

Compositional Variation in Hybrid Organic-Inorganic Lead Halide Perovskites:  
Kinetically- versus Thermodynamically-controlled Synthesis

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**Abstract**

The formation and study of partial solid solutions in  $Az_{1-x}FA_xPbBr_3$ , using reportedly similar sized cations azetidinium ( $Az^+$ ) and formamidinium ( $FA^+$ ), was explored via mechanosynthesis and precipitation synthesis. The composition and lattice parameters of samples from both syntheses were analyzed by  $^1H$  NMR and Rietveld refinement of powder X-ray diffraction. A clear mismatch in the composition of the perovskite was found between the precipitated samples and the corresponding solutions. Such a mismatch was not observed for samples obtained via mechanosynthesis. The discrepancy suggests products are kinetically-controlled during precipitation, compared to thermodynamically controlled mechanosynthesis. Furthermore, the cell volume as a function of composition in both hexagonal, 6H (Az-rich) and cubic, 3C (FA-rich) perovskite solid solutions suggests that  $FA^+$  is actually smaller than  $Az^+$ , contradicting the literature. In the 3C (Az-poor) solid solutions, the extent of  $Az_{1-x}FA_xPbBr_3$  is unexpectedly smaller than in the corresponding methylammonium ( $MA^+$ ) system,  $Az_{1-x}MA_xPbBr_3$ , which suggests that the extent of solid solution formation in these halide perovskites is predominantly dependent on the average A-cation size while the size mismatch plays a lesser role in comparison to oxides.

## Introduction

Organic-inorganic hybrid perovskites (OIHPs), which share a general formula  $ABX_3$ , where the A-cation is typically an organic ammonium group, the B-cation is typically a group 14 cation and most commonly Pb(II) and the X-anion is a halide. OIHPs have emerged as promising materials for next-generation solar cells,<sup>1-3</sup> light-emitting diodes,<sup>4,5</sup> optically-pumped lasers<sup>6</sup> and photodetectors.<sup>7,8</sup> The optoelectronic properties of OIHPs are highly dependent on the nature of B-X interactions as their orbital interactions determine the formation of valence and conduction bands and band gap. The Goldschmidt tolerance factor,  $t$ , which relates the relative sizes of the A, B and X ionic radii, is a simple metric to ascertain if a stable 3D-perovskite structure is adopted and whether any structural distortion from the cubic aristotype is likely to be present. The most common type of distortion driven by the size of the A-cation is octahedral tilting, which affects the B-X orbital overlap and hence the optical bandgap.<sup>9</sup> The pioneering work in OIHPs used methylammonium ( $MA^+$ ) as the A-site cation to produce a cubic 3D-perovskite structure,<sup>10</sup> with formamidinium ( $FA^+$ ) also adopting the cubic structure.<sup>11</sup> The band structure of perovskite materials can be tuned directly by varying the B-cation and the halide (although the choice of suitably large B-cations is rather limited) or indirectly due to structural distortions driven by the A-cation size. As a result, the A- and X-site species are commonly manipulated via solid solution formation in order to tune the optoelectronic properties such as the bandgap,<sup>11-13</sup> emission energies<sup>14,15</sup> and photoluminescence lifetime.<sup>16,17</sup> In addition to structural diversity,<sup>18-21</sup> other advantages of A-cation doping have been shown to include improved stability<sup>22</sup> and power conversion efficiency of photovoltaic devices,<sup>23</sup> and reduced trap states in the fabrication of solar cells.<sup>24,25</sup> For example, Saliba *et al.* achieved high efficiency solar cells up to 21.6% with a mixed A-cation composition – (Rb,Cs,MA,FA)PbI<sub>3</sub>, which retained 95% power conversion efficiency after 500 hours at 85 °C.<sup>26</sup> Prochowicz *et al.* obtained a mixed A-cation solid solution system  $MA_xFA_{1-x}PbI_3$  by mechano-synthesis to stabilise the  $\alpha$ -FAPbI<sub>3</sub> cubic phase in air, which is a key absorber layer in high-efficient solar cells.<sup>22</sup>

To obtain perovskite solid solutions (e.g., with mixed A-cations), synthetic methods including anti-solvent<sup>21,27</sup> and oversaturation<sup>3,9</sup> precipitation or mechano-synthesis (grinding)<sup>13,28</sup> are typically used. Principally, the choice of synthetic method has an impact on the morphology of the perovskite material: precipitation and mechano-synthetic methods have been widely used to obtain

large single crystals or powders that can then be used for structural and photophysical studies. During precipitation synthesis, however, it is usually assumed that the final (actual) sample composition retains the ‘nominal’ initial molar ratio of ion sources of the precursor solution. Importantly, this assumes that the kinetics of precipitation are independent of the precursor species and nominal composition. The validity of this assumption is often not checked by compositional analysis but rather ‘validated’ by the observation of a systematic change in properties. In contrast, during mechanosynthesis, all the precursor materials are retained, and the reaction product is obtained under thermodynamic control in a manner analogous to conventional (mixed salt) high temperature solid-state routes. Under such conditions, the final product(s) must reflect the constituent global starting composition and, therefore, if a single phase (perovskite) product is achieved then this must, perforce, have the nominal starting composition.

Any mismatch between nominal and actual composition may reduce the reliability of the conclusions drawn from subsequent structural and photophysical studies. Examples of nominal and actual composition mismatch in mixed-metal<sup>24,29-32</sup> and mixed-halide<sup>24</sup> perovskite systems have been studied using X-ray photoelectron spectroscopy (XPS) and flame atomic absorption spectroscopy (FAAS). These studies demonstrated that the actual amount of Sn and Bi, incorporated in  $\text{FAPb}_{1-x}\text{Sn}_x\text{Br}_3$ <sup>24</sup> and Bi-doped  $\text{MAPbX}_3$  ( $X = \text{Cl}, \text{Br}, \text{I}$ )<sup>29-31</sup> single crystals respectively, was significantly less than the nominal percentages of Sn and Bi in the initial respective solution. In another example, the actual Cl% in  $\text{FAPbBr}_{3-x}\text{Cl}_x$ <sup>24</sup> crystals was found to be larger than the nominal value for Cl-poor target compositions ( $< 50\%$  Cl) but smaller for Cl-rich reactions. Similar instances were also found for A-cation substitutions.<sup>15,33</sup> For instance, Spanopoulos *et al.*<sup>15</sup> demonstrated by NMR analysis that the actual ethylenediammonium (en) incorporated in  $(\text{MA}_{1-x}\text{en}_x)\text{PbI}_3$  was less than the nominal composition. To account for such mismatches, several explanations<sup>29,31,34</sup> have been proposed including the difference between valence (and hence induced compensating defects) and ionic radii, and surface effects (especially for XPS analysis) for mixed metal (B-site) solid solutions. Such explanations for mixed halide and mixed A-cation systems are absent as the composition with respect to halide and organic A-cation content is overlooked in most studies. Most compositional studies on nominal and actual compositions of solid solutions with substitutions at A, B, and X sites are carried out on samples prepared by precipitation methods and in systems that can support a complete solid solution due to isostructural end-members. Beyond simple observation of lattice parameter variations (Vegard’s

law), the paucity of structural contrast makes it challenging to determine if the system sustains solid solution formation or has phase separation. Using  $^{207}\text{Pb}$  NMR spectroscopy, Askar *et al*<sup>35</sup> revealed that while mechanosynthesis provides fine control over the halide composition in mixed halide  $\text{FAPbX}_3$  ( $X = \text{Cl/Br, Br/I}$ ) samples, solution synthesized samples showed composition mismatch compared with the precursor solution (e.g., Br-rich product is formed from a nominal starting composition of  $\text{FAPb}(\text{Br}_{0.5}\text{I}_{0.5})_3$ ). Considering the compositional consistency of mechanosynthesis, the formation of 6H and 3C lead bromide perovskite with mixed organic A-cations is here explored to study the relation between the nominal and actual composition using both NMR and PXRD analyses.

