

## Study of the $K^+ K^-$ invariant-mass dependence of $CP$ asymmetry in $B^+ \rightarrow K^+ K^- K^+$ decays

J. P. Lees,<sup>1</sup> V. Poireau,<sup>1</sup> V. Tisserand,<sup>1</sup> E. Grauges,<sup>2</sup> A. Palano<sup>ab,3</sup> G. Eigen,<sup>4</sup> B. Stugu,<sup>4</sup> D. N. Brown,<sup>5</sup>  
L. T. Kerth,<sup>5</sup> Yu. G. Kolomensky,<sup>5</sup> M. J. Lee,<sup>5</sup> G. Lynch,<sup>5</sup> H. Koch,<sup>6</sup> T. Schroeder,<sup>6</sup> C. Hearty,<sup>7</sup> T. S. Mattison,<sup>7</sup>  
J. A. McKenna,<sup>7</sup> R. Y. So,<sup>7</sup> A. Khan,<sup>8</sup> V. E. Blinov<sup>ac,9</sup> A. R. Buzykaev<sup>a,9</sup> V. P. Druzhinin<sup>ab,9</sup> V. B. Golubev<sup>ab,9</sup>  
E. A. Kravchenko<sup>ab,9</sup> A. P. Onuchin<sup>ac,9</sup> S. I. Serednyakov<sup>ab,9</sup> Yu. I. Skovpen<sup>ab,9</sup> E. P. Solodov<sup>ab,9</sup>  
K. Yu. Todyshev<sup>ab,9</sup> A. N. Yushkov<sup>a,9</sup> D. Kirkby,<sup>10</sup> A. J. Lankford,<sup>10</sup> M. Mandelkern,<sup>10</sup> B. Dey,<sup>11</sup> J. W. Gary,<sup>11</sup>  
O. Long,<sup>11</sup> G. M. Vitug,<sup>11</sup> C. Campagnari,<sup>12</sup> M. Franco Sevilla,<sup>12</sup> T. M. Hong,<sup>12</sup> D. Kovalskyi,<sup>12</sup> J. D. Richman,<sup>12</sup>  
C. A. West,<sup>12</sup> A. M. Eisner,<sup>13</sup> W. S. Lockman,<sup>13</sup> B. A. Schumm,<sup>13</sup> A. Seiden,<sup>13</sup> D. S. Chao,<sup>14</sup> C. H. Cheng,<sup>14</sup>  
B. Echenard,<sup>14</sup> K. T. Flood,<sup>14</sup> D. G. Hitlin,<sup>14</sup> P. Ongmongkolkul,<sup>14</sup> F. C. Porter,<sup>14</sup> R. Andreassen,<sup>15</sup> Z. Huard,<sup>15</sup>  
B. T. Meadows,<sup>15</sup> B. G. Pushpawela,<sup>15</sup> M. D. Sokoloff,<sup>15</sup> L. Sun,<sup>15</sup> P. C. Bloom,<sup>16</sup> W. T. Ford,<sup>16</sup> A. Gaz,<sup>16</sup>  
U. Nauenberg,<sup>16</sup> J. G. Smith,<sup>16</sup> S. R. Wagner,<sup>16</sup> R. Ayad,<sup>17,\*</sup> W. H. Toki,<sup>17</sup> B. Spaan,<sup>18</sup> R. Schwierz,<sup>19</sup>  
D. Bernard,<sup>20</sup> M. Verderi,<sup>20</sup> S. Playfer,<sup>21</sup> D. Bettoni<sup>a,22</sup> C. Bozzi<sup>a,22</sup> R. Calabrese<sup>ab,22</sup> G. Cibinetto<sup>ab,22</sup>  
E. Fioravanti<sup>ab,22</sup> I. Garzia<sup>ab,22</sup> E. Luppi<sup>ab,22</sup> L. Piemontese<sup>a,22</sup> V. Santoro<sup>a,22</sup> R. Baldini-Ferrolli,<sup>23</sup>  
A. Calcaterra,<sup>23</sup> R. de Sangro,<sup>23</sup> G. Finocchiaro,<sup>23</sup> S. Martellotti,<sup>23</sup> P. Patteri,<sup>23</sup> I. M. Peruzzi,<sup>23,†</sup> M. Piccolo,<sup>23</sup>  
M. Rama,<sup>23</sup> A. Zallo,<sup>23</sup> R. Contri<sup>ab,24</sup> E. Guido<sup>ab,24</sup> M. Lo Vetere<sup>ab,24</sup> M. R. Monge<sup>ab,24</sup> S. Passaggio<sup>a,24</sup>  
C. Patrignani<sup>ab,24</sup> E. Robutti<sup>a,24</sup> B. Bhuyan,<sup>25</sup> V. Prasad,<sup>25</sup> M. Morii,<sup>26</sup> A. Adametz,<sup>27</sup> U. Uwer,<sup>27</sup> H. M. Lacker,<sup>28</sup>  
P. D. Dauncey,<sup>29</sup> U. Mallik,<sup>30</sup> C. Chen,<sup>31</sup> J. Cochran,<sup>31</sup> W. T. Meyer,<sup>31</sup> S. Prell,<sup>31</sup> A. V. Gritsan,<sup>32</sup> N. Arnaud,<sup>33</sup>  
