# Model-independent and quasi-model-independent search for new physics at CDF 

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Blair, ${ }^{2}$ C. Blocker, ${ }^{5}$ B. Blumenfeld, ${ }^{24}$ A. Bocci, ${ }^{15}$ A. Bodek, ${ }^{47}$ V. Boisvert, ${ }^{47}$ G. Bolla, ${ }^{46}$ A. Bolshov, ${ }^{31}$ D. Bortoletto, ${ }^{46}$ J. Boudreau, ${ }^{45}$ A. Boveia, ${ }^{9}$ B. Brau, ${ }^{9}$ L. Brigliadori, ${ }^{4}$ C. Bromberg, ${ }^{34}$ E. Brubaker, ${ }^{12}$ J. Budagov, ${ }^{14}$ H. S. Budd, ${ }^{47}$ S. Budd, ${ }^{23}$ K. Burkett, ${ }^{16}$ G. Busetto, ${ }^{41}$ P. Bussey, ${ }^{20}$ A. Buzatu, ${ }^{32}$ K. L. Byrum, ${ }^{2}$ S. Cabrera, ${ }^{15,5}$ M. Campanelli, ${ }^{34}$ M. Campbell, ${ }^{33}$ F. Canelli, ${ }^{16}$ A. Canepa, ${ }^{43}$ D. Carlsmith, ${ }^{57}$ R. Carosi, ${ }^{44}$ S. Carrillo,,${ }^{17, m}$ S. Carron, ${ }^{32}$ B. Casal, ${ }^{10}$ M. Casarsa, ${ }^{16}$ A. Castro, ${ }^{4}$ P. Catastini, ${ }^{44}$ D. Cauz, ${ }^{52}$ A. Cerri, ${ }^{27}$ L. Cerrito,,${ }^{29, q}$ S. H. Chang, ${ }^{26}$ Y.C. Chen, ${ }^{1}$ M. Chertok, ${ }^{6}$ G. Chiarelli, ${ }^{44}$ G. Chlachidze, ${ }^{16}$ F. Chlebana, ${ }^{16}$ K. Cho, ${ }^{26}$ D. Chokheli, ${ }^{14}$ J. P. Chou, ${ }^{21}$ G. Choudalakis, ${ }^{31}$ S. H. Chuang, ${ }^{50}$ K. Chung, ${ }^{11}$ W. H. Chung, ${ }^{57}$ Y. S. Chung, ${ }^{47}$ C. I. Ciobanu, ${ }^{23}$ M. A. Ciocci, ${ }^{44}$ A. Clark, ${ }^{19}$ D. Clark,,${ }^{5}$ G. Compostella, ${ }^{4}$ M.E. Convery, ${ }^{16}$ J. Conway, ${ }^{6}$ B. Cooper, ${ }^{29}$ K. Copic, ${ }^{33}$ M. Cordelli, ${ }^{18}$ G. Cortiana, ${ }^{41}$ F. Crescioli, ${ }^{44}$ C. Cuenca Almenar,, ,s, J. Cuevas, ${ }^{10, p}$ R. Culbertson, ${ }^{16}$ J. C. Cully, ${ }^{33}$ D. Dagenhart, ${ }^{16}$ M. Datta, ${ }^{16}$ T. Davies, ${ }^{20}$ P. de Barbaro, ${ }^{47}$ S. De Cecco, ${ }^{49}$ A. Deisher, ${ }^{27}$ G. De Lentdecker, ${ }^{47, \mathrm{e}}$ M. Dell'Orso, ${ }^{44}$ L. Demortier, ${ }^{48}$ J. Deng, ${ }^{15}$ M. Deninno, ${ }^{4}$ D. De Pedis, ${ }^{49}$ P. F. Derwent, ${ }^{16}$ G. P. Di Giovanni, ${ }^{42}$ C. Dionisi, ${ }^{49}$ B. 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Data collected in run II of the Fermilab Tevatron are searched for indications of new electroweak scale physics. Rather than focusing on particular new physics scenarios, CDF data are analyzed for discrepancies with respect to the standard model prediction. A model-independent approach (VISTA) considers the gross features of the data and is sensitive to new large cross section physics. A quasi-model-independent approach (SLEUTH) searches for a significant excess of events with large summed transverse momentum and is particularly sensitive to new electroweak scale physics that appears predominantly in one final state. This global search for new physics in over 300 exclusive final states in $927 \mathrm{pb}^{-1}$ of $p \bar{p}$ collisions at $\sqrt{s}=1.96 \mathrm{TeV}$ reveals no such significant indication of physics beyond the standard model.

[^1]
## I. INTRODUCTION

In the past 30 years of frontier energy collider physics, the only objects discovered were those for which the predictions were definite. The $W$ and $Z$ bosons (discovered at CERN in 1983 [1-4]) and the top quark (discovered at Fermilab in 1995 [5,6]) were well-known objects long before their discoveries, with all quantum numbers but mass uniquely specified. The present situation is qualitatively different, with plausible predictions for physics lying beyond the standard model running the gamut of possible experimental signatures.

Searches for physics beyond the standard model typically begin with a particular model. A region is selected in the data where the model's expected contribution is enhanced, and the extent to which the data (dis)favor the model is determined by comparing the prediction to data.

The state of the theoretical landscape and the vastness of most model spaces suggests the utility of searching in a different space altogether. The experimental space, defined by the isolated and energetic objects observed in frontier energy collisions, forms a natural space to consider.

This article describes a systematic and modelindependent look (VISTA) at gross features of the data, and a quasi-model-independent search (SLEUTH) for new physics at high transverse momentum. These global algorithms provide a complementary approach to searches optimized for more specific new physics scenarios.

## II. STRATEGY

The search for new physics described in this article is designed with the intention of maximizing the chance for discovery, and not excluding model parameter space if no discrepancy is found. Discrepancies between data and a complete standard model background estimate are identified in a global sample of high transverse momentum (high- $p_{T}$ ) collision events. Three statistics are employed to identify and quantify disagreement: populations of exclusive final states defined by the objects the events contain, shapes of kinematic distributions, and excesses on the tail of summed scalar transverse momentum distributions.

The VISTA [7] algorithm provides a global study of the standard model prediction and CDF detector response in the bulk of the high- $p_{T}$ data; an algorithm called SLEUTH complements this with a search for possibly small crosssection physics in the high- $p_{T}$ tails. The purpose of these algorithms is to identify discrepancies worthy of further consideration.

A claim of discovery requires convincing arguments that the observed discrepancy between data and standard model prediction
(1) is not a statistical fluctuation,
(2) is not due to a mismodeling of the detector response, and
(3) is not due to an inadequate implementation of the standard model prediction,
and therefore must be due to new underlying physics. Any observed discrepancy is subject to scrutiny, and explanations are sought in terms of the above points.

The VISTA and SLEUTH algorithms provide a means for making the above three arguments, with a high threshold placed on the statistical significance of a discrepancy in order to minimize the chance of a false discovery claim. As described later, this threshold is the requirement that the false discovery rate is less than 0.001 , after taking into account the total number of final states, distributions, or regions being examined.

This analysis employs a correction model implementing specific hypotheses to account for mismodeling of detector response and imperfect implementation of standard model prediction. Achieving this on the entire high- $p_{T}$ data set requires a framework for quickly implementing and testing modifications to the correction model. The specific details of the correction model are intentionally kept as simple as possible in the interest of transparency in the event of a possible new physics claim. VISTA's toolkit includes a global comparison of data to the standard model prediction, with a check of thousands of kinematic distributions and an easily adjusted correction model allowing a quick fit for values of associated correction factors.

The traditional notions of signal and control regions are modified. Without prejudice as to where new physics may appear, all regions of the data are treated as both signal and control. This analysis is not blind, but rather seeks to identify and understand discrepancies between data and the standard model prediction. With the goal of discovery, emphasis is placed on examining discrepancies, focusing on outliers rather than global goodness of fit. Individual discrepancies that are not statistically significant are generally not pursued.

VISTA and SLEUTH are employed simultaneously, rather than sequentially. An effect highlighted by SLEUTH prompts additional investigation of the discrepancy, usually resulting in a specific hypothesis explaining the discrepancy in terms of a detector effect or adjustment to the standard model prediction that is then fed back and tested for global consistency using VISTA.

Forming hypotheses for the cause of specific discrepancies, implementing those hypotheses to assess their wider consequences, and testing global agreement after the implementation are emphasized as the crucial activities for the investigator throughout the process of data analysis. This process is constrained by the requirement that all adjustments be physically motivated. The investigation and resolution of discrepancies highlighted by the algo-
rithms is the defining characteristic of this global analysis [8].

This search for new physics terminates when one of two conditions are satisfied: either a compelling case for new physics is made, or there remain no statistically significant discrepancies on which a new physics case can be made. In the former case, to quantitatively assess the significance of the potential discovery, a full treatment of systematic uncertainties must be implemented. In the latter case, it is sufficient to demonstrate that all observed effects are not in significant disagreement with an appropriate global standard model description.

## III. VISTA

This section describes VISTA: object identification, event selection, estimation of standard model backgrounds, simulation of the CDF detector response, development of a correction model, and results.

## A. CDF II detector

CDF II is a general purpose detector $[9,10$ ] designed to detect particles produced in $p \bar{p}$ collisions. The detector has a cylindrical layout centered on the accelerator beam line.

CDF uses a cylindrical coordinate system with the $z$-axis along the axis of the colliding beams. The variable $\theta$ is the polar angle relative to the incoming proton beam, and the variable $\phi$ is the azimuthal angle about the beam axis. The pseudorapidity of a particle trajectory is defined as $\eta=$ $-\ln (\tan (\theta / 2))$. It is also useful to define detector pseudorapidity $\eta_{\text {det }}$, denoting a particle's pseudorapidity in a coordinate system in which the origin lies at the center of the CDF detector rather than at the event vertex. The transverse momentum $p_{T}$ is the component of the momentum projected on a plane perpendicular to the beam axis.

Charged particle tracks are reconstructed in a $3.1-\mathrm{m}-$ long open cell drift chamber that performs up to 96 measurements of the track position in the radial region from 0.4 m to 1.4 m . Between the beam pipe and this tracking chamber are multiple layers of silicon microstrip detectors, enabling high precision determination of the impact parameter of a track relative to the primary event vertex. The tracking detectors are immersed in a uniform 1.4 T solenoidal magnetic field.

Outside the solenoid, calorimeter modules are arranged in a projective tower geometry to provide energy measurements for both charged and neutral particles. Proportional chambers are embedded in the electromagnetic calorimeters to measure the transverse profile of electromagnetic showers at a depth corresponding to the shower maximum for electrons. The outermost part of the detector consists of a series of drift chambers used to detect and identify muons, minimum ionizing particles that typically pass through the calorimeter.

A set of forward gas Čerenkov detectors is used to measure the average number of inelastic $p \bar{p}$ collisions per

Tevatron bunch crossing, and hence determine the luminosity acquired. A three level trigger and data acquisition system selects the most interesting collisions for offline analysis.

Here and below the word "central" is used to describe objects with $\left|\eta_{\text {det }}\right|<1.0$; "plug" is used to describe objects with $1.0<\left|\eta_{\text {det }}\right|<2.5$.

## B. Object identification

Energetic and isolated electrons, muons, taus, photons, jets, and $b$-tagged jets with $\left|\eta_{\text {det }}\right|<2.5$ and $p_{T}>17 \mathrm{GeV}$ are identified according to standard criteria. The same criteria are used for all events. The isolation criteria employed vary according to object, but roughly require less than 2 GeV of extra energy flow within a cone of $\Delta R=\sqrt{\Delta \eta^{2}+\Delta \phi^{2}}=0.4$ in $\eta-\phi$ space around each object.

Standard CDF criteria [11] are used to identify electrons $\left(e^{ \pm}\right)$in the central and plug regions of the CDF detector. Electrons are characterized by a narrow shower in the central or plug electromagnetic calorimeter and a matching isolated track in the central gas tracking chamber or a matching plug track in the silicon detector.

Standard CDF muons ( $\mu^{ \pm}$) are identified using three separate subdetectors in the regions $\left|\eta_{\text {det }}\right|<0.6,0.6<$ $\left|\eta_{\text {det }}\right|<1.0$, and $1.0<\left|\eta_{\text {det }}\right|<1.5$ [11]. Muons are characterized by a track in the central tracking chamber matched to a track segment in the central muon detectors, with energy consistent with minimum ionizing deposition in the electromagnetic and hadronic calorimeters along the muon trajectory.

Narrow central jets with a single charged track are identified as tau leptons ( $\tau^{ \pm}$) that have decayed hadronically [12]. Taus are distinguished from electrons by requiring a substantial fraction of their energy to be deposited in the hadron calorimeter; taus are distinguished from muons by requiring no track segment in the muon detector coinciding with the extrapolated track of the tau. Track and calorimeter isolation requirements are imposed.

Standard CDF criteria requiring the presence of a narrow electromagnetic cluster with no associated tracks are used to identify photons $(\gamma)$ in the central and plug regions of the CDF detector [13].

Jets $(j)$ are reconstructed using the JetClu [14] clustering algorithm with a cone of size $\Delta R=0.4$, unless the event contains one or more jets with $p_{T}>200 \mathrm{GeV}$ and no leptons or photons, in which case cones of $\Delta R=0.7$ are used. Jet energies are appropriately corrected to the parton level [15]. Since uncertainties in the standard model prediction grow with increasing jet multiplicity, up to the four largest $p_{T}$ jets are used to characterize the event; any reconstructed jets with $p_{T}$-ordered ranking of five or greater are neglected, except in final states with small summed scalar transverse momentum containing only jets.

A secondary vertex $b$-tagging algorithm is used to identify jets likely resulting from the fragmentation of a bottom quark ( $b$ ) produced in the hard scattering [16].

Momentum visible in the detector but not clustered into an electron, muon, tau, photon, jet, or $b$-tagged jet is referred to as unclustered momentum (uncl).

Missing momentum $(p)$ is calculated as the negative vector sum of the 4 -vectors of all identified objects and unclustered momentum. An event is said to contain a $\not p$ object if the transverse momentum of this object exceeds 17 GeV , and if additional quality criteria discriminating against fake missing momentum due to jet mismeasurement are satisfied [17].

## C. Event selection

Events containing an energetic and isolated electron, muon, tau, photon, or jet are selected. A set of three level online triggers requires:
(i) a central electron candidate with $p_{T}>18 \mathrm{GeV}$ passing level 3, with an associated track having $p_{T}>8 \mathrm{GeV}$ and an electromagnetic energy cluster with $p_{T}>16 \mathrm{GeV}$ at levels 1 and 2 ; or
(ii) a central muon candidate with $p_{T}>18 \mathrm{GeV}$ passing level 3, with an associated track having $p_{T}>$ 15 GeV and muon chamber track segments at levels 1 and 2 ; or
(iii) a central or plug photon candidate with $p_{T}>$ 25 GeV passing level 3 , with hadronic to electromagnetic energy less than $1: 8$ and with energy surrounding the photon to the photon's energy less than 1:7 at levels 1 and 2 ; or
(iv) a central or plug jet with $p_{T}>20 \mathrm{GeV}$ passing level 3, with 15 GeV of transverse momentum required at levels 1 and 2, with corresponding prescales of 50 and 25 , respectively; or
(v) a central or plug jet with $p_{T}>100 \mathrm{GeV}$ passing level 3, with energy clusters of 20 GeV and 90 GeV required at levels 1 and 2 ; or
(vi) a central electron candidate with $p_{T}>4 \mathrm{GeV}$ and a central muon candidate with $p_{T}>4 \mathrm{GeV}$ passing level 3 , with a muon segment, electromagnetic cluster, and two tracks with $p_{T}>4 \mathrm{GeV}$ required at levels 1 and 2 ; or
(vii) a central electron or muon candidate with $p_{T}>$ 4 GeV and a plug electron candidate with $p_{T}>$ 8 GeV , requiring a central muon segment and track or central electromagnetic energy cluster and track at levels 1 and 2, together with an isolated plug electromagnetic energy cluster; or
(viii) two central or plug electromagnetic clusters with $p_{T}>18 \mathrm{GeV}$ passing level 3 , with hadronic to electromagnetic energy less than $1: 8$ at levels 1 and 2 ; or
(ix) two central tau candidates with $p_{T}>10 \mathrm{GeV}$ passing level 3 , each with an associated track
having $p_{T}>10 \mathrm{GeV}$ and a calorimeter cluster with $p_{T}>5 \mathrm{GeV}$ at levels 1 and 2 .
Events satisfying one or more of these online triggers are recorded for further study. Offline event selection for this analysis uses a variety of further filters. Single object requirements keep events containing:
(i) a central electron with $p_{T}>25 \mathrm{GeV}$, or
(ii) a plug electron with $p_{T}>40 \mathrm{GeV}$, or
(iii) a central muon with $p_{T}>25 \mathrm{GeV}$, or
(iv) a central photon with $p_{T}>60 \mathrm{GeV}$, or
(v) a central jet or $b$-tagged jet with $p_{T}>200 \mathrm{GeV}$, or
(vi) a central jet or $b$-tagged jet with $p_{T}>40 \mathrm{GeV}$ (prescaled by a factor of roughly $10^{4}$ ),
possibly with other objects present. Multiple object criteria select events containing:
(i) two electromagnetic objects (electron or photon) with $|\eta|<2.5$ and $p_{T}>25 \mathrm{GeV}$, or
(ii) two taus with $|\eta|<1.0$ and $p_{T}>17 \mathrm{GeV}$, or
(iii) a central electron or muon with $p_{T}>17 \mathrm{GeV}$ and a central or plug electron, central muon, or central tau with $p_{T}>17 \mathrm{GeV}$, or
(iv) a central photon with $p_{T}>40 \mathrm{GeV}$ and a central electron or muon with $p_{T}>17 \mathrm{GeV}$, or
(v) a central or plug photon with $p_{T}>40 \mathrm{GeV}$ and a central tau with $p_{T}>40 \mathrm{GeV}$, or
(vi) a central photon with $p_{T}>40 \mathrm{GeV}$ and a central $b$-jet with $p_{T}>25 \mathrm{GeV}$, or
(vii) a central jet or $b$-tagged jet with $p_{T}>40 \mathrm{GeV}$ and a central tau with $p_{T}>17 \mathrm{GeV}$ (prescaled by a factor of roughly $10^{3}$ ), or
(viii) a central or plug photon with $p_{T}>40 \mathrm{GeV}$ and two central taus with $p_{T}>17 \mathrm{GeV}$, or
(ix) a central or plug photon with $p_{T}>40 \mathrm{GeV}$ and two central $b$-tagged jets with $p_{T}>25 \mathrm{GeV}$, or
(x) a central or plug photon with $p_{T}>40 \mathrm{GeV}$, a central tau with $p_{T}>25 \mathrm{GeV}$, and a central $b$-tagged jet with $p_{T}>25 \mathrm{GeV}$,
possibly with other objects present. Explicit online triggers feeding this offline selection are required. The $p_{T}$ thresholds for these criteria are chosen to be sufficiently above the online trigger turn-on curves that trigger efficiencies can be treated as roughly independent of object $p_{T}$.

Good run criteria are imposed, requiring the operation of all major subdetectors. To reduce contributions from cosmic rays and events from beam halo, standard CDF cosmic ray and beam halo filters are applied [18].

These selections result in a sample of roughly $2 \times 10^{6}$ high- $p_{T}$ data events in an integrated luminosity of $927 \mathrm{pb}^{-1}$.

## D. Event generation

Standard model backgrounds are estimated by generating a large sample of Monte Carlo events, using the PYTHIA [19], MADEVENT [20], and HERWIG [21] generators.

MADEVENT performs an exact leading order matrix element calculation and provides 4 -vector information corresponding to the outgoing legs of the underlying Feynman diagrams, together with color flow information. PYTHIA 6.218 is used to handle showering and fragmentation. The CTEQ5L [22] parton distribution functions are used.

QCD jets.-QCD dijet and multijet production are estimated using PYTHIA. Samples are generated with Tune A [23] with lower cuts on $\hat{p}_{T}$, the transverse momentum of the scattered partons in the center of momentum frame of the incoming partons, of $0,10,18,40,60,90,120,150$, 200,300 , and 400 GeV . These samples are combined to provide a complete estimation of QCD jet production, using the sample with greatest statistics in each range of $\hat{p}_{T}$.
$\gamma+j e t s$.-The estimation of QCD single prompt photon production comes from PYTHIA. Five samples are generated with Tune A corresponding to lower cuts on $\hat{p}_{T}$ of 8 , $12,22,45$, and 80 GeV . These samples are combined to provide a complete estimation of single prompt photon production in association with one or more jets, placing cuts on $\hat{p}_{T}$ to avoid double counting.
$\gamma \gamma+j e t s .-\mathrm{QCD}$ diphoton production is estimated using PYTHIA.
$V+$ jets.-The estimation of $V+$ jets processes (with $V$ denoting $W$ or $Z$ ), where the $W$ or $Z$ decays to first or second generation leptons, comes from MADEVENT, with PYTHIA employed for showering. Tune AW [23] is used within PYTHIA for these samples. The CKKW matching prescription [24] with a matching scale of 15 GeV is used to combine these samples and avoid double counting. Additional statistics are generated on the high- $p_{T}$ tails using the MLM matching prescription [25]. The factorization scale is set to the vector boson mass; the renormalization scale for each vertex is set to the $p_{T}$ of the jet. $W+4$ jets are generated inclusively in the number of jets; $Z+3$ jets are generated inclusively in the number of jets.
$V V+$ jets.-The estimation of $W W, W Z$, and $Z Z$ production with zero or more jets comes from PYTHIA.
$V \gamma+j e t s$.-The estimation of $W \gamma$ and $Z \gamma$ production comes from MADEVENT, with showering provided by PYTHIA. These samples are inclusive in the number of jets.
$W(\rightarrow \tau \nu)+j e t s$. Estimation of $W \rightarrow \tau \nu$ with zero or more jets comes from PYTHIA.
$Z(\rightarrow \tau \tau)+j e t s$.-Estimation of $Z \rightarrow \tau \tau$ with zero or more jets comes from PYTHIA.
$t \bar{t}$.-Top quark pair production is estimated using HERWIG assuming a top quark mass of 175 GeV and next-to-next-to-leading order (NNLO) cross section of $6.77 \pm 0.42 \mathrm{pb}$ [26].

Remaining processes, including for example $Z(\rightarrow \nu \bar{\nu}) \gamma$ and $Z\left(\rightarrow \ell^{+} \ell^{-}\right) b \bar{b}$, are generated by systematically looping over possible final state partons, using MADGRAPH [27] to determine all relevant diagrams and using MADEVENT to perform a Monte Carlo integration over the final state
phase space and to generate events. The MLM matching prescription is employed to combine samples with different numbers of final state jets.

A higher statistics estimate of the high- $p_{T}$ tails is obtained by computing the thresholds in $\sum p_{T}$ corresponding to the top $10 \%$ and $1 \%$ of each process, where $\sum p_{T}$ denotes the scalar summed transverse momentum of all identified objects in an event. Roughly 10 times as many events are generated for the top $10 \%$, and roughly 100 times as many events are generated for the top $1 \%$.

Cosmic rays.-Backgrounds from cosmic ray or beam halo muons that interact with the hadronic or electromagnetic calorimeters, producing objects that look like a photon or jet, are estimated using a sample of data events containing fewer than three reconstructed tracks. This procedure is described in more detail in Appendix A 2 a.

Minimum bias.-Minimum bias events are overlaid according to run-dependent instantaneous luminosity in some of the Monte Carlo samples, including those used for inclusive $W$ and $Z$ production. In all samples not containing overlaid minimum bias events, including those used to estimate QCD dijet production, additional unclustered momentum is added to events to mimic the effect of the majority of multiple interactions, in which a soft dijet event accompanies the rare hard scattering of interest. A random number is drawn from a Gaussian centered at 0 with width 1.5 GeV for each of the $x$ and $y$ components of the added unclustered momentum. Backgrounds due to two rare hard scatterings occurring in the same bunch crossing are estimated by forming overlaps of events, as described in Appendix A 2 b.

Each generated standard model event is assigned a weight, calculated as the cross section for the process (in units of picobarns) divided by the number of events generated for that process, representing the number of such events expected in a data sample corresponding to an integrated luminosity of $1 \mathrm{pb}^{-1}$. When multiplied by the integrated luminosity of the data sample used in this analysis, the weight gives the predicted number of such events in this analysis.

## E. Detector simulation

The response of the CDF detector is simulated using a GEANT-based detector simulation (CDFSIM) [28], with GFLASH [29] used to simulate shower development in the calorimeter.

In $p \bar{p}$ collisions there is an ordering of frequency with which objects of different types are produced: many more jets $(j)$ are produced than $b$-jets $(b)$ or photons $(\gamma)$, and many more of these are produced than charged leptons ( $e$, $\mu, \tau)$. The CDF detectors and reconstruction algorithms have been designed such that the probability of misreconstructing a frequently produced object as an infrequently produced object is small. The fraction of central jets that CDFSIM misreconstructs as photons, electrons, and muons
is $\sim 10^{-3}, \sim 10^{-4}$, and $\sim 10^{-5}$, respectively. Because of these small numbers, the use of CDFSIM to model these fake processes would require generating samples with prohibitively large statistics. Instead, the modeling of a frequently produced object faking a less frequently produced object (specifically: $j$ faking $b, \gamma, e, \mu$, or $\tau$; or $b$ or $\gamma$ faking $e$, $\mu$, or $\tau$ ) is obtained by the application of a misidentification probability, a particular type of correction factor in the VISTA correction model, described in the next section.

In Monte Carlo samples passed through CDFSIM, reconstructed leptons and photons are required to match to a corresponding generator level object. This procedure removes reconstructed leptons or photons that arise from a misreconstructed quark or gluon jet.

## F. Correction model

Unfortunately some numbers that cannot be determined from first principles enter the comparison between data and the standard model prediction. These numbers are referred to as "correction factors" in the VISTA correction model. This correction model is applied to generated Monte Carlo events to obtain the standard model prediction across all final states.

Correction factors must be obtained from the data themselves. These factors may be thought of as Bayesian nuisance parameters. The actual values of the correction factors are not directly of interest. Of interest is the comparison of data to standard model prediction, with correction factors adjusted to whatever they need to be, consistent with external constraints, to bring the standard model into closest agreement with the data.

The traditional prescription for determining these correction factors is to measure them in a control region in which no signal is expected. This procedure encounters difficulty when the entire high- $p_{T}$ data sample is considered to be a signal region. The approach adopted instead is to ask whether a consistent set of correction factors can be chosen so that the standard model prediction is in agreement with the CDF high- $p_{T}$ data.

