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# Stratospheric Gravity Waves as a Proxy for Hurricane Intensification: a Case Study of WRF Simulation for Hurricane Joaquin

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## Key Points:

- High-resolution WRF simulations for Hurricane Joaquin show spiral gravity waves (GWs) emanating into the stratosphere.
- Stratospheric GW activity is more frequent and intense before and during hurricane intensification than during weakening.
- This study provides further evidence that stratospheric GW activity is a valid proxy for hurricane intensification.

## Abstract

We conducted simulations with a 4-km resolution for Hurricane Joaquin in 2015 using the Weather Research and Forecast (WRF) model. The model data are used to study stratospheric gravity waves (GWs) generated by the hurricane and how they correlate with hurricane intensity. The simulation results show spiral GWs propagating upward and anticlockwise away from the hurricane center. GWs with vertical wavelengths up to 14 km are generated. We find that GW activity is more frequent and intense during hurricane intensification than during weakening, particularly for the most intense GW activity. There are significant correlations between the change of stratospheric GW intensity and hurricane intensity. Therefore, the emergence of intensive stratospheric GW activity may be considered a useful proxy for identifying hurricane intensification.

## 35 **Plain Language Summary**

36 Accurate predictions of changes in hurricane intensity are essential to provide sufficient lead  
37 time for warning and evacuation. As a hurricane intensifies, gravity waves (GWs) are emitted  
38 into the stratosphere to partially rebalance the sudden energy changes. If a correlation between  
39 hurricane intensification and GWs is verified, observing stratospheric GWs with satellite  
40 instruments could provide a possible predictor of hurricane intensification. This approach is  
41 advantageous when clouds obscure the direct view from above by visible and infrared  
42 instruments into the inner state of the hurricane. This study uses mesoscale model simulations  
43 to test and verify the correlation between hurricane intensification and GWs and finds that  
44 stratospheric GW activity increases prior to peaks in hurricane intensity.

## 45 **1 Introduction**

46 Tropical cyclones (TCs) are among the most destructive natural weather phenomena  
47 and can cause extensive damage to coastal countries and regions. Close monitoring and  
48 accurate forecasts of the tracks and intensity of TCs are needed to reduce human and  
49 financial losses.

50 Tropical cyclones are powered by latent heating, mainly from strong updrafts in the  
51 eyewall (Charney and Eliassen, 1964; Emanuel, 1986; Kuo, 1965), and latent heat release in  
52 the storm is responsible for the dynamical structure and intensity change of the storm (Braun,  
53 2002; Cecil and Zipser, 1999). Latent heat release is also involved in generating stratospheric  
54 gravity waves (GWs) (Beres et al., 2004; Song and Chun, 2005; Kuester et al., 2008).  
55 Previous studies found a dependence of dominant phase speed and wavelengths of GWs on  
56 the depth of the latent heating in the troposphere (e.g., Alexander et al., 1995; Beres et al.,  
57 2002, 2004; Salby and Garcia, 1987). Thus, the spatial scale and temporal variation of  
58 heating rate determine the spectrum of GWs in the stratosphere (e.g., Alexander and Holton,  
59 2004; Holton et al., 2002; Nicholls et al., 1991; Stephan and Alexander, 2015). Ground-based  
60 and satellite observations, reanalysis data, and model simulations have been widely used to  
61 study the characteristics of stratospheric GWs generated by convective systems, particularly  
62 TCs (e.g., Chane-Ming et al., 2010, 2019; Chow et al., 2002; Kim and Chun, 2010; Miller et  
63 al., 2015; Nolan and Zhang, 2017; Wu et al., 2018; Yue et al., 2014), and confirmed that the  
64 characteristics of GWs vary significantly as the intensity of TCs changes.

65 Since stratospheric GW activity and TC intensity change are both driven by heating,  
66 recent works have suggested stratospheric GWs can be used as a proxy for intensity change  
67 (Hoffmann et al., 2018; Tratt et al., 2018). Model simulations have revealed that strong  
68 updrafts or convective bursts appear up to 3 h before TC intensification (Hazelton et al.,  
69 2017). GWs with long vertical wavelengths generated by the deep latent heat can propagate  
70 to the stratosphere in less than one hour (Fritts and Alexander, 2003; Yue et al., 2013, 2014),  
71 and this means that intensive stratospheric GW activity could be a predictor for TC  
72 intensification on short-term time scales. Using 13.5 years of Atmospheric Infrared Sounder  
73 (AIRS) observations of stratospheric GWs, Hoffmann et al. (2018) found a statistically robust  
74 correlation that more intensive stratospheric GWs are observed during the intensification of  
75 TCs than during weakening. Wright (2019) presented a study of TC-induced GWs using the  
76 Microwave Limb Sounder (MLS), the Sounding of the Atmosphere using Broadband

77 Emission Radiometry (SABER), and the High-Resolution Dynamics Limb Sounder  
78 (HIRDLs). Despite different GW spectrum ranges revealed by the sounders, Wright (2019)  
79 found a similar result that GW amplitudes steadily increase before TCs reaching peak  
80 intensity. However, these relationships require further verification due to the coarse time and  
81 space sampling of these satellite observations.