M. Davier,<sup>33</sup> D. Derkach,<sup>33</sup> G. Grosdidier,<sup>33</sup> F. Le Diberder,<sup>33</sup> A. M. Lutz,<sup>33</sup> B. Malaescu,<sup>33,‡</sup> P. Roudeau,<sup>33</sup>  
A. Stocchi,<sup>33</sup> G. Wormser,<sup>33</sup> D. J. Lange,<sup>34</sup> D. M. Wright,<sup>34</sup> J. P. Coleman,<sup>35</sup> J. R. Fry,<sup>35</sup> E. Gabathuler,<sup>35</sup>  
D. E. Hutchcroft,<sup>35</sup> D. J. Payne,<sup>35</sup> C. Touramanis,<sup>35</sup> A. J. Bevan,<sup>36</sup> F. Di Lodovico,<sup>36</sup> R. Sacco,<sup>36</sup> G. Cowan,<sup>37</sup>  
J. Bougher,<sup>38</sup> D. N. Brown,<sup>38</sup> C. L. Davis,<sup>38</sup> A. G. Denig,<sup>39</sup> M. Fritsch,<sup>39</sup> W. Gradl,<sup>39</sup> K. Griessinger,<sup>39</sup> A. Hafner,<sup>39</sup>  
E. Prencipe,<sup>39</sup> K. Schubert,<sup>39</sup> R. J. Barlow,<sup>40,§</sup> G. D. Lafferty,<sup>40</sup> E. Behn,<sup>41</sup> R. Cenci,<sup>41</sup> B. Hamilton,<sup>41</sup>  
A. Jawahery,<sup>41</sup> D. A. Roberts,<sup>41</sup> R. Cowan,<sup>42</sup> D. Dujmic,<sup>42</sup> G. Sciolla,<sup>42</sup> R. Cheaib,<sup>43</sup> P. M. Patel,<sup>43,¶</sup>  
S. H. Robertson,<sup>43</sup> P. Biassoni<sup>ab,44</sup> N. Neri<sup>a,44</sup> F. Palombo<sup>ab,44</sup> L. Cremaldi,<sup>45</sup> R. Godang,<sup>45,\*\*</sup> P. Sonnek,<sup>45</sup>  
D. J. Summers,<sup>45</sup> M. Simard,<sup>46</sup> P. Taras,<sup>46</sup> G. De Nardo<sup>ab,47</sup> D. Monorchio<sup>ab,47</sup> G. Onorato<sup>ab,47</sup> C. Sciacca<sup>ab,47</sup>  
M. Martinelli,<sup>48</sup> G. Raven,<sup>48</sup> C. P. Jessop,<sup>49</sup> J. M. LoSecco,<sup>49</sup> K. Honscheid,<sup>50</sup> R. Kass,<sup>50</sup> J. Brau,<sup>51</sup> R. Frey,<sup>51</sup>  
N. B. Sinev,<sup>51</sup> D. Strom,<sup>51</sup> E. Torrence,<sup>51</sup> E. Feltresi<sup>ab,52</sup> M. Margoni<sup>ab,52</sup> M. Morandin<sup>a,52</sup> M. Posocco<sup>a,52</sup>  
M. Rotondo<sup>a,52</sup> G. Simi<sup>a,52</sup> F. Simonetto<sup>ab,52</sup> R. Stroili<sup>ab,52</sup> S. Akar,<sup>53</sup> E. Ben-Haim,<sup>53</sup> M. Bomben,<sup>53</sup>  
G. R. Bonneaud,<sup>53</sup> H. Briand,<sup>53</sup> G. Calderini,<sup>53</sup> J. Chauveau,<sup>53</sup> Ph. Leruste,<sup>53</sup> G. Marchiori,<sup>53</sup> J. Ocariz,<sup>53</sup> S. Sitt,<sup>53</sup>  
M. Biasini<sup>ab,54</sup> E. Manoni<sup>a,54</sup> S. Pacetti<sup>ab,54</sup> A. Rossi<sup>a,54</sup> C. Angelini<sup>ab,55</sup> G. Batignani<sup>ab,55</sup> S. Bettarini<sup>ab,55</sup>  
M. Carpinelli<sup>ab,55,††</sup> G. Casarosa<sup>ab,55</sup> A. Cervelli<sup>ab,55</sup> F. Forti<sup>ab,55</sup> M. A. Giorgi<sup>ab,55</sup> A. Lusiani<sup>ac,55</sup> B. Oberhof<sup>ab,55</sup>  
E. Paoloni<sup>ab,55</sup> A. Perez<sup>a,55</sup> G. Rizzo<sup>ab,55</sup> J. J. Walsh<sup>a,55</sup> D. Lopes Pegna,<sup>56</sup> J. Olsen,<sup>56</sup> A. J. S. Smith,<sup>56</sup>  
R. Faccini<sup>ab,57</sup> F. Ferrarotto<sup>a,57</sup> F. Ferroni<sup>ab,57</sup> M. Gaspero<sup>ab,57</sup> L. Li Gioi<sup>a,57</sup> G. Piredda<sup>a,57</sup> C. Büniger,<sup>58</sup>  
