



THE UNIVERSITY *of* EDINBURGH

Edinburgh Research Explorer

## DEM-LBM simulation of stress-dependent absolute and relative permeabilities in porous media

### Citation for published version:

Huang, J, Xiao, F, Labra, C, Sun, J & Yin, X 2021, 'DEM-LBM simulation of stress-dependent absolute and relative permeabilities in porous media', *Chemical Engineering Science*, vol. 239, pp. 116633.  
<https://doi.org/10.1016/j.ces.2021.116633>

### Digital Object Identifier (DOI):

[10.1016/j.ces.2021.116633](https://doi.org/10.1016/j.ces.2021.116633)

### Link:

[Link to publication record in Edinburgh Research Explorer](#)

### Document Version:

Peer reviewed version

### Published In:

Chemical Engineering Science

### General rights

Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

### Take down policy

The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact [openaccess@ed.ac.uk](mailto:openaccess@ed.ac.uk) providing details, and we will remove access to the work immediately and investigate your claim.



1                   **DEM-LBM Simulation of Stress-dependent Absolute and Relative**  
2                                   **Permeabilities in Porous Media**

3                   Jingwei Huang<sup>1,2\*</sup>, Feng Xiao<sup>2</sup>, Carlos Labra<sup>3</sup>, Jin Sun<sup>3</sup> and Xiaolong Yin<sup>2\*</sup>

4                             1. Department of Petroleum Engineering, Texas A&M University

5                             2. Department of Petroleum Engineering, Colorado School of Mines

6                             3. School of Engineering, University of Edinburgh

7  
8   **Abstract**

9       In this work, stress-dependent absolute and relative permeabilites in porous media are studied  
10 using the discrete element method and lattice Boltzmann method. The change of absolute  
11 permeability and porosity during compaction is found follow a power-law relation. The stress-  
12 dependent absolute permeability in homogeneous pack is in agreement with the prediction of  
13 Carman-Kozeny equation. Porosity exponent is increased due to the existence of vugs but is  
14 decreased with fractures. Relative permeability, on the other hand, is found not only affected by  
15 pore structure of compacted media, but also properties of fluids and rock surface. Our simulations  
16 indicate that relative permeability of wetting phase increases slightly with increasing stress, due to  
17 the formation of more continuous pathways. Relative permeability of non-wetting phase, however,  
18 either increases or decreases depending on viscosity ratio and capillary number. It is found that  
19 lubrication effects play an important role in the stress sensitivity of relative permeability.

20  
21   **Keywords:** Stress sensitivity, absolute/relative permeability, DEM-LBM, lubrication effects

## 23 1. Introduction

24 In subsurface environment, rocks are continuously under the influences of overburden,  
25 confining, and pore pressures. The state of stress in these rocks evolves gradually during geological  
26 time. Rapid changes in stress can be induced by engineering activities such as withdrawal and  
27 replenishment of aquifers [1, 2], primary production of petroleum [3, 4], injection of fluids during  
28 CO<sub>2</sub> sequestration [5, 6] and enhanced oil recovery [7, 8]. Pore shape and pore size are altered by  
29 the change of stress, which results in changes in macroscopic porosity, absolute permeability and  
30 relative permeability of the rock that are central to the rate of flows. Stress sensitivity of intrinsic  
31 rock properties is therefore essential to accurately model the single- and multi-phase flow at  
32 subsurface.

33 Absolute permeability and porosity of rocks vary in a wide range, depending on rock types and  
34 effective stress [9]. Reduction in porosity and absolute permeability by compaction has been well  
35 documented in the literature [3, 10]. Both linear and nonlinear relations have been observed  
36 between absolute permeability/porosity and strain in different porous media [11-14]. When  
37 changed absolute permeability is correlated to changed porosity, a particularly simple correlation  
38 is a power-law

$$39 \left( \frac{\phi}{\phi_0} \right)^A = \frac{k}{k_0} \quad (1)$$

40 where  $\phi_0$  and  $k_0$  are the porosity and permeability at a reference state, respectively, and  $\phi$  and  $k$   
41 are changed porosity and permeability at another stress state.  $A$  is a material constant named the  
42 porosity-sensitivity exponent. The value of  $A$  in the literature varies [15-18], depending on type of  
43 rock and range/history of applied stress [19]. Heterogeneity of rocks also has great impact on  $A$ .  
44 Experimental results showed that  $A$  in fractured rocks are higher than those in carbonates, which  
45 in turn are higher than those in sandstones [20]. It was pointed out that pore throats are more stress

46 sensitive than pore bodies, which would lead to larger values of  $A$  [21]. Similarly, as conductive  
47 fractures are more stress sensitive than pores in rock's matrix, fractured rocks also exhibit larger  
48 values of  $A$  [20].

49 Compared to absolute permeability, fewer attempts have been made to study stress sensitivity  
50 of relative permeability, and findings reported in the literature have significant variability. For gas-  
51 liquid flows, some experiments showed for sandstones that the relative permeability of gas was  
52 not affected by changed overburden pressures [22, 23]. Zhang et al. [24] found for coal that the  
53 relative permeability of gas increased and that of water decreased when the confining pressure was  
54 increased. Experiments from Haghi et al. [25] showed for sandstone, however, that the relative  
55 permeability of water increased but that of nitrogen decreased under increased confining stress.  
56 Experiments conducted on water-oil systems also generated variable results. Some researchers  
57 reported that relative permeability of water slightly increased or did not change while that of oil  
58 decreased under increased stress [26-30]. However, experiments of Wilson [31] indicated that  
59 relative permeability of water decreased and that of oil increased when the overburden pressure  
60 was increased. Hamoud et al. [32] found that stress sensitivity of relative permeability depends on  
61 the range of strain. Their experiments showed that relative permeability of water increased when  
62 strain was less than 2% but decreased when strain was within 2%-15%. Relative permeability of  
63 oil increased when strain was less than 5% but decreased when strain was within 5%-15%. Al-  
64 Quraishi et al. [33] investigated changes in relative permeabilities of sandstones under different  
65 conditions of loading. They found that relative permeability of water increased and that of oil  
66 decreased when the axial stress was increased at fixed confining pressure. Opposite trends were  
67 observed for the relative permeabilities of both phases when the confining pressure was increased  
68 at fixed axial stress. Table 1 summarizes the experimental studies to date on stress sensitivity of

69 relative permeabilities including types of rocks, properties of fluids and rock surface, and  
70 conditions of stress employed.

71 Apart from experiments, some pore-scale numerical simulations have also been conducted  
72 to study the behavior of relative permeability under stress. Fagbemi et al. [34] simulated drainage  
73 and imbibition in a digital sandstone medium under quasi-static triaxial loading. Deformation of  
74 rock was solved using a finite element method and multiphase flow was modeled using a volume  
75 of fluid method. They found the relative permeability of non-wetting phase (oil) decreased when  
76 stress loading was increased and explained it as due to the reduction in the cross-sections of oil's  
77 pathways. The relative permeability of water was not significantly affected. In another study from  
78 the same authors [35], the same methods were applied and relative permeabilities of both wetting  
79 and non-wetting phases decreased with increasing stress. Fan et al. [36] studied the relative  
80 permeability in a proppant-packed hydraulic fracture under compaction. They found that the  
81 relative permeability of oil increased first and then decreased when the effective stress was  
82 increased continuously. The relative permeability of water was less sensitive to the stress.

83 The behavior of relative permeability with stress is highly variable because, unlike absolute  
84 permeability that only depends on the structure and connectivity of pores, relative permeability is  
85 affected by other factors such as wettability, viscosity ratio and capillary number. In the absence  
86 of compaction, it was shown that the relative permeability of water increased when pore surface  
87 became more oil-wet [37]. The relative permeability of the non-wetting phase increased with  
88 increasing viscosity ratio between the non-wetting phase and the wetting phase. The relative  
89 permeability of the wetting phase, on the other hand, was less sensitive to viscosity ratio [38, 39].  
90 On the effect of capillary number, Li et al. [39] and Ramstad et al. [40] both found that relative  
91 permeabilities of wetting and non-wetting phases increased with increasing capillary number. The

92 above studies indicate that when compaction changes the geometry of pores, its effect on relative  
93 permeability should also depend on the state of wettability, viscosity ratio and capillary number.  
94 Existing experiments and simulations on stress sensitivity of relative permeability however have  
95 not evaluated these conditions comprehensively.

96 Pore-scale, direct numerical simulation of two-phase flow is an effective approach to obtain  
97 relative permeability of porous media under controlled conditions, and the lattice Boltzmann  
98 method is a particularly simple and efficient numerical tool. Various multiphase lattice Boltzmann  
99 models have been developed, such as the color-gradient model [41-43], pseudo-potential model  
100 [44, 45], free energy model [46] and mean-field model [47]. They all have been successfully  
101 applied to investigate multiphase flow problems such as co-current flows with viscosity contrast  
102 [39], imbibition and drainage in porous media [48], and multiphase flows with mixed wettability  
103 [49]. Relative permeability has been calculated for both synthetic media [48] and digitalized rocks  
104 [40, 50].

105 In this study, we aim to comprehensively evaluate the stress sensitivity of absolute and relative  
106 permeability in a simple porous medium made by spherical particles. A sphere pack can be  
107 regarded as a standard representation of unconsolidated porous media [14]. Deformations of sphere  
108 pack under isotropic and uniaxial loading conditions were modeled by using discrete element  
109 method (DEM). In this work, only small and linearly elastic deformations were modeled. Single-  
110 and multiphase flows through original and deformed sphere packs at different stages of loading  
111 were simulated by the lattice Boltzmann method (LBM). The rest of the paper is organized as  
112 follows. We first present methods of DEM and LBM applied in this study. Then, original porosities  
113 and absolute permeabilities of sphere packs and changes in them due to stress are presented for  
114 both homogeneous and heterogeneous sphere packs. Finally, relative permeabilities are calculated

115 at different stages of loading for the homogeneous pack, with varied fluid properties and wetting  
116 conditions.

117

Table 1: Summary of experimental results on the stress sensitivity of relative permeability.

Authors (dates)	Fluids	Porous medium	Wettability	Viscosity	Stress condition	Conclusions
Fatt, 1953	Gas-oil	Sandstone	Not reported	Not reported	Overburden pressure	Relative permeability of gas was not affected under 3000 Psi.
Tomas and Ward, 1972	Gas-water	Sandstone	Not reported	Not reported	Overburden pressure	Relative permeability of gas was not significantly affected under 6000 Psi.
Zhang et al. 2017	Gas-water	Coal	Not reported	Not reported	Confining pressure	Relative permeability of water decreased; Relative permeability of gas increased.
Haghi et al. 2019	Nitrogen-water	Sandstone	Not reported	Water: 0.6527 cp Nitrogen: 0.184 cp	Confining pressure	Relative permeability of water increased; Relative permeability of nitrogen decreased.
Wilson, 1956	Brine-oil	Sandstone	Water wet	Oil: 1.7-2.7 cp Brine: not reported	Overburden pressure	Relative permeability of brine decreased; Relative permeability of oil increased.
Ali et al. 1987	Water-oil	Sandstone	Water wet	Not reported	Overburden pressure	Relative permeability of water was not significantly affected; Relative permeability of oil decreased.
Jones et al. 2001	Brine-oil	Sandstone	Strongly water-wet	Oil: 1.33 cp Brine: 1.31 cp	Overburden pressure	Relative permeability of water slightly increased; Relative permeability of oil decreased.
Al-Quraishi and Khairy 2005	Brine-oil	Sandstone	Water wet	Oil: 7.1 cp Brine: 0.98 cp	Overburden pressure	Relative permeability of water lightly increased; Relative permeability of oil decreased.
Gawish and Al-Homadhi 2008	Brine-oil	Sandstone	Water wet	Oil: not reported Brine: 1.06 cp	Overburden pressure	Relative permeability of water was not significantly affected; Relative permeability of oil decreased.
Al-Quraishi et al. 2010	Water-oil	Sandstone	Strongly water-wet	Oil: 18 cp Water: 1 cp	Confining pressure or axial stress	Relative permeability of water increased and that of oil decreased when increasing the axial stress at fixed confining pressure. An opposite trend was found when increasing the confining pressure at fixed axial stress.
Hamoud et al. 2012	Water-oil	Sandstone	Water wet	Not reported	Triaxial compression	Relative permeability of water increased within 0%-2% strain but decreased within 2%-15%; Relative permeability of oil increased within 0%-5% strain but decreased within 5%-15%.
Adenutsi et al. 2019	Water-oil	Artificial core samples	Water wet	Oil: 1.48 cp Water: 0.89 cp	Confining pressure	Relative permeability of water slightly increased; Relative permeability of oil decreased.



## 120 2. Numerical Methods

121 In this section, we briefly explain the numerical methods used in this study. As introduced,  
122 DEM was employed to solve the deformation of porous media. A single-phase LB model was used  
123 for calculation of absolute permeability and a color-gradient LB model was applied to simulate  
124 multiphase flows for characterization of relative permeability.

