

# Thermal models of dyke intrusion during development of continent–ocean transition

Katherine A. Daniels, I. D. Bastow, D. Keir, R.S.J. Sparks, Thierry Menand

## ▶ To cite this version:

Katherine A. Daniels, I. D. Bastow, D. Keir, R.S.J. Sparks, Thierry Menand. Thermal models of dyke intrusion during development of continent–ocean transition. Earth and Planetary Science Letters, Elsevier, 2014, 385, pp.145-153. <10.1016/j.epsl.2013.09.018>. <hal-01131788>

## HAL Id: hal-01131788 https://hal.archives-ouvertes.fr/hal-01131788

Submitted on 17 Mar 2015  $\,$ 

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

1	Thermal models of dyke intrusion during development of Continent-
2	Ocean Transition
3	Daniels, K.A. <sup>1</sup> *, Bastow, I.D. <sup>2</sup> , Keir, D. <sup>3</sup> , Sparks, R.S.J. <sup>1</sup> and Menand, T. <sup>4,5,6</sup>
4	<sup>1</sup> School of Earth Sciences, University of Bristol, Wills Memorial Building, Queen's Road,
5	Bristol, BS8 1RJ, U.K.
6	<sup>2</sup> Department of Earth Science and Engineering, Imperial College London, Exhibition Road,
7	London, SW7 2AZ, U.K.
8	<sup>3</sup> National Oceanography Centre Southampton, University of Southampton, European Way,
9	Southampton, SO14 3ZH, U.K.
10	<sup>4</sup> Clermont Université, Université Blaise Pascal, Laboratoire Magmas et Volcans, BP 10448,
11	F-63000, Clermont-Ferrand, France.
12	<sup>5</sup> CNRS, UMR 6524, LMV, F-63038 Clermont-Ferrand, France.
13	<sup>6</sup> IRD, R 163, LMV, F-63038 Clermont-Ferrand, France.
14	*Present address: Department of Earth Sciences, University of Cambridge, Downing Street,
15	Cambridge, CB2 3EQ, U.K.
16	
17	Email addresses: kad43@cam.ac.uk; I.Bastow@imperial.ac.uk; D.Keir@soton.ac.uk;
18	Steve.Sparks@bristol.ac.uk; T.Menand@opgc.univ-bpclermont.fr;
19	Keywords: Dyke intrusion; Magmatic extension; Continental rifting; Heat-flow; Thermal
20	modelling.
21	
22	Abstract

- 23 A consensus has emerged in recent years from a variety of geoscientific disciplines that
- 24 extension during continental rifting is achieved only partly by plate stretching: dyke intrusion
- 25 also plays an important role. Magma intrusion can accommodate extension at lower yield

26 stresses than are required to extend thick, strong, unmodified continental lithosphere 27 mechanically, thereby aiding the breakup process. Dyke intrusion is also expected to heat 28 and thereby weaken the plate, but the spatial extent of heating and the effect of different 29 rates of magmatic extension on the timescales over which heating occurs are poorly 30 understood. To address this issue, a numerical solution to the heat flow equation is 31 developed here to quantify the thermal effects of dyke intrusion on the continental crust 32 during rifting. The thermal models are benchmarked against a priori constraints on crustal 33 structure and dyke intrusion episodes in Ethiopia. Finite difference models demonstrate that 34 magmatic extension rate exerts a first order control on the crustal thermal structure. Once 35 dyke intrusion supersedes faulting and stretching as the principal extensional mechanism 36 the crust will heat and weaken rapidly (less than 1 Ma).

37 In the Main Ethiopian Rift (MER), the majority of present-day extension is focused on ~20 38 km-wide Quaternary-Recent axial magmatic segments that are mostly seismogenic to mid-39 crustal depths and show P-wave seismic velocities characteristic of heavily intruded 40 continental crust. When reviewed in light of our models, these observations require that no 41 more than half of the MER's extension since ~2Ma has been achieved by dyke intrusion. 42 Magmatic heating and weakening of the crust would have rendered it aseismic if dyke 43 intrusion accounted for the entire 6 mm/yr extension rate. In the older, faster extending (16 44 mm/yr) Red Sea rift (RSR) in Afar, dyke intrusion is expected to have had a more dramatic 45 impact on crustal rheology. Accordingly, effective elastic plate thickness and Moho depth in 46 the Danakil region of northernmost Afar are markedly reduced and seismicity is shallower 47 than in the MER. Thermally driven variations in crustal rheology over time in response to 48 dyke intrusion thus play an important role in the development of continent-ocean transition.

49

50 1. Introduction

51 It is well established that continental rifts develop initially in a mechanical fashion, with along 52 axis segmentation governed by large-scale border faults defining early half-graben rift 53 morphology (e.g., Hayward and Ebinger 1996). A consensus is gradually emerging from a 54 number of tectonically active rifts and rifted continental margins worldwide, however, that 55 magma intrusion also plays an important role in extension prior to the onset of sea-floor 56 spreading (e.g., Maguire et al. 2006, White et al. 2008, Thybo and Nielsen 2009). This is an 57 appealing idea, since it obviates the need for large-scale tectonic forces to rupture thick, 58 strong cratonic lithosphere: dyke intrusion can occur at lower stresses than are required for 59 the stretching of thick continental lithosphere (e.g., Buck 2004, 2006, Bialas et al., 2010). 60 However, the subsequent effect of magma intrusion on the thermal structure (and by 61 inference, the strength) of the plate over time is poorly understood. It likely has important implications for the thermal evolution and subsidence history of the extending plate (e.g., 62 63 Thybo and Nielsen 2009), including whether or not continent-ocean transition is heralded by 64 an abrupt episode of continental plate thinning and subsidence after a period of heating and weakening by protracted magma intrusion (Bastow and Keir 2011; Keir et al., 2013). 65

66 To address these issues, a thermal model is developed to understand better the evolution of 67 continental crust during extension by dyke intrusion. The model space is parameterised as 68 an array of cells for which the heat-flow equation is solved numerically by finite difference 69 scheme. The effects of variable magma temperature, dyke injection frequency and size, and 70 geothermal gradient on the thermal evolution of the crust over time during rifting are tested 71 by mapping the solidus and 600°C isotherm (representing the brittle-ductile transition 72 temperature) positions. In a tectonically active rift this is a testable hypothesis seismically, 73 since crustal seismicity is not expected to develop at temperatures greater than ~600°C 74 (e.g., Maggi et al., 2000a).

To ground-truth the thermal models and input parameters, this study draws on geoscientific
 constraints from on-going extension in the East African (EAR) and Red Sea (RSR) rift
 systems in Ethiopia (Figure 1). The region exposes sub-aerially several sections of

78 asynchronous rift sector development above a hot (e.g., Rooney et al., 2012; Ferguson et 79 al., 2013), low wavespeed (Bastow et al., 2008) mantle; from embryonic continental rifting in 80 the slowly (~6 mm/yr) extending Main Ethiopian rift (MER) in the south (Kogan et al., 2012), 81 to incipient oceanic spreading in the more rapidly extending RSR and Gulf of Aden Rift in 82 Afar (e.g., Hayward and Ebinger, 1996; McClusky et al., 2010). Real-time geodetic and 83 seismic observations of dyke intrusion episodes (Wright et al. 2006, Keir et al. 2009, Grandin 84 et al., 2011) are available from the region, offering considerable advantage over studies of 85 extinct or buried rifted margins in constraining when and how dykes intrude the crust. The 86 region is also well-understood geophysically, with detailed constraints on parameters such 87 as crustal thickness, effective elastic plate thickness and P-wave seismic velocity structure all available (for reviews, see e.g., Bastow et al., 2011; Keir et al., 2013). 88

89 In the MER, a combination of GPS surveys and structural geology studies point towards 90  $\sim$ 80% of present-day strain being accommodated at least partly by magma intrusion within a 91 relatively narrow (~20 km) rift-axial zone, also known as the Wonji Fault Belt (WFB: Mohr 92 1967, Ebinger and Casey 2001). However, precisely what proportion of extension has been 93 accommodated by dyke intrusion into the still-thick MER crust since ~2 Ma is uncertain. In 94 the Danakil depression, where crustal thickness is markedly thinner than elsewhere in Afar 95 (Makris and Ginzburg 1987), it has been proposed that Pliocene-Recent basin development 96 and voluminous Quaternary volcanism are the result of a late-stage of plate stretching 97 following a protracted period of localised magma-intrusion (Bastow and Keir 2011, Keir et al. 98 2013). This study explores whether episodes of dyke intrusion during continental breakup 99 are capable of heating the continental crust sufficiently over time for it then to behave in a 100 ductile manner by plate stretching, prior to the development of a new mid-ocean spreading 101 centre.

102

## 103 2. Mathematical Model

104 The thermal evolution of a vertical dyke intruded into continental crust (Figure 2) is modelled 105 by solving the two-dimensional (2D) heat flow equation both horizontally (x-direction) and in 106 depth (z). The model is set up in a similar manner to previous studies (Royden et al., 1980; 107 Buck, 2004; Buck et al., 2005; Bialas et al., 2010) with a vertical cross-section through the 108 crust incorporating a model rift axis where consecutive dykes intrude along the centre of the 109 previous one. The dykes are intruded at a time-averaged rate which is constant at all depths 110 (z) beneath the rift axis. Homogeneous composition continental crust is assumed, such that 111 thermal conductivity (K), diffusivity ( $\kappa$ ), density ( $\rho$ ), specific heat capacity ( $C_{\rho}$ ) and latent heat 112 of fusion (L) remain constant as a function of depth and temperature. The 2D heat-flow 113 equation, incorporating the latent heat of fusion is

114 
$$\rho C_p \frac{\partial T}{\partial \tau} + \rho L \frac{\partial X}{\partial \tau} = K \nabla^2 T$$

115 Equation 1

116 where  $\nabla = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial z^2}$ ,  $T(x, z, \tau)$  is the temperature,  $X(x, z, \tau)$  is the melt fraction and  $\tau$  is the 117 time (e.g., Turcotte and Schubert 2002). Melt fraction is assumed to depend only on 118 temperature such that

 $119 \quad X = F(T)$ 

### 120 Equation 2

where *F* is a function derived from a simple three-component phase diagram based on a

Hawaiian olivine tholeiite basalt (Sample 14, Yoder and Tilley 1962) with three components;

the chemical analysis was recalculated as a CIPW norm (Cox et al. 1979) and the

124 components were re-normalised to give olivine, clinopyroxene and plagioclase. The melt

125 fractions corresponding to temperatures in the range 0 to 1320°C were calculated using the

simulated phase equilibria model of Witham (2008). The simple three-phase system was

127 used to test the model's performance when compared with analytical solutions, and to

- 128 explore the effects of different parameters. F (Equation 2) is generally determined from
- 129 experimental studies. Here, it is approximated by a series of linear trends.
- 130 The far-field geotherm T(z) is assumed to satisfy the boundary conditions

$$T \to \frac{Q_0}{K} z - \frac{A}{2K} z^2 \text{ as } x \to \pm \infty$$

132 Equation 3

- 133 where the surface temperature is taken to be zero. This equation is valid for all values of z.
- 134 The initial condition for a single injection is

T = T<sub>m</sub>, 
$$|x| < \omega$$
; T =  $\frac{Q_0}{K} z - \frac{A}{2K} z^2$ ,  $|x| > \omega$  at  $\tau = 0$ 

#### 136 Equation 4

for  $z_0 \le z \le z_1$ , where  $z_0$  and  $z_1$  define the upper and lower surfaces of the modelled region of the crust (Figure 2) and whose temperature satisfies Equation (3) such that

139  $T = \frac{Q_0}{\kappa} z_0$  at  $z = z_0$  and  $T = \frac{Q_0}{\kappa} z_1$  at  $z = z_1$ ,  $T_m$  is the magma injection temperature at 140 time  $\tau = 0$  and  $2\omega$  is the dyke width. Above and below the intruded region ( $z < z_0$  and  $z > z_1$ ), 141 the thermal evolution of the crust is governed by the geotherm (Equation 3). Solutions of 142 Equations (1) – (4) are required to determine how the temperature and melt fraction evolve 143 as functions of *x*, *z*, and  $\tau$ . Numerical solutions of Equations (1) – (4) were determined using 144 an explicit finite difference method. A full description of the finite difference method is 145 included as an appendix.

