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Visual Servoing using the Sum of Conditional Variance

Bertrand Delabarre and Eric Marchand

Abstract—In this paper we propose a new way to achieve direct visual servoing. The novelty is the use of the sum of conditional variance to realize the optimization process of a positioning task. This measure, which has previously been used successfully in the case of visual tracking, has been shown to be invariant to non-linear illumination variations and inexpensive to compute. Compared to other direct approaches of visual servoing, it is a good compromise between techniques using the illumination of pixels which are computationally inexpensive but non robust to illumination variations and other approaches using the mutual information which are more complicated to compute but offer more robustness towards the variations of the scene. This method results in a direct visual servoing task easy and fast to compute and robust towards non-linear illumination variations. This paper describes a visual servoing task based on the sum of conditional variance performed using a Levenberg-Marquardt optimization process. The results are then demonstrated through experimental validations and compared to both photometric-based and entropy-based techniques.

I. INTRODUCTION

Visual servoing uses the information provided by a vision sensor to control the movements of a dynamic system [10], [1], [2]. This approach requires to extract and track visual information (usually geometric features) from the image in order to design the control law. This difficult tracking process is one of the bottlenecks in the development of visual servoing techniques.

Recent works have tried to circumvent these problems by using directly the information provided by the entire image [13], [7], [12], [4], [6]. Features are no longer extracted from the image. Those works have began with [13] and [7], where the images were reduced to eigenspaces. Later works have used directly the whole images. In [4], a control law was proposed that minimizes the error between the current image and the desired one. In that case the vector of visual feature in nothing but the image itself and the error to be regulated is the sum of squared differences (the SSD). This approach features many advantages: it does not require any matching or tracking process. Furthermore since the image measurements are nothing but the pixel intensity, there are no error in the feature extraction process leading to a very precise realization of the task.

Nevertheless, considering image intensities is quite sensitive to modification of the environment [4] and more robust registration function have to be considered. [3] use a full reflection model to tackle complex illumination changes thus creating the possibility to take into account some non-global illumination changes (occurrence of specularities, lighting

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direction non constant wrt. the surface, etc). But this method is limited since the range of application only applies to illumination conditions that can be represented with the considered model. A more recent approach also considered the mutual information [15] as the similarity measure between desired and current images [6]. This information theoretic method allows to servo the camera in order to maximize the quantity of information shared by the current and desired image (that is the mutual information which is build by a measure of image entropy [15]). The approach is therefore well suited for a large range of variations such as occlusions, specularities and even different modality images. A drawback of this method is that it is quite complex to compute and therefore computationally expensive.

In this paper we propose a compromise between this two branches. Our method is based on the sum of conditional variance, a measure using the probability distribution functions of the luminance in the image to adapt a template. When considering direct visual servoing method, the choice of the similarity function is fundamental. Between the simplest alignment function that is the sum of squared differences [4] and the mutual information [6], one can consider other metric such as the Zero-mean Normalized Cross Correlation (or ZNCC [11]) which has proved to be very robust to linear brightness variation [8] thanks to the normalization embodied into the ZNCC. In this paper, to be able to handle non-linear brightness variation and to have a low computational complexity, we propose to consider, as a similarity function, the sum of conditional variance (or SCV). With respect to the simple SSD function, SCV allows to dynamically adapt the reference image to the illumination conditions of the current image acquired by the camera. The reference image is replaced by an expected image computed using a probabilistic expectation operator (that take into account illumination condition in both current and learned desired image). Let us note that this approach has proved recently to be very efficient in a tracking context as demonstrated in [14].

Dynamically adapting the desired image makes the approach able to tackle brutal illumination variations. Furthermore, this approach is computationally very efficient since it is still based on a simple difference between pixels. It is also easy and fast to compute which makes it a good solution for visual servoing tasks involving illumination variations of the scene.

In this paper we will first have a quick reminder of the direct visual servoing methods before describing the new method based on the sum of conditional variance. Several experiments are then exposed, showing the advantages and limitations of the approach.