The previously reported solid solution study<sup>21</sup> of  $\text{AZ}_{1-x}\text{MA}_x\text{PbBr}_3$ , prepared by antisolvent precipitation, indicated partial solid solutions of the hexagonal (6H)  $\text{AzPbBr}_3$  and cubic (3C)  $\text{MAPbBr}_3$  parent perovskite structures with an intermediate 6H-3C two phase region for  $0.3 \leq x \leq 0.8$ . The compositional variation also allows tuning of the bandgap from the two end members: 2.20 eV ( $\text{MAPbBr}_3$ ) to 2.81 eV ( $\text{AzPbBr}_3$ ). In this system, there is a large difference in cation size between Az and MA. In the current study, the impact of using cations of reportedly similar size, Az and FA ( $r_{\text{Az}} = 250$  pm,  $r_{\text{FA}} = 253$  pm,  $r_{\text{MA}} = 217$  pm)<sup>36</sup> in the solid solution  $\text{AZ}_{1-x}\text{FA}_x\text{PbBr}_3$  was explored. The hypothesis is that a wider range of solid solutions should exist for this system given the similar cation size. The extent of solid solution formation using both mechanosynthesis and precipitation methods was investigated and compared with two related systems:  $\text{AZ}_{1-x}\text{MA}_x\text{PbBr}_3$  and  $\text{MA}_{1-x}\text{FA}_x\text{PbBr}_3$  ( $0 \leq x \leq 1$ ). By comparing the solid solutions of the  $\text{AZ}_{1-x}\text{MA}_x$  and  $\text{AZ}_{1-x}\text{FA}_x$  systems, the experimentally-determined range of the 3C (MA- and FA-rich) solid solution is smaller in  $\text{AZ}_{1-x}\text{MA}_x$ , in contrast to the expectation based simply on cation size. In addition, a clear mismatch between the nominal (reaction) and actual (product) composition was found during precipitation synthesis for both  $\text{AZ}_{1-x}\text{MA}_x$  and  $\text{AZ}_{1-x}\text{FA}_x$  systems, indicating that this method is under kinetic control. In comparison, mechanosynthesis is thermodynamically controlled and results in more extensive solid solutions where the nominal composition is retained as the actual composition. Solvent-free mechanosynthesis is highly recommended as a greener approach to study mixed composition perovskite.

## Experimental section

**Synthesis.** Formamidineum bromide<sup>37</sup> and azetidinium bromide,<sup>21</sup> starting materials were synthesised according to the literature. Formamidineum acetate (99%) and PbBr<sub>2</sub> (98%) were purchased from Alfa Aesar. Hydrobromic acid in water (48%) and AzCl (95%) were purchased from Fluorochem. All other reagents and solvents were obtained from commercial sources and used as received.

*FABr.* The synthesis was largely adapted from the literature.<sup>37</sup> Formamidineum acetate (1.04 g, 10 mmol, 1 equiv.) and hydrobromic acid (2.3 mL, 20 mmol, 2.0 equiv.), were mixed stirred at 50 °C for 20 min. The solvent was removed under reduced pressure. The crude products were dissolved in 2 mL EtOH and the product recrystallized from diethyl ether. The recovered solid was dried under vacuum for 24 h before use. White needle-like crystals were obtained. Yield: 91%. Mp.: 132 – 136 °C (Lit. Mp<sup>38</sup> = 133 – 140 °C) <sup>1</sup>H NMR (400 MHz, DMSO-*d*<sub>6</sub>) δ (ppm) 8.75 (s, 4H), 7.86 (s, 1H). <sup>13</sup>C NMR (101 MHz, DMSO-*d*<sub>6</sub>) δ (ppm) 40.19. Elemental Analysis. Calculated for CH<sub>5</sub>BrN<sub>2</sub>: C, 9.61; H, 4.03; N, 22.42; Br, 63.94; Found: C, 9.42; H, 4.14; N, 22.30.

*Az<sub>1-x</sub>FA<sub>x</sub>PbBr<sub>3</sub>* ( $0 \leq x \leq 1$ ). Mechano-synthesis: Az<sub>1-x</sub>FA<sub>x</sub>PbBr<sub>3</sub> samples were prepared by mixing appropriate molar ratios of vacuum dried AzBr and FABr with PbBr<sub>2</sub> in mortar and pestle and gently grinding for 3 min. The mixture was then transferred into the ball mill and ground at 600 rpm for 1 h. The samples obtained ranged from pale yellow (low *x*) to red orange (high *x*), Figure **1a**. Precipitation synthesis: Az<sub>1-x</sub>FA<sub>x</sub>PbBr<sub>3</sub> samples were prepared by mixing appropriate molar ratios of AzBr and FABr with PbBr<sub>2</sub> in DMF/DMSO (4:1, 2.5 mL, 0.4 M) solution at room temperature and in air. After stirring for 1 h, clear solutions were obtained. 20 mL acetonitrile was added slowly into the solution and the solution was shaken for 3 min and then left to stand for 15 min before filtration. The resulting powders were washed with 10 mL acetonitrile twice and dried in vacuum for 24 h. The samples obtained ranged from pale yellow (low *x*) to red orange (high *x*), Figure **1b**.

*Az<sub>1-x</sub>MA<sub>x</sub>PbBr<sub>3</sub>* ( $0 \leq x \leq 1$ ). Mechano-synthesis: Az<sub>1-x</sub>MA<sub>x</sub>PbBr<sub>3</sub> were prepared by mixing appropriate molar ratios of vacuum dried AzBr and MABr with PbBr<sub>2</sub> in the ball mill and ground at 600 rpm for 1 h. Precipitation synthesis: Az<sub>1-x</sub>MA<sub>x</sub>PbBr<sub>3</sub> is adapted from the literature.<sup>21</sup>

*MA<sub>1-x</sub>FA<sub>x</sub>PbBr<sub>3</sub>* ( $0 \leq x \leq 1$ ). Mechano-synthesis: MA<sub>1-x</sub>FA<sub>x</sub>PbBr<sub>3</sub> samples were prepared by mixing appropriate molar ratios of vacuum dried MABr and FABr with PbBr<sub>2</sub> in the ball mill and ground at 600 rpm for 1 h. Precipitation synthesis: MA<sub>1-x</sub>FA<sub>x</sub>PbBr<sub>3</sub> ( $0 \leq x \leq 1$ ) samples were prepared by mixing appropriate molar ratios of MABr and FABr with PbBr<sub>2</sub> in DMF solution at room

temperature. After stirring for 1 h, clear solutions were obtained. 20 mL acetonitrile was added slowly into the solution and the solution was left to stand for 15 min before filtration. The resulting powders were washed with 10 mL acetonitrile twice and dried in vacuum for 24 h. The samples obtained are red orange.

