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1                   Crack Monitoring using Short-gauged Brillouin Fiber Optic Sensor

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3                   Tianran Han <sup>a,b</sup>, Gang Wu <sup>a,b,\*</sup>, Yong Lu <sup>c</sup>

4                   <sup>a</sup> *National and Local Joint Engineering Research Center for Intelligent Construction and*  
5                   *Maintenance, Nanjing 211189, China*

6                   <sup>b</sup> *Key Laboratory of Concrete and Prestressed Concrete Structures of the Ministry of*  
7                   *Education, Southeast University, Nanjing 211189, China*

8                   <sup>c</sup> *Institute for Infrastructure and Environment, School of Engineering, The University of*  
9                   *Edinburgh, Edinburgh EH9 3JL, UK*

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10  
11                  **Abstract**

12                  Detection and quantification of cracks for various civil infrastructures on a large scale  
13                  are difficult both technologically and economically through current sensing  
14                  methodologies. This study presents a novel fiber-optic sensor named short-gauged  
15                  Brillouin fiber optic sensor, which enables basic Brillouin-based analyzers to achieve  
16                  early crack detection and accurate crack width measurement. The concept and design  
17                  of the proposed sensor are firstly introduced, followed by respective instrumentation  
18                  procedures. On this basis, theoretical deduction and numerical simulations of the  
19                  crack-induced Brillouin gain spectrum (BGS) response using the proposed sensor are  
20                  carried out, verified subsequently by controlled laboratory tests. The measured BGS  
21                  responses are then leveraged for crack detection and quantification. A  
22                  peak-fitting-based methodology was adopted to analyze the BGS data to achieve  
23                  accurate crack width measurement. The proposed methodology may facilitate  
24                  economical long-distance distributed crack sensing and quantification for various  
25                  infrastructures as a genetic technique.

26  
27                  *Keywords:* distributed fiber optic sensing, crack sensing, short-gauged Brillouin fiber

30 **1. Introduction**

31 Crack formation is a common form of structural degradation in civil infrastructure  
32 due to aging, fatigue, unfavorable loading, or environmental processes [1]. Crack  
33 development in structures inevitably affects the infrastructure in terms of its  
34 functionality, aesthetics, durability, and even safety. For reinforced concrete (RC)  
35 structures, when crack opening exceeds a certain level (0.2 to 0.4 mm depending on  
36 environment), the corrosion process of steel reinforcement within the structures may  
37 be accelerated by chemical ingression, thus adversely affecting structural durability.  
38 Larger cracks in the order of 1 mm or greater could indicate severe damage in the  
39 structures that may require immediate attention for retrofitting [1, 2]. Therefore,  
40 awareness and assessment of the in-place cracks are crucial for various infrastructure  
41 structural elements.

42 However, early-stage structural cracks are small and often take place randomly in a  
43 sporadic distributive manner. Compounded with the size and scale of the  
44 infrastructure systems, these make detection of early-stage cracks particularly difficult  
45 and even harder for quantification. Monitoring options that can tackle large-scale  
46 crack detection and quantification problems, and do it economically, could produce  
47 crucial information for timely preventive structural maintenance, leading to prolonged  
48 service life and reduced maintenance costs in life-cycle management.

49        In engineering practice, the acquisition of crack information has conventionally  
50        relied on periodic visual inspections, which can be time-consuming, expensive, and  
51        unreliable. While various nondestructive testing (NDT) techniques may be used to  
52        facilitate the examination for structural damages or cracks, they share the difficulty of  
53        accurately measuring crack openings and render real-time evaluations for the  
54        structural status [3].

55        On the other front, sensors capable of continuous monitoring in time, such as strain  
56        sensors (electrical or fiber Bragg grating) are typically discrete or quasi-distributive  
57        sensors that can only detect cracks if they occur at immediate proximity of the sensing  
58        locations. Such sensors tend to suffer from possible miss detection of cracks, and  
59        extensive scale application of these types of sensors will be constrained by the high  
60        sensor costs and the hosting capacity of the analyzers [4, 5].

61        Although distributed fiber optic crack sensing can be realized using  
62        signal-loss-based methods based on OTDR (Optical Time Domain Reflectometer) [6,  
63        7]. These applications usually involve orchestrating special zigzag sensor installation  
64        schemes and can be challenging to achieve long-range monitoring due to the potential  
65        depletion of the light power budget along the sensing fiber. Likewise, the  
66        Rayleigh-scattering-based technique, which has recently grown in popularity, can  
67        achieve high spatial resolution (smaller than 10 mm) but at the cost of a short  
68        achievable measurement range (upper limits within 100 meters). As such, their  
69        application has been primarily limited to laboratory tests [8, 9].

70        Brillouin-based fiber-optic distributed sensing is a promising technology for  
71        long-range deformation monitoring of many types of infrastructure such as bridges

72 [10, 11], pipelines [12, 13], tunnels [14]. The technology enables retrieval of  
73 continuous measurement of strain for structures up to tens of kilometers.

74 Studies have been carried out in crack and deterioration sensing using Brillouin  
75 fiber optic sensors, valuing their fully distributive nature to achieve a higher  
76 likelihood of intersecting potential cracks. Those sensing methods customarily rely on  
77 searching for spikes in the distributed strain profiles obtained by the sensing systems  
78 [15, 16]. However, with the standard options of commercially-available Brillouin  
79 sensing systems, the best achievable spatial resolution (SR) is often in the order of 0.5  
80 to 1.0 m, which is apparently a significant drawback when it comes to crack or  
81 deterioration detection where information of localized deformation is of interest. SR  
82 defines the smallest length corresponding to strain events that can be measured with  
83 defined or targeted accuracy [17]. An experimental study involving a 15-m-long beam  
84 showed that the strain localization due to structural defects tended to be masked by  
85 the low spatial resolution effect of the Brillouin analyzer, making the distributed strain  
86 measurement insensitive to the crack formation[18]. Consequently, the sensing  
87 measurement was neither capable of accurately localizing the defects nor capable of  
88 indicating their severity via the measured strain amplitudes.

89 In coping with the unfavorable effects from low SR of the Brillouin analyzer on  
90 crack detection, a signal-processing approach was described based on the  
91 decomposition of the distributed strain data from BOTDR (Brillouin optical  
92 time-domain reflectometer) using the stationary wavelet-transform method. It  
93 achieved improved crack features and enhanced data quality [19]. However, this  
94 method requires a dense spatial sampling rate from the analyzer along the

95 measurement fiber, which may not be commonly available, and the specific wavelet  
96 function and determination of the vanishing moment may differ for different  
97 problems. Another attempt involved a data processing methodology using the  
98 maximum compressive or tensile peaks in the Brillouin frequency spectrum to obtain  
99 the distributed strain instead of the distributed strain obtained by conventional  
100 methods [20]. As such, enhanced sensitivity was achieved for crack detection.  
101 However, these methods cannot be used to quantify crack width accurately.  
102 Quantification for crack sizes and numbers based on distributed strain has relied  
103 primarily on statistical and empirical approaches, such as proposing quantitative  
104 empirical parameters and relating them to many experimental observations [21],  
105 rendering crack assessment on a case-by-case basis. Understandably, crack formation  
106 will introduce complicated strain distribution to the distributed fiber optic sensors,  
107 which will create distortions to the Brillouin gain spectrum (BGS) [21, 22]. A  
108 Brillouin-based crack sensor was developed capable of detecting cracks less than 1  
109 mm in width, and a sensor installation technique was devised using specialized glue to  
110 avoid sensor breakage as crack occurs [23]. The sensor relies on redistribution of  
111 crack-induced strain through partial sensor detachment from the attached structure to  
112 achieve crack detection by examining the respective spectrum feature. However, the  
113 mechanical interface behavior may possess a considerable degree of variation in  
114 relation to crack opening based on specific interfacial conditions. Tests revealed that  
115 the detachment could only happen when relatively large cracks occur. Therefore,  
116 while the methodology enabled detecting relatively large cracks (in the order of 0.5  
117 mm or more), it is also difficult to obtain accurate crack quantification [24].

118 To quantitatively assess cracks, long-gauge distributed fiber optic sensors (gauge  
119 length greater than SR of the analyzer) were adopted along with several other unique  
120 installation methods involving the usage of acrylic disk guides[25]. Their  
121 effectiveness in measuring total crack width within a particular structural region  
122 through strain-displacement conversion was verified by reinforced concrete (RC)  
123 beam testing. However, these long-gauge arrangements would only obtain the  
124 averaged crack width information, likely missing the detailed information for  
125 individual cracks. It would also be difficult to tell if the measured strain increments  
126 indeed arise from the crack formation. Besides, the installation methods involving  
127 superposition loops can be complex to apply in the field.

128 Another way to obtain a more sensitive crack-sensing capability for the Brillouin  
129 fiber optic strain sensors relies on directly improving the SR of the analyzers.  
130 Although directly decreasing the pump pulse duration could supposedly improve the  
131 spatial resolution, it comes at a price of lowered signal-to-noise ratio (SNR) and thus  
132 decreased accuracy of sensor sensitivity, thereby practically limiting the spatial  
133 resolution to about 1 m. Some similar special techniques have been proposed to  
134 achieve higher SR, and at the same time, avoid compromising the strain resolution.  
135 For instance, Differential Pulse-width Pair BOTDA (Brillouin optical time-domain  
136 analysis) [26], Pump pre-pulse BOTDA [27], Gain-Profile Tracing BOTDA [28], and  
137 other techniques involving ‘Bright pulse’ [29], ‘Dark pulse’ [30] or ‘Brillouin  
138 echoes’[31]. The common basis of these techniques is the pre-excitation of the  
139 acoustic field. While some of these techniques can facilitate the attainment of SRs in  
140 the order of several centimeters, enabling crack sensing capacity for micro-cracks

141 [32], expenses always follow at other aspects, such as the requirement for long time  
142 measuring, shorter sensing length, increased system sensitivity to noises, more  
143 sophisticated and sensitive systems which are rarely commercially available and often  
144 expensive.