146 The heat-flow equation (Equation 1) was discretised using forward difference

147 approximations in  $\tau$  and a central difference approximation in x. The solution was computed

- forwards in time by incrementing the timestep (k) through integer values, starting with k = 0
- 149 where *T* and *X* are determined by the initial temperature profile (Equation 6). Due to the
- symmetrical nature of the solution about x = 0, the computational domain was restricted to

151 positive x values and a symmetry condition applied to the left hand edge of the domain. 152 Successive intrusions of basalt at a constant injection rate were modelled numerically by 153 displacing previously computed values of temperature rightwards (mimicking advection) by 154 the half-dyke width at each new injection time and inserting the new intrusion of the same dyke width and temperature  $T_m$  in the space vacated. The advection of heat due to ductile 155 156 stretching of the crust is not considered in our models since it will be negligible over the 157 time-scales we model intrusions. Brittle deformation by faulting has also not been accounted 158 for in the model. The injection frequency  $\psi$  was defined as the ratio of the magmatic 159 extension rate S to the dyke thickness  $2\omega$  so that  $S = 2\omega\psi$ .

160

## 161 **3.** Specific Model Parameterisation for Ethiopia

162 The tectonically active East African Rift (EAR) and southern Red Sea Rift (RSR) in Ethiopia 163 provide an excellent opportunity to source realistic input parameters for our thermal model (Figure 1). The starting composition was established using the lava from a 2007 fissure 164 165 eruption in Afar (sample A2, Ferguson et al. 2010), with a water content of 0.4 wt% assumed at all depths. The series of linear fits used for the temperature-melt fraction relationship 166 167 were determined using the MELTS (Ghiorso and Sack 1995, Asimow and Ghiorso 1998) 168 and Rhyolite-MELTS (Gualda et al. 2012) thermodynamic modelling programs. The 169 composition of the injected material and the intruded crust are assumed to be the same. 170 Because the injected material mainly cools and the host rock predominantly slowly increases 171 in temperature, the temperature-melt fraction relationship of the host material is not 172 important and will not affect the temperatures produced (Daniels, 2012). The solidus 173 temperature was based on previously published model temperatures (Annen and Sparks 174 2002).

The temperature-melt fraction relationship was calculated for four different pressures corresponding to different depths in the crust: z = 5, 10, 15-6 and 20 km (Figure 3). It has 177 been inferred from wide-angle seismic (Maguire et al., 2006), gravity (Cornwell et al., 2006) 178 and electrical resistivity (Desissa et al., 2013) study in Ethiopia that gabbroic intrusions occur 179 in this depth range in the upper crust beneath Quaternary-Recent zones of magmatic 180 extension. Partial melt is also known to reside at these depths, as revealed by 181 magnetotelluric analysis of the subsurface (Whaler and Hautot, 2006). The lithostatic pressures and corresponding depths (calculated using  $\rho gh$  with  $\rho$  = 2800 kg/m<sup>3</sup>, Annen and 182 Sparks 2002), along with all of the crystallisation points, are in Table 1. Values of the 183 184 physical parameters assumed are summarised in Table 2. A dyke thickness of 15 m allowed 185 different extension rates S to be achieved by varying the dyke injection frequency  $\psi$ . 186 Previous models that varied dyke thickness and injection frequency whilst fixing extension 187 rate have shown that thinner, more frequently intruded dykes increase the crustal 188 temperature more quickly than thicker, less frequently intruded dykes, but the effect is 189 insignificant compared with other parameters such as the extension rate (Daniels, 2012). It 190 is for this reason that only one dyke thickness is chosen. Injection temperatures ( $T_m$ ) in the 191 range 1240-1320°C were studied.

192

## 193 **4.** <u>Results</u>

Two-dimensional model runs with  $x_0 = 0$ ,  $x_1 = 10$  km,  $z_0 = 0$ ,  $z_1 = 10$  km,  $\Delta x = \Delta z = 5$  m and dyke width = 15 m were conducted for extension rates of 5, 10, 15 and 20 mm/yr and for a duration of 200 ka. In these models, the injected dyke extended over the depth of the computational array. Figure 4 shows the output of these two-dimensional models and the brittle-ductile transition (black line) and solidus (red line) isotherms migrating across the computational domain. Loss of heat at the top and bottom of the domain can be seen to affect the temperatures.

As detailed in the supplementary material, the model was tested successfully against independent analytical solutions. Moreover, except at the top and bottom of the model, this 203 2D numerical model can be approximated by a 1D model where the temperature profile 204 depends only on the horizontal distance x at a given, constant depth z: both 1D and 2D 205 numerical models yield similar solutions (see the supplementary material for details). 206 However, at the top and bottom of the modelled region of the crust, the thermal boundary 207 conditions influence the solution there immediately and eventually affect the solution 208 throughout the model space. But, if these upper and lower boundaries ( $z_0$  and  $z_1$ ) are 209 sufficiently far apart, the 1D model yields a very good approximation for the model interior, 210 thus reducing computational time considerably.

At the top of the 2D model, the boundary effect is analogous to the surface cooling of the system (see the supplementary materials for details). The amount of the modelled crust affected after time  $\tau$  can be approximated using  $l^2 \sim \kappa \tau$  such that after 1 Ma, the top 4 km of the crust will have experienced surface cooling, increasing to 7 km after 3 Ma. For depths >5 km, the 1D heat flow equation is thus appropriate for the study of the thermal structure of continental crust during extension by dyke intrusion over a time period of a couple of Ma.

217 The 1D numerical model was run using the parameters in Table 2 for extension rates of 3, 5, 218 10, 20, and 25 mm/yr, for a horizontal range of  $x_0 = 0$  to  $x_1 = 30$  km and at depths (z) of 5, 219 10, 15, and 20 km. These extension rates were designed to encompass the ~6 mm/yr 220 extending MER, and the ~16.4 mm/yr extending RSR in Afar. Each model was run for 5 Ma, 221 with temperature monitored as a function of distance from dyke injection point. Particular 222 attention was paid to the solidus temperature and brittle-ductile transition (600°C) isotherms. 223 Magmatic extension rate and the time taken to reach the solidus temperature or the brittle-224 ductile 600°C isotherm at the injection position (x=0) display an inverse power law relationship (S is proportional to  $\frac{1}{\sqrt{t}}$ ; Figures 5 and 6). Thus, magmatic extension rate is 225 approximately proportional to  $\frac{1}{\sqrt{t}}$ , independent of injection temperatures (Figure 5). Injection 226 227 temperature is thus secondary to extension rate in governing the rate of temperature 228 increase.

229 The distance (x) from the dyke injection and the time taken to reach a given isotherm 230 correlate linearly for all extension rates (S) (Figure 7 A). The linear trend indicates that the 231 magmatic extension rate is dominant at distances close to the dyke injection location. 232 Figure 7 B shows modelled isotherm positions as a function of distance from the dyke 233 injection point; also shown are isotherm positions determined from extension rate alone 234 (effects of conduction are close to negligible). Extension rate is a good proxy for isotherm 235 migration rate in the near field, but with increasing distance from the injection point, 236 conduction becomes an increasingly important additional effect.

237 When the time is plotted as a function of extension rate (Figure 6), the results are

comparable with the results of Michaut and Jaupart (2006) who found that the critical

temperature in their numerical models ( $t_c$ ) was inversely proportional to injection rate

squared ( $Q^2$ ). The constant that multiplies the injection rate in Michaut and Jaupart (2006)

and the extension rate in each of the relationships in Figure 6 is dependent on the

parameters used in the modelling (Table 2) and therefore is different for each case.

However, in both this study and in Michaut and Jaupart (2006), the time taken to reach a

244 particular temperature is inversely proportional to the square of the extension rate. The

timescales for the build up of temperature calculated for different magmatic extension rates

are quite varied. Calculations show that it will take significantly longer for the ambient

temperature to build up at slower extension rates: an extension rate three times faster will

248 decrease this time by an order of magnitude (Figure 5).

249

## 250 5. Discussion

#### 251 **5.1.** <u>Overview</u>

It is now well established that dyke intrusion achieves a significant proportion of extension
during continental rifting (e.g., Maguire et al., 2006; Thybo and Nielsen, 2009; White et al.,
2008), yet relatively little attention has been paid in the rifting community to the effects this

has on the thermal evolution (and by inference the strength) of the continental crust during
breakup. Previous studies have demonstrated that appreciable crustal heating occurs due
to repeated magma intrusion in arc settings (e.g. Annen et al. 2006, Solano et al. 2012), and
a similar thermal modelling approach has been followed in this study of continental rifting.

This study demonstrates that the thermal structure of the crust is controlled by several factors: intrusion depth, injection temperature, and magmatic extension rate. Of these, magmatic extension rate exerts first order control on crustal thermal structure (Figures 5, 6 and 7). The rate of transfer of heat laterally away from the zone of dyke intrusion can be approximated in the near-field by the magmatic extension rate, but at greater distances (>3-4 km), cooling by conduction becomes an important factor (Figure 7).

265 The location of the injection relative to the previous injection is also likely play a role in the 266 timescale of the build-up of heat in the crust. Here, each successive injection has intruded 267 through the centre of the previous injection. This may have had the effect of insulating each 268 hot injection from the cooler crust to either side and therefore indicate that the timescales 269 calculated represent minimum estimates. Additionally, the advection of heat due to ductile 270 stretching of the crust has not been accounted for in the model. At slow extension rates 271 relevant for continental rift zones, this effect is negligible compared to the marked and rapid 272 heating caused by intrusion. At faster rates of extension observed at mid-ocean ridges, but 273 rare for continental rifts, the advection of heat is likely more important.

Observations of seismicity worldwide indicate strongly that earthquake depths are fundamentally limited by the brittle-ductile transition in continental crust and commonly the 600°C isotherm is used to mark this transition in typical crust (e.g., Maggi et al., 2000a,b; Jackson, 2002). A 10-20 km wide region of the crust would be expected to heat to above 600°C in <1 Ma, even at relatively slow extension rates of ~10 mm/yr (Figure 7). At slower rates, heating to 600°C will take much longer (e.g., 6.3 Ma for a 20 km-wide region at 3 mm/yr).

#### 281

#### 5.2. Implications for the thermal development of the MER

282 The MER is the northern-most sector of the EAR and displays several stages of rift sector 283 development along strike. Embryonic continental rifting in the southern MER is dominated 284 by border faulting while in the northern MER, rifting is more evolved and axial magma 285 intrusion contributes significantly to Nubia-Somalia separation (e.g., Hayward and Ebinger 286 1996; Kogan et al., 2012). The northern MER has also undergone considerable 287 development over time: initial rifting during Miocene times was characterised by upper-288 crustal extension accommodated by the large-offset border faults that define the rift valley 289 flanks today (e.g., Wolfenden et al., 2005). Since Quaternary times however, faulting and 290 volcanism have localized to the 20-30 km wide WFB axial zone. Aligned Quaternary-Recent 291 monogenetic basaltic cones and resultant lava flows cut by the most active faults within the 292 MER, coupled with geodetic evidence that ~80% of Nubia-Somalia plate separation is 293 presently accommodated within the WFB (Bilham et al., 1999), was cited by Ebinger and 294 Casey (2001) as evidence that a significant proportion of extension in the MER is achieved by episodic magma intrusion. More recent studies of GPS measurements acquired over the 295 296 last two decades confirm the MER is currently opening at 5-6 mm/yr in an ESE-WNW 297 direction (Kogan et al., 2012). The seismic moment release in the MER since 1960 is 298 around half that expected from the plate separation velocities, which suggests 50% of the 299 extension is accommodated by aseismic processes such as magma intrusion (Hofstetter 300 and Beyth, 2003).

