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Efficient Probabilistic Information Broadcast Algorithm over Random Geometric Topologies

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Abstract—This paper studies reliability of probabilistic gossip algorithms over the random geometric topologies which model ad hoc networks. We propose an efficient algorithm that ensures higher reliability at lower message complexity than the three families of gossip algorithms. Such an improvement is reasonably estimated by our reliability model. The results obtained by OMNET++ simulator confirm the prediction that our algorithm is the best choice for random geometric networks.

I. INTRODUCTION

Information broadcast is a basic service for many distributed applications in ad hoc networks. A message generated by a source is transferred to all other sites by successive retransmissions, since sites have no direct connection to each other in the network. In particular, even though global information about the topology is hardly available in large-scale system, an efficient broadcast protocol should still be able to provide high reliability and low latency with tolerable message exchanges.

The simplest solution is using a *pure flooding* protocol [14]. Upon the first reception of a message, every site delivers it to the application and also forwards it to all sites in its retransmission range once. Evidently, this form of dissemination is very wasteful and may give rise to a *broadcast storm* [21], entailing for instance packet collision and loss.

A common alternative to the flooding is to require the sites of the system to relay the message only to some of their neighbors. The decision of the neighbors is either carried out in a deterministic or probabilistic way. The problem of the former ensuring high reliability is that its implementation is commonly very hard (i.e., in some schemes it is proven to be NP-hard to reach the optimal performance) and requires more information even if the mobility is not considered [19]. Hence, in our study we are interested in probabilistic schemes that highlight their simplicity and scalability [8], [27]. More precisely, three basic probabilistic gossip algorithms are widely-deployed in ad hoc networks without overlay construction for reliable dissemination: (1) Probabilistic Edge Gossip (*GossipPE*) [25], (2) Probabilistic Broadcast Gossip (*GossipPB*) [10], and (3) Probabilistic Inverse Self-degree Broadcast Gossip (*GossipPISB*) [6]. Furthermore, we propose an efficient algorithm: Probabilistic Inverse Neighbor-degree Edge Gossip (*GossipPINE*), which exploits local information about sites in a one-hop neighborhood. It performs better than the basic gossip algorithms over two kinds of random geo-

metric topologies with and without border effects, which are commonly used to analyze the behavior of ad hoc networks.

On the other hand, we introduce a model to explain the best reliability given by our algorithm *GossipPINE* amongst all gossip algorithms. Interestingly, we find that the reliability of *GossipPINE* is accurately estimated for both topologies, and not affected by complex feature of the topology such as edge dependency and border effect. In contrary, the reliability of the other algorithms shows a significant variation from one topology to another. We therefore argue that *GossipPINE* is robust even in networks whose global characteristics are unknown beforehand.

Extensive simulations on top of OMNET++ [1] almost conform to our theoretical results of reliability. The latency, another important metric for broadcasting service, is also evaluated.

The road-map of this paper is organized as follows. An overview of the random networks and the gossip algorithms is given in Sections II and III. Section IV presents our gossip algorithm. The performance metrics are defined in Section V, while we explain our model in Section VI. Section VII evaluates our simulation and related work is discussed in Section VIII. Section IX concludes this paper.

II. SYSTEM TOPOLOGIES

A network underlying a large-scale dissemination system can be viewed as a bidirectional or undirected graph. It is comprised of N sites $\{s_1, s_2, \dots, s_N\}$. The set of sites s_j , connected to s_i (i.e., $s_i \sim s_j$), is called s_i 's neighbors, represented by Λ_i whose cardinal is the degree of s_i , denoted V_i . $P(k)$ represents the degree distribution of sites with k neighbors (i.e., the fraction of sites with degree k) in the graph and \bar{V} is the mean degree ($\bar{V} = \sum_{k=0}^{N-1} P(k) \cdot k$). Moreover, another important property of the graph is defined as follows.