145 In order to achieve accurate measurement of cracks, another hurdle exists besides  
146 the SR-related issues of the Brillouin analyzer-it is essential to understand the  
147 crack-induced strain transfer mechanisms between the cracked structures and the fiber  
148 optic sensors. The traditional approach of distributed fiber optic strain sensing aiming  
149 for crack or deterioration detection has primarily relied on overall bonding (OB) the  
150 sensing cables to the monitoring structures, such as in the cases of concrete beams [20,  
151 33], bridges [11], and pipelines [12, 16]. Although linear elastic response can be  
152 derived in coping with tiny cracks [32], this underlying assumption inevitably limits  
153 the prediction accuracy when nonlinear responses come into play. Extensive research  
154 suggests that the crack-induced strain transfer in fiber optic sensors is a highly  
155 complex and variable phenomenon that involves different types of nonlinearities, such  
156 as detachment, plasticity, and slippage between substrata layers, depending on  
157 specific fiber optical sensor design, gel properties, installation methods, and  
158 characteristics of the monitored structures [8]. Therefore, considerable difficulties  
159 exist in reaching a generic crack quantification solution that can cope with cracks of  
160 various sizes, from different origins, and for multiple applications, using the standard  
161 sensor instrumentation technique.

162 This study presents a novel fiber-optic sensor concept and design named  
163 short-gauged Brillouin fiber optic sensor, which enables basic Brillouin-based



164 analyzers to detect and accurately quantify events of cracks or structural  
165 discontinuities. The short-gauged Brillouin fiber optic sensor may potentially  
166 facilitate the attainment of economical long-distance distributed crack sensing and  
167 quantification for Structural Health Monitoring (SHM) of various infrastructures. The  
168 proposed sensor can become a powerful generic crack sensor capable of crack early  
169 warning through identifying distinctive crack signatures and accurate crack-width  
170 measurement, minimizing uncertainties from different fiber and adhesive properties  
171 and instrumentation details where the traditional OB instrumentation approach usually  
172 confronts. The proposed instrumentation method also constructs a new way to deploy  
173 distributed fiber optic sensors, besides the traditional overall bonding and  
174 point-fixation (long-gauge) approach.

175 The paper starts by introducing the concept, design, and installation scheme of the  
176 proposed sensor. Afterward, theoretical deduction and numerical simulations of the  
177 BGS response due to crack propagation, using the proposed sensors, are carried out.  
178 The results demonstrate the characteristics of the BGS transformation in different  
179 evolutionary stages as the crack propagates, which are then verified by a controlled  
180 laboratory test. Finally, the effectiveness of using the proposed sensors as crack  
181 meters is studied and discussed by extracting the crack information via proper data  
182 processing of the experimental data.

## 183 **2. Short-gauged Brillouin fiber optic sensor: concept and design**

184 For distributed fiber optic sensors, two different installation techniques usually  
185 apply in practice, namely the overall bonding (OB) method and the point-fixation (PF)

186 method [25]. The OB method continuously attaches the fiber optic sensors to the  
187 structure being monitored via adhesives or through embedment, while the PF method  
188 only fixes the fibers to the structure at discrete locations by anchorage points spaced  
189 at specific intervals. This spatial interval between the anchorage points is termed  
190 gauge length (GL), as shown in Fig. 1.

191 Both of these methods have been extensively implemented in the monitoring  
192 practice [14, 34, 35]. For example, the OB installation method was applied in tunnel  
193 SHM projects to assess the shield tunnel lining's cross-sectional performance in  
194 Barcelona[35] and London[14]. Likewise, a field trial utilizing PF installation method  
195 to monitor an existing tunnel's distortion movement due to the adjacent new tunneling  
196 activities was reported [34]. The PF was achieved by attaching an optical fiber around  
197 the circumference inside the tunnel linings using wheels. The OB method could  
198 potentially preserve the detailed distributed deformational information of the  
199 monitored structures; however, due to the complex nature of the strain transfer  
200 mechanism, extraction of local deformational information can often be tricky. Further,  
201 discontinuities in the structure, such as cracks, may render fiber optic cable to  
202 fracture, causing the sensing system to fail. On the other hand, the PF method usually  
203 takes the form of a long-gauge arrangement, providing average strain information  
204 between the fixation points, which can, in general, provide straight-forward  
205 strain-displacement conversions. The PF method also tends to be free from the risks  
206 of crack-induced cable ruptures due to avoidance of exceedingly large local stress in  
207 the fiber. For field applications, the gauge length adopted for the Brillouin sensor  
208 using PF installation ranges typically in the order of 0.5 to 2 meters, depending on

209 specific applications. In regular practice, assurances are guaranteed that the fiber optic  
210 sensor's gauge length shall be greater than the SR of analyzers for enhanced sensing  
211 system repeatability and easier on-site sensor instrumentation. However, due to the  
212 long-gauge arrangement, information loss is inevitable of the detailed strain  
213 distribution between fixation points. Moreover, for most applications, the  
214 achievement of point fixation relies on accurate positioning and installation of  
215 anchorages on site, which can be time-consuming.

216 In light of the shortcomings of the conventional installation techniques, we hereby  
217 propose a novel fiber-optic sensor concept and design that could potentially facilitate  
218 the retrieval and quantification of critical localized deformation beneath the analyzer's  
219 SR level when proper data processing methodologies are introduced. The key idea is  
220 to come up with a fiber optic sensor concept that could achieve a densely spaced array  
221 of strain measurements below the analyzer's SR, with a sufficiently simple  
222 relationship of strain-displacement conversion within the sensor, so that localized  
223 structural deformation will transform into a salient local strain of the sensor in a fully  
224 controlled manner. As such, crack information can be extracted with much ease.

225 We hereby define a sensor concept named short-gauged Brillouin fiber optic sensor  
226 (SGB-FOS). The SGB-FOSs are fiber optic strain sensors discretely spot-fixed to the  
227 monitored structure with sensing GLs smaller than half of the SR of the adopted  
228 Brillouin analyzers. The extraction of the crack quantification information will be  
229 relying on analyzing the Brillouin gain spectrum (BGS) responses. We define the GLs  
230 to be smaller than half of the analyzer's SR so that the crack-induced BGS evolutionary  
231 process could form a consistent pattern with sensitive crack signatures for further data

232 processing. Details of this will be illustrated in later sections. This concept will result  
233 in sensor GL in the order of 50 mm to 500 mm for typical commercially available  
234 Brillouin fiber-optic analyzers (basic BOTDAs and BOTDRs), depending on their  
235 achievable SRs. The specific choice of the sensor GL depends on the purpose of  
236 monitoring and the type of monitored structure. For example, it might be appropriate  
237 to select a gauge length close to or slightly smaller than the expected crack intervals  
238 of RC structures for crack quantification.

239 The spot-fixation arrangement of the SBG-FOS allows a fully controlled  
240 strain-displacement conversion. Specifically, the strain generated between the  
241 anchorage points in the sensor will resemble a uniform distribution instead of much  
242 more complicated distributions within OB sensors. This avoids unnecessary nonlinear  
243 response at the sensor level. The spot-fixation arrangement also tends to make the  
244 sensing system more robust against localized large deformation due to avoidance of  
245 extreme strains that could lead to fiber ruptures. Furthermore, the spot-fixation  
246 arrangement makes sensing of the local strain reversible, meaning that not only crack  
247 expansion but its closure can be equally measured.

248 Fiber optic sensors using PF installation can be tricky to install in practice due to  
249 the difficulty of creating a densely-spaced array of anchorages along the fiber optic  
250 sensors. Therefore, good sensor design and installation procedures are vital to make  
251 the SBG-FOS concept applicable in practice.

252 We hereby exemplify a sensor design that enables an easy short gauge formation in  
253 the sensor installation process. The proposed sensor design comprises a standard  
254 tight-buffered strain-sensing cable and a unique outer tubing sleeve, forming a

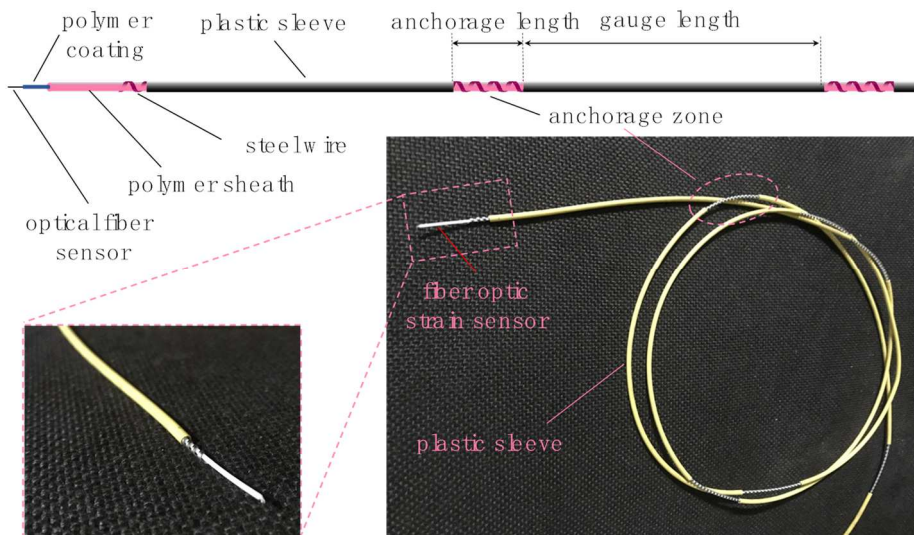
255 flexible simple-structured cable sensor. The inner sensing cable is free to slide inside  
256 of the outer sleeve. The sensing cable adopts G652D single-mode optical fiber with  
257 the core and cladding measured 9.5  $\mu\text{m}$  and 125 $\mu\text{m}$  in diameter, respectively. The  
258 coating and buffer are made of soft plastic and polyamide with an outer diameter of  
259 0.9 mm. The sleeve with an inner diameter of 1.5 mm is composed of an inner  
260 stainless steel strangle layer and an outer plastic layer. The sleeve tubing exists for  
261 two main functions: protecting the internal sensor and forming a short-gauge  
262 arrangement. The stainless steel strangle layer provides necessary strength sheltering  
263 against possible mechanical impacts and achieving high durability against corrosions.  
264 The short-gauge arrangement is pre-formed through sensor fabrication by open  
265 windows discretely at the design gauge length in the outer plastic layer of the tubing  
266 sleeve. Fig.1 schematically shows details of the proposed sensor.

