

Stochastic parameterization of geophysical flows through modelling under location uncertainty

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Stochastic parametrization of geophysical flows through modeling under location uncertainty

Valentin Resseguier,

Pierre Dérian, Etienne Mémin, Bertrand Chapron





Motivations

- Rigorously identified sudgrid dynamics effects
- Injecting likely small-scale dynamics
- Studying bifurcations and attractors



• Quantification of modeling errors



Ensemble forecasts and data assimilation

Contents

- Randomized dynamics
- SQG under Moderate Uncertainty
- Lorenz under location uncertainty

Randomized dynamics

Random equations

Random initial conditions



Underdispersive + need large ensemble

Arbitrary Gaussian forcing



Adding energy + wrong phase

• Averaging, homogenization



Assumptions and energy issues

 Adding white random velocity





$\frac{D\Theta}{Dt} = 0$

Advection of tracer Θ

$$\partial_t \Theta + w^* \cdot \nabla \Theta + \sigma \dot{B} \cdot \nabla \Theta = \nabla \cdot \left(\frac{1}{2}a \nabla \Theta\right)$$

$$\partial_t \Theta + \mathbf{w}^{\star} \cdot \nabla \Theta + \boldsymbol{\sigma} \dot{\boldsymbol{B}} \cdot \nabla \Theta = \nabla \cdot \left(\frac{1}{2} \boldsymbol{a} \nabla \Theta\right)$$

























SQG under Moderate Uncertainty

SQG MU

Code available online

$t = 17 \,\mathrm{days}$



Reference flow:

deterministic

SQG 512 x 512

$t = 17 \,\mathrm{days}$



Reference flow:

deterministic

SQG 512 x 512



One realization





One realization









Ensemble



Spectrum of the errors and its estimation at t=12 days





Ensemble



Spectrum of the errors and its estimation at t=12 days



Summary of QG models

- Better small scales
- Estimate position and amplitude of errors
- Extreme events
- Bifurcations



 under Strong Uncertainty: Simple 2D description of frontolysis/frontogenesis

> Code SQG MU: link from Fluminance website - V. Resseguier

Lorenz model under location uncertainty

Do large-scale (diffusive) models lead to over-representing "stable"-states in ensemble simulations?

$$\begin{aligned} & \text{Lorenz model(s)} \\ & \frac{\mathrm{d}X}{\mathrm{d}t} = \Pr\left(Y - X\right) - \frac{4}{2\Upsilon}X \\ & \mathrm{d}Y = \left[X(\rho - Z) - Y - \frac{4}{2\Upsilon}Y\right]\mathrm{d}t + \frac{\rho - Z}{\Upsilon^{1/2}}\mathrm{d}B_t \\ & \mathrm{d}Z = \left[XY - bZ - \frac{8}{2\Upsilon}bZ\right]\mathrm{d}t + \frac{Y}{\Upsilon^{1/2}}\mathrm{d}B_t \end{aligned}$$

- (usual) **deterministic** model ~ DNS, accurate but impossible to compute
- (deterministic) **diffusive** model ~ LES
- **stochastic** model under location uncertainty
 - ➡ behaviors of ensembles?



Short time behavior

Comparison ensemble ↔reference 3 metrics: minimum distance, bias, RMS distance





Short time behavior



16



Long time





Long time





Long time





100 initial conditions



100 initial conditions

Conclusion

Conclusion

- Random transport applicable to any dynamics
- Better small scales
- Efficient spreading of the ensemble
- Likely scenarios
- Exploration of the attractor

Thank you for your attention

Code SQG MU: link from Fluminance website - V. Resseguier

Drift correction

Drift correction





Bifurcations in SQG

tracked by SQG MU

Reference flow: deterministic SQG

512² versus 128²

Initial condition 1





Reference flow: deterministic SQG

512² versus 128²

Initial condition 1















SQG under Strong Uncertainty

SQG SU

Mesoscale divergence

Geostrophic balance

$$m{f} imes m{u} = -rac{1}{
ho_b} m{
abla} p' + rac{a}{2} \Delta m{u}$$

$$\bigtriangledown \left\{ oldsymbol{
abla} \cdot oldsymbol{u} \propto \Delta oldsymbol{
abla}^{oldsymbol{oldsymbol{\omega}}^{oldsymbol{oldsymbol{\omega}}} \cdot oldsymbol{u}
ight\}$$

Filtering of model outputs:

Gula, Jonathan, M. Jeroen Molemaker, and James C. McWilliams "Gulf Stream dynamics along the southeastern US seaboard." *Journal of Physical Oceanography* 45.3 (2015): 690-715.



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Spatial test



Spatial test



Spectral test





Long time: weak noise





Long time: weak noise





Long time: weak noise









Computing the visit rate

- Discrete covering of the Lorenz attractor (GAIO)
 → 611,550 cubic boxes of radius=0.15625
- For each ensemble, the visit rate:

 $\tau(T) = \frac{\#\{\text{ unique boxes visited by ensemble over } [0;T]\}}{\text{total } \# \text{ of boxes}}$