The correction model is obtained by an iterative procedure informed by observed inadequacies in modeling. The process of correction model improvement, motivated by observed discrepancies, may allow a real signal to be artificially suppressed. If adjusting correction factor values within allowed bounds removes a signal, then the case for the signal disappears, since it can be explained in terms of known physics. This is true in any analysis. The stronger the constraints on the correction model, the more difficult it is to artificially suppress a real signal. By requiring a consistent interpretation of hundreds of final states, VISTA is less likely to mistakenly explain away new physics than if it had more limited scope.

The 44 correction factors currently included in the VISTA correction model are shown in Table I. These factors can be
classified into two categories: theoretical and experimental. A more detailed description of each individual correction factor is provided in Appendix A 4.

Theoretical correction factors reflect the practical difficulty of calculating accurately within the framework of the standard model. These factors take the form of $k$-factors, so-called "knowledge factors," representing the ratio of the unavailable all order cross section to the calculable leading order cross section. Twenty-three $k$-factors are used for standard model processes including QCD multijet production, $W+$ jets, $Z+$ jets, and (di)photon + jets production.

Experimental correction factors include the integrated luminosity of the data, efficiencies associated with triggering on electrons and muons, efficiencies associated with the correct identification of physics objects, and fake rates associated with the mistaken identification of physics objects. Obtaining an adequate description of object misidentification has required an understanding of the underlying physical mechanisms by which objects are misreconstructed, as described in Appendix A 1.

In the interest of simplicity, correction factors representing $k$-factors, efficiencies, and fake rates are generally taken to be constants, independent of kinematic quantities such as object $p_{T}$, with only five exceptions. The $p_{T}$ dependence of three fake rates is too large to be treated as approximately constant: the jet faking electron rate $p(j \rightarrow e)$ in the plug region of the CDF detector; the jet faking $b$-tagged jet rate $p(j \rightarrow b)$, which increases steadily with increasing $p_{T}$; and the jet faking tau rate $p(j \rightarrow \tau)$, which decreases steadily with increasing $p_{T}$. Two other fake rates possess geometrical features in $\eta-\phi$ due to the construction of the CDF detector: the jet faking electron rate $p(j \rightarrow e)$ in the central region, because of the fiducial tower geometry of the electromagnetic calorimeter; and the jet faking muon rate $p(j \rightarrow \mu)$, due to the nontrivial fiducial geometry of the muon chambers. After determining appropriate functional forms, a single overall multiplicative correction factor is used.

Correction factor values are obtained from a global fit to the data. The procedure is outlined here, with further details relegated to Appendix A 3.

Events are first partitioned into final states according to the number and types of objects present. Each final state is then subdivided into bins according to each object's detector pseudorapidity ( $\eta_{\text {det }}$ ) and transverse momentum $\left(p_{T}\right)$, as described in Appendix A 3 a.

Generated Monte Carlo events, adjusted by the correction model, provide the standard model prediction for each bin. The standard model prediction in each bin is therefore a function of the correction factor values. A figure of merit is defined to quantify global agreement between the data and the standard model prediction, and correction factor values are chosen to maximize this agreement, consistent with external experimental constraints.

TABLE I. The 44 correction factors introduced in the VISTA correction model. The leftmost column (Code) shows correction factor codes. The second column (Category) shows correction factor categories. The third column (Explanation) provides a short description. The correction factor best fit value (Value) is given in the fourth column. The correction factor error (Error) resulting from the fit is shown in the fifth column. The fractional error [Error (\%)] is listed in the sixth column. All values are dimensionless with the exception of code 0001 (luminosity), which has units of $\mathrm{pb}^{-1}$. The values and uncertainties of these correction factors are valid within the context of this correction model.

| Code | Category | Explanation | Value | Error | Error(\%) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0001 | luminosity | CDF integrated luminosity | 927 | 20 | 2.2 |
| 0002 | $k$-factor | cosmic $\gamma$ | 0.69 | 0.05 | 7.3 |
| 0003 | $k$-factor | cosmic $j$ | 0.446 | 0.014 | 3.1 |
| 0004 | $k$-factor | $1 \gamma 1 j$ | 0.95 | 0.04 | 4.2 |
| 0005 | $k$-factor | $1 \gamma 2 j$ | 1.2 | 0.05 | 4.1 |
| 0006 | $k$-factor | $1 \gamma 3 j$ | 1.48 | 0.07 | 4.7 |
| 0007 | $k$-factor | $1 \gamma 4 j+$ | 1.97 | 0.16 | 8.1 |
| 0008 | $k$-factor | $2 \gamma 0 j$ | 1.81 | 0.08 | 4.4 |
| 0009 | $k$-factor | $2 \gamma 1 j$ | 3.42 | 0.24 | 7.0 |
| 0010 | $k$-factor | $2 \gamma 2 j+$ | 1.3 | 0.16 | 12.3 |
| 0011 | $k$-factor | W0j | 1.453 | 0.027 | 1.9 |
| 0012 | $k$-factor | W1j | 1.06 | 0.03 | 2.8 |
| 0013 | $k$-factor | W2j | 1.02 | 0.03 | 2.9 |
| 0014 | $k$-factor | W3j+ | 0.76 | 0.05 | 6.6 |
| 0015 | $k$-factor | Z0j | 1.419 | 0.024 | 1.7 |
| 0016 | $k$-factor | Z1j | 1.18 | 0.04 | 3.4 |
| 0017 | $k$-factor | Z2j+ | 1.03 | 0.05 | 4.8 |
| 0018 | $k$-factor | $2 j, \hat{p}_{T}<150$ | 0.96 | 0.022 | 2.3 |
| 0019 | $k$-factor | $2 j, 150<\hat{p}_{T}$ | 1.256 | 0.028 | 2.2 |
| 0020 | $k$-factor | $3 j, \hat{p}_{T}<150$ | 0.921 | 0.021 | 2.3 |
| 0021 | $k$-factor | $3 j, 150<\hat{p}_{T}$ | 1.36 | 0.03 | 2.4 |
| 0022 | $k$-factor | $4 j, \hat{p}_{T}<150$ | 0.989 | 0.025 | 2.5 |
| 0023 | $k$-factor | $4 j, 150<\hat{p}_{T}$ | 1.7 | 0.04 | 2.3 |
| 0024 | $k$-factor | $5 j+$ | 1.25 | 0.05 | 4.0 |
| 0025 | ID eff | $p(e \rightarrow e)$ central | 0.986 | 0.006 | 0.6 |
| 0026 | ID eff | $p(e \rightarrow e)$ plug | 0.933 | 0.009 | 1.0 |
| 0027 | ID eff | $p(\mu \rightarrow \mu),\|\eta\|<0.6$ | 0.845 | 0.008 | 0.9 |
| 0028 | ID eff | $p(\mu \rightarrow \mu), 0.6<\|\eta\|$ | 0.915 | 0.011 | 1.2 |
| 0029 | ID eff | $p(\gamma \rightarrow \gamma)$ central | 0.974 | 0.018 | 1.8 |
| 0030 | ID eff | $p(\gamma \rightarrow \gamma)$ plug | 0.913 | 0.018 | 2.0 |
| 0031 | ID eff | $p(b \rightarrow b)$ central | 1 | 0.04 | 4.0 |
| 0032 | fake rate | $p(e \rightarrow \gamma)$ plug | 0.045 | 0.012 | 27.0 |
| 0033 | fake rate | $p(q \rightarrow e)$ central | $9.71 \times 10^{-5}$ | $1.9 \times 10^{-6}$ | 2.0 |
| 0034 | fake rate | $p(q \rightarrow e)$ plug | 0.000876 | $1.8 \times 10^{-5}$ | 2.1 |
| 0035 | fake rate | $p(q \rightarrow \mu)$ | $1.157 \times 10^{-5}$ | $2.7 \times 10^{-7}$ | 2.3 |
| 0036 | fake rate | $p(j \rightarrow b)$ | 0.01684 | 0.00027 | 1.6 |
| 0037 | fake rate | $p(q \rightarrow \tau), p_{T}<60$ | 0.00341 | 0.00012 | 3.5 |
| 0038 | fake rate | $p(q \rightarrow \tau), 60<p_{T}$ | 0.00038 | $4 \times 10^{-5}$ | 10.5 |
| 0039 | fake rate | $p(q \rightarrow \gamma)$ central | 0.000265 | $1.5 \times 10^{-5}$ | 5.7 |
| 0040 | fake rate | $p(q \rightarrow \gamma)$ plug | 0.00159 | 0.00013 | 8.2 |
| 0041 | trigger | $p(e \rightarrow$ trig $)$ central, $p_{T}>25$ | 0.976 | 0.007 | 0.7 |
| 0042 | trigger | $p(e \rightarrow$ trig $)$ plug, $p_{T}>25$ | 0.835 | 0.015 | 1.8 |
| 0043 | trigger | $p(\mu \rightarrow$ trig $)\|\eta\|<0.6, p_{T}>25$ | 0.917 | 0.007 | 0.8 |
| 0044 | trigger | $p(\mu \rightarrow \operatorname{trig}) 0.6<\|\eta\|<1.0, p_{T}>25$ | 0.96 | 0.01 | 1.0 |

Letting $\vec{s}$ represent a vector of correction factors, for the $k$ th bin

$$
\begin{equation*}
\chi_{k}^{2}(\vec{s})=\frac{(\mathrm{Data}[k]-\mathrm{SM}[k])^{2}}{\sqrt{\mathrm{SM}[k]^{2}}+\delta \mathrm{SM}[k]^{2}} \tag{1}
\end{equation*}
$$

where $\operatorname{Data}[k]$ is the number of data events observed in the $k$ th bin, $\operatorname{SM}[k]$ is the number of events predicted by the standard model in the $k$ th bin, $\delta \mathrm{SM}[k]$ is the Monte Carlo statistical uncertainty on the standard model prediction in the $k$ th bin [30], and $\sqrt{\mathrm{SM}[k]}$ is the statistical uncertainty on the expected data in the $k$ th bin. The standard model prediction $\operatorname{SM}[k]$ in the $k$ th bin is a function of $\vec{s}$.

Relevant information external to the VISTA high- $p_{T}$ data sample provides additional constraints in this global fit. The CDF luminosity counters measure the integrated luminosity of the sample described in this article to be $902 \mathrm{pb}^{-1} \pm 6 \%$ by measuring the fraction of bunch crossings in which zero inelastic collisions occur [31]. The integrated luminosity of the sample measured by the luminosity counters enters in the form of a Gaussian constraint on the luminosity correction factor. Higher order theoretical calculations exist for some standard model processes, providing constraints on corresponding $k$-factors, and some CDF experimental correction factors are also constrained from external information. In total, 26 of the 44 correction factors are constrained. The specific constraints employed are provided in Appendix A 3 b.

The overall function to be minimized takes the form

$$
\begin{equation*}
\chi^{2}(\vec{s})=\left(\sum_{k \in \text { bins }} \chi_{k}^{2}(\vec{s})\right)+\chi_{\text {constraints }}^{2}(\vec{s}) \tag{2}
\end{equation*}
$$

where the sum in the first term is over bins in the CDF high- $p_{T}$ data sample with $\chi_{k}^{2}(\vec{s})$ defined in Eq. (1), and the second term is the contribution from explicit constraints.

Minimization of $\chi^{2}(\vec{s})$ in Eq. (2) as a function of the vector of correction factors $\vec{s}$ results in a set of correction factor values $\vec{s}_{0}$ providing the best global agreement between the data and the standard model prediction. The best fit correction factor values are shown in Table I, together with absolute and fractional uncertainties. The determined uncertainties are not used explicitly in the subsequent analysis, but rather provide information used implicitly to assist in appropriate adjustment to the correction model in light of observed discrepancies. The uncertainties are verified by subdividing the data into thirds, performing separate fits on each third, and noting that the correction factor values obtained with each subset are consistent within quoted uncertainties. Further details on the correlation matrix and other technical aspects of this global fit can be found in Appendix A 3 c .

Although the correction factors are determined from a global fit, in practice the determination of many correction factors' values are dominated by one recognizable subsam-
ple. The rate $p(j \rightarrow e)$ for a jet to fake an electron is determined largely by the number of events in the $e j$ final state, since the largest contribution to this final state is from dijet events with one jet misreconstructed as an electron. Similarly, the rates $p(j \rightarrow b)$ and $p(j \rightarrow \tau)$ for a jet to fake a $b$-tagged jet and tau lepton are determined largely by the number of events in the $b j$ and $\tau j$ final states, respectively. The determination of the fake rate $p(j \rightarrow \gamma)$, photon efficiency $p(\gamma \rightarrow \gamma)$, and $k$-factors for prompt photon production and prompt diphoton production are dominated by the $\gamma j, \gamma j j$, and $\gamma \gamma$ final states. Additional knowledge incorporated in the determination of fake rates is described in Appendix A 1.

The global fit $\chi^{2}$ per number of bins is $288.1 / 133+$ 27.9, where the last term is the contribution to the $\chi^{2}$ from the imposed constraints. A $\chi^{2}$ per degree of freedom larger than unity is expected, since the limited set of correction factors in this correction model is not expected to provide a complete description of all features of the data. Emphasis is placed on individual outlying discrepancies that may motivate a new physics claim, rather than overall goodness of fit.

Corrections to object identification efficiencies are typically less than $10 \%$; fake rates are consistent with an understanding of the underlying physical mechanisms responsible; $k$-factors range from slightly less than unity to greater than two for some processes with multiple jets. All values obtained are physically reasonable. Further analysis is provided in Appendix A 4.

With the details of the correction model in place, the complete standard model prediction can be obtained. For each Monte Carlo event after detector simulation, the event weight is multiplied by the value of the luminosity correction factor and the $k$-factor for the relevant standard model process. The single Monte Carlo event can be misreconstructed in a number of ways, producing a set of Monte Carlo events derived from the original, with weights multiplied by the probability of each misreconstruction. The weight of each resulting event is multiplied by the probability the event satisfies trigger criteria. The resulting standard model prediction, corrected as just described, is referred to as "the standard model prediction" throughout the rest of this paper, with "corrected" implied in all cases.

## G. Results

Data and standard model events are partitioned into exclusive final states. This partitioning is orthogonal, with each event ending up in one and only one final state. Data are compared to standard model prediction in each final state, considering the total number of events observed and predicted, and the shapes of relevant kinematic distributions.

In a data driven search, it is crucial to explicitly account for the trials factor, quantifying the number of places an interesting signal could appear. Fluctuations at the level of
three or more standard deviations are expected to appear simply because a large number of regions are considered. A reasonably rigorous accounting of this trials factor is possible as long as the measures of interest and the regions to which these measures are applied are specified a priori, as is done here. In this analysis a discrepancy at the level of $3 \sigma$ or greater after accounting for the trials factor (typically corresponding to a discrepancy at the level of $5 \sigma$ or greater before accounting for the trials factor) is considered "significant."

Discrepancy in the total number of events in a final state (fs) is measured by the Poisson probability $p_{\mathrm{fs}}$ that the number of predicted events would fluctuate up to or above (or down to or below) the number of events observed. To account for the trials factor due to the 344 VISTA final states examined, the quantity $p=1-\left(1-p_{\mathrm{fs}}\right)^{344}$ is calculated for each final state. The result is the probability $p$ of observing a discrepancy corresponding to a probability less than $p_{\mathrm{fs}}$ in the total sample studied. This probability $p$ can then be converted into units of standard deviations by solving for $\sigma$ such that $\int_{\sigma}^{\infty} \frac{1}{\sqrt{2 \pi}} e^{-\left(x^{2} / 2\right)} d x=p$ [32]. A final state exhibiting a population discrepancy greater than $3 \sigma$ after the trials factor is thus accounted for is considered significant.

Many kinematic distributions are considered in each final state, including the transverse momentum, pseudorapidity, detector pseudorapidity, and azimuthal angle of all objects, masses of individual jets and $b$-jets, invariant masses of all object combinations, transverse masses of object combinations including $\not p$, angular separation $\Delta \phi$ and $\Delta R$ of all object pairs, and several other more specialized variables. A Kolmogorov-Smirnov (KS) test is used to quantify the difference in shape of each kinematic distribution between data and standard model prediction. As with populations, a trials factor is assessed to account for the 16486 distributions examined, and the resulting probability is converted into units of standard deviations. A distribution with KS statistic greater than 0.02 and probability corresponding to greater than $3 \sigma$ after assessing the trials factor is considered significant.

Table II shows a subset of the VISTA comparison of data to standard model prediction. Shown are all final states containing ten or more data events, with the most discrepant final states in population heading the list. After accounting for the trials factor, no final state has a statistically significant ( $>3 \sigma$ ) population discrepancy. The most discrepant final state $\left(3 j \tau^{ \pm}\right)$contains 71 data events and $113.7 \pm 3.6$ events expected from the standard model. The Poisson probability for $113.7 \pm 3.6$ expected events to result in 71 or fewer events observed in this final state is $2.8 \times 10^{-5}$, corresponding to an entry at $-4.03 \sigma$ in Fig. 1 . The probability for one or more of the 344 populated final states considered to display disagreement in population corresponding to a probability less than $2.8 \times 10^{-5}$ is $1 \%$. The $3 j \tau^{ \pm}$population discrepancy is thus not statisti-
cally significant. The most discrepant kinematic distribution in this final state is the invariant mass of the tau lepton and the two highest transverse momentum jets, shown in Fig. 2.

The six final states with largest population discrepancy are $3 j \tau, 5 j, 2 j \tau, 2 j 2 \tau$, $b e j$, and the low- $p_{T} 3 j$ final state, with bej being the only one of these six to exhibit an excess of data. The $3 j \tau, 2 j \tau$, and $2 j 2 \tau$ final states appear to reflect an incomplete understanding of the rate of jets faking taus $(p(j \rightarrow \tau))$ as a function of the number of jets in the event, at the level of $\sim 30 \%$ difference between the total number of observed and predicted events in the most populated of these final states. The value of $p(j \rightarrow \tau)$ is primarily determined by the $j \tau$ final state. Interestingly, although the underlying physical mechanism for $p(j \rightarrow e)$ is very similar to that for $p(j \rightarrow \tau)$, as discussed in Appendix A 1 , a significant dependence on the presence of additional jets is not observed for $p(j \rightarrow e)$.

The $5 j$ discrepancy results from a tension with the $e 4 j$ final state, whose dominant contribution comes from $5 j$ production convoluted with $p(j \rightarrow e)$. The low- $p_{T} 3 j$ discrepancy results from a tension with the $e 2 j$ final state, whose dominant contribution comes from $3 j$ production convoluted with $p(j \rightarrow e)$. The bej final state is predominantly $3 j$ production convoluted with $p(j \rightarrow b)$ and $p(j \rightarrow$ $e)$; this discrepancy also arises from a tension with the low- $p_{T} 3 j$ and $e 2 j$ final states. The bej final state is the VISTA final state in which the largest excess of data over standard model prediction is seen. The fraction of hypothetical similar CDF experiments that would produce a VISTA normalization excess as significant as the excess observed in this final state is $8 \%$. The $5 j$, bej, and low- $p_{T} 3 j$ discrepancies correspond to a difference of $\sim 10 \%$ between the total number of observed and predicted events in these final states.

Figure 1 summarizes in a histogram the measured discrepancies between data and the standard model prediction for CDF high- $p_{T}$ final state populations and kinematic distributions. Values in this figure represent individual discrepancies and do not account for the trials factor associated with examining many possibilities.

Of the 16484 kinematic distributions considered, 384 distributions are found to correspond to a discrepancy greater than $3 \sigma$ after accounting for the trials factor, entering with a KS probability of roughly $5 \sigma$ or greater in Fig. 1. Of these 384 discrepant distributions, 312 are attributed to modeling parton radiation, deriving from the $3 j \Delta R\left(j_{2}, j_{3}\right)$ discrepancy shown in Fig. 3, with 186 of these 312 shape discrepancies pointing out that individual jet masses are larger in data than in the prediction, as shown in Fig. 4. A careful reading of the literature reveals that the same effect was observed (but not emphasized) by both CDF [33,34] and D0 [35] in Tevatron run I. The $3 j \Delta R\left(j_{2}, j_{3}\right)$ and jet mass discrepancies appear to be two different views of a single underlying discrepancy, noting that two sufficiently

TABLE II. A subset of the VISTA comparison between Tevatron run II data and standard model prediction, showing the 20 most discrepant final states and all final states populated with ten or more data events. Events are partitioned into exclusive final states based on standard CDF object identification criteria. Final states are labeled in this table according to the number and types of objects present, and whether (high $\sum p_{T}$ ) or not (low $\sum p_{T}$ ) the summed scalar transverse momentum of all objects in the events exceeds 400 GeV , for final states not containing leptons or photons. Final states are ordered according to decreasing discrepancy between the total number of events expected, taking into account the error from Monte Carlo statistics and the total number observed in the data. Final states exhibiting mild discrepancies are shown together with the significance of the discrepancy in units of standard deviations $(\sigma)$ after accounting for a trials factor corresponding to the number of final states considered. Final states that do not exhibit even mild discrepancies are listed below the horizontal line in inverted alphabetical order. Only Monte Carlo statistical uncertainties on the background prediction are included.