267 During the field deployment, the outer sleeve is segmented into 10-20 meter  
268 sections to facilitate easier handling. After properly cleaning the structural surface, the  
269 proposed sensor is first attached to the monitoring structure surface by gluing the  
270 sleeves sparsely in the plastic-covering zones. After this, one end of the internal strain  
271 sensor is point-glued to the structure by fast glue or otherwise fastened by clamps.  
272 After the anchorage becomes effective, pre-stress is applied sequentially to the  
273 internal sensing cable until the complete coverage of the sensor is under stress. The  
274 conservation of the pre-stress is ensured by timely fixing the other end of the internal  
275 sensing cable to the structure, either by glue or clamps as anchorages. The procedure  
276 to pre-stress the strain-sensing cable on site, is to the greatest extent, attempting to

277 generate a uniform initial strain distribution within the fiber optic sensor, which is  
278 essential for crack identification at the later stage.

279 The pre-stress enables the sensor to detect compressive deformation of the  
280 structure. The magnitude of the pre-stress should be chosen according to the specific  
281 application and fiber optic sensors. In our installation, the fibers are generally  
282 pre-strained to around 3000  $\mu\epsilon$ . Care should be taken on-site to prevent dust and dirt  
283 from penetrating the sensor in the installation stage, which can be achieved by  
284 providing certain coverage or protection before the pre-stressing process. After  
285 pre-stressing, a special gel is applied to cover the sensor, gluing it to the structure  
286 entirely. Meanwhile, short-gauged anchorages are automatically formed due to gel  
287 penetration through the windows in the sensor sleeves to the internal strain cable. The  
288 gel is epoxy-resin-based, specially developed through a series of laboratory tests to  
289 possess optimized viscosity and working time, which enable it to penetrate the sensor  
290 sleeves, stably glue the sensors to the structure and accurately stay in the window area  
291 without spreading to the unintended region of the internal sensor. After hardening, the  
292 gel provides another effective protection layer for the sensor against potential  
293 detrimental environmental impacts. Additional protection should be provided for the  
294 exposed fiber regions. Fig.1 and Fig.2 demonstrate the design and instrumentation  
295 procedure of the proposed sensor. Fig.3 illustrates an example of the SGB-FOS  
296 application inside an operational shield metro tunnel to assess the tunnel lining  
297 structures' long-term circumferential structural performance. The tunnel is buried in  
298 the Eastern China soft ground, being disturbed by some nearby construction activities.  
299 The instrumentation of the sensors was carried out at mid-night time windows after all

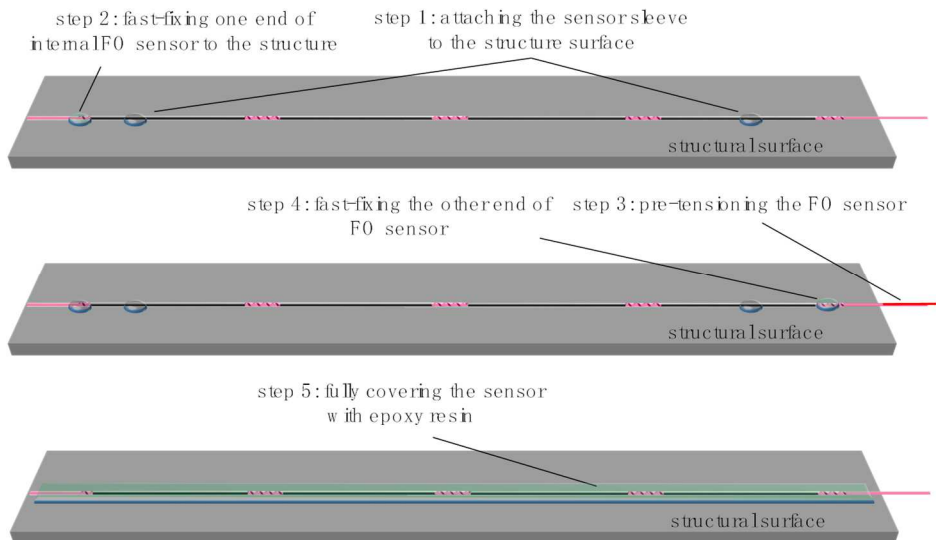
300 train operations were stopped. The installation of the proposed sensor inside the  
 301 tunnel was proved to be convenient and fast.



302

303 **Fig.1.** Distributed short-gauged Brillouin fiber optic sensor.

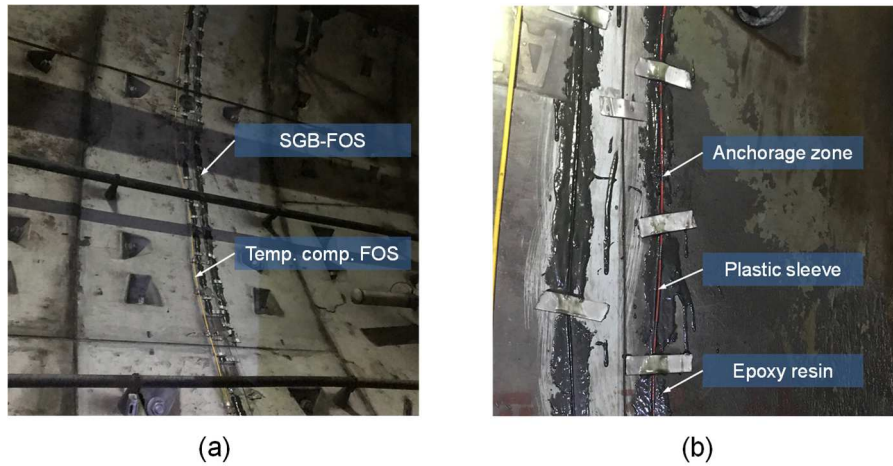
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305

306 **Fig.2.** SGB-FOS installation procedures.

307



308

309 **Fig.3.** Example of SGB-FOS installed inside a shield metro tunnel: (a)  
 310 instrumentation of the SGB-FOS for tunnel cross-sectional SHM; (b) the close-up  
 311 view of the installed SGB-FOS on tunnel lining.

312 **3. SGB-FOSs for crack sensing: theory and numerical simulation**

313 As crack forms, the concentrated strain will occur in the proposed fiber optic  
 314 sensor. This crack-induced strain is generally much larger than the strain at uncracked  
 315 structural sections. For example, a 0.2 mm crack would introduce a  $2000 \mu\epsilon$  in an  
 316 SGB-FOS of 100 mm GL, which can be one order greater than the background strain  
 317 of uncracked sections. This major sub-spatial resolution event will distort the shape of  
 318 the BGS profile from the standard one when the strain within the SR is uniformly  
 319 distributed. Therefore, the extraction of the Brillouin frequency shift (BFS) adopted  
 320 by the analyzers through standard peak fitting procedures will render significant error,  
 321 thus no longer suited to accurately extract the quantitative information of the crack



322 [36, 37]. Therefore, a theoretical framework of the BGS evolution with crack  
323 propagation using the proposed fiber optic sensor should be established.

### 324 *3.1. Crack-induced strain in SGB-FOSs*

325 Due to the spot-fixation arrangement, the strain transfer mechanism between the  
326 structure and the short-gauged fiber optic sensor is considerably simplified. As a crack  
327 occurs, the crack displacement will translate into a spiking localized strain between  
328 anchorage points of the sensor bridging over the crack. For simplicity, we assume that  
329 the crack-induced strain is uniformly distributed within a certain gauge length,  
330 featuring a prominent rectangular peak. Although there exist transient regions for the  
331 strain to build up from the background strain to the rectangular peak, we can  
332 approximate this effect by introducing a nominal gauge length to cope with their  
333 influence on the BGS response (see Fig. 4). Theoretically, this nominal gauge length  
334 is always greater than the fiber optic sensors' design gauge length.

335 Let  $k_1$  denote the ratio of the design gauge length ( $GL_d$ ) to the nominal gauge  
336 length ( $GL_n$ ), which is a value of less than 1.0 (see Eq.1). Also, due to the shear lag in  
337 the substrata of the fiber optic sensors, the strain transfer from the crack displacement  
338 to the optical fiber core can never be 100%. Therefore, the measured strain from the  
339 fiber optic sensor will always be smaller than that from direct crack width ( $d$ )  
340 conversion. This effect is indicated by a strain transfer factor  $k_2$ , which is also a  
341 factor smaller than 1.0. The specific values of  $k_1$  and  $k_2$  may rely on various  
342 factors, such as the strain sensing cable, fixation methods, and gauge length.  
343 Individual estimation of the exact values of  $k_1$  and  $k_2$  would require detailed

344 material qualities of the fiber optic sensor or via refined experimental measurements  
345 capable of obtaining high-SR distributed strain using, for example, the  
346 Rayleigh-scattering-based strain measuring technique. However, their effect for crack  
347 strain evaluation can be represented by a combined factor  $k$ , which could be obtained  
348 experimentally. Therefore, the crack induced strain ( $\varepsilon_c$ ) for the short-gauge sensor can  
349 be formulated in equation (2).

$$k_1 = GL_d / GL_n \quad (1)$$

$$\varepsilon_c = k_2 d / GL_n = k_2 d / GL_n = k_1 k_2 d / GL_d = kd / GL_d \quad (2)$$

### 350 *3.2. Modeling the measurement system*

351 The proposed sensor is based on the Brillouin nonlinear process that takes place in  
352 single-mode optical fibers. The most commonly used Brillouin fiber optic  
353 interrogation systems are BOTDA and BOTDR, which employ the principles of  
354 stimulated Brillouin scattering and spontaneous Brillouin scattering, respectively. The  
355 proposed crack sensing methodology can be applied to both of these systems.  
356 However, for the theoretical introduction, we will base our discussion on BOTDA  
357 systems.

358 In stimulated Brillouin scattering (SBS), the interference of the forward  
359 propagating pump wave ( $A_{\text{pump}}$ ) and the backward propagating probe wave ( $A_{\text{probe}}$ )  
360 creates a moving optical intensity wave. Due to the phenomenon of electrostriction,  
361 the moving intensity wave induces a corresponding acoustic wave ( $Q$ ) moving in the  
362 same direction as the pump. The generation efficiency of the acoustic wave depends

363 on the relative magnitude of the pump-probe frequency offset ( $v_a$ ) and a characteristic  
 364 frequency shift called Brillouin frequency shift ( $v_B$ ), which is a function of the local  
 365 temperature and mechanical stress in the fiber. The maximum growth of the acoustic  
 366 wave is reached provided  $v_a$  equals to  $v_B$ . Due to the elasto-optic effect, the  
 367 optically-induced acoustic wave functions as a moving refractive Bragg grating.  
 368 Coupled with the Doppler effect, this moving Bragg grating is responsible for a  
 369 coherent power transfer that results in a net gain of the probe and net loss of the pump  
 370 for Stokes process.