Clustering Coefficient, denoted C of a given random graph, for distinct sites s_i, s_j, s_k , is the conditional probability that, given the existence of edges $s_i \sim s_k$ and $s_j \sim s_k$, an edge $s_i \sim s_j$ also exists (i.e., $P_{connect}(s_i \sim s_j | s_i \sim s_k, s_j \sim s_k)$).

Our study focuses on the random geometric graphs [22], which model ad hoc networks in [6], [10], [25].

More precisely, the sites are distributed uniformly at random in a bounded region, which composes a random geometric graph. In this article, such a region is a rectangular plane with

length a and width b . Furthermore, two sites are connected, as long as the distance between them is at most ρ . Based on [23], we can fine-tune $\rho > \sqrt{\frac{(1+\varepsilon) \cdot \ln(N) \cdot a \cdot b}{N \cdot \pi}}$ with a positive constant ε in order to ensure that the graph is connected.

As observed in [12], this random graph can have **Border Effect**, where the degree of the sites close to boundaries is much smaller than the mean degree. If we ignore it, the topology, denoted $\mathcal{T}(N, \rho)$, follows a Poisson-distribution [16]: $P_t(k) = \exp(-\bar{V}_t) \frac{\bar{V}_t^k}{k!}$ with mean degree $\bar{V}_t = \frac{N \cdot \pi \cdot \rho^2}{a \cdot b}$. In [3], the edge dependency is calculated as $C = 0.5865$.

Otherwise, the sites with low degree near the boundary, which in fact have an important impact on reliability of gossip algorithm, should be taken into account. As shown in [11], the topology with the *border effect*, denoted $\mathcal{G}(N, \rho)$, has the degree distribution: $P_g(k) = P_t(k) \left(\frac{(a-2\rho)(b-2\rho)}{ab} + \frac{2a\rho+(b-2\rho)\rho}{ab} \psi(k) \right)$ where $\psi(k) = \int_0^1 \exp(-\bar{V}_t(F(x)-1)) \cdot F(x)^k dx$ with $F(x) := \frac{1}{\pi} (x\sqrt{1-x^2} - \arccos(x)) + 1$. Trivially, the mean degree can be calculated as $\bar{V}_g = \sum_{k=0}^{N-1} P_g(k) \cdot k$.

III. GOSSIP ALGORITHMS

Broadcast in large-scale network is commonly studied on the basis of Algorithm 1. Initially, the source sends a message to *all* of its neighbors (Lines 2 and 3). A site delivers and retransmits a received message provided it has not previously received it; otherwise, the message is discarded. Sites that have received the message at least once are called **infected sites**.

Algorithm 1: Generic Gossip Algorithm

```

1 Broadcast ( $\langle msg \rangle$ )
2   foreach  $s_j \in \Lambda_i$  do
3      $\lfloor$  Send( $\langle msg \rangle, s_j$ )
4 Receive ( $\langle msg \rangle$ )
5   if  $msg \notin msgHistory$  then
6     Deliver( $\langle msg \rangle$ )
7      $msgHistory \leftarrow msgHistory \cup \{\langle msg \rangle\}$ 
8     Gossip( $\langle msg \rangle, parameters$ )

```

Basically, probabilistic gossip algorithms, which disseminate information in ad hoc networks without overlay construction can be classified into three families, to implement Gossip() procedure: (1) Probabilistic Edge Gossip (*GossipPE*) [25], (2) Probabilistic Broadcast Gossip (*GossipPB*) [10], and (3) Probabilistic Inverse Self-degree Broadcast Gossip (*GossipPISB*) [6]. Besides the received message, the Gossip() procedure takes one parameter which is identical for all sites. In the sequel, Random() generates a random number in the interval $[0, 1]$.