| Final state | Data | Background | $\sigma$ | Final state | Data | Background | Final state | Data | Background |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $3 j \tau^{ \pm}$ | 71 | $113.7 \pm 3.6$ | -2.3 | $2 j \mu^{ \pm}$ | 9513 | $9362.3 \pm 166.8$ | $e^{ \pm} p \tau^{ \pm}$ | 20 | $18.7 \pm 1.9$ |
| $5 j$ | 1661 | $1902.9 \pm 50.8$ | -1.7 | $2 e^{ \pm} j$ | 13 | $9.8 \pm 2.2$ | $e^{ \pm} \gamma p$ | 141 | $144.2 \pm 6$ |
| $2 j \tau^{ \pm}$ | 233 | $296.5 \pm 5.6$ | -1.6 | $2 e^{ \pm} e^{\mp}$ | 12 | $4.8 \pm 1.2$ | $e^{ \pm} \mu^{\mp} p$ | 54 | $42.6 \pm 2.7$ |
| $2 j 2 \tau^{ \pm}$ | 6 | $27 \pm 4.6$ | -1.4 | $2 e^{ \pm}$ | 23 | $36.1 \pm 3.8$ | $e^{ \pm} \mu^{ \pm} \not p$ | 13 | $10.9 \pm 1.3$ |
| $b e^{ \pm} j$ | 2207 | $2015.4 \pm 28.7$ | +1.4 | $2 b$, low $\sum p_{T}$ | 327 | $335.8 \pm 3.7$ | $e^{ \pm} \mu^{\mp}$ | 153 | $127.6 \pm 4.2$ |
| $3 j$, high $\sum p_{T}$ | 35436 | $37294.6 \pm 524.3$ | -1.1 | $2 b$, high $\sum p_{T}$ | 187 | $173.1 \pm 7.1$ | $e^{ \pm} j$ | 386880 | $392614 \pm 5031.8$ |
| $e^{ \pm} 3 j \not p$ | 1954 | $1751.6 \pm 42$ | +1.1 | $2 b 3 j$, high $\sum p_{T}$ | 28 | $33.5 \pm 5.5$ | $e^{ \pm} j 2 \gamma$ | 14 | $15.9 \pm 2.9$ |
| $b e^{ \pm} 2 j$ | 798 | $695.3 \pm 13.3$ | +1.1 | $2 b 2 j$, low $\sum p_{T}$ | 355 | $326.3 \pm 8.4$ | $e^{ \pm} j \tau^{ \pm}$ | 79 | $79.3 \pm 2.9$ |
| $3 j p$, low $\sum p_{T}$ | 811 | $967.5 \pm 38.4$ | $-0.8$ | $2 b 2 j$, high $\sum p_{T}$ | 56 | $80.2 \pm 5$ | $e^{ \pm} j \tau^{\mp}$ | 162 | $148.8 \pm 7.6$ |
| $e^{ \pm} \mu^{ \pm}$ | 26 | $11.6 \pm 1.5$ | +0.8 | $2 b 2 j \gamma$ | 16 | $15.4 \pm 3.6$ | $e^{ \pm} j \not p$ | 58648 | $57391.7 \pm 661.6$ |
| $e^{ \pm} \gamma$ | 636 | $551.2 \pm 11.2$ | +0.7 | $2 b \gamma$ | 37 | $31.7 \pm 4.8$ | $e^{ \pm} j \gamma p$ | 52 | $76.2 \pm 9$ |
| $e^{ \pm} 3 j$ | 28656 | $27281.5 \pm 405.2$ | +0.6 | $2 b j$, low $\sum p_{T}$ | 415 | $393.8 \pm 9.1$ | $e^{ \pm} j \mu^{\mp} \not p$ | 22 | $13.1 \pm 1.7$ |
| b5j | 131 | $95 \pm 4.7$ | +0.5 | $2 b j$, high $\sum p_{T}$ | 161 | $195.8 \pm 8.3$ | $e^{ \pm} j \mu^{\mp}$ | 28 | $26.8 \pm 2.3$ |
| $j 2 \tau^{ \pm}$ | 50 | $85.6 \pm 8.2$ | -0.4 | $2 b j \not p$, low $\sum p_{T}$ | 28 | $23.2 \pm 2.6$ | $e^{ \pm} e^{\mp} 4 j$ | 103 | $113.5 \pm 5.9$ |
| $j \tau^{ \pm} \tau^{\mp}$ | 74 | $125 \pm 13.6$ | -0.4 | $2 b j \gamma$ | 25 | $24.7 \pm 4.3$ | $e^{ \pm} e^{\mp} 3 j$ | 456 | $473 \pm 14.6$ |
| $b \not p$, low $\sum p_{T}$ | 10 | $29.5 \pm 4.6$ | -0.4 | $2 b e^{ \pm} 2 j p$ | 15 | $12.3 \pm 1.6$ | $e^{ \pm} e^{\mp} 2 j p$ | 30 | $39 \pm 4.6$ |
| $e^{ \pm} j \gamma$ | 286 | $369.4 \pm 21.1$ | -0.3 | $2 b e^{ \pm} 2 j$ | 30 | $30.5 \pm 2.5$ | $e^{ \pm} e^{\mp} 2 j$ | 2149 | $2152 \pm 40.1$ |
| $e^{ \pm} j \not p \tau^{\mp}$ | 29 | $14.2 \pm 1.8$ | +0.2 | $2 b e^{ \pm} j$ | 28 | $29.1 \pm 2.8$ | $e^{ \pm} e^{\mp} \tau^{ \pm}$ | 14 | $11.1 \pm 2$ |
| $2 j$, high $\sum p_{T}$ | 96502 | $92437.3 \pm 1354.5$ | +0.1 | $2 b e^{ \pm}$ | 48 | $45.2 \pm 3.7$ | $e^{ \pm} e^{\mp} p$ | 491 | $487.9 \pm 12$ |
| $b e^{ \pm} 3 j$ | 356 | $298.6 \pm 7.7$ | +0.1 | $\tau^{ \pm} \tau^{\mp}$ | 498 | $428.5 \pm 22.7$ | $e^{ \pm} e^{\mp} \gamma$ | 127 | $132.3 \pm 4.2$ |
| $8 j$ | 11 | $6.1 \pm 2.5$ |  | $\gamma \tau^{ \pm}$ | 177 | $204.4 \pm 5.4$ | $e^{ \pm} e^{\mp} j$ | 10726 | $10669.3 \pm 123.5$ |
| $7 j$ | 57 | $35.6 \pm 4.9$ |  | $\gamma \not p$ | 1952 | $1945.8 \pm 77.1$ | $e^{ \pm} e^{\mp} j p$ | 157 | $144 \pm 11.2$ |
| $6 j$ | 335 | $298.4 \pm 14.7$ |  | $\mu^{ \pm} \tau^{ \pm}$ | 18 | $19.8 \pm 2.3$ | $e^{ \pm} e^{\mp} j \gamma$ | 26 | $45.6 \pm 4.7$ |
| $4 j$, low $\sum p_{T}$ | 39665 | $40898.8 \pm 649.2$ |  | $\mu^{ \pm} \tau^{\mp}$ | 151 | $179.1 \pm 4.7$ | $e^{ \pm} e^{\mp}$ | 58344 | $58575.6 \pm 603.9$ |
| $4 j$, high $\sum p_{T}$ | 8241 | $8403.7 \pm 144.7$ |  | $\mu^{ \pm} \not p$ | 321351 | $320500 \pm 3475.5$ | $b 6 j$ | 24 | $15.5 \pm 2.3$ |
| $4 j 2 \gamma$ | 38 | $57.5 \pm 11$ |  | $\mu^{ \pm} \not p \tau^{\mp}$ | 22 | $25.8 \pm 2.7$ | $b 4 j$, low $\sum p_{T}$ | 13 | $9.2 \pm 1.8$ |
| $4 j \tau^{ \pm}$ | 20 | $36.9 \pm 2.4$ |  | $\mu^{ \pm} \gamma$ | 269 | $285.5 \pm 5.9$ | $b 4 j$, high $\sum p_{T}$ | 464 | $499.2 \pm 12.4$ |
| $4 j p p$, low $\sum p_{T}$ | 516 | $525.2 \pm 34.5$ |  | $\mu^{ \pm} \gamma \underline{p}$ | 269 | $282.2 \pm 6.6$ | $b 3 j$, low $\sum p_{T}$ | 5354 | $5285 \pm 72.4$ |
| $4 j \gamma \nsim$ | 28 | $53.8 \pm 11$ |  | $\mu^{ \pm} \mu^{\mp} \not p$ | 49 | $61.4 \pm 3.5$ | $b 3 j$, high $\sum p_{T}$ | 1639 | $1558.9 \pm 24.1$ |
| $4 j \gamma$ | 3693 | $3827.2 \pm 112.1$ |  | $\mu^{ \pm} \mu^{\mp} \gamma$ | 32 | $29.9 \pm 2.6$ | b3jp, low $\sum p_{T}$ | 111 | $116.8 \pm 11.2$ |
| $4 j \mu^{ \pm}$ | 576 | $568.2 \pm 26.1$ |  | $\mu^{ \pm} \mu^{\mp}$ | 10648 | $10845.6 \pm 96$ | b3j\% | 182 | $194.1 \pm 8.8$ |
| $4 j \mu^{ \pm} \not \underline{ }$ | 232 | $224.7 \pm 8.5$ |  | $j 2 \gamma$ | 2196 | $2200.3 \pm 35.2$ | b3j $\mu^{ \pm} \not p$ | 37 | $34.1 \pm 2$ |
| $4 j \mu^{ \pm} \mu^{\mp}$ | 17 | $20.1 \pm 2.5$ |  | $j 2 \gamma p$ | 38 | $27.3 \pm 3.2$ | $b 3 j \mu^{ \pm}$ | 47 | $52.2 \pm 3$ |
| $3 \gamma$ | 13 | $24.2 \pm 3$ |  | $j \tau^{ \pm}$ | 563 | $585.7 \pm 10.2$ | $b 2 \gamma$ | 15 | $14.6 \pm 2.1$ |
| $3 j$, low $\sum p_{T}$ | 75894 | $75939.2 \pm 1043.9$ |  | $j p$, low $\sum p_{T}$ | 4183 | $4209.1 \pm 56.1$ | $b 2 j$, low $\sum p_{T}$ | 8812 | $8576.2 \pm 97.9$ |
| $3 j 2 \gamma$ | 145 | $178.1 \pm 7.4$ |  | $j \gamma$ | 49052 | $48743 \pm 546.3$ | $b 2 j$, high $\sum p_{T}$ | 4691 | $4646.2 \pm 57.7$ |
| $3 j \not p$, high $\sum p_{T}$ | 20 | $30.9 \pm 14.4$ |  | $j \gamma \tau^{ \pm}$ | 106 | $104 \pm 4.1$ | $b 2 j p$, low $\sum p_{T}$ | 198 | $209.2 \pm 8.3$ |
| $3 j \gamma \tau^{ \pm}$ | 13 | $11 \pm 2$ |  | j\%p | 913 | $965.2 \pm 41.5$ | $b 2 j \gamma$ | 429 | $425.1 \pm 13.1$ |
| $3 j \gamma p$ | 83 | $102.9 \pm 11.1$ |  | $j \mu^{ \pm}$ | 33462 | $34026.7 \pm 510.1$ | $b 2 j \mu^{ \pm} \not p$ | 46 | $40.1 \pm 2.7$ |
| $3 j \gamma$ | 11424 | $11506.4 \pm 190.6$ |  | $j \mu^{ \pm} \tau^{\mp}$ | 29 | $37.5 \pm 4.5$ | $b 2 j \mu^{ \pm}$ | 56 | $60.6 \pm 3.4$ |
| $3 j \mu^{ \pm} \not \underline{p}$ | 1114 | $1118.7 \pm 27.1$ |  | $j \mu^{ \pm} \not p \tau^{\mp}$ | 10 | $9.6 \pm 2.1$ | $b \tau^{ \pm}$ | 19 | $19.9 \pm 2.2$ |
| $3 j \mu^{ \pm} \mu^{\mp}$ | 61 | $84.5 \pm 9.2$ |  | $j \mu^{ \pm} \not p$ | 45728 | $46316.4 \pm 568.2$ | $b \gamma$ | 976 | $1034.8 \pm 15.6$ |
| $3 j \mu^{ \pm}$ | 2132 | $2168.7 \pm 64.2$ |  | $j \mu^{ \pm} \gamma \not \underline{ }$ | 78 | $69.8 \pm 9.9$ | brp | 18 | $16.7 \pm 3.1$ |
| $3 b j$, low $\sum p_{T}$ | 14 | $9.3 \pm 1.9$ |  | $j \mu^{ \pm} \gamma$ | 70 | $98.4 \pm 12.1$ | $b \mu^{ \pm}$ | 303 | $263.5 \pm 7.9$ |
| $2 \tau^{ \pm}$ | 316 | $290.8 \pm 24.2$ |  | $j \mu^{ \pm} \mu^{\mp}$ | 1977 | $2093.3 \pm 74.7$ | $b \mu^{ \pm} \not p$ | 204 | $218.1 \pm 6.4$ |
| $2 \gamma p$ | 161 | $176 \pm 9.1$ |  | $e^{ \pm} 4 j$ | 7144 | $6661.9 \pm 147.2$ | $b j$, low $\sum p_{T}$ | 9060 | $9275.7 \pm 87.8$ |
| $2 \gamma$ | 8482 | $8349.1 \pm 84.1$ |  | $e^{ \pm} 4 j \not p$ | 403 | $363 \pm 9.9$ | $b j$, high $\sum p_{T}$ | 7236 | $7030.8 \pm 74$ |
| $2 j$, low $\sum p_{T}$ | 93408 | $92789.5 \pm 1138.2$ |  | $e^{ \pm} 3 j \tau^{\mp}$ | 11 | $7.6 \pm 1.6$ | $b j 2 \gamma$ | 13 | $17.6 \pm 3.3$ |
| $2 j 2 \gamma$ | 645 | $612.6 \pm 18.8$ |  | $e^{ \pm} 3 j \gamma$ | 27 | $21.7 \pm 3.4$ | $b j \tau^{ \pm}$ | 13 | $12.9 \pm 1.8$ |
| $2 j \tau^{ \pm} \tau^{\mp}$ | 15 | $25 \pm 3.5$ |  | $e^{ \pm} 2 \gamma$ | 47 | $74.5 \pm 5$ | $b j p$, low $\sum p_{T}$ | 53 | $60.4 \pm 19.9$ |
| $2 j p p$, low $\sum p_{T}$ | 74 | $106 \pm 7.8$ |  | $e^{ \pm} 2 j$ | 126665 | $122457 \pm 1672.6$ | $b j \gamma$ | 937 | $989.4 \pm 20.6$ |
| $2 j p b$, high $\sum p_{T}$ | 43 | $37.7 \pm 100.2$ |  | $e^{ \pm} 2 j \tau^{\mp}$ | 53 | $37.3 \pm 3.9$ | bjop | 34 | $30.5 \pm 4$ |
| $2 j \gamma$ | 33684 | $33259.9 \pm 397.6$ |  | $e^{ \pm} 2 j \tau^{ \pm}$ | 20 | $24.7 \pm 2.3$ | $b j \mu^{ \pm} \nsim$ | 104 | $112.6 \pm 4.4$ |

TABLE II. (Continued)

| Final state | Data | Background | $\sigma$ | Final state | Data | Background | Final state |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |



FIG. 1 (color online). Distribution of observed discrepancy between data and the standard model prediction, measured in units of standard deviation $(\sigma)$, shown as the solid (green) histogram, before accounting for the trials factor. The upper pane shows the distribution of discrepancies between the total number of events observed and predicted in the 344 populated final states considered. Negative values on the horizontal axis correspond to a deficit of data compared to standard model prediction; positive values indicate an excess of data compared to standard model prediction. The lower pane shows the distribution of discrepancies between the observed and predicted shapes in 16486 kinematic distributions. Distributions in which the shapes of data and standard model prediction are in relative disagreement correspond to large positive $\sigma$. The solid (black) curves indicate expected distributions, if the data were truly drawn from the standard model background. Interest is focused on the entries in the tails of the upper distribution and the high tail of the lower distribution. The final state entering the upper histogram at $-4.03 \sigma$ is the VISTA $3 j \tau$ final state, which heads Table II. Most of the distributions entering the lower histogram with $>4 \sigma$ derive from the $3 j \Delta R\left(j_{2}, j_{3}\right)$ discrepancy, discussed in the text.
nearby distinct jets correspond to a pattern of calorimetric energy deposits similar to a single massive jet. The underlying $3 j \Delta R\left(j_{2}, j_{3}\right)$ discrepancy is manifest in many other final states. The final state $b e j$, arising primarily from QCD production of three jets with one misreconstructed as an electron, shows a similar discrepancy in $\Delta R(j, b)$ in Fig. 5.

While these discrepancies are clearly statistically significant, basing a new physics claim around them is difficult. In the kinematic regime of the discrepancy, different algorithms to match exact leading order calculations with a parton shower lead to different predictions [36]. Newer predictions have not been systematically compared to LEP 1 data, which provide constraints on parton showering reflected in PYTHIA's tuning. Further investigation into obtaining an adequate QCD-based description of this discrepancy continues.

An additional 59 discrepant distributions reflect an inadequate modeling of the overall transverse boost of the system. The overall transverse boost of the primary physics objects in the event is attributed to two sources: the intrin-


FIG. 2 (color online). The invariant mass of the tau lepton and two leading jets in the final state consisting of three jets and one positively or negatively charged tau. (The VISTA final state naming convention gives the tau lepton a positive charge.) Data are shown as filled (black) circles, with the standard model prediction shown as the shaded (red) histogram. This is the most discrepant kinematic distribution in the final state exhibiting the largest population discrepancy.


FIG. 3 (color online). A shape discrepancy highlighted by VISTA in the final state consisting of exactly three reconstructed jets with $|\eta|<2.5$ and $p_{T}>17 \mathrm{GeV}$, and with one of the jets satisfying $|\eta|<1$ and $p_{T}>40 \mathrm{GeV}$. This distribution illustrates the effect underlying most of the VISTA shape discrepancies. Filled (black) circles show CDF data, with the shaded (red) histogram showing the prediction of PYTHIA. The discrepancy is clearly statistically significant, with statistical error bars smaller than the size of the data points. The vertical axis shows the number of events per bin, with the horizontal axis showing the angular separation ( $\Delta R=\sqrt{\Delta \eta^{2}+\delta \phi^{2}}$ ) between the second and third jets, where the jets are ordered according to decreasing transverse momentum. In the region $\Delta R\left(j_{2}, j_{3}\right) \gtrsim$ 2, populated primarily by initial state radiation, the standard model prediction can to some extent be adjusted. The region $\Delta R\left(j_{2}, j_{3}\right) \lesssim 2$ is dominated by final state radiation, the description of which is constrained by data from LEP 1 .
sic Fermi motion of the colliding partons within the proton, and soft or collinear radiation of the colliding partons as they approach collision. Together these effects are here referred to as "intrinsic $k_{T}$," representing an overall momentum kick to the hard scattering. Further discussion appears in Appendix A 2 c.

The remaining 13 discrepant distributions are seen to be due to the coarseness of the VISTA correction model. Most of these discrepancies, which are at the level of $10 \%$ or less when expressed as (data - theory)/theory, arise from modeling most fake rates as independent of transverse momentum.

In summary, this global analysis of the bulk features of the high- $p_{T}$ data has not yielded a discrepancy motivating a new physics claim. There are no statistically significant population discrepancies in the 344 populated final states considered, and although there are several statistically significant discrepancies among the 16486 kinematic distributions investigated, the nature of these discrepancies makes it difficult to use them to support a new physics claim.


FIG. 4 (color online). The jet mass distribution in the $b j$ final state with $\sum p_{T}>400 \mathrm{GeV}$. The $3 j \Delta R\left(j_{2}, j_{3}\right)$ discrepancy illustrated in Fig. 3 manifests itself also by producing jets more massive in data than predicted by PYTHIA's showering algorithm. The mass of a jet is determined by treating energy deposited in each calorimeter tower as a massless 4 -vector, summing the 4 vectors of all towers within the jet, and computing the mass of the resulting (massive) 4 -vector.

This global analysis of course cannot conclude with certainty that there is no new physics hiding in the CDF data. The VISTA population and shape statistics may be insensitive to a small excess of events appearing at large


FIG. 5 (color online). The distribution of $\Delta R$ between the jet and $b$-tagged jet in the final state $b e j$. The primary standard model contribution to this final state is QCD three jet production with one jet misreconstructed as an electron. The similarity to the $3 j \Delta R\left(j_{2}, j_{3}\right)$ discrepancy illustrated in Fig. 3 in the region $\Delta R(j, b)<2$ is clear. Less clear is the underlying explanation for the difference with respect to Fig. 3 in the region $\Delta R(j, b)>2$.
$\sum p_{T}$ in a highly populated final state. For such signals another algorithm is required.

## IV. SLEUTH

Taking a broad view of all proposed models that might extend the standard model, a profound commonality is noted: nearly all predict an excess of events at high $p_{T}$, concentrated in a particular final state. The second stage of this research program involves the systematic search for such physics using an algorithm called SLEUTH [37]. SLEUTH is quasi-model-independent, where "quasi" refers to the assumption that the first sign of new physics will appear as an excess of events in some final state at large summed scalar transverse momentum ( $\sum p_{T}$ ).

The sLeuth algorithm used by CDF in Tevatron run II is essentially that developed by D0 in Tevatron run I [38-40], and subsequently improved by H1 in HERA run I [41], with small modifications.

SLEUTH's definition of interest relies on the following assumptions:
(1) The data can be categorized into exclusive final states in such a way that any signature of new physics is apt to appear predominantly in one of these final states.
(2) New physics will appear with objects at high summed transverse momentum ( $\sum p_{T}$ ) relative to standard model and instrumental background.
(3) New physics will appear as an excess of data over standard model and instrumental background.

## A. Algorithm

The sLEUTH algorithm consists of three steps, following the above three assumptions.

## 1. Final states

In the first step of the algorithm, all events are placed into exclusive final states as in VISTA, with the following modifications.
(i) Jets are identified as pairs, rather than individually, to reduce the total number of final states and to keep signal events with one additional radiated gluon within the same final state. Final state names include " $n j j$ " if $n$ jet pairs are identified, with possibly one unpaired jet assumed to have originated from a radiated gluon.
(ii) The present understanding of quark flavor suggests that $b$ quarks should be produced in pairs. Bottom quarks are identified as pairs, rather than individually, to increase the robustness of identification and to reduce the total number of final states. Final state names include " $n b b$ " if $n b$ pairs are identified.
(iii) Final states related through global charge conjugation are considered to be equivalent. Thus $e^{+} e^{-} \gamma$
is a different final state than $e^{+} e^{+} \gamma$, but $e^{+} e^{+} \gamma$ and $e^{-} e^{-} \gamma$ together make up a single SLEUTH final state.
(iv) Final states related through global interchange of the first and second generation are considered to be equivalent. Thus $e^{+} p \gamma$ and $\mu^{+} p \gamma$ together make up a single sleuth final state. The decision to consider third generation objects ( $b$ quarks and $\tau$ leptons) differently from first and second generation objects reflects theoretical prejudice that the third generation may be special, and the experimental ability (in the case of $b$ quarks) and experimental challenge (in the case of $\tau$ leptons) in the identification of third generation objects.
The symbol $\ell$ is used to denote electron or muon. The symbol $W$ is used in naming final states containing one electron or muon, significant missing momentum, and perhaps other nonleptonic objects. Thus the final states $e^{+} \not p \gamma, e^{-} \not p \gamma, \mu^{+} \not p \gamma$, and $\mu^{-} p \gamma \gamma$ are combined into the sleuth final state $W \gamma$. A table showing the relationship between vISTA and sLeuth final states is provided in Appendix B 1.

## 2. Variable

The second step of the algorithm considers a single variable in each exclusive final state: the summed scalar transverse momentum of all objects in the event ( $\sum p_{T}$ ). Assuming momentum conservation in the plane transverse to the axis of the colliding beams,

$$
\begin{equation*}
\sum_{i} \vec{p}_{i}+\overrightarrow{\mathrm{uncl}}+\vec{p}=\overrightarrow{0}, \tag{3}
\end{equation*}
$$

where the sum over $i$ represents a sum over all identified objects in the event, the $i$ th object has momentum $\vec{p}_{i}$, uncl denotes the vector sum of all momentum visible in the detector but not clustered into an identified object, $\vec{b}$ denotes the missing momentum, and the equation is a twocomponent vector equality for the components of the momentum along the two spatial directions transverse to the axis of the colliding beams. The SLEUTH variable $\sum p_{T}$ is then defined by

$$
\begin{equation*}
\sum p_{T} \equiv \sum_{i}\left|\vec{p}_{i}\right|+|\overrightarrow{\text { uncl }}|+|\vec{p}|, \tag{4}
\end{equation*}
$$

where only the momentum components transverse to the axis of the colliding beams are considered when computing magnitudes.

## 3. Regions

The algorithm's third step involves searching for regions in which more events are seen in the data than expected from standard model and instrumental background. This
search is performed in the variable space defined in the second step of the algorithm, for each of the exclusive final states defined in the first step.

The steps of the search can be sketched as follows.
(i) In each final state, the regions considered are the one-dimensional intervals in $\sum p_{T}$ extending from each data point up to infinity. A region is required to contain at least three data events, as described in Appendix B.
(ii) In a particular final state, the data point with the $d$ th largest value of $\sum p_{T}$ defines an interval in the variable $\sum p_{T}$ extending from this data point up to infinity. This semi-infinite interval contains $d$ data events. The standard model prediction in this interval, estimated from the VISTA comparison described above, integrates to $b$ predicted events. In this final state, the interest of the $d$ th region is defined as the Poisson probability $p_{d}=$ $\sum_{i=d}^{\infty} \frac{b^{i}}{i!} e^{-b}$ that the standard model background $b$ would fluctuate up to or above the observed number of data events $d$ in this region. The most interesting region in this final state is the one with smallest Poisson probability.
(iii) For this final state, pseudo experiments are generated, with pseudo data pulled from the standard model background. For each pseudo experiment, the interest of the most interesting region is calculated. An ensemble of pseudo experiments determines the fraction $\mathcal{P}$ of pseudo experiments in this final state in which the most interesting region is more interesting than the most interesting region in this final state observed in the data. If there is no new physics in this final state, $\mathcal{P}$ is expected to be a random number pulled from a uniform distribution in the unit interval. If there is new physics in this final state, $\mathcal{P}$ is expected to be small.
(iv) Looping over all final states, $\mathcal{P}$ is computed for each final state. The minimum of these values is denoted $\mathcal{P}_{\text {min }}$. The most interesting region in the final state with smallest $\mathcal{P}$ is denoted $\mathcal{R}$.
(v) The interest of the most interesting region $\mathcal{R}$ in the most interesting final state is defined by $\tilde{\mathcal{P}}=1-$ $\prod_{a}\left(1-\hat{p}_{a}\right)$, where the product is over all SLEUTH final states $a$, and $\hat{p}_{a}$ is the lesser of $\mathcal{P}_{\text {min }}$ and the probability for the total number of events predicted by the standard model in the final state $a$ to fluctuate up to or above three data events. The quantity $\tilde{\mathcal{P}}$ represents the fraction of hypothetical similar CDF experiments that would produce a final state with $\mathcal{P}<\mathcal{P}_{\text {min }}$. The range of $\tilde{\mathcal{P}}$ is the unit interval. If the data are distributed according to standard model prediction, $\tilde{\mathcal{P}}$ is expected to be a random number pulled from a uniform distribution in the unit interval. If new physics is present, $\tilde{\mathcal{P}}$ is expected to be small.

## 4. Output

The output of the algorithm is the most interesting region $\mathcal{R}$ observed in the data, and a number $\tilde{\mathcal{P}}$ quantifying the interest of $\mathcal{R}$. A reasonable threshold for discovery is $\tilde{\mathcal{P}} \leqq 0.001$, which corresponds loosely to a local $5 \sigma$ effect after the trials factor is accounted for.

Although no integration over systematic errors is performed in computing $\tilde{\mathcal{P}}$, systematic uncertainties do affect the final SLEUTH result. If SLEUTH highlights a discrepancy in a particular final state, explanations in terms of a correction to the background estimate are considered. This process necessarily requires physics judgement. A reasonable explanation of a SLEUTH discrepancy in terms of an inadequacy in the modeling of the detector response or standard model prediction that is consistent with external information is fed back into the VISTA correction model and tested for global consistency. In this way, plausible explanations for discrepancies observed by SLEUTH are incorporated into the VISTA correction model. This iteration continues until either all reasonable explanations for a significant SLEUTH discrepancy are exhausted, resulting in a possible new physics claim, or no significant SLEUTH discrepancy remains.

## B. Sensitivity

Two important questions must be asked:
(i) Will SLEUTH find nothing if there is nothing to be found?
(ii) Will SLEUTH find something if there is something to be found?
If there is nothing to be found, SLEUTH will find nothing 999 times out of 1000, given a uniform distribution of $\tilde{\mathcal{P}}$ and a discovery threshold of $\tilde{\mathcal{P}} \leqslant 0.001$. The uniform distribution of $\tilde{\mathcal{P}}$ in the absence of new physics is illustrated in Fig. 6, using values of $\tilde{\mathcal{P}}$ obtained in pseudo experiments with pseudo data generated from the standard model prediction. SLEUTH will of course return spurious signals if provided improperly modeled backgrounds. The algorithm directly addresses the issue of whether an observed hint is due to a statistical fluctuation. SLEUTH itself is unable to address systematic mismeasurement or incorrect modeling, but is quite useful in bringing these to attention.

The answer to the second question depends to what degree the new physics satisfies the three assumptions on which SLEUTH is based: new physics will appear predominantly in one final state, at high summed scalar transverse momentum, and as an excess of data over standard model prediction. SLEUTH's sensitivity to any particular new phenomenon depends on the extent to which this new phenomenon satisfies these assumptions.

## 1. Known standard model processes

Consideration of specific standard model processes can provide intuition for SLEUTH's sensitivity to new physics.



FIG. 6 (color online). Distribution of $10^{3} \tilde{P}$ values from $10^{3} \mathrm{CDF}$ pseudo experiments, in which pseudo data are pulled from the standard model prediction. The distribution of $\tilde{P}$ is shown in the unit interval (left), with one entry for each of the CDF pseudo experiments. The distribution of $\tilde{P}$ translated into units of standard deviations is also shown (right). The distribution of $\tilde{P}$ from pseudo experiments is consistent with flat (left), and consistent with a Gaussian when translated into units of standard deviations (right), as expected.

This section tests SLEUTH's sensitivity to the production of top quark pairs, $W$ boson pairs, single top, and the Higgs boson.
(a) Top quark pairs.-Top quark pair production results in two $b$ jets and two $W$ bosons, each of which may decay leptonically or hadronically. The $W$ branching ratios are such that this signal predominantly populates the SLEUTH final state $W b \bar{b} j j$, where " $W$ ", denotes an electron or muon and significant missing momentum. Although the final states $\ell^{+} \ell^{-} \not p b \bar{b}$ were important in verifying the top quark pair production hypothesis in the initial observation by CDF [5] and D0 [6] in 1995, most of the statistical power came from the final state $W b \bar{b} j j$. The all hadronic decay final state $b \bar{b} 4 j$ has only convincingly been seen after integrating substantial run II luminosity [42]. SLEUTH's first assumption that new physics will appear predominantly in one final state is thus reasonably well satisfied. Since the top quark has a mass of $170.9 \pm 1.8 \mathrm{GeV}$ [43], the production of two such objects leads to a signal at large $\sum p_{T}$ relative to the standard model background of $W$ bosons produced in association with jets, satisfying SLEUTH's second and third assumptions. SLEUTH is expected to perform reasonably well on this example.
To quantitatively test SLEUTH's sensitivity to top quark pair production, this process is removed from the standard model prediction, and the values of the VISTA correction factors are reobtained from a global fit assuming ignorance of $t \bar{t}$ production. SLEUTH easily discovers $t \bar{t}$ production in $927 \mathrm{pb}^{-1}$ in the final states $b \bar{b} \ell^{+} \ell^{\prime-} \not p$ and $W b \bar{b} j j$, shown in Fig. 7. SLEUTH finds $\mathcal{P}_{b \bar{b} \ell^{+} \ell^{\prime-} p}<1.5 \times 10^{-8}$ and $\mathcal{P}_{W b \bar{b} j j}<8.3 \times 10^{-7}$, far surpassing the discovery threshold of $\tilde{\mathcal{P}} \leqq 0.001$.