82 Following the work of Hoffmann et al. (2018), this study conducts realistic model  
83 simulations of stratospheric GWs generated by hurricane Joaquin in 2015 to verify the  
84 statistical correlation revealed by long-term satellite observations and to examine the  
85 possibility to use GW activity as a proxy of hurricane intensity change.

## 86 **2 Reanalysis and observational data**

### 87 **2.1 ERA5 reanalysis**

88 In this study, we use ERA5 reanalysis data (Hersbach et al., 2020) to provide initial  
89 and boundary conditions for the WRF simulation of Hurricane Joaquin. The ERA5 reanalysis  
90 is produced using the European Centre for Medium-Range Weather Forecasts (ECMWF) IFS  
91 Cycle 41r2 model with 4D-Var data assimilation and has a horizontal resolution of 31 km  
92 (TL639 spectral grid). The data are provided at 137 vertical hybrid sigma-pressure levels with  
93 the top level at 0.01 hPa (~80 km) as well as at the surface level. We retrieved hourly data at  
94  $0.25^\circ \times 0.25^\circ$  horizontal sampling and all model levels from the ECMWF data archive.  
95 Although tropical cyclone intensities are often underestimated in earlier reanalyses (Hodges  
96 et al., 2017), ERA5 better resolves mesoscale vertical motions both over the land and near the  
97 Intertropical Convergence Zone (ITCZ) (Hoffmann et al., 2019), which provides more  
98 accurate initial and boundary conditions for the simulations of hurricane intensity.

### 99 **2.2 Tropical cyclone track and intensity archive**

100 The International Best Track Archive for Climate Stewardship (IBTrACS) (Knapp et  
101 al., 2010) was used to evaluate the track and intensity of Hurricane Joaquin in our model  
102 simulations. The IBTrACS data were compiled from Regional Specialized Meteorological  
103 Centers within the World Meteorological Organization and other national agencies, which  
104 compile and archive TC track data individually. The IBTrACS data provides 3 to 6-hourly  
105 track and intensity estimates of hurricanes.

## 106 **3 WRF model configuration**

107 Successful reproduction of the TC track and intensity is crucial for simulating and  
108 evaluating the TC-induced GWs. A numerical simulation of Hurricane Joaquin was performed  
109 using the Weather Research and Forecasting (WRF) model version 3.9.1 (Skamarock et al.,  
110 2008). To adequately reproduce the rapid intensification phase of Hurricane Joaquin, it is  
111 necessary to conduct simulations with sufficient horizontal resolution. Horizontal resolutions  
112 coarser than 3–4 km may fail to represent the physical processes critical to TC intensity  
113 evolution (Gentry and Lackmann, 2010; Kim and Chun, 2010). In this study, the simulation  
114 used a concurrent one-way nested configuration that featured a fixed outer domain (D01) with  
115  $210 \times 105$  grid points and a vortex-following inner nested domain (D02) with  $201 \times 201$  grid  
116 points. The repositioning of D02 was calculated every 15 min. The grid spacings for D01 and