II. DIRECT VISUAL SERVOING

A. Positioning Task

The aim of a positioning task is to reach a desired pose of the camera \mathbf{r}^* , starting from an arbitrary initial pose. To achieve that goal, one needs to define a cost function that reflects, in the image space, this error. Most of the time this cost function f is an error measure which needs to be minimized. Considering the actual pose of the camera \mathbf{r} the problem can therefore be written as an optimization process:

$$\widehat{\mathbf{r}} = \arg\min_{\mathbf{r}} f(\mathbf{r}, \mathbf{r}^*) \tag{1}$$

where $\hat{\mathbf{r}}$, the pose reached after the optimization process (servoing process), is the closest possible to \mathbf{r}^* (optimally $\hat{\mathbf{r}} = \mathbf{r}^*$). For example, considering a set of geometrical features \mathbf{s} , the task will typically have to minimize the difference between $\mathbf{s}(\mathbf{r})$ and the desired configuration \mathbf{s}^* which leads to:

$$\hat{\mathbf{r}} = \arg\min_{\mathbf{r}} (\mathbf{s}(\mathbf{r}) - \mathbf{s}^*).$$
 (2)

This visual servoing task is achieved by iteratively applying a velocity to the camera. This requires the knowledge of the interaction matrix $\mathbf{L_s}$ of $\mathbf{s(r)}$ that links the variation of $\dot{\mathbf{s}}$ to the camera velocity and which is defined as:

$$\dot{\mathbf{s}}(\mathbf{r}) = \mathbf{L}_{\mathbf{s}}\mathbf{v} \tag{3}$$

where \mathbf{v} is the camera velocity.

This equation leads to the expression of the velocity that needs to be applied to the robot. The control law is classically given by:

$$\mathbf{v} = -\lambda \mathbf{L}_{\mathbf{s}}^{+}(\mathbf{s}(\mathbf{r}) - \mathbf{s}^{*}) \tag{4}$$

where λ is a positive scalar.

B. Photometric visual servoing

In the case of direct visual servoing, the feature s becomes the image itself (s(r) = I(r)). This means that the optimization process becomes [4]:

$$\widehat{\mathbf{r}} = \arg\min_{\mathbf{r}} (\mathbf{I}(\mathbf{r}) - \mathbf{I}^*) \tag{5}$$

where I(r) and I^* are respectively the image seen at the position r and the template image (both of N pixels). The control law is inspired by the Levenberg-Marquardt (LM) optimization approach. It is given by:

$$\mathbf{v} = -\lambda (\mathbf{H}_{\mathbf{I}} + \mu \ diag(\mathbf{H}_{\mathbf{I}}))^{-1} \mathbf{L}_{\mathbf{I}} (\mathbf{I}(\mathbf{r}) - \mathbf{I}^*)$$
 (6)

where λ and μ are positive scalars where $\mathbf{H_I} = \mathbf{L_I}^T \mathbf{L_I}$ and $\mathbf{L_I}$ is the interaction matrix which can be expressed as:

$$\mathbf{L}_{\mathbf{I}} = -\nabla \mathbf{I}^{\mathbf{T}} \mathbf{L}_{\mathbf{x}} \tag{7}$$

and L_x is the interaction matrix of a point (see details in [4]).

III. VISUAL SERVOING USING THE SUM OF CONDITIONAL VARIANCE

A. Sum of Conditional Variance

The works of [4] used the sum of squared differences to perform direct visual servoing. The main drawback of this method is that it is based on the hypothesis that the luminance of a point does not vary with time:

$$\mathbf{I}(\mathbf{x} + \mathbf{dx}, t + dt) = \mathbf{I}(\mathbf{x}, t) \tag{8}$$

