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# Compensation of nonlinearity in a fiber-optic transmission system using frequency-degenerate phase conjugation through counter-propagating dual pump FWM in a semiconductor optical amplifier

Abhishek Anchal<sup>1</sup> , Pradeep Kumar K<sup>2</sup>, Sean O'Duill<sup>3</sup> , Prince M Anandarajah<sup>3</sup> and Pascal Landais<sup>3</sup>

<sup>1</sup>Department of Applied Physics, The Rachel and Selim Benin School of Computer Science and Engineering, The Hebrew University of Jerusalem, Jerusalem 90401, Israel

<sup>2</sup>Department of Electrical Engineering, Indian Institute of Technology Kanpur, Kanpur 208016, India

<sup>3</sup>School of Electronic Engineering, Dublin City University, Glasnevin, Dublin 9, Ireland

## Abstract

We present a scheme of frequency-degenerate mid-span spectral inversion (MSSI) for nonlinearity compensation in fiber-optic transmission systems. The spectral inversion is obtained by using counter-propagating dual pump four-wave mixing in a semiconductor optical amplifier (SOA). Frequency-degeneracy between signal and conjugate is achieved by keeping two pump frequencies symmetrical about the signal frequency. We simulate the performance of MSSI for nonlinearity compensation by scrutinizing the improvement of the Q-factor of a 200 Gbps QPSK signal transmitted over a standard single mode fiber, as a function of launch power for different span lengths and number of spans. We demonstrate a 7.5 dB improvement in the input power dynamic range and an almost 83% increase in the transmission length for optimum MSSI parameters of  $-2$  dBm pump power and 400 mA SOA current.

Keywords: non-linearity compensation, optical phase conjugation, semiconductor optical amplifier, four-wave mixing, non-linear optics

## 1. Introduction

Technological development in recent years has created the high-speed data network, which currently serves as the backbone to cater for the increasing demand of bandwidth-rich applications such as online gaming, video sharing and streaming, voice over Internet, video on demand, and cloud computing. Such services are bandwidth intensive, pushing the capacity of network providers to their transmission limit [1, 2]. Cisco VNI predicts that there will be a five- to seven-fold increase in the global data traffic (of the order of

zettabytes) between 2016 and 2021 [3]. The advancement with wavelength division multiplexing (WDM), higher-order modulation formats such as quadrature phase shift keying (QPSK), quadrature amplitude modulation (QAM), coherent detection, and space diversity make fiber optic transmission system a true candidate to support high capacity network in the present scenario as well as in the near future context [4–7]. The capacity can be further enhanced by using a superchannel with several sub-carriers separated by a smaller channel spacing [8]. However, the capacity of fiber-optic transmission systems is limited by distortion due to fiber

nonlinearities resulting from large launched powers for higher modulation formats and/or small channel spacing [2, 4, 5, 9–11]. Therefore, recent research have been focused on reducing the effect of fiber nonlinearities through various compensation techniques, such as phase-conjugated twin wave, optical back-propagation, digital nonlinearities compensation, nonlinear Fourier transform, mid-span spectral inversion (MSSI) and so on [10–15].

Among these techniques, MSSI using optical phase conjugation (OPC) has been shown to fully compensate for the distortion due to fiber nonlinearities, in intensity and phase modulated systems [11, 16, 17]. Other advantages of using MSSI are: transparency to modulation formats, scalability in WDM systems, and implementation in the optical domain to take advantage of the underlying optical fiber infrastructure. MSSI using OPC was first demonstrated in [18], in which the distortion due to fiber dispersion and nonlinearities in the first half of the transmission link is inverted by OPC and canceled by similar distortion in the second half of the transmission link. As the effect of fiber dispersion in higher modulation formats is less than the legacy on-off-keyed systems, various MSSI schemes have been reported to compensate for fiber nonlinearities, including OPC based on three-wave mixing in a lithium niobate crystal and four-wave mixing (FWM) in highly nonlinear fiber (HNLF), semiconductor optical amplifier (SOA), and silicon waveguide [16, 17, 19, 20, 21]. However, frequency conversion during the OPC process results in a crosstalk in WDM system causing bit-errors and hence resulting in a reduction in the overall improvement in capacity of the transmission system. There have been various attempts to generate frequency-degenerate MSSI using dual pump orthogonally polarized co-propagating FWM in fibers or SOAs [22, 23]. These techniques require the signal to be co- and orthogonally-polarized with respect to the two pumps and result in an orthogonally-polarized conjugate with respect to the signal. Since the polarization of the signal cannot be readily controlled in a transmission system, both frequency and polarization shift free MSSI is required.

In this paper, we utilize our previously reported method of frequency and polarization shift free OPC (FS-OPC) in SOA [24] as MSSI, for nonlinearities compensation of a 200 Gbps QPSK modulated signal transmitted over 800 km–1200 km standard single mode fiber (SSMF). High nonlinearities, excellent phase-matching with short active lengths (500  $\mu\text{m}$ –2000  $\mu\text{m}$ ), small pump power requirements due to inherent amplification, and easier photonic integration makes SOA a better candidate for MSSI than HNLF [25]. Hence, we discuss MSSI using FS-OPC by a counter-propagating dual pump FWM in an SOA. The two counter-propagating pumps are input at the opposite ends of the SOA and a signal co-propagating with one of the pumps is input to the SOA. The beating between the co-propagating pump and the signal creates a refractive index and gain grating in the active layer of the SOA. The other pump diffracts from the grating to generate a phase-conjugate version of the signal. The signal and its conjugate appear at opposite ends of the SOA [24]. A frequency shift between the signal and its conjugate is

avoided by keeping the two pump frequencies symmetrical about the signal frequency, while polarization-shift is avoided by keeping the two pumps co-polarized [26]. It is important to note that the MSSI can compensate for fiber nonlinearities in QAM and other higher modulation formats [27]. However, we considered the nonlinearities compensation of QPSK modulated signal, to reduce the computational complexity.