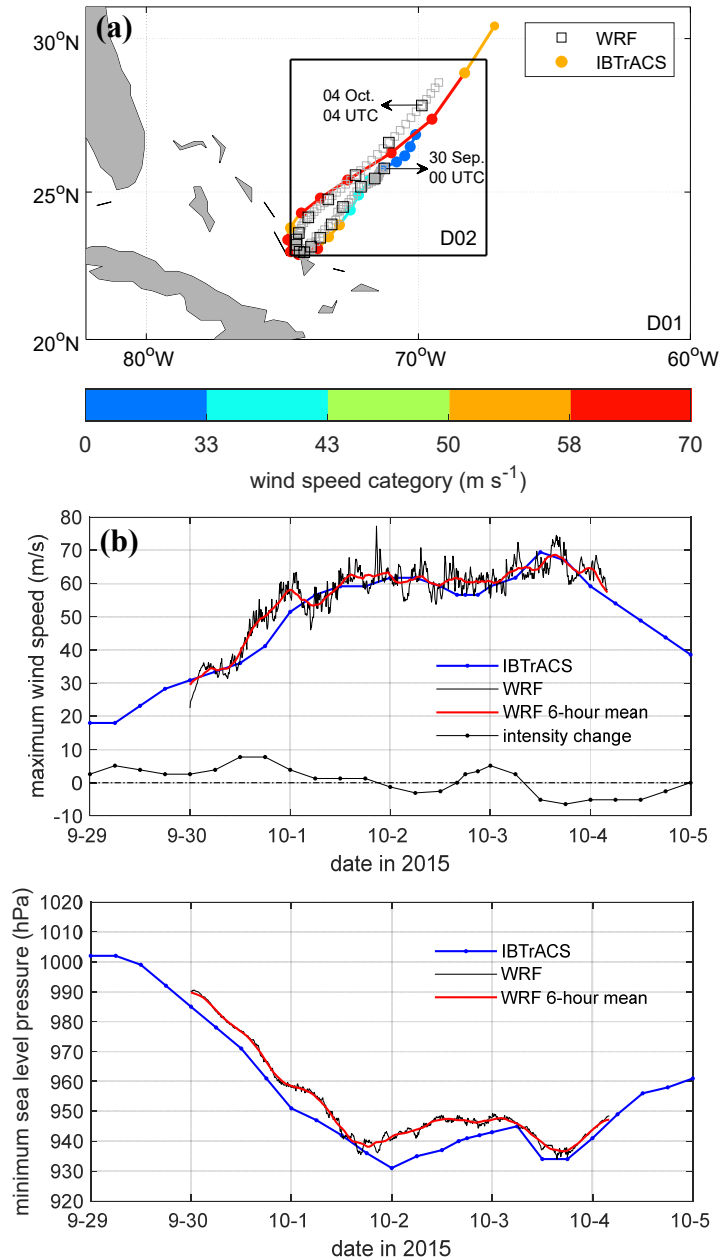
117 D02 are 12 and 4 km, and the time steps for D01 and D02 are 12 s and 4 s, respectively. A  
118 vertical domain with 90 sigma levels was set from the surface up to 1 hPa (~49 km), and the  
119 topmost 5 km was established as a damping layer. The vertical grid spacing was about 500 m in  
120 the stratosphere. The simulation spans 100 h from 00:00 UTC 30 September to 04:00 UTC 4  
121 October 2015, and simulation outputs were stored every 6 min.

122 Initial and boundary conditions were established using the ERA5 reanalysis data. For  
123 both domains, the Kain-Fritsch scheme (Kain, 2004) for cumulus parameterization, the WRF  
124 single moment 6-class scheme (Hong and Lim, 2006) for microphysics, the new version of  
125 rapid radiative transfer model scheme (Iacono et al., 2008) for longwave and shortwave  
126 radiation, and the Yonsei University planetary boundary layer scheme (Hong et al., 2006) for  
127 the vertical diffusion process were applied. As in Kim and Chun (2010), GWs structures are  
128 not fully represented in model outputs from D01, so we emphasize analyzing the outputs  
129 from D02. D01 is only used to provide initial and lateral boundary conditions for the  
130 vortex-following D02.