O. Grünberg,<sup>58</sup> T. Hartmann,<sup>58</sup> T. Leddig,<sup>58</sup> C. Voß,<sup>58</sup> R. Waldi,<sup>58</sup> T. Adye,<sup>59</sup> E. O. Olaiya,<sup>59</sup> F. F. Wilson,<sup>59</sup>  
S. Emery,<sup>60</sup> G. Hamel de Monchenault,<sup>60</sup> G. Vasseur,<sup>60</sup> Ch. Yèche,<sup>60</sup> F. Anulli,<sup>61,‡‡</sup> D. Aston,<sup>61</sup> D. J. Bard,<sup>61</sup>  
J. F. Benitez,<sup>61</sup> C. Cartaro,<sup>61</sup> M. R. Convery,<sup>61</sup> J. Dorfan,<sup>61</sup> G. P. Dubois-Felsmann,<sup>61</sup> W. Dunwoodie,<sup>61</sup>  
M. Ebert,<sup>61</sup> R. C. Field,<sup>61</sup> B. G. Fulsom,<sup>61</sup> A. M. Gabareen,<sup>61</sup> M. T. Graham,<sup>61</sup> C. Hast,<sup>61</sup> W. R. Innes,<sup>61</sup>  
P. Kim,<sup>61</sup> M. L. Kocian,<sup>61</sup> D. W. G. S. Leith,<sup>61</sup> P. Lewis,<sup>61</sup> D. Lindemann,<sup>61</sup> B. Lindquist,<sup>61</sup> S. Luitz,<sup>61</sup>  
V. Luth,<sup>61</sup> H. L. Lynch,<sup>61</sup> D. B. MacFarlane,<sup>61</sup> D. R. Muller,<sup>61</sup> H. Neal,<sup>61</sup> S. Nelson,<sup>61</sup> M. Perl,<sup>61</sup> T. Pulliam,<sup>61</sup>  
B. N. Ratcliff,<sup>61</sup> A. Roodman,<sup>61</sup> A. A. Salnikov,<sup>61</sup> R. H. Schindler,<sup>61</sup> A. Snyder,<sup>61</sup> D. Su,<sup>61</sup> M. K. Sullivan,<sup>61</sup>  
J. Va'vra,<sup>61</sup> A. P. Wagner,<sup>61</sup> W. F. Wang,<sup>61</sup> W. J. Wisniewski,<sup>61</sup> M. Wittgen,<sup>61</sup> D. H. Wright,<sup>61</sup> H. W. Wulsin,<sup>61</sup>  
V. Ziegler,<sup>61</sup> W. Park,<sup>62</sup> M. V. Purohit,<sup>62</sup> R. M. White,<sup>62,§§</sup> J. R. Wilson,<sup>62</sup> A. Randle-Conde,<sup>63</sup> S. J. Sekula,<sup>63</sup>  
M. Bellis,<sup>64</sup> P. R. Burchat,<sup>64</sup> T. S. Miyashita,<sup>64</sup> E. M. T. Puccio,<sup>64</sup> M. S. Alam,<sup>65</sup> J. A. Ernst,<sup>65</sup> R. Gorodeisky,<sup>66</sup>  
N. Guttman,<sup>66</sup> D. R. Peimer,<sup>66</sup> A. Soffer,<sup>66</sup> S. M. Spanier,<sup>67</sup> J. L. Ritchie,<sup>68</sup> A. M. Ruland,<sup>68</sup> R. F. Schwitters,<sup>68</sup>  
B. C. Wray,<sup>68</sup> J. M. Izen,<sup>69</sup> X. C. Lou,<sup>69</sup> F. Bianchi<sup>ab,70</sup> F. De Mori<sup>ab,70</sup> A. Filippi<sup>a,70</sup> D. Gamba<sup>ab,70</sup>  
S. Zambito<sup>ab,70</sup> L. Lanceri<sup>ab,71</sup> L. Vitale<sup>ab,71</sup> F. Martinez-Vidal,<sup>72</sup> A. Oyanguren,<sup>72</sup> P. Villanueva-Perez,<sup>72</sup>  
H. Ahmed,<sup>73</sup> J. Albert,<sup>73</sup> Sw. Banerjee,<sup>73</sup> F. U. Bernlochner,<sup>73</sup> H. H. F. Choi,<sup>73</sup> G. J. King,<sup>73</sup> R. Kowalewski,<sup>73</sup>  
M. J. Lewczuk,<sup>73</sup> T. Lueck,<sup>73</sup> I. M. Nugent,<sup>73</sup> J. M. Roney,<sup>73</sup> R. J. Sobie,<sup>73</sup> N. Tasneem,<sup>73</sup> T. J. Gershon,<sup>74</sup>  
P. F. Harrison,<sup>74</sup> T. E. Latham,<sup>74</sup> H. R. Band,<sup>75</sup> S. Dasu,<sup>75</sup> Y. Pan,<sup>75</sup> R. Prepost,<sup>75</sup> and S. L. Wu<sup>75</sup>