We investigate the performance of MSSI for nonlinearities compensation, by studying the Q-factor of a 200 Gbps QPSK signal received with and without MSSI as a function of launched signal power for various span lengths and number of spans. Further, we study the performance dependence of MSSI on the parameters, namely, pump power and SOA current. The results achieved show that a 7.5 dB increase in input power dynamic range (IPDR) and an 83% improvement in transmission length can be obtained.

The rest of the paper is organized as follows: in section 2, we present our MSSI scheme using FS-OPC by counter-propagating dual pump FWM in an SOA. In section 3, we carry out numerical simulations to scrutinize the performance of MSSI as nonlinearities compensation of a QPSK signal by studying the Q-factor variation as a function of launched power for different span lengths and number of spans. We also investigate the performance dependence of MSSI on pump power and SOA current. Finally, in section 4, we conclude by summarizing the results.

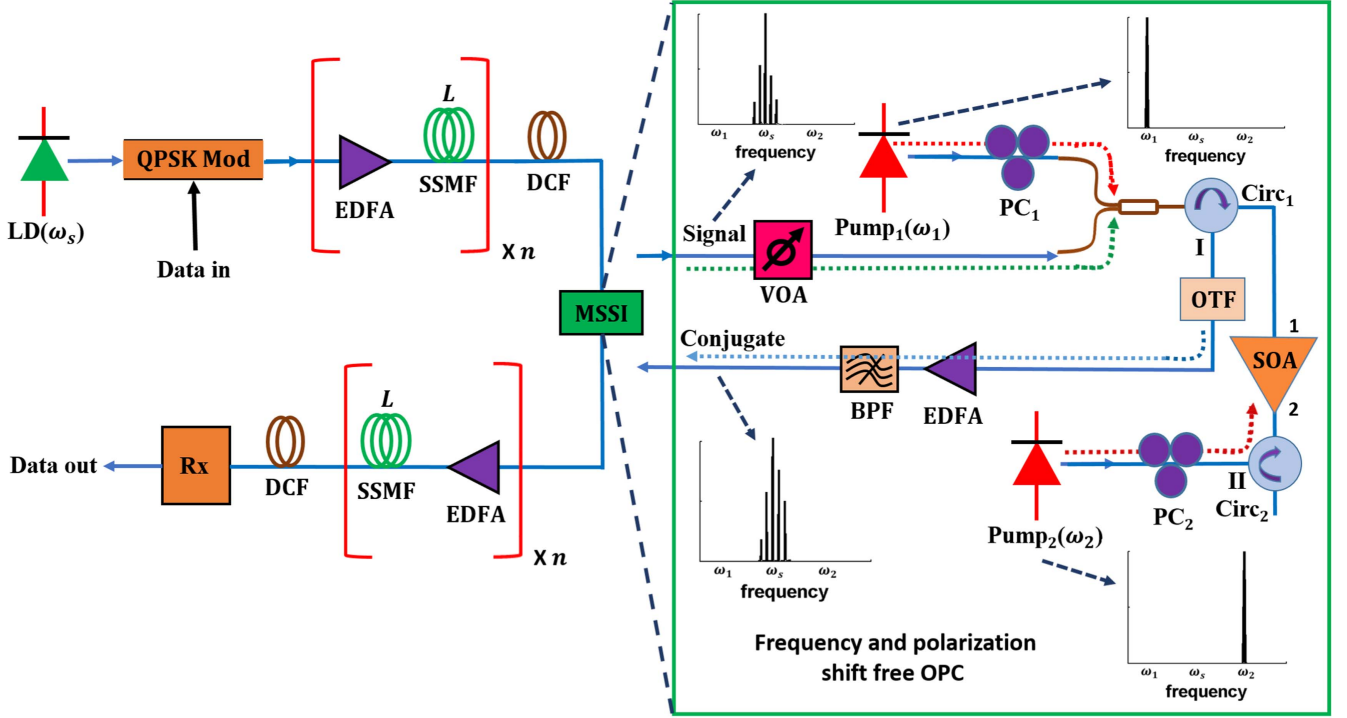
## 2. System description

Figure 1 shows the schematic diagram of a transmission link containing the frequency-degenerate MSSI using FS-OPC. The optical carrier of angular frequency  $\omega_s$  from a laser diode is QPSK modulated with symbols  $b_n \in \{1, +j, -1, -j\}$  and launched into the first half of the transmission link. The signal is distorted by dispersion and nonlinearities induced phase in  $n \times L$  km of SSMF. This distorted phase is inverted by MSSI placed at the middle of the link as shown in figure 1. The phase-inverted signal propagates through the second half of the link (of SSMF length  $n \times L$ ), where the signal experiences similar distortions as those experienced in the first half, in such a way the new distortions cancel out the inverted distortion. Subsequently, the received signal is coherently detected and original transmitted symbols are recovered. The Q-factor (in dB) is obtained by counting the bit-error rate (BER) from the detected sequence, using

$$Q = 20 \times \log_{10}(\sqrt{2} \times \text{erfc}^{-1}(2\text{BER})). \quad (1)$$

We include dispersion compensating fibre (DCF), so we can focus on the compensation of the fibre non-linearities by MSSI. Although, MSSI has proven to compensate for dispersion [18].