125

### 126 2.1 Discrete element method

127 Discrete element method (DEM) with bonded particle model has been widely applied to  
128 simulate deformation of granular media, such as rocks [51, 52], soil [53, 54] and porous ceramics  
129 [55]. In DEM, a material is represented by a collection of interacting particles with idealized shape,  
130 e. g., sphere in 3D and disk in 2D. The equations of particle motion can be described by the Newton  
131 and the Euler equations

$$132 \quad m_i \ddot{\mathbf{u}}_i = \mathbf{F}_i \quad (2)$$

$$133 \quad I_i \dot{\boldsymbol{\omega}}_i = \mathbf{T}_i \quad (3)$$

134 where  $m_i$ ,  $\mathbf{u}_i$ ,  $I_i$  and  $\boldsymbol{\omega}_i$  are the mass, displacement, moment of inertia and angular velocity of the  
135  $i$ th particle respectively.  $\mathbf{F}_i$  the force and  $\mathbf{T}_i$  the moment acting on the particle are sums of all forces  
136 and moments applied to the particle

$$137 \quad \mathbf{F}_i = \mathbf{F}_i^{\text{ext}} + \sum_{c=1}^{n_c} \mathbf{F}_i^c + \mathbf{F}_i^{\text{damp}} \quad (4)$$

$$138 \quad \mathbf{T}_i = \mathbf{T}_i^{\text{ext}} + \sum_{c=1}^{n_c} (\mathbf{r}_i^c \times \mathbf{F}_i^c) + \mathbf{T}_i^{\text{damp}} \quad (5)$$

139 where  $\mathbf{F}_i^{\text{ext}}$  and  $\mathbf{T}_i^{\text{ext}}$  are external load,  $n_c$  is the number of particles in contact with the  $i$ th particle,  
140  $\mathbf{r}_i^c$  is the vector connecting the center of the  $i$ th particle with the point of contact  $\mathbf{c}$ ,  $\mathbf{F}_i^c$  is contact  
141 interaction force.  $\mathbf{F}_i^{\text{damp}}$  and  $\mathbf{T}_i^{\text{damp}}$  are force and moment resulted from external damping. When  
142 damping is non-viscous, they are given by

143 
$$\mathbf{F}_i^{damp} = -\alpha^t \|\mathbf{F}_i^{ext} + \sum_{c=1}^{n_c} \mathbf{F}_i^c\| \frac{\dot{\mathbf{u}}_i}{\|\dot{\mathbf{u}}_i\|} \quad (6)$$

144 
$$\mathbf{T}_i^{damp} = -\alpha^r \|\mathbf{T}_i^{ext} + \sum_{c=1}^{n_c} (\mathbf{r}_i^c \times \mathbf{F}_i^c)\| \frac{\dot{\boldsymbol{\omega}}_i}{\|\dot{\boldsymbol{\omega}}_i\|} \quad (7)$$

145 where  $\alpha^t$  and  $\alpha^r$  are damping constants for transitional and rotational motions, respectively.  
 146 Contact laws that include force and moment interactions between particles determine the behavior  
 147 of the system. The contact force can be decomposed into normal component  $\mathbf{F}_{i,n}^c$  and tangential  
 148 component  $\mathbf{F}_{i,t}^c$

149 
$$\mathbf{F}_i^c = \mathbf{F}_{i,n}^c + \mathbf{F}_{i,t}^c \quad (8)$$

150 In the present work, an elastic–perfectly brittle model [56] is used. The contact interface is  
 151 characterized by normal stiffness  $k_n$  and tangential stiffness  $k_t$

152 
$$\mathbf{F}_{i,n}^c = k_n \mathbf{u}_{rn} \quad (9)$$

153 
$$\mathbf{F}_{i,t}^c = k_t \mathbf{u}_{rt} \quad (10)$$

154 where  $\mathbf{u}_{rn}$  and  $\mathbf{u}_{rt}$  are normal and tangential relative displacements, respectively. The tangential  
 155 force is constrained by the Coulomb friction law

156 
$$\|\mathbf{F}_t\| \leq \mu |f_n| \quad (11)$$

157 where  $\mu$  is the friction coefficient. Bonds between particles are broken instantaneously when  
 158 normal or tangential forces exceed their respective bond-strength constraints. For detailed  
 159 information of applied DEM model, the readers are referred to Labra et al. [54].

160

## 161 **2.2 Lattice Boltzmann method**

162 Absolute and relative permeabilities of sphere packs before and after deformation were  
 163 calculated by three-dimensional lattice Boltzmann flow simulators [48, 57]. LBM is a well-  
 164 established computational fluid dynamic (CFD) method. Since it handles no-slip boundary using

165 a simple bounce-back scheme, it is a particularly popular method for modelling fluid flows in  
 166 media with complex geometries [57, 58]. LBM solves the Navier-Stokes equation indirectly by  
 167 simulating the evolution of velocity distribution function, the moments of which give macroscopic  
 168 density and velocity of the flow. When using MRT (multi-relaxation time) collision operator, the  
 169 transport equation for the velocity distribution function is

$$170 \quad f_i(\mathbf{x} + \mathbf{c}_i \Delta t, t + \Delta t) = f_i(\mathbf{x}, t) - \mathbf{M}^{-1} \cdot \mathbf{S} \cdot \mathbf{M} \cdot [f_i(\mathbf{x}, t) - f_i^{eq}] \quad (12)$$

171 where  $f_i(\mathbf{x}, t)$  is the distribution function at position  $\mathbf{x}$  and time  $t$ ,  $f_i^{eq}$  is the equilibrium  
 172 distribution function.  $\Delta t = 1$  is the time step and  $i$  represents propagation direction corresponding  
 173 to lattice velocity  $\mathbf{c}_i$ .  $\mathbf{M}$  is an integer transformation tensor and  $\mathbf{S}$  is diagonal collision matrix [59,  
 174 60]. For two-phase flows, simulations used a color gradient model [48]. In this model,  $f_i^R$  and  $f_i^B$   
 175 are used to represent the velocity distribution functions of two immiscible fluids (red and blue).  
 176 The evolution equation can be written as

$$177 \quad f_i^k(\mathbf{x} + \mathbf{c}_i \Delta t, t + \Delta t) = f_i^k(\mathbf{x}, t) + \Omega_i^k(\mathbf{x}, t) \quad (13)$$

178 In Eqn. (13),  $f_i^k(\mathbf{x}, t)$  is the distribution function of fluid  $k$  ( $k = R$  or  $B$ ).  $\Omega_i^k$  is the collision operator  
 179 that includes three parts:

$$180 \quad \Omega_i^k = (\Omega_i^k)^3 \left[ (\Omega_i^k)^1 + (\Omega_i^k)^2 \right] \quad (14)$$

181 where  $(\Omega_i^k)^1$  is the single-phase collision operator

$$182 \quad (\Omega_i^k)^1 = -(\mathbf{M}^{-1} \mathbf{S} \mathbf{M})_{ij} [f_j - f_j^{eq}] \quad (15)$$

183 in which  $f_j$  is the total distribution function  $f_j = f_j^R + f_j^B$  and  $f_j^{eq}$  is the equilibrium distribution  
 184 of total distribution function.  $(\Omega_i^k)^2$  is the two-phase collision operator

$$185 \quad (\Omega_i^k)^2 = \frac{A}{2} |\nabla \rho^N| \left[ \omega_i \frac{(\mathbf{c}_i \cdot \nabla \rho^N)^2}{|\nabla \rho^N|^2} - B_i \right] \quad (16)$$

186 where  $\omega_i$  and  $B_i$  are weighting coefficients,  $A$  is a parameter that controls interfacial tension  $\sigma$  that  
 187 can be determined through static drop simulations.  $\rho^N$  is a phase field function defined as

$$188 \quad \rho^N(\mathbf{x}, t) = \frac{\rho_R(\mathbf{x}, t) - \rho_B(\mathbf{x}, t)}{\rho_R(\mathbf{x}, t) + \rho_B(\mathbf{x}, t)} \quad (17)$$

189 where  $\rho_R$  and  $\rho_B$  are densities of the red and the blue fluids, respectively.  $(\Omega_i^k)^3$  is the recoloring  
 190 operator that forces phase separation

$$191 \quad (\Omega_i^R)^3(f_i^R) = \frac{\rho_R}{\rho} f_i + \beta \frac{\rho_R \rho_B}{\rho^2} \cos(\varphi_i) f_i^{eq}(\rho, 0) \quad (18)$$

$$192 \quad (\Omega_i^B)^3(f_i^B) = \frac{\rho_B}{\rho} f_i - \beta \frac{\rho_R \rho_B}{\rho^2} \cos(\varphi_i) f_i^{eq}(\rho, 0) \quad (19)$$

193 where  $\rho$  is total density ( $\rho = \rho_R + \rho_B$ ),  $\beta$  is a free parameter controls interface thickness, and  $\varphi_i$   
 194 is the angle between the gradient of the phase field  $\nabla \rho^N$  and  $\mathbf{c}_i$ .

195 As to boundary conditions, the link-bounce-back scheme of Frisch et al. [61] was used to  
 196 recover the no-slip boundary condition on fluid-solid surfaces. To implement wettability, it was  
 197 assumed that the solid wall is a mixture of two fluids with a certain value of  $\rho^N$  [49, 62]. For  
 198 instance, if the contact angle of red fluid is  $\theta$ ,  $\rho^N$  should be set as  $\cos \theta$ . For detailed information  
 199 of applied two-phase LB models, the readers are referred to Huang et al. [48].

200

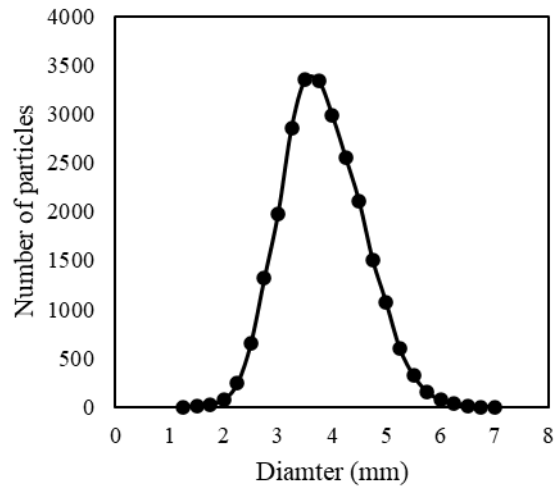
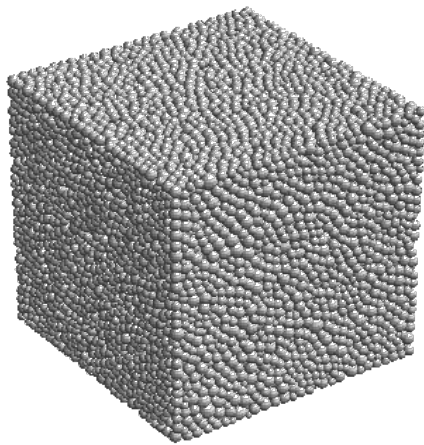
### 201 3. Numerical Results and Discussions

202 In this section, we first introduce the porous medium built by spherical particles. The changes  
 203 in porosity and absolute permeability by compaction were then studied in both homogeneous and  
 204 heterogeneous sphere packs. Both hydrostatic and uniaxial loading were investigated. In the end,  
 205 relative permeabilities of homogeneous packs were calculated for both loading conditions, with  
 206 effects of wettability, viscosity ratio and capillary number evaluated.

207

208 **3.1 Sphere packs under stress**

209 To study the effect of stress on permeability, a porous medium made up by spherical particles  
210 was built using a dense packing algorithm [63]. As shown in Figure 1(a), the porous medium  
211 consists of 25,277 spherical particles filling a cubic domain of 9 cm × 9 cm × 9 cm, bounded by  
212 six flat solid walls (not shown). The distribution of particle size is Gaussian, shown in Figure 1(b).  
213 The smallest and the largest particles have diameters of 1.34 mm and 6.64 mm, respectively.  
214 Number-averaged particle diameter is 3.71 mm. The initial net porosity of the medium is 0.2281.  
215



216

217

218 Figure 1. Porous medium built by the dense packing algorithm (a) and distribution of particle  
219 size (b).

220

221 DEM was then applied to model compaction of the medium under stress. Parameters of particle-  
222 particle interactions in DEM and resulted bulk mechanical properties of the medium are listed in  
223 Table 2. Both hydrostatic loading and uniaxial loading were tested, as illustrated in Figure 2. These  
224 loadings were implemented by moving the bounding walls. In uniaxial loading, only the walls

225 bounding the  $y$  direction of the medium were moved and those bounding  $x$  and  $z$  directions were  
 226 fixed. In hydrostatic loading, all three pairs of walls were moved. Three stages of strain were  
 227 simulated for each condition of loading, and the maximum strain reached at the third stage is about  
 228 2%. Figure 3 presents the reduction in porosity of the medium with strain. Porosity is normalized  
 229 by its initial value (0.2281) before loading. In hydrostatic loading, porosity was decreased by  
 230 11.5% at the maximum strain. In uniaxial loading, maximum reduction in porosity was about 5.4%.  
 231 Porosity of the medium decreased linearly with strain under the hydrostatic loading condition. For  
 232 uniaxial loading the trend is slightly nonlinear.