The 2001-2003 Ethiopia Afar Geoscientific Lithospheric Experiment (see Bastow et al., 2011 for a review) has facilitated the development of high-resolution sub-surface geophysical models of the MER. Wide-angle active-source, passive-seismic, and gravity studies of crustal structure have shown that zones of Quaternary-Recent magmatism in the WFB are underlain by anomalously high P-wavespeed and high-density material compared to surrounding native continental crust (e.g., Keranen et al., 2004; Mackenzie et al., 2005; Daly et al., 2008; Cornwell et al., 2006; Maguire et al., 2006; Tiberi et al., 2005). These are interpreted as zones of localised gabbroic intrusions that extend from the aligned
monogenetic cone fields along the rift axis surface to the base of the crust at 30-35 km depth
(e.g., Keranen et al., 2004; Mackenzie et al., 2005). While the total volume of new intruded
material beneath the axis is debated, the marked reduction in seismic velocities in the upper
~8 km of the crust suggests intrusion contributes a lower proportion of extension at these
shallow depths compared to elsewhere in the crust (Keranen et al., 2004).

314 The thermal models developed in this study show that ~6 mm/yr extension in the MER 315 should, if achieved 100% by magma intrusion, by now have heated the crust to 316 temperatures in excess of 600°C (Figures 5 and 7). Observations of seismicity in the MER 317 render this hypothesis implausible, however. Variations in seismicity along the WFB instead 318 demonstrate along-axis variability in the thermal state of the crust. The Boset segment 319 (Figure 1) is the most magmatically active portion of the MER (e.g. Abebe et al., 2007) and 320 accordingly exhibits the least seismicity and shallowest brittle-ductile transition at 6-9 km 321 depth (Beutel et al., 2010). Crustal tomographic studies indicate the highest P-wavespeed 322 anomalies anywhere along the MER occur in the Boset segment, with the implication that 323 the crust here contains a higher proportion of new igneous material than elsewhere along 324 the rift (e.g. Keranen et al., 2004; Maguire et al., 2006). In other areas of the MER, with 325 lower amplitude high P-wavespeed anomalies, seismicity is evident to depths of 15-18 km, 326 indicating higher crustal strength and lower temperatures (Beutel et al., 2010).

327 If only 50% of the 6 mm/yr extension in the MER has been achieved by dyke intrusion 328 beneath the WFB, the thermal models presented in this study would predict a significantly 329 smaller degree of heating and weakening. Extrapolating from Figure 7, a zone 20 km wide 330 would heat to the brittle-ductile transition at all depths only after about 6 Ma. This is a longer 331 period of time than the WFB has existed within the MER: earlier extension was confined to 332 the large-offset border faults (Wolfenden et al., 2005). The depth extent of seismicity and 333 variations in P-wave speeds beneath the magmatic segment along the axis of the MER 334 when interpreted in light of our thermal modelling supports the interpretation that the crust

beneath the WFB is not 100% new mafic material. Rather it is a zone of heavily intruded
continental crust. Mechanical extension (faulting and stretching) thus remains an important
mechanism of strain accumulation between Nubia and Somalia.

#### 338 5.3 Implications for the development of continent-ocean transition

339 In contrast to the relatively young magmatic phase of extension observed in the MER, Afar 340 has experienced magma assisted rifting since the Miocene (Wolfenden et al. 2005). Our 341 models predict that given the higher extension rate (~16 mm/yr) and longer period of time 342 elapsed since the onset of magma intrusion, crustal temperatures should be too high for 343 brittle deformation to occur; the crust should thus now be able to deform in a ductile manner 344 (stretching). However, most of sub-aerial Afar has generally thick crust (Makris and 345 Ginzburg, 1987; Hammond et al., 2011), and is still seismically active (Ayele et al., 2007a,b; 346 Keir et al., 2011a,b; Ebinger et al., 2013) indicating that magma intrusion has not thermally 347 weakened the plate as much as suggested by the model. A simple explanation for this is 348 that the Arabia-Nubia plate boundary has shifted north-eastward several times in response 349 to triple junction development in Afar. During earlier phases of magma-assisted rifting in 350 Miocene times, strain was accommodated in magmatic segments located proximal to the 351 western southern Red Sea border fault on the western margin of Afar (e.g. Wolfenden et al, 352 2005). Since then, strain has localised progressively north-eastward to form the current 353 configuration of axial volcanic segments (e.g. Dabbahu and Harraro segments) and 354 sometimes amagmatic grabens (e.g. Tendaho; Dobi and Hanle graben: Tesfaye et al., 355 2003). Consequently, magma intrusion is unlikely to have been localised for long enough in 356 any given location for sufficient crustal heating to occur. As a result, extension by dyke 357 intrusion remains the optimal straining mechanism (e.g., Buck, 2006), with plate strength 358 likely still too high to permit significant ductile stretching localised around the intrusion zone. 359 Our thermal models show that only when dyke intrusion is focused to one magmatic

360 segment for a protracted period of time would aseismic ductile deformation be expected to

361 commence (Figures 5 and 7). One region where this transition may be underway is the sub-362 aerial but below sea-level Danakil depression in northernmost Afar. Here rapid basin 363 subsidence since ~5 Ma indicated by 3-5 km accumulations of Pliocene-Recent sediments, 364 combined with a pulse of Quaternary-Recent fissural basaltic volcanism, were interpreted by 365 Bastow and Keir (2011) as evidence for a late stage of plate stretching and an increase in 366 decompression melting in the mantle. The Bastow and Keir (2011) study lacked constraint 367 on the mechanism responsible for the shift from extension by magma intrusion to extension 368 by ductile stretching, but noted that late-stage subsidence and volcanism is a common 369 feature of the geological record at magmatic rifted margins globally. The thermal models 370 presented in this study show that at the ~10 mm/yr extension rates observed in the Danakil depression (McClusky et al, 2010), a 20 km wide zone will be sufficiently heated at 5 km 371 depth after about 1 Ma of extension by magma intrusion to deform in a ductile fashion 372 373 (Figure 7). However, in the Danakil depression where plate stretching has commenced, 374 heat advection is likely to be a considerable additional component. A hotter and weaker 375 plate in the Danakil depression is supported by earthquakes restricted to the upper ~5 km of 376 the crust (e.g., Craig et al., 2011; Nobile et al., 2012), and ~5 km effective elastic plate 377 thickness derived from gravity-topography coherence studies of plate strength (Ebinger and 378 Hayward, 1996; Perez-Gussinye et al., 2009). When synthesized in light of a priori 379 geoscientific constraints from the Danakil region, our thermal models thus indicate that a 380 late-stage of localised plate stretching, with an associated pulse of decompression melting, can readily characterise the final stages of continent to ocean transition. 381

382

#### 383 6 Conclusions

We have developed a numerical solution to the heat-flow equation to quantify the effects of dyke intrusion on the thermal structure of the crust during rifting, and on the timescales of the heating at varying magmatic extension rates. The rate of extension by intrusion is shown to exert first order control on crustal thermal structure, and when extension is achieved
 entirely by dyke intrusion, the crust is expected to heat considerably on time-scales of less
 than 1 Ma.

390 We benchmarked our thermal models against recently developed constraints on crustal 391 structure and dyke intrusion episodes in Ethiopia. For the MER, our model predicts brittle 392 deformation at the ultra-slow extension rates of ~6 mm/yr will cease after only 300 ka of 393 entirely magmatic extension localised to the rift axis. Our thermal calculations, corroborated 394 by observations of seismic moment release, depth extent of seismicity, and P-wave speeds, 395 point instead to a rifting model by which only ~50% of the extension is accommodated by 396 magma intrusion. In the Danakil depression of northernmost Afar in contrast, a combination 397 of faster extension rates of ~10 mm/yr and longer history of magma intrusion has likely 398 resulted in sufficient heating and weakening of the plate to induce a late stage phase of 399 localised ductile stretching near the intruded zone. Our results demonstrate the significant 400 impact of dyke intrusion on the rheology of continental crust during rifting. The challenge 401 now is to understand better how dyke intrusion affected plate strength during the 402 development of magmatic margins worldwide.

403

#### 404 <u>Acknowledgements</u>

KAD would like to thank G. P. Daniels, P. G. Daniels and F. Witham for early assistance with the numerical coding and helpful discussions thereafter. C. Annen, J. D. Blundy, G. A. Jones and K. A. Whaler are also thanked for constructive comments and suggestions. The authors are grateful to three anonymous reviewers whose comments have strengthened and improved the manuscript. KAD was supported by a NERC Consortium Grant. RSJS is cosupported by a grant from the European Research Council. IDB is funded by the Leverhulme trust.

412

#### 413 **References**

- 414 Abebe, B., Acocella, V., Kome, T., Ayalew, D., 2007. Quaternary faulting and volcanism in
- the Main Ethiopian Rift. J. Afr. Earth Sci. 48, 115-124.
- 416 Annen, C., Sparks, R.S.J., 2002. Effects of repetitive emplacement of basaltic intrusions on
- 417 thermal evolution and melt generation in the crust. Earth Planet. Sci. Lett. 203, 937-955.
- 418 Annen, C., Blundy, J. D., and Sparks, R. S. J., 2006. The genesis of intermediate and silicic
- 419 magmas in deep crustal hot zones. J. Pet. 47(3), 505-539.
- Asimow, P.D., Ghiorso, M.S., 1998. Algorithmic Modifications Extending MELTS to Calculate
  Subsolidus Phase Relations. American Mineralogist 83, 1127-1131.
- 422 Ayele, A., Stuart, G., Bastow, I., Keir, D., 2007a. The August 2002 earthquake sequence in
- north Afar: Insights into the neotectonics of the Danakil microplate. J. Af. Earth Sci., 48(2),
- 424 70-79.
- 425 Ayele, A., Jacques, E., Kassim, M., Kidane, T., Omar, A., Tait, S., Nercessian, A.,
- 426 deChabalier, J-B. and King, G., 2007b. The volcano-seismic crisis in Afar, Ethiopia, starting
- 427 September 2005. Earth Planet. Sci. Lett. 255, 177-187.
- 428 Bastow, I.D., Nyblade, A.A., Stuart, G.W., Rooney, T., Benoit, M.H., 2008. Upper Mantle
- 429 Seismic Structure Beneath the Ethiopian Hotspot: Rifting at the Edge of the African Low
- 430 Velocity Anomaly. Geochem. Geophys. Geosyst., 9(12), doi:10.1029/2008GC002107.
- Bastow, I.D., Keir, D., 2011. The protracted development of the continent ocean transition in
  Afar. Nature Geoscience 4, 248-250.
- 433 Bastow, I.D., Keir, D., Daly, E., 2011. The Ethiopia Afar Geoscientific Lithospheric
- 434 Experiment (EAGLE): Probing the transition from continental rifting to incipient seafloor
- 435 spreading. In Volcanism and Evolution of the African Lithosphere (Beccaluva, L., Bianchini,

- 436 G., and Wilson, M., Editors). Geol. Soc. Am. Spec. Papers 478, 51-76,
- 437 doi:10.1130/2011.2478(04).
- 438 Beutel, E., van Wijk, J., Ebinger, C., Keir, D., Agostini, A., 2010. Formation and stability of
- 439 magmatic segments in the Main Ethiopian and Afar rifts. Earth Planet. Sci. Lett. 293, 225-
- 440 235.
- Bialas, R. W., Buck, W. R., and Qin, R., 2010. How much magma is required to rift a
- 442 continent? Earth Planet. Sci. Lett. 292, 68-78.
- Bilham, R., Bendick, R., Larson, K., Mohr, P., Braun, J., Tesfaye, S., Asfaw, L., 1999.
- Secular and Tidal Strain Across the Main Ethiopian Rift. Geophys. Res. Lett. 26 (18), 27892792.
- Bohrson, W. A., Spera, F. J., 2001. Energy-Constrained Open-System Magmatic Processes
- II: Application of Energy-Constrained Assimilation-Fractional Crystallisation (EC-AFC) Model
  to Magmatic Systems. J. Pet. 42 (5), 1019-1041.
- 449 Buck, W. R., 2004. Consequences of asthenospheric variability on continental rifting. In
- 450 Rheology and Deformation of the Lithosphere at Continental Margins (Karner, G. D., et al.,
- 451 Editors), Columbia University Press.
- 452 Buck, W., 2006, The role of magma in the development of the Afro-Arabian Rift System, in
- 453 The Structure and Evolution of the East African Rift System in the Afar Volcanic Province,
- 454 eds. Yirgu, G. Ebinger, C.J., Maguire, P.K.H., Geol. Soc. Lond. Spec. Pub., 259, 43-54.
- Buck, W. R., Lavier, L. L., and Poliakov, A. N. B., 2005. Modes of faulting at mid-ocean
  ridges. Nature 434, 719-723.
- 457 Carslaw, H.S., Jaeger, J.C., 1950. Conduction of Heat in Solids. Oxford University Press.
- 458 Cornwell, D.G., Mackenzie, G.D., England, R.W., Maguire, P.K.H., Asfaw, L.M., Oluma, B.,
- 459 2006. Northern Main Ethiopian Rift crustal structure from new high-precision gravity data. In