Algorithm 2: Probabilistic Edge Gossip (at s_i)

```

9 /*  $p_e$ : probability to use an edge */
10 GossipPE ( $\langle msg \rangle, p_e$ )
11   foreach  $s_j \in \Lambda_i$  do
12     if Random()  $\leq p_e$  then
13        $\lfloor$  Send( $\langle msg \rangle, s_j$ )

```

In *GossipPE* (Algorithm 2), a site s_i chooses to send msg over an edge independently from the other edges with regard to a fixed probability p_e (see Line 12). Note that when $p_e = 1$ for all sites, we obtain the flooding algorithm.

Algorithm 3: Probabilistic Broadcast Gossip (at s_i)

```

14 /*  $p_v$ : probability to broadcast */
15 GossipPB ( $\langle msg \rangle, p_v$ )
16   if Random()  $\leq p_v$  then
17     foreach  $s_j \in \Lambda_i$  do
18        $\lfloor$  Send( $\langle msg \rangle, s_j$ )

```

Unlike Algorithm 2, in *GossipPB* (Algorithm 3), each site, except the source, diffuses msg to all its neighbors with probability p_v (see line 16). In particular, when $p_v = 1$ this protocol becomes the flooding algorithm.

Algorithm 4: Probabilistic Inverse Self-degree Broadcast Gossip (at s_i)

```

19 /*  $c_v$ : constant to control broadcast */
20 GossipPISB ( $\langle msg \rangle, c_v$ )
21   if Random()  $\leq \min\{\frac{c_v}{V_i}, 1\}$  then
22     foreach  $s_j \in \Lambda_i$  do
23        $\lfloor$  Send( $\langle msg \rangle, s_j$ )

```

In *GossipPISB* (Algorithm 4), every site except the source rebroadcasts msg to all its neighbors independently with probability $\min\{\frac{c_v}{V_i}, 1\}$ (see Line 21). When $c_v \geq \max\{V_1, V_2, \dots, V_N\}$ this protocol is the flooding algorithm.

IV. OUR ALGORITHM

The idea behind our algorithm is to ensure that sites with very low degree are infected, if one of their neighbors is infected. On the other hand, fewer redundant message copies are received at the sites with high degree. This will be analyzed in Sections VI and VII.

Algorithm 5: Probabilistic Inverse Neighbor-degree Edge Gossip (at s_i)

```

24 /*  $c_e$ : constant to control edge use */
25 GossipPINE ( $\langle msg \rangle, c_e$ )
26   foreach  $s_j \in \Lambda_i$  do
27     if Random()  $\leq \min\{\frac{c_e}{V_j}, 1\}$  then
28        $\lfloor$  Send( $\langle msg \rangle, s_j$ )

```

Algorithm 5 shows our Probabilistic Inverse Neighbor-degree Edge Gossip, denoted *GossipPINE*. We assume that every site knows the degree of its neighbors. Like *GossipPE*, site s_i randomly chooses its edges over which msg should

be transmitted. However, the probability to send on one edge depends on the degree of the connected neighbor (see Line 27).

V. PERFORMANCE METRICS

For performance evaluation of the gossip algorithms, the following metrics are commonly used [7], [18], [20]:

Message Complexity, denoted M: measures the mean number of messages received (or sent, since no message loss is taken into consideration) by each site: $M = \frac{\Omega}{N-1}$, where Ω is the total number of messages exchanged during the dissemination.

Reliability, denoted R: is defined as the percentage of messages generated by a source that are delivered by all sites. A reliability value of 100% is indicative that the algorithm was successful in delivering any given message to all sites (i.e., every site is infected for any given message) ensuring thus *atomicity* similarly to pure flooding algorithms [15].

Latency, denoted L: measures the number of hops required to deliver a message to all recipients, i.e., the number of hops of the longest path among all the shortest paths from the source to all other sites that received the message.

VI. RELIABILITY MODELING

In this section, we compare the probabilistic gossip algorithms by our reliability model, which explains the best performance of our algorithm *GossipPINE* in random geometric graphs.

Since we are only interested in whether a site has been infected by the end of the broadcast, a *dissemination graph* is exploited for modeling the reliability.