## (The BABAR Collaboration)

- <sup>1</sup>Laboratoire d'Annecy-le-Vieux de Physique des Particules (LAPP),  
Université de Savoie, CNRS/IN2P3, F-74941 Annecy-Le-Vieux, France
- <sup>2</sup>Universitat de Barcelona, Facultat de Física, Departament ECM, E-08028 Barcelona, Spain
- <sup>3</sup>INFN Sezione di Bari<sup>a</sup>; Dipartimento di Fisica, Università di Bari<sup>b</sup>, I-70126 Bari, Italy
- <sup>4</sup>University of Bergen, Institute of Physics, N-5007 Bergen, Norway
- <sup>5</sup>Lawrence Berkeley National Laboratory and University of California, Berkeley, California 94720, USA
- <sup>6</sup>Ruhr Universität Bochum, Institut für Experimentalphysik 1, D-44780 Bochum, Germany
- <sup>7</sup>University of British Columbia, Vancouver, British Columbia, Canada V6T 1Z1
- <sup>8</sup>Brunel University, Uxbridge, Middlesex UB8 3PH, United Kingdom
- <sup>9</sup>Budker Institute of Nuclear Physics SB RAS, Novosibirsk 630090<sup>a</sup>,  
Novosibirsk State University, Novosibirsk 630090<sup>b</sup>,  
Novosibirsk State Technical University, Novosibirsk 630092<sup>c</sup>, Russia
- <sup>10</sup>University of California at Irvine, Irvine, California 92697, USA
- <sup>11</sup>University of California at Riverside, Riverside, California 92521, USA
- <sup>12</sup>University of California at Santa Barbara, Santa Barbara, California 93106, USA
- <sup>13</sup>University of California at Santa Cruz, Institute for Particle Physics, Santa Cruz, California 95064, USA
- <sup>14</sup>California Institute of Technology, Pasadena, California 91125, USA
- <sup>15</sup>University of Cincinnati, Cincinnati, Ohio 45221, USA
- <sup>16</sup>University of Colorado, Boulder, Colorado 80309, USA
- <sup>17</sup>Colorado State University, Fort Collins, Colorado 80523, USA
- <sup>18</sup>Technische Universität Dortmund, Fakultät Physik, D-44221 Dortmund, Germany
- <sup>19</sup>Technische Universität Dresden, Institut für Kern- und Teilchenphysik, D-01062 Dresden, Germany
- <sup>20</sup>Laboratoire Leprince-Ringuet, Ecole Polytechnique, CNRS/IN2P3, F-91128 Palaiseau, France
- <sup>21</sup>University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom
- <sup>22</sup>INFN Sezione di Ferrara<sup>a</sup>; Dipartimento di Fisica e Scienze della Terra, Università di Ferrara<sup>b</sup>, I-44122 Ferrara, Italy
- <sup>23</sup>INFN Laboratori Nazionali di Frascati, I-00044 Frascati, Italy
- <sup>24</sup>INFN Sezione di Genova<sup>a</sup>; Dipartimento di Fisica, Università di Genova<sup>b</sup>, I-16146 Genova, Italy
- <sup>25</sup>Indian Institute of Technology Guwahati, Guwahati, Assam, 781 039, India
- <sup>26</sup>Harvard University, Cambridge, Massachusetts 02138, USA
- <sup>27</sup>Universität Heidelberg, Physikalisches Institut, D-69120 Heidelberg, Germany
- <sup>28</sup>Humboldt-Universität zu Berlin, Institut für Physik, D-12489 Berlin, Germany
- <sup>29</sup>Imperial College London, London, SW7 2AZ, United Kingdom
- <sup>30</sup>University of Iowa, Iowa City, Iowa 52242, USA
- <sup>31</sup>Iowa State University, Ames, Iowa 50011-3160, USA
- <sup>32</sup>Johns Hopkins University, Baltimore, Maryland 21218, USA
- <sup>33</sup>Laboratoire de l'Accélérateur Linéaire, IN2P3/CNRS et Université Paris-Sud 11,  
Centre Scientifique d'Orsay, F-91898 Orsay Cedex, France
- <sup>34</sup>Lawrence Livermore National Laboratory, Livermore, California 94550, USA
- <sup>35</sup>University of Liverpool, Liverpool L69 7ZE, United Kingdom
- <sup>36</sup>Queen Mary, University of London, London, E1 4NS, United Kingdom
- <sup>37</sup>University of London, Royal Holloway and Bedford New College, Egham, Surrey TW20 0EX, United Kingdom
- <sup>38</sup>University of Louisville, Louisville, Kentucky 40292, USA
- <sup>39</sup>Johannes Gutenberg-Universität Mainz, Institut für Kernphysik, D-55099 Mainz, Germany
- <sup>40</sup>University of Manchester, Manchester M13 9PL, United Kingdom
- <sup>41</sup>University of Maryland, College Park, Maryland 20742, USA
- <sup>42</sup>Massachusetts Institute of Technology, Laboratory for Nuclear Science, Cambridge, Massachusetts 02139, USA
- <sup>43</sup>McGill University, Montréal, Québec, Canada H3A 2T8
- <sup>44</sup>INFN Sezione di Milano<sup>a</sup>; Dipartimento di Fisica, Università di Milano<sup>b</sup>, I-20133 Milano, Italy
- <sup>45</sup>University of Mississippi, University, Mississippi 38677, USA
- <sup>46</sup>Université de Montréal, Physique des Particules, Montréal, Québec, Canada H3C 3J7
- <sup>47</sup>INFN Sezione di Napoli<sup>a</sup>; Dipartimento di Scienze Fisiche,  
Università di Napoli Federico II<sup>b</sup>, I-80126 Napoli, Italy
- <sup>48</sup>NIKHEF, National Institute for Nuclear Physics and High Energy Physics, NL-1009 DB Amsterdam, The Netherlands
- <sup>49</sup>University of Notre Dame, Notre Dame, Indiana 46556, USA
- <sup>50</sup>Ohio State University, Columbus, Ohio 43210, USA
- <sup>51</sup>University of Oregon, Eugene, Oregon 97403, USA
- <sup>52</sup>INFN Sezione di Padova<sup>a</sup>; Dipartimento di Fisica, Università di Padova<sup>b</sup>, I-35131 Padova, Italy
- <sup>53</sup>Laboratoire de Physique Nucléaire et de Hautes Energies,  
IN2P3/CNRS, Université Pierre et Marie Curie-Paris6,  
Université Denis Diderot-Paris7, F-75252 Paris, France
- <sup>54</sup>INFN Sezione di Perugia<sup>a</sup>; Dipartimento di Fisica, Università di Perugia<sup>b</sup>, I-06123 Perugia, Italy