The frequency-degenerate MSSI using counter-propagating dual pump FWM in an SOA is shown in the inset of figure 1. The signal power is reduced by an attenuator (to avoid operating the SOA in a saturation regime), then combined with pump<sub>1</sub> (at angular frequency  $\omega_1$ ) and injected into the SOA from port 1. Pump<sub>2</sub> (at angular frequency  $\omega_2$ ) is



**Figure 1.** Simulation setup to study nonlinearity compensation of QPSK signal transmission through  $n$  span of  $L$  km SSMF using frequency-degenerate MSSI through counter-propagating dual pumped FWM in SOA. LD = laser diode, QPSK Mod = quadrature phase-shift keying modulator, EDFA = erbium doped fiber amplifier, SSMF = standard single mode fiber, DCF = dispersion compensating fiber, PC<sub>1,2</sub> = polarization controller, VOA = variable optical attenuator, Circ<sub>1,2</sub> = circulator, SOA = semiconductor optical amplifier, OTF = optical tunable filter, BPF = band pass filter, Rx = receiver.

injected from port 2. The pump frequencies are kept symmetrical about the signal frequency as shown in the spectra of figure 1. The beating between signal and pump<sub>1</sub> leads to a refractive index and gain grating inside the active layer of the SOA, which diffracts the pump<sub>2</sub> to create a conjugate copy of the signal (with inverted spectrum at the central frequency  $\omega_s$ ) propagating in the opposite direction of the signal [24, 28]. Polarization controllers (PC<sub>1,2</sub>) are used to keep the two pumps co-polarized, to obtain a higher conjugate efficiency. In a recent study, we have demonstrated an OPC efficiency of 1% with an SOA [24]. The conjugated signal is filtered from the co-propagating pump<sub>2</sub> by an optical tunable filter and amplified by an EDFA before being transmitted in the second half of the network. A band pass filter removes the noise introduced by the EDFA.

#### Expression for phase-conjugation

We obtain the equations governing the evolution of signal and conjugate by solving the nonlinear Schrödinger equation with a total electric field inside the SOA,  $\sum_{i=1,2} E_i(z, t) \exp(j(\omega_i t + (-1)^i k_i z)) + E_s(z, t) \exp(j(\omega_s t - k_s z)) + E_c(z, t) \exp(j(\omega_s t + k_s z))$  and assuming the gain saturation is dominated by two pumps, as [28],

$$\begin{aligned} \frac{\partial E_s}{\partial z} &= -\mu_s E_s + j\nu_s E_c^* \exp(j\Delta k z) \\ \frac{\partial E_c^*}{\partial z} &= \mu_c^* E_c^* + j\nu_c^* E_s \exp(-j\Delta k z) \end{aligned} \quad (2)$$

where  $E_m$ ,  $m = 1, 2, s, c$  are the electric field envelopes of pump<sub>1</sub>, pump<sub>2</sub>, signal, and conjugate respectively,  $\Delta k = k_1 - k_2$ ,  $k_n$ ,  $n = 1, 2, s$  are propagation constant of pump<sub>1</sub>, pump<sub>2</sub>, and signal, respectively, and  $\mu_{s,c}$  and  $\nu_{s,c}$  are given by

$$\begin{aligned} \mu_{s,c} &= -\frac{g_0}{2(1+P_0)} \left[ 1 - j\beta - \frac{\omega^2}{\Delta\omega_g^2} - \frac{(1-j\beta)CrP_0}{1 \mp j\Omega T_2/2} \right] \\ &\quad + \frac{g_0}{2(1+P_0)} \frac{(1-j\beta)CrP_0}{1 \mp j\Omega T_2/2} \frac{1}{1 \mp j\Omega T_1} \\ \nu_{s,c} &= \frac{jg_0}{2(1+P_0)} \frac{Cr[1-j\beta(1 \mp j\Omega T_2)]}{(1 \mp j\Omega T_2)(1 \mp j\Omega T_1)} 2E_1 E_2 \end{aligned} \quad (3)$$

where  $-$  and  $+$  sign goes for  $s$  and  $c$  respectively  $\Omega$  is the detuning between the pump and the signal,  $g_0 = \Gamma a \bar{N}_0 (I/I_0 - 1)$  is the small signal gain,  $\Gamma$  denotes the confinement factor,  $a$  ( $\approx 2 \times 10^{-16}$  to  $3 \times 10^{-16}$  cm<sup>2</sup>) the gain coefficient, and  $I$  is the SOA current.  $I_0$  is the current needed to achieve transparency in the active region of the SOA,  $\bar{N}_0$  ( $\approx 1 \times 10^{18}$  to  $2 \times 10^{18}$  cm<sup>-3</sup>) is the carrier density at  $I_0$ ,  $\beta$  ( $\approx 3$  to  $6$ ) is the linewidth enhancement factor, and  $P_0$  is the intracavity pump power. Other parameters are given in [28]. Equation (2) is valid for a large pump-signal detuning exceeding 100 GHz [28]. The expression for a phase-conjugated signal is obtained by solving (2) subjected to boundary conditions:

$E_s(z=0) = E_{s0}$  and  $E_c(z=L_{SOA}) = 0$ ,

$$E_c(z) = -jv_c E_{s0}^* e^{-(\chi^* - \mu_c)z} \times \left[ \frac{\sin \zeta(L_{SOA} + z)}{\chi \sin \zeta L_{SOA} + \zeta \cos \zeta L_{SOA}} \right]^* \quad (4)$$

where  $\chi = (\mu_s + \mu_c^* + \Delta k)/2$  and  $\zeta = \sqrt{(2\chi)^2 - v_s v_c^*}/2$ . Thus, at  $z=0$ ,  $E_c$  is a phase-conjugate of the input signal  $E_{s0}$  with an additional phase-constant. It is interesting to note that the perfect phase-conjugation is possible with a similar scheme using HNLf as reported in our previous work [26]. We see that, at  $z=0$ , conjugate ( $E_c(0)$ ) and conjugate efficiency ( $\frac{|E_c(0)|^2}{|E_{s0}|^2}$ ) depend upon the pump power and the SOA current through  $\chi$  and  $\zeta$ . Therefore, the MSSSI transmission performance is dependent on these two as well.

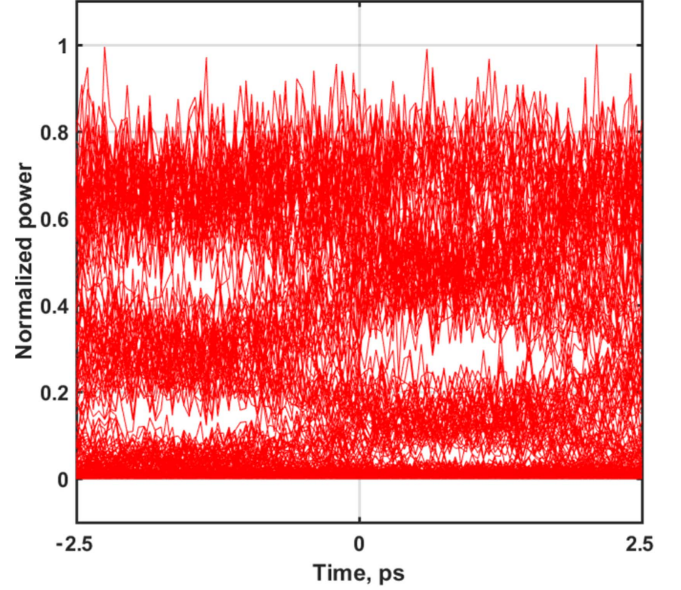
### 3. Performance of SOA-based MSSSI

We investigate the performance of MSSSI by numerically simulating the scheme shown in figure 1, by evaluating the Q-factor of a 200 Gbps QPSK transmission system with and without MSSSI. For the sake of simplicity, we only consider a single polarization QPSK transmission system. The length ( $L$ ) of SSMF ( $\alpha = 0.2$  dB/km,  $D = 16$  ps/nm-km) is taken as 80 km and the total number of spans ( $2n$ ) as 10 throughout the simulation unless otherwise specified. The parameters for DCF are:  $\alpha_{dcf} = 0.5$  dB/km and  $D = -80$  ps/nm-km and length of DCF are chosen to compensate the dispersion in the SSMF, whereas the parameters of the EDFA are taken as: gain = 30 dB and noise-figure = 5 dB. The wavelengths of the signal, pump<sub>1</sub>, and pump<sub>2</sub> are 1550 nm, 1550.8 nm, and 1549.2 nm, respectively. The linewidth of the signal and the pump waves are taken as 100 kHz and 10 kHz, respectively, whereas the optical signal to noise ratio (OSNR) of the signal and the pump waves is kept at 40 dB and 60 dB, respectively. Parameters of the SOA are:  $\beta = 4$ ,  $\Gamma = 0.5$ ,  $L_{SOA} = 1$  mm,  $\bar{N}_0 = 2 \times 10^{18}$  cm<sup>-3</sup>,  $a = 3 \times 10^{-16}$  cm<sup>2</sup>. We use a MATLAB-based simulation toolbox Optilux to simulate the transmission system [29].

