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Towards an Efficient Discovery of Topological Representative Subgraphs

Wajdi Dhifli ^{1,2}, Mohamed Moussaoui ³, Engelbert Mephu Nguifo ^{1,2} and Rabie Saidi ⁴

¹ CNRS, UMR 6158, LIMOS, F-63173 Aubiere, France.

² Clermont University, Blaise Pascal University, LIMOS, BP 10448, F-63000 Clermont-Ferrand, France.

³ Department of Computer Science - FSEGJ - University of Jendouba, Jendouba 8100, Tunisia.

⁴ European Bioinformatics Institute, Hinxton, Cambridge, CB10 1SD, United Kingdom.

{dhifli,mephu}@isima.fr - rsaidi@ebi.ac.uk.

Résumé

La sélection de motifs basée sur la similarité structurelle exacte ou approximative est un moyen de réduire le nombre élevé des sous-graphes fréquents. Cependant, les stratégies actuelles de similarité structurelle ne sont pas efficaces dans beaucoup de contextes réels. En outre, la nature combinatoire des graphes rend l'isomorphisme exact ou approximatif très coûteux. Dans ce papier, nous proposons une approche qui permet de sélectionner un sous-ensemble de sous-graphes topologiques représentatifs parmi les fréquents. L'approche proposée surmonte le coûteux test d'isomorphisme exact ou approximatif en mesurant la similarité structurelle globale en se basant sur un ensemble d'attributs topologiques considérés. Elle permet aussi de détecter des similaritées structurelles cachées (tels que la densité, le diamètre, etc.) qui ne sont pas considérées par les approches existantes. En outre, l'approche proposée est flexible et peut être facilement étendue avec des attributs définis par l'utilisateur selon l'application. Les analyses expérimentales sur des bases de graphes réelles et synthétiques montrent l'efficacité de notre approche.

Mots Clef

Sélection de motifs, sous-graphes topologiques représentatifs, sous-graphes fréquents, bases de graphes.

Abstract

Feature selection based on exact or approximate structural similarity is a way to reduce the high number of frequent subgraphs. However, current structural similarity strategies are not efficient in many real-world cases. Besides, the combinatorial nature of graphs makes performing exact or approximate isomorphism very costly. In this paper, we propose an approach that mines a subset of topological representative subgraphs among frequent ones. The proposed approach overcomes the costly exact or approximate isomorphism by measuring the overall structural similarity based on a considered set of topological attributes. It also allows detecting hidden structural similarities (such as density, diameter, etc.) that existing approaches ignore. In addition, the proposed approach is flexible and can be easily extended with any user defined attributes depending on the application. Empirical studies on real and synthetic graph datasets show the efficiency of our approach.

Keywords

Feature selection, topological representative subgraphs, frequent subgraphs, graph databases.

1 Introduction

With the emergence of graph databases, the task of frequent subgraph discovery has been extensively addressed. Many approaches have been proposed in the literature allowing the extraction of frequent subgraphs in an efficient way. Yet, the number of discovered frequent subgraphs is extremely high which causes *information overload* that may hinder or even makes unfeasible further exploration.

Feature selection is a way to tackle this information overload problem. As structural similarity represents one major cause of redundancy in frequent subgraphs, many works have been proposed for subgraph selection based on exact or approximate structural similarity [1, 2, 3, 4]. Some works have been proposed based on closed and maximal subgraphs such as [1, 2, 6, 5]. Although the set of closed or maximal subgraphs is much smaller than that of frequent ones, the number of subgraphs is still very high. In some applications, slight differences between subgraphs do not matters. Yet, in real-world cases very similar subgraphs sometimes slightly differ in structure. Exact structural isomorphism does not help to overcome this issue.

Many works have been proposed for subgraph selection based on approximate structural similarity. In [3], authors proposed an approach for subgraphs extraction and selection. For selection, the structural similarity between two subgraphs is measured by how much does their maximum common subgraph represents from their overall structure. A very close work is [4], where authors proposed an approach for mining a set of structural representative subgraphs among the frequent ones. They adopted a two-step approach that is based on approximate structural similarity on micro and macro sides. In the first step, they consider a tolerance threshold to summarize approximately isomorphic subgraphs into one representative. In the second step, they collapse multiple structurally similar subgraphs into one representative using a clustering algorithm.