- <sup>55</sup>INFN Sezione di Pisa<sup>a</sup>; Dipartimento di Fisica,  
Università di Pisa<sup>b</sup>; Scuola Normale Superiore di Pisa<sup>c</sup>, I-56127 Pisa, Italy
- <sup>56</sup>Princeton University, Princeton, New Jersey 08544, USA
- <sup>57</sup>INFN Sezione di Roma<sup>a</sup>; Dipartimento di Fisica,  
Università di Roma La Sapienza<sup>b</sup>, I-00185 Roma, Italy
- <sup>58</sup>Universität Rostock, D-18051 Rostock, Germany
- <sup>59</sup>Rutherford Appleton Laboratory, Chilton, Didcot, Oxon, OX11 0QX, United Kingdom
- <sup>60</sup>CEA, Irfu, SPP, Centre de Saclay, F-91191 Gif-sur-Yvette, France
- <sup>61</sup>SLAC National Accelerator Laboratory, Stanford, California 94309 USA
- <sup>62</sup>University of South Carolina, Columbia, South Carolina 29208, USA
- <sup>63</sup>Southern Methodist University, Dallas, Texas 75275, USA
- <sup>64</sup>Stanford University, Stanford, California 94305-4060, USA
- <sup>65</sup>State University of New York, Albany, New York 12222, USA
- <sup>66</sup>Tel Aviv University, School of Physics and Astronomy, Tel Aviv, 69978, Israel
- <sup>67</sup>University of Tennessee, Knoxville, Tennessee 37996, USA
- <sup>68</sup>University of Texas at Austin, Austin, Texas 78712, USA
- <sup>69</sup>University of Texas at Dallas, Richardson, Texas 75083, USA
- <sup>70</sup>INFN Sezione di Torino<sup>a</sup>; Dipartimento di Fisica, Università di Torino<sup>b</sup>, I-10125 Torino, Italy
- <sup>71</sup>INFN Sezione di Trieste<sup>a</sup>; Dipartimento di Fisica, Università di Trieste<sup>b</sup>, I-34127 Trieste, Italy
- <sup>72</sup>IFIC, Universitat de Valencia-CSIC, E-46071 Valencia, Spain
- <sup>73</sup>University of Victoria, Victoria, British Columbia, Canada V8W 3P6
- <sup>74</sup>Department of Physics, University of Warwick, Coventry CV4 7AL, United Kingdom
- <sup>75</sup>University of Wisconsin, Madison, Wisconsin 53706, USA

