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Closed Set Based Discovery of Association Rules

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Plan of the Presentation

- 1 Association rule framework
- 2 Existing algorithms
- 3 A-Close algorithm
- 4 Illustration
- 5 Experimental results
- 6 Conclusion
- 7 Present work

1 Association Rules

- Data mining context (dataset)
 - binary relation $\mathcal{R} \subseteq \mathcal{O} \times \mathcal{I}$
 - \mathcal{O} : finite set of objects (transactions)
 - \mathcal{I} : finite set of items (attributes)

OID	Items			
1	A	C	D	
2	B	C	E	
3	A	B	C	E
4	B	E		
5	A	B	C	E

Figure 1: The example data mining context \mathcal{D}

- Itemset (set of items) support
 - proportion of objects containing the itemset
$$support(BC) = \|\{2, 3, 5\}\|/5 = 3/5$$
- Association rules
 - implications between two itemsets
$$r : BC \rightarrow E \quad (support\%, confidence\%)$$
- Association rule support
 - support of the union of antecedent and consequent of the rule
$$support(r) = support(BCE) = \|\{2, 3, 5\}\|/5 = 3/5$$
- Association rule confidence
 - proportion of objects verifying the implication
$$confidence(r) = support(BCE)/support(BC) = 1$$
- Minimum support and confidence thresholds defined by the user

2 Existing Algorithms

- Problem decomposition
 1. determination of frequent itemsets
($support \geq minsupport$)
 2. generation of association rules using frequent itemsets
($confidence \geq minconfidence$)
- The problem of extracting association rules is reduced to the problem of discovering frequent itemsets
- Pruning subset lattice \mathcal{L}_I to extract frequent itemsets