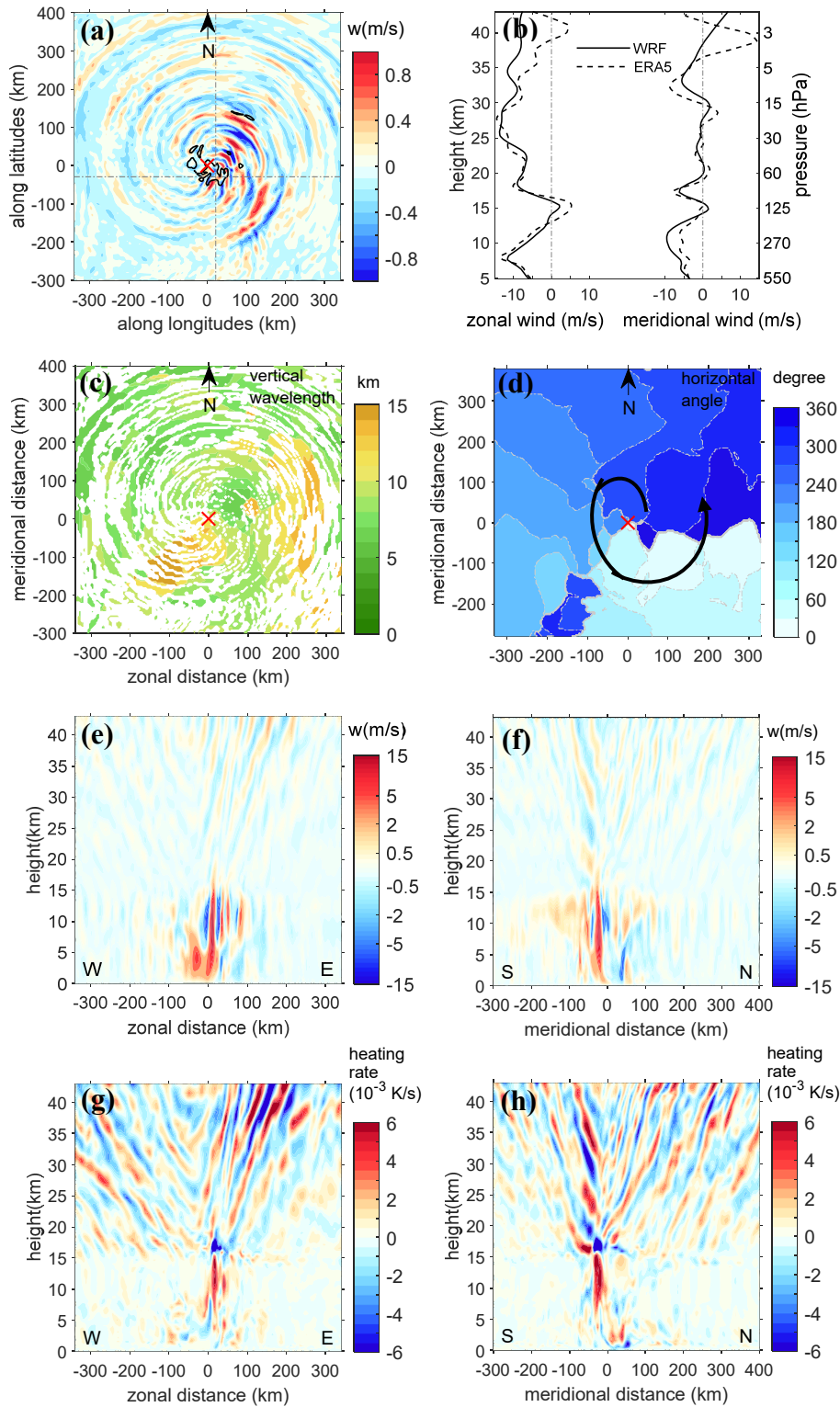
## 131 **4 Results**

### 132 **4.1 WRF-simulated track and intensity of Hurricane Joaquin**

133 Figure 1a shows the geographic region covered by D01 and the initial location of D02,  
134 and compares the WRF-simulated hurricane track with the hurricane track provided by  
135 IBTrACS. The WRF-simulated hurricane track reproduced the slow southwestward  
136 movement of Joaquin before it stalled near the Bahamas and eventually accelerated  
137 northeastward. Figure 1b,c compares the time series of hurricane intensity, represented by  
138 IBTrACS maximum sustained wind speed (MSW), versus maximum surface wind speed  
139 from the WRF simulation (referred to as MSFCW hereafter) and the IBTrACS versus WRF  
140 simulated minimum sea level pressure (MSLP). After a spin-up time of about 12 h, the  
141 simulation results generally represent the hurricane intensity evolution well. Rapid  
142 intensification (i.e., MSW's change exceeding 15.4 m/s during 24 h) is well reproduced until  
143 18:00 UTC 1 October. The simulation results also reproduce the subsequent weakening,  
144 re-intensification, and second weakening of the hurricane. Please refer to the supplement for  
145 the verification of model parameters related to latent heating.



146  
 147 **Figure 1.** Comparison of the track and intensity of Hurricane Joaquin from WRF model simulation and  
 148 IBTrACS data. (a) shows the hourly IBTrACS hurricane center positions (dots) from 00 UTC 29 September to 12  
 149 UTC 4 October, and WRF-simulated hurricane centers (squares) from 00 UTC 30 September to 04 UTC 4  
 150 October 2015, respectively. (b) Comparison of IBTrACS MSW and WRF-simulated MSFCW, where the 6-hourly  
 151 intensity change is derived from IBTrACS data. (c) Comparison of IBTrACS and WRF simulated MSLP. In (b)  
 152 and (c), the thin black lines indicate model outputs every 6 min, and the thin red lines indicate the 6-h moving  
 153 mean of the model outputs.



154

155 **Figure 2.** Features of GWs at 00:00 UTC 1 October 2015. The location of the hurricane center was 23.9°N,  
 156 72.9°W. (a) Vertical velocities at 30 km (GWs with amplitude < 0.1 m/s are excluded); the red cross denotes the  
 157 hurricane center, and the black contours enclose regions where the 5–15 km net heating rate ( $\partial T/\partial t$ ) exceed  $5 \times 10^{-4}$   
 158 K/s. The grey dot-dashed lines indicate the longitude and latitude the cross-sections in (e–h) are made. (b)  
 159 Comparison of the simulated mean zonal and meridional wind in the inner domain with the same parameters  
 160 derived from the ERA5 data. (c) Vertical wavelengths at 30 km. (d) Angles of horizontal propagation (clockwise

161 from north) at 30 km. The black curve with an arrow schematically shows the direction of wave propagation. (e–f)  
 162 Cross-section of WRF simulated vertical velocities. (g–h) Cross-section of WRF simulated net heating rate  
 163 ( $\partial T/\partial t$ ). W: west; E: east; S: south; N: north.

