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1 **Optimization and Design of Carbon Fabric-Reinforced Cementitious** 2 **Matrix Composites**

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13
14 **Abstract:** Interest in carbon fabric-reinforced cementitious matrix (C-FRCM) composites as
15 structural strengthening materials for reinforced concrete structures has recently increased. In
16 such applications, the mechanical properties of C-FRCM composites are the key to unlocking
17 the corresponding strengthening effects. Therefore, this study explores different optimization
18 approaches to improve the loading behaviors of C-FRCM composites, such as different
19 carbon fabric contents in the cementitious matrix and different surface treatments of the
20 carbon fiber meshes. Then, a series of tensile tests are carried out to evaluate the performance
21 of the modified C-FRCM composites. Furthermore, experimental results of other FRCM
22 composites are collected from the literature to create a larger data pool for analysis. Finally,
23 two existing constitutive models for FRCM composites — the Aveston-Cooper-Kelly (ACK)
24 model and the AC434 model — are compared against these experimental data.

25
26 **Key words:** C-FRCM; carbon fiber mesh; constitutive models; tensile tests

27 **1. Introduction**

28 Externally bonded fiber composite materials have become a common a common means to
29 improve the performance and extend the service life of existing reinforced concrete structures.
30 Over the last 20 years, fiber-reinforced polymer (FRP) plates/sheets/meshes, consisting of
31 continuous fiber sheets and organic epoxy resin, have been the most popular strengthening
32 materials [1,2]. However, externally bonded FRP systems are difficult to construct in
33 low-temperature environments and are not durable in humid and corrosive environments;
34 furthermore, FRP systems have poor fire resistance properties and are incompatible with
35 concrete substrates (due to the different chemical properties between organic and inorganic
36 materials) [3-8]. With the development of structural strengthening technologies, a relatively
37 new composite called fabric-reinforced cementitious matrix (FRCM) composite has attracted
38 attention from researchers and engineers. FRCM composites are a type of composite with one
39 or multiple layers of continuous bidirectional fiber mesh embedded in a cementitious matrix
40 [9-12]. Compared to the bonding material used in FRPs (e.g., epoxy resin), the inorganic
41 cementitious materials used in FRCM composites are superior in terms of fire resistance,
42 durability and compatibility with concrete (i.e., allows vapor permeability and application on
43 a wet surface). FRCM composites also exhibit advantages over FRPs in applications on
44 irregular surfaces [13].

45 Although both FRPs and FRCM composites are mainly subjected to tension when used
46 for structural strengthening, the structural responses of these two composites are quite
47 different. The stress-strain curve of an FRP under tension is linear until reaching the ultimate
48 state, whereas the load transfer in an FRCM composite occurs through the interfacial bond

49 between the cement matrix and the fiber mesh, and the corresponding constitutive model for
50 an FRCM composite is bilinear or trilinear, for which the cracking of the cementitious matrix
51 corresponds to a transition point [14]. Research on FRPs started in the 1940s, and FRPs began
52 to be implemented in a wide range of applications in the 1960s. Compared to FRPs, FRCM
53 composites have more-complex structural responses; research on FRCM composites started in
54 the 1980s. The tensile properties of FRCM composites were significantly connected to the
55 bond behavior between matrix and fiber, while the strengthening intervention also relies on
56 the composite/substrate bond behavior. According to the literatures, the fiber
57 mesh/cementitious matrix interface is normally more critical compared to the
58 composite/substrate interface [11-12, 15-18]. This is because cementitious matrix and
59 concrete are both inorganic materials; the bonding between inorganic materials is typically
60 better than the bonding between inorganic and organic materials. Existing experimental
61 investigations on the tensile behavior of FRCM composites include the clarification of the
62 effects of clamping grips (i.e., different boundary conditions) [19,20], layers of fiber mesh
63 [8,21,22], and chopped fibers in the cementitious matrix [23] on the loading behaviors of the
64 composites. Experimental results have shown that the mechanical properties of FRCM
65 composites could be significantly limited due to the combination of premature filament
66 failure and core filament slippage [11-12, 24-25]. Compared to clevis grips, clamping grips
67 resulted in a better utilization of the capacities of fibre meshes which embed in cementitious
68 matrix, thereby leading to generally higher tensile strength results [19,20]. In the macro level,
69 Larrinaga et al. [21], Caggegi et al. [22] and Donnini and Corinaldesi [8] found that as the
70 number of fiber layers increased, the bond between the fiber bundles and mortar became less

