

Determining maximum entropy in 3D remote sensing height distributions and using it to improve aboveground biomass modelling via stratification

Adnan, Syed; Maltamo, Matti; Mehtätalo, Lauri; Ammaturo, Rhei N.L.; Packalen, Petteri; Valbuena, Rubén

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1 Title:

- 2 Determining maximum entropy in 3D remote sensing height distributions and using it to
- 3 improve aboveground biomass modelling via stratification.
- 4 Authors:
- 5 Syed Adnan*(1), Matti Maltamo (1), Lauri Mehtätalo (2), Rhei N. L. Ammaturo (3), Petteri
- 6 Packalen (1), Rubén Valbuena*(4)
- 7 Affiliations:
- 8 (1) University of Eastern Finland, School of Forest Sciences. PO Box 111. FI-80101. Joensuu,
- 9 Finland. adnan@uef.fi; matti.maltamo@uef.fi; petteri.packalen@uef.fi
- 10 (2) University of Eastern Finland, School of Computing, P.O. Box 111, FI-80101 Joensuu,
- 11 Finland. lauri.mehtatalo@uef.fi
- 12 (3) University of Cambridge, Department of Plant Sciences, Forest Ecology and Conservation,
- Downing Street, CB2 3EA Cambridge, UK. nla32@cam.ac.uk
- 14 (4) Bangor University. School of Natural Sciences, Thoday building. Bangor. Gwynedd, LL57
- 15 2UW. UK. <u>r.valbuena@bangor.ac.uk</u>
- *Corresponding authors.

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- 19 forest structure, forest aboveground biomass, Gini Coefficient, L-moments, airborne laser
- 20 scanning

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26 Abstract

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McArthur's foliage height diversity (FHD) has been the gold standard in the determination of structural complexity of forests characterized by LiDAR vertical height profiles. It is based on Shannon's entropy index, which was originally designed to describe evenness in abundances among qualitative typologies, and thus the calculation of FHD involves subjective layering steps which are essentially unnatural to describe a continuous variable (X) such as height. In this contribution we aim to provide a mathematical framework for determining maximum entropy in 3D remote sensing datasets based on the Gini Coefficient of theoretical continuous distributions, intended to replace FHD as entropy measure in vertical profiles of LiDAR heights (1D; X), with extensions to variables expressing dimensions of higher order (2D or 3D, $Z \propto$ X^2 or X^3). Then we apply this framework to Boreal forests in Finland to describe landscape heterogeneity with the intention to improve the modelling of forest aboveground biomass (AGB), hypothesizing that LiDAR models of AGB should essentially be different in areas of differing structural characteristics. We carried out a pre-stratification of LiDAR data collected in 2012 using simple rules applied to the L-skewness (L_{skew}) and L-coefficient of variation of LiDAR echo heights (L_{cv} ; equivalent to the Gini coefficient, GC_H), determining a new threshold at $GC_H = 0.33$ as a consequence of the newly developed mathematical proofs. We observed only moderate improvements in terms of model accuracies: RMSDs reduced from 41.7% to 38.9 or 37.0%. More remarkably, we identified critical differences in the metrics selected at each stratum, which is useful to understand what predictor variables are more important for estimating AGB at each area of a forest. We observed that higher LiDAR height percentiles are more relevant at open canopies and heterogeneous forests, whereas closed canopies in homogeneous forests obtain most accurate predictions from a combination of cover metrics and percentiles around the median. Without stratification, the overall model would neglect explained variability in the structural types of lower occurrence, and predictions from

- a model influenced by structural types of higher occurrence would be biased at those areas.
- 52 These results are thus useful in terms of improving our understanding on the relationships
- underlying LiDAR-*AGB* models.

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1. Introduction

- 56 Structural complexity is an essential morphological trait of ecosystems, complementary to 57 others like vegetation height or cover (Schneider et al. 2017; Fahey et al. 2019; Valbuena et al. 2020), which is relevant to various ecological processes such as nutrients cycling, carbon 58 59 sequestration and species interactions (Brokaw and Lent 1999; Lindenmayer et al. 2000; McElhinny et al. 2005). There is however a lack of consensus on the most appropriate means 60 to measure the structural complexity of ecosystems (Neumann and Starlinger 2001; Lexerød 61 and Eid 2006), with approaches focused on measuring either entropy, e.g. Simpson or Shannon 62 indices (McArthur and McArthur 1961), or variability, e.g. variance or Gini coefficient (GC) 63 (Weiner 1990). The most popular approach follows the early works of McArthur and McArthur 64 (1961) who calculated the Shannon-based foliage height diversity (FHD) after layering the 65 ecosystem vertical profile into three strata, but there have been pleas for alternative measures 66 (Lovejoy 1972; Pearson 1975; Erdelen 1984; Weiner and Thomas, 1986; Valbuena et al. 2012). 67 This dichotomy has been reflected in the derivation of structural complexity measures from 68 LiDAR, with alternatives based on either layering the vertical profile (Lefsky et al. 2002a; 69 Vierling et al. 2008; Simonson et al. 2014; Weisberg et al. 2014; Listopad et al. 2015; Wilkes 70 et al. 2016; Almeida et al. 2019a; Bakx et al. 2019) or measuring variability in LiDAR heights 71 72 (Valbuena et al. 2017a; Moran et al. 2018; Mononen et al. 2019; Crespo-Peremarch et al. 2020; Hagar et al. 2020). 73
- 74 In this contribution we propose a mathematical framework (**Appendix A**) which effectively
- 75 merges both approaches, by showing how maximum entropy can be flagged up from values of

a variability measure such as the Gini coefficient. They constitute formal deductive proofs of ideas that have previously been presented on the basis of empirical indications: such as a threshold at GC = 0.5 employed to discriminate ecosystem structural heterogeneity (Valbuena et al. 2012, 2017a). Based on these mathematical developments, we further argue that different thresholds apply for GC depending on whether calculated from LiDAR heights (GC_H) , or tree basal areas (GC_{BA}) , because the former is a variable representing one dimension (X) and the latter is an area, and thus bi-dimensional (X^2) (Appendix A). This mathematical framework thus provides unified means for determining maximum entropy in the 3D space of information provided by remote sensing tools such as LiDAR. To quantify the amount of carbon sequestered by forests over large geographical areas, and use them to inform global policies, it is important to attain reliable estimations of forest aboveground biomass (AGB) from local to global scales (Gibbs et al. 2007). In this context, remote sensing in general, and LiDAR in particular, are the key technologies to monitor reductions in emissions of greenhouse gases from deforestation and forest degradation (REDD) (Boudreau et al. 2008; Asner et al. 2010). Airborne LiDAR produces detailed canopy information (Maltamo et al. 2005; Gobakken and Næsset 2008) that provides opportunities for predicting accurately various ecosystem attributes such as vegetation height (Magnussen et al. 1999; Maltamo et al. 2004; Koukoulas and Blackburn, 2005), tree diameters (Næsset, 2002; Räty et al. 2018), structural heterogeneity (Vierling et al. 2008; Weisberg et al. 2014; Adnan et al. 2019), tree species (Van Aardt et al. 2008), or forest biomass and carbon (Næsset and Gobakken 2008; Kronseder et al. 2012; Valbuena et al. 2017b). Metrics derived from airborne LiDAR are the most promising information for efficient and accurate AGB prediction (Asner and Mascaro 2014; Bouvier et al. 2015; Longo et al. 2017). For this reason, these metrics are employed as auxiliary variables in airborne LiDAR-assisted estimations (Gobakken and Næsset 2008; Asner et al. 2010). Mehtätalo and Nyblom (2009, 2012) developed the