Given a graph $G = (S; E)$, and a source site s_0 , the probabilistic gossip algorithms follow the same principle: when a new message arrives at a site, this site chooses a subset (possibly empty) of its neighbors in G and forwards the message to these neighbors.

In our analysis, we assume that every site selects a set of neighbors to receive the message in an initial phase. We thus obtain a directed graph $\vec{G} = (S; \vec{E})$ with sites identical to G . For an edge $(s_i \sim s_j) \in E$, the arc $\vec{s}_i \vec{s}_j$ is a part of \vec{G} , if s_i has selected s_j in the initial phase. Then, a site s_i is infected during dissemination, if there is a path from s_0 to s_i in \vec{G} . Furthermore, if every site receives the message, the number of arcs in \vec{G} expresses the message complexity. We call \vec{G} **Dissemination Graph**.

We call a site **isolated** in the dissemination graph, if it has no incoming arcs. Evidently, an isolated site is not infected by a given gossip algorithm. We call the probability that an edge in E becomes an arc towards one site in S the **forwarding probability**, denoted p_{forw} .

We assume as a precondition that the random network $G = (S; E)$ is connected. Thus, any message will reach all sites by *pure flooding*. We model the reliability as the probability that no site is isolated in the dissemination graph. Hence, for

a random topology with N sites and degree distribution $P(k)$ we model the probability R as

$$R = \prod_{i=1}^{N-1} (1 - (1 - p_{forw}(i))^i)^{P(i) \cdot N} \quad (1)$$

where $p_{forw}(i)$ denotes the probability that a site with degree i has an incoming arc from a neighbor. Our evaluation shows that this equation provides a good estimate for the reliability while assuming that every site is isolated independently as done in [8]. However, due to high clustering coefficient in random geometric graphs, one isolated site can even make adjacent sites never receive the message, particularly in sparse density area. Our model shown in Equation (1) will consequently overestimate the reliability, especially in $\mathcal{G}(N, \rho)$ with border effect. Yet, our simulations show that our model still gives a valuable estimate and correctly indicates which algorithm is more or less reliable.

GossipPE enables every site to be selected at random by neighbors with probability p_e . Therefore, its forwarding probability: $p_{forw}^{PE} = p_e$. In the same way, $p_{forw}^{PB} = p_v$ and $p_{forw}^{PINE}(i) = \min\{\frac{c_v}{i}, 1\}$ for *GossipPB* and *GossipPINE* respectively. The message reception by *GossipPISB* in a site s_i depends on the degree of its neighbors, while the latter is highly associated with the degree of s_i . Lemma 1 studies the average degree of an arbitrary neighbor of s_i whose degree is given, ignoring the border effect of random geometric graphs.

Lemma 1: In $\mathcal{T}(N, \rho)$, given a site s_i with degree V_i and one adjacent site s_j with V_j neighbors, we can get the average value of V_j as:

$$NeighD = 1 + (V_i - 1) \cdot C + (\bar{V}_t - 1) \cdot (1 - C) \quad (2)$$

where $\bar{V}_t = \frac{N \cdot \pi \cdot \rho^2}{a \cdot b}$ is the mean degree of the graph.

Proof: Figure 1 shows s_i , a neighbor s_j , and the retransmission zones (i.e., $Disc(s_i)$, $Disc(s_j)$). We call the overlapped part between two discs **lune** (i.e., $Lune(s_i, s_j)$). Let $disc$ be the area of $Disc(s_j)$. Then, the average area of the lune is $C \cdot disc$. Clearly, the density of sites inside $Disc(s_i)$, and also inside $Lune(s_i, s_j)$ is $\frac{V_i}{disc}$. If $disc$ is small, we can assume that the density outside $Disc(s_i)$ is $\frac{\bar{V}_t}{disc}$. Therefore, s_j has $\frac{V_i}{disc} \cdot C \cdot disc$ neighbors in $Lune(s_i, s_j)$, $\frac{\bar{V}_t}{disc} \cdot (1 - C) \cdot disc$ neighbors outside $Lune(s_i, s_j)$, plus s_i .