**Powder X-ray diffraction.** Powder XRD (PXRD) was carried out either using a PANalytical Empyrean diffractometer with Cu K $\alpha_1$  ( $\lambda = 1.5406 \text{ \AA}$ ).

**Rietveld refinements.** Rietveld refinements of PXRD data, using the General Structure Analysis System (GSAS)<sup>39</sup> software, were used to confirm phase formation and for determination of lattice parameters.

**Optical Spectroscopy.** Solid-state absorption spectra were recorded using a JASCO-V650 double beam spectrophotometer and the bandgap was determined using the 'Band-Gap Calculation' program of the spectrophotometer which applies the Tauc method.

**Scanning Electron Microscope (SEM).** A Jeol JSM-5600 Scanning Electron Microscope was used to obtain images of samples and accelerating voltage set at 5 kV.

**Nuclear magnetic resonance (NMR).**  $^1\text{H}$  and  $^{13}\text{C}$  NMR spectra were recorded on a Bruker Advance spectrometer (400 MHz for  $^1\text{H}$ , 101 MHz for  $^{13}\text{C}$ ).  $^1\text{H}$  and  $^{13}\text{C}$  NMR spectra were referenced to residual solvent peaks with respect to TMS ( $\delta = 0 \text{ ppm}$ ).

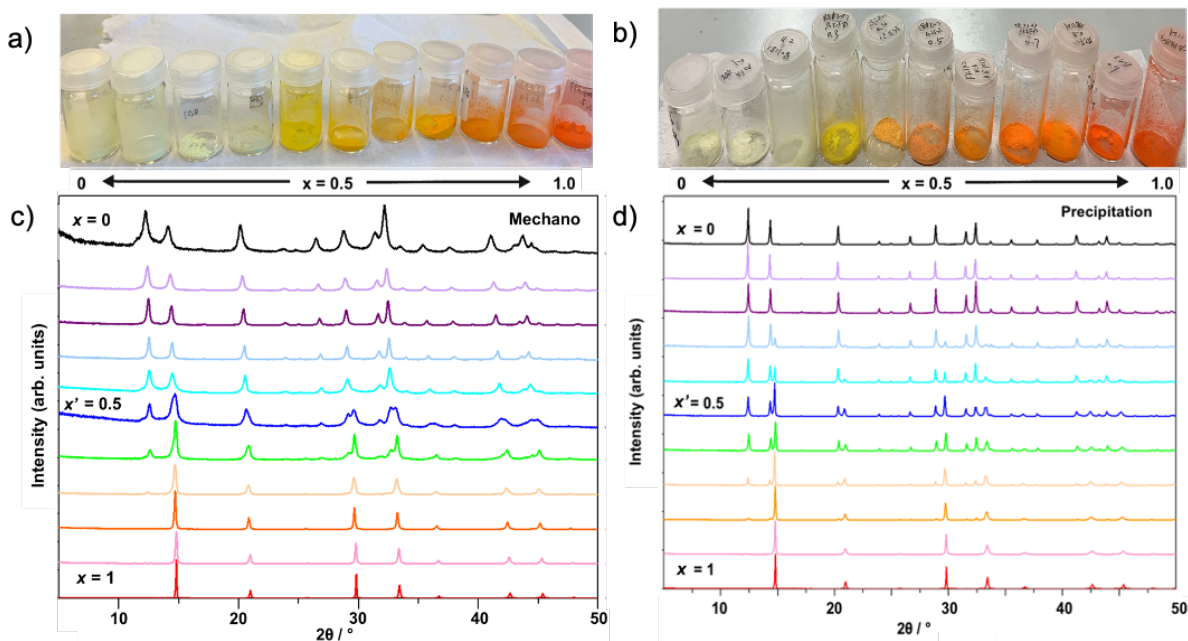
## Results and Discussion

For mechanosynthesis, samples of  $\text{Az}_{1-x}\text{FA}_x\text{PbBr}_3$  ( $0 \leq x \leq 1$ ) were prepared by mixing appropriate molar ratios of AzBr and FABr with  $\text{PbBr}_2$  with a mortar and pestle and the mixture was then transferred into the ball mill and ground at 600 rpm for 1 hour. For the antisolvent precipitation synthesis, samples of  $\text{Az}_{1-x}\text{FA}_x\text{PbBr}_3$  were prepared by mixing appropriate molar ratios of AzBr and FABr with  $\text{PbBr}_2$  in a DMF/DMSO (4:1) solution. Acetonitrile was slowly added to the reaction mixture and the resulting precipitate was collected by filtration. Detailed procedures are given in the Supporting Information. The SEM of the single phase  $\text{AzPbBr}_3$  and  $\text{FAPbBr}_3$  samples obtained from both syntheses are shown in Figure S1. As expected, the particle size of precipitation-synthesized samples is larger than that of mechanosynthesized ones. During the

precipitation synthesis, gradual addition of the antisolvent produced a noticeable change in color of the precipitate. Initially, the color of the precipitate was closer to the color of the perovskite with the richer cation source, ( $\text{AZPbBr}_3$  is pale yellow and  $\text{FAPbBr}_3$  is red-orange) and in later stages of precipitation, the color of the precipitate appeared to be midway between the pale yellow and red-orange colors of the end member compositions. The observation of color progression is difficult during grinding due to the opaque chamber of the ball mill. However, the progress of mechanosynthesis of one sample ( $\text{AZ}_{0.5}\text{FA}_{0.5}\text{PbBr}_3$ ) was tracked by periodic interruption of the grinding process – the color was orange in the early stage of mechanosynthesis and bright yellow in the late stage of grinding (Figure S2). The systematic color change with composition of samples from both synthetic routes is shown in Figures 1a and 1b. Empirically, the transition from yellow to red-orange was observed at a smaller nominal composition ( $x' = 0.4$ ) for the precipitation samples than mechanosynthesized ones ( $x' = 0.6$ ); here,  $x'$  and  $x$  is used to represent the nominal and actual  $\text{FA}^+$  composition in the mixed cation perovskite, respectively.