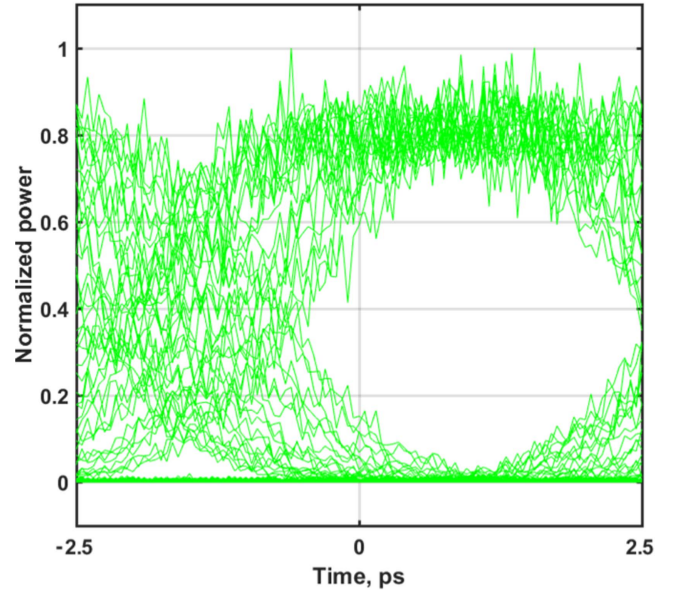
We simulate a 200 Gbps QPSK transmission system with and without MSSSI for total transmission distance of 1600 km to understand the impact of MSSSI. Figures 2(a) and (b) show the eye-diagram of the received signal with and without MSSSI, respectively. In figure 2(a), a nearly complete eye closure of the transmitted signal can be seen. It can be ascribed to signal distortion due to fiber nonlinearities, while in figure 2(b), the effect of the nonlinearities compensation by the MSSSI can be observed validated by the wide open eye with respect to the previous eye.

#### 3.1. Q-factor versus launched power with increased span length

We simulate a 200 Gbps QPSK transmission system with and without MSSSI as a function of launched signal power for different span lengths but with a number of spans ( $n$ ) set to



(a)

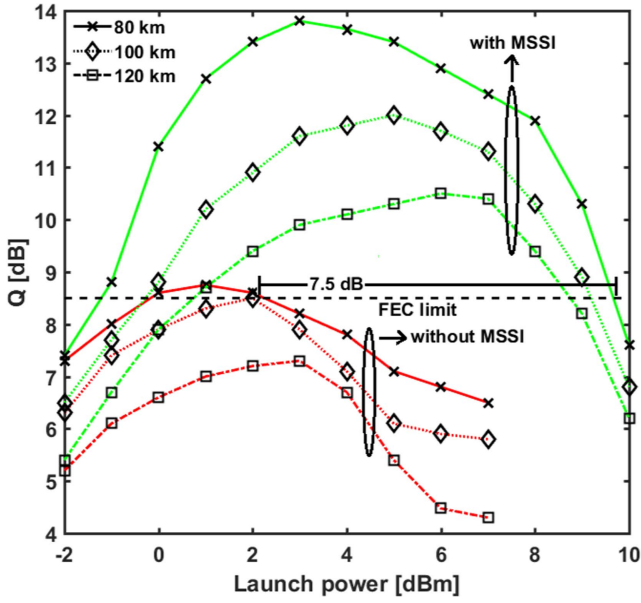


(b)

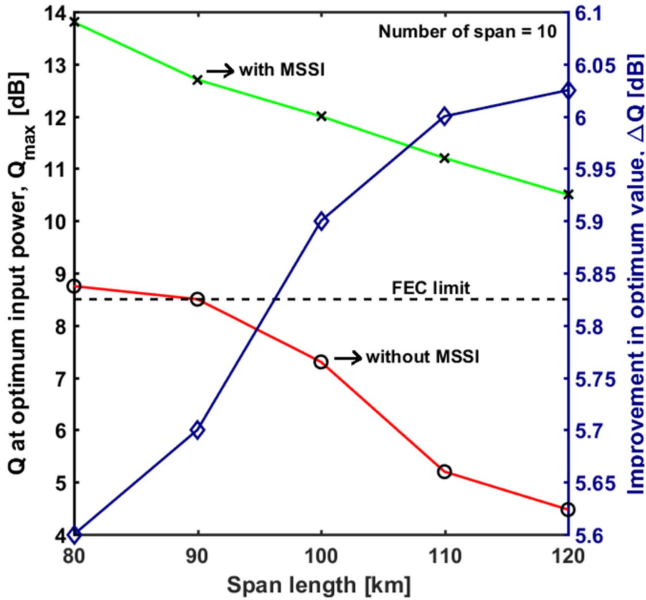
**Figure 2.** Eye diagram of 200 Gbps received signal (a) with and (b) without MSSSI. Span length, total number of spans, and SOA current are kept at 80 km, 20, and 400 mA, respectively.

10. Pump power and SOA current are kept at  $-2$  dBm and 400 mA, respectively, to avoid saturation of the SOA.

Figure 3(a) shows the simulation results of Q-factor versus launch power for increased span length (80 km:  $\times$ , 100 km:  $\diamond$ , 120 km:  $\square$ ). All red lines show Q-factors for the reference system without MSSSI, whereas all green lines represent the Q-factors for the transmission system with MSSSI. The black dashed ( $-$ ) line shows the FEC limit corresponding to a BER of  $4 \times 10^{-3}$  [30]. The Q-factor increases with launch power due to an increase in the OSNR and then decreases due to an increase in SSMF nonlinearities



(a)



(b)

**Figure 3.** (a) Q-factor versus launch power with and without MSSSI for 200 Gbps QPSK transmission with different span lengths (80 km, 90 km, and 120 km). (b) Optimum Q-factor and improvement versus span length. The total number of span, pump power, and SOA current are 10,  $-2$  dBm, and 400 mA, respectively.

at higher launched powers. There is an improvement of Q-factor when MSSSI is deployed in the reference system. As the launched power increases, the improvement in the Q-factor augments due to an increase in the conjugate-efficiency. However, at launch powers higher than 8 dBm the Q-factors decreases sharply and falls below the forward error correction (FEC) limit. This is due to the saturation of the SOA at higher powers. The maximum Q-factor of 13.8 dB is obtained at an optimum launched power of 3 dBm for a system with a span length of 80 km and the improvement in

Q-factor at this optimum launched power is 5.6 dB. Further, we observe the IPDR spanning from 2 dBm to 9.5 dBm with a total improvement of 7.5 dB, when MSSSI is used with a  $10 \times 80$  km transmission reach.