As a followup to the latest *BABAR* amplitude analysis of the decay  $B^+ \rightarrow K^+ K^- K^+$ , we investigate the  $K^+ K^-$  invariant-mass dependence of the  $CP$  asymmetry and compare it to that obtained by the LHCb collaboration. The results are based on a data sample of approximately  $470 \times 10^6 B\bar{B}$  decays, collected with the *BABAR* detector at the PEP-II asymmetric-energy  $B$  factory at the SLAC National Accelerator Laboratory.

A study of  $CP$  violation in a Dalitz-plot analysis of  $B^+ \rightarrow K^+ K^- K^+$  decays was performed by the *BABAR* collaboration [1]. Based on this existing analysis, we exploit the *sPlot* technique [2] to investigate the  $K^+ K^-$  invariant-mass dependence of the  $CP$  asymmetry,  $A_{CP} = \frac{\Gamma(B^-) - \Gamma(B^+)}{\Gamma(B^-) + \Gamma(B^+)}$ . The dependence of the  $CP$  asymmetry on  $K^+ K^-$  invariant mass is compared to a recent preliminary result from the LHCb collaboration [3], where the direct  $CP$  asymmetry in  $B^+ \rightarrow K^+ K^- K^+$  over the entire phase space excluding charm decays was measured to be

$$A_{CP}(B^+ \rightarrow K^+ K^- K^+) = -0.046 \pm 0.009(\text{stat.}) \pm 0.005(\text{syst.}) \pm 0.007(J/\psi K^\pm). \quad (1)$$

The first quoted uncertainty is statistical, the second is systematic, and the third is due to the uncertainty on the measured value of the  $CP$  asymmetry in  $B \rightarrow J/\psi K^\pm$  decays (see below). This result has a significance of  $3.7\sigma$  to be non-zero and is claimed to be the first evidence of  $CP$  violation observed in inclusive charmless  $B$  decays. The corresponding measurement from *BABAR* is

$$A_{CP}(B^+ \rightarrow K^+ K^- K^+) = -0.017_{-0.014}^{+0.019}(\text{stat.}) \pm 0.014(\text{syst.}), \quad (2)$$

where no significant  $CP$  violation is observed, although it is not inconsistent with the result from LHCb.

The analysis method used to extract  $A_{CP}$  is rather different between the experiments. *BABAR* performs an amplitude analysis, based on a maximum-likelihood fit to the Dalitz plot as well as the output of a neural network based on event shape variables and the kinematic variables  $m_{ES}$  and  $\Delta E$  [1]. The energy-substituted mass is defined as  $m_{ES} \equiv \sqrt{(s/2 + \mathbf{p}_i \cdot \mathbf{p}_B)^2 / E_i^2 - p_B^2}$  and the energy difference  $\Delta E \equiv E_B^* - \frac{1}{2}\sqrt{s}$ , where  $(E_B, \mathbf{p}_B)$  and  $(E_i, \mathbf{p}_i)$  are the

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\*Now at the University of Tabuk, Tabuk 71491, Saudi Arabia

†Also with Università di Perugia, Dipartimento di Fisica, Perugia, Italy

‡Also with Laboratoire de Physique Nucléaire et de Hautes Energies, IN2P3/CNRS, Paris, France