where \mathbf{x} represents the pixel coordinates and \mathbf{dx} the motion underwent by the image during the laps of time dt. When performing a visual servoing task, this hypothesis is often violated and, as the light changes in the scene, the task can quickly fail. This is the reason why this paper describes a visual servoing process using the Sum of Conditional Variance (SCV), a measure which was used in [14] to track planar object using a KLT like approach with very good results in illumination-varying conditions. As in our case, this measure was used in [14] because it no longer relies a simple difference between current and a reference image (or template image). Indeed, the template is dynamically adapted to the illumination conditions of the current image seen at each new iteration. To adapt the template, an expected image $\hat{\mathbf{I}}$ is defined as:

$$\hat{\mathbf{I}}(\mathbf{x}) = \mathcal{E}(\mathbf{I}(\mathbf{x}) \mid \mathbf{I}^*(\mathbf{x})) \tag{9}$$

where \mathcal{E} is an expectation operator and \mathbf{x} a pixel in the image. With this expected template computed, a good correlation measure is given by:

$$SCV = \sum_{\mathbf{x}} (\mathbf{I}(\mathbf{x}) - \hat{\mathbf{I}}(\mathbf{x})). \tag{10}$$

The expected image $\hat{\mathbf{I}}$ is computed from the joint probability distribution between \mathbf{I} and \mathbf{I}^* . Those probabilities are computed from the empirical analysis of \mathbf{I} and \mathbf{I}^* . As they both have the same dynamic d, which usually is 256, for each couple of grey levels i in \mathbf{I} and j in \mathbf{I}^* it is possible to compute:

$$P_{II^*}(i,j) = P(\mathbf{I}(\mathbf{x}) = i, \mathbf{I}^*(\mathbf{x}) = j)$$
(11)
=
$$\frac{1}{N} \sum_{\mathbf{x}} \phi(\mathbf{I}(\mathbf{x}) - i) \phi(\mathbf{I}^*(\mathbf{x}) - j)$$
(12)

where $\phi(a)$ equals 1 if a=0, 0 otherwise and P_{II^*} represents the probability that a pixel **x** takes the value i in **I** and j in **I***. From this joint probability distribution, the probability distributions of **I*** can easily be found. For example the probability distribution for the apparition of a grey level j in **I*** is given by:

$$P_{I^*}(j) = \sum_{i} P_{II^*}(i,j). \tag{13}$$

From this probability distribution functions the computation of the expected grey levels in $\hat{\mathbf{I}}$ becomes, for each grey level j in \mathbf{I}^* :

$$\hat{\mathbf{I}}(j) = \sum_{i} i \frac{P_{II^*}(i,j)}{P_{I^*}(j)}.$$
 (14)

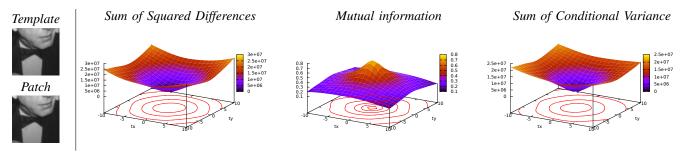


Fig. 1. Cost function in nominal case. Here the displayed current patch is the one resulting of tx = 0 and ty = 0 pixel.

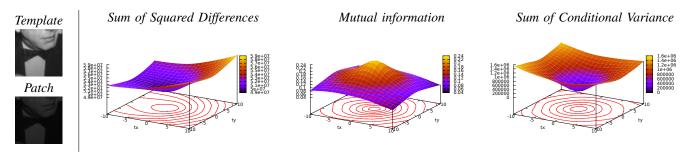


Fig. 2. Cost function when the light has been significantly lowered. The displayed current patch is the one resulting of tx = 0 and ty = 0 pixel.

B. Analysis of the SCV cost function

In order to assess the suitability of the sum of conditional variance in the case of illumination changes, a comparison of various similarity functions was realized. The comparison between two images (a reference image and a current image) follows the following pattern. On the images, a patch of 100x100 pixels is selected. The patch is extracted from the reference image, creating a reference template. In the current image, patches are extracted by moving a 100x100 window, starting from a translation (tx,ty) equal to (-10,-10) pixels with relation to the position of the template and finishing with (tx,ty) equal to (10,10) pixels. The cost function is then computed between each patch extracted and the template, leading to the shape of the cost function.