Existing selections approaches, that are based on exact or approximate structural similarity, look into every single detail and test the structural similarity by establishing a matching between subgraphs. This similarity detection strategy is not efficient in many real-world applications. On one hand, because computing every possible matching between subgraphs is very costly. On the other hand, exact structural similarity does not allow detecting similar yet slightly different subgraphs, and approximate structural similarity has the problem of threshold setting. Since a tight threshold will prevent detecting similar subgraphs that slightly differ in structure beyond the tolerance threshold. In contrast, a loose threshold will hinder the soundness of the selection because of false positives. This rises the need for a different way to consider the structural similarity such that both close and distant structural similarities would be detected with respect to the soundness of results.

In order to overcome these drawbacks, we propose a novel approach that mines a subset of topological representative subgraphs among frequent ones. At a glance, our approach involves two steps. In the first step, each subgraph is encoded into a topological description-vector containing the corresponding values for a set of topological attributes. In the second step, subgraphs with similar topological descriptions are clustered and the central subgraph in each cluster is considered as the representative delegate. Our approach overcomes the costly exact or approximate isomorphisms and allows detecting hidden similarities between subgraphs (such as spectral radius or closeness centrality) that existing structural similarity approaches ignore. Besides, It can be easily extended by enabling the user to target a specific set of topological attributes depending on how important each one is to the application.

Considering topological properties was inspired by works like [8, 9, 10] where authors showed the efficiency of topological attributes in describing graph data. For instance, in [8], authors proposed a classification framework based on the assumption that graphs belonging to the same class have similar topological descriptions. Our approach is based on similar assumption and consider that structurally similar subgraphs should have similar topological properties such that even a slight difference does not affect the overall topological similarity. Besides, in some applications, the user may be only interested in some specific structural properties. Considering exact or approximate structural similarity approaches does not allow this specificity.

The remainder of the paper is organized as follows. Section 2 presents and defines the preliminary concepts as well as the main algorithm of our approach. Section 3 describes the datasets and the experimental settings. In Section 4, we present the obtained results and the discussion.

2 Material and methods

In this section, we present the fundamental definitions and the formal problem statement of the proposed approach.

2.1 Preliminaries

Definition 1. (*Graphs and graph databases*) Let \mathcal{G} be a database of connected graphs. Each graph $G = (V, E, \Sigma, L)$ of \mathcal{G} is given as a set of nodes V and edges E. The nodes are labeled within an alphabet Σ and L is the label function. |V| and |E| represent the number of nodes and edges.

Definition 2. (Subgraph isomorphism) A labeled graph G is subgraph of another one G', denoted by $G \subseteq G'$, if there exists an injective function $f : V \to V'$, such that :

-
$$\forall u, v \in V : \forall \{u, v\} \in E \rightarrow \{f(u), f(v)\} \in E'$$

$$- \forall v \in V : L(v) = L'(f(v))$$

- $\forall \{u, v\} \in E(G) : L\{u, v\} = L'\{f(u), f(v)\}$

where L and L' are the label functions of G and G'. Under these conditions, f is called an embedding of G in G', G is a subgraph of G', and G' is a supergraph of G.

Definition 3. (Frequent subgraph) Given a subgraph g, a graph database \mathcal{G} , and a minimum frequency threshold τ , let \mathcal{G}_g be the set of graphs where g appears (i.e. g has a subgraph isomorphism in each graph in \mathcal{G}_g). The subgraph g is considered as frequent if $support(g) = \frac{|\mathcal{G}_g|}{|\mathcal{G}|} \geq \tau$.

Problem Statement : Even though the existing approaches for subgraph selection greatly enhanced the selection process, the number of selected subgraphs is still high. Yet, we want to show as few subgraphs as possible so that the user's reviewing efforts are minimized. The general framework of our selection strategy is as follows. Given a set of frequent subgraphs Ω and an integer $k \in [1..|\Omega|]$, we want to select up to k representative subgraphs $\Omega_k \subseteq \Omega$ such that each frequent subgraph $g \in \Omega$ has one representative subgraphdelegate $g^* \in \Omega_k$, and each representative subgraph is the closest one to all the subgraph it represents.

2.2 Naïve approach

A fundamental part in our selection approach is the graph encoding which consists in transforming each subgraph into a different format that is accepted by the clustering algorithm. A very common way of encoding in the literature (for instance [8] and [12]) is to transform the input subgraphs into a context-matrix where each subgraph is represented by a binary vector denoting by 1 or 0 the presence or the absence of the subgraph in each graph in the database. After that, the context-matrix is considered as input for clustering. We term this method *naïve approach* and we consider it for comparison.