71 effective, and the fiber bundles became more prone to slip. Barhum and Mechtcherine [23]
72 incorporated chopped glass and carbon fibers into a cementitious matrix and reported that the
73 cracking load of the composite materials significantly increased and that a greater number of
74 fine cracks appeared on the specimen surface due to the incorporation of the reinforcing
75 materials; however, the increase in ultimate strength was limited. Studies on the surface
76 treatment of fiber bundles have also been carried out. Contamine and Si Larbi [26]
77 preimpregnated glass fiber meshes with epoxy resin and latex before embedding the fiber
78 meshes into a cementitious matrix; this process significantly increased the strength of the
79 FRCM composites. This increase in strength occurred because the preimpregnation process
80 resulted in the fiber filaments having a more uniform stress distribution [27]. Donnini et al.
81 [15] used different mortar matrices and applied different coating treatments to carbon fabric.
82 The results show that the use of a polymer coating on carbon fabric increases the mechanical
83 capacity of the FRCM system. In addition, applying sand to the surface of carbon fabric
84 further increased the mechanical characteristics of the carbon fabric. Other studies have
85 investigated different anchorage configurations of embedded fiber meshes [28], effective fiber
86 mesh overlap lengths [29] and loop-shaped elements [30] to improve the loading behaviors of
87 FRCM composites. However, the experimental results presented in the literature are still
88 limited. Moreover, as mentioned above, the loading responses of FRCM composites are quite
89 distinct under different conditions, making it difficult to reach consistent conclusions for
90 different FRCM composites, considering that there are a substantial number of variables
91 associated with the cementitious matrix, embedded fiber meshes, loading configurations, etc.
92 Currently, there are two commonly used simplified tensile stress-strain models for FRCM

93 composites: the bilinear model codified in AC434.13 [31] (called the AC434 model in the
94 following discussion) and the trilinear model proposed by Aveston and Kelly [32] (called the
95 ACK model in the following discussion). The appropriateness of these two existing models
96 for different FRCM composites requires investigation.

97 Thus, this study aims to further optimize FRCM composites with reference to the
98 commercial products and engineering cementitious composites (ECCs) available and to
99 evaluate the appropriateness of the existing FRCM constitutive models against the newly
100 developed and collected experimental results. First, different modifications regarding the
101 cementitious matrix and carbon fiber mesh (CF-MESH) are used to prepare new carbon
102 FRCM (C-FRCM) composites. Although it is the flexural behavior of the FRCM composite
103 which is closely related to the design, tension properties of the FRCM could be used to
104 initially assess the quality of the FRCM composites. Uniaxial tensile tests are carried out to
105 obtain the stress-strain curves of these C-FRCM composites. The types of considered
106 cementitious materials include mortar, mortar with chopped carbon fibers, ECC and
107 commercial mortar; the types of CF-MESH considered in this study include dry CF-MESH
108 without a coating, CF-MESH coated at the nodes and commercial carbon FRP (CFRP) grids.
109 In addition, this paper summarizes the existing results of tensile tests on FRCM composites
110 available in the literature to form a larger data pool with the newly generated test results.
111 Based on this data pool, the AC434 model and ACK model are assessed, and suggestions for
112 FRCM composite design are discussed. To simulate the real load transfer mechanism in
113 structures, beam bending tests are needed in the future, but that should be built on the
114 development of a reasonably good FRCM composite, which is the main purpose of this study.

115 2. Experimental program

116 2.1 Raw materials

117 The embedded carbon fibers used in this study are the dry CF-MESH shown in Figure 1(a)
118 (denoted as T1 – TEX of 1200g/km, non-woven), and the coated carbon fiber mesh shown in
119 Figure1(b) (denoted as T2 - weight of the mesh of 200g/m², woven). The reason for including
120 the commercial products with polymer-impregnated textiles is to see the possible
121 improvement of bond brought by the coating. CF-MESH T3 represents CF-MESH T1 with
122 coating at selected nodes (see Figure 1(c)), which were along the whole length of the textile
123 strip embedded in the tensile coupon. The material used resulted in coating of the yarns'
124 junctions. Uniaxial tensile tests of a single bundle of fibers from the aforementioned three
125 meshes (three parallel tests for each type of mesh) were carried out using a 10 kN
126 servo-controlled testing machine, and the average test results are presented in Table 1. Note
127 that during the tensile test of T2 fiber, the premature slippage between the fibers and its
128 coating was occurred, which caused the fiber to slip out of the clamping jaws. Whereas, for
129 the other specimens, the failure mode is fiber breakage. This is the main reason causing the
130 large difference of the tensile strength between T2 and the others. Seven different types of
131 cementitious materials were considered in this study; more information about these materials
132 is provided in Table 2. According to the manufacturer, the commercial mortar (M7) contains
133 an activator which can actively react with the coating of CF-MESH, and thus improve the
134 bonding between CF-MESH (T2) and mortar (M7). The compressive, and flexural properties
135 of cementitious materials after 28 days of curing (temperature 20 °C, relative humidity 100%,
136 complied with Chinese standard GB/T50081-2016 [33] were obtained by tests conducted in