- 460 The Afar Volcanic Province within the East African Rift System (Yirgu, G., Ebinger, C. J.,
- 461 Maguire, P. K. H., Editors). Geol. Soc. Lond. Spec. Pub. 259, 307-321.
- 462 Cox, K.G., Bell, J.D., Pankhurst, R.J., 1979. The Interpretation of Igneous Rocks. George463 Allen and Unwin.
- 464 Craig, T. J., Jackson, J. A., Priestley, K., and McKenzie, D., 2011. Earthquake distribution
- 465 patterns in Africa: their relationship to variations in lithospheric and geological structure, and
- their rheological implications. Geophys. J. Int. 185(1), 403-434.
- 467 Daly, E., Keir, D., Ebinger, C.J., Stuart, G.W., Bastow, I.D. and Ayele, A., 2008. Crustal
- tomographic imaging of a transitional continental rift: the Ethiopian rift. Geophys. J. Int.
  172(3), 1033-1048.
- 470 Daniels, K., 2012. Modelling magma transport: a study of dyke injection. Ph.D. thesis,
  471 University of Bristol.
- 472 Desissa, M., Johnson, N. E., Whaler, K. A., Hautot, S., Fisseha, S., Dawes, G. J. K., 2013. A
- 473 mantle magma reservoir beneath an incipient mid-ocean ridge in Afar, Ethiopia. Nat. Geosci.474 In press.
- Ebinger, C. J., Hayward, N. J., 1996. Soft plates and hot spots: Views from Afar. J.
- 476 Geophys. Res. 101, (B10), 21859–21876.
- 477 Ebinger, C.J., Casey, M., 2001. Continental breakup in magmatic provinces: An Ethiopian
- 478 example. Geology 29, 527-530.
- 479 Ebinger, C.J., van Wijk, J., Keir, D., 2013. The time scales of continental rifting: Implications
- 480 for global processes. Geological Society of America Special Paper, 500,
- 481 doi:10.1130/2013.2500(11).

- 482 Ferguson, D.J., Barnie, T.D., Pyle, D.M., Oppenheimer, C., Yirgu, G., Lewi, E., Kidane, T.,
- Carn, S., Hamling, I., 2010. Recent rift-related volcanism in Afar, Ethiopia. Earth Planet. Sci.
  Lett. 292, 409-418.
- 485 Ferguson, D.J., Maclennan, J., Bastow, I.D., Pyle, D.M., Jones, S.M., Keir, D., Blundy, J.
- 486 Plank, T., Yirgu, G. Melting during late-stage rifting in Afar is hot and deep. Nature 499, 70-
- 487 73 (doi:10.1038/nature12292).
- 488 Ghiorso, M.S., Sack, R.O., 1995. Chemical Mass Transfer in Magmatic Processes. IV. A
- 489 Revised and Internally Consistent Thermodynamic Model for the Interpolation and
- 490 Extrapolation of Liquid-Solid Equilibria in Magmatic Systems at Elevated Temperatures and
- 491 Pressures. Contrib. Min. Pet. 119, 197-212.
- 492 Grandin, R., Jacques, E., Nercessian, A., Ayele, A., Doubre, C., Socquet, A., Keir, D.,
- 493 Kassim, M., Lemarchand, A., King, G. C. P., 2011. Seismicity during lateral dike
- 494 propagation: Insights from new data in the recent Manda Hararo–Dabbahu rifting episode
- 495 (Afar, Ethiopia). Geochem. Geophys. Geosyst. 12(4), Q0AB08.
- 496 Gualda, G.A.R., Ghiorso, M.S., Lemons, R.V., Carley, T.L., 2012. Rhyolite-MELTS: A
- 497 modified calibration of MELTS optimized for silica-rich, fluid-bearing magmatic systems. J.
- 498 Pet. 53(5), 875-890.
- Hammond, J.O.S., Kendall, J-M., Stuart, G.W., Keir, D., Ebinger, C., Ayele, A., Belachew,
- 500 M., 2011. The nature of the crust beneath the Afar triple junction: Evidence from receiver
- 501 functions. Geochem. Geophys. Geosyst. 12, Q12004.
- 502 Hayward, N. J., Ebinger, C., 1996. Variations in the along-axis segmentation of the Afar Rift
- 503 system. Tectonophysics 15(2), 244-257.
- Hofstetter, R., Beyth, M., 2003. The Afar Depression: Interpretation of the 1960-2000
- 505 earthquakes. Geophys. J. Int. 155, 715-732.

- Jackson, J., 2002. Strength of the continental lithosphere: Time to abandon the jelly
- 507 sandwich? GSA Today, September, 4-9.
- Jaupart, C., and Mareschal, J-C., 2007. Heat flow and thermal structure of the lithosphere. In
- 509 Crust and Lithosphere Dynamics (Watts, A. B., Editor), Treatise on Geophysics 6, 217–250.
- Jaupart, C., and Mareschal, J-C., 2011. Heat Generation and Transport in the Earth.
- 511 Cambridge University Press.
- 512 Keir, D., Hamling, I.J., Ayele, A., Calais, E., Ebinger, C., Wright, T.J., Jacques, E.,
- 513 Mohammed, K., Hammond, J.O.S., Belachew, M., Baker, E., Rowland, J.V., Lewi, E.,
- 514 Bennati, L., 2009. Evidence for focussed magmatic accretion at segment centres from lateral
- dike injections captured beneath the Red Sea Rift in Afar. Geology 37(1), 59-62.
- 516 Keir, D., Belachew, M., Ebinger, C., Kendall, J-M., Hammond, J.O.S., Stuart, G.W., Ayele,
- 517 A., Rowland, J.V., 2011a. Mapping the evolving strain field during continental breakup from
- 518 crustal anisotropy in the Afar Depression. Nature Communications 2:285, doi:
- 519 10.1038/ncomms1287.
- 520 Keir, D., Pagli, C., Bastow, I., Ayele, A., 2011b. The magma-assisted removal of Arabia in
- 521 Afar: Evidence from dike injection in the Ethiopian rift captured using InSAR and seismicity.
- 522 Tectonophysics 30, TC2008, doi:10.1029/2010TC002785.
- 523 Keir, D., Bastow, I., Pagli, C., Chambers, E.L., 2013. Spatial and temporal constraints on
- 524 mechanisms of continental breakup: evidence from Afar. Tectonophysics,
- 525 doi:10.1016/j.tecto.2012.10.015.
- 526 Keranen, K., Klemperer, S.L., Gloaguen, R., Group, E.W., 2004. Three-dimensional seismic
- 527 imaging of a protoridge axis in the main Ethiopian rift. Geology 32, 949-952.

- 528 Kogan, L., Fisseha, S., Bendick, R., Reilinger, R., McClusky, S., King, R., and Solomon, T.,
- 529 2012. Lithospheric strength and strain localization in continental extension from observations
- of the East African Rift. J. Geophys. Res. 17, B03402.
- Laube, N., Springer, J., 1998. Crustal melting by ponding of mafic magmas: A numerical
  model. J. Volc. Geotherm. Res. 81, 19-35.
- 533 Mackenzie, G.D., Thybo, H. and Maguire, P.K.H., 2005. Crustal velocity structure across the
- Main Ethiopian Rift: Results from 2-dimensional wide-angle seismic modelling. Geophys. J.
  Int. 162, 994-1006.
- 536 Maggi, A., Jackson, J., McKenzie, D., Priestley, K., 2000a. Earthquake focal depths,
- effective elastic thickness, and the strength of the continental lithosphere. Geology 28, 495-498.
- 539 Maggi, A., Jackson, J., Priestley, K., Baker, C., 2000b. A reassessment of focal depth
- 540 distributions in southern Iran, the Tien Shan and northern India: Do earthquakes really occur
- in the continental mantle? Geophys. J. Int. 143, 629-661.
- 542 Maguire, P.K.H., Keller, G.R., Klemperer, S.L., Mackenzie, G.D., Keranen, K., Harder, S.,
- 543 O'Reilly, B., Thybo, H., Asfaw, L., Khan, M.A., Amha, M., 2006. Crustal structure of the
- northern Main Ethiopian Rift from the EAGLE controlled source survey; a snapshot of
- 545 incipient lithospheric break-up. In The Afar Volcanic Province within the East African Rift
- 546 System (Yirgu, G., Ebinger, C. J., Maguire, P. K. H., Editors). Geol. Soc. Lond. Spec. Pub.
- 547 259, 271-293.
- 548 Makris, J., Ginzburg, A., 1987. The Afar Depression: transition between continental rifting
- and sea-floor spreading. Tectonophysics 141, 199-214.
- 550 McClusky, S., Reilinger, R., Ogubazghi, G., Amleson, A., Healeb, B., Vernant, P., Sholan, J.,
- 551 Fisseha, S., Asfaw, L., Bendick, R., and Kogan, L., 2010. Geophys. Res. Lett. 37, L05301.

- 552 Michaut, C., Jaupart, C., 2006. Ultra-rapid formation of large volumes of evolved magma.
- 553 Earth Planet. Sci. Lett. 250 (1-2), 38-52.
- Mohr, P.A., 1967. Major volcanotectonic lineament in the Ethiopian Rift System. Nature 213,
  664-665.
- Nobile, A., Pagli, C., Keir, D., Wright, T. J., Ayele, A., Ruch, J. and Acocella, V., 2012 Dike-
- 557 fault interaction during the 2004 Dallol intrusion at the northern edge of the Erta Ale Ridge
- 558 (Afar, Ethiopia). Geophys. Res. Lett. 39(19), L19305.
- 559 Pérez-Gussinyé, M., Metois, M., Fernández, M., Vergés, J., Fullea, J., Lowry, A. R., 2009.
- 560 Effective elastic thickness of Africa and its relationship to other proxies for lithospheric
- structure and surface tectonics. *Earth Planet. Sci. Lett. 287*(1), 152-167.
- Rivers, M. L., Carmichael, I. S. E., 1987. Ultrasonic Studies of Silicate Melts. J. Geophys.
  Res. 92 (B9), 9247-9270.
- 564 Rooney, T.O., Herzberg, C., Bastow, I.D., 2012. Elevated mantle temperature beneath East

565 Africa. *Geology*, 40(1), 27-30, G32382, doi:10.1130/G32382.1

- 566 Royden, L., Sclater, J.G., Von Herzen, R.P., 1980. Continental margin subsidence and heat
- flow: important parameters in formation of petroleum hydrocarbons. Bull. Am. Assoc. Pet.
- 568 Geol. 64, 173-187.
- 569 Solano, J.M.S., Jackson, M.D., Sparks, R.S.J., Blundy, J.D., and Annen, C., 2012. Melt
- 570 Segregation in Deep Crustal Hot Zones: a Mechanism for Chemical Differentiation, Crustal
- 571 Assimilation and the Formation of Evolved Magmas. J. Pet. 53(10), 1999-2026.
- 572 Spera, F. J., 2000. Physical Properties of Magmas. In Encyclopaedia of Volcanoes
- 573 (Sigurdsson, H., Editor-in-Chief). Academic Press, 1417 pp.
- 574 Stern, C. R., Wyllie, P. J., 1973. Water-saturated and undersaturated melting relations of a
- granite to 35 kilobars. Earth Planet. Sci. Lett. 18, 163-167.