The maximum span length of the reference system is 80 km, after which the Q-factor degrades below the FEC limit. On the other hand, the transmission system with MSSSI sustains its Q-factor above the FEC limit up to 120 km of span length. Therefore, the total transmission length is increased from  $10 \times 80$  km to  $10 \times 120$  km. Figure 3(b) shows a maximum Q-factor for span lengths of 80 km to 120 km for a transmission system with (green line with  $\times$ ) and without (red line with  $\circ$ ) MSSSI and a corresponding improvement in Q-factor with MSSSI (blue line with  $\diamond$ ). The increase in span length causes the increase in nonlinear power asymmetry in the two halves of the transmission fiber resulting in less efficient functioning of MSSSI, leading to a degradation of the Q-factor. However, the improvement in  $\Delta Q$  with an increase in span length suggests that the effect of nonlinearities compensation due to MSSSI extends the span length. This is due to an improvement in the maximum permissible launched power when MSSSI is used.

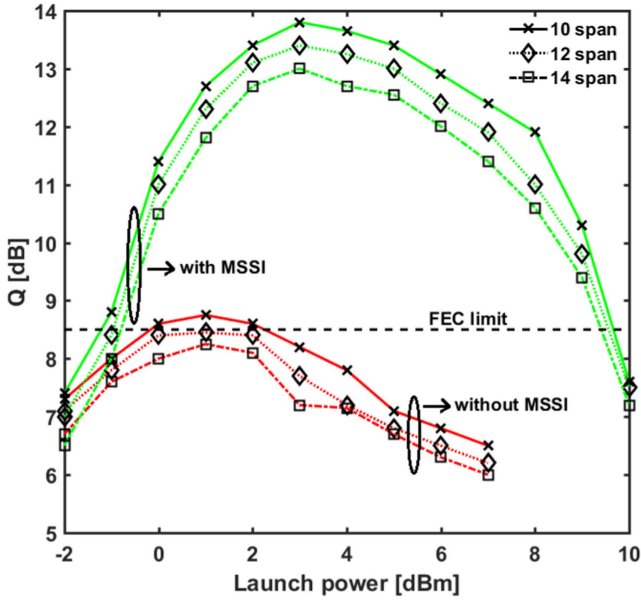
With a BER set at  $10^{-3}$ , we observe a IPDR between  $-1$  dBm and 10 dBm, between 0 dBm and 9.5 dBm, and between 1 dBm and 9 dBm for the span lengths 80 km, 100 km, and 120 km, respectively.

Finally, we observe the improvement in Q-factors, maximum launched power, and IPDR when MSSSI is used, suggesting the fiber nonlinearities compensation by MSSSI. The transmission system is also able to benefit from an increase in the maximum permissible launched power to the transmission length by having a longer span. At the transmission length of  $10 \times 80$  km, improvement in Q-factor and maximum launched power due to MSSSI are 5.6 dB and 7.5 dB, respectively.

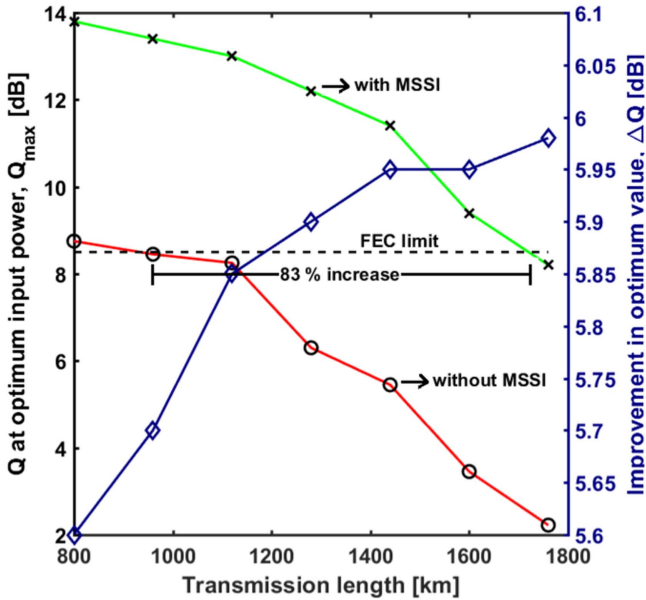
### 3.2. Q-factor versus launched power with increased number of span

We also investigate the improvement in Q-factor due to MSSSI for a longer transmission length with an increasing number of spans and keeping span length fixed to 80 km. Figure 4(a) shows the Q-factor versus launched power for three different span numbers (10:  $\times$ , 12:  $\diamond$ , 14:  $\square$ ) for both, a transmission system with (green lines) and without MSSSI (red line). The Q-factor of the reference transmission system without MSSSI falls below the FEC limit for any span number larger than 10. However, the transmission system with MSSSI shows less degradation in Q-factor with increasing transmission length as the nonlinear power asymmetry on either side of MSSSI becomes less and less significant with increasing number of spans (as compared to increasing transmission length by increasing span length at fixed number of span). The IPDR is between  $-1.2$  dBm and 9.6 dBm for 10 spans, between  $-1$  dBm and 9.5 dBm for 12 spans, and between  $-0.8$  dBm and 9.4 dBm for 14 spans.