2.3 Topological representative subgraph selection

The main idea of our approach, termed *TRS* (for Topological **R**epresentative **S**ubgraph), is based on the assumption that structurally similar subgraphs should have

similar topological properties such that even a slight difference in the structure does not affect the overall similarity. Accordingly, we adopt a two-step selection approach. In the first step, we encode each subgraph into a topological description-vector based on a set of topological attributes. In the second step, we cluster the topological descriptionvectors in order to select one representative delegate from each set of topologically similar subgraphs.

Topological attributes. We select a set of topological attributes from the literature [8] that are interesting and efficient in describing connected graphs. In the following, we list and define the considered attributes :

- 1. Number of nodes : The total number of nodes in the graph, also called the graph order |V|.
- 2. Number of edges : The total number of edges in the graph, also called the graph size |E|.
- 3. Average degree : The degree of a node u, denoted deg(u), represents the number of nodes adjacent to u. The average degree of a graph G is the average value of the degrees of all nodes in G. Formally : $deg(G) = \frac{1}{n} \sum_{i=1}^{n} deg(u_i)$ where $deg(u_i)$ is the degree of the node u_i and n is the number of nodes in G.
- 4. **Density** : The density of a graph G = (V, E) measures how many edges are in E compared to the maximum possible number of edges between the nodes in V. Formally : $den(G) = \frac{2|E|}{(|V|*(|V|-1))}$.
- 5. Average clustering coefficient : The clustering coefficient of a node u, denoted by c(u), measures how complete the neighborhood of u is *i.e.* $c(u) = \frac{2e_u}{k_u(k_u-1))}$ where k_u is the number of neighbors of u and e_u is the number of connected pairs of neighbors. The average clustering coefficient of an entire graph G having n nodes, is given as the average value over all the nodes in G. Formally : $C(G) = \frac{1}{n} \sum_{i=1}^{n} c(u_i)$.
- 6. Average effective eccentricity : For a node u, the effective eccentricity represents the maximum length of the shortest paths between u and every other node v in G, i.e., e(u) = max{d(u,v) : v ∈ V}. The average effective eccentricity is defined as Ae(G) = 1/n ∑_{i=1}ⁿ e(u_i), where n is the number of nodes of G.
- 7. Effective diameter : The effective diameter represents the maximum value of effective eccentricity over all nodes in the graph G, *i.e.*, $diam(G) = max\{e(u) \mid u \in V\}$ where e(u) represents the effective eccentricity of u as defined above.
- 8. Effective radius : The effective radius represents the minimum value of effective eccentricity over all nodes in the graph G, *i.e.*, $rad(G) = min\{e(u) \mid u \in V\}$ where e(u) represents the effective eccentricity of u.
- 9. Closeness centrality : It measures how fast information spreads from a given node to other reachable nodes in the graph. For a node u, it represents the reciprocal of the average shortest path length between

u and every other reachable node in the graph, *i.e.*, $C_c(u) = \frac{n-1}{\sum_{v \in \{V \setminus u\}} d(u,v)}$ where d(u,v) is the length of the shortest path between the nodes *u* and *v*. For a graph *G*, we consider the average value of closeness centrality of all the nodes, *i.e.*, $C_c(G) = \frac{1}{n} \sum_{i=1}^n u_i$.

- 10. **Percentage of central nodes** : Here, we compute the ratio of the number of central nodes from the number of nodes in the graph. A node u is considered as central point if the value of its eccentricity is equal to the effective radius of the graph, *i.e.*, e(u) = rad(G).
- 11. Percentage of end points : It represents the ratio of the number of end points from the total number of nodes of the graph. A node u is considered as end point if deg(u) = 1.
- 12. Number of distinct eigenvalues : Any graph G can be represented by an adjacency matrix A. Here, we count the number of distinct eigenvalues of A.
- 13. Spectral radius : Let A be the adjacency matrix of the graph G and λ₁, λ₂, ..., λ_m be the set of eigenvalues of A. The spectral radius of G, denoted ρ(G), represents the largest magnitude eigenvalue, *i.e.*, ρ(G) = max(| λ_i |) where i ∈ {1,..,m}.
- 14. **Second largest eigenvalue :** The value of the second largest eigenvalue of the adjacency matrix.
- 15. Energy : The energy of an adjacency matrix A of a graph G is defined as the squared sum of the eigenvalues of A. Formally : $E(G) = \sum_{i=1}^{n} \lambda_i^2$.
- 16. Neighborhood impurity : The impurity degree of a node u belonging to a graph G, having a label L(u) and a neighborhood (adjacent nodes) N(u), is defined as $ImpurityDeg(u) = | L(v) : v \in N(u), L(u) \neq L(v) |$. The neighborhood impurity of a graph G represents the average impurity degree over all nodes with positive impurity.
- 17. Link impurity : An edge (u, v) is considered to be impure if $L(u) \neq L(v)$. The link impurity of a graph *G* with *k* edges is defined as : $\frac{|(u,v)\in E:L(u)\neq L(v)|}{k}$.