The test is repeated as a function of assumed integrated luminosity, and SLEUTH is found to highlight the top quark signal at an integrated luminosity of roughly $80 \pm 60 \mathrm{pb}^{-1}$, where the large variation arises from statistical fluctuations in the $t \bar{t}$ signal events. Weaker constraints on the VISTA correction factors at lower integrated luminosity marginally increase the integrated luminosity required to claim a discovery.
(b) $W$ boson pairs.-The sensitivity to standard model $W W$ production is tested by removing this process from the standard model background prediction and allowing the VISTA correction factors to be refit. In $927 \mathrm{pb}^{-1}$ of Tevatron run II data, SLEUTH identifies an excess in the final state $\ell^{+} \ell^{\prime-} \not p$, consisting of an electron and muon of opposite sign and missing momentum. This excess corresponds to $\tilde{\mathcal{P}}<2 \times$ $10^{-4}$, sufficient for the discovery of $W W$, as shown in Fig. 8.
(c) Single top.-Single top quarks are produced weakly, and predominantly decay to populate the SLEUTH final state $W b \bar{b}$, satisfying SLEUTH's first assumption. Single top production will appear as an excess of events, satisfying SLEUTH's third assumption. SLEUTH's second assumption is not well satisfied for this example, since single top production does not lie at large $\sum p_{T}$ relative to other standard model processes. SLEUTH is thus expected to be outperformed by a targeted search in this example.
(d) Higgs boson.-Assuming a standard model Higgs boson of mass $m_{h}=115 \mathrm{GeV}$, the dominant observable production mechanism is $p \bar{p} \rightarrow W h$ and $p \bar{p} \rightarrow Z h$, populating the final states $W b \bar{b}, \ell^{+} \ell^{-} b \bar{b}$, and $\not p b \bar{b}$. The signal is thus spread over three


FIG. 7 (color online). Top left: the SLEUTH final state $b \bar{b} \ell^{+} \ell^{\prime-} \not p$, consisting of events with one electron and one muon of opposite sign, missing momentum, and two or three jets, one or two of which are $b$-tagged. Data corresponding to $927 \mathrm{pb}^{-1}$ are shown as filled (black) circles; the standard model prediction is shown as the (red) shaded histogram. Top right: the same final state with $t \bar{t}$ subtracted from the standard model prediction. Bottom row: the SLEUTH final state $W b \bar{b} j j$, with the standard model $t \bar{t}$ contribution included (lower left) and removed (lower right). Significant discrepancies far surpassing SLEUTH's discovery threshold are observed in these final states with $t \bar{t}$ removed from the standard model background estimate. If the top quark had not been predicted, SLEUTH would have discovered it.

SLEUTH final states. Events in the last of these ( $\not p b \bar{b}$ ) do not pass the VISTA event selection, which does not use $\not p$ as a trigger object. SLEUTH's first assumption is thus poorly satisfied for this example. The standard model Higgs boson signal will appear as an excess, but as in the case of single top production it does not appear at particularly large $\sum p_{T}$ relative to other standard model processes. Since the standard model Higgs boson poorly satisfies SLEUTH's first and second assumptions, a targeted search for this specific signal is expected to outperform sleuth.

## 2. Specific models of new physics

To build intuition for SLeUth's sensitivity to new physics signals, several sensitivity tests are conducted for a variety of new physics possibilities. Some of the new physics models chosen have already been considered by more specialized analyses within CDF, making possible a comparison between SLEUTH's sensitivity and the sensitivity of these previous analyses.

SLEUTH's sensitivity can be compared to that of a dedicated search by determining the minimum new physics cross section $\sigma_{\text {min }}$ required for a discovery by each. The discovery for sLEUTH occurs when $\tilde{\mathcal{P}}<0.001$. In most


FIG. 8 (color online). Left: the final state $\ell^{+} \ell^{\prime-} \not p$, consisting of events with an electron and muon of opposite sign and missing transverse momentum, in $927 \mathrm{pb}^{-1}$ of CDF data. Right: the same final state with standard model $W W, W Z$, and $Z Z$ contributions subtracted, and with the VISTA correction factors refit in the absence of these contributions. SLEUTH finds the final state $\ell^{+} \ell^{\prime-} \not p$ to contain a discrepancy surpassing the discovery threshold of $\tilde{\mathcal{P}}<0.001$ with the processes $W W, W Z$, and $Z Z$ removed from the standard model background.

SLEUTH regions satisfying the discovery threshold of $\tilde{\mathcal{P}}<0.001$, the probability for the predicted number of events to fluctuate up to or above the number of events observed corresponds to greater than $5 \sigma$. The discovery for the dedicated search occurs when the observed excess of data corresponds to a $5 \sigma$ effect. Smaller $\sigma_{\text {min }}$ corresponds to greater sensitivity.

The sensitivity tests are performed by first generating pseudo data from the standard model background prediction. Signal events for the new physics model are generated, passed through the chain of CDF detector simulation and event reconstruction, and consecutively added to the pseudo data until SLEUTH finds $\tilde{\mathcal{P}}<0.001$. The number of signal events needed to trigger discovery is used to calculate $\sigma_{\text {min }}$.

For each dedicated analysis to which SLEUTH is compared, the number of standard model events expected in $927 \mathrm{pb}^{-1}$ within the region targeted is used to calculate the number of signal events required in that region to produce a discrepancy corresponding to $5 \sigma$. Using the signal efficiency determined in the dedicated analysis, $\sigma_{\text {min }}$ is calculated. The effect of systematic uncertainties are removed from the dedicated analyses and are not included for SLEUTH. The inclusion of systematic uncertainties will reduce the sensitivity of both SLEUTH and the dedicated analysis to the extent that the systematic parameters are allowed to vary. VISTA and SLEUTH have the advantage of using a large data set to constrain them.

The results of five such sensitivity tests are summarized in Table III. SLEUTH is seen to perform comparably to targeted analyses on models satisfying the assumptions
on which SLEUTH is based. For models in which SLEUTH's simple use of $\sum p_{T}$ can be improved upon by optimizing for a specific feature, a targeted search may be expected to achieve greater sensitivity. One of the important features of SLEUTH is that it not only performs reasonably well, but that it does so broadly. In model 1, a search for a particular model point in a gauge mediated supersymmetry breaking (GMSB) scenario, SLEUTH gains an advantage by exploiting a final state not considered in the targeted analysis [44]. In model 2, a search for a $Z^{\prime}$ decaying to lepton pairs, the targeted analysis [45] exploits the narrow resonance in the $e^{+} e^{-}$invariant mass. In models 3 and 4, which are searches for a hadronically decaying $Z^{\prime}$ of different masses, there is no targeted analysis against which to compare. In Model 5, a search for a $Z^{\prime} \rightarrow t \bar{t}$ resonance, the signal appears at large summed scalar transverse momentum in a particular final state, resulting in comparable sensitivity between SLEUTH and the targeted analysis [46].

## C. Results

The distribution of $\mathcal{P}$ for the final states considered by SLEUTH in the data is shown in Fig. 9. The concavity of this distribution reflects the degree to which the correction model described in Sec. III F has been tuned. A crude correction model tends to produce a distribution that is concave upwards, as seen in this figure, while an overly tuned correction model produces a distribution that is concave downwards, with more final states than expected having $\mathcal{P}$ near the midpoint of the unit interval.

The most interesting final states identified by SLEUTH are shown in Fig. 10, together with a quantitative measure $(\mathcal{P})$

TABLE III. Summary of SLEUTH's sensitivity to several new physics models, expressed in terms of the minimum production cross section needed for discovery with $927 \mathrm{pb}^{-1}$. Where available, a comparison is made to the sensitivity of a dedicated search for this model. The solid (red) box represents SLEUTH's sensitivity, and the open (white) box represents the sensitivity of the dedicated analysis. Systematic uncertainties are not included in the sensitivity calculation. The width of each box shows typical variation under fluctuation of data statistics. In models 3 and 4, there is no targeted analysis available for comparison. SLEUTH is seen to perform comparably to the targeted analyses on models satisfying the assumptions on which SLEUTH is based.

$2 \quad Z^{\prime} \rightarrow \ell^{+} \ell^{-}, m_{Z^{\prime}}=250 \mathrm{GeV}$, with standard model couplings to leptons.

3
$Z^{\prime} \rightarrow q \bar{q}, m_{Z^{\prime}}=700 \mathrm{GeV}$, with standard model couplings to quarks.
4
$Z^{\prime} \rightarrow q \bar{q}, \quad m_{Z^{\prime}}=1 \mathrm{TeV}$,
with standard model couplings to quarks.
5
$Z^{\prime} \rightarrow t \bar{t}, \quad m_{Z^{\prime}}=500 \mathrm{GeV}$,
with standard model couplings to $t \bar{t}$.

of the interest of the most interesting region in each final state, determined as described in Sec. IVA 3. The legends of Fig. 10 show the primary contributing standard model processes in each of these final states, together with the fractional contribution of each. The top six final states, which correspond to entries in the leftmost bin in Fig. 9.


FIG. 9 (color online). The distribution of $\mathcal{P}$ in the data, with one entry for each final state considered by SLEUTH.
span a range of populations, relevant physics objects, and important background contributions.

The final state $b \bar{b}$, consisting of two or three reconstructed jets, one or two of which are $b$-tagged, heads the list. These events enter the analysis by satisfying the VISTA offline selection requiring one or more jets or $b$-jets with $p_{T}>200 \mathrm{GeV}$. The definition of SLEUTH's $\sum p_{T}$ variable is such that all events in this final state consequently have $\sum p_{T}>400 \mathrm{GeV}$. SLEUTH chooses the region $\sum p_{T}>$ 469 GeV , which includes nearly $10^{4}$ data events. The standard model prediction in this region is sensitive to the $b$-tagging efficiency $p(b \rightarrow b)$ and the fake rate $p(j \rightarrow b)$, which have few strong constraints on their values for jets with $p_{T}>200 \mathrm{GeV}$ other than those imposed by other VISTA kinematic distributions within this and a few other related final states. For this region slevth finds $\mathcal{P}_{b \bar{b}}=$ 0.0055 , which is unfortunately not statistically significant after accounting for the trials factor associated with looking in many different final states, as discussed below.

The final state $j \not p$, consisting of events with one reconstructed jet and significant missing transverse momentum, is the second final state identified by SLEUTH. The primary background is due to noncollision processes, including cosmic rays and beam halo backgrounds, whose estimation is discussed in Appendix A 2 a. Since the hadronic energy


FIG. 10 (color online). The most interesting final states identified by SLEUTH. The region chosen by SLEUTH, extending up to infinity, is shown by the (blue) arrow just below the horizontal axis. Data are shown as filled (black) circles, and the standard model prediction is shown as the shaded (red) histogram. The SLEUTH final state is labeled in the upper left corner of each panel, with $\ell$ denoting $e$ or $\mu$, and $\ell^{+} \ell^{\prime+}$ denoting an electron and muon with the same electric charge. The number at upper right in each panel shows $\mathcal{P}$, the fraction of hypothetical similar experiments in which something at least as interesting as the region shown would be seen in this final state. The inset in each panel shows an enlargement of the region selected by SLEUTH, together with the number of events (SM) predicted by the standard model in this region, and the number of data events (d) observed in this region.
is not required to be deposited in time with the beam crossing, SLEUTH's analysis of this final state is sensitive to particles with a lifetime between 1 ns and $1 \mu \mathrm{~s}$ that lodge temporarily in the hadronic calorimeter, complementing Ref. [47].

The final states $\ell^{+} \ell^{\prime+} \not p j j, \ell^{+} \ell^{\prime+} \not p$, and $\ell^{+} \ell^{\prime+}$ all contain an electron ( $\ell$ ) and muon ( $\ell^{\prime}$ ) with identical reconstructed charge (either both positive or both negative). The final states with and without missing transverse momentum are qualitatively different in terms of the standard model processes contributing to the background estimate, with the final state $\ell^{+} \ell^{\prime-}$ composed mostly of dijets where one jet is misreconstructed as an electron and a second jet is misreconstructed as a muon; $Z \rightarrow \tau^{+} \tau^{-}$, where one tau decays to a muon and the other to a leading $\pi^{0}$, one of the two photons from which converts while traveling through the silicon support structure to result in an electron reconstructed with the same sign as the muon, as described in Appendix A 1 ; and $Z \rightarrow \mu^{+} \mu^{-}$, in which a photon is produced, converts, and is misreconstructed as an electron. The final states containing missing transverse momentum are dominated by the production of $W(\rightarrow \mu \nu)$ in association with one or more jets, with one of the jets misreconstructed as an electron. The muon is significantly more likely than the electron to have been produced in the hard interaction, since the fake rate $p(j \rightarrow \mu)$ is roughly an order of magnitude smaller than the fake rate $p(j \rightarrow e)$, as observed in Table I. The final state $\ell^{+} \ell^{\prime-} \not p j j$, which contains two or three reconstructed jets in addition to the electron, muon, and missing transverse momentum, also has some contribution from $W Z$ and top quark pair production.

The final state $\tau \not p$ contains one reconstructed tau, significant missing transverse momentum, and one reconstructed jet with $p_{T}>200 \mathrm{GeV}$. This final state in principle also contains events with one reconstructed tau, significant missing transverse momentum, and zero reconstructed jets, but such events do not satisfy the offline selection criteria described in Sec. III C. Roughly half of the background is noncollision, in which two different cosmic ray muons (presumably from the same cosmic ray shower) leave two distinct energy deposits in the CDF hadronic calorimeter, one with $p_{T}>200 \mathrm{GeV}$, and one with a single associated track from a $p \bar{p}$ collision occurring during the same bunch crossing. Less than a single event is predicted from this noncollision source (using techniques described in Appendix A 2 a) over the past five years of Tevatron running.

In these CDF data, SLEUTH finds $\tilde{\mathcal{P}}=0.46$. The fraction of hypothetical similar CDF experiments (assuming a fixed standard model prediction, detector simulation, and correction model) that would exhibit a final state with $\mathcal{P}$ smaller than the smallest $\mathcal{P}$ observed in the CDF run II data is approximately $46 \%$. The actual value obtained for $\tilde{\mathcal{P}}$ is not of particular interest, except to note that this value is significantly greater than the threshold of $\lesssim 0.001$ re-
quired to claim an effect of statistical significance. SLEUTH has not revealed a discrepancy of sufficient statistical significance to justify a new physics claim.

Systematics are incorporated into SLEUTH in the form of the flexibility in the VISTA correction model, as described previously. This flexibility is significantly more important in practice than the uncertainties on particular correction factor values obtained from the fit, although the latter are easier to discuss. The relative importance of correction factor value uncertainties on SLEUTH's result depends on the number of predicted standard model events (b) in SLEUTH's high $\sum p_{T}$ tail. The uncertainties on the correction factors of Table I are such that the appropriate addition in quadrature gives a typical uncertainty of $\approx 10 \%$ on the total background prediction in each final state. Using $\sigma_{\text {sys }} \approx 10 \% \times b$ and $\sigma_{\text {stat }} \approx \sqrt{b}$, the relative importance of systematic uncertainty and statistical uncertainty is estimated to be $\sigma_{\text {sys }} / \sigma_{\text {stat }}=10 \% \times b / \sqrt{b}$. The importance of systematic and statistical uncertainties are thus comparable for high $\sum p_{T}$ tails containing $b \sim 100$ predicted events. The effect of systematic uncertainties is provided in this approximation rather than through a rigorous integration over these uncertainties as nuisance parameters due to the high computational cost of performing the integration. This estimate of systematic uncertainty is valid only within the particular correction model resulting in the list of correction factors shown in Table I; additional changes to the correction model may result in larger variation. The inclusion of additional systematic uncertainties does not qualitatively change the conclusion that SLEUTH has not revealed a discrepancy of sufficient statistical significance to justify a new physics claim.

Because of the large number of final states considered, there are regions (such as those shown in Fig. 10) in which the probability for the standard model prediction to fluctuate up to or above the number of events observed in the data corresponds to a significance exceeding $3 \sigma$ if the appropriate trials factor is not accounted for. A doubling of data may therefore result in discovery. In particular, although the excesses in Fig. 10 are currently consistent with simple statistical fluctuations, if any of them are genuinely due to new physics, SLEUTH will find they pass the discovery threshold of $\tilde{\mathcal{P}}<0.001$ with roughly a doubling of data.

## V. CONCLUSIONS

A broad search for new physics (VISTA) has been performed in $927 \mathrm{pb}^{-1}$ of CDF run II data. A complete standard model background estimate has been obtained and compared with data in 344 populated exclusive final states and 16486 relevant kinematic distributions, most of which have not been previously considered. Consideration of exclusive final state populations yields no statistically significant $(>3 \sigma)$ discrepancy after the trials factor is accounted for. Quantifying the difference in shape of kine-
matic distributions using the Kolmogorov-Smirnov statistic, significant discrepancies are observed between data and standard model prediction. These discrepancies are believed to arise from mismodeling of the parton shower and intrinsic $k_{T}$, and represent observables for which a QCD-based understanding is highly motivated. None of the shape discrepancies highlighted motivates a new physics claim.

A further systematic search (SLEUTH) for regions of excess on the high- $\sum p_{T}$ tails of exclusive final states has been performed, representing a quasi-model-independent search for new electroweak scale physics. Most of the exclusive final states searched with SLEUTH have not been considered by previous Tevatron analyses. A measure of interest rigorously accounting for the trials factor associated with looking in many regions with few events is defined and used to quantify the most interesting region observed in the CDF run II data. No region of excess on the high- $\sum p_{T}$ tail of any of the SLEUTH exclusive final states surpasses the discovery threshold.

Although this global analysis of course cannot prove that no new physics is hiding in these data, this broad search of the Tevatron run II data represents one of the single most encompassing tests of the particle physics standard model at the energy frontier.

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## APPENDIX A: VISTA CORRECTION MODEL DETAILS

This appendix contains details of the VISTA correction model. Appendix A 1 covers the physical mechanisms underlying fake rates. Appendix A 2 contains information about additional background sources, including backgrounds from cosmic rays and beam halo, multiple interactions, and the effects of intrinsic $k_{T}$. Appendix A 3 contains details of the VISTA correction factor fit, including the construction of the $\chi^{2}$ function that is minimized and the resulting covariance matrix. Appendix A 4 discusses the values of the correction factors that are obtained.

## 1. Fake rate physics

The following facts begin to build a unified understanding of fake rates for electrons, muons, taus, and photons. This understanding is woven throughout the VISTA correction model and significantly informs and constrains the VISTA correction process. Explicit constraints derived from these studies are provided in Appendix A 3. The underlying physical mechanisms for these fakes lead to simple and well-justified relations among them.

Table IV shows the response of the CDF detector simulation, reconstruction, and object identification algorithms to single particles. Using a single particle gun, $10^{5}$ particles of each type shown at the left of the table are shot with $p_{T}=25 \mathrm{GeV}$ into the CDF detector, uniformly distributed in $\theta$ and in $\phi$. The resulting reconstructed object types are shown at the top of the table, labeling the columns. The first four entries on the diagonal at upper left show the efficiency for reconstructing electrons and muons [48]. The fraction of electrons misidentified as photons, shown in the top row, seventh column, is seen to be roughly equal to the fraction of photons identified as electrons or positrons, shown in the fifth row, first and second columns, and measures the number of radiation lengths in the innermost regions of the CDF tracker. The fraction of $B$ mesons identified as electrons or muons, primarily through semileptonic decay, are shown in the four left columns, eleventh through fourteenth rows. Other entries provide similarly useful information, most easily comprehensible from simple physics.

The transverse momenta of the objects reconstructed from single particles are displayed in Fig. 11. The relative resolutions for the measurement of electron and muon momenta are shown in the first four histograms on the diagonal at upper left. The histograms in the left column, sixth through eighth rows, show that single neutral pions misreconstructed as electrons have their momenta well measured, while single charged pions misreconstructed as electrons have their momenta systematically undermeasured, as discussed below. The histogram in the top row, second column from the right, shows that electrons misreconstructed as jets have their energies systematically overmeasured. Other histograms in Fig. 11 contain simi-

TABLE IV. Central single particle misidentification matrix. Using a single particle gun, $10^{5}$ particles of each type shown at the left of the table are shot with $p_{T}=25 \mathrm{GeV}$ into the central CDF detector, uniformly distributed in $\theta$ and in $\phi$. The resulting reconstructed object types are shown at the top of the table, labeling the table columns. Thus the rightmost element of this matrix in the fourth row from the bottom shows $p\left(\tau^{-} \rightarrow b\right.$ ), the number of negatively charged tau leptons (out of $10^{5}$ ) reconstructed as a $b$-tagged jet.

|  | $e^{+}$ | $e^{-}$ | $\mu^{+}$ | $\mu^{-}$ | $\tau^{+}$ | $\tau^{-}$ | $\gamma$ | $j$ | $b$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $e^{+}$ | 62228 | 33 | 0 | 0 | 182 | 0 | 2435 | 28140 | 0 |
| $e^{-}$ | 24 | 62324 | 0 | 0 | 0 | 192 | 2455 | 28023 | 1 |
| $\mu^{+}$ | 0 | 0 | 50491 | 0 | 6 | 0 | 0 | 606 | 0 |
| $\mu^{-}$ | 0 | 1 | 0 | 50294 | 0 | 6 | 0 | 577 | 0 |
| $\gamma$ | 1393 | 1327 | 0 | 0 | 1 | 1 | 67679 | 21468 | 0 |
| $\pi^{0}$ | 1204 | 1228 | 0 | 0 | 5 | 8 | 58010 | 33370 | 0 |
| $\pi^{+}$ | 266 | 0 | 115 | 0 | 41887 | 6 | 95 | 54189 | 37 |
| $\pi^{-}$ | 1 | 361 | 0 | 88 | 13 | 41355 | 148 | 54692 | 44 |
| $K^{+}$ | 156 | 1 | 273 | 0 | 42725 | 7 | 37 | 52317 | 24 |
| $K^{-}$ | 1 | 248 | 0 | 165 | 28 | 41562 | 115 | 53917 | 22 |
| $B^{+}$ | 100 | 0 | 77 | 1 | 100 | 10 | 40 | 66062 | 25861 |
| $B^{-}$ | 2 | 85 | 3 | 68 | 11 | 99 | 45 | 66414 | 25621 |
| $B^{0}$ | 88 | 27 | 87 | 17 | 77 | 32 | 21 | 65866 | 25046 |
| $\overline{B^{0}}$ | 17 | 79 | 11 | 71 | 41 | 77 | 21 | 66034 | 25103 |
| $D^{+}$ | 126 | 6 | 62 | 0 | 1485 | 67 | 207 | 79596 | 11620 |
| $D^{-}$ | 4 | 134 | 3 | 74 | 64 | 1400 | 234 | 79977 | 11554 |
| $D^{0}$ | 60 | 13 | 27 | 2 | 312 | 1053 | 248 | 88821 | 5487 |
| $\overline{D^{0}}$ | 15 | 46 | 5 | 28 | 1027 | 253 | 237 | 89025 | 5480 |
| $K_{L}^{0}$ | 1 | 4 | 0 | 0 | 71 | 60 | 202 | 96089 | 26 |
| $K_{S}^{0}$ | 26 | 31 | 2 | 1 | 170 | 525 | 9715 | 76196 | 0 |
| $\tau^{+}$ | 1711 | 13 | 1449 | 0 | 4167 | 2 | 673 | 50866 | 607 |
| $\tau^{-}$ | 12 | 1716 | 0 | 1474 | 6 | 3940 | 621 | 51125 | 580 |
| $u$ | 8 | 10 | 1 | 0 | 446 | 31 | 247 | 94074 | 26 |
| $d$ | 3 | 4 | 0 | 0 | 64 | 308 | 191 | 94322 | 22 |
| $g$ | 2 | 0 | 0 | 0 | 17 | 14 | 12 | 81865 | 99 |

larly relevant information, easily overlooked without the benefit of this study, but understandable from basic physics considerations once the effect has been brought to attention.

Here and below $p(q \rightarrow X)$ denotes a quark fragmenting to $X$ carrying nearly all of the parent quark's energy, and $p(j \rightarrow X)$ denotes a parent quark or gluon being misreconstructed in the detector as $X$.

The probability for a light quark jet to be misreconstructed as an $e^{+}$can be written

$$
\begin{align*}
p\left(j \rightarrow e^{+}\right)= & p(q \rightarrow \gamma) p\left(\gamma \rightarrow e^{+}\right) \\
& +p\left(q \rightarrow \pi^{0}\right) p\left(\pi^{0} \rightarrow e^{+}\right) \\
& +p\left(q \rightarrow \pi^{+}\right) p\left(\pi^{+} \rightarrow e^{+}\right) \\
& +p\left(q \rightarrow K^{+}\right) p\left(K^{+} \rightarrow e^{+}\right) \tag{A1}
\end{align*}
$$

A similar equation holds for a light quark jet faking an $e^{-}$.
The probability for a light quark jet to be misreconstructed as a $\mu^{+}$can be written

$$
\begin{align*}
p\left(j \rightarrow \mu^{+}\right)= & p\left(q \rightarrow \pi^{+}\right) p\left(\pi^{+} \rightarrow \mu^{+}\right) \\
& +p\left(q \rightarrow K^{+}\right) p\left(K^{+} \rightarrow \mu^{+}\right) \tag{A2}
\end{align*}
$$

Here $p(\pi \rightarrow \mu)$ denotes pion decay-in-flight, and $p(K \rightarrow$
$\mu)$ denotes kaon decay-in-flight; other processes contribute negligibly. A similar equation holds for a light quark jet faking a $\mu^{-}$.