371 Mathematically, the assumed co-polarized, but counter-propagating pump ( $A_{pump}$ )  
 372 and probe ( $A_{probe}$ ) waves generate an acoustic field ( $Q$ ), which couples the two optical  
 373 fields. The propagation of these three waves is governed by [38]

$$\frac{\partial A_{pump}(z,t)}{\partial z} + \frac{1}{V_g} \frac{\partial A_{pump}(z,t)}{\partial t} = i \frac{1}{2} g_2 A_{probe}(z,t) Q(z,t) - \frac{\alpha}{2} g_2 A_{pump}(z,t) \quad (3)$$

$$\frac{\partial A_{probe}(z,t)}{\partial z} - \frac{1}{V_g} \frac{\partial A_{probe}(z,t)}{\partial t} = -i \frac{1}{2} g_2 A_{pump}(z,t) Q^*(z,t) + \frac{\alpha}{2} A_{probe}(z,t) \quad (4)$$

$$\frac{\partial Q(z,t)}{\partial t} + \Gamma_A Q(z,t) = i g_1 A_{pump}(z,t) A_{probe}^*(z,t) \quad (5)$$

$$\Gamma_A = 2\pi i \frac{v_B^2 - v^2 - i v \Gamma_B / 2\pi}{2v} \quad (6)$$

374 where  $g_1$  and  $g_2$  represent the electrostrictive and elasto-optic coupling effects,  
 375 respectively.  $\Gamma_B$  is the acoustic damping constant and  $\alpha$  is the logarithmic optical loss  
 376 in the fiber.

377 When the pump and probe powers are kept weak enough so that small-signal gain  
 378 holds and pump depletion is avoided, the evolution of the amplitude  $A_{probe}(z)$ , and  
 379 power,  $P_{probe}(z)$ , (in Watt), for a backward propagating CW probe, over a segment  
 380 of fiber with length  $L$  can be obtained as

$$\begin{aligned}
A_{probe}(z) = & |A_{probe}(z=L)| \exp \left[ \frac{g_1 g_2 |A_{pump}|^2}{2} \operatorname{Re} \left( \frac{1}{\Gamma_A} \right) (L-z) + \frac{\alpha}{2} (L-z) \right] \\
& \times \exp \left[ i \frac{g_1 g_2 |A_{pump}|^2}{2} \operatorname{Im} \left( \frac{1}{\Gamma_A} \right) (L-z) \right]
\end{aligned} \tag{7}$$

381 and

$$P_{probe}(z) = P_{probe}(z=L) \exp \left[ g(v) P_{pump}(L-z) / A_{eff} - \alpha(L-z) \right] \tag{8}$$

382 where  $A_{eff}$  is the effective area of the fiber core. The logarithmic Brillouin gain,  $g$   
383 ( $v$ ), is given by:

$$g(v = v_{pump} - v_{probe}) = g_1 g_2 \operatorname{Re} \left[ \frac{1}{\Gamma_A} \right] \xrightarrow{\Delta v_B \ll v_B} g_B \frac{(\Delta v_B / 2)^2}{(v - v_B)^2 + (\Delta v_B / 2)^2} \tag{9}$$

384 which takes the line shape of a Lorentzian profile with a peak gain of  $g_B = 2g_1 g_2 / \Gamma_B$   
385 and a full width at half maximum (FWHM) linewidth of  $\Delta v_B = 1 / (2\pi\tau_A)$ . Typically,  
386 for standard single-mode optical fibers at around 1550 nm,  $v_B \sim 11$  GHz ,  
387  $\Delta v_B \sim 30$  MHz ,  $g_B \sim 2 - 3 \times 10^{-11}$  m/W ,  $\alpha = 0.2$  dB/km ,  $A_{eff} = (50 - 80) \times$   
388  $10^{-12}$  m<sup>2</sup> [39].

389 Equation (9) characterizes the spectrum shape from the interaction of a CW  
390 pump and probe. However, for standard BOTDA in structural monitoring, the pump is  
391 modulated as a pulse to achieve a certain SR for discerning localized information  
392 along the fiber. The SR is determined by the pump pulse half duration multiplied by  
393 the group velocity of the guided mode [36]. Mathematically, the following formula is  
394 given,

$$SR = TV_g / 2 \tag{10}$$

395 As the pump is pulsed, the BGS can be obtained from the convolution of the  
396 Lorentzian-shaped intrinsic Brillouin gain spectrum given by Eq. (9) and the

397 normalized power spectral density (PSD) of the pump [40]. For the case of a  
 398 rectangular pulse pump of duration T, the BGS profile can be analytically calculated  
 399 in a closed-form expression [41]:

$$g_T(\Omega) = g_B(\Omega) \left( 1 - \frac{(\Gamma^2 + \Omega^2)(1 - e^{-\Gamma T} \cos(T\Omega)) + 2\Gamma\Omega e^{-\Gamma T} \sin(T\Omega)}{\Gamma T(\Gamma^2 + \Omega^2)} \right) \quad (11)$$

400 where  $\Omega = 2\pi(\nu - \nu_B)$  is the frequency detuning from the BFS, and  $\Gamma =$   
 401  $\pi\Delta\nu_B \sim 30\pi$  Mrad/s is the half-width at half maximum (HWHM). Expression (11)  
 402 renders a lower gain peak and broader spectrum profile comparing with the intrinsic  
 403 Lorentzian profile given by  $g_B(\Omega)$  with enhancing spatial resolution improvement.

404 The corresponding ratio of lowered peak height over the CW-induced peak height  
 405 can be derived to be:

$$g_{\max} = \left( 1 - \frac{1 - e^{-\Gamma T}}{\Gamma T} \right) \quad (12)$$

### 406 3.3. The crack-induced Brillouin backscattered-light power spectrum 407 based on SGB-FOS

408 The BFS in the fiber is affected by the strain and temperature, which can be  
 409 formulated as:

$$\nu_B(T, \varepsilon) = C_\varepsilon(\varepsilon - \varepsilon_0) + C_T(T - T_0) + \nu_{B0}(T_0, \varepsilon_0) \quad (13)$$

410 When a temperature compensation sensor is presented, the temperature-induced  
 411 BFS is,

$$\nu_B(T, \varepsilon_0) = C_T(T - T_0) + \nu_{B0}(T_0, \varepsilon_0) \quad (14)$$

412 Therefore, after temperature compensation, the purely strain-induced Brillouin  
 413 frequency shift can be obtained,

$$v_B(\varepsilon - \varepsilon_0) = v_B(T, \varepsilon) - v_B(T, \varepsilon_0) \quad (15)$$

414 where  $\varepsilon$  and  $T$  are the strain and temperature,  $C_T$  and  $C_\varepsilon$  are the temperature and  
 415 strain coefficients, which are determined by calibration. For standard single-mode  
 416 fibers using wavelengths around 1550 nm, the near-room temperature  $C_T$  are 1 MHz  
 417 per degree °C, while  $C_\varepsilon$  50 MHz per 1000  $\mu\varepsilon$ .  $T_0$  and  $\varepsilon_0$  are the strain and  
 418 temperature corresponding to the reference Brillouin frequency  $v_{B0}$ , respectively.

419 The local gain observed at the fiber near end is proportional to the local pump  
 420 power and the local Brillouin gain coefficient. Specifically, the Brillouin  
 421 backscattered-light power produced in a small section of the fiber translated by the  
 422 strain variation detected at an optical receiver is given by:

$$dP_B(z, \nu) = g_T(\nu, v_B(\varepsilon - \varepsilon_0)) \frac{c}{2n} p(z) e^{-2\alpha z} dz \quad (16)$$

423 where  $z = ct/(2n)$  is distance along the fiber from the light input,  $p(z)$  is the launched  
 424 light power at  $z$ ,  $\nu$  is the optical frequency of the Brillouin backscattered light,  $c$  is the  
 425 velocity of light in vacuum,  $n$  is the refractive index of the fiber,  $\alpha$  is the attenuation  
 426 coefficient of the fiber, and  $t$  is the time interval between the launching of the pulsed  
 427 light and the detection of the scattered light. Therefore, for any arbitrary given strain  
 428 distribution within the SR of the analyzer, at the  $i$ th measurement  $z_i$ ,

$$G_i(\nu) = \int_{z_i - SR/2}^{z_i + SR/2} g_T\{\nu, v_B[\varepsilon(z) - \varepsilon_0]\} \frac{c}{2n} p(z) e^{-2\alpha z} dz \quad (17)$$

429 For a  $SR \ll L$ , power variation due to fiber attenuation within the SR can be  
 430 neglected, and as we are only interested in the shape change of the spectrum, a  
 431 normalized spectrum can be obtained as,

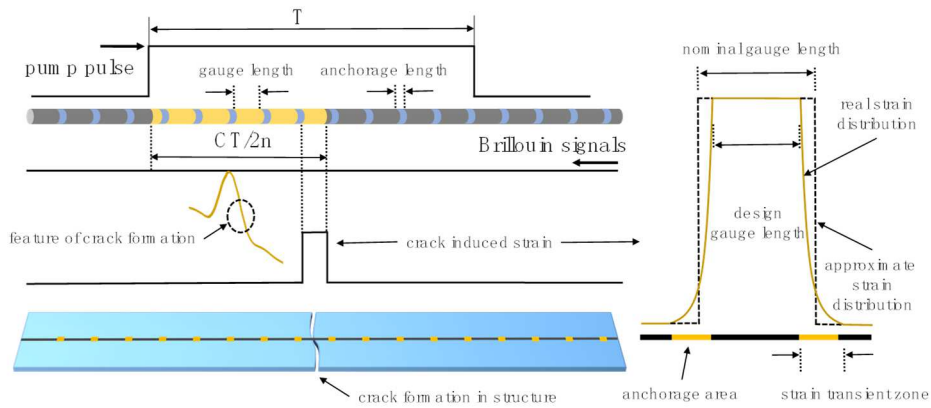
$$G_i(\nu) = \frac{1}{g_{\max}} \int_{z_i - SR/2}^{z_i + SR/2} g_T \{ \nu, \nu_B [\varepsilon(z) - \varepsilon_0] \} dz \quad (18)$$