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relationship between canopy height obtained from airborne LiDAR data and forest attributes such as stand density and mean tree height, improving model-based estimations. However, we still lack information on the relationship between LiDAR metrics with the forest AGB, and how the predictive models are affected by forest structures (Drake et al. 2003; Knapp et al. 2020). Researchers have developed a wide variety of LiDAR models estimating AGB stocked in forests (Zolkos et al. 2013). The prediction error of the total AGB is dependent on the relationship between foliage observed by LiDAR and various AGB components (Lefsky et al. 2002b; Næsset and Gobakken 2008; Hernando et al. 2019). Thus, high heterogeneity in the structural complexity of forests may cause difficulties in modelling (Drake et al. 2003; Hall et al. 2005; Jaskierniak et al. 2011; Vincent et al. 2014). While there have been many attempts to generalize LiDAR modelling of AGB (Asner and Mascaro 2014; Bouvier et al. 2015), a general relationship may not be appropriate for all regions, both even and uneven sized forests or dense and sparse spatial structures (Vincent et al. 2014; Häbel et al. 2019; Knapp et al. 2020). To overcome this difficulty, the forest area can be stratified into different development classes (Næsset 2002) or forest structural types (FSTs) (Mascaro et al. 2011; Vincent et al. 2014), and a separate model can be applied to each of them to obtain more reliable AGB estimations. With these regards, we hypothesised that the Gini coefficient can be useful for such FST stratification prior to modelling the forest AGB. Bollandsås and Næsset (2007) obtained reliable results following such approach with the support of field information (i.e., GC_{BA}). Alternatively, we postulated that these FSTs could be detected directly from airborne LiDAR data (i.e. GC_H), and apply a separate AGB model in each FST to improve AGB predictions. Based on results in Valbuena et al. (2017a), we considered the use of L-moment ratios for such stratifications: Lcoefficient of variation of LiDAR echo heights (L_{cv} ; equivalent to the Gini coefficient, GC_H) and L-skewness (L_{skew}). We considered a new threshold at $GC_H = 0.33$ for separating even sized from uneven sized forest structures, based on findings in Appendix A. Furthermore,

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Valbuena et al. (2017a) also identified FSTs according to their light environment characteristics using the $L_{skew}=0$ threshold which segregate the euphotic/open canopy and oligophotic/closed canopy forest areas (Lefsky et al. 2002a), by separating them as positive and negative skewness in between the [-1,1] bounds of L_{skew} . We evaluated the potential of these detected FSTs in improving the AGB prediction from the airborne LiDAR data.

In this article, we set the mathematical foundations for determining maximum entropy from a distribution of heights in 3D remote sensing (Appendix A), as an alternatively to common binning procedures employed to determine McArthur and McArthur's (1961) FHD. Then we employed this rationale, stratified the LiDAR-surveyed area according to the $L_{cv}=0.33$ and $L_{skew}=0$ rules following Valbuena et al. (2017a), and carried out stratified sampling with roughly equal sample sizes within each FST. The aim of this stratification was to evaluate the potential of FSTs to improve forest AGB predictions in the pre-stratified airborne LiDAR data compared to the AGB predictions in the whole dataset without pre-stratification. We developed a general LiDAR-AGB model for the whole dataset without pre-stratification, and separate FST-specific models at each stratum. We hypothesized that LiDAR models predicting AGB should essentially be different in areas of differing structural characteristics. For this reason, we also paid careful attention to the LiDAR metrics selected at each model, and used those results to make inferences on the relationship behind the choice of metrics at each forest area, with the intention to shed light on the effects of forest heterogeneity on LiDAR models predicting AGB.

2. Material and Methods

- 2.1. Study Area and data collection
- This study was conducted in a 252,000 ha boreal forest located in the North Karelia region of Finland (Figure 1). The dominant species in the study area are Norway spruce (*Picea abies* (L.)

Karst.), Scots pine (*Pinus sylvestris* L.) and Birch species (*Betula* spp.), and some other deciduous species such as *Alnus* spp. and *Populus* spp. are also present. In May 2012, a Leica ALS60 laser scanning system was used to collect airborne LiDAR data. Flight elevation was 2,300 m above ground level, which resulted in a scan density of 0.91 pulses per square meter. The digital terrain model with 2 m resolution derived from the same LiDAR dataset was provided by National Land Survey (Finland). The DTM was subtracted from the LiDAR echo heights and area-based LiDAR metrics were computed using the FUSION software (Version 3.70, USDA Forest Service; McGaughey 2019). With the intention to get in the full structural characteristics of forests and commensurate with forest data acquisition, a very small height threshold (< 0.1 m) was used to exclude ground echoes in the computation of area-based metrics (Görgens et al. 2017). This eliminates ground echoes but consider seedlings and saplings, which were included in the field inventory (Valbuena et al. 2016). Among the set of FUSION metrics, two L-moment ratios were used for simulating a pre-stratification: L-coefficient of variation (L_{cv}) and L-skewness (L_{skew}). The remaining metrics were involved in the modelling of AGB.

approximate position of Figure 1*

Field data for the calibration/validation of *AGB* models were jointly collected by the Finnish Forest Centre (Suomen Metsäkeskus; SMK) and University of Eastern Finland (UEF) in 2013 (Valbuena et al. 2017a). There were 244 field plots in total from eight different strata and sample size was approximately equal in each stratum. The stratification was based on the forest development classes – seedling, sapling, young, advanced, mature, shelterwood, seed-tree and multi-storey (Valbuena et al. 2016) –, determined on the basis of the SMK stand-wise information from the previous forest management plan, randomly selecting plot locations over areas covering each development class. Field data acquisition consisted in a concentric circle

design, recording species and diameter at breast height (dbh; cm) of trees within each concentric plot according to its size (Valbuena et al. 2016). Tree heights (h; m) were measured only for the basal area median tree of each species. For the even sized development classes (young, advanced and mature), the field data were collected by SMK using a plot size of 9 m radius for trees with dbh > 8 cm, while saplings were recorded within 5.64 m radius and seedlings were counted using a 2.82 m long stick in distributed sub-plots (Figure 2). Plots within the seed tree, shelterwood and multi-storey development classes were collected by UEF using the same plot design. However, the size of the outer plot in these three development classes was slightly increased to 9.77 m so that its size would become integer multiplier of the inner subplots, which is convenient for the calculation of GC_{BA} following Valbuena et al. (2013). For visual comparison of these development classes, mean leaf area density (LAD) vertical profiles with 95% confidence intervals from all plots within each development class were calculated from LiDAR data using the R package LeafR (Almeida et al. 2019b).

approximate position of Figure 2*

- 2.2 Rule-based stratification of forest structural types using airborne lidar data
 - Postulating that LIDAR models of AGB should be essentially different in areas of differing structural characteristics, we employed this dataset to simulate a pre-stratification scenario by classifying the prediction area into FSTs detected directly from the LiDAR data. The study area was stratified using the abovementioned two L-moment ratios of airborne LiDAR height distributions, and the rules were deduced from their mathematical properties instead of inductive statistical distributions or supervised classification, thus absence of any field information is involved (Valbuena et al. 2016). As L_{cv} is mathematically equivalent to the Gini coefficient of LiDAR echo heights (GC_H) (Valbuena et al. 2017a), it could be used to describe the structural properties related to the inequality in tree sizes within a forest area. L_{cv} =

0.33 was used as a boundary line to discriminate forests with even-sized FSTs ($L_{cv} < 0.33$) from uneven-sized ones ($L_{cv} > 0.33$), on the grounds that maximum entropy in the distribution of LiDAR heights is reached at $L_{cv} = 0.33$ (**Appendix A**). Similarly, asymmetry (L_{skew}) describes the structural heterogeneity related to light availability and tree size dominance (Valbuena et al. 2017a). $L_{skew} = 0$, which represents the symmetric distribution of LiDAR echo heights, was used to separate forests having oligophotic areas/closed canopy ($L_{skew} < 0$) from euphotic areas/open canopy areas ($L_{skew} > 0$) (Lefsky et al. 2002a).

2.3 Aboveground biomass calculation from field data

R statistical software (R Core Team 2019) was used for all statistical analyses and modelling. Locally developed species-specific biomass equations were used to calculate tree above-ground biomass (agb; kg) for Scots pine and Norway spruce (Repola, 2009), and another for birch (Repola, 2008) which was used for all deciduous species. These were based on dbh and h, and thus individual tree heights were subsequently predicted using the Näslund's height curve (1936):

$$h = 1.3 + \left(\frac{dhb}{\beta_0 + \beta_1 dbh}\right)^{\alpha}, \tag{1}$$

where the exponent was $\alpha=2$ for pine and deciduous species, and $\alpha=3$ for spruce. We followed the methods suggested by Siipilehto (1999) in the estimation the Näslund's height curve model parameters (β_0, β_1) for each species. which included plot-level calibration with species-specific diameter $(D_{\widetilde{ba}})$ and height $(H_{\widetilde{ba}})$ of the tree with median basal area (\widetilde{ba}) . Then the species-specific parameters were used in the height curve model to predict the missing tree heights from their dbh. Once calculated all the tree level agb values, they were aggregated to plot level $(AGB; Mg \cdot ha^{-1})$ according to their corresponding hectare expansion factors, and used as a response variable in subsequent LiDAR models.