Figure 4(b) shows the Q-factor at the optimum input power as a function of transmission length for a system with



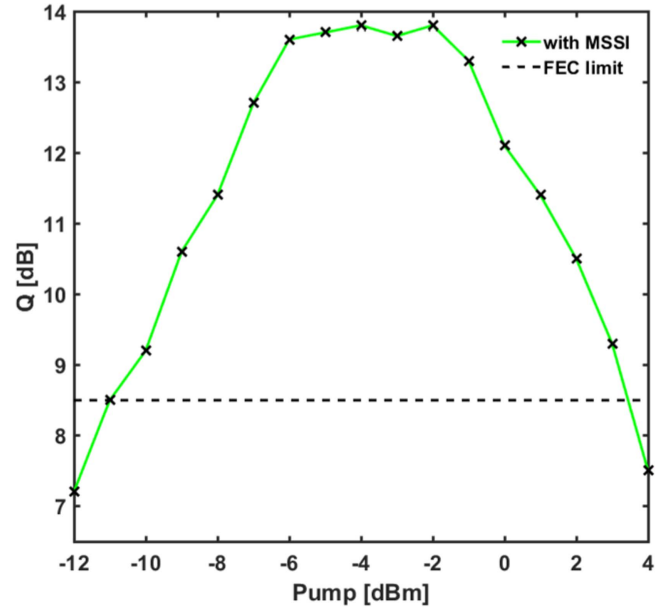
(a)



(b)

**Figure 4.** (a) Q-factor versus launch signal power with and without MSSI for 200 Gbps QPSK transmission with different transmission lengths ( $10 \times 80$  km,  $12 \times 80$  km, and  $14 \times 80$  km). (b) Optimum Q-factor and improvement versus transmission length. The span length, pump power, and SOA current are 80 km,  $-2$  dBm, and 400 mA, respectively.

(green line with  $\times$ ) and without MSSI (green line with  $\circ$ ). The optimum Q-factor in the reference system falls below the FEC limit after  $12 \times 80$  km of transmission system distance, while the Q-factor for the MSSI system is above the FEC limit before  $22 \times 80$  km. This shows that SOA-based MSSI can improve the maximum transmission length by more than 83% with a span length of 80 km. The blue line with  $\diamond$  in figure 4(b) shows a 5.6 dB improvement in Q-factor when



**Figure 5.** Q-factors dependence on SOA pump power. The FEC limit corresponds to BER of  $4 \times 10^{-3}$ .

MSSI is used in  $10 \times 80$  km transmission length. Further, this improvement increases by 0.4 dB when transmission length increases from  $10 \times 80$  km to  $22 \times 80$  km.

#### Performance dependence of transmission system on MSSI parameters

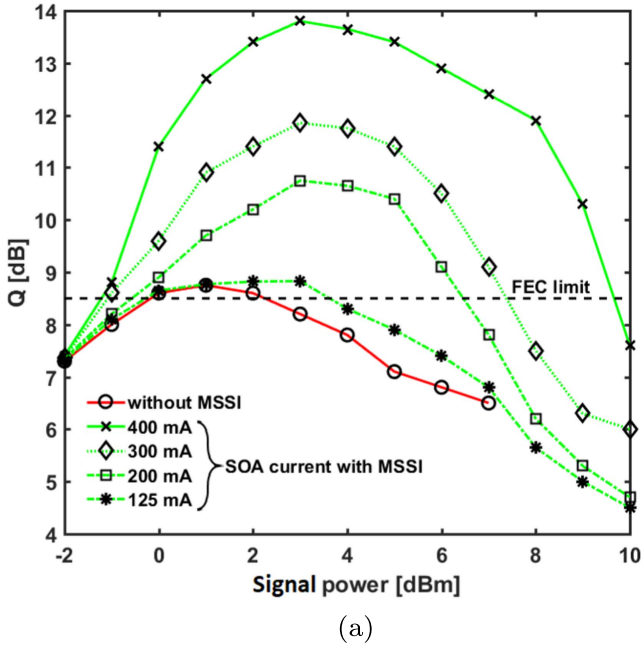
We next investigate the performance dependence of MSSI for nonlinearities compensation in a transmission system on parameters of MSSI itself, by changing its control parameters, namely, pump power and SOA current.