137 accordance with EN 1015-11 [34]. The tensile properties after 28 days of curing were
138 obtained by dog bone tensile test in accordance with JSCE [35], as shown in Table 2, which
139 were thereafter used in the calculation in Section 6. The dimensions of the specimens used for
140 the compression tests are 40 mm × 40 mm × 40 mm, whereas the dimensions for the
141 three-point bending test specimens are 40 mm × 40 mm × 160 mm. Three parallel tests were
142 conducted for each type of cementitious matrix. The length of chopped carbon fibers is 6 mm.

143 **2.2 Test specimens**

144 A total of eight different FRCM composites were considered in this study, and three tests were
145 conducted for each composite. The labeling scheme for the specimens is given in Table 3.

146 The preparation procedure of the FRCM composites includes the following steps: (1) place a
147 5 mm cementitious matrix in a wooden mold (Figure 2(a)), (2) firmly fix a layer of mesh on
148 top of the cementitious matrix (see Figure 2(b)), (3) place another 5 mm cementitious matrix
149 layer on top of the mesh and trowel its surface, and (4) demold the FRCM composite coupon
150 after 24 hours (Figure 2(c)). The FRCM composite coupons were then cured for 28 days at
151 20 °C and 70% humidity. Afterwards, each FRCM composite plate was cut into three
152 specimens using a diamond cutter for tests (Figure 2(d)); each specimen contained five fiber
153 bundles in the longitudinal direction. Figure 3 shows the dimensions of a FRCM composite
154 tensile specimen., the length of the FRCM-anchorage plate is 100 mm.

155 **2.3 Test setup and measurements**

156 Uniaxial tensile tests were performed in accordance with ACI 549.4R-13 [36] and AC 434.13
157 [31]. These tests were conducted on a 10 kN servo-controlled testing machine at a loading
158 rate of 0.2 mm/min. The clevis grip configuration was adopted in the experimental. The

159 specimen deformation was measured with two symmetrically arranged linear variable
160 differential transformers (LVDTs) (Figure 4(a)). The loads and specimen deformations were
161 synchronously collected with a datalogger. Both ends of the specimen were hinged to the
162 machine to avoid bending moments, as shown in Figure 4(b).

163 **3. Experimental results**

164 The stress-strain curves obtained from the tensile tests are shown in Figure 5, and the test
165 results, including the cracking strength (f_t), peak strength (f_u), ultimate strain (ϵ_u), uncracked
166 modulus (E_1) and post-cracking modulus (E_2), are presented in Table 4. Note that the
167 post-cracking modulus is the linear fitting result of the post-cracking stress-strain curve. In
168 the initial stage of loading, the load was mainly carried by the cementitious matrix and the
169 CF-MESH. The first part of the stress-strain curve is linear. Later, cracks occurred on the
170 surface of the cementitious matrix when the ultimate strain was reached. The load suddenly
171 dropped when new cracks occurred; thus, the stress-strain curves fluctuate during this stage.
172 Afterwards, when the number of cracks became stable, the load started to increase gradually
173 again until reaching the peak value; during this stage, the load was transferred from the
174 cementitious matrix to the CF-MESH and was carried by the CF-MESH. Both this study and
175 previous investigations [2,15,24,37] found that the typical failure mode of FRCM composites
176 is a combination of slippage between the CF-MESH and the cementitious matrix and partial
177 fracturing of external carbon fiber filaments in the CF-MESH.