Comparison of the PXRD data between mechano- and precipitation syntheses is shown in Figures 1c and 1d. Regions of solid solution formation (single phase regions) separated by a region of two-phase mixture at intermediate  $x'$  can be identified for both syntheses on  $\text{AZ}_{1-x'}\text{FA}_{x'}\text{PbBr}_3$ , but the extent of solid solution formation is different. The PXRD of the mechanosynthesized samples indicates that for  $x' \leq 0.4$  only peaks associated with the 6H polytype are observed, and for  $x' \geq 0.7$  only the 3C phase is present, while at intermediate  $x'$  values the PXRD indicates a two-phase mixture. The PXRD of the precipitation synthesis samples shows less extensive solid solutions, where for  $x' \leq 0.2$  or for  $x' \geq 0.8$  only the 6H or 3C polytypes were observed, in comparison to the previously reported  $\text{AZ}_{1-x}\text{MA}_x\text{PbBr}_3$  solid solution.<sup>21</sup> To ensure all starting materials were consumed during the grinding synthesis, one sample ( $\text{AZ}_{0.4}\text{FA}_{0.6}\text{PbBr}_3$ ) in the two-phase solid solution region was reground for an additional hour. The PXRD of the starting materials and samples before and after regrinding are shown in Figure S3. No trace of starting materials, nor change in lattice parameters are observed in samples before and after regrinding. The PXRD peaks for  $\text{AZ}_{1-x'}\text{FA}_{x'}\text{PbBr}_3$  prepared by mechanosynthesis are generally wider than that of the precipitation synthesis, presumably due to the smaller crystallite size. The crystallite size of the 6H phase in the Az-rich mixture was estimated from the Scherrer equation<sup>40</sup> (Table S1). The crystallite size of the 6H phase from the precipitation synthesis is more than twice as large as that from mechanosynthesis, which was confirmed by SEM (Figure S4). However, the crystallite size

of 3C phase was hard to determine, especially in the phase mixture region, due to the presence of overlapping major peaks from the 6H phase. The crystallite size of  $\text{FAPbBr}_3$  from the precipitation synthesis was estimated visually to be slightly larger than that from the mechanosynthesis, which is in agreement with the SEM images in Figure S1.

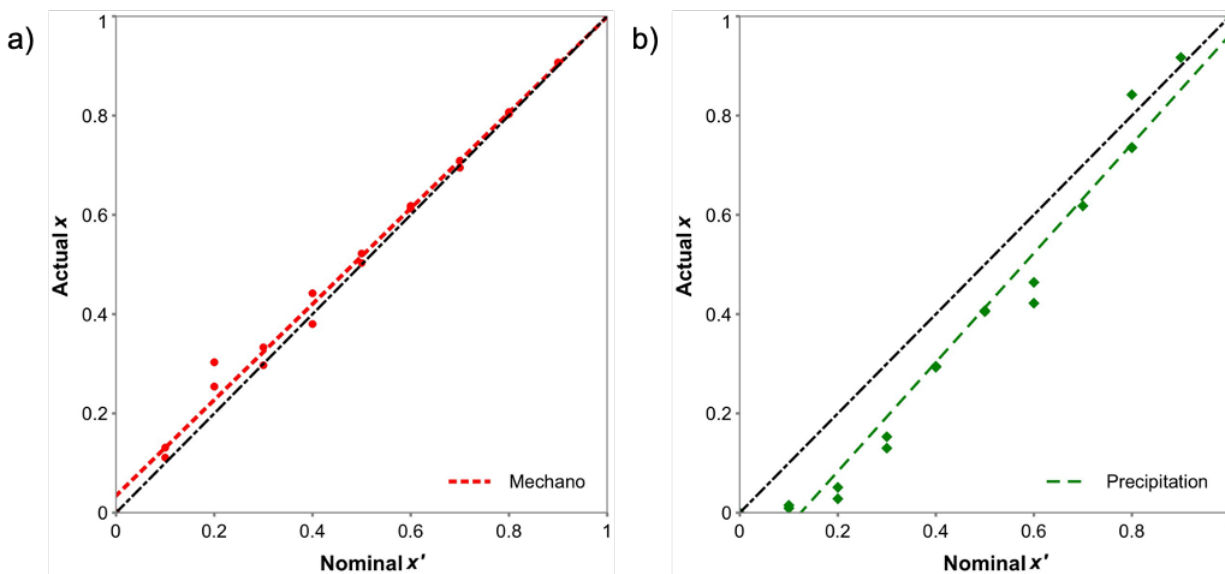


**Figure 1.** Photos and PXRD data of powders of  $\text{AZ}_{1-x}\text{FA}_x\text{PbBr}_3$  with nominal composition  $0 \leq x' \leq 1$  (in  $x' = 0.1$  increments) prepared by (a, c) mechanosynthesis and (b, d) precipitation synthesis.

Using *o*-dichlorobenzene as an internal standard, solution-state  $^1\text{H}$  NMR analysis (Figure S5) was carried out on the as-synthesized samples to determine the actual  $\text{FA}^+$  composition,  $x$ , and compare it with nominal  $x'$ , in  $\text{AZ}_{1-x}\text{FA}_x\text{PbBr}_3$  prepared by both syntheses routes. The comparison between actual  $x$  and nominal  $x'$  is shown in Figure 2. As expected, the actual  $x$  obtained by  $^1\text{H}$  NMR closely matches with nominal  $x'$  in the mechanosynthesis samples as all starting materials are retained during the ball milling reaction. To ensure that this analysis represented the as-synthesized perovskite,  $^1\text{H}$  NMR analysis of both the isolated bulk powder and the residue left in the ball mill was carried out, with both samples revealing similar compositions (Table S2). By contrast, the  $^1\text{H}$  NMR analysis of samples from the precipitation synthesis indicated that the actual FA content ( $x$ ) is consistently lower than the nominal value in the precursor solution ( $x'$ ). The cation composition mismatch is apparent for  $x' < 0.6$ , which suggests the mixed cation perovskite precipitation is



affected by the relative cation concentration of the precursor solution. Possible reasons for this are discussed below.



**Figure 2.** The comparison of nominal ( $x'$ ) and actual ( $x$ )  $\text{FA}^+$  cation content determined by  $^1\text{H}$  NMR analysis on  $\text{AZ}_{1-x}\text{FA}_x\text{PbBr}_3$  samples prepared by a) mechano-synthesis and b) precipitation synthesis. Dash lines are linear fit to the actual values and black dot-dash lines indicate the instance for  $x = x'$  composition for comparison.

Rietveld refinement of the PXRD data of samples from both syntheses was carried out to study the phase mixture and the solid solution regions; an example of such a refinement is shown in Figure S6. The weight fraction of both 6H and 3C phase was determined from the refinements and are shown in terms of mol fraction *versus* actual  $x$  (obtained by  $^1\text{H}$  NMR analysis) in Figures 3a and 3b. For samples obtained by mechano-synthesis, an intermediate two-phase region appears for  $0.42 \leq x \leq 0.79$ . This contrasts with samples obtained from the precipitation synthesis, where the region is a much larger  $0.10 \leq x \leq 0.94$ . A rise in temperature of the milling beaker was observed and thus the temperature inside the beaker was measured with a hand-held pyrometer immediately after the grinding. The temperature was found to be  $50.4 \pm 3.9$  °C. It is possible that the increase in temperature could provide sufficient thermal energy to aid  $\text{FA}^+$  and  $\text{Az}^+$  diffusion into 6H and 3C phases during grinding. The observation of the precipitate color change mentioned in the beginning of discussion section, on the other hand, indicates that the precipitation of 6H and 3C phases tend to progress at different rates, which is related to their cation concentration in the precursor solution.