432 For our short gauge sensor, under the assumption of rectangular pulsed pump and  
 433 uniform crack-induced strain, when the background strain variation can be regarded  
 434 as sufficiently small, the strain distribution within SR at  $z_i$  can be expressed as  
 435 follows:

$$\varepsilon_i(z) = \begin{cases} \varepsilon_c - \varepsilon_0 & (z_i - SR/2) \leq z_{lb} \leq z \leq z_{ub} \leq (z_i + SR/2) \\ \varepsilon_0 & (z_i - SR/2) \leq z < z_{lb}, z_{ub} < z \leq (z_i + SR/2) \end{cases} \quad (19)$$

436 where  $z_{lb}$  and  $z_{ub}$  denote the lower and upper boundary of crack-induced strain  
 437 distribution. Therefore, we can arrive at an approximation of the crack-induced  
 438 spectrum response in a simple closed form,

$$G_{i,c}(\nu) = \frac{1}{g_{\max}} \left( \frac{GL_n}{SR} \right) g_T(\nu, \nu_B(\varepsilon_c - \varepsilon_0)) + \frac{1}{g_{\max}} \left( 1 - \frac{GL_n}{SR} \right) g_T(\nu, \nu_B(\varepsilon_0)) \quad (20)$$



439  
 440 **Fig. 4.** Schematics of the short gauge Brillouin fiber optic sensor.

441 *3.4. Numerical simulation of the crack-induced BGS response using*  
442 *SGB-FOS*

443 Following the methodologies introduced in section 3.1 to section 3.3, numerical  
444 simulation of the BGS evolution using SGB-FOS in response to crack formation can  
445 be carried out by implementing the respective formulas in Matlab codes. The  
446 following simulation exemplifies the BGS response to crack expansion based on a  
447 typical combination of a Brillouin fiber-optic analyzer (560 mm SR) and the  
448 SGB-FOS (112 mm GL).

449 Fig.5(a) demonstrates the predicted BGS evolution of the SGB-FOS corresponding  
450 to the varied spectrum of crack-induced strain. We can see that the BGS profile is  
451 predicted to change markedly in shape as the crack-induced strain increases. To  
452 characterize different spectrum evolutionary stages, we extract the peak position from  
453 the predicted BGS response demonstrated in Fig.5(a) with the varying crack strain  
454 (Fig.5(b)). The BGS peak position is characterized by its frequency shift and power  
455 variation compared to its initial position when no crack is present.

456 In Fig.5(b), it is interesting to note that as the crack strain increases, the BGS peak  
457 shifting is predicted to undergo complex nonlinear behavior instead of a simple linear  
458 response from the fiber-optic sensors uniformly stressed within the SR of the  
459 analyzer. Moreover, the peak power of the BGS is also predicted to evolve  
460 nonlinearly with the varying crack-induced strain. Fig.5(b) illustrates the evolution of  
461 normalized peak power with varying crack strain. Overall, a three-staged BGS  
462 peak-shifting response can be identified. In stage I, the BGS peak begin to shift to  
463 higher frequencies with the crack width growth. However, after the peak shifting



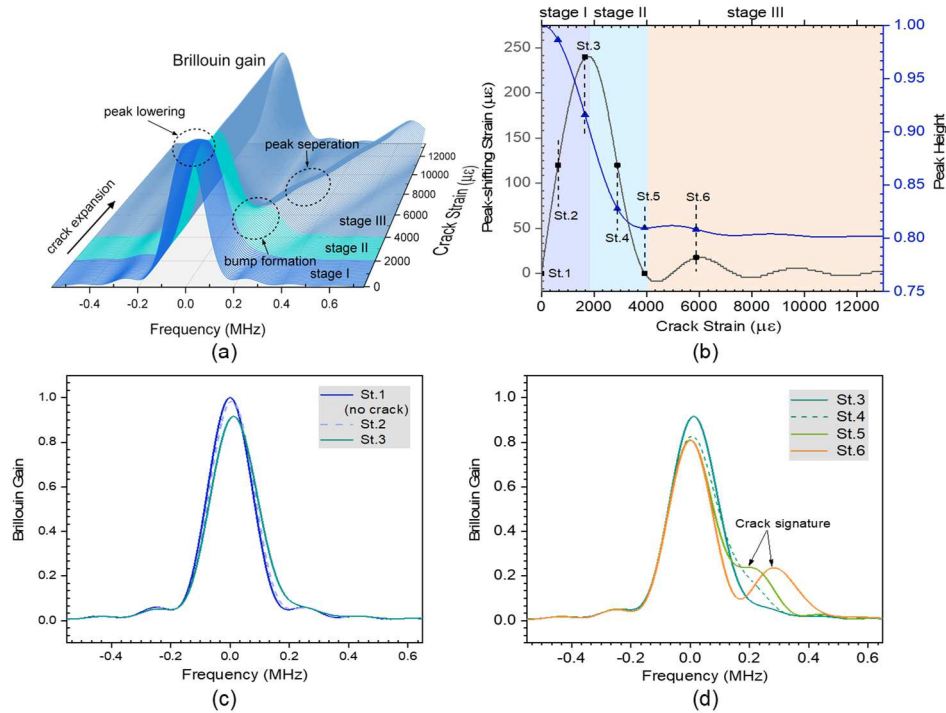
464 surpasses a certain level, the trend is reversed, and the peak starts to shift back to its  
465 original position as the crack grows. We categorize this reversal-peak-shifting stage as  
466 stage II. After this, the peak position becomes relatively stable in response to the  
467 increased crack width, undergoing only minor ups and downs. We categorize this as  
468 stage III. For peak power evolution, it is noticeable that in stage I and II, the peak  
469 power experiences a pronounced decrease. In contrast, the peak power becomes  
470 relatively stable when the crack-induced strain enters the stage III region.

471 In fact, these three stages also characterize the evolutionary features of the BGS  
472 configuration with different sensitivity to crack width variation. Specifically, when no  
473 crack is present, the BGS resembles a Lorentzian curve and is symmetrical against its  
474 peak. As small crack forms in stage I, the BGS features a broader spectrum base,  
475 asymmetrically leaning leftwards, with a steeper curve slope at its left side in  
476 comparison to the right. To illustrate more clearly the characteristic change of the  
477 BGS response in stage I, the BGS profiles corresponding to the three representative  
478 highlighted crack-induced strain levels in stage I ( St.1, St.2, and St.3 in Fig.5(b)) are  
479 demonstrated in Fig.5(c). As can be seen, these BGS profiles tend to have a relatively  
480 smooth right side curve without localized changes in curvature distribution. During  
481 this stage, the characteristics of the BGS configuration undergo no prominent changes  
482 as the crack expands, apart from the peak shifting and lowering behaviors, indicating  
483 that the BGS shape variation is relatively insensitive to crack expansion at this stage.

484 In stage II, however, a bump appears rapidly at the high-frequency side of the BGS  
485 profile corresponding to the crack expansion, and the configuration of the BGS  
486 changes dramatically. Therefore, the occurrence of a bump in the BGS can be served

487 as a clear indicator of crack formation. Two BGS profiles corresponding to the  
488 representative crack-induced strain levels in stage II (St.4 and St.5 in Fig.5(b)) are  
489 presented in Fig.5(d) to show the corresponding spectrum evolutionary process.  
490 Obviously, the evolution of the BGS at this stage demonstrates enhanced sensitivity  
491 with crack width variation comparing to stage I. In stage III, as the crack further  
492 increases in width, the bump formed in stage II is predicted to transform into a  
493 separated secondary peak, shedding off from the primary peak. After this, the distance  
494 between the secondary and primary peak is predicted to grow in response to further  
495 crack width enlargement. One particular BGS profile corresponding to the  
496 representative crack-induced strain level in stage III (St.6 in Fig.5(b)) is presented in  
497 Fig.5(d) to demonstrate the BGS profile after peak separation when a large crack  
498 occurs.

499 By applying the SGB-FOS, the predicted shape-changing phenomenon of the BGS  
500 responding to crack variations demonstrated above can be leveraged for crack  
501 detection and potentially its quantification. It is also noticeable that the crack strain  
502 corresponding to the peak of the peak-shifting curve (St.3) in Fig.5(b) characterizes  
503 the hinge point where prominent changes of the BGS configuration initiate with  
504 enlarged crack width, offering a reasonable estimation of the sensor's capability for  
505 small crack detection judging on BGS shape only. Bump formation or peak separation  
506 in stages II and III can be very straight-forward signs of crack formation. The bump  
507 feature is predicted to become very pronounced at the later stage of stage II.



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**Fig.5.** The numerically simulated BGS response to crack expansion using SGB-FOS: (a) BGS evolution with varying crack-induced strain using SGB-FOS of 112 mm GL and Brillouin analyzer of 560 mm SR; (b) BGS peak shifting effect and peak lowering effect (indicated by the normalized peak height) vs different crack-induced strain; (c) simulated BGS response corresponding to selected crack-induced strain in stage I (CS = St.1, St.2, and St.3, respectively); (d) simulated BGS response corresponding to selected crack-induced strain in stage II and III (CS = St.4, St.5, and St.6, respectively).

## 517 **4. Experimental testing**

### 518 *4.1. Testing setup*

519 To simulate structural crack formation, we deployed two aluminum plates as  
520 templates to create a single artificial crack. Each plate spans 1100 mm in length,  
521 providing sufficient space to avoid possible interference to the crack-induced signals  
522 that may arise due to the distortion effect generated by the strain variations at the plate  
523 boundaries. The two plates were bolted to a high-precision fixture frame specifically  
524 designed for the fiber optic sensor calibration. SGB-FOSs with the GLs of 60 mm, 90  
525 mm, and 120 mm were installed across the two plates. A tight-buffered fiber optic  
526 strain sensing cable of 0.9 mm outer diameter was selected for the assembly of the  
527 short-gauged sensor. The fiber optic sensors were glued to the plates by epoxy resin.