178 **3.1 Effect of chopped carbon fibers**

179 The effect of the number of chopped carbon fibers (see Figure 6) in the cementitious matrix is
180 considered by comparing the performance of specimens M2-T1, M3-T1, M4-T1, and M5-T1

181 with the reference specimens M1-T1 (specimens without chopped carbon fibers); the results
182 are shown in Figure 5(a) and Table 4. The test program included four different chopped fiber
183 loadings: 0.50%, 0.75%, 1.00% and 1.25% of the cement weight. The cracking strength of the
184 specimens with chopped fibers was 28-45% higher than that of the corresponding reference
185 specimens; this result is consistent with the findings reported in previous studies [23], which
186 stated that chopped fibers can effectively inhibit the cracking of cementitious materials. When
187 the chopped fiber content was less than 0.75% of the cement weight, the mechanical
188 properties of the FRCM composite, such as the cracking strength, ultimate strength and
189 modulus, increased. However, when the chopped fiber content exceeded 0.75% of the cement
190 weight, the excess chopped fibers decreased the FRCM composite strength. It is presumed
191 that the main reason for this phenomenon is that the excess fibers could not be sufficiently
192 dispersed, causing the agglomeration of fibers in the cementitious material.

193 **3.2 Effect of node coating in a CF-MESH**

194 Based on the literature review, coating a CF-MESH could improve the uniformity of the stress
195 distribution in the fiber bundles because the coating can penetrate the core of the yarns,
196 thereby increasing the inner bond between the fiber filaments [27,38]. Therefore, specimens
197 M1-T3 were prepared to investigate the node coating. A comparison of the stress-strain curves
198 of specimens M1-T3 and that of the reference specimens (M1-T1) is shown in Figure 5(b).
199 Before the reference specimens failed, the stress-strain curves of M1-T3 consistently
200 coincided with those of the reference specimens. Afterwards, the M1-T3 curves continued to
201 increase stably. The ultimate strength, ultimate strain and post-cracking modulus of specimens
202 M1-T3 were 42%, 57% and 70% higher than those of the reference specimens, respectively.

203 In the failed M1-T3 specimens, partial fracturing of the fiber bundles was observed (see
204 Figure 7). Similar experimental results were also reported by Kim et al. [28].

205 **3.3 Performance of ECC as a cementitious material**

206 ECC is also a type of cement-based composite that has recently attracted extensive research
207 interest [39,40] due to its advantageous characteristics such as a high toughness, impact
208 resistance, freeze-thaw resistance and fatigue resistance. The key difference between ECCs
209 and other cementitious materials is the high ductility characteristics of ECCs. In this study,
210 ECC is also used as an alternative bonding material for CF-MESH (i.e., specimen M6-T1);
211 the experimental results are presented in Table 4, and the stress-strain curves are shown in
212 Figure 5(c). The M6-T1 specimens clearly exhibited multiple cracking characteristics,
213 wherein new fine cracks continued to appear throughout the entire loading process until
214 specimen failure (see Figure 8). The number of cracks in the M6-T1 specimens was seven
215 times that in the reference specimens, whereas the crack width in the former specimens was
216 notably smaller. For the reference specimens, before the width of the crack suddenly
217 increased, the load was resisted mainly by the bond capacity of the CF-MESH/cementitious
218 matrix. When a major crack occurred, the carbon fiber bundles and cementitious matrix
219 started to experience slippage, and the load was resisted mainly by friction at the
220 CF-MESH/cementitious matrix interface and the external part of the carbon fiber filaments. It
221 should be noted that before matrix-fiber friction is engaged, the matrix-fiber bond capacity
222 should be exploited [41]. However, for the M6-T1 specimens, no major cracks occurred in the
223 cementitious material, and the load was resisted by both the CF-MESH and the ECC
224 throughout the loading procedure. Therefore, although the cracking loads of the M6-T1

225 specimens were close to those of the reference specimens, the ultimate strength, ultimate
226 strain and post-cracking modulus results of the M6-T1 specimens were 77%, 18% and 83%
227 higher than those of the reference specimens, respectively.

228 **3.4 Performance of commercial FRCM composite**

229 For comparison, a commercial FRCM composite (specimens M7-T2) was also considered
230 herein to understand the quality parameters of products on the market and explore whether
231 our FRCM composite materials can generally meet the market requirements. The stress-strain
232 curves from the tests of this material are shown in Figure 5(d), and the test results are
233 presented in Table 4. During loading, all the fiber bundles were pulled out from the
234 cementitious matrix, and the coating on the surface of the fiber bundles peeled off, as shown
235 in Figure 9. This failure mode suggests that the poor performance of the commercial FRCM
236 composites was caused by the premature slippage of the fibers and their coating, although the
237 coating had reasonably good bonding with the cementitious matrix. Thus, the mechanical
238 properties of the commercial FRCM composite specimens were not as good as those of the
239 reference specimens: the cracking strength, ultimate strength, ultimate strain and postcracking
240 modulus of M7-T2 were 69%, 84%, 36%, and 59% lower than those of the reference
241 specimens, respectively.