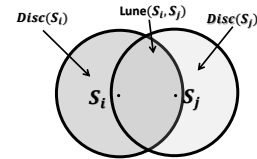


Figure 1: Two kinds of s_j 's neighbors

From Lemma 1, we can derive $p_{forw}^{PISB}(i) = \min\{\frac{c_v}{1 + (i-1) \cdot C + (\bar{V}_t - 1) \cdot (1 - C)}, 1\}$ for $\mathcal{T}(N, \rho)$, while we approximate it for $\mathcal{G}(N, \rho)$ in replacing \bar{V}_t by \bar{V}_g that is the

mean degree of the random topology with the border effect (see Section II).

Theorem 2: If all algorithms generate the same message complexity, then for $k < \bar{V}$

$$p_{forw}^{PINE}(k) > p_{forw}^{PISB}(k) > p_{forw}^{PE} = p_{forw}^{PB} \quad (3)$$

holds.

Proof: According to the study in [12], we infer input parameters of gossip algorithms to reach a given message complexity. Therefore, when identical message complexity holds for all gossip algorithms, $c_e = c_v$, $p_e = p_v$, and $c_v \geq p_e \cdot \bar{V}$. Trivially, $p_{forw}^{PE} = p_{forw}^{PB}$.

Since $k < \bar{V}$ implies $k < NeighD < \bar{V}$, it follows for $k \geq c_e$: $p_{forw}^{PINE} = \frac{c_e}{k} = \frac{c_v}{k} > \frac{c_v}{NeighD} = p_{forw}^{PISB}$, and $\frac{c_v}{NeighD} \geq \frac{p_e \cdot \bar{V}}{NeighD} > p_e = p_{forw}^{PE}$. Then, $p_{forw}^{PINE}(k) > p_{forw}^{PISB}(k) > p_{forw}^{PE} = p_{forw}^{PB}$.

Furthermore, we can deduce that the sites with degree smaller than \bar{V} are the majority in $\mathcal{T}(N, \rho)$ and $\mathcal{G}(N, \rho)$, which dominate the site isolations. In regard to our reliability model described in Equation (1), *GossipPINE*, which ensures the message reception in sites with lower degree, is thus more reliable in random geometric graphs than the other gossip algorithms.

VII. PERFORMANCE EVALUATION

In this section, we evaluate performance of the four probabilistic gossip algorithms in Sections III and IV: *GossipPE*, *GossipPB*, *GossipPISB*, and our algorithm *GossipPINE*. These algorithms are executed over two kinds of random geometric graphs described in Section II.

Our simulations are conducted on top of OMNET++. We consider networks composed of $N = 1000$ sites and, in order to ensure connectivity, $\varepsilon = 1$ for every random geometric graph, where $a = 7500$, $b = 3000$, $\rho = 330$, such that the mean degree of $\mathcal{G}(N, \rho)$ (resp., $\mathcal{T}(N, \rho)$) is about 14 (resp., 15). The graphs without border effect are generated by bending the rectangular region into a Torus $\mathcal{T}(N, \rho)$, while the Euclidean distance between every site is measured.

The results, obtained by our reliability modeling, are also compared with our simulation. We can observe that in terms of reliability, our algorithm outperforms the other gossip algorithms, which conforms to Theorem 2.

For each gossip algorithm, we fixed the parameter values to reach a given message complexity in using the method introduced in [12], and then evaluated the reliability and the latency of the algorithm. 200 different messages are generated by 200 different sources that are chosen uniformly amongst 1000 sites over 50 different graphs related to each of the topologies. Then, the results for each message complexity are averaged by the $200 \times 50 = 10000$ message disseminations.