- Tesfaye, S., Harding, D.J., and Kusky, T.M., 2003. Early continental breakup boundary and
  migration of the Afar triple junction, Ethiopia. GSA Bull. 115(9), 1053-1067.
- 578 Thybo, H., Nielsen, C.A., 2009. Magma compensated crustal thinning in continental rift 579 zones. Nature 457, doi:10.1038/nature07688, 873-876.
- 580 Tiberi, C., Ebinger, C., Ballu, V., Stuart, G.W. and Oluma, B., 2005. Inverse models of
- gravity data from the Red Sea-Aden-East African rifts triple junction zone. Geophys. J. Int.
  163(2), 775-787.
- 583 Turcotte, D. L., Schubert, G., 2002. Geodynamics. Cambridge University Press, pp 456.
- 584 Whaler, K.A., Hautot, S., 2006. The electrical resistivity structure of the crust beneath the
- 585 northern Main Ethiopian Rift. In The Afar Volcanic Province within the East African Rift
- System (Yirgu, G., Ebinger, C.J., Maguire, P.K.H., Editors). Geol. Soc. Lond. Spec. Pub.
  259, 293-305.
- 588 White, R.S., Smith, L.K., Roberts, A.W., Christie, P.A.F., Kusznir, N.J., the rest of the iSIMM
- Team, 2008. Lower crustal intrusion on the North Atlantic continental margin. Nature 452,
- 590 doi:10.1038/nature06687, 460-464.
- Witham, F., 2008. The degassing of basaltic magma chambers. Ph.D. thesis, University ofBristol.
- 593 Wolfenden, E., Ebinger, C., Yirgu, G., Renne, P., Kelley, S.P., 2005. Evolution of the
- southern Red Sea rift: birth of a magmatic margin. Geol. Soc. Am. Bull. 117, 846-864.
- 595 Wright, T.J., Ebinger, C., Biggs, J., Ayele, A., Yirgu, G., Keir, D., Stork, A., 2006. Magma-
- maintained rift segmentation at continental rupture in the 2005 Afar dyking episode. Nature42, 291-294.
- Yoder, H.S., Tilley, C.E., 1962. Origin of Basalt Magmas An Experimental Study of Natural
  and Synthetic Rock Systems. J. Pet. 3(3), 342-532.

601 Figure captions

Figure 1: Tectonic setting of the East African rift system in the Horn of Africa. Solid black lines show Oligocene-Miocene border faults of the Red Sea, Gulf of Aden and East African rifts. Red segments show the Quaternary-Recent subaerial rift axes. DD: Danakil Depression. TGD: Tendaho-Goba'ad Discontinuity. MS: magmatic segments. DG: Dobi Graben. HG: Hanli Graben. Dashed red lines are sea-floor spreading centres in the Red Sea and Gulf of Aden. Top left inset: topography of NE Africa and Arabia. Arrows show plate motions relative to a fixed Nubian plate. Red lines are plate boundaries.

609 Figure 2: A schematic diagram showing the set-up of the model relative to the overlying rift

topography, and the dimensions and position of the computational domain within the crust.

611 Figure 3: Temperature versus melt fraction for 4 different pressures, calculated using

612 MELTS (Ghiorso and Sack, 1995; Asimow and Ghiorso, 1998), Rhyolite-MELTS (Gualda et

al., 2012) and experimental estimates of the water-saturated granite solidus (Stern and

614 Wyllie, 1973; Annen and Sparks, 2002). Small differences in the melt fraction-temperature

relationship will have a minimal effect on the results.

Figure 4: Outputs from two-dimensional model runs with  $z_0 = 0$  and  $z_1 = 10$  km, and  $\tau = 20$ 

ka, 100ka and 200 ka. Above: extension rate S = 5 mm/yr. Below: S = 20 mm/yr. The brittle-

ductile transition (black line) and solidus (red line) isotherms are highlighted.

Figure 5: Extension rate versus the time, expressed in ka, taken to reach the solidus and 600°C isotherm temperatures at 5 km depth at the injection position. The extension rates of the MER (~6 mm/yr) and RSR (15 - 20 mm/yr) are highlighted. The injection temperatures are in the range  $T_m = 1220$  to  $1320^{\circ}$ C.

Figure 6: Time taken to reach the 600°C isotherm temperature as a function of extension rate.

600

625 Figure 7: A) Time taken to reach the solidus temperatures as a function of the distance away 626 from the dyke injection point, at 5 km depth. B) The position of the 600°C isotherm (solid 627 lines and unfilled dots) due to the model (lines) and the extension rate alone (dots). The 628 component of the extension rate alone is calculated using the time taken to reach the 600°C 629 isotherm at distance x = 0 as the starting point, and then migrating the isotherm away from 630 the starting point at the magmatic extension rate. Extension rates of 5 mm/yr (grey solid 631 lines and unfilled dots) and 20 mm/yr (black solid lines and unfilled dots) are shown. The 632 arrows show the components of extension alone (black arrow) versus the cooling due to 633 conduction (grey arrow). The first arrow is much longer than the second one, illustrating that 634 the time taken to reach the isotherm is primarily controlled by the extension rate; accounting 635 for heat loss by conduction increases this time but this effect appears to be secondary.

636

#### 637 **Table captions**

Table 1: Temperatures (T) in °C, and corresponding melt fractions (X) for four different

639 pressures: 137.34 MPa (5 km depth); 274.68 MPa (10 km depth); 412.02 MPa (15 km

640 depth); and 549.36 MPa-(20 km depth). Subscripts I, e and s correspond to the liquidus,

- 641 eutectic and solidus temperatures respectively; c and c2 are arbitrary points on the X-T
- 642 diagram chosen to give the best fit to the data.
- Table 2: Nomenclature Model parameters and input values. <sup>a</sup>Annen and Sparks (2002).

```
<sup>b</sup>Jaupart and Mareschal (2007). <sup>c</sup>Jaupart and Mareschal (2011).
```

- Table 3: Time taken in years for the temperature at the injection line, x = 0, to reach the
- solidus temperature and the 600°C isotherm for different extension rates and depths.

647

#### 648 Supplementary Material

## 649 Practical Implementation of the Model

Numerical solutions of Equations (1) - (4) were determined using an explicit finite difference

- 651 method. The heat-flow equation (Equation 1) was discretised using forward difference
- approximations in  $\tau$  and a central difference approximation in x to give

$$\frac{T_{(i,j,k+1)}}{\Delta \tau} + C \frac{X_{(i,j,k+1)}}{\Delta \tau} = \kappa \left( \frac{T(i+1,j,k) - 2T(i,j,k) + T(i-1,j,k)}{(\Delta x)^2} + \frac{T(i,j+1,k) - 2T(i,j,k) + T(i,j-1,k)}{(\Delta z)^2} \right)$$

654 Equation A1

653

where  $C = L / C_p$ . Here  $T_{(i,j,k)}$  and  $X_{(i,j,k)}$  are numerical approximations to *T* and *X* at location *x*   $i \Delta x, z = z_0 + j \Delta z$  and time  $\tau = k \Delta \tau$  where  $\Delta x, \Delta z$  and  $\Delta \tau$  are the step lengths in *x*, *z* and  $\tau$  respectively. The modelled region of the crust is taken as  $-x_{\infty} \le x \le x_{\infty}, z_0 \le z \le z_1$  where *i* ranges from *-N* to *N* with  $x_{\infty} = N \Delta x$ ; *j* ranges from 0 to *M* with  $z_1 - z_0 = M \Delta z$ . *N* and *M* are sufficiently large to accommodate the outer behaviour. Equation (5) can then be written as

661 
$$T_{(i,j,k+1)} + C X_{(i,j,k+1)} = R_{(i,j,k)}$$

662 Equation A2

663 where

$$R_{(i,j,k)} = T_{(i,j,k)} + C X_{(i,j,k)} + A \left( T_{(i+1,j,k)} - 2 T_{(i,j,k)} + T_{(i-1,j,k)} \right) + B \left( T_{(i,j+1,k)} - 2 T_{(i,j,k)} + T_{(i,j-1,k)} \right)$$

664

666 and  $A = \frac{\kappa \Delta \tau}{(\Delta x)^2}$ ,  $B = \frac{\kappa \Delta \tau}{(\Delta x)^2}$  and must be solved in conjunction with the *X*-*T* relation 667 (Equation 2) in discretised form to find the solution values  $T_{(i,j,k+1)}$  and  $X_{(i,j,k+1)}$  at the new timestep and each internal grid point *(i,j)*. With *F* of piecewise linear form,  $T_{(i,j,k+1)}$  and  $X_{(i,j,k+1)}$  can be found exactly, depending on which linear section of F is relevant for any given value of  $R_{(i,j,k)}$ . Since Equation (8) describes a straight line of gradient -1 / C, its intersection with Equation (2) is determined by the size of  $R_{(i,j,k)}$  relative to the value of *R* associated with each crystallisation point. The new temperature and melt fraction are thus calculated as

673 
$$T_{(i,j,k+1)} = \frac{R_{(i,j,k)} - C q}{1 + mC}, \qquad X_{(i,j,k+1)} = m T_{(i,j,k+1)} + q$$

674 Equation A4

where *m* and *q* are defined by the gradients and intercepts respectively, of the linear sections of *F*.

Values of *T* and *X* on the boundaries of the modelled region of the crust are given by the boundary conditions (Equations 3, 4 and 5) applied at  $x = \pm x_{\alpha}$ . Because the solutions for *T* and *X* are generally symmetric about x = 0, the computational domain can be halved by applying the boundary condition  $\frac{\delta T}{\delta x} = 0$ , at x = 0 and restricting attention to the region  $0 \le x \le$  $x_{\infty}, z_0 \le z \le z_1$ . Numerically, this condition can be applied using a quadratic interpolation of *T* near x = 0, leading to the result that

$$T_{(0,k+1)} = \frac{1}{3} \left( 4 T_{(1,k+1)} - T_{(2,k+1)} \right).$$

684 Equation A5

Once the values of  $T_{(i,j,k+1)}$  are determined, Equation (9) can be used to determine *T* at the dyke injection point (*x* = 0).

## 687 Analytical Solutions

Various analytical results can be obtained for the 1D heat-flow equation, which can then be used as approximations for the 2D heat-flow equation (Equation 1). The excess heat content, *Q*, is independent of time and can be used to calculate the temperature at any given time. This is because the excess heat content over all space  $-\infty < x < \infty$  at a general time  $\tau$ must be equal to that of the dyke at  $\tau = 0$ . At large time  $\tau$ , the temperature can be found explicitly via  $x \sim 2 (\kappa \tau)^{1/2}$  (Turcotte and Schubert, 2002)

It is also possible to obtain an exact analytical solution to Equations (1) - (4) if the effect of
latent heat is neglected (L=0) (see, Carslaw and Jaeger 1950), which gives the peak
temperature at the centre of the domain, x=0, in terms of error functions (see Daniels 2012
for full details).

698

#### 699 Model Validation

#### 700 **<u>1D Model</u>**

701 The physical parameters were assigned values according to Table A.1. Initially, latent heat 702 effects were ignored. This was done to test the model against the analytical solution that 703 exists without L (Carlsaw and Jaeger, 1950). Assuming the upper and lower surfaces ( $z_{0}$  and 704  $z_1$  respectively) are sufficiently far apart, 1D analytical results are applicable to the 2D case 705 for a fixed value of z. The decay over time of the dyke's thermal anomaly relative to the 706 ambient temperature gives an analytical solution at large time  $\tau$  (Equation 4-170, Turcotte 707 and Schubert 2002). An exact solution is obtained if the effect of latent heat is neglected 708 (L=0, see, Carslaw and Jaeger 1950).

Figure A.1 A) shows the numerical solution for the peak temperature at the centre of the dyke, x = 0, as a function of time, along with the corresponding exact solution. There is excellent agreement, with the error reaching a maximum, yet small, value at small time where the numerical method has difficulty in accurately resolving the large change in temperature at the edge of the dyke (Figure A.1 B). Figure A.1 C) shows the heat content integral, per unit area of the dyke-country rock interface, plotted as a function of time. For these parameters (Table 4) it should have the constant value Q /  $\rho = 9.768 \times 10^6 \text{ J kg}^{-1} \text{ m}^{-1}$  and this is accurately reproduced for times  $\tau$  of up to about 1.5 x 10<sup>9</sup> s. For larger times the outer boundaries of the computational domain begin to influence the solution because the diffusion scale  $x \sim 2$  ( $\kappa \tau$ ) <sup>1/2</sup> becomes comparable with the size of the domain.