242 **4. Experimental data collected from the literature**

243 A number of tensile tests on FRCM composites have been carried out and reported in the
244 literature. This paper summarizes a total of 29 available test results covering different fiber
245 meshes (i.e., carbon, glass, polyparaphenylene benzobisoxazole (PBO) and basalt fibers),
246 cementitious materials and gripping devices (i.e., clamping or clevis grips) in Table 5. These

247 data were used with the 24 newly generated test results from this study to form a large data
248 pool for the following discussions. Note that data of only FRCM composites with a single
249 layer of fiber mesh were collected herein and that the stress of the FRCM composites during
250 the tensile test was calculated by dividing the load by the cross-sectional area of the fiber. In
251 these calculations, note that f_f represents the ultimate tensile strength of the fiber, whereas ε_f
252 represents the ultimate tensile strain of the fiber.

253 **5. Discussion on the testing configuration**

254 The experimental data show that in addition to the parameters of the FRCM composites
255 discussed in Section 3, the gripping devices used also affect the structural responses of FRCM
256 composites. The two commonly used gripping devices are clamping grips and clevis grips.
257 The clamping grip method [36] is to directly clamp the ends of the FRCM specimens using
258 the wedge-shaped chuck of the testing machine (the load can be applied to the specimens),
259 and the clevis grip method [19] is to using metallic plates bonded to the specimen ends and
260 connected to the machine (the load is transferred to the specimens through the metallic plates).
261 The tensile behavior of FRCM composites is related to the test set-up adopted. If clevis grip
262 tensile tests are carried out, a bi-linear behavior is generally observed, whereas clamping grip
263 test set-ups usually provide tri-linear curves [42]. The ultimate strength results of the tested
264 FRCM composites with respect to the ultimate strengths of the fibers is shown in Figure 10.
265 In general, when using clamping grips, the ultimate strength results of the FRCM composites
266 are very similar to those of the dry fiber bundles, which indicates that the clamping force
267 effectively improves the interfacial friction between the cementitious matrix and the
268 CF-MESH. This improved interfacial friction postpones slippage of the CF-MESH at the grip,

269 which enables the mechanical properties of the CF-MESH to be better utilized. In contrast,
270 when using clevis grips, the ultimate strength results of the FRCM composites are notably
271 lower than those of the fiber bundles without extra pressure from the grips. Notably, FRCM
272 composites are generally not subjected to lateral pressure when externally bonded to concrete
273 structures as strengthening materials in practical engineering applications. Therefore, FRCM
274 composites are generally not subjected to lateral pressure when externally bonded to concrete
275 structures as strengthening materials in practical engineering applications and the clevis grip
276 configuration can more closely resemble the *in situ* cases which has limited length to fix both
277 ends of the FRCM composite.

278 **6. Discussion on the constitutive models**

279 **6.1 AC434 model and result comparison**

280 The bilinear simplified model for FRCM composites is codified in AC434 [31] with the
281 symbols defined in Figure 11. The model provided by AC434 [31] describes the idealized
282 behavior of a clevis-type test providing a methodology to identify the parameters that will be
283 used in the design of the strengthening intervention, according to ACI 549.4R-13 [36]. In the
284 AC434 model, the stress-strain curve is simplified into two linear parts. The first part of the
285 curve corresponds to the first loading stage (i.e., the uncracked stage). The slope of the linear
286 part corresponding to the uncracked behavior of the specimen can be defined by two points
287 within this linear range [31]. Thus, the tensile elastic modulus $E_{1-AC434}$ of the uncracked
288 specimen is calculated using the following expression:

$$289 \quad E_{1-AC434} = \frac{\Delta f}{\Delta \varepsilon} \quad \text{Eq. 1}$$

290 where Δf is the difference in tensile stress between two selected points and $\Delta \varepsilon$ is the

291 difference in tensile strain between two selected points.