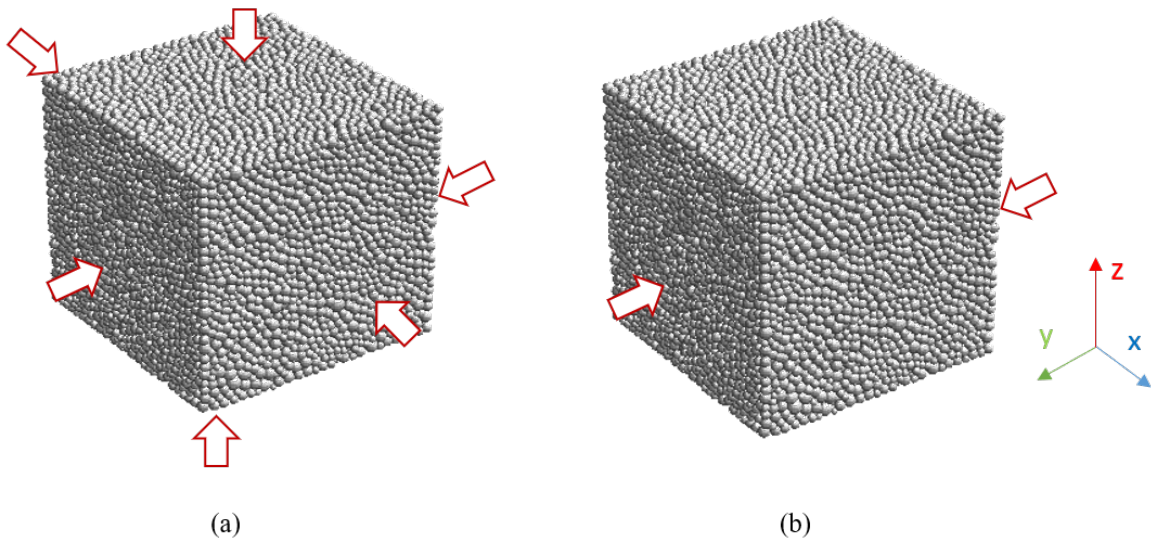
233

234 Table 2. Particle-particle interaction model parameters for DEM and porous medium bulk

235 mechanical properties [20].

Particle normal stiffness (MN/m)	60.37
Particle tangential stiffness (MN/m)	11.47
Particle friction coefficient	0.5
Bond normal strength (kN)	2.81
Bond tangential strength (kN)	1.12
Young's modulus (GPa)	18.7
Poisson's ratio	0.21
Compressive strength (GPa)	1.27
Tensile strength (GPa)	0.12

236

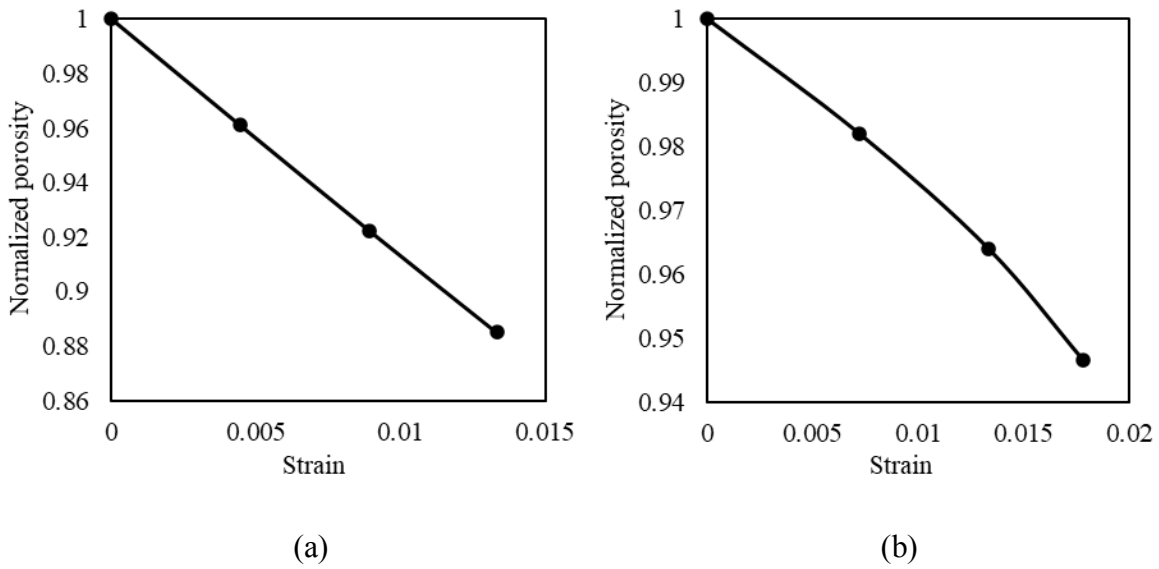


237

238

Figure 2. Porous medium under hydrostatic loading (a) and uniaxial loading (b).

239



240

241

242 Figure 3. Relations between porosities of porous medium and external strains during hydrostatic  
 243 loading (a) and uniaxial loading (b).

244

### 245 3.2 Absolute permeability under stress

246 In this section, we present stress sensitivity of absolute permeability. Fluid flow was simulated

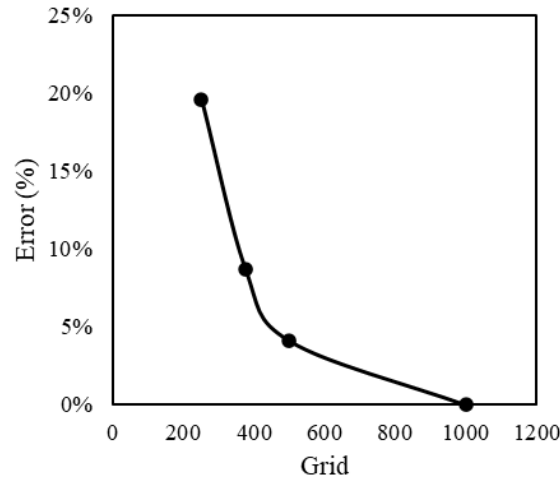
247 by using a single-phase LBM. A constant external body force  $F = 1 \times 10^{-5}$  was used to drive the  
248 flows. The viscosity of fluid is 0.1667 by setting relaxation time as one. When MRT collision  
249 operator is applied, calculated permeability is independent of relaxation time [39, 48]. The Mach  
250 number of the system was in the magnitude of  $10^{-7}$ . After flows became steady, absolute  
251 permeabilities of the medium before and after compaction were calculated by Darcy's law, using  
252 viscosity of the fluid, body force, and the steady superficial velocity of the fluid through the  
253 medium.

254 The medium before compaction was resolved by a  $N \times N \times N$  cubic lattice. It is known that  
255 resolution can affect calculated permeability [39]. Thus, a convergence test was first conducted by  
256 setting  $N$  to 250, 375, 500, and 1000. Errors of calculated absolute permeabilities along  $x$  direction  
257 of the original medium are presented in Figure 4. These errors are defined as  $|k_N - k_{1000}|/k_{1000}$ ,  
258 where  $k_N$  is the absolute permeability using resolution  $N$ . Figure 4 shows that the relative error  
259 between the case with  $N = 500$  and that with  $N = 1000$  is within 4%. To save computational time,  
260 a  $500^3$  computational domain was used to resolve the medium. When  $N = 500$ , the size of a voxel  
261 is  $180^3 \mu\text{m}^3$ . Under this resolution, spheres are resolved by 21 voxels in average along their  
262 diameters and the smallest sphere is resolved by 7 voxels. Compacted media were resolved at the  
263 same resolution, i.e.  $180^3 \mu\text{m}^3$ . Lattices for compacted media were therefore slightly shorter than  
264 the original  $N^3$  lattice along the direction of compaction, by about ten lattices at the maximum  
265 strain of 2%. We note that, since in DEM compaction of the medium was achieved by movement  
266 of the confining walls, there are ordered, high-porosity zones near the walls where particles are  
267 excluded. These zones, if not excluded from simulations, would create high-permeability pathways  
268 and affect absolute permeabilities. To exclude these zones from simulations, a  $400^3$  sub-domain in  
269 the center of the larger domain was used in the flow simulations. Periodic boundary conditions



270 were applied on all sides of simulated domain.

271



272

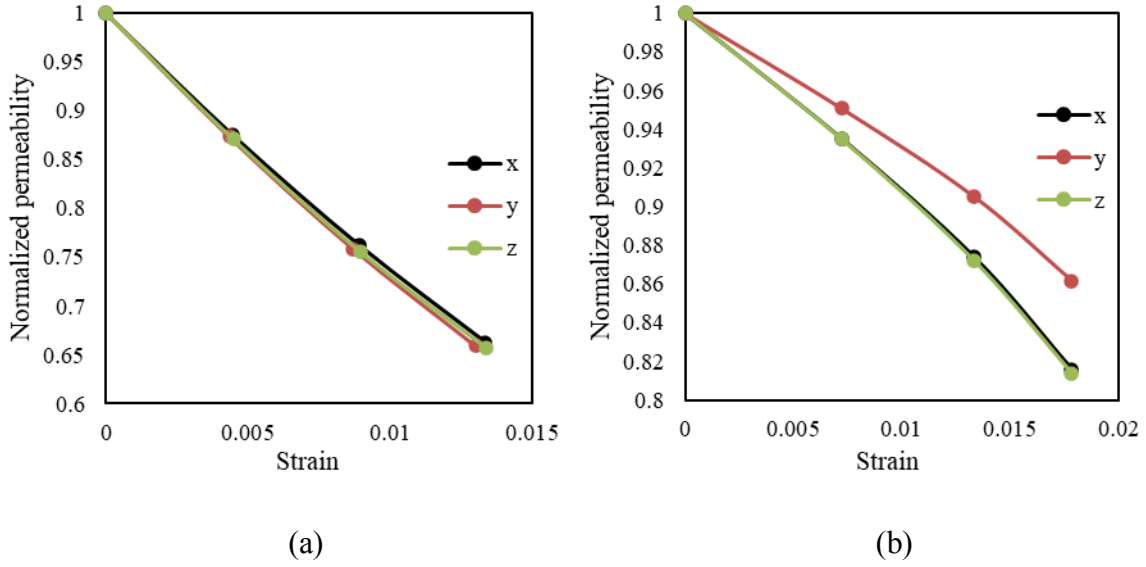
273 Figure 4. Effect of grid resolution on convergence of the absolute permeability of the original  
274 medium.

275

276 Absolute permeabilities of compacted media in three directions are presented in Figure 5 as  
277 functions of strain. These absolute permeabilities are normalized using the original permeabilities  
278 of the medium before compaction, which are very close to each other due to the isotropy of the  
279 medium:  $1.52 \times 10^{-9} m^2$ ,  $1.53 \times 10^{-9} m^2$ , and  $1.54 \times 10^{-9} m^2$  in  $x$ ,  $y$ , and  $z$  directions,  
280 respectively. Figure 5 shows that the absolute permeability is reduced by 34% at the maximum  
281 strain under the hydrostatic loading condition. In the case of uniaxial loading, the maximum  
282 reduction of absolute permeability is 14% in the direction of applied stress ( $y$  direction) and 19%  
283 in the lateral directions ( $x$  and  $z$  directions). Similar to the changes in porosity in Section 3.1,  
284 absolute permeability decreased linearly under the hydrostatic loading condition and nonlinearly  
285 under the uniaxial loading condition in all directions. Changed porosity and permeability during  
286 compaction follow the power-law relation in Eqn. (1). Figure 6 shows that linear relations were

287 present between  $\log_{10}(k/k_0)$  and  $\log_{10}(\phi/\phi_0)$  in all directions. The slopes of the lines gave  
 288 porosity exponents  $A$ , summarized in Table 3.