719 The effect of latent heat is now considered. The parameter values used are the same as those in Table 4 with latent heat L =  $4 \times 10^5$  J kg<sup>-1</sup> (Turcotte and Schubert 2002). Figures A.2 720 A) and B) show the temperature profile obtained numerically at time  $\tau = 3.11 \times 10^9$  s for a 721 dyke width of 5 m with  $\Delta \tau$  = 3600 s,  $\Delta x$  = 1 m and  $x_{\infty}$  = 200 m, in excellent agreement with 722 723 the analytical solutions. Figures A.2 C) and D) show the temperature at the centreline x = 0724 as a function of time. A comparison is made with the analytical result where Q /  $\rho$  = 1.1768 x 10<sup>7</sup> J kg<sup>-1</sup> m<sup>-1</sup>. Figure A.2 E) and F) show that the numerical solution is consistent except for 725 very small times where inaccuracy is introduced through the rapid change in temperature at 726 727 the edge of the dyke.

Also, the 1D numerical model is tested against the analytical solution for the decay over time of the dyke thermal anomaly relative to the ambient temperature. At large time, the temperature at the centre of the numerical domain should decay as the square root of time:  $T(0, \tau) = \frac{Q}{2\rho Cp \sqrt{(\pi \kappa)} \tau^{0.5}}$  (Equation 4.170, Turcotte and Schubert, 2002) Figure A.3 confirms

that this behaviour is accurately reproduced by the numerical solution.

733 Finally, tests were carried out to investigate the effect of step lengths  $\Delta x$  and  $\Delta \tau$  on the 734 numerical solution. Figure A.4 A shows results obtained for the parameter values in Table 4,  $L = 4 \times 10^5$  J kg<sup>-1</sup> and a dyke width of 30 m. Computations were performed with  $x_{\infty} = 400$  m, 735  $\Delta \tau$  = 3600 s and three different spatial steps  $\Delta x$  = 2 m, 6 m and 10 m. These confirm the 736 737 gradual loss of accuracy with increasing  $\Delta x$ . Figure A.4 B shows results obtained for the 738 same physical parameters but with a dyke width of 3 m. Here the computations were carried 739 out with  $x_{\infty}$  = 100 m,  $\Delta x$  = 1 m and two different time steps  $\Delta \tau$  = 5000 s and 10000 s. The 740 reduction in accuracy by using the larger time step is not significant and justifies the use of a 741 larger time step in subsequent calculations, provided the condition for numerical stability is742 maintained.

#### 743 One-dimensional versus two-dimensional models

744 The boundary effect at the top and bottom of the 2D model gradually has an effect on larger 745 and larger areas of the interior solution with increasing time. At the top of the computational 746 domain, this is analogous to the surface cooling of the system and allows an appreciation of the likely effect of surface cooling on the system after any specified time (Figure A.5). Except 747 748 at the top and bottom of the two-dimensional model, the one and two-dimensional models 749 yield same solutions. This is shown in Figure A.6 where the two-dimensional solution at 750 different depths (z) has been compared with a one-dimensional model solution for that 751 depth. The interior solutions to the 2D numerical model are comparable with the 1D model 752 results.

753

#### 754 Figure captions

Figure A.1: Comparison of the 1D numerical solution for L=0 J/kg,  $T_m = 1320^{\circ}C$  and  $\omega = 2.5$ m with the analytical solution for the peak temperature over time. A) The numerical and analytical peak temperatures. B) The difference between the analytically and numerically calculated temperature values. The difference is calculated as the analytical temperature minus the numerical temperature. C) Heat content integral as a function of time for the computation of A) and B). D) The percentage difference between the calculated heat content integral and the expected analytical value.

Figure A.2: A) 1D numerical solution for L = 4 x  $10^5$  J/kg, Tm =  $1320^{\circ}$ C and  $\omega$  = 2.5 m at time = 3.11 x  $10^9$ s (100 years) using  $\Delta \tau$  = 3600 s and  $\Delta x$  = 1 m; the large-time analytical solution is also shown. B) The difference between the analytical and numerical solutions. C) 1D numerical solution for the peak temperature at the centreline x = 0 as a function of time for the computation of A) and B); the large-time analytical solution is also shown. D) The

767 difference between the analytical and numerical solutions. E) Heat content (Q) as a function

768 of time for the computation of A) and B). F) The percentage difference between the

Figure A.3: The ratio of the 1D numerical solution to the exact analytical solution for the

771 temperature at the centre of the dyke  $\tau^{\frac{1}{2}}T(0,\tau)x 2\rho Cp(\pi \kappa)^{\frac{1}{2}}/Q$ , as a function of time for the

computation of Figure A.2. Close proximity to the analytical solution is achieved almost

immediately with the exact analytical solution reached in 30.95 years or 315 time steps.

Figure A.4: A) Difference between the analytical and numerical solutions for  $L = 4 \times 10^5 \text{ J/kg}$ ,

775 Tm = 1320°C and = 15 m at time  $\tau$  = 3.11 x 10<sup>9</sup>s (100 years) using  $\Delta \tau$  = 3600 s and  $\Delta x$  = 2

m, 6 m, and 10 m. B) Difference between the analytical and numerical solutions for L = 4 x

777 10<sup>5</sup> J/kg, Tm = 1320°C and ω = 1.5 m at time τ = 10<sup>8</sup> s (1157 days / ~3.2 years) using Δx =

778 1 m with  $\Delta \tau$  = 5000 s and 10000 s.

Figure A.5: Temperature contours for the numerical computations of the 2D heat-flow equation with L = 4 x 10<sup>5</sup> J/kg, T<sub>m</sub> = 1320°C,  $z_0$  = 1000 m,  $z_1$  = 5000 m,  $Q_0/K$  = 0.03°C/m and  $\omega$  = 7.5 m, obtained using x<sub>∞</sub> = 4000 m,  $\Delta x = \Delta z = 5$  m,  $\Delta \tau = 3.11 \times 10^6$ s. The temperature shown is that recorded at the time step immediately prior to the next injection at time = 2.49 x 10<sup>12</sup>s (80 ka) for extension rate S = 25 mm/yr.

Figure A.6: Numerical solutions for the 2D model with L = 4 x  $10^5$  J/kg, T<sub>m</sub>= 1320°C, z<sub>0</sub>=

785 1000 m,  $z_1$  = 5000 m,  $Q_0/K$  = 0.03°C/m and  $\omega$  = 7.5 m with an extension rate S = 25 mm/yr;

786 also the equivalent 1D calculations at depths z given by A) 1500 m, B) 2750 m, C) 3000 m,

D) 3250 m, E) 4500 m obtained using  $z(Q_0/K)$ . The computations were performed with  $x_{\infty}$ =

4000 m,  $\Delta x = \Delta z = 5$  m,  $\Delta \tau = 3.11$  x 10<sup>6</sup>s and show the temperature recorded immediately

prior to the next injection at time=  $6.22 \times 10^{11}$ s (~20 ka).

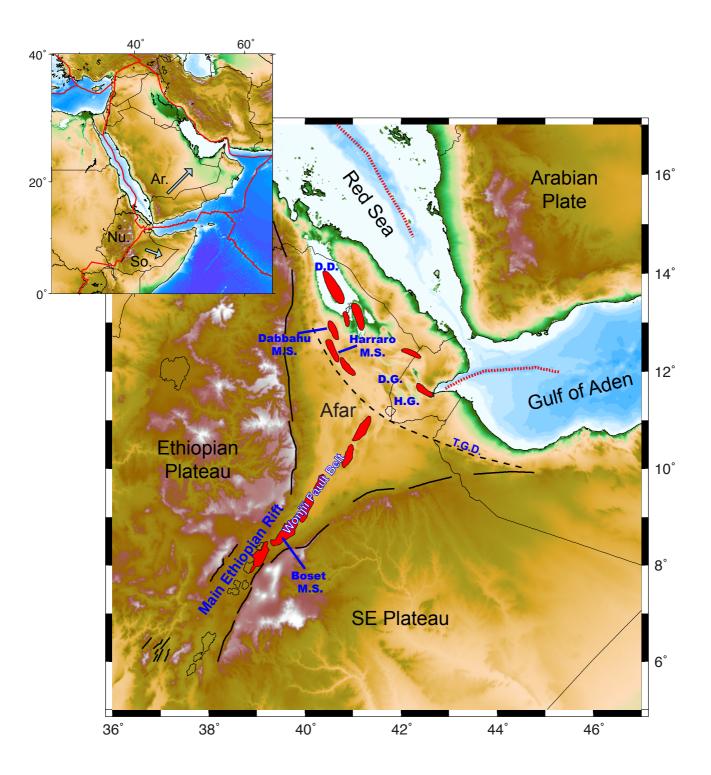
790

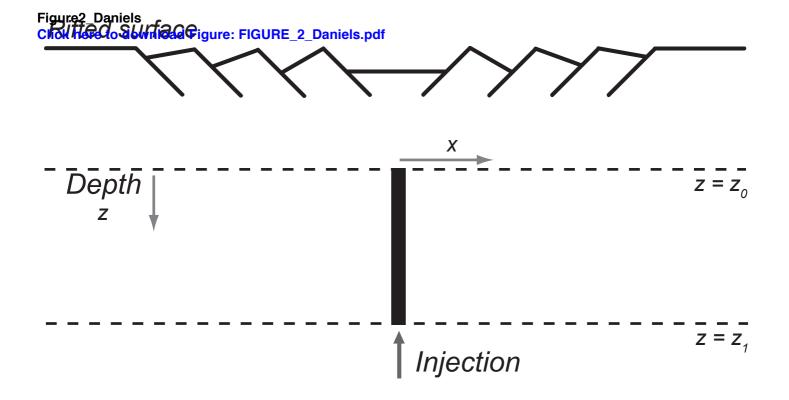
## 791 **Table caption**

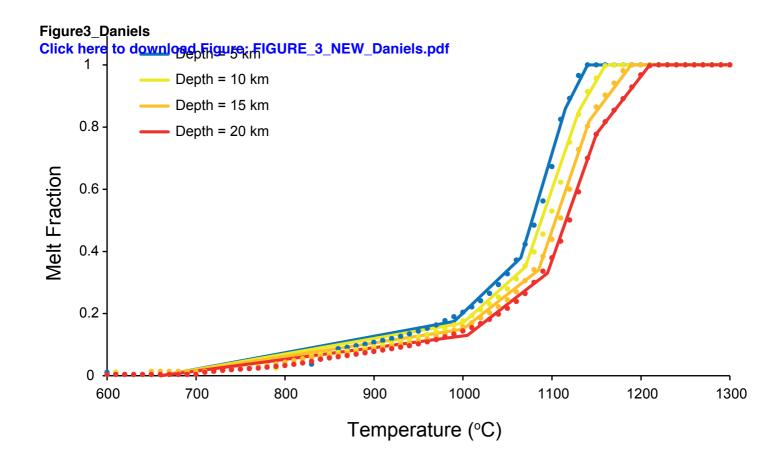
- Table A.1: The initial parameter values used to test the 1D model against the analytical
- solution. <sup>a</sup>Annen and Sparks (2002); Bohrson and Spera (2001); Laube and Springer (1998);
- 794 Rivers and Carmichael (1987). <sup>b</sup>Using  $\kappa = K / \rho C_p$ , with K = 1.15 W/m/K (Spera, 2000),  $\rho =$
- 795 2.8 x  $10^3$  kg/m<sup>3</sup> (Annen and Sparks, 2002) and C<sub>p</sub> = 1.48 x  $10^3$ .J/kg (Annen and Sparks,
- 796 2002)