The only nonnegligible underlying physical mechanisms for a jet to fake a photon are for the parent quark or gluon to fragment into a photon or a neutral pion, carrying nearly all the energy of the parent quark or gluon. Thus

$$
\begin{align*}
p(j \rightarrow \gamma)= & p\left(q \rightarrow \pi^{0}\right) p\left(\pi^{0} \rightarrow \gamma\right) \\
& +p(q \rightarrow \gamma) p(\gamma \rightarrow \gamma) \tag{A3}
\end{align*}
$$

Up and down quarks and gluons fragment nearly equally to each species of pion; hence

$$
\begin{equation*}
\frac{1}{3} p(q \rightarrow \pi)=p\left(q \rightarrow \pi^{+}\right)=p\left(q \rightarrow \pi^{-}\right)=p\left(q \rightarrow \pi^{0}\right) \tag{A4}
\end{equation*}
$$

where $p(q \rightarrow \pi)$ denotes fragmentation into any pion carrying nearly all of the parent quark's energy. Fragmentation into each type of kaon also occurs with equal probability; hence


FIG. 11 (color online). Transverse momentum distribution of reconstructed objects (labeling columns) arising from single particles (labeling rows) with $p_{T}=25 \mathrm{GeV}$ shot from a single particle gun into the central CDF detector. The area under each histogram is equal to the number of events in the corresponding misidentification matrix element of Table IV, with the vertical axis of each histogram scaled to the peak of each distribution. A different vertical scale is used for each histogram, and histograms with fewer than ten events are not shown. The horizontal axis ranges from 0 to 50 GeV .


FIG. 12 (color online). A few of the most discrepant distributions in the final states $e j$ and $j \mu$, which are greatly affected by the fake rates $p(j \rightarrow e)$ and $p(j \rightarrow \mu)$, respectively. These distributions are among the 13 significantly discrepant distributions identified as resulting from coarseness of the correction model employed. The vertical axis shows the number of events; the horizontal axes show the transverse momentum and pseudorapidity of the lepton. Filled (black) circles show CDF data, and the shaded (red) histogram shows the standard model prediction. Events enter the $e j$ final state either on a central electron trigger with $p_{T}>25 \mathrm{GeV}$, or on a plug electron trigger with $p_{T}>40 \mathrm{GeV}$. The fake rate $p(j \rightarrow e)$ is significantly larger in the plug region than in the central region of the CDF detector. Muons are identified with separate detectors covering the regions $|\eta|<0.6$ and $0.6<|\eta|<1.0$.

$$
\begin{align*}
\frac{1}{4} p(q \rightarrow K) & =p\left(q \rightarrow K^{+}\right) \\
& =p\left(q \rightarrow K^{-}\right) \\
& =p\left(q \rightarrow K^{0}\right) \\
& =p\left(q \rightarrow \bar{K}^{0}\right), \tag{A5}
\end{align*}
$$

where $p(q \rightarrow K)$ denotes fragmentation into any kaon carrying nearly all of the parent quark's energy.

PYTHIA contains a parameter that sets the number of string fragmentation kaons relative to the number of fragmentation pions. The default value of this parameter, which has been tuned to LEP I data, is 0.3 ; for every 1 up quark and every 1 down quark, 0.3 strange quarks are produced. Strange particles are produced perturbatively in the hard interaction itself, and in perturbative radiation,
at a ratio larger than $0.3: 1: 1$. This leads to the inequality

$$
\begin{equation*}
0.3 \leqq \frac{p(q \rightarrow K)}{p(q \rightarrow \pi)}<1 \tag{A6}
\end{equation*}
$$

where $p(q \rightarrow K)$ and $p(q \rightarrow \pi)$ are as defined above.
The probability for a jet to be misreconstructed as a tau lepton can be written

$$
\begin{equation*}
p\left(j \rightarrow \tau^{+}\right)=p\left(j \rightarrow \tau_{1}^{+}\right)+p\left(j \rightarrow \tau_{3}^{+}\right), \tag{A7}
\end{equation*}
$$

where $p\left(j \rightarrow \tau_{1}^{+}\right)$denotes the probability for a jet to fake a 1-prong tau, and $p\left(j \rightarrow \tau_{3}^{+}\right)$denotes the probability for a jet to fake a 3 -prong tau. For 1-prong taus,


FIG. 13 (color online). A few of the most discrepant distributions in the final states $j \tau$ and $j \gamma$, which are greatly affected by the fake rates $p(j \rightarrow \tau)$ and $p(j \rightarrow \gamma)$, respectively. The vertical axis shows the number of events; the horizontal axes show the transverse momentum and pseudorapidity of the tau lepton and photon. Filled (black) circles show CDF data, and the shaded (red) histogram shows the standard model prediction. The distributions in the $j \gamma$ final state are among the 13 significantly discrepant distributions identified as resulting from coarseness of the correction model employed.

$$
\begin{align*}
p\left(j \rightarrow \tau_{1}^{+}\right)= & p\left(q \rightarrow \pi^{+}\right) p\left(\pi^{+} \rightarrow \tau^{+}\right) \\
& +p\left(q \rightarrow K^{+}\right) p\left(K^{+} \rightarrow \tau^{+}\right) \tag{A8}
\end{align*}
$$

Similar equations hold for negatively charged taus.
Figure 14 shows the probability for a quark (or gluon) to fake a one-prong tau, as a function of transverse momentum. Using fragmentation functions tuned on LEP 1 data, PYTHIA predicts the probability for a quark jet to fake a one-prong tau to be roughly 4 times the probability for a gluon jet to fake a one-prong tau. This difference in fragmentation is incorporated into VISTA's treatment of jets faking electrons, muons, taus, and photons. The VISTA correction model includes such correction factors as the probability for a jet with a parent quark to fake an electron (0033 and 0034) and the probability for a jet with a parent quark to fake a muon $(0035)$; the probability for
a jet with a parent gluon to fake an electron or muon is then obtained by dividing the values of these fitted correction factors by four.

The physical mechanism underlying the process whereby an incident photon or neutral pion is misreconstructed as an electron is a conversion in the material serving as the support structure of the silicon vertex detector. This process produces exactly as many $e^{+}$as $e^{-}$, leading to

$$
\begin{align*}
\frac{1}{2} p(\gamma \rightarrow e) & =p\left(\gamma \rightarrow e^{+}\right)=p\left(\gamma \rightarrow e^{-}\right) \\
\frac{1}{2} p\left(\pi^{0} \rightarrow e\right) & =p\left(\pi^{0} \rightarrow e^{+}\right)=p\left(\pi^{0} \rightarrow e^{-}\right) \tag{A9}
\end{align*}
$$

where $e$ is an electron or positron.
From Fig. 11, the average $p_{T}$ of electrons reconstructed from 25 GeV incident photons is $23.9 \pm 1.4 \mathrm{GeV}$. The


FIG. 14 (color online). The probability for a generated parton to be misreconstructed as a one-prong $\tau$, as a function of the parton's generated $p_{T}$. Filled (red) circles show the probability for a jet arising from a parent quark to be misreconstructed as a one-prong tau. Filled (blue) triangles show the probability for a jet arising from a parent gluon to be misreconstructed as a oneprong tau.
average $p_{T}$ of electrons reconstructed from incident 25 GeV neutral pions is $23.7 \pm 1.3 \mathrm{GeV}$.

The charge asymmetry between $p\left(K^{+} \rightarrow e^{+}\right)$and $p\left(K^{-} \rightarrow e^{-}\right)$in Table IV arises because $K^{-}$can capture on a nucleon, producing a single hyperon. Conservation of baryon number and strangeness prevents $K^{+}$from capturing on a nucleon, reducing the $K^{+}$cross section relative to the $K^{-}$cross section by roughly a factor of 2.

The physical process primarily responsible for $\pi^{ \pm} \rightarrow$ $e^{ \pm}$is inelastic charge exchange

$$
\begin{equation*}
\pi^{-} p \rightarrow \pi^{0} n, \quad \pi^{+} n \rightarrow \pi^{0} p \tag{A10}
\end{equation*}
$$

occurring within the electromagnetic calorimeter. The charged pion leaves the "electron's" track in the CDF tracking chamber, and the $\pi^{0}$ produces the "electron's" electromagnetic shower. No true electron appears at all in this process, except as secondaries in the electromagnetic shower originating from the $\pi^{0}$.

The average $p_{T}$ of reconstructed "electrons" originating from a single charged pion is $18.8 \pm 2.2 \mathrm{GeV}$, indicating that the misreconstructed "electron" in this case is measured to have on average only $75 \%$ of the total energy of the parent quark or gluon. This is expected, since the recoiling nucleon from the charge exchange process carries some of the incident pion's momentum.

An additional small loss in energy for a jet misreconstructed as an electron, photon, or muon is expected since the leading $\pi^{+}, K^{+}, \pi^{0}$, or $\gamma$ takes only some fraction of the parent quark's energy.

The cross sections for $\pi^{-} p \rightarrow \pi^{0} n$ and $\pi^{+} n \rightarrow \pi^{0} p$, proceeding through the isospin $I$ conserving and $I_{3}$ independent strong interaction, are roughly equal. The corre-
sponding particles in the two reactions are related by interchanging the signs of their $z$-components of isospin.

The probability for a $25 \mathrm{GeV} \pi^{+}$to decay to a $\mu^{+}$can be written

$$
\begin{align*}
p\left(\pi^{+} \rightarrow\right. & \left.\mu^{+}\right) \\
= & p(\text { decays within tracker }) \\
& +p(\text { decays within calorimeter }) . \tag{A11}
\end{align*}
$$

The probability for the pion to decay within the tracking volume is

$$
\begin{equation*}
p(\text { decays within tracker })=1-e^{-R_{\text {tracker }} / \gamma(c \tau)} \tag{A12}
\end{equation*}
$$

where $\quad \gamma=25 \mathrm{GeV} / 140 \mathrm{MeV}=180$ is the pion's Lorentz boost, the proper decay length of the charged pion is $(c \tau)=7.8$ meters, and the radius of the CDF tracking volume is $R_{\text {tracker }}=1.5$ meters, giving $p($ decays within tracker $)=0.001$. The probability for the pion to decay within the calorimeter volume is

$$
\begin{equation*}
p(\text { decays within calorimeter }) \approx \lambda_{I} / \gamma(c \tau) \tag{A13}
\end{equation*}
$$

where $\lambda_{I} \approx 0.4$ meters is the nuclear interaction length for charged pions on lead or iron and the path length through the calorimeter is $L_{\text {cal }} \approx 2$ meters, leading to $p($ decays within calorimeter $) \approx 0.00025$. Summing the contributions from decay within the tracking volume and decay within the calorimeter volume, $p\left(\pi^{+} \rightarrow \mu^{+}\right) \approx$ 0.00125.

The primary physical mechanism by which a jet fakes a photon is for the parent quark or gluon to fragment into a leading $\pi^{0}$ carrying nearly all the momentum. The highly boosted $\pi^{0}$ decays within the beam pipe to two photons that are sufficiently collinear to appear in the preshower, electromagnetic calorimeter, and shower maximum detector as a single photon. Thus

$$
\begin{equation*}
p(j \rightarrow \gamma)=p\left(q \rightarrow \pi^{0}\right) p\left(\pi^{0} \rightarrow \gamma\right) \tag{A14}
\end{equation*}
$$

An immediate corollary is that the misreconstructed "photon" carries the energy of the parent quark or gluon, and is well measured.

Typical jets are measured with poorer energy resolution than jets that have faked electrons, muons, or photons.

Since $p\left(q \rightarrow \pi^{0}\right) \gg p(q \rightarrow \gamma)$, it follows from Eq. (A4) and Table IV that the conversion contribution to $p(j \rightarrow e)$ is $\approx 75 \%$, and the charge exchange contribution is $\approx 25 \%$ :

$$
\begin{align*}
\frac{0.75}{0.25}= & \left(p(q \rightarrow \gamma) p\left(\gamma \rightarrow e^{+}\right)\right. \\
& \left.+p\left(q \rightarrow \pi^{0}\right) p\left(\pi^{0} \rightarrow e^{+}\right)\right) /\left(p\left(q \rightarrow \pi^{+}\right) p\left(\pi^{+} \rightarrow e^{+}\right)\right. \\
& \left.+p\left(q \rightarrow K^{+}\right) p\left(K^{+} \rightarrow e^{+}\right)\right) . \tag{A15}
\end{align*}
$$

The number of $e^{+} j$ events in data is 0.9 times the number of $e^{-} j$ events. This charge asymmetry arises from $p\left(K^{+} \rightarrow e^{+}\right)$and $p\left(K^{-} \rightarrow e^{-}\right)$in Table IV. Quantitatively,

$$
\begin{equation*}
\frac{p\left(j \rightarrow e^{+}\right)}{p\left(j \rightarrow e^{-}\right)}=\frac{0.9+0.2 p\left(K^{+} \rightarrow e^{+}\right) / p(K \rightarrow e)}{0.9+0.2 p\left(K^{-} \rightarrow e^{-}\right) / p(K \rightarrow e)} \tag{A16}
\end{equation*}
$$

where 0.9 is the sum of 0.75 from Eq. (A15) and $0.15 \approx$ $0.25 \times 0.6$ from Eq. (A6), and 0.2 is twice $1-0.9$. From $p\left(K^{+} \rightarrow e^{+}\right)$and $p\left(K^{-} \rightarrow e^{-}\right)$in Table IV, $p\left(K^{+} \rightarrow\right.$ $\left.e^{+}\right) / p(K \rightarrow e)=1 / 3 \quad$ and $\quad p\left(K^{-} \rightarrow e^{-}\right) / p(K \rightarrow e)=$ $2 / 3$, predicting $p\left(j \rightarrow e^{+}\right) / p\left(j \rightarrow e^{-}\right)=0.935$, in reasonable agreement with the ratio of the observed number of events in the $e^{+} j$ and $e^{-} j$ final states.

The number of $j \mu^{+}$events observed in CDF run II is 1.1 times the number of $j \mu^{-}$events observed. This charge asymmetry arises from $p\left(K^{+} \rightarrow \mu^{+}\right)$and $p\left(K^{-} \rightarrow \mu^{-}\right)$in Table IV.

The physical mechanism by which a prompt photon fakes a tau lepton is for the photon to convert, producing an electron or positron carrying most of the photon's energy, which is then misreconstructed as a tau. The probability for this to occur is equal for positively and negatively charged taus,

$$
\begin{equation*}
\frac{1}{2} p(\gamma \rightarrow \tau)=p\left(\gamma \rightarrow \tau^{+}\right)=p\left(\gamma \rightarrow \tau^{-}\right) \tag{A17}
\end{equation*}
$$

and is related to previously defined quantities by

$$
\begin{equation*}
p(\gamma \rightarrow \tau)=p(\gamma \rightarrow e) \frac{1}{p(e \rightarrow e)} p(e \rightarrow \tau) \tag{A18}
\end{equation*}
$$

where $p(\gamma \rightarrow e)$ denotes the fraction of produced photons that are reconstructed as electrons, $p(e \rightarrow e)$ denotes the fraction of produced electrons that are reconstructed as electrons, and hence $p(\gamma \rightarrow e) / p(e \rightarrow e)$ is the fraction of produced photons that pair produce a single leading electron.

Note $p(e \rightarrow \gamma) \approx p(\gamma \rightarrow e)$ from Table IV, as expected, with a value of $\approx 0.03$ determined by the amount of 5 material in the inner detectors and the tightness of isolation criteria. A hard bremsstrahlung followed by a conversion is responsible for electrons to be reconstructed with opposite sign; hence

$$
\begin{align*}
p\left(e^{ \pm} \rightarrow e^{\mp}\right) & =p\left(e^{+} \rightarrow e^{-}\right) \\
& =p\left(e^{-} \rightarrow e^{+}\right) \\
& \approx \frac{1}{2} p\left(e^{ \pm} \rightarrow \gamma\right) p\left(\gamma \rightarrow e^{\mp}\right) \tag{A19}
\end{align*}
$$

where the factor of $1 / 2$ comes because the material already traversed by the $e^{ \pm}$will not be traversed again by the $\gamma$. In particular, track curvature mismeasurement is not responsible for erroneous sign determination in the central region of the CDF detector.

From knowledge of the underlying physical mechanisms by which jets fake electrons, muons, taus, and photons, the simple use of a reconstructed jet as a lepton or photon with an appropriate fake rate applied to the weight of the event needs slight modification to correctly handle the fact that a jet that has faked a lepton or photon generally is measured
more accurately than a hadronic jet. Rather than using the momentum of the reconstructed jet, the momentum of the parent quark or gluon is determined by adding up all Monte Carlo particle level objects within a cone of $\Delta R=$ 0.4 about the reconstructed jet. In misreconstructing a jet in an event, the momentum of the corresponding parent quark or gluon is used rather than the momentum of the reconstructed jet. A jet that fakes a photon then has momentum equal to the momentum of the parent quark or gluon plus a fractional correction equal to $0.01 \times\left(\right.$ parent $p_{T}-$ $25 \mathrm{GeV}) /(25 \mathrm{GeV})$ to account for leakage out of the cone of $\Delta R=0.4$, and a further smearing of $0.2 \sqrt{\mathrm{GeV}} \times$ $\sqrt{\text { parent } p_{T}}$, reflecting the electromagnetic resolution of the CDF detector. The momenta of jets that fake photons are multiplied by an overall factor of 1.12 , and jets that fake electrons, muons, or taus are multiplied by an overall factor of 0.95 . These numbers are determined by the $\ell \not p, \ell j$, and $\gamma j$ final states. The distributions most sensitive to these numbers are the missing energy and the jet $p_{T}$.

A $b$ quark fragmenting into a leading $b$ hadron that then decays leptonically or semileptonically results in an electron or muon that shares the $p_{T}$ of the parent $b$ quark with the associated neutrino. If all hadronic decay products are soft, the distribution of the momentum fraction carried by the charged lepton can be obtained by considering the decay of a scalar to two massless fermions. Isolated and energetic electrons and muons arising from parent $b$ quarks in this way are modeled as having $p_{T}$ equal to the parent $b$ quark $p_{T}$, multiplied by a random number uniformly distributed between 0 and 1 .

## 2. Additional background sources

This appendix provides additional details on the estimation of the standard model prediction.

## a. Cosmic ray and beam halo muons

There are four dominant categories of events caused by cosmic ray muons penetrating the detector: $\mu \not p, \mu^{+} \mu^{-}$, $\gamma \not p$, and $j \not p$. There is negligible contribution from cosmic ray secondaries of any particle type other than muons.

A cosmic ray muon penetrating the CDF detector whose trajectory passes within 1 mm of the beam line and within $-60<z<60 \mathrm{~cm}$ of the origin may be reconstructed as two outgoing muons. In this case the cosmic ray event is partitioned into the final state $\mu^{+} \mu^{-}$. If one of the tracks is missed, the cosmic ray event is partitioned into the final state $\mu \not p$. The standard CDF cosmic ray filter, which makes use of drift time information in the central tracking chamber, is used to reduce these two categories of cosmic ray events.

CDF data events with exactly one track (corresponding to one muon) and events with exactly two tracks (corresponding to two muons) are used to estimate the cosmic ray muon contribution to the final states $\mu \not p$ and $\mu^{+} \mu^{-}$ after the cosmic ray filter. This sample of events is used as
the standard model background process cosmic $\mu$. The cosmic $\mu$ sample does not contribute to the events passing the analysis offline trigger, whose cleanup cuts require the presence of three or more tracks. Roughly 100 events are expected from cosmic ray muons in the categories $\mu^{+} \not p$ and $\mu^{+} \mu^{-}$. The sample cosmic $\mu$ is neglected from the background estimate, since there is no discrepancy that demands its inclusion.

The remaining two categories are $\gamma \not p$ and $j \not p$, resulting from a cosmic ray muon that penetrates the CDF electromagnetic or hadronic calorimeter and undergoes a hard bremsstrahlung in one calorimeter cell. Such an interaction can mimic a single photon or a single jet, respectively. The reconstruction algorithm infers the presence of significant missing energy balancing the "photon" or "jet." If this cosmic ray interaction occurs during a bunch crossing in which there is a $p \bar{p}$ interaction producing three or more tracks, the event will be partitioned into the final state $\gamma p$ or $j \not p$.

CDF data events with fewer than three tracks are used to estimate the cosmic ray muon contribution to the final states $\gamma \not p$ and $j \not p$. These samples of events are used as standard model background processes cosmic $\gamma$ and cosmic $j$ for the modeling of this background, corresponding to offline triggers requiring a photon with $p_{T}>$ 60 GeV , or a jet with $p_{T}>40 \mathrm{GeV}$ (prescaled) or $p_{T}>$ 200 GeV (unprescaled), respectively. These samples do not contribute to the events passing the analysis offline trigger, whose cleanup cuts require three or more tracks. The contribution of these events is adjusted with correction factors that are listed as cosmic $\gamma$ and cosmic $j$ " $k$-factors" in Table I, but which are more properly understood as reflecting the number of bunch crossings with zero $p \bar{p}$ interactions (resulting in zero reconstructed tracks) relative to the number of bunch crossings with one or more interactions (resulting in three or more reconstructed tracks). Since the number of bunch crossings with no inelastic $p \bar{p}$ interactions is used to determine the CDF instantaneous luminosity, these cosmic correction factors can be viewed as containing direct information about the luminosity-averaged instantaneous luminosity.

The cosmic ray muon contribution to the final states $\gamma \not p$ and $j \not p$ is uniform as a function of the CDF azimuthal angle $\phi$. Consider the CDF detector to be a thick cylindrical shell, and consider two arbitrary infinitesimal volume elements at different locations in the material of the shell. Since the two volume elements have similar overburdens, the number of cosmic ray muons with $E \gtrsim 20 \mathrm{GeV}$ penetrating the first volume element is very nearly the same as the number of cosmic ray muons with $E \gtrsim 20 \mathrm{GeV}$ penetrating the second volume element. Since the material of the CDF calorimeters is uniform as a function of CDF azimuthal angle $\phi$, it follows that the cosmic ray muon contribution to the final states $\gamma \not p$ and $j \not p$ should also be uniform as a function of $\phi$. In particular, it is noted that the
$\phi$ dependence of this contribution depends solely on the material distribution of the CDF calorimeter, which is uniform in $\phi$, and has no dependence on the distribution of the horizon angle of the muons from cosmic rays streaking through the atmosphere.

The final states $\gamma \not p$ and $j \not p$ are also populated by beam halo muons, traveling horizontally through the CDF detector in time with a bunch. A beam halo muon can undergo a hard bremsstrahlung in the electromagnetic or hadronic calorimeters, producing an energy deposit that can be reconstructed as a photon or jet, respectively. These beam halo muons tend to lie in the plane and outside of the Tevatron ring, thus horizontally penetrating the CDF detector along $\hat{z}$ at $y=0, x>0$, and hence $\phi=0$.

Figure 15 shows the $\gamma \not p$ and $j \not p$ final states, in which events come primarily from cosmic ray and beam halo muons.

## b. Multiple interactions

In order to estimate event overlaps, consider an interesting event observed in final state C , which looks like an overlap of two events in the final states $A$ and $B$. An example is $C=e+e-4 j, A=e+e-$, and $B=4 j$. It is desired to estimate how many C events are expected from the overlap of A and B events, given the observed frequencies of A and B .

Let $\mathcal{L}(t)$ be the instantaneous luminosity as a function of time $t$; let

$$
\begin{equation*}
L=\int_{\text {RunII }} \mathcal{L}(t) d t=927 \mathrm{pb}^{-1} \tag{A20}
\end{equation*}
$$

denote the total integrated luminosity; and let

$$
\begin{equation*}
\overline{\mathcal{L}}=\frac{\int_{\text {RunII }} \mathcal{L}(t) \mathcal{L}(t) d t}{\int_{\text {RunII }} \mathcal{L}(t) d t} \approx 10^{32} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \tag{A21}
\end{equation*}
$$

be the luminosity-averaged instantaneous luminosity. Denote by $t_{0}$ the time interval of 396 ns between successive bunch crossings. The total number of effective bunch crossings $X$ is then

$$
\begin{equation*}
X=\frac{L}{\overline{\mathcal{L}} t_{0}} \approx 2.3 \times 10^{13} \tag{22}
\end{equation*}
$$

Letting $A$ and $B$ denote the number of observed events in final states A and B, it follows that the number of events in the final state C expected from overlap of A and B is

$$
\begin{equation*}
C=\frac{A B}{X} \tag{A23}
\end{equation*}
$$

Overlap events are included in the VISTA background estimate, although their contribution is generally negligible.

## c. Intrinsic $\boldsymbol{k}_{\boldsymbol{T}}$

Significant discrepancy is observed in many final states containing two objects $\circ 1$ and $\circ 2$ in the variables


FIG. 15 (color online). The distribution of transverse momentum and azimuthal angle for photons and jets in the $\gamma \not p$ and $j \not p$ final states, dominated by cosmic ray and beam halo muons. The vertical axis shows the number of events in each bin. Data are shown as filled (black) circles; the standard model prediction is shown as the shaded (red) histogram. Here the "standard model" prediction includes contributions from cosmic ray and beam halo muons, estimated using events containing fewer than three reconstructed tracks. The contribution from cosmic ray muons is flat in $\phi$, while the contribution from beam halo is localized to $\phi=0$. The only degrees of freedom for the background to these final states are the cosmic $\gamma$ and cosmic $j$ correction factors, whose values are determined from the global VISTA fit and provided in Table I.
$\Delta \phi(\circ 1, \circ 2)$, uncl $p_{T}$, and $\phi_{T}$. These discrepancies are ascribed to the sum of two effects: (1) an intrinsic Fermi motion of the colliding partons within the proton and antiproton, and (2) soft radiation along the beam axis. The sum of these two effects appears to be larger in nature than predicted by PYTHIA with the parameter tunes used for the generation of the samples employed in this analysis. This discrepancy is well known from previous studies at the Tevatron and elsewhere and affects this analysis similarly to other Tevatron analyses.