When computing the cost functions, histogram binning was used (see more details in section IV-A). The mutual information was computed with 8 bins as in [6] and the sum of conditional variance with 64 bins. A first comparison was made with both the current and reference image being the same, creating a baseline (see fig 1). This shows the shapes of the functions in the ideal case were the conditions do not vary during the visual servoing. The three cost functions possess a marked optimum when (tx,ty) equals to (0,0) pixels. They also present a smooth shape and no local extrema which make them well suited for optimization processes in nominal conditions. With that baseline established, a second comparison was made. For this comparison, the current image was not the same as the reference but had undergone a variation of the luminance rendering it darker than the reference (see fig 2). This time, the shape of the SSD is greatly impacted with a flatten area resulting in a significant shift in the extremum location which means it is not suitable for an optimization process in this conditions. The MI and SCV on the other hand show only a small attenuation of the slopes around their optimum but stay sharp enough to assure convergence toward the correct position during an optimization process.

Obviously, this analysis considers only 2 dof, whereas in the visual servoing experiments considered in this paper, the 6 camera dof are controlled. Nevertheless these experiments (along with other which can be found in [14]) allow to illustrates that SCV is far less sensitive than SSD to illumination variations.

C. SCV-based control law

Using the SCV to measure the difference between $\mathbf{I}(\mathbf{r})$ and $\mathbf{\hat{I}}$ the optimization process becomes:

$$\hat{\mathbf{r}} = \arg\min_{\mathbf{r}} (\mathbf{I}(\mathbf{r}) - \hat{\mathbf{I}}).$$
 (15)

Considering the LM approach shown in equation (6), the control law becomes:

$$\mathbf{v} = -\lambda (\mathbf{H}_{\mathbf{S}} + \mu \ diag(\mathbf{H}_{\mathbf{S}}))^{-1} \mathbf{L}_{\mathbf{SCV}} (\mathbf{I}(\mathbf{r}) - \hat{\mathbf{I}})$$
 (16)

where $\mathbf{H_S} = \mathbf{L_{SCV}}^T \mathbf{L_{SCV}}$ and $\mathbf{L_{SCV}}$ is the interaction matrix associated to the task. Only illumination variations (and not camera pose) impact $\hat{\mathbf{I}}$ the interaction matrix matrix can be chosen as in [4]:

$$\mathbf{L_{SCV}} = \frac{\partial \mathbf{I}(\mathbf{r})}{\partial \mathbf{r}} = -\nabla \mathbf{I}(\mathbf{r})^{\mathbf{T}} \mathbf{L_{x}}.$$
 (17)

IV. EXPERIMENTAL VALIDATIONS

A. Histogram Binning

To compute the probability distribution functions used by the SCV and compute for each new frame the new reference image $\hat{\mathbf{I}}$, histogram binning was used. This was done both to smooth the resulting image $\hat{\mathbf{I}}$ and to decrease the computation time in order to enhance the quality of the servoing task. To



Fig. 3. Influence of the number of bins on the predicted image when far from reach. On the left, with 8 bins the image is flattened and has lost a lot of high frequencies. 256 bins introduces more noise when the difference between I and I^* increases than 64. The frame on the borders represent the area in the image which is not included in the computation.

compute such histograms a number of bins Nc is set, then the source image is scaled:

$$\overline{\mathbf{I}}(\mathbf{x}) = \mathbf{I}(\mathbf{x}) \frac{(Nc - 1)}{d - 1}.$$
(18)

The histograms are then computed on this scaled image which dynamic is Nc, ensuring that they are composed of only Nc bins. An other reason for choosing not to use the full dynamic of the image is that computing probabilities from the histograms as in (14) results in approximating them. This is the case because an empirical observation of a probability distribution function does not necessarily equal its 'real' distribution. The main problem with those approached probabilities is that they can result in noise in the predicted image when using an important number of bins. On the other hand, if the chosen number of bins is too low, the resulting image loses a lot of details. See figure (3) for examples.