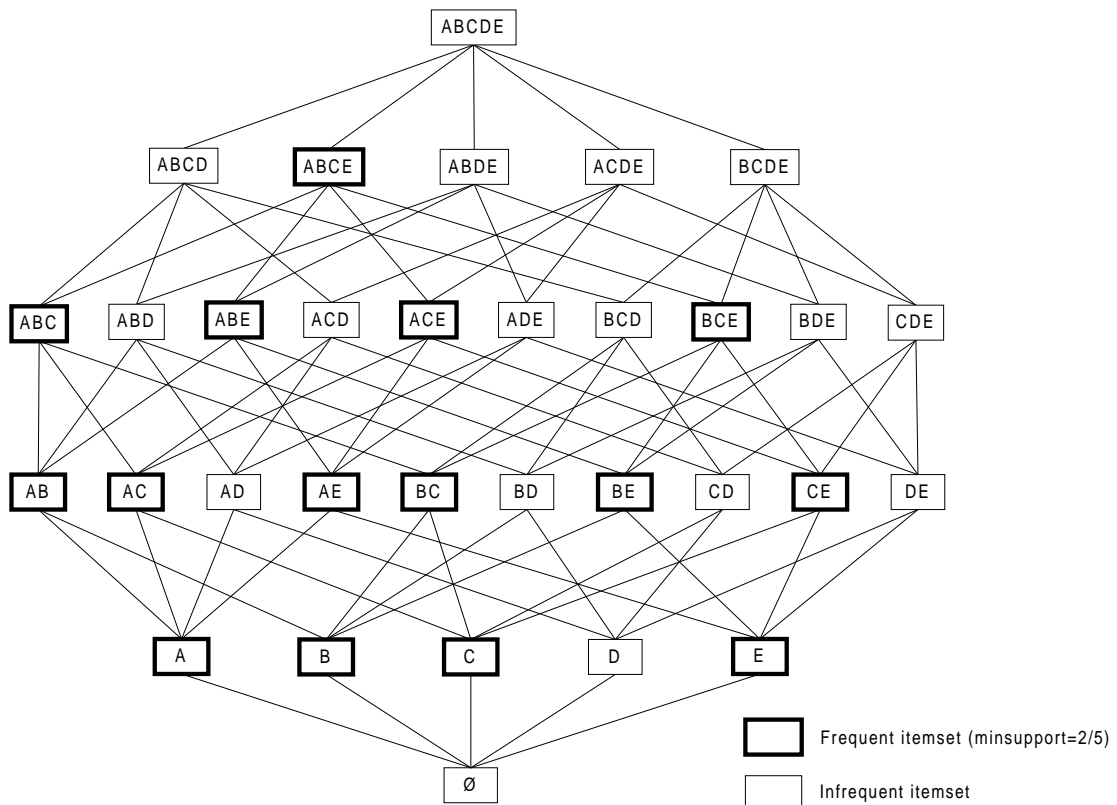


Figure 2: Subset lattice of \mathcal{D}

- Size is exponential $|\mathcal{L}_I| = 2^{|\mathcal{I}|}$

3 A-Close Algorithm

- Closure operator of the Galois connection of a binary relation
- Closed itemset: maximal set of items common to a set of objects
ex: BC is not closed since $Objects(BC) = 2, 3, 5$ but $Items(2, 3, 5) = BCE$
- Problem decomposition
 1. discovering frequent closed itemsets
 2. deriving frequent itemsets from frequent closed itemsets
 3. generating association rules using frequent itemsets
- The problem of extracting association rules is reduced to the problem of discovering frequent closed itemsets
- Closed itemset properties
 - i) all maximal frequent itemsets are maximal frequent closed itemsets
 - ii) the support of a non-closed itemset is equal to the support of its closure
 - iii) the maximal frequent closed itemsets characterise all frequent itemsets
- Pruning closed itemset lattice \mathcal{L}_C to extract frequent closed itemsets

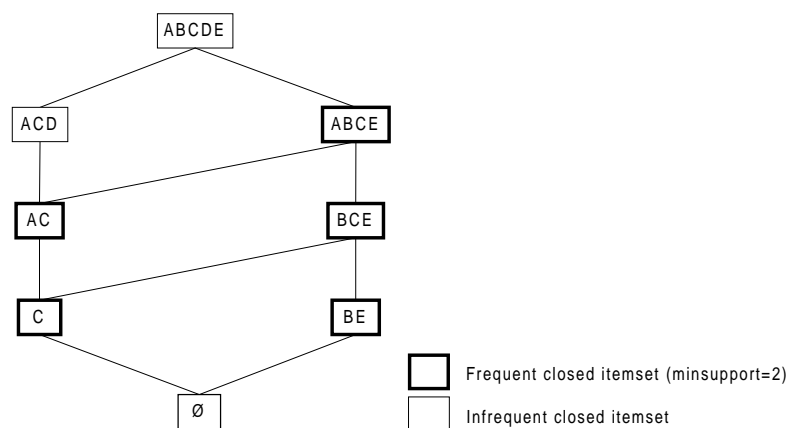


Figure 3: Closed itemset lattice of \mathcal{D}

- Determining minimal generator itemsets of all frequent closed itemsets
 - generators of a closed itemset: itemsets for which closure is the closed itemset
 - X is a minimal generator itemset if $\forall X' \subset X, support(X) \neq support(X')$
- Closure of an itemset is the intersection of all objects containing it
ex: $Closure(BC) = Intersect(2, 3, 5) = BCE$