2.4 Modelling of aboveground biomass from airborne LiDAR data

Many airborne LiDAR derived metrics (predictors) were available for modelling the AGB. We used function "regsubset" of the R package "leaps" (Lumley and Miller, 2017), which performed a selection of the best subset of predictors using an exhaustive search among typical LiDAR-AGB models (Valbuena et al. 2017b). We made an independent selection, the best subset of predictors for the general model including the whole dataset (i.e. without stratification), and also for each FST-specific model (even versus uneven sized forest structures, and euphotic/open canopy versus oligophotic/closed canopy areas). Thereafter, modelling based on the k-nearest neighbour (k-NN) method was used to predict the response variable (AGB) from the best subset of airborne LiDAR predictors (Mcinerney et al. 2010). We used Euclidean distance with k = 5 in the k-NN implementation available in the R package "Yalmpute" (1.0-31 version; Crookston and Finley, 2008).

2.5 Accuracy assessment of aboveground biomass prediction

We used a 10-fold cross validation method for assessing the accuracy of the resulting models.

The results of the general model and FST-specific models were evaluated and compared by

means of their mean difference (MD) and root mean square difference (RMSD):

$$RMSD = \sqrt{\frac{\sum_{i=1}^{n} ((y_i^{cv} - \hat{y}_i)^2}{n}}, \qquad (2)$$

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$$MD = \frac{\sum_{i=1}^{n} ((y_i^{cv} - \hat{y}_i))}{n},$$
 (3)

where n is the total number of observations (field plots), y_i^{cv} and \hat{y}_i are the predicted and observed value of AGB for observation i, respectively. Relative values (%) of MD and RMSD were obtained as the percentage over the mean observed AGB. As an additional quality control measure, we used a hypothesis test on the 1:1 correspondence between the observed (obs_i) and

predicted (pre_i^{cv}) values from the intercept (α) and slope (β) of their linear regression (Leite and Oliveira, 2002; Piñeiro et al. 2008),

$$obs_i = \alpha + \beta pre_i^{cv}, \tag{4}$$

To avoid overfitting the models to the sample, the best subset procedure was constrained by additional restrictions to the sum of squares ratio (SSR), which evaluates the inflation in the unexplained variance when the model is not cross-validated (Valbuena et al. 2017b). SSR is the ratio between the squared root sum of the squares obtained by cross validation (SS^{cv}) and without cross validation (SS^{fit}) .

$$SSR = \sqrt{SS^{cv}} / \sqrt{SS^{fit}}, \tag{5}$$

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$$SS^{cv} = \sum_{i=1}^{n} (y_i^{cv} - \hat{y}_i)^2$$
 (6)

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$$SS^{fit} = \sum_{i=1}^{n} (y_i^{fit} - \hat{y}_i)^2$$
 (7)

Where, \hat{y}_i is the observed value of the *AGB* for observation *i*, and y_i^{cv} and y_i^{fit} are the predicted values using cross validation and without cross validation, respectively.

3. Results

257 3.1. Airborne LiDAR based forest structural types

Table 1 gives a development class-wise summary of plot-level characteristics calculated from the field data – density (N), quadratic mean diameter (QMD), above ground biomass density (AGB) and Gini coefficient of basal area (GC_{BA}) –, and also from the LiDAR data – L-coefficient of variation $(L_{cv};$ equivalent to the Gini coefficient, GC_H) and L-skewness (L_{skew}) . of LiDAR return heights –. Height profiles of each development class calculated from LiDAR data are given in **Figure 3**, which shows mean changes in LAD through the vertical profiles at each development class. **Figure 4** further shows how different forest structural types detected

directly from airborne LiDAR data are distributed either sides of the $L_{cv}(GC_H)=0.33$ and $L_{skew} = 0$ thresholds. Some structural dynamics can be observed from these figures, since the majority of areas in seedling development classes were separated as even sized by $L_{cv}(GC_H)$ < 0.33, because they are very small and roughly equal in size at first, to later more inequality in diameter distribution toward the sapling stage $(L_{cv}(GC_H) > 0.33)$ (Figure 4a). Likewise, the young, advanced and mature development classes which mostly contain equality in diameter/basal area distribution were mostly separated as even sized ($L_{cv}(GC_H) < 0.33$). Seed trees and multi-storied development classes have higher inequality in their diameter distribution, they show high dispersion in their LiDAR echoes, and thus they were separated as uneven sized structure ($L_{cv}(GC_H) > 0.33$). Similarly, in **Figure 4b** most seedling and sapling development classes were separated as euphotic areas $(L_{skew} > 0)$ because their canopies have not closed yet at these stages of development. As they grow and increase in AGB through young, advanced and mature development classes, they shift toward oligophotic areas with closed canopies and negative skewness of LiDAR return heights ($L_{skew} < 0$). The shelterwood development class which has a dense overstory and high LiDAR returns was classified as oligophotic ($L_{skew} < 0$), whereas seed-tree areas and multi-storey development classes with sparse overstorey were mainly classified as euphotic ($L_{skew} > 0$).

- ***approximate position of Table 1****
- 283 ***approximate position of Figure 3****

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284 ***approximate position of Figure 4****

We were then interested on whether the different thresholds that **Appendix A** shows for LiDAR heights ($GC_H(L_{cv}) = 0.33$) and field data ($GC_{BA} = 0.5$) would segregate forests with similar structural properties. **Figure 5** shows a comparison of aggregated diameter distributions (plus basal area-weighted distributions, in darker colors in the background) with confidence

intervals. The difference between the distribution of proportions in density of stems versus basal area highlights structural differences which cannot be easily appreciated in diameter distributions, since in highly complex structures with large differences in tree sizes the proportion of basal area taken by larger trees becomes predominant. This could be appreciated in the distributions of strata yielded from the LiDAR data only $(GC_H(L_{cv}) < 0.33)$ and $GC_H(L_{cv}) > 0.33$, respectively in **Figures 5a** and **b**), as much as it was for the distributions yielded when the strata was generated using the field data itself $(GC_{BA} < 0.50)$ and $GC_{BA} > 0.50$, respectively in **Figures 5c** and **d**). These results emphasize the reliability of a purely LiDAR-based classification in the structural heterogeneity assessment of forests.

approximate position of Figure 5*

3.3. Best-subset variable selection

In order to facilitate direct comparison of all models, we fixed the number of LiDAR predictors to be six for all models, based on the *SSR* restriction of the best-subset procedure which assured that none of them had over-fitting effects, plus a positive outcome in the hypothesis test of 1:1 correspondence. **Table 2** shows the variables selected at each of them: the general model developed for the whole data without pre-stratification, and each FST-specific model developed for the even and uneven sized forest structures and oligophotic/closed canopy and euphotic/open canopy areas, obtained from the direct classification of airborne LiDAR data. While all the selected predictors were those typically included in LiDAR-*AGB* modelling – averages (e.g. quadratic or cubic means), dispersion statistics (e.g., variance), percentiles, and cover metrics (i.e. percentages above thresholds) of LiDAR return heights –, we identified critical differences in the metrics selected at each stratum, which is useful to understand what predictor variables are more important for estimating *AGB* at each area of a forest. We observed that higher LiDAR height percentiles were more relevant at open canopies and heterogeneous

forests, whereas closed canopies in homogeneous forests obtained a best subset based on combinations of cover metrics and percentiles around the median. In the uneven-sized structures, higher percentiles, variance and absolute average deviation of LiDAR return heights were selected. On the other hand, in the even-sized stratum the model included the mode, L_{skew} , the median, and cover metrics (percentage of all returns above mode and total first returns). Similarly, in the oligophotic/closed canopy areas, the median and cover metrics were important, while in the euphotic areas/open canopy areas, higher percentiles and mean absolute deviation from median and variance were selected. Thus, the similarities of even-sized with oligophotic areas on one hand, and uneven with euphotic areas observed in **Figure 4**, showed an influence in the modelling itself (**Table 2**), thus indicating convergence in the relationships between structure and modelling results.