It is also interesting to note that as the number of bins decreases, so does the precision of the positioning task since more high frequency details are lost. This is why during, the servoing task the number of bins is adapted dynamically. First, the binning is done using 64 bins as the level of detail in the image is sufficient with this number of bins and increases to 256 when close from reach to get more precision. To do that, the value of the SCV at the beginning of the task is kept in memory and the switch is effected when the current SCV reaches a certain percentage of that value.

B. First Experiment: Nominal case

The first experience aims to analyze the behaviour of the SCV approach in a classical case. The positioning task controls all 6 degrees of freedom. The interaction matrix during the servoing is computed assuming that the Z coordinate of each point is constant, in this case it assumed as equal to 70 cm. As for the λ and μ parameters of the optimization, they were empirically chosen as 4 and 0.001 respectively. For the initial pose, the difference was $\Delta {\bf r} = \{16cm, -20cm, 6cm, -0.27rad, -0.19rad, -0.09rad\}$ with relation to the desired pose. Figure 4 shows the behaviour of the model during the optimization process. In

the error image between the current and expected images, a pixel of luminance l=128 (grey pixel) means there is no difference between the two images. The graphics show the evolution of a chosen parameter with relation to the iterations of the algorithm.

Several observations can be made concerning this first experiment. First, the task converges, leading the robot to the good position with a good precision of $\Delta {\bf r}^* = \{0.07mm, 0.16mm, 0.01mm, 1e^{-4}rad, 2e^{-5}rad, 1e^{-4}rad\}.$ The second observation is that the evolution of the camera location is smooth. The SCV also vanishes without being noisy, showing that the SCV is well suited in this case.

C. Second Experiment: Robustness with relation to illumination changes

The goal of this experiment is to show the robustness of our method towards illumination variations in the scene. In order to do that, after acquiring the image at the desired position, the servoing is launched after the lights have been attenuated. The results of this experiment are exposed on figure 5. The initial position was a little bit less complicated with a difference of $\Delta \mathbf{r} = \{14cm, -18cm, 1cm, -0.28rad, -0.18rad, -0.03rad\}$ from the desired position, which is still a consequent movement.

In these conditions, the servoing task still converged, thanks to the adaptation of the predicted image to the current one as we can see on figure 5. The final position was reached with a precision of $\Delta \mathbf{r}^* = \{0.4mm, 0.8mm, 0.9mm, 1e^{-3}rad, 4e^{-4}rad, 1e^{-3}rad\}$ which gives a distance to the desired position of 1.3mm. It is slightly less precise than in the nominal case but it was still a good result compared to the other methods since the SSD diverged and the mutual information showed a repositioning precision of 2.4mm. The graph of SCV also shows around iteration 300 the change in the number of bins which caused an improvement in the precision without impacting the convergence of the task.