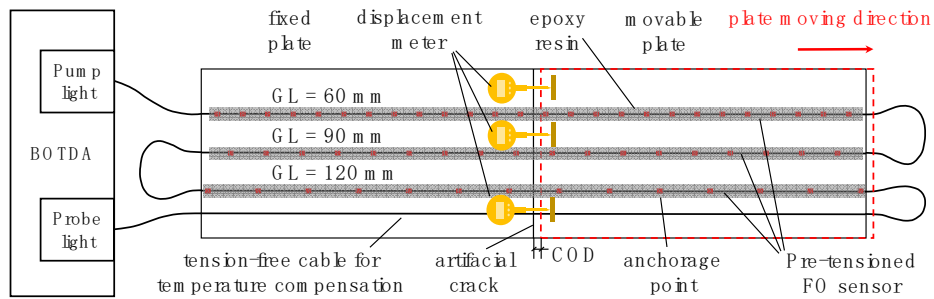
528 The Omnisense DiTeSt BOTDA fiber optic analyzer was used as the interrogation  
529 system during the testing, which could reportedly achieve repeatability of  $\pm 2\mu\epsilon$  and  
530 spatial resolution as low as 0.5 m. The spatial resolution for the experiment was set to  
531 0.5 m, and the spatial sampling rate was set to every 0.25 m.

532 Fig.6 shows the design of the testing system. Three displacement gauges with an  
533 accuracy of 0.001 mm are placed dispersedly at three different locations along the  
534 width of the plates to provide reference measurements for the crack opening.

535 In the loading stage, the loading system generated an artificial crack by driving the  
536 movable plate away from the fixed plate, creating a gap between the two plates. The  
537 crack width ranged from 0 mm to 2.0 mm under displacement control during the

538 testing, with increments of 0.025 mm for each step before 0.4 mm and 0.05 mm  
 539 afterward.

540 Multiple displacement gauges enabled measuring crack width at different locations  
 541 along the crack; the crack width measurement from the displacement gauges at each  
 542 fiber-optic sensor position can be accurately calculated by applying linear regression  
 543 taken into consideration of the spatial positions of the displacement gauges and the  
 544 fiber optic sensors.



545

546 **Fig.6.** Schematics of the crack-sensing testing using SGB-FOSs

547 *4.2. Verification of the crack-induced BGS response using SGB-FOS*

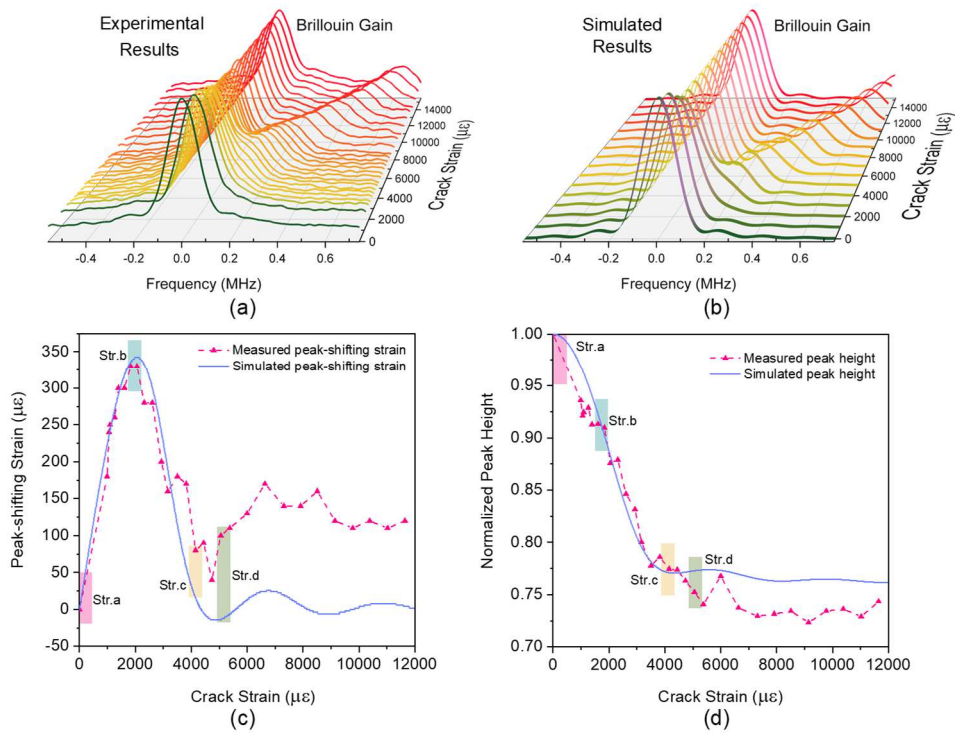
548 Fig.7 shows the experimental results and the corresponding numerical simulation  
 549 results according to the methodologies proposed in Section 3 for SGB-FOS with 120  
 550 mm GL as an example for comparison. Fig.7(a) and Fig.7(b) present the BGS  
 551 evolutionary process in response to crack expansion. Highly consistent results are  
 552 obtained in terms of the overall spectrum evolutionary pattern between the  
 553 experimental and simulation results, which confirms the theoretical predictions in  
 554 Section 3.

555 Detailed comparisons between the experiment and simulations of the BGS  
556 response are demonstrated in Fig.7(c) to Fig.7(h). From Fig.7(c) and Fig.7(d), the  
557 peak shifting and peak lowering phenomenon predicted theoretically can be clearly  
558 observed in the experimental results. The experimental curves match reasonably well  
559 with the simulated results in terms of the evolutionary trend. For the peak-shifting  
560 behavior shown in Fig.7(c), close consistency between the theoretical and  
561 experimental results can be observed for crack expansion in stage I and stage II.  
562 Although some discrepancy in magnitude occurs between the experimental and the  
563 simulated results for crack expansion in stage III, the two curves still share a very  
564 similar trend in the evolutionary pattern. We believe the discrepancy is most likely to  
565 be caused by the deviation of the actual strain distribution in the fiber optic sensor  
566 from the simplified theoretical assumption of a rectangular-shaped crack strain  
567 distribution (see Fig.4). The strain transition zone in the sensor's anchorage area  
568 inevitably contributes its respective spectrum energy to the measured BGS, which  
569 tends to drag the primary peak to a higher frequency even after the secondary  
570 peak separation. In contrast, the peak lowering behavior from the experiment  
571 matches well with the theoretical prediction in terms of both the overall trend and  
572 magnitude (see Fig.7(d)).

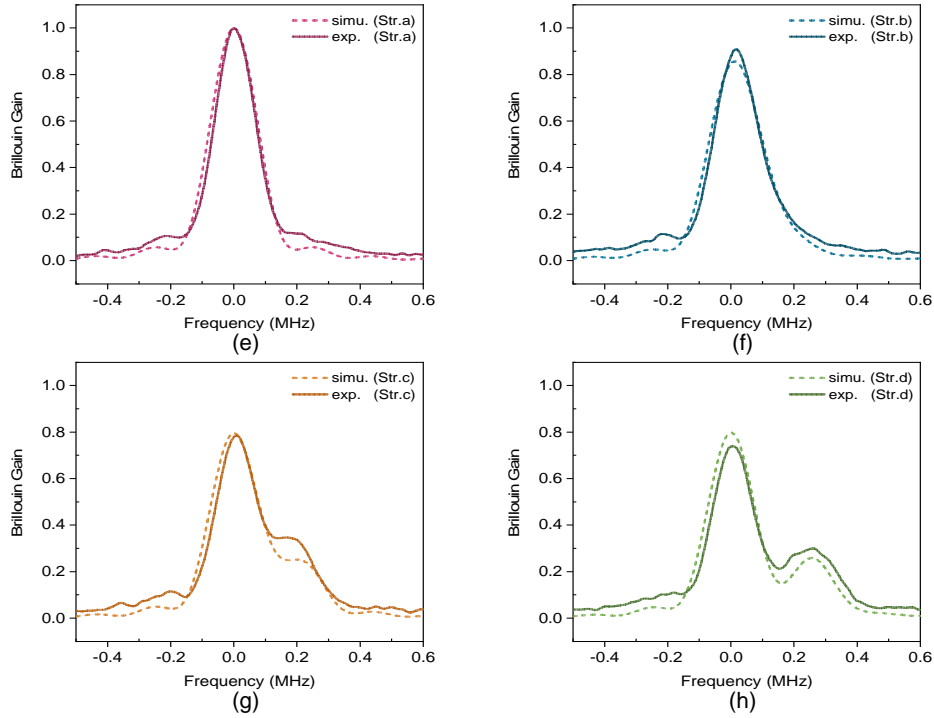
573 Some representative BGS profiles through the crack expansion process are selected  
574 for comparison in Fig.7(e) through Fig.7(h). These profiles are the experimental and  
575 simulation results that correspond to the crack-induced strains highlighted by colored  
576 bars in Fig.7(c) and Fig.7(d), respectively. These spectra demonstrate the entire  
577 evolutionary process of crack-induced BGS response as the crack expands. The

578 theoretical BGS responses are thus proven to match reasonably well with the  
 579 experimental results, where the characteristics of the experimentally obtained BGSs  
 580 are observed to evolve closely as theoretically predicted. Namely, the experimentally  
 581 obtained BGSs are observed to experience evolutionary stages through a process of  
 582 peak leaning (stage I), bump forming (stage II), and secondary peak separation (stage  
 583 III).

584 The consistency between the theoretical and experimental results in various aspects  
 585 confirms our proposed theoretical framework's suitability to predict the crack-induced  
 586 BGS response for the SGB-FOSs.



587



588

589 **Fig. 7.** Experimental and simulated crack-induced BGS response using SGB-FOS: (a)  
 590 experimental BGS response vs. crack-induced strain (CS); (b) simulated BGS  
 591 response vs. crack-induced strain; (c) experimental and simulated peak-shifting strain  
 592 vs. crack-induced strain; (d) experimental and simulated normalized BGS peak height  
 593 vs. crack-induced strain; (e) experimental and simulated BGS at the crack-free stage  
 594 (CS = Str.a); (f) experimental and simulated BGS at the end of stage I (CS = Str.b);  
 595 (g) experimental and simulated BGS at the end of stage II (CS = Str.c); (h)  
 596 experimental and simulated BGS at stage III (CS = Str.d).