approximate position of Table 2*

- 3.3. Modelling aboveground biomass from airborne LiDAR based forest structural types
 - The *AGB* was predicted in each model using the associated best subset of LiDAR predictors, and their accuracies were assessed. In the general model (**Table 3** and **Figure 6**), i.e. a model fitted using the whole dataset, the RMSD between the observed and predicted *AGB* was 37.4 Mg·ha⁻¹. We disaggregated these accuracy statistics by strata, to allow direct comparison with the FST-specific models, which resulted in 37.1 and 37.6 Mg·ha⁻¹ respectively in the even and uneven-sized forest areas and resulted in 37.6 and 37.3 Mg·ha⁻¹ in oligophotic and euphotic areas, respectively. In relative terms, the general model RMSD 41.7%, which seems high because of the inclusions of seedling and sapling areas of very low *AGB* in the dataset. The general model showed some bias when applied to specific FSTs, as it can be appreciated by underpredictions of around 4.8-5.5% in terms of their MDs, with the even-sized forests being the only areas where not such strong bias effect was observed (-2.33% only).

approximate position of Table 3*

approximate position of Figure 6*

The results for the FTS-specific models are summarized in **Tables 4a-b**, and the scatterplots in **Figures 7-8**. The RMSD improved both in the even sized (34.6 Mg·ha⁻¹) and uneven sized (35.3 Mg·ha⁻¹) forest structures (**Table 4a**) as compared to the general model (**Table 3**). The MD similarly improved in the uneven sized forest structure (-2.72 Mg·ha⁻¹) and only slightly decreased in the even sized areas (-2.30 Mg·ha⁻¹). These specific models developed for the even and uneven sized forest structures also showed an improvement in the MD and RMSD when aggregated for the whole area (-2.52 and 34.9 Mg·ha⁻¹) (**Table 4a**), compared to the general model (-3.55 and 37.4 Mg·ha⁻¹) (**Table 3**). Similar improvements in the MD and RMSD were observed in the FST specific models developed for the oligophotic/closed canopy areas (-2.22, 33.5 Mg·ha⁻¹), euphotic areas/open canopies (-2.52, 32.9 Mg·ha⁻¹), and whole data (-2.37, 33.2 Mg·ha⁻¹) (**Table 4b**). All the FST-specific modelling approaches, thus, showed improvements compared to the general model both in terms of unbiasedness and improving the precision of predictions.

- ***approximate position of Table 4****
- ***approximate position of Figure 7****
- ***approximate position of Figure 8****

4. Discussion

4.1. Determining maximum entropy from a distribution of heights in 3D remote sensing

In previous contributions we have showed a threshold of interest which flags up maximum entropy at the Gini Coefficient value of $GC_{BA} = 0.50$ (Valbuena et al. 2012, 2017). This

threshold allows to compare the entropy of the ecosystem using a statistic of dispersion, arguing that is more correct for continuous variables because it avoids the factitious binning step required when computing foliage height diversity (McArthur and McArthur, 1961), based on Shannon's entropy index which was originally meant for discrete variables (Shannon, 1948). It is important to note that this threshold is applicable for a Gini coefficient of a Lorenz curve representing differences in basal area among trees growing within a given area (GC_{BA}) (Valbuena et al. 2012). On the other hand, in this contribution we further argue that for a Gini coefficient of a Lorenz curve representing differences in LiDAR heights within that same area (GC_H) , the alternative value of $GC_H = 0.33$ should be the one used instead to identify maximum entropy. The reason is that height is a one-dimensional variable (X), whereas basal areas are two-dimensional (X^2) . In order to achieve these generalized conclusions, we need to use theoretical distribution functions and show how their parameters propagate into Lorenz curves and values of the Gini Coefficient directly dependent on those parameters. In the **Appendix A**, we show formal proofs for these values obtained from theoretical distributions, to illustrate the reasoning employed in this contribution. We also show how these maxim entropy values of GC_X extend to higher dimensions (e.g. GC_{X^2}), thus developing a mathematical framework which provides unified means for determining maximum entropy in the 3D space of information provided by remote sensing tools such as LiDAR. Figure 5 illustrates empirically the equivalence of the LiDAR and field approaches.

4.2. Rule-based pre-stratification into different forest structural types

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Airborne LiDAR explains the key characteristics of forests related to the structural heterogeneity that can be relevant to describe tree size hierarchy (Valbuena et al. 2013), vegetation growth (Stark et al. 2012) and light availability (Lefsky et al. 2002a). Advancement in airborne LiDAR remote sensing promises reliable accuracies in the prediction of biophysical

stand properties (Lefsky et al. 2002b; Valbuena et al. 2020) and various studies have evaluated and found that the pre-stratification of forests using airborne LiDAR can improve the attribute estimation (Næsset 2002; Maltamo et al. 2015) and reduce the sampling efforts (Papa et al. 2020). Following the same concept but using solely the LIDAR data as opposed to using field information, in this study different FST were obtained from the direct classification of airborne LiDAR data. We applied rule-based pre-stratifications and used $L_{cv}(GC_H)$ and L_{skew} of the LiDAR echo heights which are the two prominent LiDAR metrics in separating the even from uneven sized structures and oligophotic/closed canopy from euphotic/open canopy forest areas, respectively (Valbuena et al. 2017a). In Figure 4a, we found that the young, advanced and mature development classes which have similar diameters and basal areas distributions $(GC_{BA} < 0.5)$ usually backscatter most of the LiDAR returns and hold smaller variance in their height values were mostly separated by the lower values of $L_{cv}(GC_H) < 0.33$. There is a consistency on results in Table 1 showing that LiDAR values of GC_H are reflected by higher values in GC_{BA} , with the proofs in **Appendix A** being the explanation for this effect. A notable exception is observed in the case of the sapling development, which showed a high uncertainty in terms of GC, with a wide range of values in both GC_{BA} and GC_H (**Table 1**). This is the reason that L_{skew} was important to add as an additional LiDAR metric because the similarity between GC_{BA} (Valbuena et al. 2013) and GC_{H} (L_{cv}) only occurs if the higher values of GC is due to the presence of canopy gaps which allow large a portion of laser pulses to pass and disperse in the canopy (Stark et al. 2012, Valbuena et al. 2017a). Thus, by looking at the L_{skew} values, the sapling was separated as euphotic/open canopy areas ($L_{skew} > 0$) which could be the reason of the higher L_{cv} values. Other development classes such as seed-tree and multi-storey areas were separated as even sized by both GC_{BA} (0.73 and 0.92) and GC_{H} ($L_{cv} = 0.58$ and 0.58), however, the shelterwood development class wherein the mean GC_{BA} was 0.95 was not properly separated and many plots were below $L_{cv}(GC_H) = 0.33$ (Figure 4 and Table 1). This

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might be due to the omission of the understory vegetation by the lower point density of the ALS data in our study area (0.91 points.m⁻²) and any pointy density lower than at least 3 points.m⁻² are unsuitable for the structural heterogeneity assessment, using the GC in particular (Adnan et al. 2017). Thus, the disintegration of such classes could further be improved by increasing the pulse density of the LiDAR data (Gobakken and Næsset 2008; Ruiz et al. 2014). When laser pulses hit a closed canopy vegetation, only a small portion of pulses penetrate the canopy, which is represented by LiDAR height distributions with negative asymmetry L_{skew} < 0. This also indicates the shady/oligophotic areas where only a smaller portion of light will reach the ground, for example, young, advance and mature development classes. Similarly, areas where smaller portion of LiDAR returns due to the presence of sparse vegetation denotes the open/euphotic areas which were detected by $L_{skew} > 0$, for example, seedlings, saplings, seed trees, shelterwood and multi-storey (Figure 4b and Table 1). Figure 5 further highlights the importance of this rule-based classification and presents an adequate comparison between the even and uneven sized forest structures separated by the $GC_H(L_{cv}) = 0.33$, or $GC_{BA} = 0.5$ (Appendix A). In this figure, it is clear that the diameter and basal area weighted distributions in both even sized and uneven sized structure which are obtained from the GC_H (Figure 5a and **5b**) and GC_{BA} (Figure 5c and 5d) are very similar and the small differences are due to missing detection of seedling in the smallest size class. This provides further insights that GC_H is an appropriate option to separate structural heterogeneity of forest.