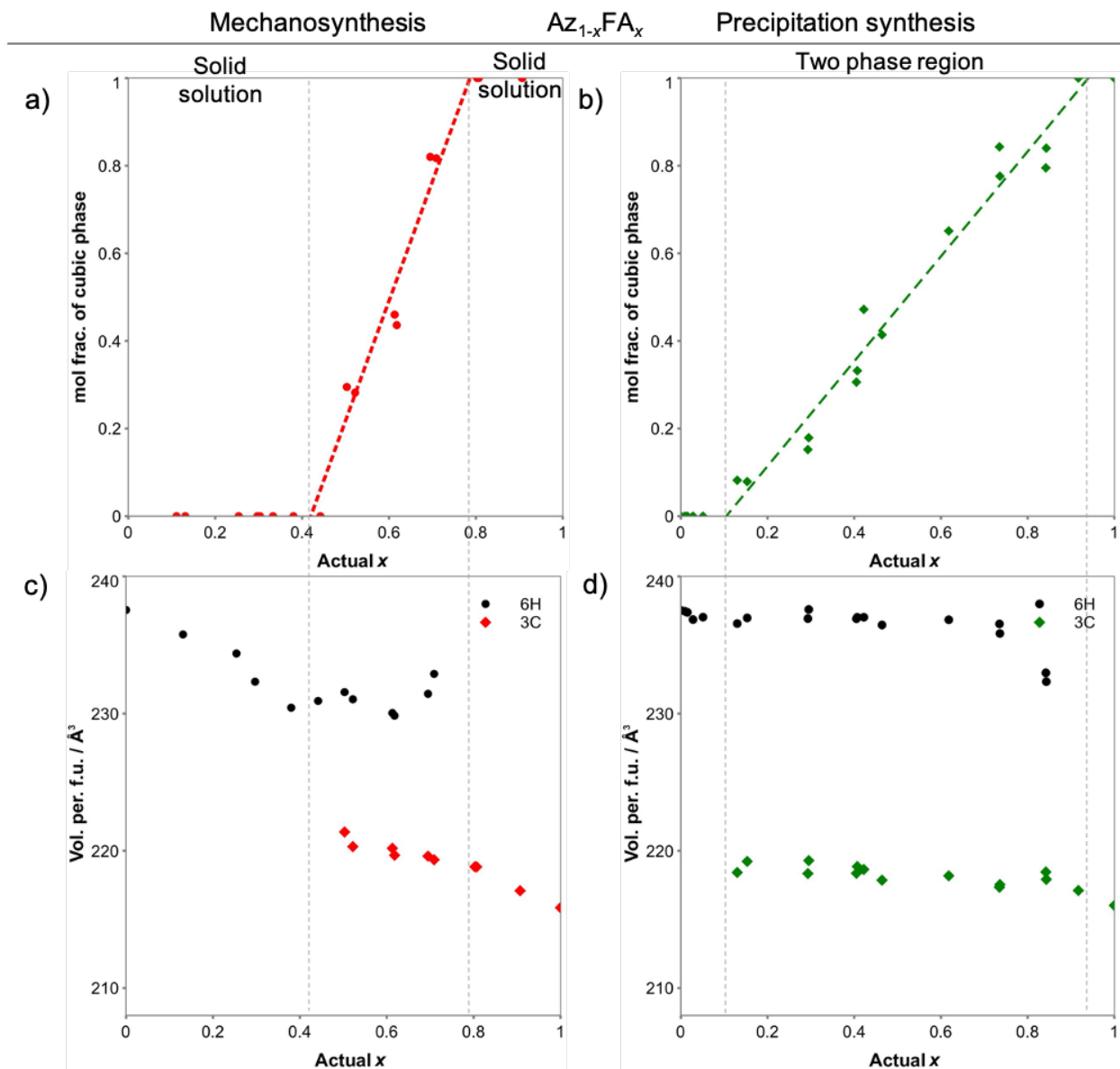
To investigate the stoichiometry of the A-cation of samples along precipitation progression, a stepwise antisolvent addition experiment was performed (experimental details in Supporting Information). Based on the observed color change during precipitation, the initial assumption was that the 6H phase precipitates first and the 3C phase follows with increasing volume of antisolvent. The actual  $x$  obtained by  $^1\text{H}$  NMR analysis (Table S2) of the precipitated samples shows that they are deficient in  $\text{FA}^+$  in the early stages of addition of the antisolvent. The incorporation of such a small amount (ca. 6%) of  $\text{FA}^+$  in the early stages of precipitation is evident from the color of the powders, which appeared close in color to  $\text{AzPbBr}_3$  (Figure S7). Similarly, there is no 3C phase detected by PXRD in these precipitated samples, the actual  $x$  of which is less than 0.07. This result is consistent with the solid solution/two phase regions indicated in Figure 3. These step-wise antisolvent experiments show that the 6H phase is more likely to precipitate first with antisolvent present under a similar cation concentration, while the 3C phase only precipitates with lower  $\text{Az}^+$  cation concentrations. This kinetic difference accounts for composition mismatch found in Figure 2b and the small solid solution region observed in  $\text{AZ}_{1-x}\text{FA}_x\text{PbBr}_3$  samples obtained by precipitation.

In our mixed-cation system  $\text{AZ}_{1-x}\text{FA}_x\text{PbBr}_3$ , a complete solid solution is impossible as the end members are not isostructural (6H and 3C perovskite), although partial solid solutions may form at either end given the similar A-cation size. In the single phase (solid solution) regions (as determined by PXRD, Figures 3c and 3d), the actual  $x$  values as determined from  $^1\text{H}$  NMR analysis correspond to the actual  $\text{FA}^+$  composition of the solid solution. A more conventional expression of the solid solution general formula is needed as  $\text{AZ}_{1-y}\text{FA}_y\text{PbBr}_3$  (6H, Az-rich) and  $\text{AZ}_z\text{FA}_{1-z}\text{PbBr}_3$  (3C, FA-rich), where  $y$  and  $z$  denote the degree of substitution of FA and Az at the A-site from the parent structure. This also allows us to distinguish them from  $\text{AZ}_{1-x}\text{FA}_x\text{PbBr}_3$  especially for mixed phase samples; in the two-phase region,  $x$  corresponds to the global FA content with an unknown distribution over the two phases.

The lattice parameters of each polytype as a function of  $x$  were determined by Rietveld refinement, including two-phase refinement for intermediate  $x$ . The cell volume (Figure 3c and d) of  $\text{AZ}_{1-x}\text{FA}_x\text{PbBr}_3$  as a function of composition shows a close resemblance to the reported  $\text{BaTiO}_3$ – $\text{CaTiO}_3$  solid solution<sup>41</sup> system, in which the lattice parameter progression shifted from decreasing to invariant as the composition extends from the single phase region into the two-phase region. In

the single phase 6H solid solution region, the lattice constant and cell volume show a systematic decrease with increasing FA content. This is more evident in samples obtained via mechanosynthesis. For the 3C region of those samples, the solid solution shows an increase in cell volume with increasing Az content. These volume-composition dependencies suggest that  $\text{FA}^+$  is smaller than  $\text{Az}^+$  in contrast to computational studies which suggest they are very similar (actually FA marginally larger).<sup>36,42</sup> The suggestion that  $\text{FA}^+$  is smaller than  $\text{Az}^+$  is also consistent with the experimental results that  $\text{AzPbBr}_3$  forms a 6H structure and  $\text{FAPbBr}_3$  forms a cubic structure while their tolerance factors, using computed cation sizes, are both 1.00. However, the size effect of organic cations in extended structures is largely based on a hard sphere approximation, which implies their free rotation. This may not be true for either  $\text{FA}^+$  or  $\text{Az}^+$  in these structures at room temperature and requires more study.