289

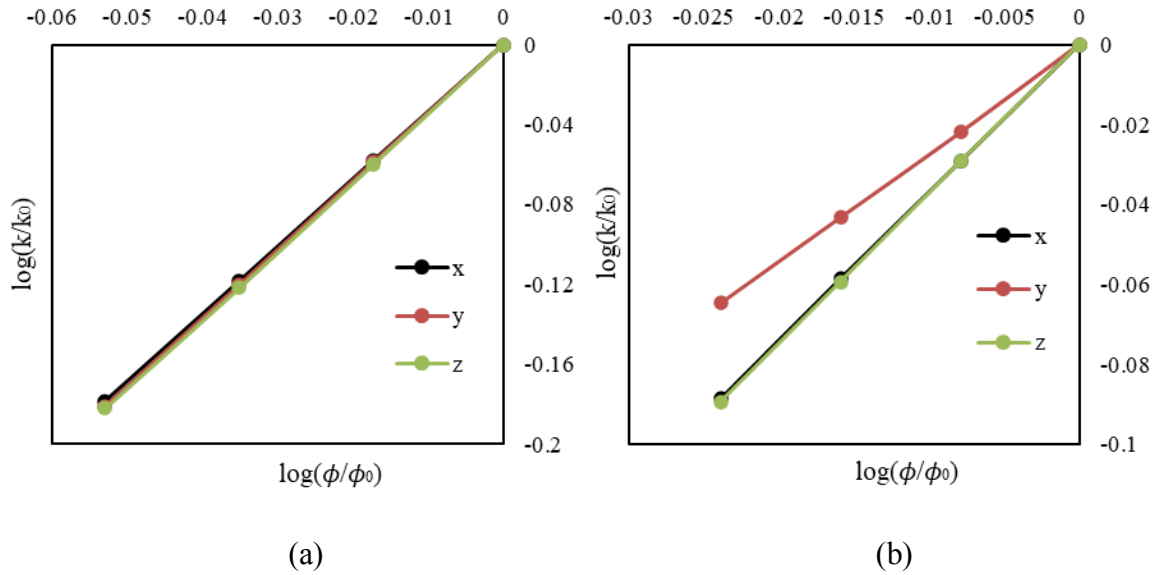


290

291

292 Figure 5. Relations between absolute permeabilities of porous medium and external strains under  
 293 hydrostatic loading (a) and uniaxial loading (b).

294



295

296

297 Figure 6. Changes in porosity correlated to changes in permeability under the hydrostatic loading  
 298 condition (a) and the uniaxial loading condition (b).

299

300 Table 3. Porosity exponents of homogeneous sphere pack

Hydrostatic loading			Uniaxial loading		
$A_x$	$A_y$	$A_z$	$A_x$	$A_y$	$A_z$
3.4	3.5	3.5	3.8	2.8	3.8

301

302 We note that according to the Carman-Kozeny equation

$$303 \quad k = \frac{\phi^3(1-\phi)^2}{C\tau^2S^2} \quad (20)$$

304 where  $\tau$  is the tortuosity,  $C$  is a constant and  $S$  is the surface area of connected pores per unit solid  
 305 volume,  $A$  should take the value of three if tortuosity, surface area and solid volume are nearly  
 306 independent of stress and changes in  $\phi$  and  $k$  are small relative to  $\phi_0$  and  $k_0$ . Under the  
 307 hydrostatic loading condition,  $A_x, A_y, A_z$  are nearly identical due to the isotropy of the medium  
 308 and that of the applied stress. Moreover, all of them are close to the theoretical value of three from  
 309 the Carman-Kozeny equation. Under the uniaxial loading condition,  $A_x$  and  $A_z$  are identical as  
 310 expected, and they are both larger than  $A_y$ , which indicates that this loading condition generated  
 311 anisotropy in the absolute permeability, and those along the lateral directions ( $x$  and  $z$  direction)  
 312 are more sensitive to porosity compaction.

313 In a previous experimental study [19], porosity and permeability changes in sandstones,  
 314 carbonates and fractured sandstones and carbonates under hydrostatic stress conditions were  
 315 reported. Between the initial and the maximum stress levels, generally 6-8 points were taken to

316 obtain the porosity exponent  $A$ . As shown in Table 4, porosity exponents  $A$  in unfractured  
 317 sandstone cores were in the range 1.9-2.3. There is general agreement between the exponents from  
 318 simulations and those from the Carman-Kozeny equation and experiments. This agreement  
 319 indicates that stress sensitivity of porosity and absolute permeability of our medium is mostly  
 320 similar to those of an idealized capillary tube bundle and the tight sandstones previously studied.  
 321

Table 4. Porosity exponents in real rocks from experiments of Petunin et al. [19], under hydrostatic loading condition.

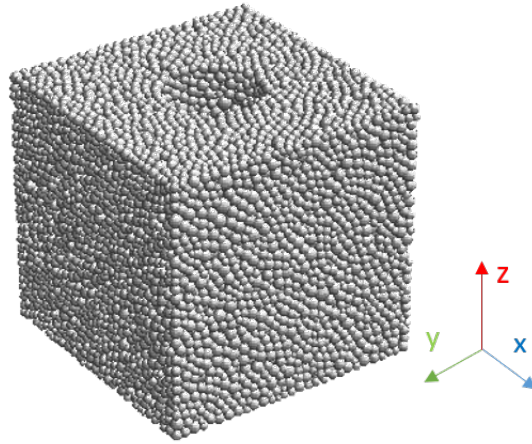
Rock Type	$A$ , range	$A$ , average	$A$ , median	Porosity	Permeability
Tight Sandstones	1.9-2.3	2.1	2.1	~9%	~0.04 md
Carbonates	2.7-40	11.5	10	3.9%-28.2%	0.002-5 md
Fractured cores	11-128	36	31	n/a	3.8-1150 md

322  
 323 Experimental data additionally indicate that values of  $A$  are higher in unfractured carbonates  
 324 and fractured cores.  $A$  varied from 2.7 to 40 in unfractured carbonates and from 11 to 128 in  
 325 fractured cores. High values of  $A$  in carbonates and fractured cores were attributed to their  
 326 heterogeneous pore structure and dual-porosity nature [19, 20]. Pore throats or fractures that  
 327 control the overall permeabilities of cores only contribute to a small fraction of the net porosity. If  
 328 they are also the “weakest” parts of the net porosity that are collapsed during a compaction, a small  
 329 reduction in porosity from collapsed pore throats or fractures can lead to a very high reduction in  
 330 permeability, generating high values of  $A$  [21]. Take carbonates as an example: many carbonates  
 331 contain vugs that contribute significantly to the overall porosity. These vugs, however, do not form  
 332 a continuous flow path and permeability is controlled by much smaller pores that connect the vugs.

333 During a compaction, a certain fraction of porosity reduction, if occurred in the vugs, would not  
334 significantly affect permeability of the medium. If, however, this fraction of reduction occurs to  
335 the connecting pores, drastic reduction in the absolute permeability of the medium is to be  
336 expected.

337 To study stress sensitivity of absolute permeability in heterogeneous media, we constructed a  
338 model of a vuggy porous medium as shown in Figure 7. Within the homogeneous sphere pack, a  
339 large cylindrical tube free of particles was created along the  $z$  direction. The diameter of the tube  
340  $d$  is 3 cm. The net porosity of this sphere pack with tube is now 0.3484 before compaction. For  
341 flows along  $x$  and  $y$  directions this cylindrical tube acts as a vug, and absolute permeabilities  
342 before compaction along these two directions,  $2.18 \times 10^{-9} m^2$  and  $2.17 \times 10^{-9} m^2$ , were only  
343 moderately increased compared to those of the original medium ( $1.52 \times 10^{-9} m^2$ ,  $1.53 \times$   
344  $10^{-9} m^2$ ). Permeability along the  $z$  direction, however, is dominated by the tube at  
345  $4.54 \times 10^{-6} m^2$ . The cylindrical tube is acting like a fracture in this case. The obtained  $z$ -  
346 permeability is in excellent agreement with the analytical permeability of a medium with a single  
347 cylindrical pore:  $\phi_A d^2/32 = 4.58 \times 10^{-6}$ , where  $\phi_A$  is the area fraction of the pore (0.163 in this  
348 case).

349



350

351

Figure 7. Heterogeneous sphere pack with a cylindrical tube in the center.

352

353

354

355

356

357

358

359

360

361

362

363

364

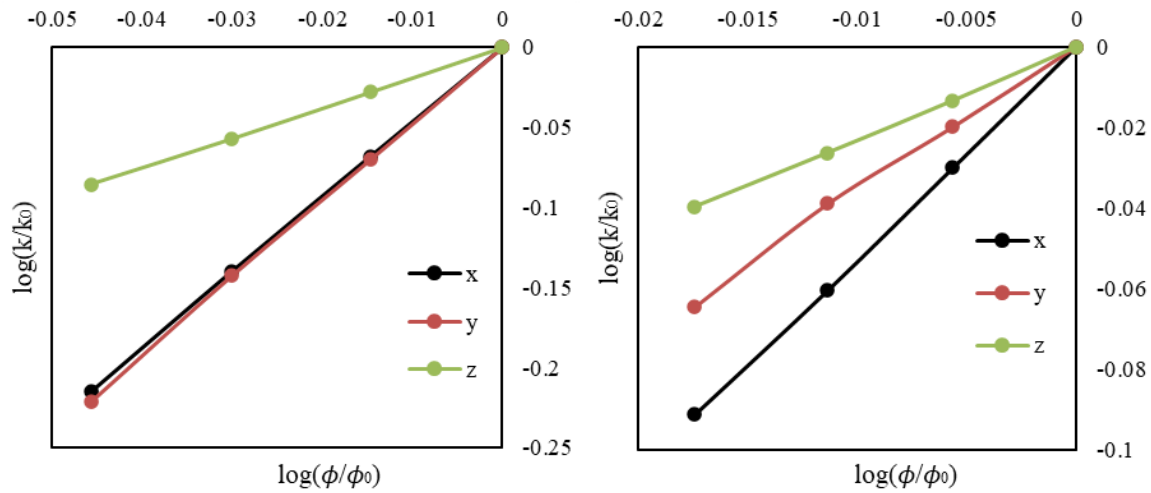
365

366

Following the same procedure for the homogeneous medium, we compacted this heterogeneous medium with tube under hydrostatic and uniaxial loading conditions using DEM and obtained changes in permeabilities using LBM. Figure 8 shows that linear relations persisted between  $\log_{10}(k/k_0)$  and  $\log_{10}(\phi/\phi_0)$  in all directions, indicating that the power-law correlation between  $k/k_0$  and  $\phi/\phi_0$  still exists. Porosity exponents  $A$  of this heterogeneous medium pack are presented in Table 5. With hydrostatic loading, along  $x$  and  $y$  directions  $A_x$  and  $A_y$  increased from 3.4~3.5 of the original medium to 4.7~4.9, indicating that permeability-controlling pores in the medium were more severely compacted. Isolated vugs therefore could indeed increase porosity exponent  $A$ . Along the  $z$  direction,  $A_z$  decreased from 3.5 to 1.9. Different from flows along  $x$  and  $y$  directions, flow and permeability along  $z$  is dominated by the cylindrical tube. At the end of compaction, pore volume of the cylinder only decreased by 1.34%. In contrast, pore volume of the entire medium decreased by 13.6%. The permeability of the medium did not decrease significantly because the volume of the cylinder did not change significantly. Thus, a lower  $A_z$  was observed. With uniaxial loading,  $A_x$  and  $A_y$  of the vuggy medium increased to 5.2 and 3.7, respectively. By

367 comparing to those of the homogenous medium ( $A_x = 3.8, A_y = 2.8$ ), we observed that the tube  
 368 in the role of an isolated vug increased porosity exponent.  $A_z$  on the other hand decreased, from  
 369 3.8 to 2.3, similar to hydrostatic loading.

370



371

372

373 Figure 8. Relations between changes of porosities and permeabilities in heterogeneous sphere  
 374 pack; hydrostatic loading (a); uniaxial loading (b).