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4.3 Selection of best subsets of airborne LiDAR predictors in the AGB prediction models

Various alternatives are used to select the optimum number of parameters (predictors) to predict a response variable such as best subset, stepwise, and nearest neighbor (MSN) selection methods (Næsset et al. 2002; Van Aardt et al. 2008; Asner et al. 2010; Valbuena et al. 2017b, Almeida et al. 2019a). We used the best subset method which because the selection of a given

variable is independent of interactions among variables as they are selected (Hudak et al. 2006). Thus, the selection of the six predictors was independent from the other LiDAR metrics and the different modelling options, yet reaching several convergences. Minimizing the number of meaningful predictors that describe various aspects of the forest structures is an important consideration (Hudak et al. 2006, Asner and Mascaro 2014; Vincent et al. 2014; Bouvier et al., 2015; Valbuena et al. 2017b), and our selection of six predictors to allow model comparison (Table 2) was a compromise balance between model error and overfitting that worked well for all the options. The results obtained in variable selection are as valuable as the accuracy assessment itself, since it shows convergences between some areas of the forest and discrepancies between opposing FSTs. They also show which FSTs influence more the general model, with effects both in the overall error but also biasing effects in the areas of the forest that had a lower influence in the composition of the general model. Cover metrics were important in all model but more predominant in oligophotic areas. The variance of LiDAR return heights was only selected in the uneven sized structures and euphotic/open canopy areas. Different height percentiles were influential in different FST-specific models, with the median (50th height percentile) being important in the even sized and oligophotic structures, and higher percentiles (70th or 99th, representing dominant trees) becoming selected in the uneven sized structure and euphotic areas (Adnan et al. 2017). Most importantly, the variables selected in the general model were highly influenced by the even-sized areas of the forest, with both models presenting large similarities (Table 2), which is a good explanation for the results observed in the accuracy assessment, since the general model showed lesser error in those areas and high levels of biasness in the remaining FSTs. All these demonstrate the superiority of obtaining FST-specific models to predict forest AGB from LiDAR, as opposed to approaches seeking a single model valid for all forest areas.

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4.4 Comparison of the aboveground biomass predicted in the whole data without stratification and each pre-stratified FSTs

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In addition to the typical statistics employed to evaluate the quality of AGB predictions, namely MD and RMSD (Van Aardt et al. 2008; Kankare et al. 2013; Straub et al. 2013; Räty et al. 2018), we also employed an evaluation of the inflation of error in cross-validation (the SSR) and hypothesis test of 1:1 correspondence between observed and predicted AGB to enhance the reliability of our resulting models (Valbuena et al. 2017b). Considering the results obtained for whole dataset with either alternative, the 37.4 Mg·ha⁻¹ RMSD of the general model (**Table 3**), was improved by the FST-specific model approaches, reaching 34.9 Mg·ha⁻¹ (**Table 4a**), and 33.2 Mg·ha⁻¹ (**Table 4b**). Considering results obtained by FST, all figures also show improvements, even and even-sized areas where RMSDs improved from the 37.1 Mg·ha⁻¹ (**Table 3**) to 34.6 Mg·ha⁻¹ (**Table 4a**), with only a slight increase in MD. This is very important, as otherwise result in FST-wise MDs for the general model showed bias effects in forest areas highly structured. This is explained by the higher influence that even-sized areas had in the general model, possibly because LiDAR metrics have a larger explanatory capacity for AGB in these areas, thus showing potential harmful consequences in AGB modelling approaches neglecting the effects of forest structure. While the accuracies in AGB prediction improved only moderately in the FST-specific models as compared to the general model, the differences observed in the selection of airborne LiDAR predictors in each model can be critical, as they can produce biased results at specific areas of the forest. We thus encourage the prior classification into different FSTs for selecting the most relevant LiDAR predictors at each area of the forest, which besides of improving the estimation of AGB could provide important ecological insights on forest dynamics such as regeneration (Valbuena et al. 2013), selfthinning (Coomes and Allen, 2007) or productivity (Bourdier et al. 2016), and reduce the sampling efforts needed for a given level of accuracy (Papa et al. 2020), assisting in better forest inventory, management and planning (Næsset 2002; Maltamo et al. 2015). Thus, the improved *AGB* prediction approach is suitable for purposes such as quantification of carbon stock for REDD activities for a large forest area, but also for a better forest management, planning and understanding of the natural dynamics within a large forest area.

5. Conclusions

Our results demonstrate the superiority of obtaining FST-specific models to predict forest *AGB* from LiDAR, as opposed to approaches seeking a single model valid for all forest areas. We recommend the use of LiDAR information to pre-stratify the forest area prior to the field campaign, so that forest data acquisition can be tailored to the structural characteristics of the area. In order to determine these structural characteristics, we defended the use of *GC* above the use of FHD, being less computationally demanding but also conceptually better. **Appendix A** provides a mathematical framework for determining maximum entropy in 3D remote sensing datasets based on the *GC* of theoretical continuous distributions, intended to replace FHD as entropy measure in one-dimensional LiDAR vertical profiles (1D), with extensions to higher order dimensions bi- or three-dimensional (2D or 3D).

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- Appendix A. Proofs for maximum entropy thresholds corresponding to $GC_X = 0.33$ and
- 506 $GC_{X^2} = 0.50$.

- Let X be a random variable taking values in the set of positive numbers, and E[X] its
- expectation. Let $f_X(x)$ and $F_X(x)$ be their probability density function (p.d.f.) and cumulative
- distribution function (c.d.f.), respectively, and further let $F_X^{-1}(p)$ be the quantile function
- (inverse of the c.d.f.; its generalized definition is $F_X^{-1}(p) = \inf\{x : p \le F(x)\}$). The Lorenz
- curve $L_X(p)$ specifies the accumulated proportion of the total of X that is attributed to a given
- accumulated share of the population ordered by increasing X. Thus, the Lorenz curve provides
- a mapping from interval [0,1] to interval [0,1], where the domain includes the proportion from
- the ordered population and the codomain the share of X. The Lorenz curve can be written as

515 (A.1)
$$L_X(p) = \frac{\int_0^p F^{-1}(t)dt}{E[X]}$$
, for $0 \le p \le 1$

- The Gini coefficient is the twice area between the Lorenz curve and the diagonal line $L_X(p) =$
- p, which is thus assessed with the integral:

518 (A.2)
$$GC_X = 1 - 2 \int_0^1 L_X(p) dp$$

- The Lorenz curve for aX for a positive constant a is the same as that of X. Therefore the Lorenz
- 520 curve and Gini coefficient have the property of being invariant under linear scaling of X by a
- 521 positive constant.
- In applications using the distribution LiDAR heights X = H, the Lorenz curve $L_H(p)$ specifies
- 523 the proportion of total accumulated heights at the 100p % of lower (or higher) vertical strata.
- In forest science, from the distribution of tree diameters X = D, the Lorenz curve $L_D(p)$ gives
- 525 the proportion of total accumulated diameters for the 100p % smallest (or largest) trees. It is
- bowever more common to use variables which are logical to accumulate, such as basal area
- 527 X = BA or above-ground biomass X = AGB, as it is more useful to know the proportion of
- basal area or biomass accumulated from for the 100p % smallest (or largest) trees. These

variables are however never measured directly, and instead derived from a transformation of D or H, or both (Mehtätalo and Lappi, 2020). The following proofs demonstrate: (1) the threshold $GC_X = 0.33$ denotes maximum entropy for unidimensional measures, i.e. D or H; and (2) that this value of maximum entropy for D derives into $GC_{X^2} = 0.50$ for the transformed variable $Z = X^2$, namely the bi-dimensional measure BA, as it was empirically devised in Valbuena et al. (2012).

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- Proofs for the Lorenz curve and Gini Coefficient of a uniformly distributed variable
- (maximum entropy) 537
- The continuous uniform distribution $U(x_{\text{max}}, x_{\text{min}})$ has equal probability density for any u-538 length interval [x, x + u] within the range $X \in [x_{\min}, x_{\max}]$. It has the maximum entropy 539
- 540 among all continuous distributions which have the same range (Sung and Bera, 2009). Thus,
- for a given range $\theta = x_{\text{max}} x_{\text{min}}$ and a given number of strata θ/u considered, the uniform

distribution yields the maximum value of Shannon's (1848) entropy index (Valbuena et al.