292 After the specimen cracks, some experimental results [27] suggest that new cracks are
293 generated as the crack expansion and fiber filament slippage occurs. According to AC434,
294 two points are selected on the experimental curve at a stress level equal to $0.90 f_u$ and $0.60 f_u$.
295 The slope of the line that connects these two points represents the tensile modulus at the
296 post-cracking modulus. Note that the tensile specimen must have sufficient fabric area to
297 achieve 50% strength over transition point, so that the selected two points will be in the
298 correct part of the curve. The modulus $E_{2-AC434}$ (Eq. 2) is used to define the second linear part
299 of the curve.

$$300 \quad E_{2-AC434} = \frac{0.9f_u - 0.6f_u}{\varepsilon_{u@0.9f_u} - \varepsilon_{u@0.6f_u}} \quad \text{Eq. 2}$$

301 Where f_u is the experimental ultimate strength.

302 The intersection point of the initial and secondary parts of the curves corresponds to the
303 cracking strength $f_{t-AC434}$ and the cracking strain. Thus, the cracking strength can be calculated
304 by the mathematical relationship according to Figure 11, as shown in Eq. 3:

$$305 \quad f_{t-AC434} = E_{1-AC434} \varepsilon_{t-AC434} = E_{2-AC434} \varepsilon_{t-AC434} + (f_u - E_{2-AC434} \varepsilon_u) \quad \text{Eq. 3}$$

306 By converting Eq. 3, the cracking strain $\varepsilon_{t-AC434}$ can be obtained as follows:

$$307 \quad \varepsilon_{t-AC434} = \frac{f_u - E_{2-AC434} \varepsilon_u}{E_{1-AC434} - E_{2-AC434}} \quad \text{Eq. 4}$$

308 The cracking strength $f_{t-AC434}$ can be calculated with the following expression:

$$309 \quad f_{t-AC434} = E_{1-AC434} \left(\frac{f_u - E_{2-AC434} \varepsilon_u}{E_{1-AC434} - E_{2-AC434}} \right) \quad \text{Eq. 5}$$

310 The stress-strain curves obtained from the experiments are compared to the results from
311 the AC434 simplified in model Figure 12. For the AC434 model, the prediction curves fit

312 closely with most of the experimental curves except those of M7-T2. The uncommon
313 stress-strain curves of the M7-T2 specimens might be due to the premature debonding
314 between the fiber bundles and their coating.

315 Furthermore, the predictions of the cracking strength and postcracking modulus by the
316 AC434 models are also compared to the new and collected test results, as shown in Figure 13.
317 For cracking strength (see Figure 13(a)), the AC434 model generally underestimated the test
318 results. In terms of the postcracking modulus (see Figure 13(b)), the predictions of the AC434
319 model were more accurate and consistent with the experimental results.

320 **6.2 ACK model and result comparison**

321 The ACK model for FRCM composites (see Figure 14) was proposed by Aveston and Kelly
322 [32] and Bertolesi et al. [7]. The ACK model can predict the tensile behavior of the FRCM
323 composite once the properties of its components are known. In this model, the stress-strain
324 curve has three stages: the uncracked stage, the crack development stage, and the crack
325 expansion stage. The uncracked stage is the first elastic stage of the curve, which is defined
326 by the initial elastic modulus E_{1-ACK} , as given by Eq. 6:

$$327 \quad E_{1-ACK} = E_f V_f + E_m V_m \quad \text{Eq. 6}$$

328 where E_f and E_m are the tensile Young's modulus of the fiber and cementitious matrix,
329 respectively, and V_f and V_m are the volume fractions of the fiber and the cementitious matrix,
330 respectively.

331 The crack development phase begins with the occurrence of the first crack (point T1 in
332 Figure 14), and the cracking strength (f_{t-ACK}) can be calculated by Eq. 7:

$$333 \quad f_{t-ACK} = \frac{E_{1-ACK} f_m}{E_m} \quad \text{Eq. 7}$$

334 where f_m is the tensile ultimate strength of the cementitious matrix.

335 Multiple fine cracks appear on the specimen as the load continues to increase [44,45].

336 Slips at cementitious matrix and CF-MESH interface begin to take place after the first crack

337 occurs. It is assumed that the frictional shear stress between the cementitious matrix and the

338 CF-MESH (τ) is constant. The spacing of the cracks (δ) is expressed with Eq. 8 based on the

339 force equilibrium along the loading axis of the fiber [21]:

$$340 \quad \delta = \frac{rf_m V_m}{2\tau V_f} \quad \text{Eq. 8}$$

341 where r is the radius of a single filament.