The $W$ and $Z$ electroweak samples used in this analysis have been generated with an adjusted PYTHIA parameter that increases the intrinsic $k_{T}$. For all other generated standard model events, the net effect of the Fermi motion
of the colliding partons and the soft nonperturbative radiation is hypothesized to be described by an overall "effective intrinsic $k_{T}$," and the center of mass of each event is given a transverse kick. Specifically, for every event of invariant mass $m$ and generated summed transverse momentum $\sum p_{T}$, a random number $k_{T}$ is pulled from the probability distribution

$$
\begin{align*}
p\left(k_{T}\right) \propto & \left(k_{T}<m / 5\right)\left[\frac{4}{5} g\left(k_{T} ; \mu=0, \sigma_{1}\right)\right. \\
& \left.+\frac{1}{5} g\left(k_{T} ; \mu=0, \sigma_{2}\right)\right], \tag{A24}
\end{align*}
$$

where ( $k_{T}<m / 5$ ) evaluates to unity if true and zero if false; $g\left(k_{T} ; \mu, \sigma\right)$ is a Gaussian function of $k_{T}$ with center at $\mu$ and width $\sigma ; \sigma_{1}=2.55 \mathrm{GeV}+0.0085 \sum p_{T}$ is the
width of the core of the double Gaussian; and $\sigma_{2}=$ $5.25 \mathrm{GeV}+0.0175 \sum p_{T}$ is the width of the second, wider Gaussian. The event is then boosted to an inertial frame traveling with speed $|\vec{\beta}|=k_{T} / m$ with respect to the lab frame, in a direction transverse to the beam axis, where $m$ is the invariant mass of all reconstructed objects in the event, along an azimuthal angle pulled randomly from a uniform distribution between 0 and $2 \pi$. The momenta of identified objects are recalculated in the lab frame. Sixty percent of the recoil kick is assigned to unclustered momentum in the event. The remaining $40 \%$ of the recoil kick is assumed to disappear down the beam pipe, and contributes to the missing transverse momentum in the event. This picture, and the particular parameter values that accompany this story, are determined primarily by the uncl $p_{T}$ and $\not p_{T}$ distributions in highly populated two-object final states, including the low- $p_{T} 2 j$ final state, the high $-p_{T} 2 j$ final state, and the final states $j \gamma, e^{+} e^{-}$, and $\mu^{+} \mu^{-}$.

Under the hypothesis described, reasonable although imperfect agreement with observation is obtained. The result of this analysis supports the conclusions of previous studies indicating that the effective intrinsic $k_{T}$ needed to match observation is quite large relative to naive expectation. That the data appear to require such a large effective intrinsic $k_{T}$ may be pointing out the need for some basic improvement to our understanding of this physics.

## 3. Global fit

This section describes the construction of the global $\chi^{2}$ used in the VISTA global fit.

$$
\text { a. } \chi_{k}^{2}
$$

The bins in the CDF high- $p_{T}$ data sample are labeled by the index $k=\left(k_{1}, k_{2}\right)$, where each value of $k_{1}$ represents a phrase such as "this bin contains events with three objects: one with $17<p_{T}<25 \mathrm{GeV}$ and $|\eta|<0.6$, one with $40<$ $p_{T}<60 \mathrm{GeV}$ and $0.6<|\eta|<1.0$, and one with $25<$ $p_{T}<40 \mathrm{GeV}$ and $1.0<|\eta|, "$ and each value of $k_{2}$ represents a phrase such as "this bin contains events with three objects: an electron, muon, and jet, respectively." The reason for splitting $k$ into $k_{1}$ and $k_{2}$ is that a jet can fake an electron (mixing the contents of $k_{2}$ ), but an object with $|\eta|<0.6$ cannot fake an object with $0.6<|\eta|<1.0$ (no mixing of $k_{1}$ ). The term corresponding to the $k$ th bin takes the form of Eq. (1), where Data $[k]$ is the number of data events observed in the $k$ th bin, $\operatorname{SM}[k]$ is the number of events predicted by the standard model in the $k$ th bin, $\delta \mathrm{SM}[k]$ is the Monte Carlo statistical uncertainty on the standard model prediction in the $k$ th bin, and $\sqrt{\operatorname{SM}[k]}$ is the statistical uncertainty on the prediction in the $k$ th bin. To legitimize the use of Gaussian errors, only bins containing eight or more data events are considered. The standard model prediction $\mathrm{SM}[k]$ for the $k$ th bin can be written in terms of the introduced correction factors as

$$
\begin{align*}
\mathrm{SM}[k]= & \mathrm{SM}\left[\left(k_{1}, k_{2}\right)\right] \\
= & \sum_{k_{2}^{\prime} \in \text { object lists }} \sum_{l \in \text { processes }}\left(\int \mathcal{L} d t\right) \\
& \cdot(\operatorname{kFactor}[l]) \cdot\left(\mathrm{SM}_{0}\left[\left(k_{1}, k_{2}^{\prime}\right)\right][l]\right) \\
& \cdot\left(p\left[\left(k_{1}, k_{2}^{\prime}\right)\right]\left[k_{2}\right]\right) \cdot\left(t\left[\left(k_{1}, k_{2}\right)\right]\right), \tag{A25}
\end{align*}
$$

where $\operatorname{SM}[k]$ is the standard model prediction for the $k$ th bin; the index $k$ is the Cartesian product of the two indices $k_{1}$ and $k_{2}$ introduced above, labeling the regions of the detector in which there are energy clusters and the identified objects corresponding to those clusters, respectively; the index $k_{2}^{\prime}$ is a dummy summation index; the index $l$ labels standard model background processes, such as dijet production or $W+1$ jet production; $\operatorname{SM}_{0}\left[\left(k_{1}, k_{2}^{\prime}\right)\right][l]$ is the initial number of standard model events predicted in bin $\left(k_{1}, k_{2}^{\prime}\right)$ from the process labeled by the index $l$; $p\left[\left(k_{1}, k_{2}^{\prime}\right)\right]\left[k_{2}\right]$ is the probability that an event produced with energy clusters in the detector regions labeled by $k_{1}$ that are identified as objects labeled by $k_{2}^{\prime}$ would be mistaken as having objects labeled by $k_{2}$; and $t\left[\left(k_{1}, k_{2}\right)\right]$ represents the probability that an event produced with energy clusters in the detector regions labeled by $k_{1}$ that are identified as objects labeled by $k_{2}$ would pass the trigger.

The quantity $\mathrm{SM}_{0}\left[\left(k_{1}, k_{2}^{\prime}\right)\right][l]$ is obtained by generating some number $n_{l}$ (say $10^{4}$ ) of Monte Carlo events corresponding to the process $l$. The event generator provides a cross section $\sigma_{l}$ for this process $l$. The weight of each of these Monte Carlo events is equal to $\sigma_{l} / n_{l}$. Passing these events through the CDF simulation and reconstruction, the sum of the weights of these events falling into the bin $\left(k_{1}, k_{2}^{\prime}\right)$ is $\mathrm{SM}_{0}\left[\left(k_{1}, k_{2}^{\prime}\right)\right][l]$.

$$
\text { b. } \chi_{\text {constraints }}^{2}
$$

The term $\chi_{\text {constraints }}^{2}(\vec{s})$ in Eq. (2) reflects constraints on the values of the correction factors determined by data other than those in the global high- $p_{T}$ sample. These constraints include $k$-factors taken from theoretical calculations and numbers from the CDF literature when use is made of CDF data external to the VISTA high- $p_{T}$ sample. The constraints imposed are
(i) The luminosity $(0001)$ is constrained to be within $6 \%$ of the value measured by the CDF Čerenkov luminosity counters.
(ii) The fake rate $p(q \rightarrow \gamma)$ (0039) is constrained to be $2.6 \times 10^{-4} \pm 1.5 \times 10^{-5}$, from the single particle gun study of Appendix A 1 .
(iii) The fake rate $p(e \rightarrow \gamma)$ (0032) plus the efficiency $p(e \rightarrow e)(0026)$ for electrons in the plug is constrained to be within $1 \%$ of unity.
(iv) Noting $p(q \rightarrow \gamma)$ corresponds to correction factor 0039, $p\left(q \rightarrow \pi^{ \pm}\right)=2 p\left(q \rightarrow \pi^{0}\right)$, and $p\left(q \rightarrow \pi^{0}\right)=p(q \rightarrow \gamma) / p\left(\pi^{0} \rightarrow \gamma\right)$, and taking $p\left(\pi^{0} \rightarrow \gamma\right)=0.6$ and $p\left(\pi^{ \pm} \rightarrow \tau\right)=0.415$ from the single particle gun study of Appendix A 1, the
fake rate $p(q \rightarrow \tau)$ (0038) is constrained to $p(q \rightarrow \tau)=p\left(q \rightarrow \pi^{ \pm}\right) p\left(\pi^{ \pm} \rightarrow \tau\right) \pm 10 \%$.
(v) The $k$-factors for dijet production (0018 and $0019)$ are constrained to $1.10 \pm 0.05$ and $1.33 \pm$ 0.05 in the kinematic regions $\hat{p}_{T}<150 \mathrm{GeV}$ and $\hat{p}_{T}>150 \mathrm{GeV}$, respectively, where $\hat{p}_{T}$ is the transverse momentum of the scattered partons in the $2 \rightarrow 2$ process in the colliding parton center of momentum frame.
(vi) The inclusive $k$-factor for $\gamma+N$ jets ( $0004-$ 0007 ) is constrained to $1.25 \pm 0.15[49,50]$.
(vii) The inclusive $k$-factor for $\gamma \gamma+N$ jets (00080010 ) is constrained to $2.0 \pm 0.15$ [51].
(viii) The inclusive $k$-factors for $W$ and $Z$ production (0011-0014 and 0015-0017) are subject to a 2-dimensional Gaussian constraint, with mean at the NNLO/LO theoretical values [52], and a covariance matrix that encapsulates the highly correlated theoretical uncertainties, as discussed in Appendix A 4.
(ix) Trigger efficiency correction factors are constrained to be less than unity.
(x) All correction factors are constrained to be positive.

## c. Covariance matrix

This section describes the correction factor covariance matrix $\Sigma$. The inverse of the covariance matrix is obtained from

$$
\begin{equation*}
\Sigma_{i j}^{-1}=\left.\frac{1}{2} \frac{\partial^{2} \chi^{2}(\vec{s})}{\partial s_{i} \partial s_{j}}\right|_{\vec{s}_{0}} \tag{A26}
\end{equation*}
$$

where $\chi^{2}(\vec{s})$ is defined by Eq. (2) as a function of the correction factor vector $\vec{s}$, vector elements $s_{i}$ and $s_{j}$ are the $i$ th and $j$ th correction factors, and $\vec{s}_{0}$ is the vector of correction factors that minimizes $\chi^{2}(\vec{s})$. Numerical estimation of the right-hand side of Eq. (A26) is achieved by calculating $\chi^{2}$ at $\vec{s}_{0}$ and at positions slightly displaced from $\vec{s}_{0}$ in the direction of the $i$ th and $j$ th correction factors, denoted by the unit vectors $\hat{i}$ and $\hat{j}$. Approximating the second partial derivative

$$
\begin{aligned}
\left.\frac{\partial^{2} \chi^{2}}{\partial s_{j} \partial s_{i}}\right|_{\vec{s}_{0}}= & \frac{\chi^{2}\left(\vec{s}_{0}+\hat{i} \delta s_{i}+\hat{j} \delta s_{j}\right)-\chi^{2}\left(\vec{s}_{0}+\hat{j} \delta s_{j}\right)}{\delta s_{j} \delta s_{i}} \\
& -\frac{\chi^{2}\left(\vec{s}_{0}+\hat{i} \delta s_{i}\right)-\chi^{2}\left(\vec{s}_{0}\right)}{\delta s_{j} \delta s_{i}}
\end{aligned}
$$

leads to

$$
\begin{align*}
\Sigma_{i j}^{-1}= & {\left[\chi^{2}\left(\vec{s}_{0}+\delta s_{i} \hat{i}+\delta s_{j} \hat{j}\right)-\chi^{2}\left(\vec{s}_{0}+\delta s_{i} \hat{i}\right)\right.} \\
& \left.-\chi^{2}\left(\vec{s}_{0}+\delta s_{j} \hat{j}\right)+\chi^{2}\left(\vec{s}_{0}\right)\right] /\left(2 \delta s_{i} \delta s_{j}\right) \tag{A27}
\end{align*}
$$

for appropriately small steps $\delta s_{i}$ and $\delta s_{j}$ away from the minimum. The covariance matrix $\Sigma$ is calculated by inverting $\Sigma^{-1}$. The diagonal element $\Sigma_{i i}$ is the variance $\sigma_{i}^{2}$ of the $i$ th correction factor, and the correlation $\rho_{i j}$ between
the $i$ th and $j$ th correction factors is $\rho_{i j}=\Sigma_{i j} / \sigma_{i} \sigma_{j}$. The variances of each correction factor, corresponding to the diagonal elements of the covariance matrix, are shown in Table I. The correlation matrix obtained is shown in Table V.

## 4. Correction factor values

This section provides notes on the values of the VISTA correction factors obtained from a global fit of standard model prediction to data. The correction factors considered are numbers that can in principle be calculated a priori, but whose calculation is in practice not feasible. These correction factors divide naturally into two classes, the first of which reflects the difficulty of calculating the standard model prediction to all orders, and the second of which reflects the difficulty of understanding from first principles the response of the experimental apparatus.

The theoretical correction factors considered are of two types. The difficulty of calculating the standard model prediction for many processes to all orders in perturbation theory is handled through the introduction of $k$-factors, representing the ratio of the true all orders prediction to the prediction at lowest order in perturbation theory. Uncertainties in the distribution of partons inside the colliding proton and antiproton as a function of parton momentum are in principle handled through the introduction of correction factors associated with parton distribution functions, but there are currently no discrepancies to motivate this.

Experimental correction factors correspond to numbers describing the response of the CDF detector that are precisely calculable in principle, but that are in practice best constrained by the high- $p_{T}$ data themselves. These correction factors take the form of the integrated luminosity, object identification efficiencies, object misidentification probabilities, trigger efficiencies, and energy scales.

## a. $k$-factors

For nearly all standard model processes, $k$-factors are used as an overall multiplicative constant, rather than being considered to be a function of one or more kinematic variables. The spirit of the approach is to introduce as few correction factors as possible, and to only introduce correction factors motivated by specific discrepancies.

0001 .-The integrated luminosity of the analysis sample has a close relationship with the theoretically determined values of inclusive $W$ and $Z$ production at the Tevatron. Figure 16 shows the variation in calculated inclusive $W$ and $Z k$-factors under changes in the assumed parton distribution functions. Each point represents a different $W$ and $Z$ inclusive cross section determined using modified parton distribution functions. The use of 16 bases to reflect systematic uncertainties results in 32 black dots in Fig. 16. The uncertainties in the $W$ and $Z$ cross sections due to variations in the renormalization and factorization scales

TABLE V．Correction factor correlation matrix．The top row and left column show correction factor codes．Each element of the matrix shows the correlation between the correction factors corresponding to the column and row．Each matrix element is dimensionless；the elements along the diagonal are unity；the matrix is symmetric；positive elements indicate positive correlation，and negative elements anticorrelation．

|  | 0001 | 0002 | 0003 | 0004 | 0005 | 0006 | 0007 | 0008 | 0009 | 0010 | 0011 | 0012 | 0013 | 0014 | 0015 | 0016 | 0017 | 0018 | 0019 | 0020 | 0021 | 0022 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0001 | 1 | －． 32 | －． 7 | $-.56$ | $-.53$ | －． 45 | －． 26 | －． 36 | －． 21 | －． 14 | －． 87 | －． 77 | $-.51$ | －． 28 | －． 82 | $-.55$ | $-.31$ | －． 95 | －． 96 | －． 94 | －． 94 | $-.88$ |
| 0002 | －． 32 | 1 | ＋． 21 | ＋． 37 | ＋． 38 | ＋． 33 | ＋． 2 | ＋． 34 | ＋． 18 | ＋． 12 | ＋． 28 | ＋． 25 | ＋． 17 | ＋． 09 | ＋． 27 | ＋． 18 | ＋． 1 | ＋． 3 | ＋． 31 | ＋． 31 | ＋． 3 | ＋． 28 |
| 0003 | －． 7 | ＋． 21 | 1 | ＋． 39 | $+.37$ | ＋． 31 | ＋． 18 | ＋． 25 | $+.14$ | ＋． 1 | ＋． 61 | $+.53$ | ＋． 35 | ＋． 2 | $+.57$ | ＋． 38 | $+.21$ | ＋． 66 | $+.66$ | ＋． 66 | ＋． 65 | ＋． 61 |
| 0004 | －． 56 | ＋． 37 | ＋． 39 | 1 | ＋． 9 | $+.77$ | ＋． 48 | ＋． 61 | $+.33$ | ＋． 23 | ＋． 49 | ＋． 43 | ＋． 29 | ＋． 16 | ＋． 46 | ＋． 32 | ＋． 18 | ＋． 5 | $+.53$ | ＋． 53 | ＋． 52 | ＋． 49 |
| 0005 | －． 53 | ＋． 38 | ＋． 37 | ＋． 9 | 1 | ＋． 75 | ＋． 46 | ＋． 62 | ＋． 31 | ＋． 21 | ＋． 46 | ＋． 41 | ＋． 27 | ＋． 15 | ＋． 44 | ＋． 3 | $+.17$ | ＋． 5 | $+.51$ | ＋． 48 | ＋． 5 | ＋． 47 |
| 0006 | －． 45 | ＋． 33 | ＋． 31 | $+.77$ | ＋． 75 | 1 | ＋． 4 | ＋． 54 | ＋． 29 | ＋． 13 | ＋． 4 | $+.35$ | ＋． 24 | ＋． 13 | ＋． 38 | ＋． 26 | ＋． 14 | ＋． 43 | $+.44$ | ＋． 42 | ＋． 42 | ＋． 35 |
| 0007 | －． 26 | ＋． 2 | ＋． 18 | ＋． 48 | ＋． 46 | ＋． 4 | 1 | ＋． 34 | ＋． 18 | ＋． 09 | $+.23$ | ＋． 2 | ＋． 13 | ＋． 08 | ＋． 22 | ＋． 15 | ＋． 08 | ＋． 24 | $+.25$ | ＋． 25 | ＋． 24 | ＋． 21 |
| 0008 | －． 36 | ＋． 34 | ＋． 25 | ＋． 61 | ＋． 62 | $+.54$ | ＋． 34 | 1 | ＋． 37 | ＋． 28 | ＋． 32 | ＋． 28 | ＋． 19 | ＋． 1 | ＋． 3 | ＋． 22 | ＋． 12 | ＋． 34 | ＋． 34 | ＋． 34 | ＋． 33 | ＋．31 |
| 0009 | －． 21 | ＋． 18 | ＋． 14 | $+.33$ | ＋． 31 | ＋． 29 | ＋． 18 | ＋． 37 | 1 | ＋． 06 | ＋． 19 | ＋． 17 | ＋． 11 | ＋． 06 | ＋． 2 | ＋． 06 | ＋． 11 | ＋． 2 | ＋． 2 | ＋． 19 | ＋． 19 | ＋． 18 |
| 0010 | －． 14 | ＋． 12 | ＋． 1 | ＋． 23 | ＋． 21 | ＋． 13 | ＋． 09 | ＋． 28 | ＋． 06 | 1 | ＋． 13 | ＋． 11 | ＋． 08 | ＋． 06 | ＋． 13 | ＋． 11 | －． 03 | ＋． 13 | ＋． 14 | ＋． 13 | ＋． 13 | ＋． 12 |
| 0011 | －． 87 | ＋． 28 | ＋． 61 | ＋． 49 | ＋． 46 | ＋． 4 | ＋． 23 | ＋． 32 | ＋． 19 | ＋． 13 | 1 | ＋． 85 | $+.58$ | ＋． 32 | ＋． 89 | ＋． 61 | ＋． 33 | ＋． 83 | $+.84$ | ＋． 82 | ＋． 82 | ＋． 76 |
| 0012 | －． 77 | ＋． 25 | ＋． 53 | ＋． 43 | ＋． 41 | ＋． 35 | ＋． 2 | ＋． 28 | $+.17$ | ＋． 11 | ＋． 85 | 1 | ＋． 33 | ＋． 35 | ＋． 79 | ＋． 49 | ＋． 33 | ＋． 72 | $+.74$ | ＋． 74 | ＋． 72 | ＋． 68 |
| 0013 | －． 51 | ＋． 17 | ＋． 35 | ＋． 29 | ＋． 27 | ＋． 24 | ＋． 13 | ＋． 19 | ＋． 11 | ＋． 08 | $+.58$ | ＋． 33 | 1 | －． 21 | ＋． 52 | ＋． 35 | ＋． 15 | ＋． 5 | ＋． 49 | ＋． 46 | ＋． 48 | ＋． 46 |
| 0014 | －． 28 | ＋． 09 | ＋． 2 | ＋． 16 | ＋． 15 | ＋． 13 | ＋． 08 | ＋． 1 | ＋． 06 | ＋． 06 | ＋． 32 | ＋． 35 | －． 21 | 1 | ＋． 29 | ＋． 26 | －． 04 | ＋． 28 | ＋． 27 | ＋． 28 | ＋． 26 | ＋． 21 |
| 0015 | －． 82 | ＋． 27 | $+.57$ | ＋． 46 | $+.44$ | ＋． 38 | ＋． 22 | ＋． 3 | ＋． 2 | ＋． 13 | ＋． 89 | ＋． 79 | $+.52$ | ＋． 29 | 1 | ＋． 58 | ＋． 35 | ＋． 77 | $+.78$ | ＋． 77 | ＋． 76 | ＋． 71 |
| 0016 | －． 55 | ＋． 18 | ＋． 38 | ＋． 32 | ＋． 3 | ＋． 26 | ＋． 15 | ＋． 22 | ＋． 06 | ＋． 11 | ＋． 61 | ＋． 49 | ＋． 35 | ＋． 26 | ＋． 58 | 1 | －． 09 | ＋． 52 | $+.53$ | ＋． 52 | ＋． 52 | ＋． 49 |
| 0017 | －． 31 | ＋． 1 | ＋． 21 | ＋． 18 | ＋． 17 | ＋． 14 | ＋． 08 | ＋． 12 | ＋． 11 | －． 03 | ＋． 33 | ＋． 33 | ＋． 15 | －． 04 | ＋． 35 | －． 09 | 1 | ＋． 3 | ＋． 3 | ＋． 29 | ＋． 29 | $+.25$ |
| 0018 | －． 95 | ＋． 3 | ＋． 66 | ＋． 5 | $+.5$ | $+.43$ | ＋． 24 | ＋． 34 | ＋． 2 | ＋． 13 | ＋．83 | ＋． 72 | ＋． 5 | ＋． 28 | ＋． 77 | ＋． 52 | ＋． 3 | 1 | ＋．91 | ＋． 92 | ＋． 89 | ＋．85 |
| 0019 | －． 96 | ＋． 31 | ＋． 66 | $+.53$ | $+.51$ | ＋． 44 | ＋． 25 | ＋． 34 | ＋． 2 | ＋． 14 | ＋．84 | ＋． 74 | ＋． 49 | ＋． 27 | ＋． 78 | $+.53$ | ＋． 3 | ＋． 91 | 1 | ＋． 91 | ＋． 91 | ＋．84 |
| 0020 | －． 94 | $+.31$ | ＋． 66 | $+.53$ | ＋． 48 | $+.42$ | ＋． 25 | ＋． 34 | ＋． 19 | ＋． 13 | ＋． 82 | $+.74$ | ＋． 46 | ＋． 28 | ＋． 77 | $+.52$ | ＋． 29 | ＋． 92 | ＋．91 | 1 | ＋． 87 | ＋．84 |
| 0021 | －． 94 | ＋． 3 | ＋． 65 | $+.52$ | ＋． 5 | ＋． 42 | ＋． 24 | ＋． 33 | ＋． 19 | ＋． 13 | ＋．82 | ＋． 72 | ＋． 48 | ＋． 26 | ＋． 76 | ＋． 52 | ＋． 29 | ＋． 89 | ＋． 91 | $+.87$ | 1 | ＋．82 |
| 0022 | －． 88 | ＋． 28 | ＋． 61 | ＋． 49 | ＋． 47 | ＋． 35 | ＋． 21 | ＋． 31 | ＋． 18 | ＋． 12 | ＋． 76 | ＋． 68 | ＋． 46 | ＋． 21 | ＋． 71 | ＋． 49 | ＋． 25 | ＋．85 | ＋．84 | ＋． 84 | ＋．82 | 1 |
| 0023 | －． 88 | ＋． 28 | ＋． 61 | ＋． 49 | ＋． 46 | ＋． 4 | ＋． 22 | ＋． 31 | ＋． 18 | ＋． 12 | ＋． 77 | ＋． 67 | $+.45$ | ＋． 26 | $+.71$ | ＋． 48 | ＋． 28 | ＋． 83 | ＋．85 | $+.83$ | ＋． 83 | ＋． 73 |
| 0024 | －． 62 | ＋． 2 | ＋． 43 | ＋． 35 | ＋． 33 | ＋． 28 | ＋． 02 | ＋． 22 | ＋． 13 | ＋． 09 | $+.54$ | ＋． 47 | ＋． 36 | ＋． 09 | ＋． 5 | ＋． 35 | ＋． 16 | ＋． 6 | ＋． 59 | ＋． 6 | $+.57$ | ＋． 55 |
| 0025 | －． 54 | ＋． 18 | ＋． 38 | ＋． 3 | ＋． 29 | ＋． 25 | ＋． 14 | ＋． 18 | ＋． 08 | ＋． 05 | ＋． 25 | ＋． 21 | ＋． 15 | ＋． 08 | ＋． 09 | ＋． 1 | ＋． 03 | $+.51$ | ＋． 52 | $+.51$ | $+.51$ | ＋． 47 |
| 0026 | －． 17 | ＋． 06 | ＋． 12 | ＋． 1 | ＋． 1 | ＋． 09 | ＋． 05 | ＋． 06 | $+.03$ | －． 01 | ＋． 09 | ＋． 08 | ＋． 06 | $+.03$ | ＋． 04 | ＋． 03 | －． 02 | ＋． 16 | ＋． 16 | ＋． 16 | ＋． 16 | ＋． 15 |
| 0027 | －． 46 | ＋． 15 | ＋． 32 | $+.25$ | $+.24$ | ＋． 2 | ＋． 12 | ＋． 16 | ＋． 07 | ＋． 05 | ＋． 16 | ＋． 15 | ＋． 1 | $+.05$ | ＋． 06 | ＋． 08 | ＋． 04 | ＋． 43 | $+.44$ | $+.43$ | ＋． 43 | ＋． 4 |
| 0028 | －． 37 | ＋． 12 | ＋． 26 | ＋． 2 | ＋． 19 | ＋． 16 | ＋． 09 | ＋． 12 | ＋． 06 | ＋． 04 | ＋． 15 | ＋． 13 | ＋． 09 | $+.05$ | ＋． 05 | ＋． 07 | ＋． 04 | ＋． 35 | ＋． 36 | ＋． 35 | ＋． 35 | ＋． 33 |
| 0029 | －． 09 | $-.31$ | ＋． 06 | －． 46 | －． 49 | $-.45$ | －． 29 | －． 61 | －． 31 | －． 19 | ＋． 07 | ＋． 06 | ＋． 04 | ＋． 02 | ＋． 05 | ＋． 03 | ＋． 02 | ＋． 09 | ＋． 09 | ＋． 08 | ＋． 08 | ＋． 08 |
| 0030 | －． 1 | ＋． 02 | ＋． 07 | ＋． 03 | ＋． 03 | ＋． 02 | ＋． 01 | －． 03 | ＋． 05 | ＋． 06 | ＋． 07 | ＋． 06 | ＋． 04 | ＋． 02 | ＋． 02 | ＋． 02 | ＋． 04 | ＋． 1 | ＋． 1 | ＋． 1 | ＋． 1 | ＋． 09 |
| 0031 | 0 | 0 | －． 01 | 0 | －． 02 | －． 01 | －． 02 | 0 | 0 | 0 | 0 | ＋． 01 | －． 01 | 0 | 0 | 0 | 0 | －． 07 | ＋． 03 | $-.05$ | ＋． 04 | －． 04 |
| 0032 | －． 24 | ＋． 08 | ＋． 17 | ＋． 13 | ＋． 12 | ＋． 1 | ＋． 06 | ＋． 11 | ＋． 06 | ＋． 07 | ＋． 12 | ＋． 11 | ＋． 07 | ＋． 03 | ＋． 03 | ＋． 04 | ＋． 04 | ＋． 23 | ＋． 23 | ＋． 23 | ＋． 23 | $+.21$ |
| 0033 | ＋． 08 | －． 14 | －． 05 | $-.44$ | －． 43 | $-.36$ | －． 23 | －． 29 | －． 15 | －． 1 | ＋． 1 | ＋． 1 | ＋． 05 | ＋． 01 | －． 02 | －． 03 | －． 03 | －． 16 | $-.07$ | $-.13$ | －． 07 | －． 1 |
| 0034 | ＋． 17 | －． 06 | －． 12 | －． 09 | －． 09 | －． 07 | －． 04 | －． 06 | －． 03 | －． 03 | ＋． 04 | －． 02 | $+.07$ | 0 | －． 03 | －． 01 | －． 06 | －． 23 | －． 17 | －． 24 | －． 16 | －． 21 |
| 0035 | ＋． 08 | －． 03 | －． 06 | －． 03 | $-.04$ | $-.04$ | $-.02$ | －． 03 | －． 01 | －． 01 | ＋． 02 | －． 09 | $-.07$ | $-.07$ | －． 06 | －． 1 | $-.06$ | －． 16 | $-.08$ | $-.13$ | －． 07 | －． 1 |
| 0036 | －． 01 | 0 | ＋． 01 | －． 01 | 0 | 0 | ＋． 01 | 0 | 0 | 0 | 0 | －． 01 | 0 | 0 | 0 | 0 | 0 | ＋． 02 | $-.06$ | ＋． 01 | －． 08 | $+.01$ |
| 0037 | －． 04 | ＋． 01 | ＋． 03 | ＋． 02 | ＋． 02 | ＋． 01 | ＋． 01 | ＋． 01 | ＋． 01 | ＋． 01 | ＋． 01 | ＋． 01 | 0 | 0 | 0 | ＋． 01 | ＋． 01 | 0 | ＋． 04 | $+.01$ | ＋． 04 | ＋． 02 |
| 0038 | ＋． 01 | －． 03 | －． 01 | －． 32 | －． 29 | －． 24 | －． 15 | －． 09 | －． 04 | －． 04 | －． 01 | －． 01 | －． 01 | －． 01 | －． 01 | －． 01 | －． 01 | －． 01 | －． 01 | －． 02 | －． 01 | －． 01 |
| 0039 | ＋． 02 | －． 07 | －． 01 | －． 62 | －． 57 | －． 46 | －． 3 | －． 17 | －． 08 | －． 07 | －． 02 | $-.01$ | $-.01$ | －． 01 | $-.02$ | －． 02 | －． 01 | －． 03 | －． 02 | $-.03$ | －． 02 | －． 03 |
| 0040 | －． 02 | －． 07 | ＋． 01 | －． 17 | －． 16 | $-.14$ | $-.09$ | －． 28 | －． 29 | －． 26 | ＋． 01 | ＋． 01 | ＋． 01 | $+.01$ | ＋． 03 | ＋． 02 | －． 02 | ＋． 01 | $+.02$ | ＋． 01 | ＋． 02 | ＋． 02 |
| 0041 | －． 22 | ＋． 07 | $+.15$ | ＋． 11 | ＋． 11 | ＋． 09 | ＋． 05 | ＋． 07 | ＋． 04 | ＋． 03 | －． 13 | $-.14$ | －． 1 | －． 05 | ＋． 04 | 0 | ＋． 03 | ＋． 21 | $+.21$ | $+.21$ | ＋． 2 | ＋． 19 |
| 0042 | －． 21 | $+.07$ | ＋． 14 | $+.11$ | ＋． 1 | ＋． 09 | ＋． 05 | ＋． 07 | ＋． 04 | ＋． 04 | －． 04 | ＋． 01 | －． 07 | －． 01 | ＋． 03 | ＋． 01 | $+.05$ | ＋． 18 | ＋． 2 | ＋． 2 | ＋． 19 | ＋． 18 |
| 0043 | －． 13 | ＋． 04 | ＋． 09 | $+.07$ | $+.07$ | ＋． 06 | ＋． 03 | ＋． 04 | $+.03$ | ＋． 01 | －． 11 | －． 06 | －． 06 | －． 03 | ＋． 04 | －． 02 | ＋． 01 | ＋． 12 | ＋． 12 | ＋． 12 | ＋． 12 | $+.11$ |
| 0044 | －． 11 | ＋． 04 | ＋． 08 | ＋． 06 | ＋． 06 | ＋． 05 | ＋． 03 | ＋． 04 | ＋． 02 | ＋． 01 | －． 09 | $-.05$ | $-.05$ | －． 02 | ＋． 03 | $-.01$ | ＋． 01 | ＋． 1 | ＋． 11 | ＋． 11 | ＋． 1 | ＋． 1 |