#### 164 4.2 Characteristics of GWs generated by Joaquin 2015

165 As an example of the stratospheric GWs generated by Joaquin, Fig. 2a–c shows GW  
 166 features on a single level at 30 km altitude at 00:00 UTC 1 October 2015, when the hurricane  
 167 was intensifying rapidly. Patterns in vertical velocity show tight spirals, similar to spiral GWs  
 168 shown in the theoretical and idealized studies of Chow et al. (2002), Nolan and Zhang (2017),  
 169 and Tratt et al. (2018). As seen in Fig. 2a., under the influence of the easterly flow, the GWs  
 170 show asymmetric patterns: the waves are suppressed downstream on the west side of the  
 171 hurricane, and the wavefronts are compacted more closely on the east side. Mean zonal and  
 172 meridional winds in the inner domain are shown in Fig. 2b, and winds averaged from ERA5  
 173 data in the same area are also shown for comparison. At 30 km, the simulated mean zonal  
 174 wind is about  $-10$  m/s (i.e., easterly). GW activity and interactions with the mean flow in the  
 175 4 km WRF model output are not entirely resolved in ERA5 data at this horizontal resolution  
 176 of  $\sim 31$  km, and so the discrepancy between the mean winds from the model and from ERA5  
 177 increases in the stratosphere.

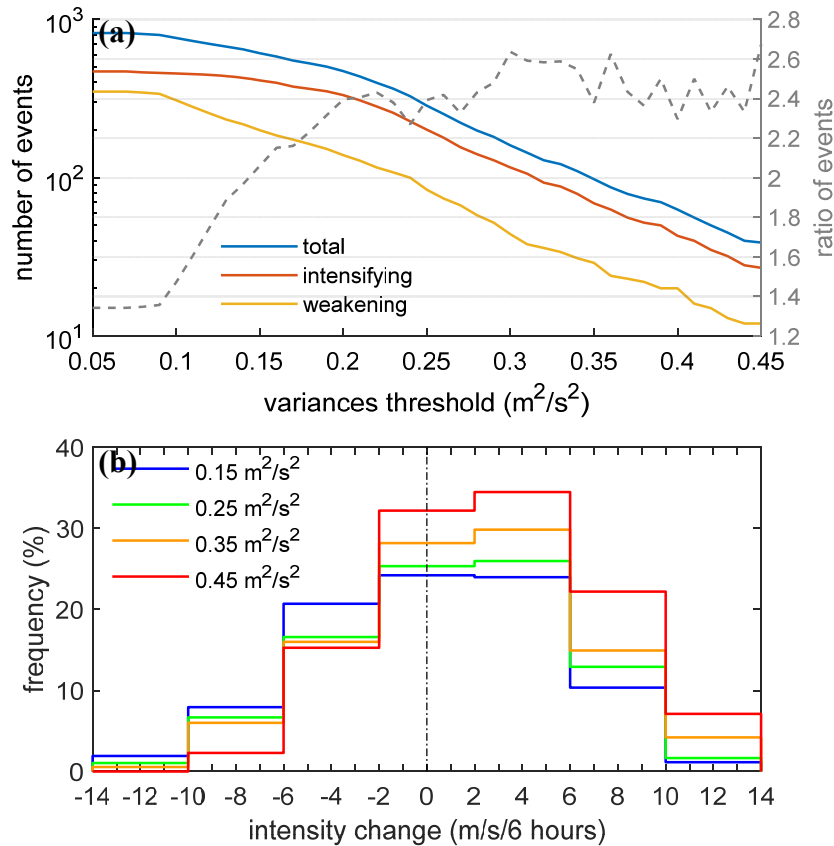
178 GW vertical wavelengths and wave propagation angles (Fig. 2c,d) are calculated by a  
 179 3D Stockwell transform method (Hindley et al., 2016, 2019; Wright et al., 2017). The wave  
 180 propagation angles confirm that GWs propagate outward from the center in an anticlockwise  
 181 manner. The peak vertical wavelength is about 10–14 km. As estimated from Fig. 2a, at the  
 182 altitude of 30 km, the horizontal wavelengths within 200 km of the hurricane center are about  
 183 40 km. GWs with spectral characteristics such as this tend to propagate primarily vertically  
 184 rather than horizontally, and as such propagation time from the troposphere to the  
 185 stratosphere is usually less than 1 h (Yue et al., 2014). Strong updrafts in the upper  
 186 troposphere associated with TCs produce large heating rates, also called “hot towers” (Braun  
 187 et al., 2002; Montgomery et al., 2006). The tropospheric net heating rates (here defined as  
 188 temperature tendency,  $\partial T/\partial t$ ) larger than  $3 \times 10^{-3}$  K/s are mainly seen between 5–15 km, and  
 189 net heating rates larger than  $5 \times 10^{-3}$  K/s between 10–15 km (Fig. 2g,h) along with the  
 190 tropospheric updrafts (Fig. 2e,f).