342 In the crack development stage, the distances between cracks are between δ and 2δ . The

343 cracks initiate randomly until new cracks can no longer be generated. According to Widom

344 [46] and Cuypers and Wastiels [44], the average distance between cracks is 1.337δ , so the

345 strain at the end of the second stage (ε_{t2}) can be calculated with Eq. 9 [21,47]:

$$346 \quad \varepsilon_{t2} = \frac{f_{t-ACK}}{E_{1-ACK}} + 1.337\delta \frac{\tau}{E_f} \quad \text{Eq. 9}$$

347 Substituting Eq. 7 and Eq. 8 into Eq. 9 yields the following expression:

$$348 \quad \varepsilon_{t2} = \left(1 + 0.666 \frac{E_m V_m}{E_f V_f} \right) \frac{f_m}{E_m} \quad \text{Eq. 10}$$

349 The third stage (starting from point T2 and continuing to the peak) is the crack expansion

350 stage, in which the widths of the existing cracks increase and the fiber filaments slip or

351 fracture, causing failure. In this stage, the load is carried by only the embedded CF-MESH

352 [19]. The modulus E_{2-ACK} in this stage can be obtained from Eq. 11.

$$353 \quad E_{2-ACK} = E_f V_f \quad \text{Eq. 11}$$

354 Note that Eq. 11 does not consider the presence of tension stiffening, which could be

355 relevant for the high-performance matrices considered in this study. However, since the
356 purpose of this study is to compare the predictions by the ACK model with the tensile
357 behavior of the FRCM composites obtained from tests, the existing equations in the ACK
358 model are remained.

359 The stress-strain curves obtained from the experiments are compared to the results from
360 the ACK model in Figure 15. The ACK model can accurately predict the stress-strain curves
361 in the uncracked stage for all the tested specimens. In the crack development stage, the ACK
362 model curve is also close to the experimental curves of most specimens, with the exception of
363 those of M6-T1 and M7-T2. However, the ACK model predictions for the crack expansion
364 stage are significantly different from all the test curves. According to the discussion in
365 Section 5, a possible reason for these discrepancies might be the use of clevis grips in this
366 study; hence, the strength of the FRCM composite specimens did not continue to increase
367 significantly after cracking without the presence of additional clamping pressure.

368 Furthermore, the predictions of the cracking strength and post-cracking modulus by the
369 ACK models are also compared to the new and collected test results, as shown in Figure 16.
370 For cracking strength (see Figure 16(a)), the ACK model significantly overestimated most of
371 the test results. In terms of the post-cracking modulus (see Figure 16(b)), the predictions of
372 the ACK model cannot accurately predict experimental values.

373 **7. Conclusions**

374 In this study, a total of eight different types of FRCM composites were considered by
375 optimizing the cementitious matrix and carbon fiber meshes. Uniaxial tensile tests were
376 carried out to obtain their structural responses and mechanical properties. The experimental

377 results showed that including a small content of chopped carbon fibers (up to 0.75% of the
378 cement weight) in the cementitious matrix and a preimpregnated epoxy coating on the nodes
379 of the fiber meshes were beneficial for the mechanical properties of FRCM composites. In
380 addition, ECC was also found to be a good bonding material for use in FRCM composites.
381 Both coating the nodes of the fiber meshes and the use of ECC as a bonding material can
382 delay the slippage of carbon fibers. Existing tensile test data of FRCM composites, covering
383 different types of fiber meshes, cementitious materials and experimental gripping devices,
384 were also collected from the literature. Both the newly generated experimental and the
385 collected data are compared with AC434 model and ACK model. The AC434 model was
386 found to be able to capture the experimental curves rather accurately; however, the
387 predictions by the ACK model seems inaccurate. The prediction result of the ACK model
388 overestimates most experimental data.

389 **Data Availability Statement**

390 Some or all data, models, or code that support the findings of this study are available from the
391 corresponding author upon reasonable request.

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Table 1 Material properties of the carbon fiber meshes

Type of fiber meshes	Tensile strength (MPa)	Elastic modulus (GPa)	Break elongation	Fiber area (A_f) (mm^2/mm)
T1	2077	196	0.011	0.0462
T2	441	66	0.007	0.1170
T3	2225	195	0.012	0.0462

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Table 2 Mixing proportion and material properties of the cementitious matrix

Components	M1 (%)	M2 (%)	M3 (%)	M4 (%)	M5 (%)	M6 (%)	M7 (%)
Cement	100	100	100	100	100	100.00	
Limestone powder	/	/	/	/	/	14.29	
Silica fume	/	/	/	/	/	21.43	
Ground granulated blast furnace slag	/	/	/	/	/	107.14	
Silica sand	100	100	100	100	100	71.43	
Water	35	35	35	35	35	46.14	
PE fiber	/	/	/	/	/	2.86	
Carbon fiber	0	0.5	0.75	1	1.25	/	
Polycarboxylate-based high range water	0.18	0.18	0.18	0.18	0.18	9.71	
Water / (Cement + Silica fume + Ground granulated blast furnace)	0.35	0.35	0.35	0.35	0.35	0.22	0.35
Compressive strength (MPa)	60.1	53.2	51.7	52.4	52.0	79.4	34.3
Tensile strength (MPa)	3.3	3.9	4.3	4.0	4.1	3.7	4.7
Elastic modulus (GPa)	12.4	35.2	30.6	43.2	27.1	36.7	20.1