As a matter of fact, we can configure the topology parameters with other values, whereas the best reliability of our algorithm *GossipPINE* is always obtained, as estimated by our model for the geometric graphs. Due to lack of space in our paper, we do not give exhaustive presentation.

Reliability: We now discuss the reliability values for the gossip algorithms in $\mathcal{T}(N, \rho)$ and $\mathcal{G}(N, \rho)$, obtained by the simulations as well as our model.

The results are plotted in Figure 2, where the models for *GossipPINE* and *GossipPISB* are called **ModelPINE** and **ModelPISB** respectively. As explained in Section VI, our model gives the same result for *GossipPE* and *GossipPB*. This is depicted as **ModelPE**.

GossipPINE exhibits the best performance in both Figures 2(a) and 2(b), while *GossipPB* and *GossipPE* show the worst reliability. In regard to $\mathcal{T}(N, \rho)$, the reliability is more or less degraded in $\mathcal{G}(N, \rho)$ for every gossip algorithm. Especially, *GossipPB* is far less reliable than the other algorithms in $\mathcal{G}(N, \rho)$. Compared with $\mathcal{T}(N, \rho)$, on the boundaries of the rectangular field $\mathcal{G}(N, \rho)$ lie a large number of sites with low degree (see Section II). These sites are easily isolated in *GossipPB*, which results from the clustering effect explained in [12].

Due to the high clustering coefficient, as shown in Lemma 1, sites with low degree are very likely to be clustered together in random geometric graphs (i.e., small groups of interconnected sites with relatively few edges to other groups). As a result, a single isolated site can render many adjacent sites isolated. This effect is further reinforced by the border of the rectangular region comprising sites with low degree. *GossipPISB* leverage this clustering, so that the forwarding probability $p_{forw}^{PISB}(i)$ for small i is larger than p_{forw}^{PE} . It thus mitigates isolating sites in a cluster with low degree and achieve higher reliability than *GossipPE*.

Since the site isolation dependency is not included in our model, the results from our modeling overestimate the performance obtained by simulation in Figures 2(a) and 2(b). We see that such dependency in $\mathcal{G}(N, \rho)$ has a greater impact on *GossipPB* and *GossipPISB*, for which the reliability falls behind the predicted model, in regard with *GossipPINE* and *GossipPE*. The reason is that the message retransmitted by *GossipPB* or *GossipPISB* stays within a cluster few hops away from the source, when the retransmission probability is not high enough. In accordance with the percolation theory [9], *GossipPE* is never worse than *GossipPB* on any topology.

It is worth pointing out that in *GossipPINE* the probability for a message to be spread out of a cluster with high degree sites and into a cluster with low degree sites is larger than in *GossipPISB* and *GossipPE* (see Theorem 2). As expected, *GossipPINE* is accurately described by our model over both $\mathcal{T}(N, \rho)$ and $\mathcal{G}(N, \rho)$.

Latency: An efficient broadcasting algorithm aims at providing high reliability, while minimizing both message complexity and latency. We analyze the latency performance when the reliability reaches at least 85%. Figures 3(a) and 3(b) show the simulation results in $\mathcal{T}(N, \rho)$ and $\mathcal{G}(N, \rho)$ respectively.

Over all random topologies, after a given message complexity, latency does not decrease anymore, but converges towards the pure flooding approach (i.e., the shortest routes between the source and the other sites), and therefore, towards the minimum latency.