375

376

Table 5. Porosity exponents of the heterogeneous sphere pack

Hydrostatic loading			Uniaxial loading		
$A_x$	$A_y$	$A_z$	$A_x$	$A_y$	$A_z$
4.7	4.9	1.9	5.2	3.7	2.3

377

### 378 3.3 Relative permeability under stress

379 In this section, stress sensitivity of relative permeability is evaluated using a color-gradient LB  
 380 model. Validation of the applied model was conducted through simulation of a layered two-phase

381 flow in a 2D horizontal channel. The width of the channel is  $2b$  ( $-b \leq y \leq b$ ). The non-wetting  
382 fluid was placed in the center of the channel ( $-a \leq y \leq a$ ) and the wetting fluid was placed near  
383 solid walls at  $y = \pm b$ . The channel was bounded by periodic boundaries in the  $x$  direction. A  
384 constant body force  $F$  in the  $x$  direction was applied to both fluids, leading to quadratic velocity  
385 profiles in the channel

$$386 \quad u_x(y) = \begin{cases} A_1 y^2 + C_1, & |y| < a \\ A_2 y^2 + B_2 y + C_2, & a \leq |y| \leq b \end{cases} \quad (21)$$

387 In Eq. (21),  $A_1 = -\frac{F}{2\mu_{nw}}$ ,  $A_2 = -\frac{F}{2\mu_w}$ ,  $B_2 = 2(A_1 M - A_2)a$ ,  $C_1 = (A_2 - A_1)a^2 - B_2(b - a) -$   
388  $A_2 b^2$ , and  $C_2 = -A_2 b^2 - B_2 b$ .  $M = \frac{\mu_{nw}}{\mu_w}$  is the viscosity ratio of the fluids. From the velocity  
389 profiles, the relative permeabilities of the two fluids are [64]

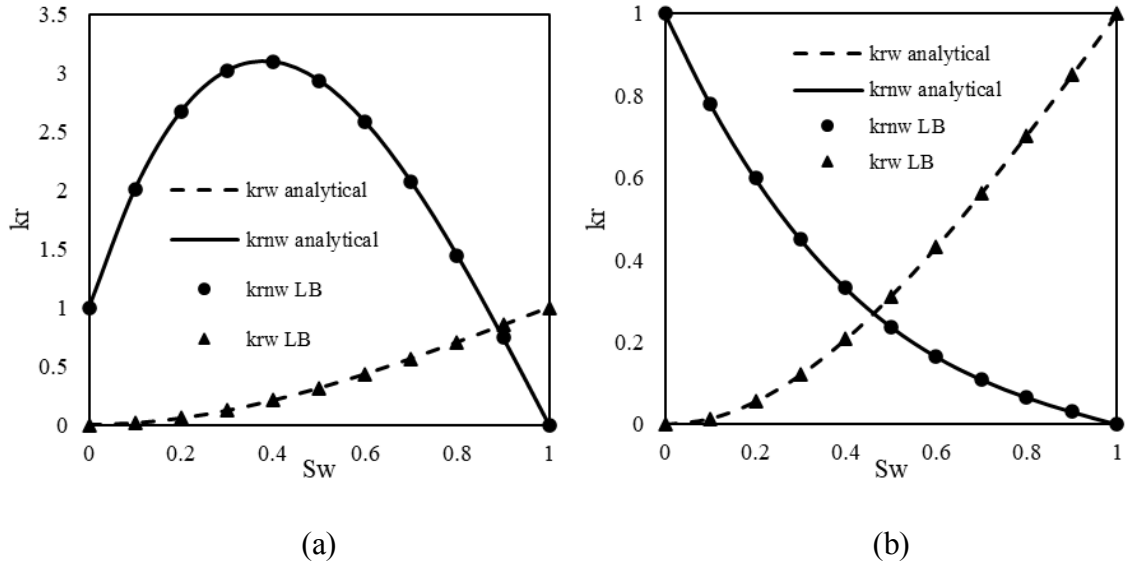
$$390 \quad k_{rw} = \frac{1}{2} S_w^2 (3 - S_w) \quad (22)$$

$$391 \quad k_{rnw} = S_{nw} \left[ \frac{3}{2} M + S_{nw}^2 \left( 1 - \frac{3}{2} M \right) \right] \quad (23)$$

392 where  $k_{rw}$  and  $k_{rnw}$  are relative permeabilities of wetting fluid and non-wetting fluid respectively,  
393  $S_w$  and  $S_{nw}$  are the saturations of wetting fluid and non-wetting fluid respectively. The relative  
394 permeability is calculated by using the extended Darcy's law [39]. In simulation, the size of the  
395 channel was  $10 \times 100$ . Simulated relative permeabilities are compared with analytical solutions  
396 in Figure 9, using two viscosity ratios ( $M = 0.2$  and  $5$ ). Our simulated relative permeabilities match  
397 well with analytical solutions for both cases.

398





399

400

401 Figure 9. Comparison of relative permeabilities of layered two-phase flows in a channel, (a)  $M =$   
 402  $5.0$ ; (b)  $M = 0.2$ .

403

404 In the study of stress-dependent relative permeability, we only studied homogenous medium.

405 To obtain a steady relative permeability for heterogeneous medium, it is required that fluids travel

406 through pore space representative of the entire domain several times. For LB simulations of

407 multiphase flows in porous media, we also need to keep the Mach number of the flow small to

408 reduce compressibility error and control the capillary number. This requirement means hundreds

409 of millions of time steps are generally needed. Though our simulator is parallelized, such a

410 simulation in 3D is still not practical. Thus, two-phase flows through heterogeneous medium,

411 where it is needed that fluids flow through not only the matrix of the medium but also the

412 embedded tube, was not attempted. In two-phase flow simulations carried out for the compacted

413 homogeneous medium, a  $200^3$  computational domain was taken from the center of the  $400^3$

414 domain used in single-phase flow simulations to reduce computational cost. Since the strain of the

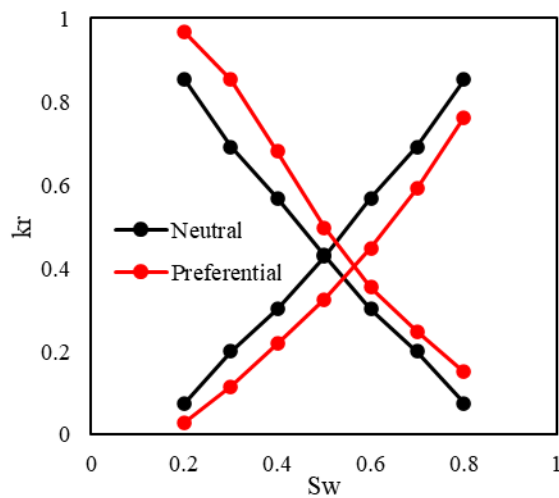
415 medium is relatively small and changes in relative permeability are not as significant as that in

416 absolute permeability, only the uncompacted medium and the medium at the final stage of  
417 compaction were studied. For the homogeneous medium, the reduced domain is still a good  
418 representation of the medium because its porosity and permeability are only different from those  
419 of the larger domain by 0.2% and 3.5%, respectively. In the simulations, periodic boundary  
420 condition was applied to all sides. Saturation was established by initializing all fluid nodes  
421 probabilistically, i.e. a fluid node's probability to be assigned with the wetting fluid is  $S_w$ . After  
422 initialization, a body force of  $F = 10^{-4}$  was assigned to the fluids along the direction of interest.  
423 Densities of fluids are identical. When there is a viscosity contrast, velocities of different phases  
424 are not the same, and it is not straightforward to calculate the capillary number using its common  
425 definition. In some work [64, 65], a capillary number  $Ca = F/\sigma$ , where  $\sigma$  is the interfacial tension,  
426 was used to characterize the flows. However, we found such a capillary number is not  
427 dimensionless. Instead, we defined the capillary number as  $Ca = Fk_a/\sigma$ , where  $k_a$  is the absolute  
428 permeability of uncompacted medium. For medium compacted by hydrostatic loading, relative  
429 permeabilities for flows along  $x$ ,  $y$ , and  $z$  directions are very similar. For this reason, we will only  
430 present results obtained with  $F$  set in the  $x$  direction. For medium compacted by uniaxial loading,  
431 we found that relative permeability was not affected by compaction, when flow was aligned to the  
432 direction of compaction ( $y$ ). Thus, only relative permeabilities of flows along  $x$  and  $z$  directions  
433 are presented.

434 On the effect of wettability, Figure 10 presents the relative permeabilities of the original sphere  
435 pack using two different contact angles:  $\theta = 90^\circ$  and  $30^\circ$ . In these cases, the two fluids have equal  
436 viscosity,  $\sigma = 0.0167$ , and  $Ca = 2.9 \times 10^{-4}$ . Changing the wetting condition from neutral ( $90^\circ$ )  
437 to preferential ( $30^\circ$ ) decreased the relative permeability of the wetting fluid and increased that of  
438 the non-wetting fluid which was also reported in previous studies [39, 66]. Figure 11 presents the

439 stress sensitivity of these two sets of relative permeabilities under different conditions of loading.  
 440 Figure 11a and Figure 11b are for hydrostatic loading and Figure 11c and Figure 11d are for  
 441 uniaxial loading. These cases show that, although porosity and permeability were clearly changed  
 442 by compaction, relative permeability curves were nearly not affected. It is only in the medium with  
 443 preferential wettability that we found the relative permeability of the wetting phase slightly  
 444 increased. This observed increase may be attributed to increased accumulation of the wetting phase  
 445 near pore throats. We note that slightly increased relative permeability of the wetting phase has  
 446 been found in some experimental studies [31, 33].

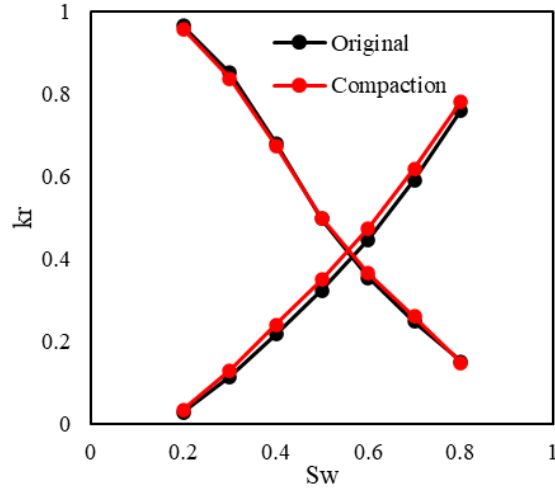
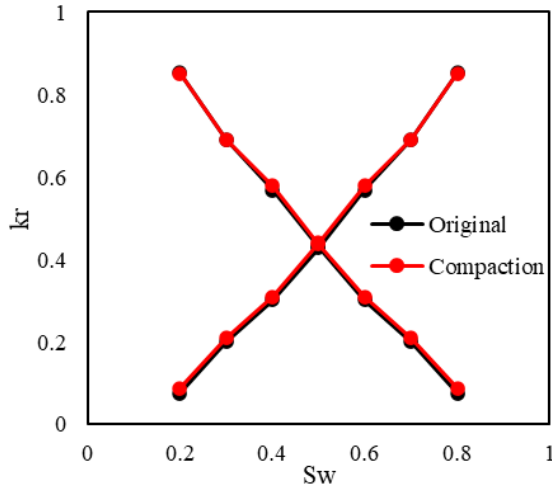
447



448

449 Figure 10. Effect of wettability on the relative permeability of the original medium. Black lines  
 450 are at neutral wetting condition ( $\theta = 90^\circ$ ) and red lines are at preferential wetting condition ( $\theta =$   
 451  $30^\circ$ ).

452

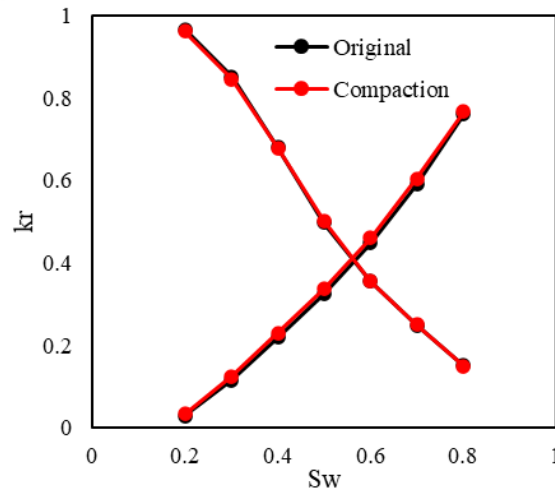
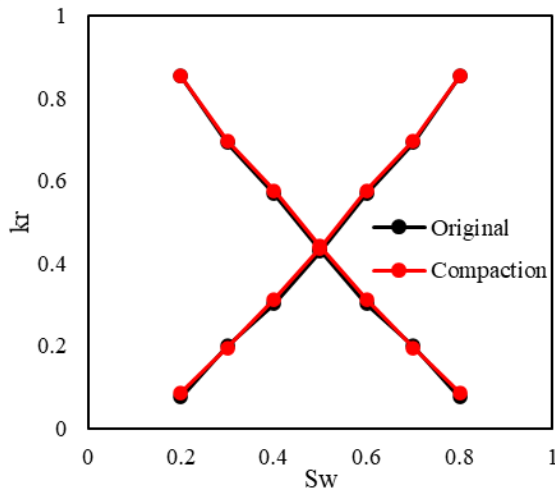


453

454

(a)

(b)



455

456

(c)

(d)

457 Figure 11. Relative permeabilities of compacted media with neutral and preferential wettability;

458 (a) hydrostatic loading,  $\theta = 90^\circ$ ; (b) hydrostatic loading,  $\theta = 30^\circ$ ; (c) uniaxial loading,  $\theta = 90^\circ$ ;

459 (d) uniaxial loading,  $\theta = 30^\circ$ .