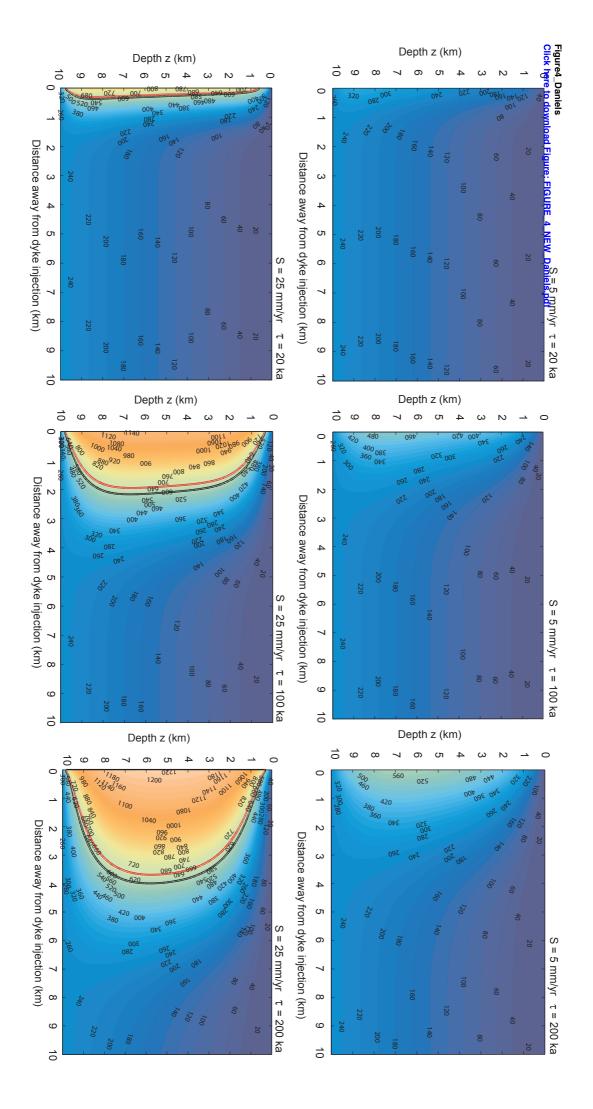
## **Highlights**

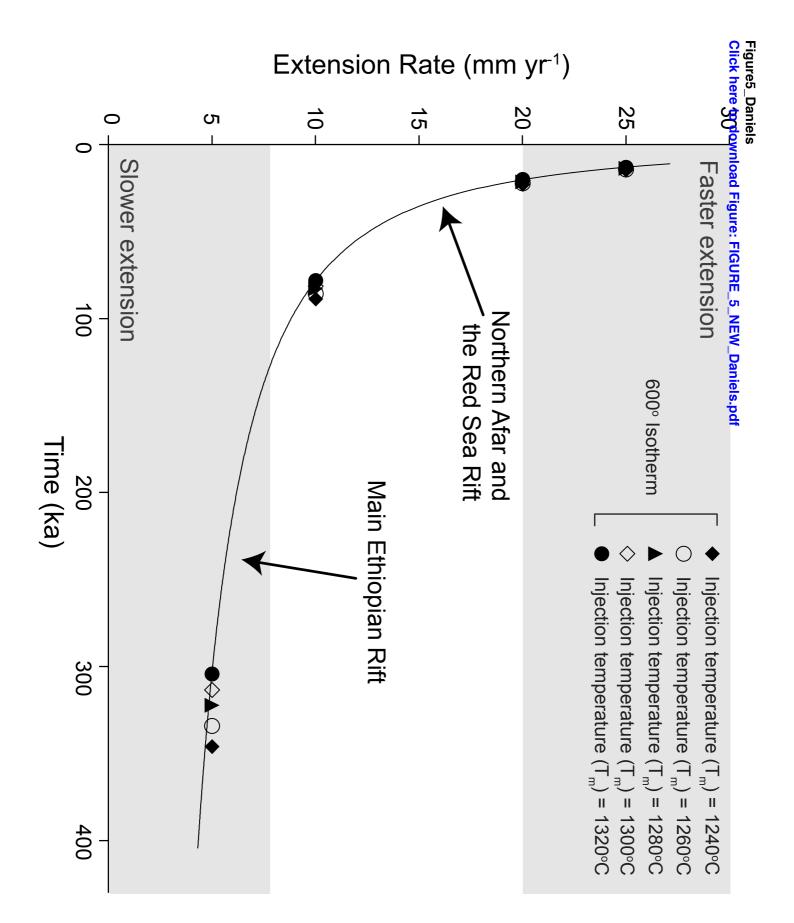
- A numerical solution to the heat-flow equation is developed
- Dyking has a significant thermal effect on crust rheology during rifting
- Extension rate exerts first-order control on crustal thermal structure during rifting
- The crust is expected to heat considerably on time-scales of less than 1 Ma
- In the MER dyking has localised for insufficient time for significant crustal heating

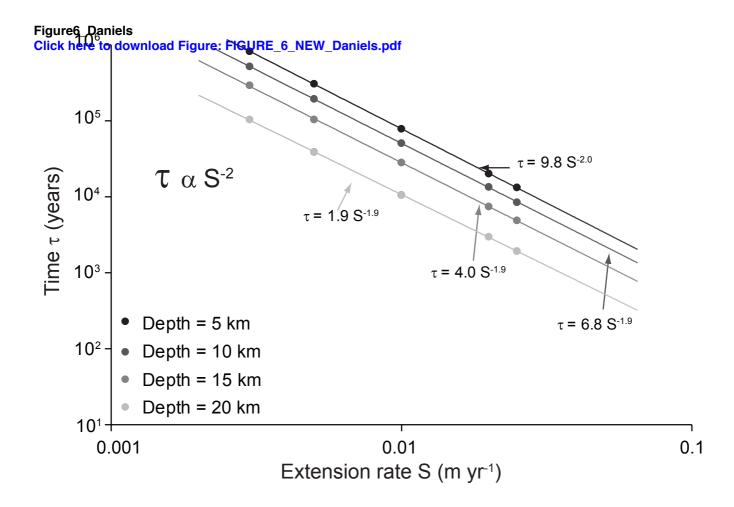


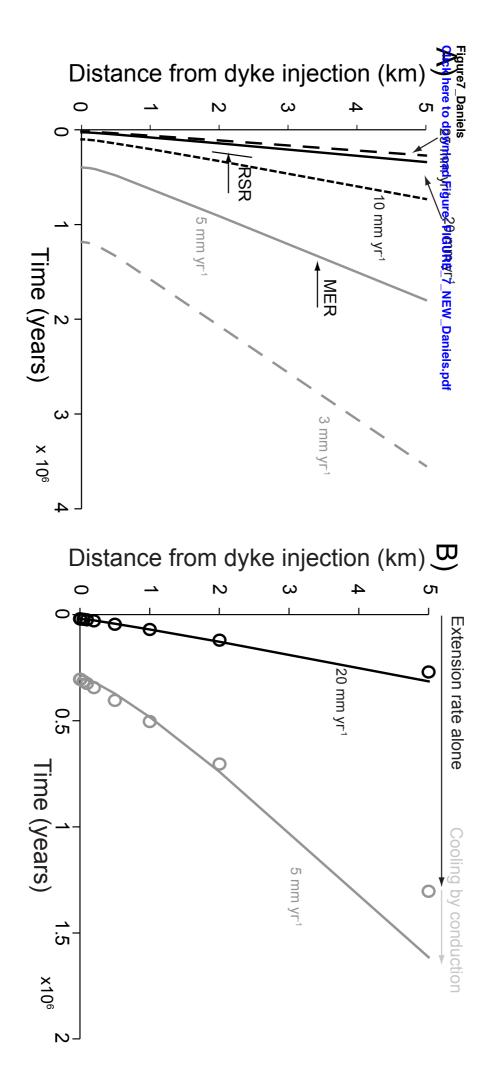












## Table1\_Daniels Click here to download Table: Table1\_NEW\_Daniels.xlsx

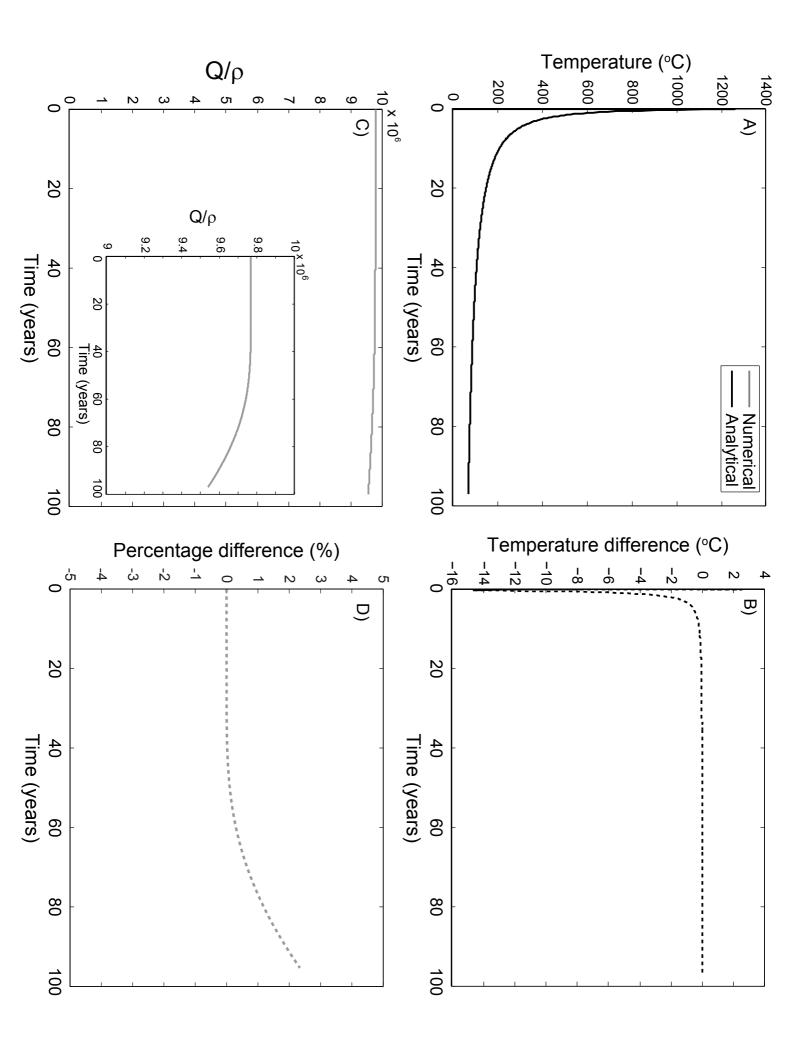
Pressure	1373.4	2746.8	4120.4	5493.6
T	1140	1160	1189	1210
XI	1	1	1	1
T <sub>c</sub>	1115	1130	1142	1150
X <sub>c</sub>	0.860	0.850	0.820	0.778
T <sub>c2</sub>	1065	1070	1085	1095
X <sub>c2</sub>	0.380	0.350	0.340	0.330
T <sub>e</sub>	990	1000	1000	1005
X <sub>e</sub>	0.175	0.170	0.150	0.130
Ts	660	660	660	660
X <sub>s</sub>	0	0	0	0