§Now at the University of Huddersfield, Huddersfield HD1 3DH, UK

¶Deceased

\*\*Now at University of South Alabama, Mobile, Alabama 36688, USA

††Also with Università di Sassari, Sassari, Italy

‡‡Also with INFN Sezione di Roma, Roma, Italy

§§Now at Universidad Técnica Federico Santa María, Valparaiso, Chile 2390123

four-vectors of the  $B$  candidate and the initial electron-positron system measured in the laboratory frame, respectively. The asterisk denotes the  $e^+e^-$  CM frame, and  $s$  is the invariant mass squared of the electron-positron system. Signal events peak at the  $B$  mass ( $\approx 5.279 \text{ GeV}/c^2$ ) for  $m_{ES}$ , and at zero for  $\Delta E$ . The inclusive  $A_{CP}$  is calculated by separately integrating over the Dalitz plane the efficiency-corrected charmless isobar amplitudes for  $B^+$  and  $B^-$ . The LHCb result is obtained by fitting the  $K^+K^-K^+$  and  $K^-K^+K^-$  invariant mass distributions, integrated over the Dalitz plot without any efficiency correction, and calculating  $A_{CP}^{RAW} = \frac{N^- - N^+}{N^- + N^+}$ . This raw asymmetry is corrected by their observed  $J/\psi K^\pm$  asymmetry of  $-0.014 \pm 0.007$  to subtract residual charge asymmetries in production and detection. This correction uses the world-average measured asymmetry of  $0.001 \pm 0.007$  [4] for  $B^\pm \rightarrow J/\psi K^\pm$ . In the LHCb analysis, to remove contributions from the charm decays  $B^\pm \rightarrow \bar{D}^0(D^0)h^\pm$  (where  $h$  stands for  $K$  or  $\pi$ ) with  $\bar{D}^0(D^0) \rightarrow h^+h^-$ , a  $m_{K^+K^-}$  veto was applied at  $\pm 30 \text{ MeV}/c^2$  around the  $D^0$ -mass value. The inclusive  $A_{CP}$  extracted by LHCb is the integral over all the observed events in the  $K^+K^-K^+$  Dalitz plane. Unlike *BABAR*, LHCb does not include a correction for varying efficiency across the phase space, but evaluates a systematic uncertainty of 0.15% due to this effect.

LHCb also obtained the raw asymmetry as a function of the squared  $K^+K^-$  invariant mass. They observe a broad structure in the asymmetry at  $m_{K^+K^-}^2 \approx 1.6 \text{ GeV}^2/c^4$ , peaking at  $A_{CP} \approx -0.2$ . The *BABAR* publication did not directly include this study, although Fig. 8 in the *BABAR* paper shows the  $m_{K^+K^-}$  distributions for  $B^+$  and  $B^-$  separately. In this note, we have reproduced the binning and Dalitz plot cuts of the LHCb study in order to directly compare the mass dependence of  $A_{CP}$  between the two experiments. The *BABAR*  $A_{CP}$  distributions were produced with the  $s$ Plot technique, using the  $m_{ES}$  and  $\Delta E$  variables, which are not correlated to each other or to the  $K^+K^-$  invariant mass. In Fig.1, we show the extracted charge asymmetry as a function of the lower of the two  $K^+K^-$  masses,  $m_{K^+K^-,low}$ .

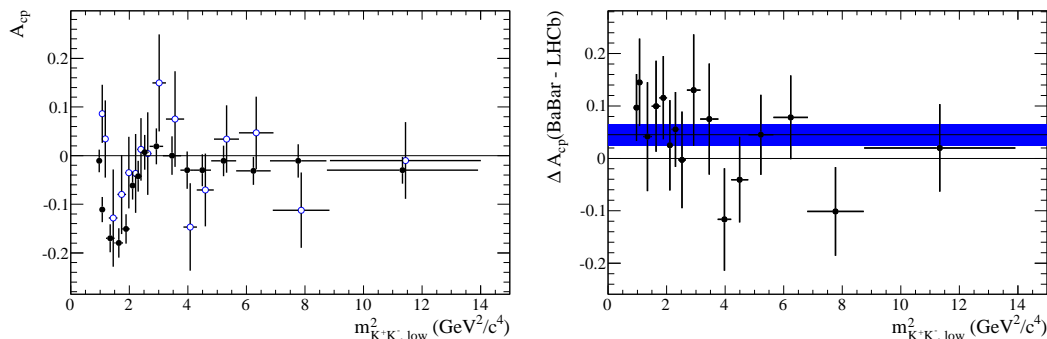


FIG. 1: Left:  $A_{CP}$  as a function of  $m_{K^+K^-,low}^2$  in  $B^+ \rightarrow K^+K^-K^+$  from LHCb (solid dots) and *BABAR* (open dots). The LHCb distribution is  $A_{CP}^{RAW}$ . The distribution from *BABAR* is obtained by the  $s$ Plot technique. For both experiments the error bars are statistical only. The systematic effects for *BABAR* are estimated to be approximately 0.01. The *BABAR* data points on the plot are shifted to the right by  $0.1 \text{ GeV}^2/c^4$  for clarity. Right: The difference between the *BABAR* and LHCb asymmetries,  $A_{CP}(BABAR) - A_{CP}^{RAW}(LHCb)$ . Also shown is the average shift of  $0.045 \pm 0.021$ .