TABLE V．（Continued）

|  | 0023 | 0024 | 0025 | 0026 | 0027 | 0028 | 0029 | 0030 | 0031 | 0032 | 0033 | 0034 | 0035 | 0036 | 0037 | 0038 | 0039 | 0040 | 0041 | 0042 | 0043 | 0044 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0001 | －． 88 | $-.62$ | $-.54$ | $-.17$ | －． 46 | －． 37 | －． 09 | －． 1 | 0 | －． 24 | ＋． 08 | ＋． 17 | ＋． 08 | －． 01 | －． 04 | ＋． 01 | ＋． 02 | －． 02 | －． 22 | －． 21 | $-.13$ | －． 11 |
| 0002 | ＋． 28 | ＋． 2 | ＋． 18 | ＋． 06 | ＋． 15 | ＋． 12 | －． 31 | ＋． 02 | 0 | ＋． 08 | －． 14 | －． 06 | －． 03 | 0 | ＋． 01 | －． 03 | －． 07 | $-.07$ | ＋． 07 | ＋． 07 | ＋． 04 | ＋． 04 |
| 0003 | ＋． 61 | $+.43$ | ＋． 38 | ＋． 12 | ＋． 32 | $+.26$ | ＋． 06 | ＋． 07 | $-.01$ | $+.17$ | $-.05$ | －． 12 | －． 06 | ＋． 01 | ＋． 03 | －． 01 | －． 01 | ＋． 01 | ＋． 15 | ＋． 14 | ＋． 09 | ＋．08 |
| 0004 | ＋． 49 | $+.35$ | ＋． 3 | ＋． 1 | ＋． 25 | ＋． 2 | －． 46 | ＋． 03 | 0 | ＋． 13 | －． 44 | －． 09 | －． 03 | $-.01$ | ＋． 02 | －． 32 | －． 62 | －． 17 | ＋． 11 | ＋． 11 | ＋． 07 | ＋． 06 |
| 0005 | ＋． 46 | ＋． 33 | ＋． 29 | ＋． 1 | ＋． 24 | ＋． 19 | －． 49 | ＋． 03 | －． 02 | ＋． 12 | －． 43 | －． 09 | －． 04 | 0 | ＋． 02 | －． 29 | －． 57 | －． 16 | ＋． 11 | ＋． 1 | ＋． 07 | ＋． 06 |
| 0006 | ＋． 4 | ＋． 28 | ＋． 25 | ＋． 09 | ＋． 2 | ＋． 16 | －． 45 | ＋． 02 | －． 01 | ＋． 1 | －． 36 | －． 07 | －． 04 | 0 | ＋． 01 | －． 24 | －． 46 | －． 14 | ＋． 09 | ＋． 09 | ＋． 06 | ＋． 05 |
| 0007 | ＋． 22 | ＋． 02 | ＋． 14 | ＋． 05 | ＋． 12 | ＋． 09 | －． 29 | ＋． 01 | －． 02 | ＋． 06 | －． 23 | －． 04 | －． 02 | ＋． 01 | ＋． 01 | －． 15 | －． 3 | －． 09 | ＋． 05 | ＋． 05 | ＋． 03 | ＋． 03 |
| 0008 | ＋． 31 | ＋． 22 | ＋． 18 | ＋． 06 | ＋． 16 | ＋． 12 | －． 61 | －． 03 | 0 | ＋． 11 | －． 29 | －． 06 | －． 03 | 0 | ＋． 01 | －． 09 | －． 17 | －． 28 | ＋． 07 | ＋． 07 | ＋． 04 | ＋． 04 |
| 0009 | ＋． 18 | ＋． 13 | ＋． 08 | ＋． 03 | ＋． 07 | ＋． 06 | －． 31 | ＋． 05 | 0 | ＋． 06 | －． 15 | －． 03 | －． 01 | 0 | ＋． 01 | －． 04 | －． 08 | －． 29 | ＋． 04 | ＋． 04 | ＋． 03 | ＋． 02 |
| 0010 | ＋． 12 | ＋． 09 | ＋． 05 | －． 01 | ＋． 05 | ＋． 04 | －． 19 | ＋． 06 | 0 | ＋． 07 | －． 1 | －． 03 | $-.01$ | 0 | ＋． 01 | －． 04 | －． 07 | －． 26 | ＋． 03 | ＋． 04 | ＋． 01 | ＋． 01 |
| 0011 | ＋． 77 | $+.54$ | ＋． 25 | ＋． 09 | ＋． 16 | ＋． 15 | ＋． 07 | ＋． 07 | 0 | ＋． 12 | ＋． 1 | ＋． 04 | ＋． 02 | 0 | ＋． 01 | －． 01 | －． 02 | ＋． 01 | －． 13 | －． 04 | －． 11 | －． 09 |
| 0012 | ＋． 67 | $+.47$ | ＋． 21 | ＋． 08 | ＋． 15 | ＋． 13 | ＋． 06 | ＋． 06 | ＋． 01 | ＋． 11 | ＋． 1 | －． 02 | －． 09 | $-.01$ | ＋． 01 | －． 01 | －． 01 | ＋． 01 | －． 14 | ＋． 01 | －． 06 | －． 05 |
| 0013 | ＋． 45 | ＋． 36 | ＋． 15 | ＋． 06 | ＋． 1 | ＋． 09 | ＋． 04 | ＋． 04 | $-.01$ | $+.07$ | $+.05$ | ＋． 07 | －． 07 | 0 | 0 | －． 01 | －． 01 | $+.01$ | －． 1 | －． 07 | －． 06 | －． 05 |
| 0014 | ＋． 26 | ＋． 09 | ＋． 08 | ＋． 03 | ＋． 05 | $+.05$ | ＋． 02 | ＋． 02 | 0 | ＋． 03 | ＋． 01 | 0 | －． 07 | 0 | 0 | －． 01 | －． 01 | $+.01$ | －． 05 | －． 01 | －． 03 | －． 02 |
| 0015 | ＋． 71 | ＋． 5 | ＋． 09 | ＋． 04 | ＋． 06 | $+.05$ | ＋． 05 | ＋． 02 | 0 | ＋． 03 | －． 02 | －． 03 | －． 06 | 0 | 0 | －． 01 | －． 02 | ＋． 03 | ＋． 04 | ＋． 03 | ＋． 04 | ＋． 03 |
| 0016 | ＋． 48 | ＋． 35 | ＋． 1 | ＋． 03 | ＋． 08 | ＋． 07 | ＋． 03 | ＋． 02 | 0 | ＋． 04 | －． 03 | －． 01 | －． 1 | 0 | ＋． 01 | －． 01 | －． 02 | ＋． 02 | 0 | ＋． 01 | －． 02 | －． 01 |
| 0017 | ＋． 28 | ＋． 16 | ＋． 03 | －． 02 | ＋． 04 | ＋． 04 | ＋． 02 | ＋． 04 | 0 | ＋． 04 | －． 03 | －． 06 | －． 06 | 0 | ＋． 01 | －． 01 | －． 01 | －． 02 | ＋． 03 | ＋． 05 | ＋． 01 | $+.01$ |
| 0018 | ＋． 83 | ＋． 6 | $+.51$ | ＋． 16 | ＋． 43 | $+.35$ | ＋． 09 | ＋． 1 | －． 07 | ＋． 23 | －． 16 | －． 23 | －． 16 | ＋． 02 | 0 | －． 01 | －． 03 | ＋． 01 | ＋． 21 | ＋． 18 | ＋． 12 | ＋． 1 |
| 0019 | ＋．85 | ＋． 59 | $+.52$ | ＋． 16 | ＋． 44 | ＋． 36 | ＋． 09 | ＋． 1 | ＋． 03 | ＋． 23 | －． 07 | －． 17 | －． 08 | －． 06 | ＋． 04 | －． 01 | －． 02 | ＋． 02 | ＋． 21 | ＋． 2 | ＋． 12 | $+.11$ |
| 0020 | ＋． 83 | ＋． 6 | $+.51$ | ＋． 16 | ＋． 43 | ＋． 35 | ＋． 08 | ＋． 1 | $-.05$ | ＋． 23 | －． 13 | －． 24 | $-.13$ | ＋． 01 | ＋． 01 | －． 02 | －． 03 | ＋． 01 | ＋． 21 | ＋． 2 | ＋． 12 | $+.11$ |
| 0021 | ＋． 83 | $+.57$ | $+.51$ | ＋． 16 | ＋． 43 | ＋． 35 | ＋． 08 | ＋． 1 | ＋． 04 | ＋． 23 | －． 07 | －． 16 | －． 07 | －． 08 | ＋． 04 | －． 01 | －． 02 | ＋． 02 | ＋． 2 | ＋． 19 | ＋． 12 | ＋． 1 |
| 0022 | ＋． 73 | ＋． 55 | ＋． 47 | ＋． 15 | ＋． 4 | ＋． 33 | ＋． 08 | ＋． 09 | －． 04 | ＋． 21 | －． 1 | －． 21 | －． 1 | ＋． 01 | ＋． 02 | －． 01 | －． 03 | ＋． 02 | ＋． 19 | ＋． 18 | ＋． 11 | ＋． 1 |
| 0023 | 1 | $+.53$ | ＋． 48 | ＋． 15 | ＋． 4 | ＋． 33 | ＋． 08 | ＋． 09 | ＋． 01 | ＋． 21 | －． 06 | －． 15 | $-.07$ | $-.04$ | ＋． 03 | －． 01 | －． 02 | ＋． 02 | ＋． 19 | ＋． 18 | ＋． 11 | ＋． 1 |
| 0024 | ＋． 53 | 1 | ＋． 33 | ＋． 11 | ＋． 28 | ＋． 23 | ＋． 05 | ＋． 06 | －． 01 | ＋． 15 | －． 09 | －． 16 | －． 07 | $+.01$ | ＋． 02 | －． 01 | －． 02 | $+.01$ | ＋． 13 | ＋． 13 | $+.08$ | $+.07$ |
| 0025 | ＋． 48 | ＋． 33 | 1 | ＋． 23 | ＋． 6 | ＋． 49 | ＋． 05 | ＋． 04 | －． 01 | ＋． 25 | －． 03 | －． 23 | －． 05 | ＋． 01 | ＋． 04 | $-.01$ | －． 02 | ＋． 09 | ＋． 12 | ＋． 28 | ＋． 19 | ＋． 17 |
| 0026 | ＋． 15 | ＋． 11 | ＋． 23 | 1 | ＋． 18 | ＋． 15 | ＋． 01 | ＋． 01 | 0 | －． 66 | －． 03 | ＋． 37 | －． 01 | 0 | －． 02 | 0 | －． 01 | ＋． 19 | ＋． 07 | －． 44 | ＋． 05 | ＋． 04 |
| 0027 | ＋． 4 | ＋． 28 | ＋． 6 | ＋． 18 | 1 | ＋． 29 | ＋． 05 | ＋． 1 | 0 | ＋． 27 | －． 15 | －． 25 | 0 | 0 | ＋． 05 | －． 01 | －． 01 | 0 | ＋． 35 | ＋． 3 | －． 33 | $+.33$ |
| 0028 | ＋． 33 | ＋． 23 | ＋． 49 | ＋． 15 | ＋． 29 | 1 | ＋． 05 | ＋． 08 | 0 | ＋． 23 | －． 1 | －． 19 | ＋． 03 | 0 | ＋． 04 | －． 01 | －． 01 | 0 | ＋． 26 | ＋． 23 | ＋． 32 | －． 54 |
| 0029 | ＋． 08 | ＋． 05 | ＋． 05 | ＋． 01 | ＋． 05 | ＋． 05 | 1 | ＋． 06 | 0 | ＋． 03 | ＋． 31 | －． 02 | 0 | ＋． 01 | ＋． 01 | ＋． 01 | ＋． 01 | ＋． 21 | ＋． 03 | ＋． 03 | ＋． 01 | ＋． 01 |
| 0030 | ＋． 09 | ＋． 06 | ＋． 04 | ＋． 01 | ＋． 1 | ＋． 08 | ＋． 06 | 1 | 0 | －． 13 | $-.02$ | －． 03 | 0 | 0 | ＋． 03 | 0 | 0 | $-.76$ | ＋． 08 | ＋． 05 | ＋． 01 | ＋． 01 |
| 0031 | ＋． 01 | －． 01 | －． 01 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | ＋． 07 | ＋． 04 | $+.07$ | $-.83$ | ＋． 03 | ＋． 01 | ＋． 03 | ＋． 01 | －． 01 | 0 | $-.01$ | －． 01 |
| 0032 | ＋． 21 | ＋． 15 | ＋． 25 | －． 66 | ＋． 27 | ＋． 23 | ＋． 03 | －． 13 | 0 | 1 | －． 06 | －． 48 | －． 02 | 0 | ＋． 05 | 0 | 0 | $-.08$ | ＋． 17 | $+.57$ | ＋． 06 | ＋． 05 |
| 0033 | －． 06 | －． 09 | $-.03$ | $-.03$ | －． 15 | －． 1 | ＋． 31 | －． 02 | $+.07$ | $-.06$ | 1 | ＋． 23 | ＋． 17 | －． 02 | －． 01 | ＋． 2 | ＋． 39 | ＋． 14 | －． 55 | －． 18 | －． 21 | －． 18 |
| 0034 | －． 15 | －． 16 | －． 23 | ＋． 37 | －． 25 | －． 19 | $-.02$ | －． 03 | $+.04$ | －． 48 | ＋． 23 | 1 | ＋． 16 | －． 01 | －． 04 | ＋． 01 | ＋． 02 | ＋． 09 | －． 31 | －． 89 | －． 22 | －． 19 |
| 0035 | －． 07 | －． 07 | －． 05 | $-.01$ | 0 | ＋． 03 | 0 | 0 | $+.07$ | －． 02 | ＋． 17 | ＋． 16 | 1 | －． 02 | ＋． 02 | ＋． 01 | ＋． 01 | 0 | －． 12 | －． 1 | －． 26 | －． 23 |
| 0036 | －． 04 | ＋． 01 | ＋． 01 | 0 | 0 | 0 | ＋． 01 | 0 | －． 83 | 0 | －． 02 | －． 01 | －． 02 | 1 | 0 | 0 | $+.01$ | 0 | ＋． 01 | ＋． 01 | ＋． 02 | $+.01$ |
| 0037 | ＋． 03 | ＋． 02 | ＋． 04 | －． 02 | ＋． 05 | ＋． 04 | ＋． 01 | ＋． 03 | ＋． 03 | ＋． 05 | $-.01$ | －． 04 | ＋． 02 | 0 | 1 | ＋． 01 | $+.01$ | $-.03$ | ＋． 06 | ＋． 07 | ＋． 03 | ＋． 02 |
| 0038 | －． 01 | $-.01$ | －． 01 | 0 | －． 01 | $-.01$ | $+.01$ | 0 | ＋． 01 | 0 | ＋． 2 | ＋． 01 | ＋． 01 | 0 | ＋． 01 | 1 | $+.51$ | ＋． 06 | 0 | 0 | 0 | 0 |
| 0039 | －． 02 | －． 02 | －． 02 | －． 01 | －． 01 | －． 01 | ＋． 01 | 0 | ＋． 03 | 0 | ＋． 39 | ＋． 02 | ＋． 01 | $+.01$ | ＋． 01 | $+.51$ | 1 | ＋． 12 | 0 | －． 01 | 0 | 0 |
| 0040 | ＋． 02 | ＋． 01 | ＋． 09 | ＋． 19 | 0 | 0 | $+.21$ | －． 76 | ＋． 01 | $-.08$ | ＋． 14 | ＋． 09 | 0 | 0 | －． 03 | ＋． 06 | ＋． 12 | 1 | －． 04 | －． 11 | ＋． 01 | ＋． 01 |
| 0041 | ＋． 19 | ＋． 13 | ＋． 12 | ＋． 07 | ＋． 35 | ＋． 26 | ＋． 03 | ＋． 08 | $-.01$ | ＋． 17 | －． 55 | －． 31 | －． 12 | $+.01$ | ＋． 06 | 0 | 0 | －． 04 | 1 | $+.37$ | ＋． 39 | $+.33$ |
| 0042 | ＋． 18 | ＋． 13 | ＋． 28 | －． 44 | ＋． 3 | ＋． 23 | ＋． 03 | ＋． 05 | 0 | $+.57$ | －． 18 | －． 89 | －． 1 | ＋． 01 | $+.07$ | 0 | $-.01$ | －． 11 | ＋． 37 | 1 | ＋． 25 | ＋． 22 |
| 0043 | ＋． 11 | ＋． 08 | ＋． 19 | ＋． 05 | －． 33 | ＋． 32 | ＋． 01 | ＋． 01 | －． 01 | ＋． 06 | －． 21 | －． 22 | －． 26 | ＋． 02 | ＋． 03 | 0 | 0 | ＋． 01 | ＋． 39 | ＋． 25 | 1 | ＋． 07 |
| 0044 | ＋． 1 | ＋． 07 | ＋． 17 | ＋． 04 | ＋． 33 | －． 54 | $+.01$ | ＋． 01 | $-.01$ | ＋． 05 | －． 18 | －． 19 | －． 23 | $+.01$ | ＋． 02 | 0 | 0 | $+.01$ | ＋． 33 | ＋． 22 | $+.07$ | 1 |



FIG. 16 (color online). Variation of the $k$-factors for inclusive $W$ and $Z$ production under different choices of parton distribution functions, from the Alekhin parton distribution error set [47]. The correlation of the uncertainty on these two $k$-factors due to uncertainty in the parton distribution functions is 0.955 .
are nearly $100 \%$ correlated; varying these scales affects both the $W$ and $Z$ inclusive cross sections in the same way. The uncertainties in the parton distribution functions and the choice of renormalization and factorization scales represent the dominant contributions to the theoretical uncertainty in the total inclusive $W$ and $Z$ cross section calculations at the Tevatron. The term in $\chi_{\text {constraints }}^{2}$ that reflects our knowledge of the theoretical prediction of the inclusive $W$ and $Z$ cross sections explicitly acknowledges this high degree of correlation.

Theoretical constraints on all other $k$-factors are assumed to be uncorrelated with each other, not because the uncertainties of these calculations are indeed uncorrelated, but rather because the correlations among these computations are poorly known.

0002, 0003 .-The cosmic $\gamma$ and cosmic $j$ backgrounds are estimated using events recorded in the CDF data with one or more reconstructed photons and with two or fewer reconstructed tracks. The use of events with two or fewer reconstructed tracks is a new technique for estimating these backgrounds. These correction factors are primarily constrained by the number of events in the VISTA $\gamma \not p$ and $j \not p$ final states. The values are related to (and consistent with) the fraction of bunch crossings with one or more inelastic $p \bar{p}$ interactions, complicated slightly by the requirement that any jet falling in the final state $j \not p$ has at least 5 GeV of track $p_{T}$ within a cone of 0.4 relative to the jet axis.
$0004,0005,0006,0007$.-The NLOJET ++ calculation of the $\gamma j$ inclusive $k$-factor constrains the cross section weighted sum of the $\gamma j, \gamma 2 j, \gamma 3 j$, and $\gamma 4 j$ correction factors to $1.25 \pm 0.15$ [49,50].

0008, 0009, 0010.-The DIPHOX calculation of the inclusive $\gamma \gamma$ cross section at NLO constrains the weighted sum of these correction factors to $2.0 \pm 0.15$ [51]. From Table I, the $\gamma \gamma j k$-factor (0009) appears anomalously large. Figure 17 shows a calculation of this $\gamma \gamma j k$-factor using NLOJET $++[49,50]$ as a function of summed transverse momentum. The NLO correction to the LO prediction is found to be large, and not manifestly inconsistent with the value for this $k$-factor determined from the VISTA fit. The cross section for $\gamma \gamma 2 j$ production has not been calculated at NLO.

0011, 0012, 0013, 0014 .-These correction factors correspond to $k$-factors for $W$ production in association with zero, one, two, and three or more jets, respectively. A linear combination of these correction factors is constrained by the requirement that the inclusive $W$ production cross section is consistent with the NNLO calculation of Ref. [53]. The values of these correction factors, and their trend of decreasing as the number of jets increases, depends heavily on the choice of renormalization and factorization scales. The individual correction factors are not explicitly constrained by a NLO calculation.

0015, 0016, 0017.-These correction factors correspond to $k$-factors for $Z$ production in association with zero, one, and two or more jets, respectively. A linear combination of these correction factors is constrained by the requirement that the inclusive $Z$ production cross section is consistent with the NNLO calculation of Ref. [53].