460

461 Whereas the sole influence of wettability to relative permeability was identified to be modest,

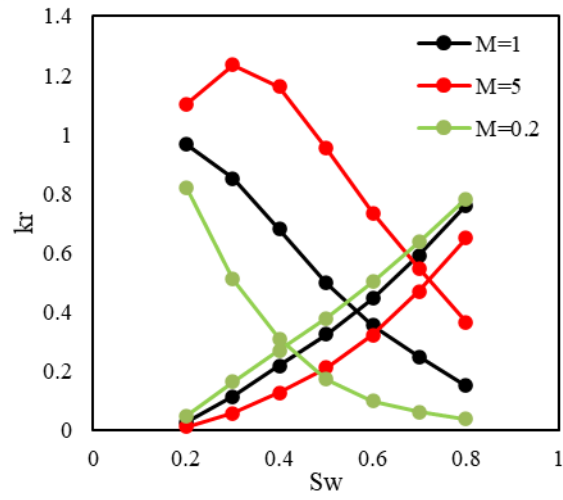
462 the dependence of relative permeability on viscosity ratio was found to be significant. Figure 12

463 presents the relative permeabilities of the uncompact medium at three different viscosity ratios

464 ( $M = 5, 1, 0.2$ ). In these cases,  $\theta = 30^\circ$ ,  $\sigma = 0.015$ , and  $Ca = 3.3 \times 10^{-4}$ . It is observed that  
465 relative permeability of the non-wetting phase increased with increasing  $M$ , and that of the wetting  
466 phase decreased. The influence of viscosity ratio on the relative permeability was much stronger  
467 for the non-wetting phase. This is because the wetting phase occupies small pores and corners of  
468 large pores, flow of the non-wetting phase tends to occur through centers of pores and it is  
469 significantly facilitated by films of wetting phase on the solid when the non-wetting phase is the  
470 more viscous. The dependence of relative permeability on viscosity ratio is well known as the  
471 lubrication effect and has been well discussed in the literature [39, 48].

472 Figure 13 presents stress sensitivity of relative permeabilities of cases of the highest and the  
473 lowest  $M$ , under hydrostatic and uniaxial loading conditions. Figure 13a and Figure 13b are for  
474 hydrostatic loading and Figure 13c and Figure 13d are for uniaxial loading. We found that  
475 hydrostatic loading and uniaxial loading have similar influences over the relative permeability  
476 curves. Relative permeabilities of the wetting phase were slightly increased by compaction,  
477 regardless of viscosity ratio. Compaction affects relative permeability of the non-wetting phase  
478 more than relative permeability of the wetting phase. This is in agreement with previous  
479 experimental studies [26, 27, 30]. Moreover, relative permeabilities of the non-wetting phase were  
480 increased by compaction when  $M = 5$ . They, however, were decreased by compaction when  $M =$   
481  $0.2$ . These trends were observed under both loading conditions but were clearer in the case of  
482 hydrostatic loading because of stronger compaction of pores. This is because the smaller pores and  
483 corners of pores in the medium were more easily compacted by stress, which is beneficial to the  
484 formation of thin films of wetting phase on rock surface. Thus, lubrication effect should be more  
485 significant in this compacted media, which explains the trend observed in altered relative  
486 permeability.

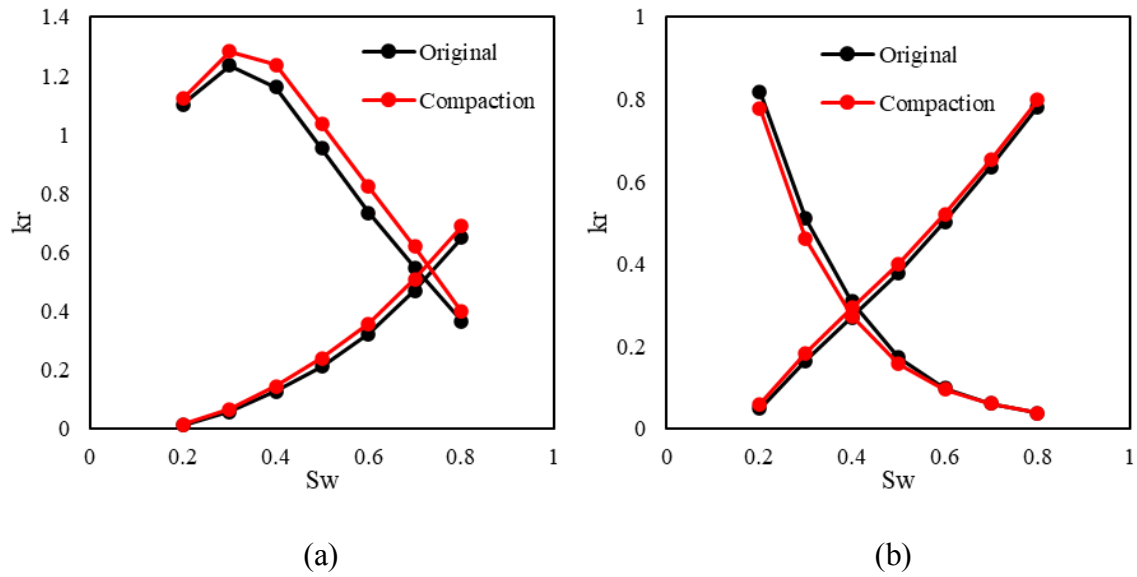
487



488

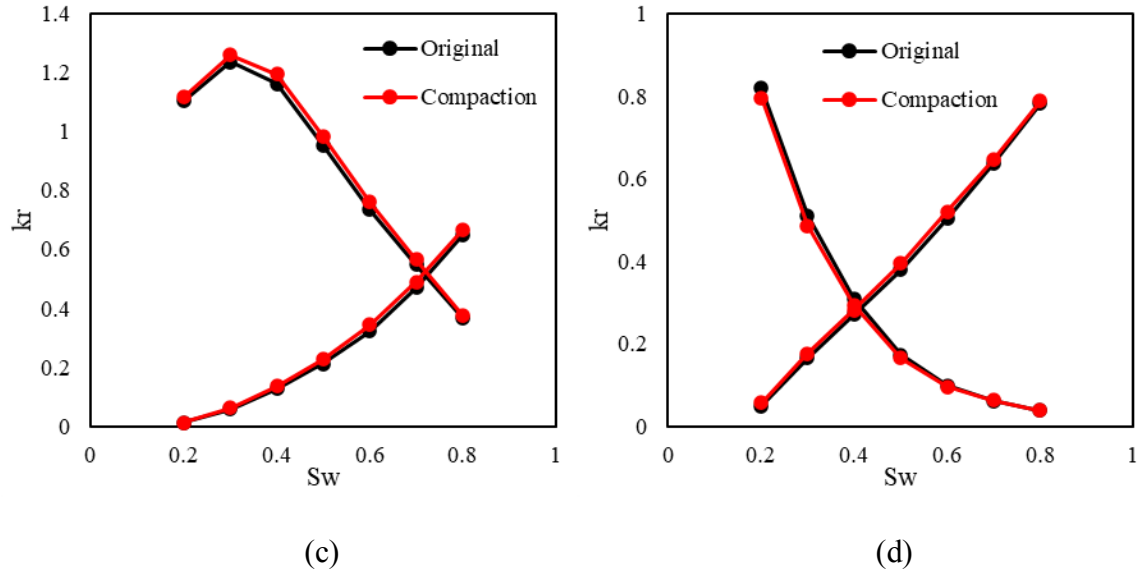
489 Figure 12. Effect of wettability on relative permeability in the original, uncompacted medium.

490



491

492



493

494

495 Figure 13. Relative permeabilities of compacted media under (a) hydrostatic loading condition,  
 496  $M = 5$ ; (b) hydrostatic loading condition,  $M = 0.2$ ; (c) uniaxial loading condition,  $M = 5$ ; (d)  
 497 uniaxial loading condition,  $M = 0.2$ .

498

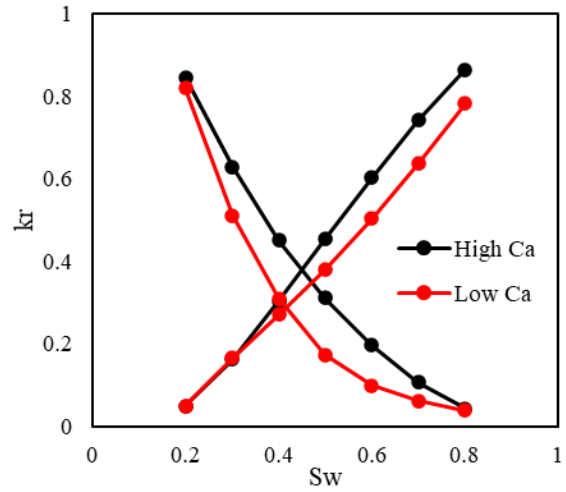
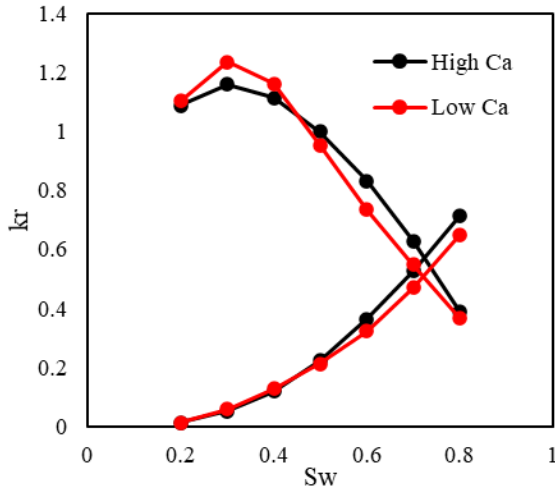
499 Two-phase flows in porous media are also strongly affected by capillary number  $Ca$  [39, 48].  
 500 Existing experiments and numerical simulations suggest that relative permeabilities of both  
 501 wetting and non-wetting phases should increase with increasing  $Ca$ . In the cases that we presented  
 502 thus far,  $Ca$  is  $2.9 \times 10^{-4}$  when  $M = 1$  and  $3.3 \times 10^{-4}$  when  $M = 0.2$  or and  $M = 5$ . To  
 503 investigate the effect of compaction on relative permeabilities during compaction at different  $Ca$ ,  
 504 additional cases were conducted with  $F = 10^{-3}$ . The interfacial tension is  $\sigma = 0.015$ , leading to  
 505 an increased capillary number of  $3.3 \times 10^{-3}$ . Contact angle was still set to  $\theta = 30^\circ$ . Figure 14  
 506 presents relative permeabilities of uncompact medium at two different capillary numbers,  
 507  $3.3 \times 10^{-4}$  (low) and  $3.3 \times 10^{-3}$  (high), for viscosity ratios of 0.2 and 5. It is known that when  
 508  $Ca$  is higher, effect of viscous force is stronger relative to capillary force, and this helps both  
 509 wetting and non-wetting phases overcome capillary resistance and flow. The observed trend that

510 relative permeabilities of both wetting and non-wetting phases increased with increasing  $Ca$  is  
511 reasonable.

512 In Figure 15 we compared relative permeability curves of original and compacted media at a  
513 higher capillary number. We found that compaction increased relative permeabilities of the wetting  
514 phase when the loading is hydrostatic, as shown in Figure 15a and 15b. When the loading is  
515 uniaxial, relative permeabilities of the wetting phase also increased with compaction, but changes  
516 were small and not clearly visible in Figure 15c and 15d. Changes in the relative permeabilities of  
517 the non-wetting phase are more complex. Figure 15a and Figure 15b show that, for hydrostatic  
518 loading and when  $M = 5$ , with compaction relative permeability of the non-wetting phase slightly  
519 increased. Compared to Figure 13a, there is no qualitative change in the trend, but the effect of  
520 compaction was *less* at the higher capillary number. When  $M = 0.2$ , with compaction relative  
521 permeability of the non-wetting phase decreased. Compared to Figure 13b, the trend is the same,  
522 but compaction reduced relative permeability of the non-wetting phase *more* when  $Ca$  is high.  
523 When  $Ca$  is low, the stronger capillary force is beneficial for the accumulation of the non-wetting  
524 phase in the middle of pores, and this accentuate the effect of wetting fluid film on the mobility of  
525 the non-wetting phase through lubrication. The results from uniaxial loading are presented in  
526 Figure 15c and Figure 15d. Compared to hydrostatic loading, similar behaviors of relative  
527 permeability were observed, but all with lesser magnitudes.

528





529

530

(a)

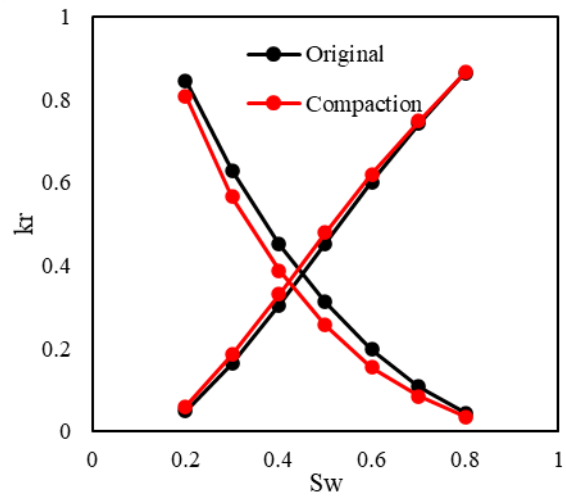
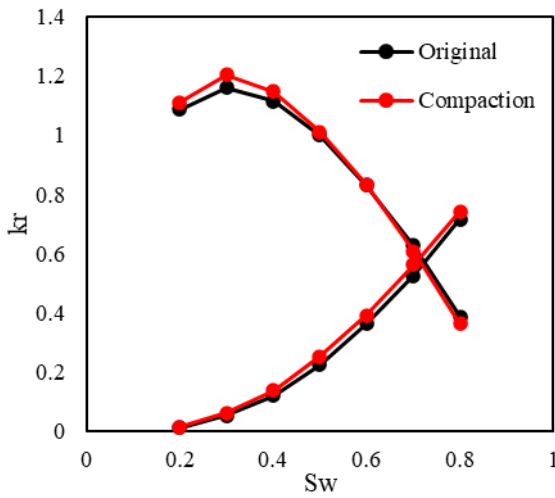
(b)

531 Figure 14. Effect of capillary number on the relative permeability of original sphere pack; (a)

532

$M = 5$ ; (b)  $M = 0.2$ .