#### 3.3. Influence of pump power

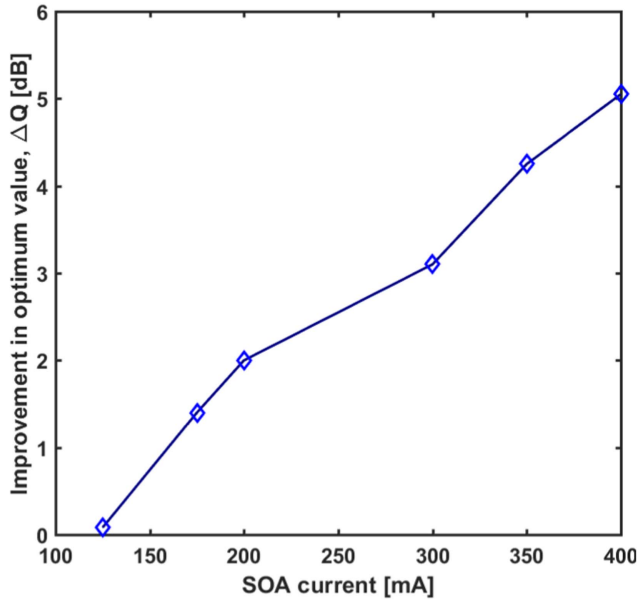
We study the effect of pump power on the nonlinearities compensation by MSSI by simulating the Q-factor as a function of pump power for a transmission length of  $10 \times 80$  km SSMF. The launched signal power and SOA current are kept at 3 dBm and 400 mA, respectively. Figure 5 shows the dependence of Q-factor on pump power. The solid line with a cross ( $\times$ ) and the dashed line ( $-$ ) denotes the Q-factor with MSSI and FEC limit corresponding to BER of  $4 \times 10^{-3}$ , respectively. The Q-factor increases with pump power, due to an increase in the conjugate-efficiency and attains a values between 13.3 dB–13.8 dB until a pump power of  $-1$  dBm is reached. Thereafter, Q-factors decreases with pump power and goes below the FEC limit after a pump power of 3 dBm. This is due to saturation of SOA resulting in a lower conjugate-efficiency at higher pump powers.

#### 3.4. Q-factor versus signal power with different SOA currents

Figure 6(a) shows the Q-factor versus signal power for the reference transmission system without MSSI and the transmission system with MSSI at different SOA currents (400 mA:  $\times$ , 300 mA:  $\diamond$ , 200 mA:  $\square$ , 125 mA:  $*$ ). The pump



(a)



(b)

**Figure 6.** (a) Q-factor versus launch power with and without MSSSI for 200 Gbps QPSK transmission with different SOA current (400 mA, 300 mA, 200 mA, and 125 mA). (b) Improvement in optimum Q-factor versus SOA current. The pump power, span length, and number of span are  $-2$  dBm, 80 km, and 10, respectively.

power, span length and number of spans are kept at  $-2$  dBm, 80 km, and 10, respectively. The green and red line show the Q-factor of the system with and without MSSSI, respectively. As the SOA current increases the small signal gain ( $g_0$ ) increases, which results in an increase in conjugate-efficiency and hence performance of MSSSI is improved resulting in a optimum Q-factor as high as 13.8 dBm at 400 mA SOA

current. Further, the improvement of MSSSI performance (in nonlinearities compensation) is suggested by the enhancement of IPDR from [0 dBm–3.8 dBm] to [ $-1$  dBm–9.7 dBm], when the SOA current is increased from 125 mA to 400 mA. Figure 6(b) shows the improvement in the optimum Q-factor when MSSSI is used as a comparison to the reference system. Improvement in the optimum Q-factor increases with an increase in SOA current and an increment of 5 dB of improvement in the optimum Q-factor is obtained when the SOA current is increased from 125 mA to 400 mA.

#### 4. Summary

We have presented a scheme of frequency-degenerate MSSSI by FS-OPC through counter-propagating dual pump FWM in SOA, for nonlinearities compensation of a 200 Gbps QPSK signal transmitted over SSMF. Frequency-degeneracy between the signal and the conjugate is obtained by placing the pump frequencies symmetrical about the signal frequency. The polarization of the signal and the conjugate are maintained (co-polarized) by using two co-polarized pumps. The SOA has proven to be a device of interest in the FS-OPC scheme as it exhibits non-linear mechanisms sustaining  $>100$  GHz pump-probe detuning.

We have examined the performance of MSSSI for nonlinearities compensation of a QPSK transmitted signal by simulating the Q-factor as a function of launched power for different span lengths and number of spans. The nonlinearities compensation is visualized by an increase in Q-factor by 5.6 dB at 3 dBm launched power for transmission length of  $10 \times 80$  km, when MSSSI is used. We also observed the improvement in maximum launched power by 7.5 dB. The increase in span length with 10 spans resulted in an asymmetric distribution of nonlinear power in the two halves of the transmission fiber caused less efficient MSSSI, which in turn led to a reduction in Q-factor with span length. However, when the number of spans is increased at 80 km of span length, the nonlinear power asymmetry in either side of MSSSI became less and less significant and resulted in an increase of the maximum transmission length by almost 83%.

In conclusion, we have demonstrated nonlinearities compensation of a 200 Gbps QPSK signal transmitted over SSMF by exploiting the FS-OPC as frequency-degenerate MSSSI. We have shown that under the right set of MSSSI parameters elucidated in this paper, fiber nonlinearities is significantly reduced, allowing data transmission at a 13.8 Q-factor for 3 dBm launched power over  $10 \times 80$  km SSMF without pre or post data processing.

#### ORCID iDs

Abhishek Anchal <https://orcid.org/0000-0003-4434-1707>  
Sean O’Duill <https://orcid.org/0000-0002-7690-4474>



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