- 2012). In applications using LIDAR heights, this is a vertical profile showing even proportions 543
- for all strata, yielding a maximum value for McArthur & McArthur's (1961) foliage height 544
- diversity, with $x_{\min} = 0$ being the ground level and $x_{\max} = \theta$ being the maximum height of 545
- vegetation. 546
- The continuous uniform distribution $X \sim U(0, \theta)$ has the p.d.f.: 547

548 (A.3)
$$f_X(x;\theta) = \begin{cases} 1/\theta, & \text{for } 0 \le x \le \theta \\ 0, & \text{otherwise} \end{cases}$$

549 The c.d.f. is:

550 (A.4)
$$F_X(x;\theta) = \begin{cases} 0, \text{ for } x < 0 \\ x/\theta, \text{ for } 0 \le x \le \theta \\ 1, \text{ for } \theta \le x \end{cases}$$

The quantile function and expected value are: 551

552 (A.5)
$$F_X^{-1}(p) = \theta p$$

553 (A.6)
$$E[X](=\mu) = \frac{\theta}{2}$$

Substituting these in Eq. (A.1), the Lorenz curve becomes (Figure A.1):

555 (A.7)
$$L_X(p) = \frac{\int_0^p \theta t \, dt}{\theta/2} = \frac{\theta p^2/2}{\theta/2} = p^2$$

And thus, substituting in Eq. (A.2), the Gini coefficient of a uniform distribution becomes:

557 (A.8)
$$GC_X = 1 - 2 \int_0^1 p^2 dp = 1 - \frac{2}{3} = \frac{1}{3}$$

- Hence, any variable X that has the minimum of zero and is distributed evenly along all its
- values, such as D or H, would have $GC_X = 0.33$, which thus is the value of Gini Coefficient
- which corresponds to maximum entropy.
- ***approximate position of Figure A.1****
- 562 Proofs for the Lorenz curve and Gini Coefficient of the second power of uniformly distributed
- 563 *variable*
- Next, we will proceed to deduce the Lorenz curves $L_{BA}(p)$ and Gini coefficient GC_{BA} values
- for basal areas that derive from this situation of maximum entropy in the distribution of tree
- diameters. The basal area is directly calculated from a transformation of the diameters BA = A
- 567 aD^2 . As per the scale-invariability property of Lorenz curves the scalar a can be further
- disregarded, and thus we now consider the Lorenz curve and Gini coefficient of transformation
- 569 $Z = X^2 \text{ when } X \sim U(0, \theta).$
- 570 The c.d.f. and p.d.f of the transformed variable are:

571 (A.9)
$$F_{X^2}(z;\theta) = \begin{cases} 0, \text{ for } z \le 0 \\ \sqrt{z}/_{\theta}, \text{ for } 0 \le z \le \theta^2 \\ 1, \text{ for } z \ge \theta^2 \end{cases}$$

572 (A.10)
$$f_{X^2}(z;\theta) = \begin{cases} \frac{1}{2\theta\sqrt{z}}, & \text{for } 0 \le z \le \theta^2 \\ 0, & \text{otherwise} \end{cases}$$

Thus, the quantile function and expected value of Z are:

574 (A.11)
$$F_{X^2}^{-1}(p) = \theta^2 p^2$$

575 (A.12)
$$E[X^2] = \frac{\theta^2}{3}$$

576 Substituting these in Eq. (A.1), the Lorenz curve becomes (Figure A.1):

577 (A.13)
$$L_{X^2}(p) = \frac{\int_0^p \theta^2 t^2 dt}{\theta^2/3} = \frac{\theta^2 p^3/3}{\theta^2/3} = p^3$$

And thus, substituting in Eq. (A.2), the Gini coefficient of a uniform distribution becomes:

579 (A.14)
$$GC = 1 - 2 \int_0^1 p^3 dp = 1 - \frac{2}{4} = \frac{1}{2}$$

Hence, for any variable $Z \propto X^2$ that is proportional to the second power of X, such as of BA

is to *D*, the $GC_{X^2} = 0.50$ corresponds to the maximum entropy of *X*.

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Table 1. Aboveground biomass and other forest attributes calculated at each forest development class.

			AGB (Mg·ha ⁻¹)	QMD (cm)	GC_{BA}	<i>N</i> (trees·ha⁻¹)	GC_H / L_{cv}	L_{skew}
		Min	2.48	0.10	0.00	13909	0.07	0.14
	Seedlings	Mean	7.96	0.10	0.00	44770	0.23	0.31
	Securings	Max	28.51	0.10	0.00	182522	0.54	0.70
		SD	5.14	0.00	0.00	32987	0.09	0.13
	Saplings	Min	6.14	0.10	0.00	1601	0.20	-0.18
		Mean	34.88	3.05	0.35	31852	0.42	0.21
		Max	112.48	6.93	0.89	110774	0.60	0.59
		SD	24.62	1.78	0.29	24754	0.12	0.20
		Min	13.09	6.23	0.25	864	0.15	-0.36
	Young	Mean	79.91	10.00	0.43	3254	0.29	-0.11
	1 oung	Max	160.01	14.44	0.66	6523	0.58	0.33
		SD	31.67	2.18	0.09	1475	0.11	0.17
7.0		Min	49.56	12.68	0.15	314	0.09	-0.41
lass	Advanced	Mean	96.98	17.27	0.42	1003	0.28	-0.20
t C		Max	182.76	22.15	0.63	2082	0.50	0.14
Development Class	_	SD	30.26	2.63	0.14	462	0.10	0.13
udo	Mature	Min	73.75	16.07	0.19	314	0.09	-0.48
velc		Mean	179.07	23.35	0.49	844	0.23	-0.21
De		Max	410.55	32.44	0.68	1807	0.41	0.00
		SD	76.81	4.60	0.17	374	0.08	0.11
	Shelterwood	Min	23.15	3.32	0.79	9020	0.21	-0.36
		Mean	171.01	5.63	0.95	33935	0.36	0.07
		Max	305.34	9.25	1.00	108805	0.57	0.26
		SD	83.39	1.65	0.06	24028	0.10	0.15
	Seed Trees	Min	23.65	2.29	0.11	117	0.14	-0.23
		Mean	70.43	14.76	0.73	9833	0.58	0.37
		Max	143.52	38.14	0.99	39601	0.85	0.90
		SD	28.29	12.14	0.35	11209	0.21	0.31
		Min	17.99	1.41	0.68	2219	0.20	-0.22
	Multi-	Mean	77.02	3.87	0.92	33279	0.58	0.30
	Storied	Max	271.39	9.60	0.99	78131	0.84	0.83
		SD	54.73	2.19	0.09	16382	0.16	0.30

AGB: aboveground biomass; QMD: quadratic mean diameter; GC_{BA} : Gini coefficient of basal area; GC_H : Gini coefficient of LiDAR; L_{cv} : L-coefficient of variation of LiDAR heights; L_{skew} : L-skewness of LiDAR heights SD: standard deviation

Predictors	General	$GC_H(L_{cv})$		L_{skew}	
	Model	Even	Uneven	Oligophotic	Euphotic
		(<0.33)	(>0.33)	(<0)	(>0)
Variance	*		*		*
Median of the absolute deviations	*	*		*	
(MAD) from the overall mode	4.	*		4	
MAD from the overall median					*
L.skewness		*			
Average absolute deviation (AAD)			*		
Cubic mean					*
Quadratic mean		*			
25th height percentile	*				
50th height percentile	*	*		*	
60th height percentile					*
70th height percentile			*		
99th height percentile			*		*
% first returns above 0.1m			*		
% all returns above 0.1 m				*	
% all returns above mean				*	
% first returns above mode		*		*	
Ratio returns above 0.1 m /	*	*	*		*
total first returns	T	T	r		ጥ
Canopy relief ratio	*			*	

Table 3. Accuracy assessment of the observed and predicted aboveground biomass of the general model.

	Whole -	GC_H ((L_{cv})	L_{skew}		
	Data	Even (<0.33)	Uneven (>0.33)	Oligophotic (<0)	Euphotic (>0)	
Sample size	244	120	124	119	125	
MD	-3.55	-2.09	-4.97	-4.56	-4.31	
MD (%)	-3.95	-2.33	-5.54	-5.08	-4.81	
RMSD	37.4	37.1	37.6	37.6	37.3	
RMSD (%)	41.7	41.4	41.9	41.9	41.6	
SSR	1.03	1.02	1.04	1.04	0.98	

 $\overline{GC_H(L_{cv})}$: Gini coefficient/L-coefficient of variation of LiDAR heights; L_{skew} : L-skewness of LiDAR heights; MD: mean difference; RMSD: relative mean square difference;.