Algorithm 1 A-Close frequent closed itemset discovery

1. $G_1 \leftarrow \{\text{frequent 1-itemsets}\};$ // scan \mathcal{D}
 2. **for** ($i \leftarrow 2; G_i.\text{generators} \neq ; i++$) **do**
 3. $G_i \leftarrow \text{join generators in } G_{i-1};$
 4. Test presence of subsets(G_i) in $G_{i-1};$
 5. Determine support(G_i); // scan \mathcal{D}
 6. Prune infrequent generators in G_i ;
 7. Prune non-minimal generators in G_i ; // level variable $\leftarrow i-1$
 8. **end**
 9. Determine closures($\cup G_i$); // scan \mathcal{D}
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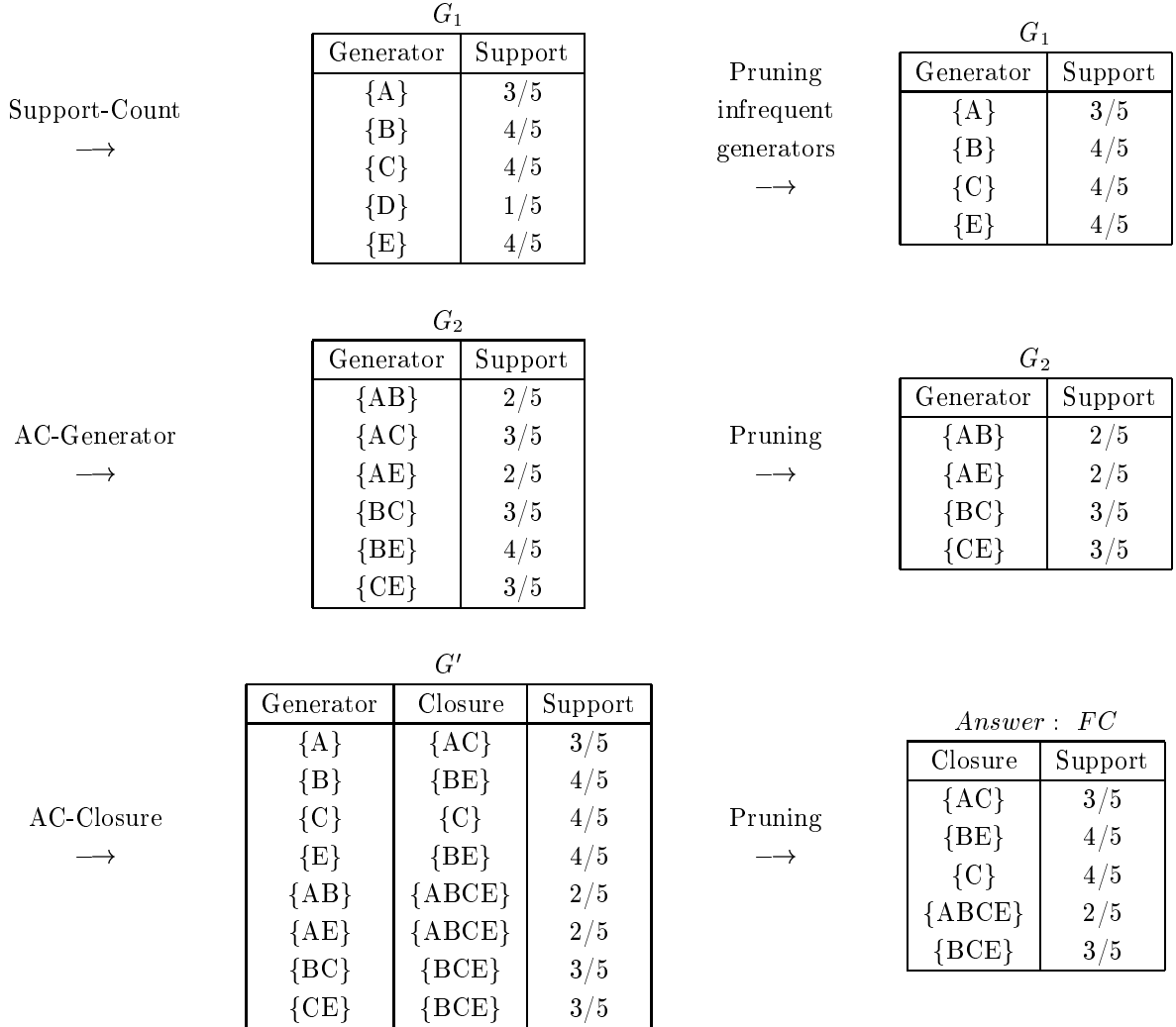


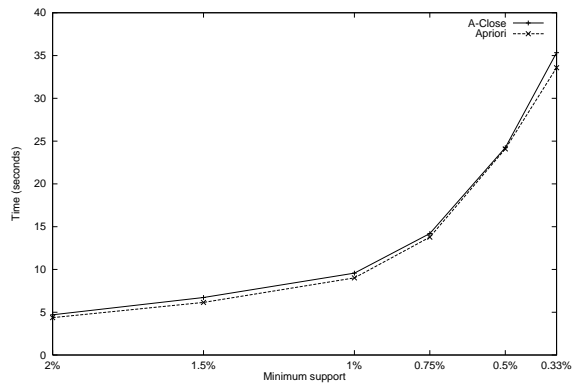
Figure 4: A-Close frequent closed itemset discovery in \mathcal{D} for $minsup = 2/5$ (40%)

4 Experimental Results

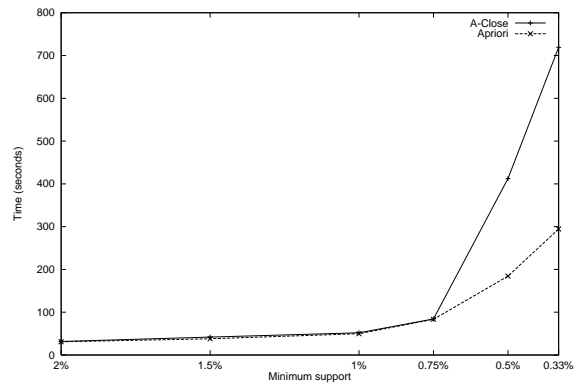
- Synthetic data: execution times
 - weakly correlated data: nearly all frequent itemsets are closed
 - additional time for A-Close in T20I6D100K (0.5%,0.33%): closure computations
- Census data: C20D10K
 - correlated data: few frequent itemsets are closed
 - closure mechanism allows to skip some iterations and consider less candidates
- Census data: C73D10K
 - differences between execution times can be measured in hours
 - maximal execution times: Apriori 14h, A-Close 1h15