#### 191 4.3 Occurrence frequency of GW events and hurricane intensity change

192 Figure 3 presents an analysis of stratospheric GW occurrence frequency with respect  
 193 to hurricane intensity change. The WRF simulation outputs were stored every 6 min, and the  
 194 GW activity sampled at a 6-min interval is referred to as one GW event hereafter. Model  
 195 outputs from the spin-up period (the first 12 h) are excluded, leaving 880 events to be  
 196 considered for statistical analysis. The intensity of stratospheric GWs is represented by the  
 197 mean vertical velocity variance between 20 and 43 km. GW intensity varies as the hurricane  
 198 intensifies and weakens. Figure 3a shows that 820 events had a vertical velocity variance  
 199 larger than  $0.05$  m<sup>2</sup>/s<sup>2</sup>, 250 events had a variance larger than  $0.25$  m<sup>2</sup>/s<sup>2</sup>, and 32 events had a  
 200 variance larger than  $0.45$  m<sup>2</sup>/s<sup>2</sup>. There is a clear separation in the number of GW events with  
 201 respect to hurricane intensity change, with more GW events found during intensification than  
 202 weakening. The distinction between intensification and weakening scenarios is particularly



203 clear for the strongest GW events. The ratio of GW events during hurricane intensification to  
 204 GW events during hurricane weakening increases from 1.34 at the threshold of  $0.05 \text{ m}^2/\text{s}^2$  to  
 205 2.67 at the threshold of  $0.45 \text{ m}^2/\text{s}^2$ . However, it should be kept in mind that for large variance  
 206 thresholds, the ratios are calculated from smaller numbers of events, so they may exhibit  
 207 larger fluctuations and uncertainties. Figure 3b shows that the probability distribution  
 208 function with respect to the intensity change of the GW events is skewed toward hurricane  
 209 intensification, particularly for stronger GWs.



210 **Figure 3.** Occurrence frequency of stratospheric GWs with respect to the hurricane intensity change. (a) The  
 211 number of GW events associated with hurricane intensification or weakening for different minimum variance  
 212 thresholds and the ratios of events during hurricane intensification to events during hurricane weakening (gray  
 213 dashed line). (b) Frequency distribution of GWs intensity with respect to intensity change for selected variance  
 214 thresholds.  
 215

216 Several sensitivity tests were conducted to confirm the results above:

217 (i) Results are consistent whether the 6-h change of MSFCW or MSLP is used as a  
 218 measure of hurricane intensity change;

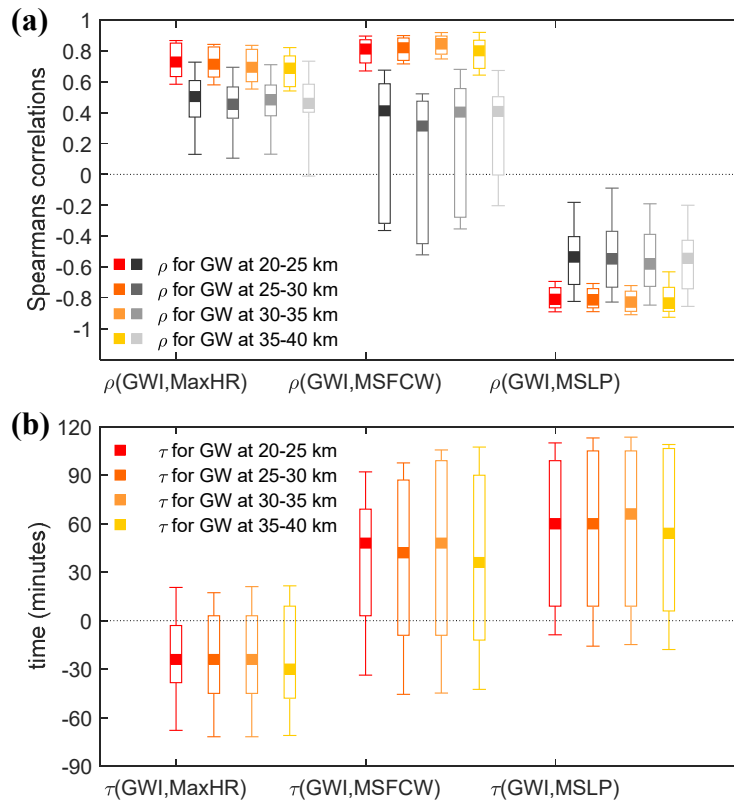
219 (ii) Results remain consistent if we use vertical velocity variances on each model level  
 220 above 20 km, instead of mean variances of vertical velocities of all levels between 20–43 km  
 221 as the intensity of GWs.