Table 4. Accuracy assessment of the observed and predicted aboveground biomass of each forest structural type specific models.

(a) Even versus uneven-sized structure

	Whole Data	$GC_H(L_{cv})$		
	whole Data	Even (<0.33)	Uneven (>0.33)	
Sample size	244	120	124	
MD	-2.52	-2.30	-2.72	
MD (%)	-2.81	-2.57	-3.03	
RMSD	34.9	34.6	35.3	
RMSD (%)	38.9	38.6	39.4	
SSR	0.97	0.96	0.99	

(b) Oligophotic/closed canopy versus euphotic/open canopy areas

		L_{skew}				
	Whole Data	Oligophotic (<0)	Euphotic (>0)			
Sample size	244	119	125			
MD	-2.37	-2.22	-2.52			
MD (%)	-2.64	-2.48	-2.81			
RMSD	33.2	33.5	32.9			
RMSD (%)	37.0	37.4	36.7			
SSR	0.98	0.98	0.98			

 $GC_H(L_{cv})$: Gini coefficient/L-coefficient of variation of LiDAR heights; L_{skew} : L-skewness of LiDAR heights; MD: mean difference; RMSD: relative mean square difference; SSR: sum of square ratio.

893 Figure Captions

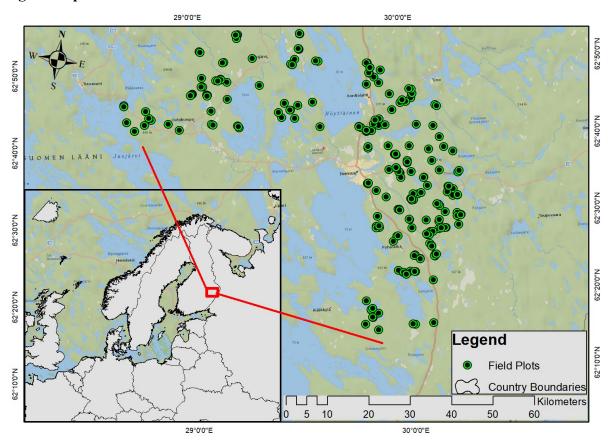


Figure 1. Map of the North Karelia Region, Finland (study area).

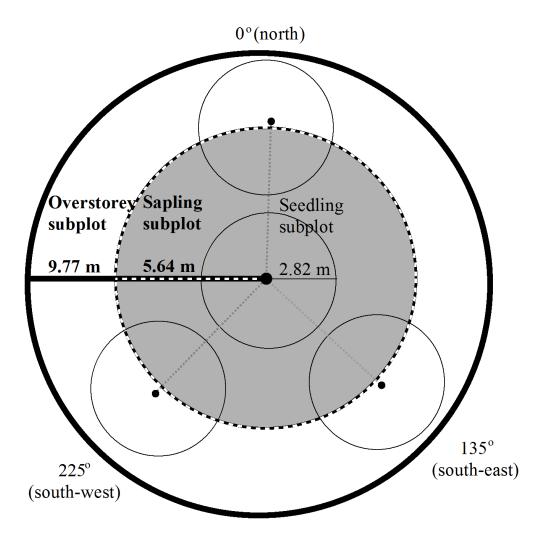


Figure 2. Plot design for field data collection.

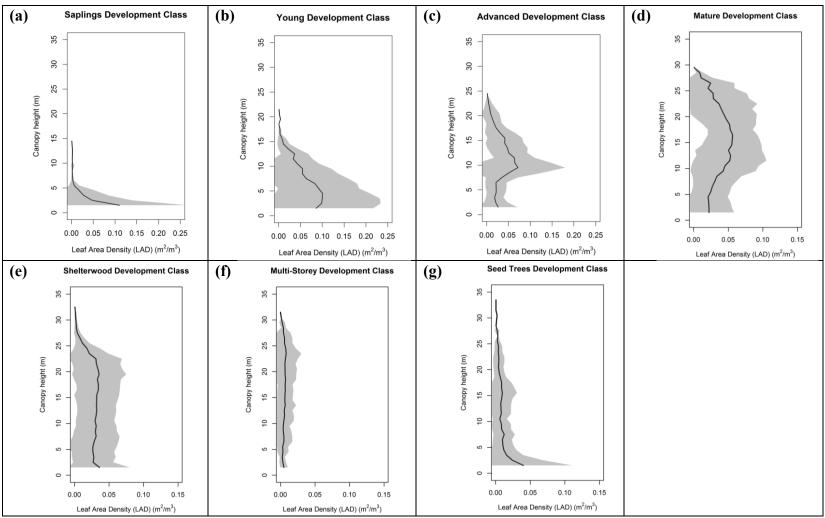


Figure 3. Mean leaf area density (LAD) profiles calculated directly from LiDAR data for each development class (a) Sapling (b) Young (c) Advanced (d) Mature (e) Shelterwood (f) Multi-storey and (g) Seed trees. Lines show mean LAD of all plots and grey areas their 95% confidence intervals.



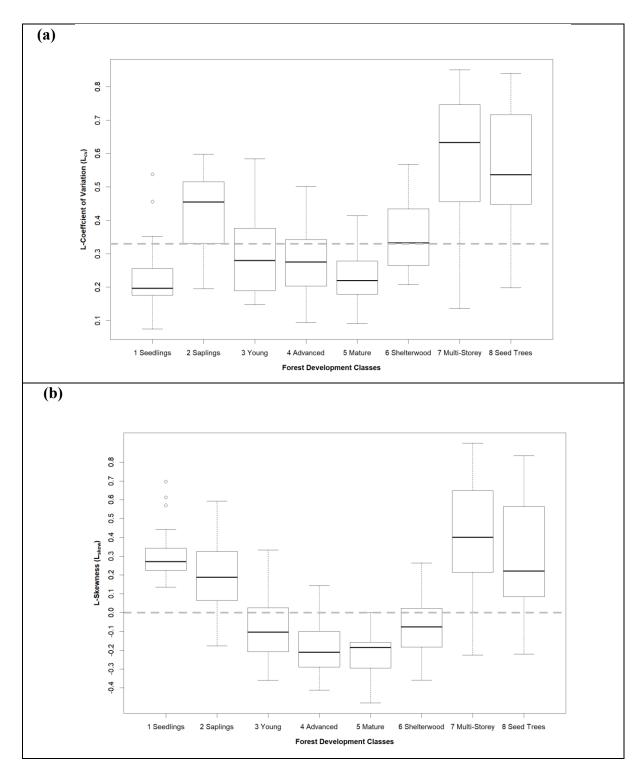


Figure 4. Distribution of different forest development classes on either side of the (a) $L_{cv}(GC_H) = 0.33$ and (b) $L_{skew} = 0$.

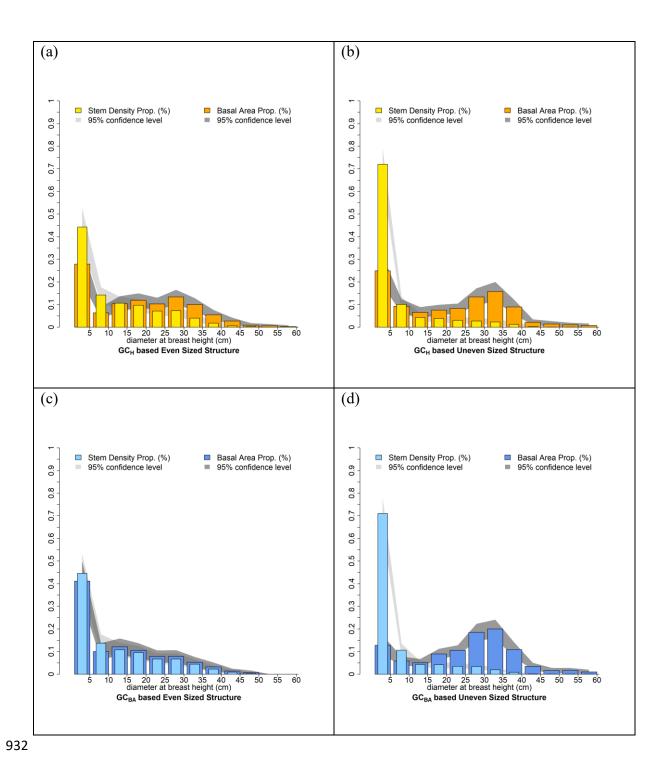


Figure 5. Comparison of diameter and basal area distribution in the even and uneven sized forest structural types separated by Gini coefficient of LiDAR ($GC_H(L_{cv}) = 0.33$) (a, b) and Gini coefficient of basal area ($GC_{BA} = 0.5$) (c, d).