533

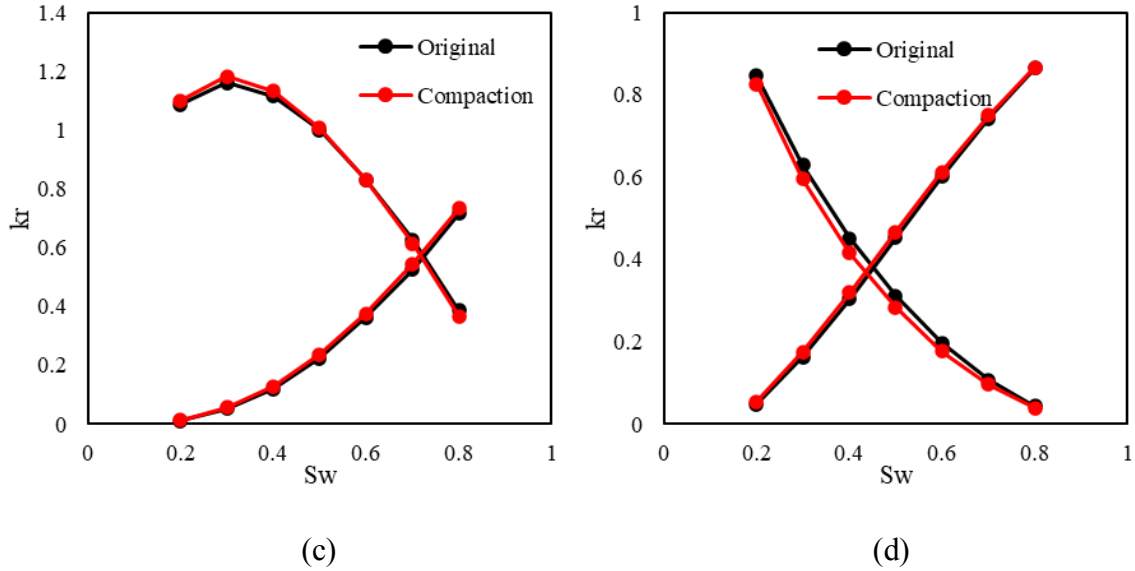


534

535

(a)

(b)



536  
537  
538  
539  
540  
541

(c) (d)

Figure 15. The relative permeabilities of compacted media with  $Ca = 3.3 \times 10^{-3}$ , under (a) hydrostatic loading condition,  $M = 5$ ; (b) hydrostatic loading condition,  $M = 0.2$ ; (c) uniaxial loading condition,  $M = 5$ ; (d) uniaxial loading condition,  $M = 0.2$ .

#### 4. Conclusions

542 In this work, we studied stress-dependent absolute and relative permeabilities in porous media  
543 packed by spherical particles. Compaction of porous media was modeled using a discrete element  
544 method. Three stages of strain were simulated for both hydrostatic loading and uniaxial loading.  
545 Absolute and relative permeabilities before and after compaction were simulated using lattice  
546 Boltzmann methods.  
547

548 In the homogeneous packing, absolute permeability decreased linearly with strain under the  
549 hydrostatic loading condition and slightly nonlinearly under the uniaxial loading condition.  
550 Uniaxial loading generated anisotropy in the absolute permeability and those along lateral  
551 directions were more sensitive to change of porosity. In all cases, changed porosity and absolute  
552 permeability during compaction follow a power-law relation. The porosity exponent of

553 homogeneous packing is close to the theoretical value from the Carman-Kozeny equation and  
554 experimental value of sandstones.

555 To study the effect of heterogeneity, a vuggy porous medium was built by creating a cylindrical  
556 tube in the middle of homogeneous pack. Insertion of this tube increased porosity exponent along  
557 the directions perpendicular to the tube. When flows are perpendicular to the cylindrical tube, the  
558 tube acts as a vug. During compactions, the permeability-controlling pores in the matrix of the  
559 medium were more severely compacted, leading to high porosity exponents. In the direction  
560 aligned with the tube, the diameter of the tube controls the permeability. The tube's deformation  
561 was less than that of the surrounding matrix. For this reason, a lower porosity exponent was  
562 observed in the direction aligned with the tube.

563 Stress-dependent relative permeability was studied at different viscosity ratios, wettability  
564 conditions, and capillary numbers. It was found that relative permeability only changes with stress  
565 when fluids demonstrate preferential wetting. Relative permeability of the wetting phase ( $k_{rw}$ )  
566 was often increased slightly by compaction, due to accumulation of wetting phase in smaller pores  
567 and formation of continuous pathways. Relative permeability of the non-wetting phase ( $k_{rnw}$ ), on  
568 the other hand, was more significantly affected by compaction. Due to more significant lubrication  
569 effect from the wetting fluid in compacted media,  $k_{rnw}$  was increased by compaction when the  
570 non-wetting phase is the more viscous but decreased when the non-wetting phase is the less viscous  
571 phase. The degree in which compaction affects relative permeability of the non-wetting phase was  
572 found to be dependent on the capillary number. Simulations with lower capillary numbers  
573 exhibited more stress dependent relative permeability of the non-wetting phase. We believe that  
574 this is due to the stronger preference for the non-wetting phase to favor centers of pores at lower  
575 capillary numbers, which accentuated the lubrication effects.

576 Finally, though we only focused on sphere pack, knowledge learned from this theoretical study  
577 could be applied to more complex media. At the same time, we are also aware that there are still  
578 gaps when one translates results from sphere packs to real rocks. Complex pore structure,  
579 distribution of pore size and kerogen types [67] in real rock may pose a challenge.

580

## 581 **Acknowledgment**

582 J.H. gratefully acknowledges the High Performance Research Computing Facilities in Texas  
583 A&M University. X.Y. acknowledges computational resource at the Colorado School of Mines  
584 provided by the Golden Energy Computing Organization. J.S. would like to acknowledge support  
585 from EPSRC EP/N025318/1, The Royal Academy of Engineering/The Leverhulme Trust Senior  
586 Research Fellowship LTSRF1617/13/2 and NERC NE/T010517/1 and NE/R011001/1.

587

## 588 **Reference**

- 589 [1] Corapcioglu, M.Y. and Brutsaert, W., 1977. Viscoelastic aquifer model applied to subsidence  
590 due to pumping. *Water Resour. Res.* 13(3): 597-604.  
591 <https://doi.org/10.1029/WR013i003p00597>.
- 592 [2] Gambolati, G., and Teatini, P., 2015. Geomechanics of subsurface water withdrawal and  
593 injection. *Water Resour. Res.* 51(6): 3922-3955.
- 594 [3] Davies, J.P., and Davies, D.K. 2001. Stress-Dependent Permeability: Characterization and  
595 Modeling. *SPE journal* 6(2): 224-235. <https://doi.org/10.2118/71750-PA>.
- 596 [4] Huang, J., Jin, T., Chai, Z. et al. 2019. Compositional simulation of fractured shale reservoir  
597 with distribution of nanopores using coupled multi-porosity and EDFM method. *Journal of*

598 Petroleum Science and Engineering 179: 1078-1089.  
599 <https://doi.org/10.1016/j.petrol.2019.05.012>.

600 [5] Kim, T.H., Cho, J., and Lee. K.S., 2017. Evaluation of CO<sub>2</sub> injection in shale gas reservoirs  
601 with multi-component transport and geomechanical effects. *Applied Energy* 190: 1195-1206.  
602 <https://doi.org/10.1016/j.apenergy.2017.01.047>.

603 [6] Huang, J., Jin, T., Barrufet, M. et al. 2020. Evaluation of CO<sub>2</sub> injection into shale gas reservoirs  
604 considering dispersed distribution of kerogen. *Applied Energy* 260, 114285.  
605 <https://doi.org/10.1016/j.apenergy.2019.114285>.

606 [7] Jin, L., Hawthorne, S., Sorensen, J., 2017. Advancing CO<sub>2</sub> enhanced oil recovery and storage  
607 in unconventional oil play—experimental studies on Bakken shale. *Applied Energy* 208: 171-  
608 183. <https://doi.org/10.1016/j.apenergy.2017.10.054>.

609 [8] Du, F., Huang, J., Chai, Z. et al. 2020. Effect of vertical heterogeneity and nano-confinement  
610 on the recovery performance of oil-rich shale reservoir, *Fuel* 267, 117199.  
611 <https://doi.org/10.1016/j.fuel.2020.117199>.

612 [9] Okazaki, K., Noda, H., Uehara, S., et al. 2014. Permeability, porosity and pore geometry  
613 evolution during compaction of Neogene sedimentary rocks. *Journal of Structural Geology* 62:  
614 1-12. <https://doi.org/10.1016/j.jsg.2013.12.010>.

615 [10] Bhandari, A.R., Flemings, P.B., Polit, P.J. 2015. Anisotropy and Stress Dependence of  
616 Permeability in the Barnett Shale. *Transport in Porous Media* volume 108: 393–411.  
617 <http://dx.doi.org/10.1007/s11242-015-0501-1>.

618 [11] He, J. Chen S.H., and Shahrour, I. 2013. Numerical estimation and prediction of stress  
619 dependent permeability tensor for fractured rock masses. *International Journal of Rock*  
620 *Mechanics and Mining Sciences* 59: 70-79. <https://doi.org/10.1016/j.ijrmms.2012.12.001>.

- 621 [12] Worthington, P.F., 2008. A diagnostic approach to quantifying the stress sensitivity of  
622 permeability. *Journal of Petroleum Science and Engineering* 61: 49-57.  
623 <https://doi.org/10.1016/j.petrol.2008.03.003>.
- 624 [13] Tan X.H., Li, X.P., Liu, J.Y., et al. 2015. Study of the effects of stress sensitivity on the  
625 permeability and porosity of fractal porous media. *Physics Letters A* 379(39): 2458-2465.  
626 <https://doi.org/10.1016/j.physleta.2015.06.025>.
- 627 [14] Bakhshian, S. and Sahimi M. 2016. Computer simulation of the effect of deformation on the  
628 morphology and flow properties of porous media. *PHYSICAL REVIEW E* 94, 042903.  
629 <https://doi.org/10.1103/PhysRevE.94.042903>.
- 630 [15] Bernabé, Y. 1991. Pore Geometry and Pressure Dependence of the Transport Properties in  
631 Sandstone. *Geophysics*, 56(4): 436-446. <https://doi.org/10.1190/1.1443061>.
- 632 [16] Doyen, P. M. 1988. Permeability, Conductivity, and Pore Geometry of Sandstone. *J. Geophys.*  
633 *Res. Solid* 93, 7729-7740. <https://doi.org/10.1029/JB093iB07p07729>.
- 634 [17] David, C., Wong, T. F., Zhu, W. et al. 1994. Laboratory measurement of compaction induced  
635 permeability change in porous rocks: Implications for the generation and maintenance of pore  
636 pressure excess in the crust. *Pure Appl. Geophy.* 143: 425-456.  
637 <https://doi.org/10.1007/BF00874337>.
- 638 [18] Dong, J. J., Hsu, J. Y., Wu, W. et al. 2010. Stress-dependence of the permeability and porosity  
639 of sandstone and shale from TCDP Hola-A. *Int. J. Rock Mech. Min.* 47(7): 1141-1157.  
640 <https://doi.org/10.1016/j.ijrmms.2010.06.019>.
- 641 [19] Petunin, V.V., Yin, X., and Tutuncu, A.N., 2011. Porosity and Permeability Changes in  
642 Sandstones and Carbonates Under Stress and Their Correlation to Rock Texture. Paper

643 presented at Canadian Unconventional Resources Conference, 15-17 November, Calgary,  
644 Alberta, Canada. <https://doi.org/10.2118/147401-MS>.

645 [20] Petunin, V.V., Labra, C., Xiao, F., et al. 2013. Porosity and Permeability Change under Stress  
646 and Correlation to Rock Texture. Paper presented at Fifth Biot Conference on Poromechanics  
647 July 10-12, 2013, Vienna, Austria. <https://doi.org/10.1061/9780784412992.124>.

648 [21] Bernabé, Y., Mok, U., and Evans, B. 2003. Permeability-porosity Relationships in Rocks  
649 Subjected to Various Evolution Processes. *Pure and applied geophysics*, 160: 937–960.  
650 <https://doi.org/10.1007/PL00012574>

651 [22] Fatt I. 1953. The Effect of Overburden Pressure on Relative Permeability. *J. Pet. Technol.* 5,  
652 15-16. <https://doi.org/10.2118/953325-G>.