As efficiency and scalability remain big challenges for graph mining algorithms, the proposed description is unified which helps to overcome both challenges. On one hand, these attributes are an efficient description that allows revealing hidden topological similarities that exact and approximate structural isomorphism do not consider. On the other hand, considering a fixed number of descriptors guarantee that the encoded vectors would be of a fixed size no matter what the number of graphs in the database is.

K-medoids clustering. Here, we discuss the second part of our selection approach which is the clustering step. We use *k-Medoids* [11] which is a well known clustering algorithm that is widely used in unsupervised learning. It takes as input a set of objects Ω and a number of clusters *k*, and gives as output the *k* clusters' centers (called *medoids*). To do so, k-Medoids uses these definitions :

Definition 4. (*Pairwise distance between objects*) Given two objects O_1 and O_2 correspondingly described by the vectors X and Y, the distance between them, denoted $d(O_1, O_2)$, is defined as follows :

$$d(O_1, O_2) = \sum_{i=1}^{|X|} |x_i - y_i|$$

Definition 5. (Global distance between objects) Given a set of objects Ω , the total distance between an object O and all the other ones in Ω is defined by :

$$D_O = \sum_{\forall O_i \in \Omega \setminus O} d(O, O_i)$$

Definition 6. (*Cluster medoid*) An object O^* is said to be cluster's medoid (the most centrally located object of the cluster), if it has the minimum sum of distances to all the other objects O_i within the cluster C. Formally :

$$D_{O^*} = min_{O_i \in C}(D_{O_i})$$

The general algorithm of k-Medoids is described in Algorithm 1. First, it randomly selects k objects from Ω to be the medoids, *i.e.* Ω^* . Then, it assigns each non-selected object to the cluster of the nearest medoid. After that, it swaps the k medoid objects with other non-medoid objects aiming to minimize the overall distance. $D(\Omega^*)$ is the total distance before the swap and $D(\Omega'_k)$ is the total distance after the swap. If the cost of the swap ($C = D(\Omega'_k) - D(\Omega^*)$) is strictly negative then the swap is considered as beneficial, otherwise it is ignored. The assignment and swap steps are iteratively performed until no change or until a user-defined maximum number of iteration is reached. Many implementations of k-Medoids have been proposed in the literature. We use CLARANS [11] since it was shown that it is efficient for large-scale data clustering.

Algorithme 1: K-MEDOIDS

Data : Set of objects Ω , number of clusters k, maximum number of iterations max_{iter} **Result** : Set of medoids $\Omega^* = \{O_1, O_2, ..., O_k\}$ 1 begin $\Omega^* \leftarrow \Omega_k$: start with K objects randomly selected 2 from Ω ; repeat 3 Assign each one of the non-selected objects to the 4 cluster having the most similar medoid; Calculate the cost $C_i = (D(\Omega'_k) - D(\Omega^*))$ for 5 each swap of one medoid with another object; if $C_i < 0$ then 6 $\Omega^* \leftarrow \Omega'_k;$ 7 $nb_{iter} = nb_{iter} + 1;$ 8 **until** (no change) or $(nb_{iter} \ge max_{iter})$;

3 Experimental analysis

3.1 Datasets

To experimentally evaluate our approach, we use different graph datasets : protein 3D-structures and chemical com-

pounds. Table 1 summarizes the characteristics of the datasets : dataset, |G|, Avg.|V|, Avg.|E| and $|\Omega|$ correspond respectively to the name of the corresponding protein family or chemical compound dataset, number of graph, average number of nodes, average number of edges and number of frequent subgraphs obtained from each dataset.