FIG. 17 (color online). Calculation of the $\gamma \gamma j k$-factor, as a function of jet transverse momentum. The effect of changing the factorization scale by a factor of two in either direction is also shown (small black points with error bars).

0018, 0019.-The two $k$-factors for dijet production correspond to two bins in $\hat{p}_{T}$, the $p_{T}$ of the hard two to two scattering in the parton center of mass frame. These correction factors are constrained by a NLO calculation [54] and show expected behavior as a function of $\hat{p}_{T}$.

0020 , 0021.-The two $k$-factors for 3 -jet production, corresponding to two bins in $\hat{p}_{T}$, are unconstrained by any NLO calculation but show reasonable behavior as a function of $\hat{p}_{T}$.

0022, 0023.-The $k$-factors for 4 -jet production, corresponding to two bins in $\hat{p}_{T}$, are unconstrained by any NLO calculation, but show reasonable behavior as a function of $\hat{p}_{T}$.

0024 .-The $k$-factor for the production of five or more jets, constrained primarily by the VISTA low- $p_{T} 5 j$ final state, is found to be close to unity.

## b. Identification efficiencies

The correction factors in this section, although billed as "identification efficiencies," are truly ratios of the identification efficiency in the data relative to the identification efficiency in CDFSIM. A correction factor value of unity indicates a proper modeling of the overall identification efficiency by CDFSIM; a correction factor value of 0.5 indicates that CDFSIM overestimates the overall identification efficiency by a factor of 2 .

0025 .-The central electron identification efficiency scale factor is close to unity, indicating the central electron efficiency measured in data is similar (to within $1 \%$ ) to the central electron efficiency in the CDF detector simulation. This reflects an emphasis within CDF on tuning the detector simulation for central electrons. The determination of this correction factor is dominated by the VISTA final states $e \not p$ and $e^{+} e^{-}$, where one of the electrons has $|\eta|<1$.

0026 .-The plug electron identification efficiency scale factor is several percent less than unity, indicating that the CDF detector simulation slightly overestimates the electron identification efficiency in the plug region of the CDF detector. The determination of this correction factor is dominated by the VISTA final states $e \not p$ and $e^{+} e^{-}$, where one of the electrons has $|\eta|>1$.

0027, 0028.-To reduce backgrounds hypothesized to arise from pion and kaon decays in flight with a substantially mismeasured track, a very good track fit in the CDF tracker is required. Partially due to this tight track fit requirement, CDF muon identification efficiencies in the regions $|\eta|<0.6$ and $0.6<|\eta|<1.5$ are overestimated in the CDF detector simulation by over $10 \%$. The determination of the identification efficiencies $p(\mu \rightarrow \mu)$ is dominated by the VISTA final states $\mu \not p$ and $\mu^{+} \mu^{-}$.
0029.-The central photon identification efficiency scale factor is determined primarily by the number of events in the VISTA final states $j \gamma$ and $\gamma \gamma$. The uncertainty on this correction factor is highly correlated with the un-
certainties on the $\gamma j k$-factor, the $p(j \rightarrow \gamma)$ fake rate, and the $\gamma \gamma k$-factor.

0030 .-The plug photon identification efficiency scale factor is determined primarily by the number of events in the VISTA final state $\gamma \gamma$. The uncertainty on this correction factor is highly correlated with the uncertainty on the plug $p(j \rightarrow \gamma)$ fake rate.

0031 .-The $b$-jet identification efficiency is determined to be consistent with the prediction from CDFSIM.

## c. Fake rates

0032.-The fake rate $p(e \rightarrow \gamma)$ for electrons to be misreconstructed as photons in the plug region of the detector is added on top of the significant number of electrons misreconstructed as photons by CDFSIM.

0033 .-In VISTA, the contribution of jets faking electrons is modeled by applying a fake rate $p(j \rightarrow e)$ to Monte Carlo jets. VISTA represents the first large scale Tevatron analysis in which a completely Monte Carlo based modeling of jets faking electrons is employed. Significant understanding of the physical mechanisms contributing to this fake rate has been achieved, as summarized in Appendix A 1. Consistency with this understanding is required; for example, $p(j \rightarrow e) \approx p(j \rightarrow \gamma) p(\gamma \rightarrow e)$. The value of this correction factor is determined primarily by the number of events in the VISTA final state $e j$, where the electron is identified in the central region of the CDF detector. It is notable that this fake rate is independent of global event properties, and that a consistent simultaneous understanding of the $e j, e 2 j, e 3 j$, and $e 4 j$ final states is obtained.

0034 .-The value of the fake rate $p(j \rightarrow e)$ in the plug region of the CDF detector is roughly 1 order of magnitude larger than the corresponding fake rate $p(j \rightarrow e)$ in the central region of the detector, consistent with an understanding of the relative performance of the detector in the central and plug regions for the identification of electrons. This correction factor is determined primarily by the number of events in the VISTA final state $e j$, where the electron is identified in the plug region of the CDF detector.

0035 .-In VISTA, the contribution of jets faking muons is modeled by applying a fake rate $p(j \rightarrow \mu)$ to Monte Carlo jets. VISTA represents the first large scale Tevatron analysis in which a completely Monte Carlo based modeling of jets faking muons is employed. The value obtained from the VISTA fit is seen to be roughly 1 order of magnitude smaller than the fake rate $p(j \rightarrow e)$ in the central region of the detector, consistent with our understanding of the physical mechanisms underlying these fake rates, as described in Appendix A 1. The value of this correction factor is determined primarily by the number of events in the VISTA final state $j \mu$.

0036 .-The fake rate $p(j \rightarrow b)$ has $p_{T}$ dependence explicitly imposed. The number of tracks inside a typical jet, and hence the probability that a secondary vertex is
(mis)reconstructed, increases with jet $p_{T}$. The values of these correction factors are consistent with the mistag rate determined using secondary vertices reconstructed on the other side of the beam axis with respect to the direction of the tagged jet [55]. The value of this correction factor is determined primarily by the number of events in the VISTA final states $b j$ and $b b$.

0037, 0038.-The fake rate $p(j \rightarrow \tau)$ decreases with jet $p_{T}$, since the number of tracks inside a typical jet increases with jet $p_{T}$. The values of these correction factors are determined primarily by the number of events in the VISTA final state $j \tau$.

0039, 0040 .-The fake rate $p(j \rightarrow \gamma)$ is determined separately in the central and plug regions of the CDF detector. The values of these correction factors are determined primarily by the number of events in the VISTA final states $j \gamma$ and $\gamma \gamma$. The value obtained for 0039 is consistent with the value obtained from a study using detailed information from the central preshower detector. The fake rate determined in the plug region is noticeably higher than the fake rate determined in the central region, as expected.

## d. Trigger efficiencies

0041 .-The central electron trigger inefficiency is dominated by not correctly reconstructing the electron's track at the first online trigger level.

0042 .-The plug electron trigger inefficiency is due to inefficiencies in clustering at the second online trigger level.

0043, 0044.-The muon trigger inefficiencies in the regions $|\eta|<0.6$ and $0.6<|\eta|<1.0$ derive partly from tracking inefficiency and partly from an inefficiency in reconstructing muon stubs in the CDF muon chambers. The value of these corrections factors are consistent with other trigger efficiency measurements made using additional information [56].

## e. Energy scales

The VISTA infrastructure also allows the jet energy scale to be treated as a correction factor. At present this correction factor is not used, since there is no discrepancy requiring it.

To understand the effect of introducing such a correction factor, a jet energy scale correction factor is added and constrained to $1 \pm 0.03$, reflecting the jet energy scale determination at CDF [15]. The fit returns a value with a very small error, since this correction factor is highly constrained by the low- $p_{T} 2 j, 3 j, e j$, and $e 2 j$ final states. Assuming perfectly correct modeling of jets faking electrons, as described in Appendix A 1, this is a correct energy scale error. The inclusion of additional correction factor degrees of freedom to reflect possible imperfections in this modeling of jets faking electrons increases the energy scale error. The interesting conclusion is that the jet energy scale
(considered as a lone free parameter) is very well constrained by the large number of dijet events; adjustment to the jet energy scale must be accompanied by simultaneous adjustment of other correction factors (such as the dijet $k$-factor) in order to retain agreement with data.

## APPENDIX B: SLEUTH DETAILS

This appendix elaborates on the SLEUTH partitioning rule and on the minimum number of events required for a final state to be considered by SLEUTH.

## 1. Partitioning

Table VI lists the VISTA final states associated with each SLEUTH final state.

## 2. Minimum number of events

This section expands on a subtle point in the definition of the SLEUTH algorithm: for purely practical considerations, only final states in which three or more events are observed in the data are considered.

Suppose $\mathcal{P}_{e^{+} e^{-} b \bar{b}}=10^{-6}$; then in computing $\tilde{\mathcal{P}}$ all final states with $b>10^{-6}$ must be considered and accounted for. (A final state with $b=10^{-7}$, on the other hand, counts as only $\approx 0.1$ final states, since the fraction of hypothetical similar experiments in which $\mathcal{P}<10^{-6}$ in this final state is equal to the fraction of hypothetical similar experiments in which one or more events is seen in this final state, which is $10^{-7}$.) This is a large practical problem, since it requires that all final states with $b>10^{-6}$ be enumerated and estimated, and it is difficult to do this believably.

To solve this problem, let SLEUTH consider only final states with at least $d_{\text {min }}$ events observed in the data. The goal is to be able to find $\tilde{\mathcal{P}}<10^{-3}$. There will be some number $N_{\mathrm{fs}}\left(b_{\mathrm{min}}\right)$ of final states with expected number of events $b>b_{\text {min }}$, writing $N_{\text {fs }}$ explicitly as a function of $b_{\text {min }}$; thus $b_{\text {min }}$ must be chosen to be sufficiently large that all of these $N_{\mathrm{fs}}\left(b_{\text {min }}\right)$ final states can be enumerated and estimated. The time cost of simulating events is such that the integrated luminosity of Monte Carlo events is at most 100 times the integrated luminosity of the data; this practical constraint restricts $b_{\min }>0.01$. The number of SLEUTH Tevatron run II final states with $b>0.01$ is $N_{\mathrm{fs}}\left(b_{\text {min }}=0.01\right) \approx 10^{3}$.

For small $\mathcal{P}_{\text {min }}$, keeping the first term in a binomial expansion yields $\tilde{\mathcal{P}}=\mathcal{P}_{\min } N_{\mathrm{fs}}\left(b_{\text {min }}\right)$, where $\mathcal{P}_{\text {min }}$ is the smallest $\mathcal{P}$ found in any final state. From the discussion above, the computation of $\tilde{\mathcal{P}}$ from $\mathcal{P}_{\text {min }}$ can only be justified if $\mathcal{P}_{\text {min }}>\left(b_{\text {min }}{ }^{d_{\text {min }}}\right)$; if otherwise, final states with $b<b_{\text {min }}$ will need to be accounted for. Thus $\tilde{\mathcal{P}}$ can be confidently computed only if $\tilde{\mathcal{P}}>\left(b_{\min }{ }^{d_{\text {min }}}\right) N_{\mathrm{fs}}\left(b_{\text {min }}\right)$.

Solving this inequality for $d_{\text {min }}$ and inserting values from above,

TABLE VI. Correspondence between SLEUTH and VISTA final states. The first column shows the SLEUTH final state formed by merging the populated VISTA final states in the second column. Charge conjugates of each VISTA final state are implied.

| SLEUTH | VISTA final states |
| :---: | :---: |
| $b \bar{b}$ | $b j, ~ b 2 j, 2 b j, 2 b, 3 b$ |
| $b \bar{b} \ell^{+} \ell^{-}$ | $e^{+} e^{-} b j, e^{+} e^{-} b 2 j, \mu^{+} \mu^{-} b j, \mu^{+} \mu^{-} b 2 j, e^{+} e^{-} 2 b$ |
| $b \bar{b} \ell^{+} \ell^{-} 2 j$ | $e^{+} e^{-} b 3 j, \mu^{+} \mu^{-} b 3 j$ |
| $b \bar{b} \ell^{+} \ell^{-} 2 j \not p$ | $\mu^{+} \mu^{-} 262 j \not p$ |
| $b \bar{b} \ell^{+} \ell^{-} \nsim$ | $e^{+} e^{-} b 2 j \not p, e^{+} e^{-} b j \not p, \mu^{+} \mu^{-} b j \not p, \mu^{+} \mu^{-} b 2 j \not p, e^{+} e^{-} 2 b j \not p, e^{+} e^{-} 2 b \not p, \mu^{+} \mu^{-} 2 b \not p$ |
| $b \bar{b} \ell^{+} 2 j \gamma \underline{p}$ | $e^{+} \gamma 63 j p$, $\mu^{+} \gamma 63 j p p$ |
| $W b \bar{b} j{ }^{\text {j }}$ | $e^{+} b 3 j p p, \mu^{+} b 3 j p p, e^{+} 2 b 2 j p b, \mu^{+} 2 b 2 j p p$ |
| $b \bar{b} \ell^{+} \ell^{\prime+}$ | $e^{+} \mu^{+} 2 b$ |
| $b \bar{b} \ell^{+} \ell^{\prime-}$ | $e^{+} \mu^{-} b j$ |
| $b \bar{b} \ell^{+} \ell^{\prime-} \not p$ | $e^{+} \mu^{-}$bjpp, $e^{+} \mu^{-}$b2jpp |
| $b \bar{b} \ell^{+} \gamma p$ | $\mu^{+} \gamma b 2 j p$ |
| $W b \bar{b}$ | $e^{+} b j \not p, \mu^{+} b j \not p, e^{+} b 2 j \not p, \mu^{+} b 2 j \not p, e^{+} 2 b \not p, e^{+} 2 b j p p, \mu^{+} 2 b j \not p, \mu^{+} 2 b \not p$ |
| $b \bar{b} \ell^{+} p \tau^{-}$ | $\mu^{+} \tau^{-}$bjp |
| $b \bar{b} \ell^{+} \tau^{+}$ | $e^{+} \tau^{+}{ }^{+}{ }^{\text {d }}$ |
| $b \bar{b} \ell^{+} \tau^{-}$ | $e^{+} \tau^{-} b j, e^{+} \tau^{-} 2 b$ |
| $b \bar{b} 2 j$ | b3j, 2b2j |
| $b \bar{b} 2 j \gamma$ | rb3j, $\gamma 2 b 2 j$ |
| $b \bar{b} 2 j \gamma \not \underline{ }$ | rb3jp |
| $b \bar{b} 2 j \not ¢$ | b3jpr, 2b2jp |
| $b \bar{b} \gamma \gamma 2 j$ | $2 \gamma b 3 j$ |
| $\gamma b \bar{b}$ | $\gamma b j, \gamma b 2 j, \gamma 2 b, \gamma 2 b j, \gamma 3 b$ |
| $b \bar{b} \gamma p$ | $\gamma b j p b, \gamma b 2 j p b, \gamma 2 b p$ |
| $b \bar{b} \not \square$ | $b 2 j \not p, b j \not p, 2 b j \not p, 2 b \not p$ |
| $\gamma \gamma b \bar{b}$ | $2 \gamma b j, 2 \gamma b 2 j, 2 \gamma 2 b$ |
| $\ell^{+} \ell^{-}$ | $e^{+} e^{-}, e^{+} e^{-} j, \mu^{+} \mu^{-}, \mu^{+} \mu^{-} j, e^{+} e^{-} b, \mu^{+} \mu^{-} b$ |
| $\ell^{+} \ell^{-} 2 j$ | $e^{+} e^{-} 2 j, e^{+} e^{-} 3 j, \mu^{+} \mu^{-} 2 j, \mu^{+} \mu^{-} 3 j$ |
| $\ell^{+} \ell^{-} 2 j \gamma$ | $e^{+} e^{-} \gamma 2 j, e^{+} e^{-} \gamma 3 j, \mu^{+} \mu^{-} \gamma 2 j, \mu^{+} \mu^{-} \gamma 3 j$ |
| $\ell^{+} \ell^{-} 2 j p$ | $e^{+} e^{-} 2 j \not p, e^{+} e^{-} 3 j \not p, \mu^{+} \mu^{-} 2 j p p, \mu^{+} \mu^{-} 3 j \not p$ |
| $\ell^{+} \ell^{-} \tau^{+} 2 j \not p$ | $e^{+} e^{-} \tau^{+} 2 j$ |
| $\ell^{+} \ell^{-} \ell^{\prime} \gamma \not p$ | $e^{+} \mu^{+} \mu^{-} \gamma j$ |
| $\ell^{+} \ell^{-} \ell^{\prime} \not p$ | $e^{+} \mu^{+} \mu^{-}, e^{+} e^{-} \mu^{+}, e^{+} e^{-} \mu^{+} \not p$ |
| $\ell^{+} \ell^{-} \gamma$ | $e^{+} e^{-} \gamma, \mu^{+} \mu^{-} \gamma, e^{+} e^{-} \gamma j, \mu^{+} \mu^{-} \gamma j$ |
| $\ell^{+} \ell^{-} \gamma p$ | $e^{+} e^{-} \gamma j p p, e^{+} e^{-} \gamma p$ |
| $\ell^{+} \ell^{-} \gamma \tau^{+} \not p$ | $e^{+} e^{-} \tau^{+} \gamma$ |
| $\ell^{+} \ell^{-} \not p$ | $e^{+} e^{-} \not p, e^{+} e^{-} j \not p, \mu^{+} \mu^{-} \not p, \mu^{+} \mu^{-} j \not p, e^{+} e^{-} b \not p$ |
| $\ell^{+} \ell^{-} \not p \tau^{+}$ | $e^{+} e^{-} \tau^{+}, e^{+} e^{-} \tau^{+} j, \mu^{+} \mu^{-} \tau^{+}$ |
| $\ell^{+} \ell^{-} 4 j$ | $e^{+} e^{-} 4 j, \mu^{+} \mu^{-} 4 j$ |
| $\ell^{+} \ell^{-} 4 j \phi$ | $e^{+} e^{-} 4 j \not p$ |
| $\ell^{+} \ell^{-} \tau^{+} 4 j \not \emptyset$ | $e^{+} e^{-} \tau^{+} 4 j$ |
| $\ell^{+} \ell^{\prime+}{ }_{j}{ }^{\text {d }}$ | $e^{+} \mu^{+} 3 j$ |
| $\ell^{+} \ell^{\prime+} \not p j j$ | $e^{+} \mu^{+} 2 j p$ |
| $\ell^{+} \ell^{\prime-}{ }^{+}{ }^{\text {d }}$ | $e^{+} \mu^{-} 2 j$ |
| $\ell^{+} \ell^{\prime-} \not \ldots j j$ | $e^{+} \mu^{-} 3 j \not p, e^{+} \mu^{-} 2 j \not \emptyset \quad$ |
| $W \gamma j j$ | $\mu^{+} \gamma 2 j \not p, e^{+} \gamma 2 j \not p, \mu^{+} \gamma 3 j \not p, e^{+} \gamma 3 j \not p$ |
| $W_{j j}$ | $e^{+} 2 j \not p, \quad \mu^{+} 2 j \not p, e^{+} 3 j \not p, \quad \mu^{+} 3 j \not p$ |
| $\ell^{+} \tau^{+} \not{ }^{\text {bj }}$ j | $\mu^{+} \tau^{+} 3 j \not p$ |
| $\ell^{+} \tau^{-} \not \chi_{j j}$ | $e^{+} \tau^{-} 2 j \not p, e^{+} \tau^{-} 3 j \not p, \mu^{+} \tau^{-} 3 j \not p, \quad \mu^{+} \tau^{-} 2 j \not p$ |
| $\ell^{+} \tau^{+} j j$ | $e^{+} \tau^{+} 2 j, \mu^{+} \tau^{+} 2 j, e^{+} \tau^{+} 3 j$ |
| $\ell^{+} \tau^{-} j j$ | $e^{+} \tau^{-} 2 j, e^{+} \tau^{-} 3 j, \mu^{+} \tau^{-} 2 j, \mu^{+} \tau^{-} 3 j$ |
| $\ell^{+} \ell^{\prime+}$ | $e^{+} \mu^{+}, e^{+} \mu^{+} j$ |
| $\ell^{+} \ell^{\prime+} \not p$ | $e^{+} \mu^{+} j \not p, e^{+} \mu^{+} \not p$ |
| $\ell^{+} \ell^{\prime-}$ | $e^{+} \mu^{-}, e^{+} \mu^{-} j$ |
| $\ell^{+} \ell^{\prime-} \gamma \not p$ | $e^{+} \mu^{-} \gamma j \not p$ |
| $\ell^{+} \ell^{\prime-} \nsim$ | $e^{+} \mu^{-} \not p, e^{+} \mu^{-} j \not p, e^{+} \mu^{-} b \not p$ |

TABLE VI. (Continued)

| SLEUTH | VISTA final states |
| :---: | :---: |
| $W \gamma$ | $\mu^{+} \gamma \not p, e^{+} \gamma \not p, \mu^{+} \gamma j p p, e^{+} \gamma j \not p$ |
| $\ell^{+} \tau^{-} \gamma$ | $e^{+} \tau^{-} \gamma$ |
| W | $e^{+} \not p, \mu^{+} \not p, e^{+} j \not p, \mu^{+} j \not p, e^{+} b \not p, \mu^{+} b \not p$ |
| $\ell^{+} \tau^{+} p$ | $e^{+} \tau^{+} \not p, \mu^{+} \tau^{+} \not p, e^{+} \tau^{+} j \not p, \mu^{+} \tau^{+} j p \underline{ }$ |
| $\ell^{+} \tau^{-} \not p$ | $e^{+} \tau^{-} \not p, e^{+} \tau^{-} j \not p, \mu^{+} \tau^{-} \not p, \mu^{+} \tau^{-} j \not p$ |
| $\ell^{+} \tau^{+}$ | $e^{+} \tau^{+}, e^{+} \tau^{+} j, \mu^{+} \tau^{+}, \mu^{+} \tau^{+}{ }_{j}$ |
| $\ell^{+} \tau^{-}$ | $e^{+} \tau^{-}, \mu^{+} \tau^{-}, e^{+} \tau^{-} j, \mu^{+} \tau^{-} j, e^{+} \tau^{-} b$ |
| $W \gamma 4 j$ | $\mu^{+} \gamma 4 j \not p, e^{+} \gamma 4 j \not p$ |
| W4j | $e^{+} 4 j p, \mu^{+} 4 j \not \underline{1}$ |
| $\ell^{+} 4 j \tau^{-}$ | $e^{+} \tau^{-} 4 j$ |
| $W \gamma \gamma$ | $e^{+} 2 \gamma \not p, \mu^{+} 2 \gamma \not p$ |
| jj | $2 j, 3 j$ |
| $\gamma j j$ | $\gamma 2 j, \gamma 3 j$ |
| $\gamma \not p j j$ | $\gamma 2 j \not p, \gamma 3 j p$ |
| jjp | $3 j p h, 2 j p$ |
| $\tau \not p j j$ | $\tau^{+} 2 j \not p, \quad \tau^{+} 3 j \not \emptyset$ |
| $\gamma \gamma j j$ | $2 \gamma 2 j, 2 \gamma 3 j$ |
| jj\% $\chi^{\prime}$ | $2 \gamma 2 j \not p$ |
| $\gamma \gamma \gamma j j$ | $3 \gamma 2 j$ |
| $\gamma j$ | $\gamma j, \gamma b$ |
| $\gamma p$ | $\gamma \not p, \gamma j p, \gamma b \nsim$ |
| $\tau \not p \gamma$ | $\tau^{+} \gamma \not p, \tau^{+} \gamma j \not p$ |
| jp | jpb, bpb |
| $\tau \underline{\square}$ | $\tau^{+} j \not p, \tau^{+} b \not p$ |
| $b \bar{b} b \bar{b}$ | $3 b j$ |
| $W b \bar{b} b \bar{b}$ | $e^{+} 3 b j p b$ |
| $\ell^{+} \ell^{+}$ | $2 e^{+}, 2 e^{+} j, 2 \mu^{+}$ |
| $\ell^{+} \ell^{-} \ell^{+} j j \not p$ | $2 e^{+} e^{-} 2 j, 2 e^{+} e^{-} 3 j$ |
| $\ell^{+} \ell^{-} \ell^{+} \not p$ | $2 e^{+} e^{-}, 2 e^{+} e^{-} j, 2 e^{+} e^{-} \not p$ |
| $\ell^{+} \ell^{+} j j$ | $2 e^{+} 2 j$ |
| $\ell^{+} \ell^{+} \ell^{\prime-} \not p$ | $e^{+} 2 \mu^{-} \not p$ |
| $\ell^{+} \ell^{+} \gamma$ | $2 e^{+} \gamma$ |
| $\ell^{+} \ell^{+} \gamma \underline{p}$ | $2 e^{+} \gamma \underline{p}$ |
| $\ell^{+} \ell^{+} \not p$ | $2 e^{+} \not p, 2 e^{+}{ }^{\text {jp }}$ |
| $\ell^{+} \ell^{+} 4 j$ | $2 e^{+} 4 j$ |
| $4 j$ | $4 j$ |
| $\gamma 4 j$ | $\gamma 4 j$ |
| $\gamma 4 j p$ | $\gamma 4 j p$ |
| $4 j p$ | 4jpb |
| $\tau^{+} \not p 4 j$ | $\tau^{+} 4 j \not p$ |
| $\gamma \gamma 4 j$ | $2 \gamma 4 j$ |
| $\gamma \gamma$ | $2 \gamma, 2 \gamma j, 2 \gamma b$ |
| $\gamma \gamma p$ | $2 \gamma \not p, 2 \gamma j \not p$ |
| $3 \gamma$ | $3 \gamma, 3 \gamma j$ |

$$
\begin{equation*}
d_{\min } \geq \frac{\log _{10} \tilde{\mathcal{P}}-\log _{10} N_{\mathrm{fs}}\left(b_{\min }\right)}{\log _{10} b_{\min }} \approx \frac{-3-3}{-2}=3 \tag{B1}
\end{equation*}
$$

A believable trials factor can be computed if $d_{\min } \geq 3$.
At the other end of the scale, computational strength limits the maximum number of events SLEUTH is able to consider to $\leq 10^{4}$. Excesses in which the number of events exceed $10^{4}$ are expected to be identified by VISTA's normalization statistic.

For each final state, pseudo experiments are run until $\mathcal{P}$ is determined to within a fractional precision of $5 \%$ or a time limit is exceeded. If the time limit is exceeded before $\mathcal{P}$ is determined to within the desired fractional precision of 5\%, SLEUTH returns an upper bound on $\mathcal{P}$, and indicates explicitly that only an upper bound has been determined. For the data described in this article, the desired precision is obtained.
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