653 [23] Thomas, R.D., and Ward, D.C., 1972. Effect of Overburden Pressure and Water Saturation  
654 on Gas Permeability of Tight Sandstone Cores. *J. Pet. Technol.* 24: 120-124.  
655 <https://doi.org/10.2118/3634-PA>.

656 [24] Zhang, X., Wu, C., and Liu, S., 2017. Characteristic analysis and fractal model of the gas-  
657 water relative permeability of coal under different confining pressures. *J. Pet. Sci. Eng.* 159:  
658 488–496. <https://doi.org/10.1016/j.petrol.2017.09.057>.

659 [25] Haghi, A.H., Chalaturnyk, R. and Talman, S. 2019. Stress-Dependent Pore Deformation  
660 effects on Multiphase Flow Properties of Porous Media. *Scientific Reports* 9, 15004.  
661 <https://doi.org/10.1038/s41598-019-51263-0>.

662 [26] Ali H., Al-Marhoun, M. and Abu-Khamsin S., 1987. The Effect of Overburden Pressure on  
663 Relative Permeability. Paper presented at Middle East Oil Show, 7-10 March, Bahrain, SPE-  
664 15730-MS. <https://doi.org/10.2118/15730-MS>.

- 665 [27] Jones, C., Al-Quraishi, A., Somerville J.M. et al. 2001. Stress Sensitivity of Saturation and  
666 End-point Relative Permeabilities. Paper presented at International Symposium of the Society  
667 of Core Analysts - Edinburgh, United Kingdom.
- 668 [28] Al-Quraishi, A. and Khairy, M. 2005. Pore pressure versus confining pressure and their effect  
669 on oil–water relative permeability curves. *Journal of Petroleum Science and Engineering* 48:  
670 120-126. <https://doi.org/10.1016/j.petrol.2005.04.006>.
- 671 [29] Gawish, A. and Al-Homadhi E. 2008. Relative permeability curves for high pressure, high  
672 temperature reservoir conditions. *Oil Gas Business*.
- 673 [30] Adenutsi, C.D., Li Z., Xu Z. et al. 2019. Influence of net confining stress on NMR T2  
674 distribution and two-phase relative permeability. *Journal of Petroleum Science and*  
675 *Engineering* 178: 766-777. <https://doi.org/10.1016/j.petrol.2019.03.083>.
- 676 [31] Wilson, J., 1956. Determination of relative permeability under simulated reservoir conditions.  
677 *AIChE J.* 2: 94–100. <https://doi.org/10.1002/aic.690020120>.
- 678 [32] Hamoud, M., Chalaturnyk, R., Leung, J. 2012. Influence of Geomechanical Processes on  
679 Relative Permeability. *Canadian Rock Mechanics Symposium*, Edmonton, Alberta, 9 p.
- 680 [33] Al-Quraish, A., Almisned, O.A., and Al-Awad M.N.J. 2010. Relative Permeabilities of  
681 Homogeneous and Heterogeneous Laminated Rock Samples under Hydrostatic and Triaxial  
682 Stresses. *J. King Saud Univ. Eng. Sci.* 22(2): 101-110. [https://doi.org/10.1016/S1018-](https://doi.org/10.1016/S1018-3639(18)30497-5)  
683 [3639\(18\)30497-5](https://doi.org/10.1016/S1018-3639(18)30497-5).
- 684 [34] Fagbemi, S., Tahmasebi P., and Piri, M. 2018. Pore-scale modeling of multiphase flow  
685 through porous media under triaxial stress. *Advances in Water Resources*, 122: 206-216.  
686 <https://doi.org/10.1016/j.advwatres.2018.10.018>.



- 687 [35] Fagbemi, S., Tahmasebi P., and Piri, M. 2020. Numerical modeling of strongly coupled  
688 microscale multiphase flow and solid deformation. *Int J Numer Anal Methods Geomech* 44(2):  
689 161-182. <https://doi.org/10.1002/nag.2999>.
- 690 [36] Fan, M., McClure, J., Han, Y. et al. 2018. Interaction Between Proppant Compaction and  
691 Single-/Multiphase Flows in a Hydraulic Fracture. *SPE Journal* 23 (04), 1290-1303.  
692 <https://doi.org/10.2118/189985-PA>.
- 693 [37] Owens, W. W. and Archer, D. L., 1971. The effect of rock wettability on oil-water relative  
694 permeability relationships, *J. Pet. Tech.* 23, 873–878. <https://doi.org/10.2118/3034-PA>.
- 695 [38] Avraam D.G. and Payatakes A.C. 1995. Flow regimes and relative permeabilities during  
696 steady-state two-phase flow in porous media. *Journal of Fluid Mechanics.* 293: 207-236.  
697 <https://doi.org/10.1017/S0022112095001698>.
- 698 [39] Li, H., Pan, C., and Miller, C.T., 2005. Pore-scale investigation of viscous coupling effects  
699 for two-phase flow in porous media. *Phys. Rev. E* 72, 026705.  
700 <https://doi.org/10.1103/PhysRevE.72.026705>.
- 701 [40] Ramstad, T., Idowu, N., Nardi, C., et al. 2012. Relative Permeability Calculations from Two-  
702 Phase Flow Simulations Directly on Digital Images of Porous Rocks. *Transport in Porous*  
703 *Media* 94: 487–504. <https://doi.org/10.1007/s11242-011-9877-8>.
- 704 [41] Gunstensen, A.K., Rothman, D.H., Zaleski, S., et al. 1991. Lattice Boltzmann model of  
705 immiscible fluids. *Physical Review A* 43, 4320. <https://doi.org/10.1103/PhysRevA.43.4320>.
- 706 [42] Liu, H., Valocchi, A.J. and Kang, Q., 2012. Three-dimensional lattice Boltzmann model for  
707 immiscible two-phase flow simulations. *Phys. Rev E* 85, 046309.  
708 <https://doi.org/10.1103/PhysRevE.85.046309>.

- 709 [43] Ba, Y., Liu, H., Li, Q., et al. 2016. Multiple-relaxation-time color-gradient lattice Boltzmann  
710 model for simulating two-phase flows with high density ratio. *Phys. Rev E* 94, 023310.  
711 <https://doi.org/10.1103/PhysRevE.94.023310>.
- 712 [44] Shan, X., and Chen, H., 1993. Lattice Boltzmann model for simulating flows with multiple  
713 phases and components. *Physical Review E* 47, 1815.  
714 <https://doi.org/10.1103/PhysRevE.47.1815>.
- 715 [45] Shan, X., and Doolen, G., 1995. Multicomponent lattice-Boltzmann model with interparticle  
716 interaction. *Journal of Statistical Physics* 81: 379-393. <https://doi.org/10.1007/BF02179985>.
- 717 [46] Swift, M.R., Osborn, W.R., and Yeomans, J.M., 1995. Lattice Boltzmann simulation of  
718 nonideal fluids. *Physical Review Letters* 75, 830. <https://doi.org/10.1103/PhysRevLett.75.830>.
- 719 [47] He, X., Chen, S., and Zhang, R. 1999. A Lattice Boltzmann Scheme for Incompressible  
720 Multiphase Flow and Its Application in Simulation of Rayleigh–Taylor Instability, *J. Comput.*  
721 *Phys.* 152(2): 642-663. <https://doi.org/10.1006/jcph.1999.6257>.
- 722 [48] Huang, J., Xiao, F., and Yin, X., 2017. Lattice Boltzmann simulation of pressure-driven two-  
723 phase flows in capillary tube and porous medium. *Computers and Fluids* 155: 134-145.  
724 <https://doi.org/10.1016/j.compfluid.2017.05.027>.
- 725 [49] Zhao, J., Kang, Q., Yao, J., et al. 2018. The effect of wettability heterogeneity on relative  
726 permeability of two-phase flow in porous media: A lattice Boltzmann study. *Water Resources*  
727 *Research*, 54, 1295–1311. <https://doi.org/10.1002/2017WR021443>.
- 728 [50] Jiang, F., and Tsuji, T. 2016. Estimation of three-phase relative permeability by simulating  
729 fluid dynamics directly on rock-microstructure images. *Water Resour. Res.* 53: 11–32,  
730 <https://doi:10.1002/2016WR01909>.

731 [51] Potyondy, D. O. and Cundall, P. A. 2004. A bonded-particle model for rock. *Int. J. Rock*  
732 *Mech. Min.* 41: 1329–1364. <https://doi.org/10.1016/j.ijrmms.2004.09.011>.

733 [52] Boutt, D.F. and McPherson B.J.O.L. 2002. Simulation of sedimentary rock deformation: Lab-  
734 scale model calibration and parameterization. *Geophysical research Letters* 29(4), 1054.  
735 <https://doi.org/10.1029/2001GL013987>.

736 [53] Powell and McBride 2006. What is required from DEM simulations to model breakage in  
737 mills? *Minerals Engineering* 19(10): 1013-1021.  
738 <https://doi.org/10.1016/j.mineng.2006.03.009>.

739 [54] Labra, C., 2012. Advances in the development of the discrete element method for excavation  
740 processes. PhD thesis. Universitat Politècnica de Catalunya.

741 [55] Jauffrès, D., Martin, C.L., Lichtner, A. et al. 2012. Simulation of the elastic properties of  
742 porous ceramics with realistic microstructure. *Modelling Simul. Mater. Sci. Eng.* 20 045009.  
743 <https://doi.org/10.1088/0965-0393/20/4/045009>.

744 [56] Rojek, J., Labra, C., Su, O., et al. 2012. Comparative study of different discrete element  
745 models and evaluation of equivalent micromechanical parameters. *International Journal of*  
746 *Solids and Structures* 49(13): 1497-1517. <https://doi.org/10.1016/j.ijsostr.2012.02.032>.

747 [57] Xiao, F, and Yin, X., 2016. Geometry models of porous media based on Voronoi tessellations  
748 and their porosity–permeability relations. *Computers & Mathematics with Applications* 72(2):  
749 328-348. <https://doi.org/10.1016/j.camwa.2015.09.009>.

750 [58] Sukop, M.C. and Thorne, D.T., 2007. *Lattice Boltzmann Modeling: An Introduction for*  
751 *Geoscientists and Engineers*. Springer. <https://doi.org/10.1007/978-3-540-27982-2>.

752 [59] Lallemand, P., and Luo, L.-S., 2000. Theory of the lattice Boltzmann method: Dispersion,  
753 dissipation, isotropy, Galilean invariance, and stability. *Physical review. E, Statistical Physics,*

754 Plasmas, Fluids, and Related Interdisciplinary Topics. 2000 Jun;61(6 Pt A):6546-6562.  
755 <https://doi.org/10.1103/physreve.61.6546>.

756 [60] d'Humières, D., 2002. Multiple-relaxation-time lattice Boltzmann models in three  
757 dimensions. Philosophical Transactions of the Royal Society of London. Series A:  
758 Mathematical, Physical and Engineering Sciences 360, 437-451.  
759 <https://doi.org/10.1098/rsta.2001.0955>.

760 [61] Frisch, U., d'Humières, D., Hasslacher, B., et al. 1987. Lattice gas hydrodynamics in two and  
761 three dimensions. AIP Conf. Proc. Complex Systems 1: 649-707.

762 [62] Zhang, L., Kang, Q., Yao, J., et al. 2015. Pore scale simulation of liquid and gas two phase  
763 flow based on digital core technology. Science China technological science 58: 1375-1384.  
764 <https://doi.org/10.1007/s11431-015-5842-z>.

765 [63] Labra, C. and Oñate, E., 2009. High-density sphere packing for discrete element method  
766 simulations. Commun. Numer. Meth. En. 25, 837-849. <https://doi.org/10.1002/cnm.1193>.

767 [64] Yiotis, A.G., Psihogios, J., Kainourgiakis, M.E., et al. 2007. A lattice Boltzmann study of  
768 viscous coupling effects in immiscible two-phase flow in porous media. Colloids and Surfaces  
769 A: Physicochemical and Engineering Aspects, 300(1): 35-49.  
770 <https://doi.org/10.1016/j.colsurfa.2006.12.045>.

771 [65] Huang, H., Lu, X-y. 2009. Relative permeabilities and coupling effects in steady-state gas-  
772 liquid flow in porous media: A lattice Boltzmann study. Physics of Fluids, 21(9), 092104.  
773 <https://doi.org/10.1063/1.3225144>.

774 [66] Anderson, W. G. 1987. Wettability literature survey part 5: The effects of wettability on  
775 relative permeability. Journal of Petroleum Technology, 39(11): 1453-1468.  
776 <https://doi.org/10.2118/16323-PA>.

777 [67] Sun, Z., Li, X., Liu, W., Zhang, T., He, M. and Nasrabadi, H., 2020. Molecular Dynamics of  
778 Methane Flow Behavior through Realistic Organic Nanopores under Geologic Shale  
779 Condition: Pore size and Kerogen Types. Chemical Engineering Journal, 398, 124341.  
780  
781