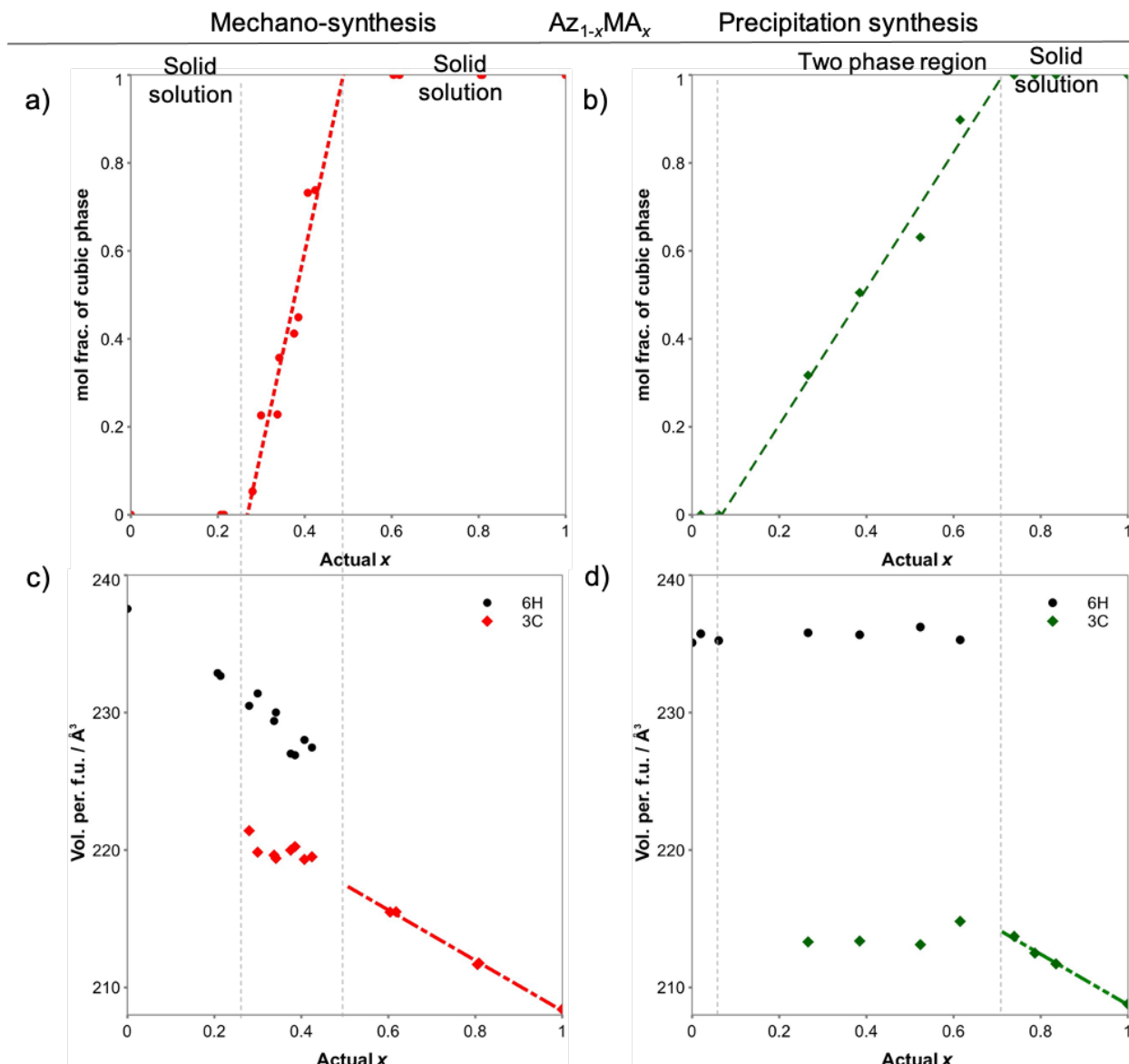
For samples obtained from the precipitation synthesis, the cell volume in the Az-rich region is invariant as a function of  $x$ , which suggests a relatively small degree of substitution by FA when compared to mechanosynthesised samples of the same composition. Presumably, this is due to the phase separation between 3C and 6H phases during the precipitation as a result of the different precipitation rates. The sharp decrease of the volume at  $x = 0.84$  is possibly due to the error of the refinement as the fraction of the 6H phase in these samples is very low. For precipitation synthesized samples in FA-rich region, the slight increase in cell volume indicates a relatively small degree of substitution by Az. Overall, there is limited solid solution formation during the precipitation synthesis.



**Figure 3.** Mole fraction and cell volume (per formula unit) of hexagonal (6H) and cubic (3C) perovskite phases as determined by Rietveld refinement of PXRD data for  $Az_{1-x}FA_xPbBr_3$  samples prepared by mechano- (a, c) and precipitation synthesis (b, d). Values are shown as a function of overall, actual  $x$  as determined by NMR. The vertical dashed lines indicate the boundaries between the single phase solid solution and intermediate two-phase regions.

To further study the competitive solid solution formation, we applied similar synthesis protocols to the  $Az_{1-x}MA_xPbBr_3$  and  $MA_{1-x}FA_xPbBr_3$  systems ( $0 \leq x \leq 1$ ). The compositional analysis of  $Az_{1-x}$

$x\text{MA}_x\text{PbBr}_3$  reveals a similar result to the  $\text{AZ}_{1-x}\text{FA}_x$  system (Figure S8), where (actual)  $x \approx$  (nominal)  $x'$  for the mechano-synthesis and  $x < x'$  for the precipitation synthesis.  $\text{MA}_{1-x}\text{FA}_x\text{PbBr}_3$ , by contrast, shows  $x \approx x'$  for both synthetic routes and Rietveld refinement of PXRD data shows that the cell volume varies linearly as a function of actual  $x$  (Figure S9). The data for the precipitation synthesis of  $\text{AZ}_{1-x}\text{MA}_x\text{PbBr}_3$  was taken from our previous study,<sup>21</sup> but this time replotted based on actual  $x$ , as determined by  $^1\text{H}$  NMR analysis. Rietveld refinements for the  $\text{AZ}_{1-x}\text{MA}_x$  system shows the presence of limited solid solutions of composition  $\text{AZ}_{1-y}\text{MA}_y\text{PbBr}_3$  (6H) and  $\text{AZ}_z\text{MA}_{1-z}\text{PbBr}_3$  (3C) for both syntheses (Figure 4). For samples obtained from the mechano-synthesis, an intermediate two-phase region appears for  $0.27 \leq x \leq 0.49$ , compared to precipitation synthesized samples, where the two-phase region is larger ( $0.07 \leq x \leq 0.71$ ). The cell volume expansion as a function of increasing Az content (fitted lines) in the 3C solid solution region is similar for both mechano- and precipitation syntheses.