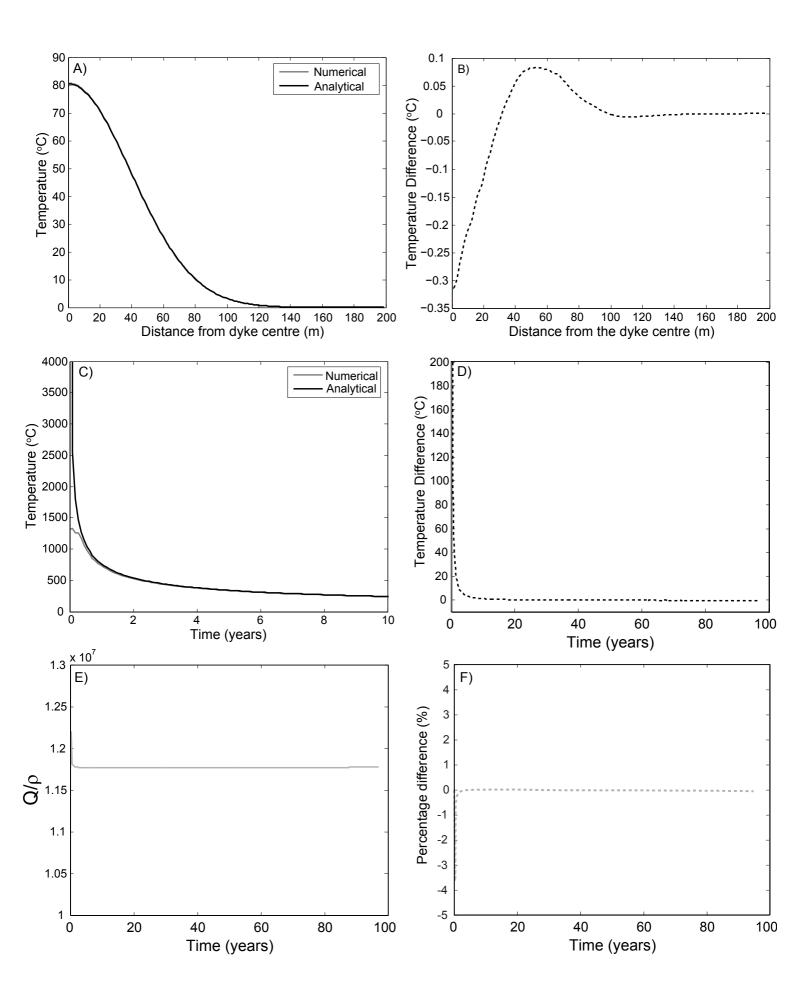
## Table2\_Daniels Click here to download Table: Table2\_NEW\_Daniels3.xlsx

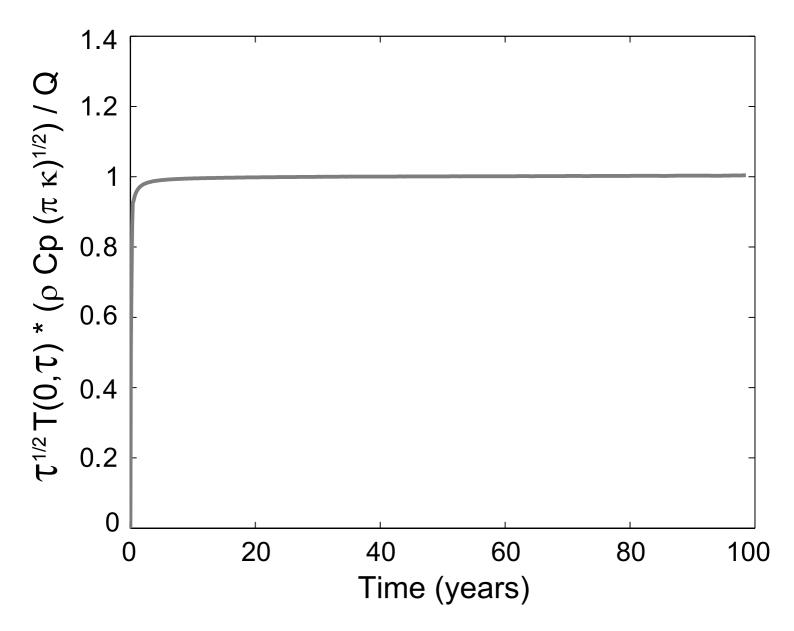
Parameter		Values	Units
Δχ, ΔΖ	Array cell size	5	m
$\Delta t$	Timestep size	3110400	S
ω	Dyke half thickness	15	m
ρ	Density <sup>a</sup>	2800	kg / m³
k	Thermal conductivity <sup>b</sup>	2.2	W / m / K
κ	Thermal diffusivity	5.3 x 10 <sup>-7</sup>	m² / s
L	Specific latent heat <sup>a</sup>	4 x 10 <sup>5</sup>	J / kg / K
C <sub>p</sub>	Specific heat capacity <sup>a</sup>	1480	J / kg
Q <sub>o</sub>	Surface heat flux <sup>c</sup>	60	mW / m <sup>2</sup>
А	Heat production <sup>c</sup>	8 x 10 <sup>-7</sup>	W/m <sup>3</sup>

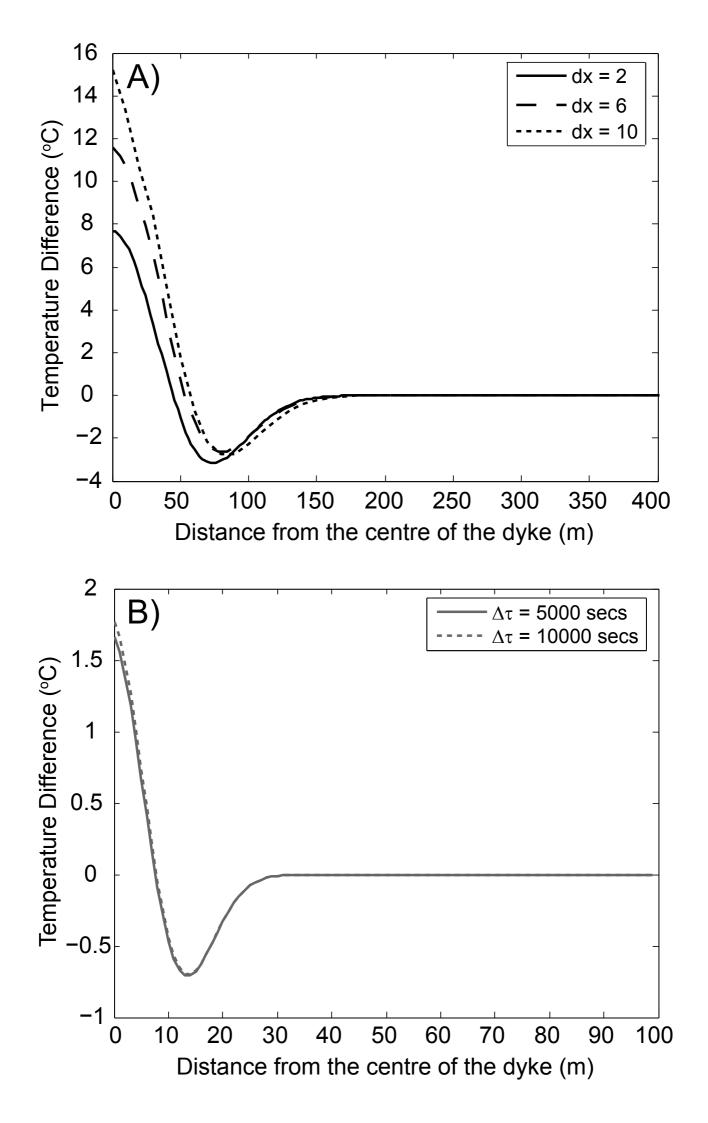
## Table3\_Daniels Click here to download Table: Table3\_NEW\_Daniels.xlsx

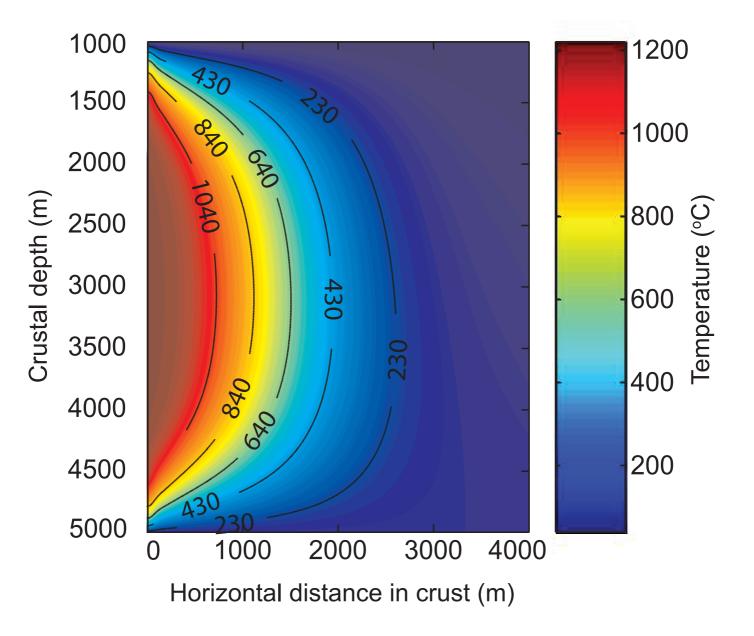
	Depth (km)	5	10	15	20
	Extension rate				
	(mm / yr)				
Solidus	3	1.18 x 10 <sup>6</sup>	8.18 x 10 <sup>5</sup>	4.63 x 10 <sup>5</sup>	2.17 x 10 <sup>5</sup>
	5	3.96 x 10 <sup>5</sup>	2.66 x 10 <sup>5</sup>	1.66 x 10 <sup>5</sup>	8.29 x 10 <sup>4</sup>
	10	1.01 x 10 <sup>5</sup>	6.96 x 10 <sup>4</sup>	4.30 x 10 <sup>4</sup>	2.23 x 10 <sup>4</sup>
	20	2.60 x 10 <sup>4</sup>	1.79 x 10 <sup>4</sup>	1.12 x 10 <sup>4</sup>	6.06 x 10 <sup>3</sup>
	25	1.67 x 10 <sup>4</sup>	1.14 x 10 <sup>4</sup>	7.24 x 10 <sup>3</sup>	3.70 x 10 <sup>3</sup>
600°C	3	8.18 x 10 <sup>5</sup>	5.18 x 10 <sup>5</sup>	2.91 x 10 <sup>5</sup>	1.04 x 10 <sup>5</sup>
Isotherm	5	3.04 x 10 <sup>5</sup>	1.92 x 10 <sup>5</sup>	1.04 x 10 <sup>5</sup>	3.86 x 10 <sup>4</sup>
	10	7.82 x 10 <sup>4</sup>	5.04 x 10 <sup>4</sup>	2.81 x 10 <sup>4</sup>	1.05 x 10 <sup>4</sup>
	20	2.01 x 10 <sup>4</sup>	1.35 x 10 <sup>4</sup>	7.39 x 10 <sup>3</sup>	2.96 x 10 <sup>3</sup>
	25	1.32 x 10 <sup>4</sup>	8.43 x 10 <sup>3</sup>	4.88 x 10 <sup>3</sup>	1.92 x 10 <sup>3</sup>

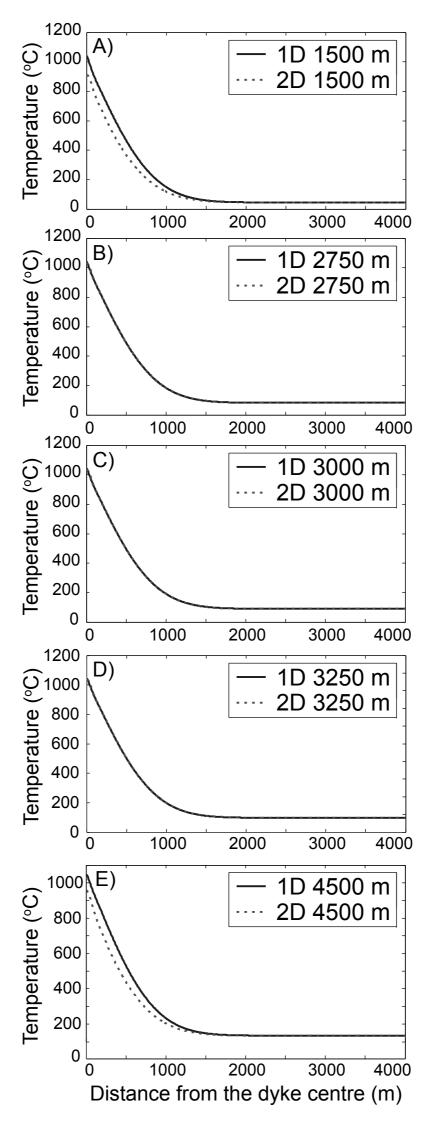












Parameter		Values	Units
T <sub>o</sub>	Initial temperature	0	°C
T <sub>m</sub>	Magma temperature	1320	°C
ω	Dyke half thickness	2.5	m
Χ ∞	Computational domain	100	m
L	Specific latent heat	4 x 10 <sup>5</sup>	J / kg
Cp	Specific heat capacity <sup>a</sup>	1480	J / kg / K
κ	Thermal diffusivity <sup>b</sup>	2.5 x 10 <sup>-7</sup>	m² / s