Although the errors on the *BABAR* data are approximately 2 times larger than those of LHCb, the pattern of the  $CP$  asymmetry as a function of  $m_{K^+K^-,low}^2$  agrees very well. The  $\chi^2$  between the data is 16.1 for 16 bins. There does appear to be, however, a clear overall shift between the measured LHCb and *BABAR* asymmetries, as shown in the right hand plot of Fig. 1. The average difference between the binned  $A_{CP}$  measurements is  $0.045 \pm 0.021$  and appears to be flat across the spectrum. To obtain this average, we weighted the binned  $A_{CP}$  values by their respective errors.

The  $K^+K^-$  invariant-mass spectrum in the region  $1.3 - 1.7 \text{ GeV}/c^2$  includes contributions from at least the  $f_0(1500)$ ,  $f_2'(1525)$ , and  $f_0(1710)$ , as well as a broad non-resonant contribution [1]. Considering the many varying strong phases involved, as well as the differing quark content of the different resonances, it is not surprising to see significant direct  $CP$  violation in this region of phase space.

For completeness, we also include similar plots the higher of the two  $K^+K^-$  masses,  $m_{K^+K^-,high}$ , in Fig. 2. Here, the average shift is  $0.053 \pm 0.021$ . The average shifts in asymmetry observed in  $m_{K^+K^-,low}$  and  $m_{K^+K^-,high}$  are similar but not identical. This behavior is expected due to the fact that we calculate the average of binned  $A_{CP}$  values weighted by the error and not by the number of signal events in each bin. The errors are influenced by the background distributions, which are different in the two variables.

In summary, we performed a study of the  $K^+K^-$  invariant-mass dependence of the  $CP$  asymmetry in  $B^+ \rightarrow K^+K^-K^+$  decays, based on a published *BABAR* Dalitz-plot analysis [1]. The *BABAR* data support the variation of the  $CP$  asymmetry over the Dalitz plot seen by LHCb. Nevertheless, a difference exists between the  $CP$  asymmetries

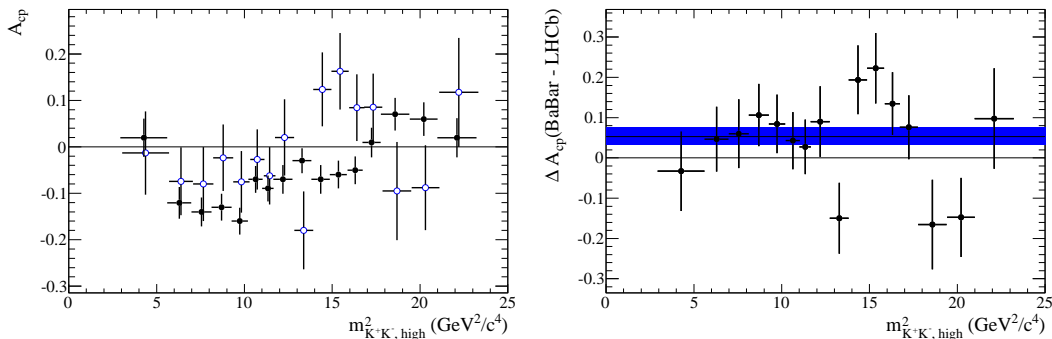


FIG. 2: Left:  $A_{CP}$  as a function of  $m_{K^+K^-,high}^2$  in  $B^+ \rightarrow K^+K^-K^+$  from LHCb (solid dots) and BABAR (open dots). The LHCb distribution is  $A_{CP}^{RAW}$ . The distribution from BABAR is obtained by the  $sPlot$  technique. For both experiments the error bars are statistical only. The systematic effects for BABAR are estimated to be approximately 0.01. The BABAR data points on the plot are shifted to the right by  $0.1 \text{ GeV}^2/c^4$  for clarity. Right: The difference between the BABAR and LHCb asymmetries,  $A_{CP}(\text{BABAR}) - A_{CP}^{RAW}(\text{LHCb})$ . Also shown is the average shift of  $0.053 \pm 0.021$ .

measured by BABAR and LHCb. This difference appears to be consistent with being uniform across the phase space and is found to be  $0.045 \pm 0.021$  between the BABAR  $A_{CP}$  distribution as a function of  $m_{K^+K^-,low}$  and that obtained by LHCb. A compatible difference is observed in  $m_{K^+K^-,high}$ . These values are consistent with the difference between the inclusive  $A_{CP}$  obtained by the two experiments. The shift, while consistent with zero within 2 standard deviation, explains the different conclusions between the two experiments concerning effects in specific regions of the phase space: the hint of direct  $CP$  asymmetry in  $B^+ \rightarrow \phi(1020)K^+$  that was seen by BABAR but not confirmed by LHCb, and the fact that BABAR finds a negative asymmetry with a smaller magnitude than LHCb around  $m_{K^+K^-}^2 \approx 1.6 \text{ GeV}^2/c^4$ . Further experimental investigation is needed to draw definitive conclusions on the source of  $CP$  violation in  $B^+ \rightarrow K^+K^-K^+$  decays.

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