222 (iii) Moreover, Joaquin is a well-organized hurricane with strong updrafts and large  
 223 net heating rates in convective bands close to the center. Stratospheric GWs with high  
 224 intrinsic frequencies and shorter horizontal wavelengths tend to appear close to the hurricane  
 225 center, while GWs with low intrinsic frequencies and longer horizontal wavelengths are

226 expected to propagate horizontally further away from the hurricane center (e.g., Alexander et  
 227 al. 1995; Fritts and Alexander 2003). Therefore, we also tested GWs within 200 km and 300  
 228 km of the hurricane center. We found that the above conclusions are robust (i.e., stratospheric  
 229 GW activity is more frequent and intensive when the hurricane is intensifying than when it is  
 230 weakening). These results are consistent with the statistical analysis of GW event occurrence  
 231 frequencies with respect to TC intensity change based on 13.5 years of AIRS observations  
 232 shown by Hoffmann et al. (2018).

#### 233 4.4 Time-lagged correlations between stratospheric GWs events and hurricane 234 intensity

235 Since both TC intensity and features of TC-induced stratospheric GWs individually  
 236 depend on latent heat release during convection, in this subsection, we analyze correlations  
 237 between heat release, hurricane intensity, and stratospheric GW activity for the Joaquin case.  
 238 Our analysis first focuses on GWs with long vertical wavelengths and thus fast vertical phase  
 239 speeds that may propagate upward to the upper stratosphere in a short time (typically in less  
 240 than 1 h).



241  
 242 **Figure 4.** Spearman correlation coefficients and time lag between variable series. Only values that have passed the  
 243 significance test with 95% are kept. (a) Spearman correlation coefficients  $\rho$  between the GWI and MaxHR,  
 244 MSFCW, and MSLP, respectively. The original  $\rho$  is marked in black and grey, and the time-lagged  $\rho$  is marked in  
 245 orange. (b) The “best” time lag  $\tau$  between GWI and MaxHR, MSFCW, and MSLP, respectively. The box plot  
 246 displays the minimum, first quartile (25%), median, third quartile (75%), and maximum values.

247 Mean vertical velocity variances between altitude ranges of 20–25 km, 25–30 km,  
 248 30–35 km, and 35–40 km are calculated as a proxy of GW intensity (referred to as GWI

249 hereafter) at different altitude ranges. According to our simulations, large heat release  
250 generally appears between 5–15 km, so we define the maximum heating rate at 5–15 km  
251 (referred to as MaxHR hereafter) as an indicator of heat release due to the hurricane. The  
252 MSFCW and MSLP are considered as a proxy of hurricane intensity. We split the entire time  
253 series of the WRF simulation, excluding the first 12 h of the spin-up period, into independent  
254 6-h segments starting from each model output at a 6-minute interval. That makes 820 cases of  
255 6-h time series of GWI, MaxHR, MSFCW, and MSLP for the statistical analysis. We then  
256 calculate the Spearman rank-order correlation coefficients  $\rho$  of each pair of time series of  
257 GWI versus MaxHR/MSFCW/MSLP. Median values of  $\rho(\text{GWI}, \text{MaxHR})$ ,  $\rho(\text{GWI},$   
258  $\text{MSFCW})$ , and  $\rho(\text{GWI}, \text{MSLP})$  are about 0.5, 0.4, and  $-0.6$ , respectively (Fig. 4a, gray),  
259 which indicates a moderate level of correlations between GW activity, heat release, and  
260 hurricane intensity. This result agrees with the statistical correlation previously found  
261 between stratospheric GW activity and TC intensification based on 13.5 years of AIRS  
262 observations of stratospheric GWs (Hoffmann et al., 2018). A sensitivity test with respect to  
263 the length of the time series shows that the correlation slightly decreases as the length of the  
264 time series increases. For the entire time series, median values of  $\rho(\text{GWI}, \text{MaxHR})$ ,  $\rho(\text{GWI},$   
265  $\text{MSFCW})$ , and  $\rho(\text{GWI}, \text{MSLP})$  are 0.32, 0.24, and  $-0.43$ , respectively (not shown). The  
266 correlation for the entire time series is slightly lower than that measured for Hurricane  
267 Joaquin by Hoffmann et al. (2018). This difference is reasonable because model output at a  
268 6-minute interval resolves more fluctuations than the 6-hourly observations in Hoffmann et al.  
269 (2018). Fluctuations weaken the monotonic relationship between two variable series and thus  
270 reduce the Spearman rank-order correlation level.

271 Considering that there may be a time lag of 0–3 h between a large heat release and TC  
272 intensification, as shown in Hazelton et al. (2017), and that GWs take time to propagate to the  
273 stratosphere, we searched for the “best” time lag within a time window of  $\pm 6$  h that produces  
274 the most significant time-lagged Spearman rank-order correlation coefficients for each 6-h  
275 GWI time series. Correlations significantly increase when the time lag is considered: the  
276 median values of time-lagged  $\rho(\text{GWI}, \text{MaxHR})$ ,  $\rho(\text{GWI}, \text{MSFCW})$ , and  $\rho(\text{GWI}, \text{MSLP})$  are  
277 about 0.7, 0.8, and  $-0.8$  (Fig. 4a, orange), and the standard deviations of the correlation  
278 coefficients considerably decrease. The “best” time lag  $\tau$  found with this procedure is shown  
279 in Fig. 4b. Negative values indicate GW intensity changes after the change of heat release  
280 represented by MaxHR, whereas positive values indicate GW intensity varies before the  
281 hurricane intensity change as represented by MSFCW and MSLP. The median time lag  
282 values show that GW intensity follows the heating rate changes within about 24–30 min, and  
283 then the hurricane intensity changes about 36–60 min after the change of GW intensity.