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Dataset	 G	Avg. V	Avg. E	$ \Omega $	
G-proteins	66	246	971	114792	
C1 set domains	76	238	928	258371	
AIDS antiviral screen	43850	28	30	6749	

The first two datasets were previously used in [12]. Both datasets will be used to evaluate the quality of the selected subgraphs. Each dataset is equally divided between positive and negative samples. Positive proteins are sampled from a selected protein family, namely G-proteins and C1 set domains, whereas negative proteins are randomly sampled from the Protein Data Bank [13]. The last dataset contains the activity test information of 43850 chemical compounds. This dataset was previously used in many studies such as [4] and is publicly available on the website of the Developmental Therapeutics Program¹.

3.2 Protocol and settings

Graph building : For chemical compounds, each atom is represented by a node and labeled with the atom type. An edge exists between two nodes if there exists a chemical bond between their corresponding atoms. For protein 3Dstructures, each protein is parsed into a graph of amino acids. Each node represents an amino acid residue and is labeled with its amino acid type. Two nodes u and v are linked by an edge if the euclidean distance between their two C_{α} atoms is below a threshold distance δ . We use $\delta = 7$ Å. Frequent subgraph mining : We use the state-of-the-art method gSpan [14] to find frequent subgraphs in each dataset. We tried different minimum frequency threshold in order to obtain a reasonable number of frequent subgraphs from each dataset. The retained minimum frequency threshold are 30% for G-proteins and C1 set domains, and 5% for AIDS antiviral screen dataset.

Representative subgraph selection : Both selection methods (naïve approach and TRS) were implemented in R. **Subgraph encoding :** To measure the quality of subgraphs, each one of them is encoded into a binary vector by denoting 1 or 0, the presence or the absence of the subgraph in each graph in the dataset. The quality of the selected subgraphs is measured over their encoding vectors.

4 Results and discussion

4.1 Empirical Results

As previously mentioned, we first evaluate our approach using the classification datasets G-proteins and C1 set do-

^{1.} http://dtp.nci.nih.gov/docs/aids/aids_data.html

mains. We measure the quality of the selected subgraphs using the information gain which is one of the most popular interestingness measures in data mining. The information gain is measured separately for each subgraph in each set in order to measure how each representative is informative for the considered task (*i.e.* classifying the two protein datasets). The average value of information gain is computed for all the frequent subgraphs then for the representative subgraphs selected by TRS and those selected by the naïve approach using different number of representatives. The average information gain value obtained with all the frequent subgraphs is considered as standard value for comparison such that a good set of representatives should be at least as informative as the whole initial set of all frequent subgraphs. Table 2 shows the obtained results.

TABLE 2 – Comparison of average information gain of the topological representative subgraphs (TRS) with those selected by the naïve approach (NA) and the initial set of all frequent subgraphs (FSG).

(oteins	C1 set domains	
FSG	0.216		0.148	
#representatives	NA	TRS	NA	TRS
50	0.104	0.324	0.068	0.254
100	0.092	0.342	0.061	0.285
200	0.096	0.343	0.044	0.273
300	0.097	0.347	0.058	0.267
400	0.094	0.339	0.051	0.276
500	0.090	0.348	0.052	0.269
600	0.096	0.340	0.054	0.267
700	0.097	0.343	0.055	0.272
800	0.098	0.352	0.054	0.274
900	0.094	0.358	0.054	0.276
1000	0.094	0.353	0.056	0.276
Average	$0.095^{+0.008}_{-0.005}$	$0.344^{+0.013}_{-0.020}$	$0.055^{+0.012}_{-0.011}$	$0.271^{+0.01}_{-0.01}$

Table 2 shows that TRS is able to select a subset of subgraphs that are more informative than those selected by the naïve approach and the initial frequent subgraphs. Whereas, the quality of the subsets of representative subgraphs selected by the naïve approach did not even reach the information gain value of the whole set of frequent subgraphs. Both previous interpretations goes with all the used numbers of representatives. This proves the reliability of our selection approach and shows that using the topological attributes for description is more efficient than using the occurrence information. It enables k-medoids to better detects similarity relations between subgraphs and thus to select a subset of representatives that are most informative.

4.2 **Runtime analysis**

In this section, we study the runtime of our algorithm compared to that of the naïve approach.