**Figure 4.** Mole fraction and cell volume (per formula unit) of hexagonal (6H) and cubic (3C) perovskite phases as determined by Rietveld refinement of PXRD data for  $Az_{1-x}MA_xPbBr_3$  samples prepared by mechano- (a, c) and precipitation synthesis (b, d). Values are shown as a function of (overall) actual  $x$  as determined by NMR. The vertical dashed lines indicate the boundaries between the single-phase solid solution and intermediate two-phase regions. The dash-dot lines and dash-dot-dot lines are linear fits to the cell volume as a function of actual  $x$  for mechano- and precipitation samples, respectively in the 3C solid solution region.

The solid solution ranges of the  $Az_{1-x}MA_x$  and  $Az_{1-x}FA_x$  systems are included in Table 1. Our experimental results suggest that the size of  $Az^+$  is larger than that of  $FA^+$ , and both cations are larger than  $MA^+$ . The relative size relationship between  $FA^+$  and  $MA^+$  can be confirmed from the lattice parameters of the reported (cubic)  $FAPbBr_3$  and  $MAPbBr_3$ , where  $a(FAPbBr_3) = 5.98 \text{ \AA}$  and  $a(MAPbBr_3) = 5.92 \text{ \AA}$ .<sup>21,43</sup> In oxide perovskites, it is generally acknowledged that solid solution formation follows Hume–Rothery rules,<sup>44</sup> which describe the empirical observation that the size difference between the solute and solvent atoms should be within 15% for substitutional solid solutions. This is because too large a size mismatch generates local strain. In the (Ba, Sr, Ca)TiO<sub>3</sub> system, for example, all three end members form (pseudo-)cubic perovskites. The cation radii for  $Ba^{2+}$ ,  $Sr^{2+}$  and  $Ca^{2+}$  are 1.61, 1.44 and 1.34 Å, respectively<sup>45</sup>, and complete solid solutions form for  $Ba_{1-x}Sr_xTiO_3$  and  $Sr_{1-x}Ca_xTiO_3$ , indicating this full range of A-cation size can be accommodated in the crystal structure (the average A-cation size varies continuously across the combined solid solutions). However, for  $Ba_{1-x}Ca_xTiO_3$  only < 30% Ca substitution can be tolerated due to the large size mismatch and resulting local strain.<sup>46–49</sup> By analogy, it would be expected to be easier for relatively larger  $Az^+$  to replace the cations in the larger A-site interspace in  $FAPbBr_3$  than  $MAPbBr_3$  independent of the synthetic method and for a more extensive solid solution to form. However, the observations here are contrary to this notion: for mechano-synthesis of the 3C solid solutions, in  $Az_zFA_{1-z}PbBr_3$ , the degree of Az substitution extends to  $z = 0.21$ , compared to  $z = 0.51$  for  $Az_zMA_{1-z}PbBr_3$ . (Precipitation synthesized samples show similar results where the solid solution range of  $Az_zFA_{1-z}PbBr_3$  is smaller than that of  $Az_zMA_{1-z}PbBr_3$ , but this observation does not take into account any possible kinetically limited aspects). A possible explanation for this observation is that the extent of solid solution formation observed here is dependent only on the global average A-cation size and that local strain due to size mismatch plays a less significant role. In other words, mixed A-cation halide perovskite would not tolerate the single phase 3C solid solution if the average A-cation size is larger than a certain value. This can be estimated by examining the maximum unit cell volume of the 3C phase in each system (Figure S10a). Under the assumption that Vegard’s law holds for these solid solutions, a linear relationship between the average A-cation radius and cell volume can be fitted to the results from  $MA_{1-x}FA_xPbBr_3$  samples with  $r_{FA} = 253 \text{ pm}$  and  $r_{MA} = 217 \text{ pm}$  (Figure S10b).<sup>36</sup> By extrapolation, the cation radius of Az is estimated to be  $315 \pm 11 \text{ pm}$  (from  $Az_{1-x}FA_x$  data) or  $304 \pm 6 \text{ pm}$  (from  $Az_{1-x}MA_x$  data). These somewhat crude estimations for the  $Az^+$  cation radius are significantly larger than the computed

cation radius ( $r_{Az} = 250$  pm) reported by Kieslich *et al.*<sup>36</sup> and clearly requires further study. The tolerance factor of  $AzPbBr_3$  calculated with  $r_{Az} = 310$  pm (average of the two values above) is 1.14, which is in agreement with the fact that it forms 6H hexagonal structure rather than cubic.<sup>21</sup> The reason behind the differing influence of local strain (size mis-match) on the extent of solid solution formation between oxide and halide perovskites might result from the strong M-O bonds and resulting rigid framework in comparison to the M-X framework in halides. The Young's moduli of halide perovskites are of the order 10 – 20 GPa (for  $MAPbX_3$ , X = Cl, Br, I),<sup>50</sup> which are approximately an order of magnitude lower than for oxide perovskites (> 100 GPa).<sup>51</sup>

The 6H solid solution ranges described by  $Az_{1-y}FA_yPbBr_3$  and  $Az_{1-y}MA_yPbBr_3$  are both extremely limited in the precipitation synthesized samples. For the mechano-synthesized 6H solid solution,  $Az_{1-y}FA_yPbBr_3$ , the degree of FA substitution extends to  $y \leq 0.42$  and to  $y \leq 0.27$  for  $Az_{1-y}MA_yPbBr_3$ , which are consistent with size predictions. In other words, the replacement of  $Az^+$  in the 6H-structured solid solutions favors the cation of similar size ( $FA^+$ ) than the smaller cation ( $MA^+$ ).

Annealing is reported to be a common method in perovskite device fabrication, which initiates and accelerates perovskite formation, removes residual solvent, and improves crystal growth.<sup>52</sup> These benefits result from interdiffusion and reorganization induced by the temperature. Samples in the two-phase region obtained by both mechano- and precipitation syntheses were kept in 100 °C (a commonly used annealing temperature<sup>7,52</sup>) for 5 hours. These heated samples were analyzed by <sup>1</sup>H NMR and PXRD and the results are shown in Figure S11. The composition (actual  $x$ ), phase fraction and lattice parameters of mechano-synthesized  $AzFA$  and  $AzMA$  perovskite samples in the two-phase region showed no significant change after heating. Similarly, the actual  $x$ , phase fraction and lattice parameters of the corresponding precipitation synthesized  $AzFA$ - and  $AzMA$ -containing perovskite samples did not vary (within error). Presumably, these perovskite samples are stable at 100 °C and no interdiffusion was observed after 5 hours of heating.