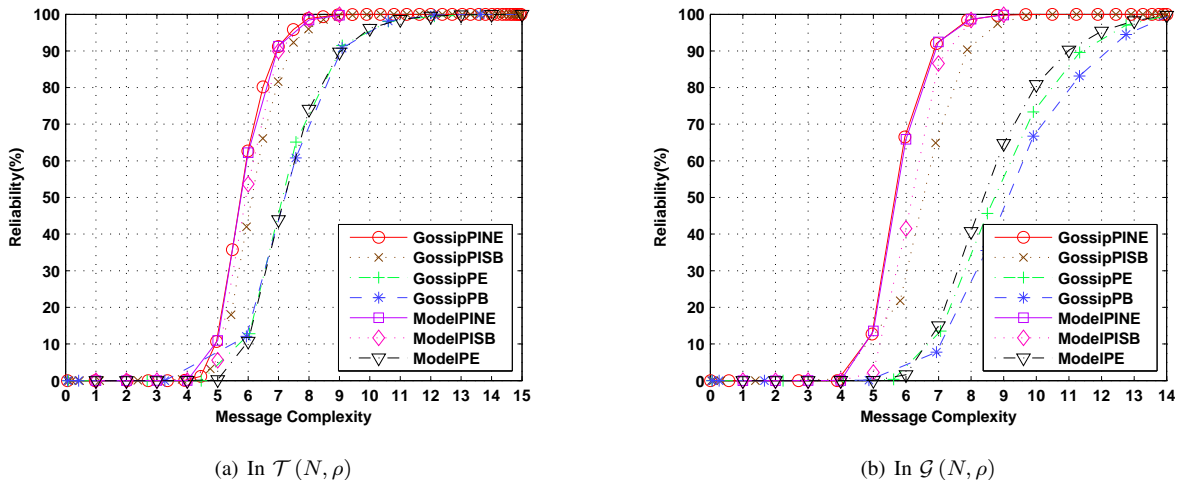


Figure 2: Reliability comparison of gossip algorithms

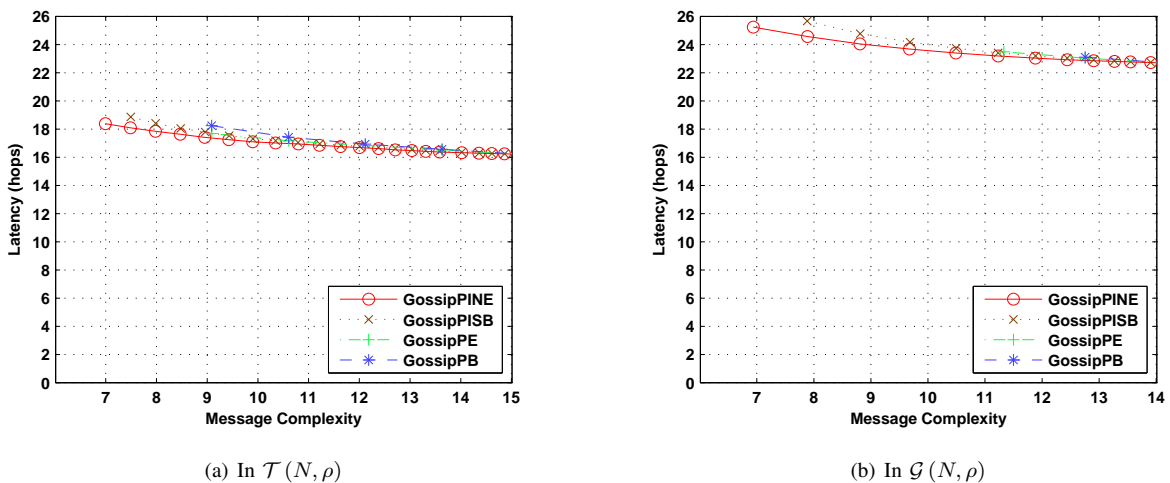


Figure 3: Latency comparison of gossip algorithms

The latency of our algorithm *GossipPINE* reaches a lower value in $\mathcal{T}(N, \rho)$ with the smallest message complexity amongst all gossip algorithms. A similar behavior of the latency curves is observed in $\mathcal{G}(N, \rho)$, except that the minimum latency value lies around 22 hops which is larger than in $\mathcal{G}(N, \rho)$, since the diameter of $\mathcal{G}(N, \rho)$ is greater than that of $\mathcal{T}(N, \rho)$.