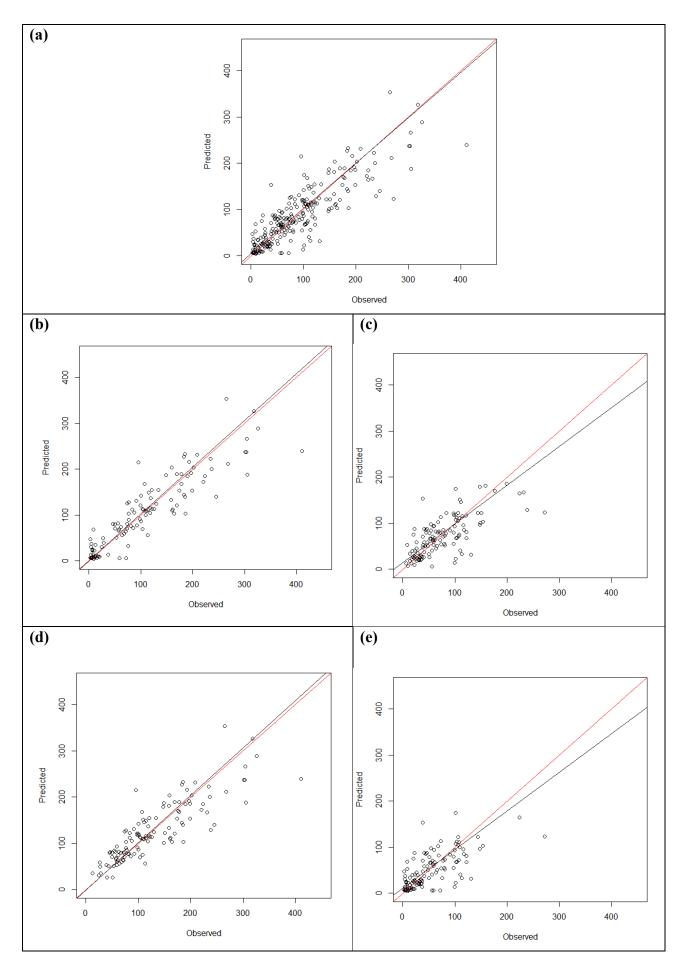


Figure 6. Observed vs predicted aboveground biomass (Mg·ha⁻¹) plots of the kNN imputation method using general model for (a) whole data without pre-stratification and each forest structural types obtained directly from airborne LiDAR classification such as (b) even sized, (c) uneven sized, (d) oligophotic/closed canopy and (e) euphotic/open canopy. The red line represents 1:1 correspondence and the black line shows linear regression fit between observed and predicted values.

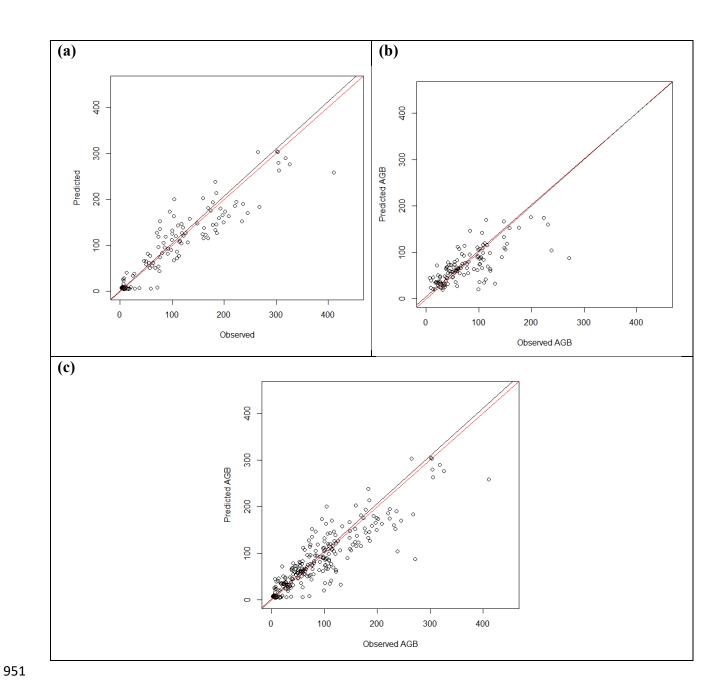


Figure 7. Observed vs predicted aboveground biomass (Mg·ha⁻¹) plots of the kNN imputation method using specific models developed for (a) even sized and (b) uneven sized forest structure and their combination for the (c) whole data. The red line represents 1:1 correspondence and the black line shows linear regression fit between observed and predicted values.

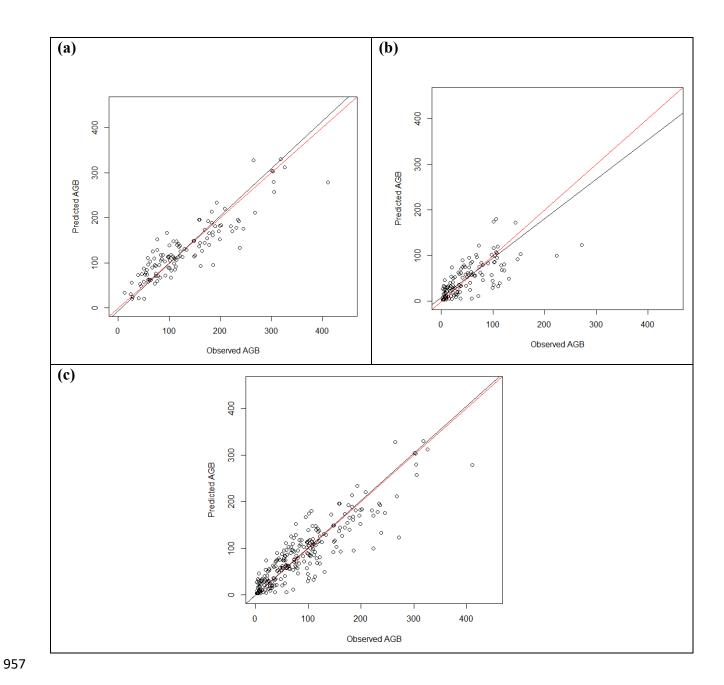
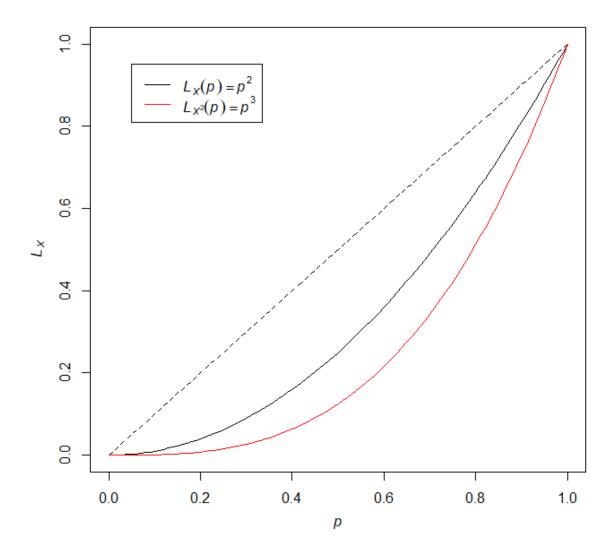


Figure 8. Observed vs predicted aboveground biomass (Mg·ha⁻¹) plots of the kNN imputation method using specific models for (a) oligophotic areas/closed canopies and (b) euphotic areas/open canopies and their combination for the (c) whole data. The red line represents 1:1 correspondence and the black line shows linear regression fit between observed and predicted values.



966 Figure A1. Lorenz curves of maximum entropy for X, and its transformed variable $Z \propto X^2$.