------|----------|----------------------------|--------------|------------------|----------------------|---------------------|
| PHC400 | 400 | 308 | 95 | 7 Φ^D 10.7 | 0.69 | Φ^b 4@45/80 | 994 | 5.99 |
| PSC400 | 400 | 308 | 95 | 7 Φ^S 11.1 | 0.57 | Φ^b 4@45/80 | 1302 | 5.57 |
| PHC500 | 500 | 406 | 100 | 11 Φ^D 10.7 | 0.79 | Φ^b 5@45/80 | 994 | 6.74 |
| PSC500 | 500 | 406 | 100 | 11 Φ^S 11.1 | 0.65 | Φ^b 5@45/80 | 1302 | 6.31 |
| PHC600 | 600 | 506 | 110 | 14 Φ^D 10.7 | 0.74 | Φ^b 5@45/80 | 994 | 6.40 |
| PSC600 | 600 | 506 | 110 | 14 Φ^S 11.1 | 0.61 | Φ^b 5@45/80 | 1302 | 5.98 |

Table 2. Material mechanical parameters of reinforcing bars

| Reinforcing bar | E_s (GPa) | f_y (MPa) | f_u (MPa) | δ (%) |
|-----------------|-------------|-------------|-------------|--------------|
| Φ^D 10.7 | 195 | 1342 | 1462 | 3.4 |
| Φ^S 11.1 | 195 | 1725 | 1920 | 6.4 |
| Φ^b 6 | 199 | 477 | 549 | 2.6 |

Table 3. Comparison of flexural performance of test specimens

| Pile type | $M_{cr,e}$ (kN·m) | $M_{cr,e,PSC}/M_{cr,e,PHC}$ | $M_{u,e}$ (kN·m) | $M_{u,e,PSC}/M_{u,e,PHC}$ | $f_{u,e}$ (mm) | $f_{u,e,PSC}/f_{u,e,PHC}$ |
|-----------|-------------------|-----------------------------|------------------|---------------------------|----------------|---------------------------|
| PHC400 | 87.6 | 0.84 | 156.0 | 1.07 | 52.47 | 1.20 |
| PSC400 | 73.8 | | 166.5 | | 63.22 | |
| PHC500 | 173.5 | 0.98 | 299.4 | 1.17 | 34.57 | 1.50 |
| PSC500 | 170.1 | | 349.8 | | 52.02 | |
| PHC600 | 279.8 | 1.05 | 484.9 | 1.11 | 30.55 | 1.26 |
| PSC600 | 294.5 | | 540.0 | | 38.63 | |

Table 4. Comparison between theoretical and experimental results

| Pile type | Experiment | General calculation method | | | Simplified calculation method | | |
|-----------|------------------|----------------------------|------------------|-------------------|-------------------------------|------------------|-------------------|
| | $M_{u,e}$ (kN·m) | h_g (mm) | $M_{u,g}$ (kN·m) | $M_{u,g}/M_{u,e}$ | h_s (mm) | $M_{u,s}$ (kN·m) | $M_{u,s}/M_{u,e}$ |
| PHC400 | 156.0 | 80.0 | 140.7 | 0.90 | 84.7 | 130.3 | 0.84 |
| PSC400 | 166.5 | 74.0 | 147.5 | 0.89 | 85.6 | 139.0 | 0.83 |
| PHC500 | 299.4 | 97.5 | 275.3 | 0.92 | 95.9 | 268.5 | 0.90 |
| PSC500 | 349.8 | 91.0 | 291.1 | 0.83 | 97.7 | 286.5 | 0.82 |
| PHC600 | 484.9 | 108.6 | 432.3 | 0.89 | 99.1 | 427.5 | 0.88 |
| PSC600 | 540.0 | 101.4 | 457.0 | 0.85 | 101.1 | 456.1 | 0.84 |

Table 5. Material parameter values of reinforcing bars

| Reinforcing bar | E_s (GPa) | f_y (MPa) | ε_y | k_1 | k_2 | k_3 |
|-----------------|-------------|-------------|-----------------|-------|-------|-------|
| $\Phi^D10.7$ | 195 | 1342 | 0.0069 | 4.93 | 5.22 | 1.09 |
| $\Phi^S11.1$ | 195 | 1725 | 0.0088 | 7.16 | 7.83 | 1.11 |
| $\Phi^b4/5$ | 199 | 477 | 0.0024 | 10.8 | 12.1 | 1.15 |

Table 6. Comparison of flexural performance between numerical and experimental results

| Pile type | $M_{cr,n}$ (kN·m) | $M_{cr,e}$ (kN·m) | $M_{cr,n}/M_{cr,e}$ | $M_{u,n}$ (kN·m) | $M_{u,e}$ (kN·m) | $M_{u,n}/M_{u,e}$ | $f_{u,n}$ (mm) | $f_{u,e}$ (mm) | $f_{u,n}/f_{u,e}$ |
|-----------|----------------------|----------------------|---------------------|---------------------|---------------------|-------------------|-------------------|-------------------|-------------------|
| PHC400 | 89.8 | 87.6 | 1.03 | 152.4 | 156.0 | 0.98 | 48.21 | 52.47 | 0.92 |
| PSC400 | 89.6 | 73.8 | 1.21 | 158.4 | 166.5 | 0.95 | 59.71 | 63.22 | 0.94 |
| PHC500 | 172.8 | 173.5 | 1.00 | 291.8 | 299.4 | 0.97 | 37.49 | 34.57 | 1.08 |
| PSC500 | 174.6 | 170.1 | 1.03 | 306.6 | 349.8 | 0.88 | 48.95 | 52.02 | 0.94 |
| PHC600 | 270.3 | 279.8 | 0.97 | 458.7 | 484.9 | 0.95 | 32.63 | 30.55 | 1.07 |
| PSC600 | 274.3 | 294.5 | 0.93 | 482.3 | 540.0 | 0.89 | 41.20 | 38.63 | 1.07 |