VIII. RELATED WORK

The initial study on the probabilistic information broadcast in ad hoc networks was conducted in [10] and later implemented on DES-Testbed [4], which evaluates *GossipPB* and its variants. A bimodal behavior of the reliability has been heuristically analyzed with regard to the retransmission probability p_v . More precisely, from a threshold value of p_v , all the sites can receive almost all the messages. Otherwise, the message can rarely reach all sites in the system. In [24], such a threshold is given on the basis of percolation theory. The percolation driven flood routing algorithm proposed in

[28] can be seen as an advanced version of *GossipPB* in large-scale ad hoc networks. It gives an answer how to choose p_v to ensure high reliability. In Section VI, we model the reliability as a function of the p_v , which at the same time takes into account the properties of underlying networks, such as degree distribution. While assuming the site isolation independency in the end of the dissemination, our model accurately establishes such a relation in infinite random geometric graphs. Even in the graphs with border effect, reasonable estimation can be adaptively given by the corrective degree distribution. Furthermore, it explains the higher reliability obtained by our algorithm than the other gossip algorithms.

GossipPISB proposed in [6] tailors the retransmission probability to the local topology, where sites in sparse density area retransmit with high probability. We have shown that the sites around boundaries of the region are hardly infected when small message complexity is allowed. In [8], the authors model the reliability, and improves the protocol by adding a pull phase. But pull algorithms are difficult to carry out

[15]. Similarly, the authors in [2] distinguish all sites by four levels. The probability in each level is reversely proportional to the number of levels predefined in ad hoc network. Nonetheless, no theoretical analysis are proposed. The Smart Gossip protocol in [17] constructs local relationship trees in two-hop neighborhoods, which consist of a parent, children and siblings. Every parent decides on an optimal forwarding probability that is computed by its children under reliability and topology constraint. Maintenance of the relationship trees is required. Moreover, in [5], the authors specify forwarding probability of a site in ad-hoc networks as function of both its degree and the mean degree of its neighbors, while introducing a mechanism where if a site suspects that some of its neighbors have not received the message, it rebroadcasts the message regardless of the initial decision. The reliability is heuristically studied. In contrary, our algorithm is efficient and very simple to apply in random geometric networks, which is confirmed by both our model and simulation.

As explained in [12] that *GossipPE* is never worse than *GossipPB* in any topology, the directional antenna is applied to implement *GossipPE* in ad hoc network in [25], which shows a better performance than *GossipPB*. In comparison, our algorithm *GossipPINE* is robust against border effect that is a common characteristic in the realistic environment with long boundary.

Other probabilistic approaches include counter-based [21], distance-based [13], and location-based mechanisms [26]. In regard to *GossipPB*, variant protocols arm a time counter as shown in [21] for copy accumulations. Hop Counter Aided Broadcast (HCAB) protocol in [13] makes the sites, upon the first reception of a message, start a random timer and record the value of hop counter. The message will be relayed by the site if, when the timer expires, no message with a hop counter higher than the first was received. Implicitly, every site in HCAB attempts to know whether each relay is done by some other sites, hopefully covering (i.e., infecting) additional regions of the network. Another distance-based protocol is also proposed in [13], which is called Self-Adaptive Probability Broadcasting (SAPB) protocol. It stipulates that the probability of a site to relay a message depends on coverage (i.e., infection) contribution brought by this site. However, those works contain little theoretical evaluation of the schemes.

IX. CONCLUSION

In this article, we have proposed an efficient probabilistic broadcast algorithm and reliability model to compare probabilistic gossip algorithms in random geometric networks. Our model gives a reasonable estimation, and explains the best reliability obtained by our gossip algorithm *GossipPINE*, which is confirmed by our simulations. *GossipPINE* also shows desirable latency performance for high reliability. In particular, our algorithm has the best resilience to the border effect degrading the reliability.

As a near future work, the random mobility in the network will be evaluated and studied.

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