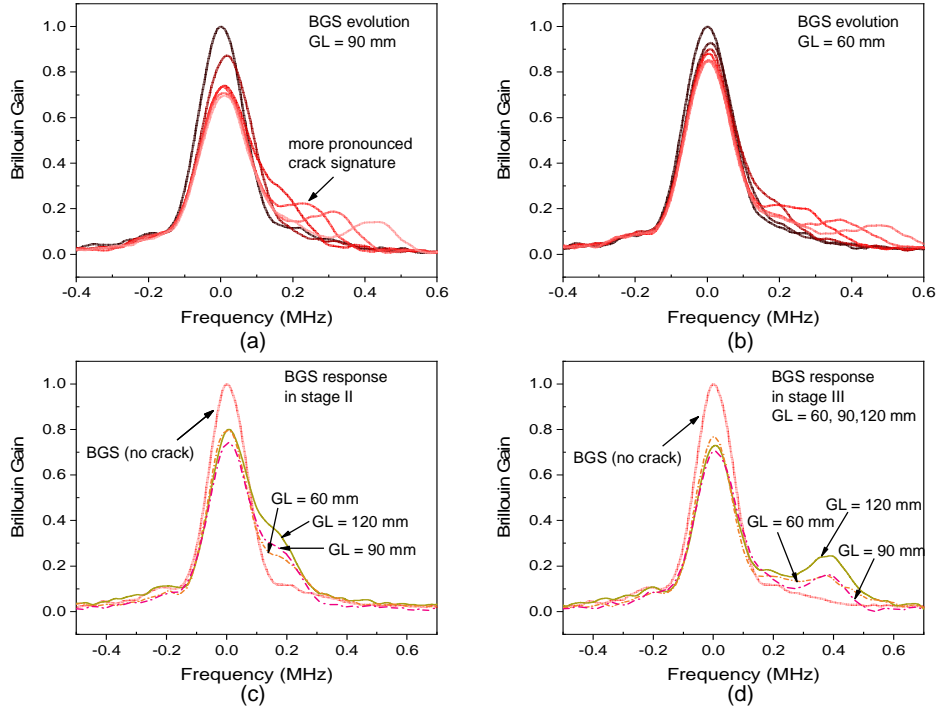
597

598 If the SGB-FOSs adopt different gauge lengths, the corresponding crack-induced  
 599 BGS response will change accordingly. In Fig.8(a) and Fig.8(b), the experimentally



600 obtained BGS evolution using SGB-FOSs in different GLs are shown for comparison.  
601 The experimental results suggest that despite different sensor GLs, the BGS  
602 evolutionary processes share the same evolutionary pattern, characterized by a sequential  
603 phenomenon that occurs through stage I to stage III as specified in Section 3.4.  
604 However, a longer sensor GL means forming a higher and more prominent secondary  
605 peak after a particular crack-induced strain is reached. Meanwhile, it also means a  
606 more significant peak-lowering behavior. However, SGB-FOSs with a longer GL will  
607 render the secondary-primary peak separation to occur later than shorter GLs cases.  
608 All these experimental phenomena agree well with the theoretical predictions  
609 according to Section 3.

610 In Fig.8(c) and Fig.8(d), the experimentally obtained BGSs using SGB-FOSs with  
611 different GLs at the same evolutionary stages are shown for comparison. These  
612 experimental results reveal that the crack signatures in the detected BGSs, namely the  
613 bump formation and peak separation behaviors, are more prominent for SGB-FOSs  
614 with longer GLs. In contrast, shorter GL sensors will render a relatively lower and  
615 flatter secondary peak, which can be harder to distinguish due to the influence of  
616 intrinsic background noises accompanying the sensing system. Nevertheless, the  
617 experimental results suggest that the crack signatures in the BGSs can still be clearly  
618 identifiable for the shortest gauge length applied (about 10% of GL/SR ratio).



619

620 **Fig. 8.** Experimental results of BGS evolution for SGB-FOSs of different GLs: (a)  
 621 crack-induced BGS response for SGB-FOS of 90 mm GL; (b) crack-induced BGS  
 622 response for SGB-FOS of 60 mm GL; (c) stage II crack-induced BGS response for  
 623 SGB-FOSs with 60 mm, 90 mm, and 120 mm GLs; (d) stage III crack-induced BGS  
 624 response for SGB-FOSs with 60 mm, 90 mm, and 120 mm GLs.

625 **5. SGB-FOS as distributed crack meter**

626 In the last section, we demonstrate the effectiveness of the theoretical framework  
 627 in predicting the crack-induced BGS response using the proposed fiber optic sensor.  
 628 Understandably, the measured BGS configurations contain the crack information, and  
 629 this could lead to refined quantification of the crack. This section will showcase the

630 possibility of using the SGB-FOS as a distributed crack meter in the engineering  
631 practice, enabling retrieval of crack width information via processing the measured  
632 BGS data. We also demonstrated in sections 3.4 and 4.2 the possibility of identifying  
633 the existence of crack by examining the characteristics of the BGS response. If the  
634 crack signatures are observed in the measured BGSs, data processing methodologies  
635 can be subsequently applied to obtain the crack width quantitatively.

636 With the closed-form formulations describing the spectrum's evolutionary process  
637 proposed in Section 3, it is theoretically possible to obtain the optimized crack width  
638 by matching the theoretical and experimental BGSs through iterative nonlinear curve  
639 fitting. However, this approach was found occasionally unstable to reach numerical  
640 convergence for some particular measurement datasets. Moreover, it also tends to be  
641 computationally expensive to process large datasets.

642 The adoption of the SGB-FOS enables the resulted BGS response after crack  
643 formation to be simplified as a linear superposition of two quasi-Lorentzian curves.  
644 According to equation (20), these two quasi-Lorentzian curves differ in power and  
645 center frequencies but share the same line width. In view of this, a simplified peak  
646 fitting algorithm can be developed to decouple the peak composition in the  
647 experimental dataset.

648 Although a pseudo-Voigt profile was deemed suitable to account for the variations  
649 of the BGS arisen from different operating conditions of the sensing systems [42],  
650 their usages tend to make the algorithm less stable to reach numerical convergence.  
651 Therefore, the peak composition of double Lorentzian curves is assumed for the  
652 measured BGS profiles. During the peak decomposition process, an equal-line-width

653 constraint is applied in a peak fitting algorithm written in Matlab codes, reducing the  
654 fitting parameters' degree of freedom. As such, the robustness and efficiency of the  
655 algorithm are thus enhanced. Reasonable initial values of the peak parameters are  
656 appropriately chosen as input for the peak fitting algorithm. Afterward, peak center  
657 frequencies and peak heights are obtained by minimizing the discrepancy between the  
658 measured BGSs and the composition of fitted peaks through an iterative least-square  
659 technique until attaining numerical convergence.

660 Fig. 9(a) to Fig.9(c) presents the correlation of the crack widths detected by the  
661 SGB-FOSs with different GLs through the proposed peak fitting algorithm and the  
662 displacement gauge measurements. Test results reveal that all sensors perform  
663 excellently in terms of a high degree of linearity for cracks that are relatively large  
664 using the peak decomposition algorithm. However, when the crack is relatively small,  
665 their quantification can be challenging. A threshold seems to exist below which a high  
666 degree of sensor linearity can be hard to achieve. Instead, a small section of nonlinear  
667 curves exists before they enter the linear zone. The experimental results suggest that  
668 the cracks become measurable when it exceeds a specific value (about 0.1 mm to 0.3  
669 mm), depending on the gauge length adopted. However, before the cracks can be  
670 measured with certainty, the peak-leaning phenomenon can already be observed,  
671 which can be used as a distinctive sign for identifying early-stage cracks.

672 To facilitate understanding the reason behind this phenomenon, selected  
673 spectrum profiles corresponding to the highlighted points in Fig.9(a) to Fig.9(c) are  
674 plotted. We can see that at the early stage of crack formation, as the BGS evolves  
675 within stage I, the peak fitting algorithm is not sensitive enough for crack width

676 quantification. However, when the BGS proceeds to stage II and stage III, namely  
677 after a bump signature forming clearly in the BGSs, the proposed peak fitting  
678 algorithm can effectively retrieve the crack width information with good repeatability  
679 and linearity.

680 Peak fitting results of the selected profiles for the 90 mm GL case (as shown in  
681 Fig.9(b)) are illustrated in Fig.9(d) through Fig.9(f) to help understand the  
682 performance of the proposed peak fitting algorithm for different stages of BGS  
683 response. As shown in Fig.9(e) and Fig.9(f), after apparent secondary peak formation,  
684 the peak fitting algorithm renders good fitting results, accurately capturing the  
685 secondary peak position, which explains the excellent linearity of the measurement  
686 results. However, before the peak separation, the fitting algorithm tends to give larger  
687 secondary peak position coordinates than the real value, although the composite curve  
688 matches close enough to the measured BGS profile (Fig.9(d)). It appears that direct  
689 peak fitting for the early-stage crack-induced BGSs can be susceptible to  
690 measurement noises and model discrepancies. Therefore, in this study, we focus our  
691 attention on relatively large cracks with relatively prominent crack signatures in the  
692 BGS response, such as bump formation and peak separation.

693 As presented in Fig.9(a) to Fig.9(c), a highly linear correlation is established  
694 between the measurement results from the displacement gauges and the fiber optic  
695 sensors for crack widths beyond a certain threshold. The corresponding linear  
696 regression formulas and the associating R-square values can be derived based on the  
697 cases with crack width greater than those thresholds. Those formulas give factors of  
698 crack width conversion from the fiber optic sensing systems with different sensor

699 designs. It is noticeable that the factors, calculated by the crack widths detected by the  
700 fiber optic sensors over those from the displacement gauges, are always smaller than  
701 one. Specifically, for the SGB-FOS of 120 mm GL and the ones of 90 mm GL, the  
702 factors are 0.86 and 0.84, respectively. For the SGB-FOS of 60 mm GL, this value  
703 declines to 0.69. These factors are, in fact, the characteristic factor  $k$  for the particular  
704 SGB-FOSs. For sensors with 120 mm and 90 mm GLs, the strain transfer mechanism  
705 from the cracked structure to the fiber optic sensor is most likely to be responsible for  
706 the discrepancy between the fiber optic measured crack widths and the actual crack  
707 widths as has been illustrated in Section 3.1. However, for the 60 mm GL cases, the  
708 flatter of the secondary peaks due to the smaller GL/SR ratio seems to render a  
709 smaller-biased detected crack width apart from the aforementioned reasons. As shown  
710 in Fig.9(g) and Fig.9(h), the relatively low energy of the secondary peak and the low  
711 signal-to-noise ratio (SNR) make it more difficult for the peak fitting algorithm to  
712 locate the accurate position of the secondary peak. In other words, when the GL/SR  
713 ratio for the SGB-FOSs is low, the crack signatures in the BGSs can be blurred by the  
714 background noises, and the secondary peak features can become insignificant. In this  
715 case, this effect tends to cause the fitted peaks to deviate to the left of where they  
716 should be, rendering smaller detected crack widths and thus a lowered crack width  
717 conversion factor than the SGB-FOSs with longer GLs.