284 As shown in Fig. 4, GWs are triggered after latent heat release and propagate fast in  
285 the vertical direction. They can be observed in the stratosphere even before the hurricane  
286 intensity itself increases. However, note that there are large peak-to-peak ranges for the time

287 lag in Fig. 4b. This variation in the peak-to-peak range shows substantial complexity in the  
288 physical relations between latent heat release, hurricane intensity, and GW activity being  
289 involved. Therefore, further modeling and observational studies are needed to better  
290 understand this complexity and to establish that stratospheric GW activity is not only a proxy  
291 but also a reliable predictor of TC intensification. The supplement contains the Spearman  
292 correlation coefficients and time lag, same as in Fig. 4 but separately for the intensification  
293 and weakening periods.

294 We conducted sensitivity tests to confirm the robustness of the above results:

295 (i) The results are consistent if the 99th percentile, median, or mean value of the net  
296 heating rates between 5–15 km is used as the indicator of heat release.

297 (ii) Time windows of  $\pm 3$  h and  $\pm 12$  h have been tested for the “best” time lag, and the  
298 results agree well with the above results with only minor differences of about 12–18 min in  
299 peak-to-peak ranges of the time lag.

300 (iii) When all stratospheric GWs in the inner domain are considered (up to around  
301 400–500 km from the hurricane center), the correlations between stratospheric GWs and  
302 hurricane intensity remain, but the median value of the “best” time lag is around 0. That is,  
303 only the fast-propagating GWs have the potential for predicting hurricane intensity.

## 304 **5 Conclusions**

305 In this study, we performed a mesoscale simulation of Hurricane Joaquin in 2015  
306 using the WRF model to study the correlations between the features of the stratospheric GWs  
307 generated by the hurricane and the hurricane intensity. First, the simulated track and intensity  
308 of Joaquin were compared with the IBTrACS “best track” data, and the characteristic of the  
309 simulated stratospheric GWs was analyzed. It was found that the storm generated spiral GWs  
310 and that the GWs rotate and spread anticlockwise away from the hurricane center.

311 The present study confirms that intensive stratospheric GW activity generated by a  
312 hurricane can be a proxy for the intensification of the hurricane itself. Analyses show a clear  
313 distinction of GW occurrence frequencies with respect to hurricane intensity change:  
314 stratospheric GW activity is more frequent and intensive when the hurricane intensifies rather  
315 than when it weakens. This phenomenon is particularly prominent for the strongest GW  
316 events. This result agrees with observational results found by Hoffmann et al. (2018) based  
317 on 13.5 years of AIRS observations and Wright (2019) based on 17 years of MLS, SABER,  
318 and HIRDLS observations of TC-induced gravity waves. Moreover, the correlation between  
319 the intensity changes of stratospheric GWs activities and the hurricane is more significant  
320 when the time lag is considered.

321 Measuring the internal structure and dynamics of TCs from space-based infrared  
322 sensors is typically not possible because the dense cloud coverage due to the TCs block the  
323 view of the instrumentation below cloud top. However, since the stratospheric GW signals  
324 that indicate the change of a TC are visible to passive infrared and microwave instruments  
325 (e.g., AIRS (Hoffmann and Alexander, 2010; Yue et al., 2013), the Infrared Atmospheric  
326 Sounding Interferometer (IASI) (Hoffmann et al., 2014), and MLS (Wright et al., 2014)), it is  
327 possible to monitor significant changes in TC intensity by observing GWs with passive

328 infrared and microwave sounders. This proxy is particularly useful when a cloud canopy  
329 obscures the direct view to the TC center for other instruments.

330 However, it should be noticed that whether intensive stratospheric GW activity can be  
331 observed before TC intensification is also largely determined by dynamical and thermal  
332 variabilities in the TCs and the effects of the atmospheric background conditions on GW  
333 generation and propagation. In addition to latent heating, other factors that may link GW  
334 activity and TC intensity, such as the interaction of GWs and TC intensity evolution with the  
335 diurnal cycle of TC intensity (Dunion et al., 2014; Evans and Nolan, 2019), will be  
336 investigated in future studies.

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### 353 **Open Research**

354 The ERA5 reanalysis data (C3S, 2017) were retrieved from ECMWF Meteorological  
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