5 Conclusion

- Correlated data
 - difficult cases: long execution times
 - few frequent itemsets are closed: A-Close is particularly efficient
 - statistical data, medical data, text data, etc.
- Weakly correlated data
 - nearly all frequent itemsets are closed
 - acceptable execution times
 - synthetic data

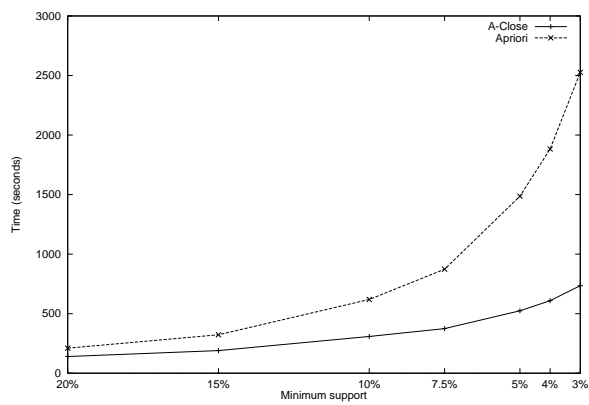


Execution times on T10I4D100K

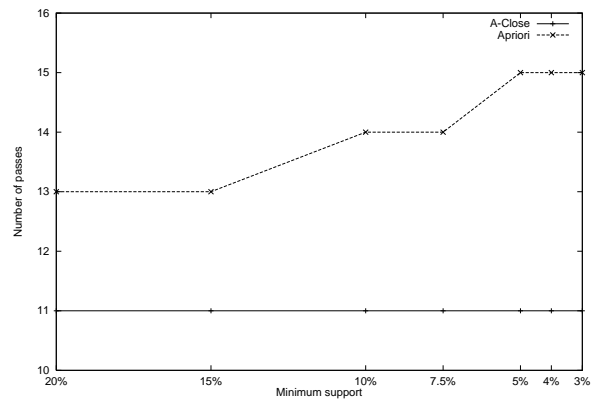


Execution times on T20I6D100K

Figure 5: Performance of Apriori and Close on synthetic data

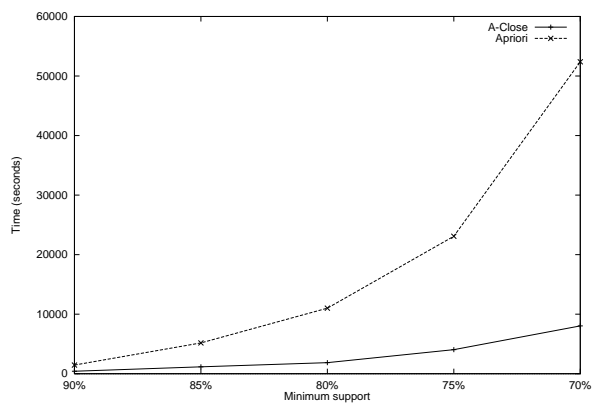


Execution times

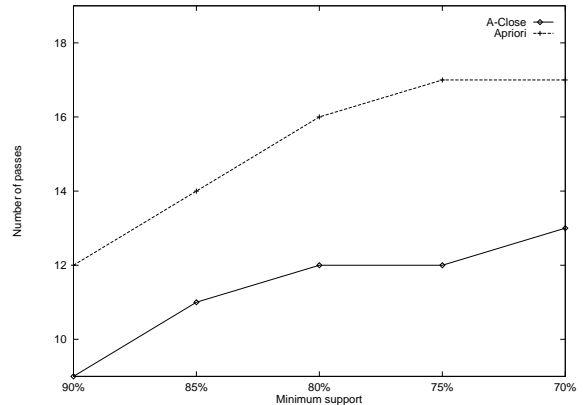


Number of database passes

Figure 6: Performance of Apriori and Close on census data C20D10K



Execution times



Number of database passes

Figure 7: Performance of Apriori and Close on census data C73D10K

6 Present Work

- Problem of the understandability and usefulness of association rules extracted
- Discovering small covers for association rules
 - small informative and structural cover for exact association rules
 - small informative cover for approximate association rules
 - small structural cover for approximate association rules

Dataset	Minimum support	Minimum confidence	Total rules	Informative cover	Structural cover
T10I4D100K	0.5%	90%	16,260	3,511	916
C73D10K	90%	90%	2,053,896	4,104	941
Mushrooms	50%	50%	1,248	87	44

Figure 8: Preliminary experimental results

References

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- [3] N. Pasquier, Y. Bastide, R. Taouil, and L. Lakhal. Discovering frequent closed itemsets for association rules. *Proceedings of the 7th ICDT Int'l Conference on Database Theory*, pages 398–416, January 1999.