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Table 3 Labeling scheme used for the test specimens

Specimens	Type of cementitious matrix	Type of fiber mesh	Node treatment
M1-T1	M1	T1	No
M2-T1	M2	T1	No
M3-T1	M3	T1	No
M4-T1	M4	T1	No
M5-T1	M5	T1	No
M6-T1	M6	T1	No
M7-T2	M7	T2	No
M1-T3	M1	T3	Yes

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Table 4 Average test results for FRCM

Specimens	Carbon fiber content* (%)	f_t (MPa)	f_u (MPa)	ε_u (%)	E_1 (GPa)	E_2 (GPa)
M1-T1	0.00	682	1225	0.81	2904	74
M2-T1	0.50	916	1257	0.82	7634	50
M3-T1	0.75	991	1307	0.75	6638	80
M4-T1	1.00	876	1276	0.90	9367	57
M5-T1	1.25	898	1251	0.70	3650	75
M1-T3	0.00	725	1740	1.27	3201	126
M6-T1	0.00	640	2168	0.96	5970	136
M7-T2	0.00	210	196	0.52	1110	30

* Percentage to cement weight

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Table 5 Collected tensile test results for FRCM composites

References	Type of fiber mesh	Type of grips	f_t (MPa)	f_u (MPa)	f_f (MPa)	ϵ_u (%)	ϵ_f (%)	E_1 (GPa)	E_2 (GPa)
Larrinaga et al. [21]	basalt	clamping	338	1088	1160	2.15	1.73	1446	43
Bertolesi et al. [7]	PBO	clamping	495	3316	3905	1.69	1.69	878	157
Arboleda et al. [19]	carbon	clamping	482	1492	1900	0.74	0.94	798	186
	PBO	clamping	890	3316	3900	1.69	1.80	1877	216
Ascione et al. [47]	carbon	clamping	137	1222	1914	0.83	1.18	164	131
	glass-aramid	clamping	511	1784	1829	2.02	2.15	274	96
	basalt-stainless steel	clamping	124	345	1471	0.54	3.00	101	61
Carozzi & Poggi [44]	PBO	clamping	724	3319	3900	1.69	1.81	1298	216
	glass	clamping	307	872	1233	0.69	2.22	699	64
	carbon	clamping	438	1492	1944	0.74	0.94	943	186
Santis & Felice [48]	glass-aramid	clamping	404	1851	1829	2.20	1.80	911	91
Caggegi et al. [22]	basalt	clamping	592	912	1089	0.75	1.94	1053	53
D'Antino & Papanicolaou [20]	carbon	clamping	229	838	938	0.73	1.80	1432	114
	carbon	clamping	1645	2745	1890	0.86	0.94	3351	188
	glass	clamping	722	1221	660	1.38	1.41	1288	53
Minafò and Mendola [49]	glass	clamping	606	1317	1400	4.00	4.38	47	32
Arboleda et al. [19]	carbon	clevis	458	1031	1900	1.00	0.94	349	80
	PBO	clevis	375	1664	3900	1.76	1.80	1877	128
Santis & Felice [48]	glass-aramid	clevis	404	1238	1829	1.40	1.80	911	53
Donnini et al. [15]	carbon fiber	clevis	986	575	4900	0.01	2.00	67669	/
	carbon fiber	clevis	1088	713	4900	0.01	2.00	67669	30
	carbon	clevis	875	1358	4900	0.02	2.00	67669	42
	carbon	clevis	782	1366	4900	0.03	2.00	67669	49
D'Antino & Papanicolaou [20]	carbon	clevis	333	417	938	0.79	1.80	693	417
	carbon	clevis	433	1393	1890	0.86	1.18	1131	172
	glass	clevis	281	593	660	1.97	1.41	630	39
Donnini et al. [29]	glass	clevis	604	1275	1405	4.90	2.40	1709	29
Ebead & Younis [50]	carbon	clevis	260	970	3580	1.25	1.50	378	75
	PBO	clevis	487	1235	4980	0.90	1.80	601	112