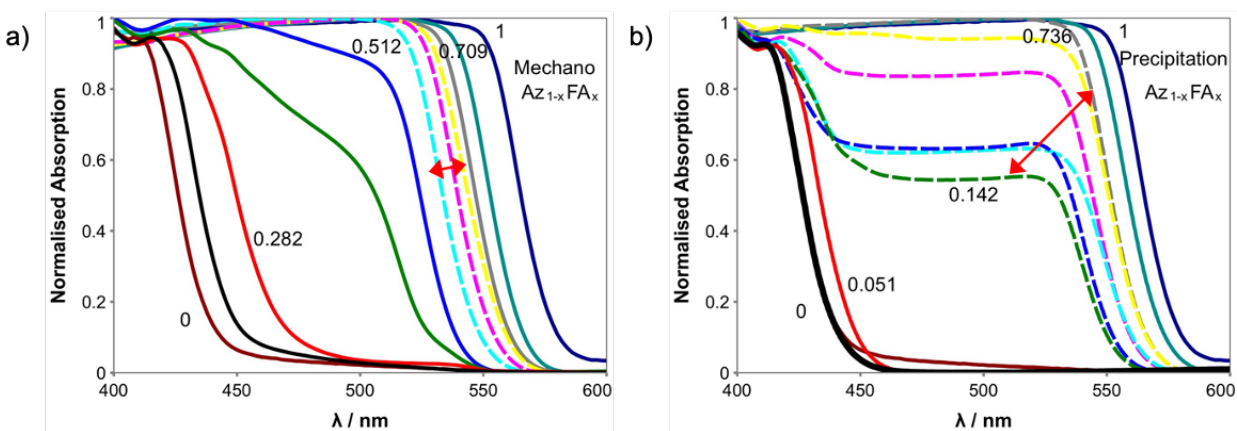


Table 1. Solid solution ranges for  $Az_{1-x}MA_x$  and  $Az_{1-x}FA_x$  samples prepared by mechano- and precipitation syntheses.

	Solid solution range	Mechano-synthesis	Precipitation synthesis
6H	$Az_{1-y}FA_yPbBr_3$	$y \leq 0.42$	$y \leq 0.10$
	$Az_{1-y}MA_yPbBr_3$	$y \leq 0.27$	$y \leq 0.07$
3C	$Az_zFA_{1-z}PbBr_3$	$z \leq 0.21$	$z \leq 0.06$
	$Az_zMA_{1-z}PbBr_3$	$z \leq 0.51$	$z \leq 0.29$

The optical properties of the solid solutions/two-phase mixtures of  $Az_{1-x}FA_xPbBr_3$  samples were studied by absorption spectroscopy (Figure 5). The absorption onsets are systematically red-shifted with increasing  $FA^+$ , regardless of how the samples were synthesized. Optical measurements indicate that the absorption edge for the 6H solid solution samples obtained from the mechanosynthesis is red-shifted from *ca.* 440 nm ( $AzPbBr_3$ ) to *ca.* 540 nm ( $y = 0.38$ ). The absorption edge of  $Az_{0.62}FA_{0.38}PbBr_3$  is relatively close to that of  $FAPbBr_3$  (585 nm). As the solid-state absorption spectra is surface sensitive, the shifted absorption edge at such composition may be due to the presence of some 3C crystallites formed at the surface, the amount of which is insufficient to be detected by PXRD. Moreover, the absorption edge for the 6H solid solution samples obtained from the precipitation synthesis remains invariant at *ca.* 440 nm ( $0 \leq y \leq 0.051$ ). By contrast, the 3C solid solution from both syntheses shows a blue-shift from *ca.* 585 nm ( $FAPbBr_3$ ) to *ca.* 565 nm ( $z = 0.20$ , mechanosynthesis) and *ca.* 576 nm ( $z = 0.08$ , precipitation synthesis), respectively. In the two-phase region ( $0.10 \leq x \leq 0.94$ ) of the precipitation-synthesized samples, the low volume fraction of the 6H phase for  $0.62 \leq x \leq 0.74$  (Figure 2b) means that the absorption is dominated by the 3C component and the absorption edge remains around 560 nm. For the  $0.14 \leq x < 0.62$  compositions, which have a significant phase fraction of both 6H and 3C, two absorption edges were observed corresponding to each phase (6H  $\sim$ 470 nm; 3C  $\sim$ 560 nm). The absorption spectra of the corresponding  $Az_{1-x}MA_x$  samples are shown in Figure S12 as a comparison, and show a similar absorption edge shift as a function of  $x$ .

The band gap values calculated from the onset of the absorption spectra from both  $Az_{1-x}FA_x$  and  $Az_{1-x}MA_x$  samples are shown in Figure S13. The bandgap of the  $Az_{1-x}FA_x$  samples in the 6H solid solution region shows a nonlinear character, which can be rationalized in terms of the bowing effect,<sup>41,53</sup> where a lower bandgap was attained for the intermediate composition of solid solutions than expected from linear interpolation of the end member values. The bandgap of the 3C solid solution and two-phase region samples show a progressive increase with increasing Az content (decreasing  $x$ ). This trend is due to the unit cell expansion as a result of elongation of the Pb-Br bond, as discussed in our previous study.<sup>21</sup>



**Figure 5.** Absorption spectra of  $Az_{1-x}FA_xPbBr_3$  samples prepared by a) mechano-synthesis b) precipitation synthesis. Spectra from single phase (solid solution) compositions as determined by PXRD are plotted with solid lines and multi-phase samples with dashed lines.

## Conclusions

Solid solution formation in the system  $Az_{1-x}FA_xPbBr_3$  ( $0 \leq x \leq 1$ ) was explored using both mechano- and precipitation syntheses. For samples obtained from precipitation synthesis, the actual FA% in the precipitate was found to be less than the nominal composition in the reaction solution as a result of different precipitation rates of 3C and 6H perovskite polytypes. No such composition mismatch was found for mechano-synthesized samples. A 3C-6H two phase region was found to be present for  $0.42 \leq x \leq 0.79$  and  $0.10 \leq x \leq 0.94$ , for mechano- and precipitation synthesis of  $Az_{1-x}FA_xPbBr_3$ , respectively. The cell volume dependence on the composition (volume increases with increasing  $Az^+$  content) in both 6H (Az-rich) and 3C (FA-rich) solid

solution regions suggests the  $Az^+$  cation is actually larger than  $FA^+$ , which is incongruent to the cation size reported in the literature.<sup>36,42</sup> Under the assumption of Vegard's law, the cation radius of  $Az^+$  is estimated to be  $\sim 310$  pm and therefore the tolerance factor of  $AzPbBr_3$  is 1.14, which is in consistent with the fact that it forms a 6H hexagonal perovskite rather than a cubic perovskite.<sup>21</sup> By comparison, in the 3C solid solution regions (Az-poor), the solid solution range in  $Az_zFA_{1-z}PbBr_3$  is surprisingly smaller than in  $Az_zMA_{1-z}PbBr_3$ , given that  $MA^+$  is much smaller than  $FA^+$ . This suggests that the extent of the single-phase solid solution of halide perovskites is dependent only on the average A-cation size, while the size mismatch is less of an influence, in contrast to solid solution formation observed in oxide perovskites. Overall, our study reveals the importance of cross-checking the nominal (reaction) with the actual (product) composition, especially when the synthetic method may be under kinetic control or multi phases can be formed in the system. While doping larger A-site organic cations in OIHPs, the average A-cation radius can be used as a guide to prevent unwanted phase separation. The computed size of organic cations and the presence of any dynamic/preferential bonding effects should be re-examined and considered during study of organic-inorganic hybrid perovskite systems.

Associated content

### **Supporting Information**

The Supporting Information contains Experimental details, SEM, details of  $^1H$  NMR analysis, examples of Rietveld refinement and absorption spectra. The research data supporting this publication can be accessed at [].

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