Scalability to higher number of clusters. We study the effect of varying the number of clusters k on the runtime of clustering for both TRS and the naïve approach. We select the representative subgraphs among the frequent ones previously extracted from the AIDS antiviral screen dataset. Figure 1 illustrates the evolution of runtime using dif-

ferent values of k ranging from 200 to 800 with a step-size of 200. Figure 1 shows a huge difference in runtime bet-

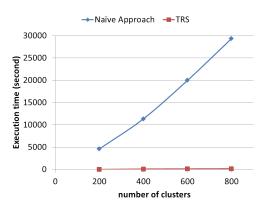


FIGURE 1 – Runtime of clustering for TRS and naïve approach with different number of clusters (k).

ween the two approaches. In fact, for 200 clusters, the naïve approach consumed more than one and half hour to finish the clustering, whereas TRS needed only few seconds. This difference becomes much bigger with higher values of k. As the number of clusters increases, the runtime of the naïve approach considerably increases as well. Yet, the clustering time in TRS did not increase significantly and almost stays steady with higher values of k. Since the clustering is almost polynomial and considers each possible pair of subgraphs for comparison, the smaller the description of the subgraphs is, the faster the clustering would be. Consequently, the huge gain in runtime is basically due to the small and fixed size of the topological description-vectors used in TRS compared to the context description-vectors in the naïve approach.

Scalability to higher number of subgraphs. Here, we study the effect of varying the number of frequent subgraphs on clustering runtime for both TRS and the naïve approach. We select the representative subgraphs among different sets of frequent subgraphs ranging from 10000 to 100000 with a step size of 10000. The input subgraphs were randomly selected among the frequent subgraphs previously extracted from the C1 set domains dataset. Figure 2 illustrates the evolution of runtime with higher number of subgraphs, for 100 clusters. As shown in the Figure, TRS takes only few seconds to select the representative subgraphs, whereas, the naïve approach takes clearly much more time. Increasing the number of subgraphs does no affect the runtime of TRS as much as it does with the naïve approach. This shows that TRS is more scalable than the naïve approach to higher numbers of subgraphs.

Scalability to higher number of graphs. In real-world applications, the size of databases is usually very high. We study the effect of varying the number of graphs on the runtime of both TRS and the naïve approach. We fix the number of subgraphs to 10000, and we synthetically manipulate the list of occurrences of each frequent subgraph and

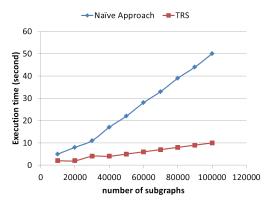


FIGURE 2 – Runtime of clustering for TRS and naïve approach to select 100 representatives among different numbers of subgraphs.

replace it by a random list of random occurrences between 0 and a considered number of graphs. The considered numbers of graphs are between 1000 and 10000, with a step size of 1000. Figure 3 illustrates the evolution of runtime with higher number of graphs for 100 clusters.

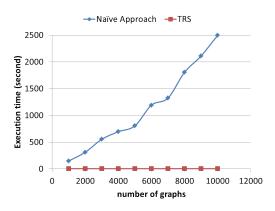


FIGURE 3 – Runtime of clustering for TRS and naïve approach to select 100 representatives among 10000 subgraphs whith variation of the number of graphs.

As the naïve approach uses the occurrence information to construct the context description-vectors, this makes it highly affected by the increasing of the size of the database. Figure 3 shows that the runtime of the naïve approach increases considerably with higher numbers of graphs. Whereas, the runtime of TRS is only few seconds and remains stable no matter what the size of the database is. This shows that TRS is scalable and more robust in real-world applications that usually deals with huge amounts of data.

5 Conclusion

We proposed a novel approach that mines a subset of topological representative subgraphs among frequent ones. Instead of exact or approximate structural similarity our approach follows a more meaningful selection strategy, that helps on both selecting a subset of topologically irredundant and informative subgraph-delegates, and detecting hidden similarities between subgraphs that current selection approaches ignore. This approach can be easily extended using any user defined attribute. Besides graph databases, it can also handle other scenarios such as subgraph selection in single graph. Empirical studies on real and synthetic graph datasets showed that our approach is fast and allows selecting informative subgraphs. In many application, the user may not be able to define a specific number of clusters. A promising future direction could be to remove the k constraint. This can be done using a parameter free clustering algorithm such as Medoids-shifts [15]. In order to extend our work to supervised classification, we also plan to compare our approach with other approaches based on structural similarity such as treelets [17, 16]. We will study how to combine this approach with a semantical based one as described in [7].

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