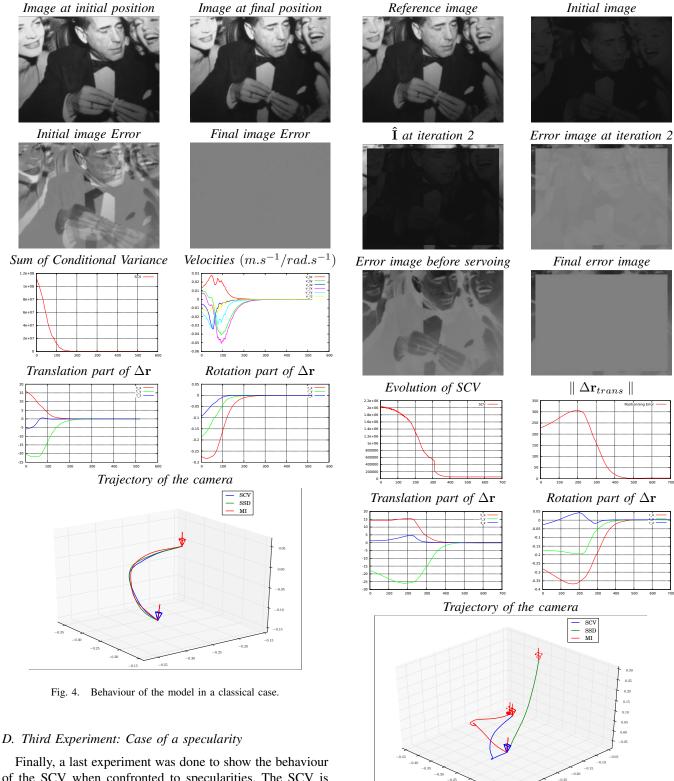


Fig. 5. Behaviour of the model in a the case of illumination variations. The evolution of the SCV shows around iteration 210 gain in precision thanks to the increase in the number of bins used.

of the SCV when confronted to specularities. The SCV is not really suited for this purpose, as local variations will change the global probabilities therefore areas where no variations occurred will be treated as areas where variations occurred which will create incoherences in the predicted image. But even if the measure is impacted by specularities, it is interesting to see how the servoing task reacts when confronted to the situation. To realize the experiment, the task was launched again from the position described in

section IV-C. Then the servoing task was launched while a light was pointed directly at the non-lambertian surface,

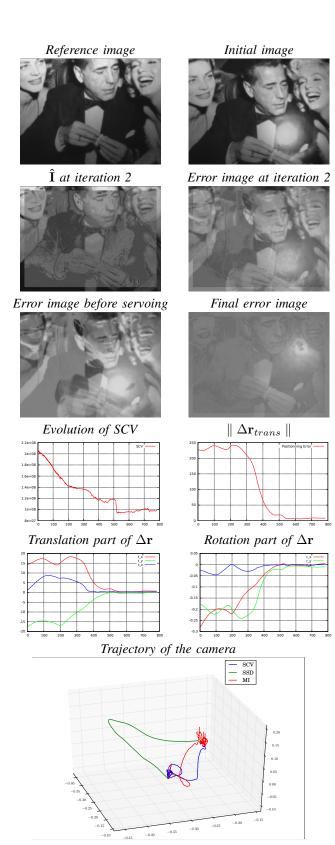


Fig. 6. Behaviour of the model in a the case of a specularity in the image.

creating a specularity in the image. The results of this experiment are shown on figure 6.

The predicted image is directly impacted, as the variations

in the probability distribution functions due to the specularity are applied to the whole considered area. The evolution of the SCV is also impacted, as the specularity in the image moves depending on the position of the camera. But even though it is lessprecise than in the nominal case, the task still converges with a distance to the goal position of 9mm when the SSD ends up at 15mm in the same conditions and the mutual information at 4mm. The analysis of $\parallel \Delta {\bf r}_{trans} \parallel$ is really interesting as it shows a shift in the minimum of the SCV because the robot came closer to the desired position before converging with a greater repositioning error.

V. CONCLUSION

In this paper we described a new way to achieve direct visual servoing. This approach is based on a similarity measure issued from the information theory called the sum of conditional variance (SCV). Compared to photometric visual servoing method [4], it performs similarly in nominal cases, when large occlusions or specularities appear in the scene and better when the illumination conditions are nonlocally changing. Compared to mutual information based visual servoing [6], the range of application is narrower for the SCV as it is less robust towards local variations and is not multi-modal. But it is easier to compute and less computationally expensive when the number of bins used for the servoing task increases. This makes it a very good compromise when performing direct visual servoing. As SCV is computed based on the image histograms, it is non-invariant to local changes. This problems could be addressed for example by using sub-regions histograms as it was mentioned in [9] or using M-estimators in the control law [5].

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