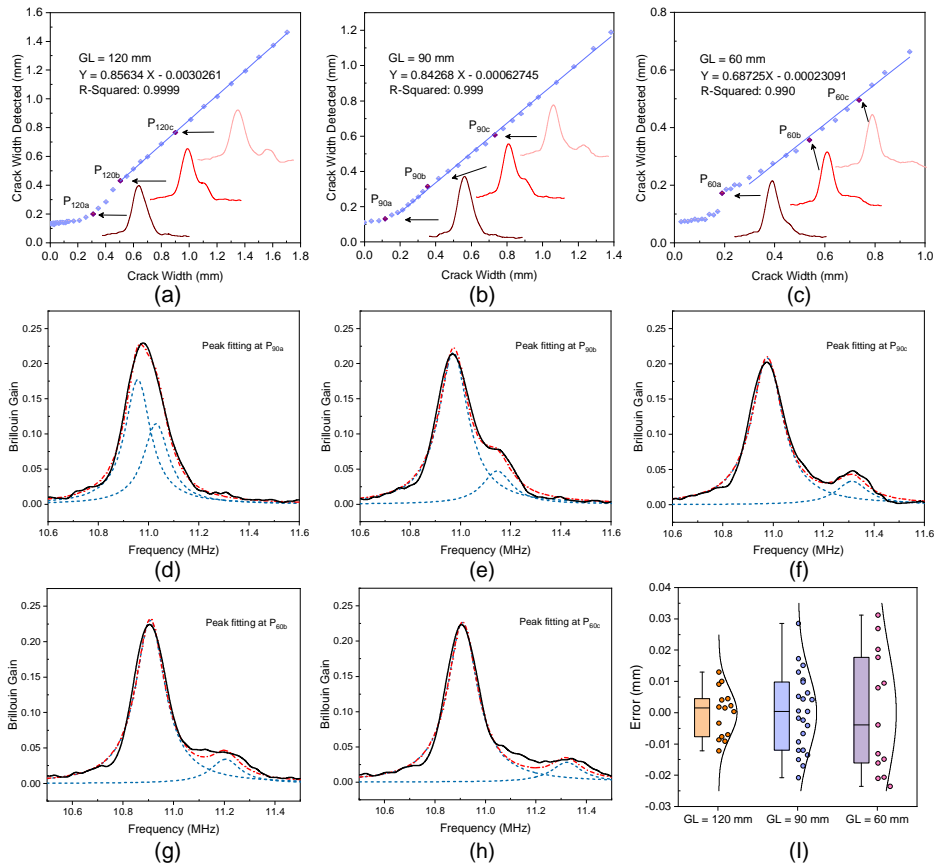
718 The linear regression formulas from the sensor calibration tests can be used for  
719 crack width quantification in the monitoring practice given a specific SGB-FOS  
720 design. From the testing results illustrated in Fig.9(a) to Fig.9(c), the crack only  
721 becomes measurable after particular crack width values have been exceeded, and

722 these thresholds relate closely to the GLs of the SGB-FOSs. Different GLs can  
723 influence the sensing capability of the crack in two ways. A shorter GL will generate  
724 a lower-powered crack signature in the BGS response, which can be more difficult to  
725 capture by the peak fitting algorithm, rendering a more challenging crack  
726 identification and compromised crack-sensing accuracy. However, a shorter GL  
727 would also mean an earlier bump formation in the BGS due to the higher  
728 crack-induced strain in the sensor responding to the same crack width, making the  
729 BGS more sensitive to the identification of early cracks. The actual performance of  
730 the SGB-FOSs for the early crack identification hinges on the comparable influence  
731 of these two opposite effects.

732 These two effects can be demonstrated by Fig.9(a) to Fig.9(c). For SGB-FOS of  
733 120 mm GL, the fiber optic sensor only becomes sensitive to crack greater than 0.3  
734 mm, due to the insignificant bump signature of the BGS at the early phase of the crack  
735 formation. To SGB-FOS of 60 mm GL, this value declined to about 0.17 mm, where a  
736 sudden jump of fiber-optic detected crack width occurs, indicating the successful  
737 identification of the crack signals in the BGS by the peak fitting algorithm. However,  
738 the SGB-FOS of 90 mm GL seems to strike a more balanced sensor design, which  
739 managed to bring down this threshold to about 0.15 mm for crack identification.

740 As the test showed that the crack width detected by the SGB-FOSs demonstrated  
741 excellent linearity after cracks become measurable, we can evaluate the measurement  
742 uncertainty using the deviations of the detected crack width to the respective linear  
743 regression values for crack width greater than a certain threshold (the measurable  
744 crack widths) for SGB-FOSs of different GLs. Fig.9(i) displayed the measurement

745 error distributions. Comparison between sensors of different GLs suggests that  
 746 SGB-FOSs with longer GLs tend to possess higher repeatability for crack width  
 747 measurement. In contrast, measurements from SGB-FOSs with shorter GLs would  
 748 involve more degrees of uncertainty. The sensor repeatability indicated by two times  
 749 the standard deviation of the measurement error is estimated to be  $\pm 0.0154$  mm,  
 750  $\pm 0.0248$  mm, and  $\pm 0.0394$  mm, for SGB-FOSs with GLs of 120 mm, 90 mm,  
 751 and 60 mm, respectively.



752  
 753 **Fig.9.** Crack width measurement through peak fitting: (a) crack width from SGB-FOS  
 754 of 120 mm GL vs that from displacement meters; (b) crack width from SGB-FOS of



755 90 mm GL vs that from displacement meters; (c) crack width from SGB-FOS of 60  
756 mm GL vs that from displacement meters; (d) peak fitting for SGB-FOS of 90 mm  
757 GL at point P<sub>90a</sub>; (e) peak fitting for SGB-FOS of 90 mm GL at point P<sub>90b</sub>; (f) peak  
758 fitting for SGB-FOS of 90 mm GL at point P<sub>90c</sub>; (g) peak fitting for SGB-FOS of 60  
759 mm GL at point P<sub>60b</sub>; (h) peak fitting for SGB-FOS of 60 mm GL at point P<sub>60c</sub>; (i)  
760 error distribution of the crack width measurement for SGB-FOSs of different GLs.

## 761 **6. Conclusions**

762 This study proposes a novel fiber-optic sensor concept and design called  
763 short-gauged Brillouin fiber optic sensor, which enables basic Brillouin-based  
764 analyzers to detect and accurately quantify events of cracks or structural  
765 discontinuities. As a generic technique, the proposed methodology could potentially  
766 facilitate the attainment of long-distance distributed crack sensing and quantification  
767 for various civil infrastructures economically.

768 A sensor example is presented demonstrating the specific design and installation  
769 procedures, which are intended to be used for large-scale applications. Theoretical  
770 deduction of the BGS transformation for the proposed sensor in response to the  
771 expanding crack is established, verified by the laboratory experiment subsequently.  
772 Both the theoretical and experimental results identified a three-stage evolutionary  
773 process of the BGS transformation in response to crack expansion. These stages are  
774 categorized by the characteristics of the BGS configurations, peak shifting, and  
775 power-lowering behaviors. By observing the presence of these distinctive crack  
776 signatures, an early crack warning can be achieved.

777        Apart from crack detection, the proposed sensor can also become a powerful  
778 generic distributed crack meter for different applications, capable of accurate  
779 crack-width measurement, minimizing uncertainties that the traditional OB  
780 instrumentation approach usually confronts. The adoption of the SGB-FOS enables  
781 the development of a simplified peak-fitting-based methodology to extract crack  
782 width information within the BGS response robustly and efficiently. The experiment  
783 demonstrates the excellent capacity of the proposed sensor to measure cracks with a  
784 width greater than a certain threshold, depending on the design GLs of the  
785 SGB-FOSs. According to the experimental results, cracks can become measurable as  
786 their widths grow greater than around 0.15 mm by the optimized sensors based on the  
787 adopted analyzer. Good sensor linearity is achieved for the measurable cracks. Test  
788 results suggest that the repeatability of the distributed sensor for crack quantification  
789 relies on the sensor gauge length, where smaller gauge sensors tend to be more  
790 sensitive to crack width variations but less accurate.

791        Successful detecting and quantifying cracks in the order of this experiment could  
792 carry significant meaning to achieve more advanced infrastructure maintenance  
793 systems based on refined structural damage dataset. A crack monitoring system could  
794 be made possible, fully aware of the crack distribution and quantification information  
795 along the sensor coverage. However, further investigations are required regarding the  
796 sensor performance in real-scale infrastructures and the improvement of the sensor's  
797 measurement capability for more minor cracks. The proposed technique could be  
798 potentially beneficial for preventive structural maintenance of various infrastructures  
799 to arrive at decreased life-cycle costs.

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807 **Conflicts of Interest**

808 The authors declare no conflicts of interest.

809 **Abbreviations**

BFS	Brillouin frequency shift	OB	overall bonding
BGS	Brillouin gain spectrum	OTDR	Optical Time Domain Reflectometer
BOTDA	Brillouin optical time-domain analysis	PF	point-fixation
BOTDR	Brillouin optical time-domain reflectometer	PSD	power spectral density
CS	crack-induced strain	RC	reinforced concrete
FOS	fiber optic sensor	SBS	stimulated Brillouin scattering
FWHM	full width at half maximum	SHM	structural health monitoring
GL	gauge length	SNR	signal-to-noise ratio

HWHM	half-width at half maximum	SR	spatial resolution
NDT	non-destructive testing		

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