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1 **Complex relationships between water discharge and sediment**
2 **concentration across the Loess Plateau, China**

3
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19 **Abstract**

20 Understanding the relationship between water discharge (Q) and suspended
21 sediment concentration (SSC) across the Loess Plateau is a prerequisite for evaluating
22 soil and water conservation measures. Using daily Q and SSC datasets, this study jointly
23 analyzes changes in Q and SSC on the central Loess Plateau, a major sediment-
24 producing area of China, during the periods 1971–1987 (P1) and 2008–2016 (P2). The
25 results show that during both P1 and P2, the contribution of the maximum-3-day-per-
26 year sediment load to the total annual sediment load (SSL) is almost invariably over 50%
27 (dominant), and in the majority of cases, the size of this contribution increases further
28 between P1 and P2. The contribution of extremely high SSL events plays an
29 overwhelming role in watersheds of area $< 10,000 \text{ km}^2$ and appears to be almost
30 independent of change in land cover condition. In the Helong section of the Yellow
31 River, there is more evident reduction in SSC than Q between these two periods
32 (streamflow became clearer), while the opposite occurred in the Jing River (streamflow
33 declined). In addition, the range of variation in SSC is large for small Q values, whereas
34 the SSC for flood events tends to be relatively stable in gullied-hilly and flat-surfaced
35 (*Yuan*) loess areas, which are major sediment producers. Based on scatter plots of SSC
36 versus Q after logarithmic transformation, we find that the lower boundary of the
37 mapped data points for an individual station fits a straight line. This boundary relates
38 to riverbed erosion. Given that soil erosion weakened on gully slopes over time and
39 streamflow in channels during P2 was generally lower, the boundary tended to move
40 downward between P1 and P2 for most watersheds, reflecting a reduction in SSC for a

41 given value of Q in P2 compared to P1.

42

43 **Key words:**

44 Loess Plateau; Extremely high *SSL* events; Discharge–sediment relationship; Stable

45 sediment concentration; Sediment carrying capacity;

46

1 Introduction

The relationship between discharge and sediment load poses a longstanding key challenge in the field of hydrology, and reflects the characteristics of sediment deposition and transport in rivers (Guan, 1999). Müller and Förstner (1968) reported that the water discharge–sediment concentration relationship of a basin can be expressed by the empirical power function $SSC = a \times Q^b$, where SSC is suspended sediment concentration (kg/m^3), Q is discharge (m^3/s), and a and b are parameters. This has been verified for different basins around the world, including the Colorado River near the Grand Canyon (Gray et al., 2008), the Sukhaya Elizovskaya River (Mouri et al., 2014), the Magdalena River (Higgins et al., 2016), and the Ceyhan River Basin (Yüce et al., 2018). However, the discharge–sediment relationship varies across space and time and is vulnerable to human activities (e.g. land use change and soil and water conservation engineering measures) and unexpected events (e.g. landslide and hillslope collapse); this makes development of accurate simulations challenging. Consequently, in addition to conventional statistical methods, new methods, such as artificial neural networks (Yang et al., 2009) and Gaussian mixture modeling (Gournelos et al., 2020), have been developed and applied in the study of discharge–sediment relationships.

The Loess Plateau, located in northern China, contains the middle Yellow River. This region is famous for its severe soil erosion and complex discharge–sediment relationships. To control soil erosion and prevent sediment from entering the Yellow River, many large-scale soil and water conservation projects were introduced starting in the 1970s, followed by ecological projects from 1999 onwards. These projects

69 profoundly changed conditions on the plateau and greatly altered the complex
70 discharge–sediment relationships (Zhang et al., 2017; Zhao et al., 2012). Researchers
71 have devoted much effort to trying to model these relationships and hence interpret their
72 temporal variation (Wang et al., 2007; Zhao et al., 2017; Zheng et al., 2020). Using a
73 monthly dataset for 14 watersheds and a daily dataset for 9 watersheds on the Loess
74 Plateau, Gao et al. (2018) proposed a generalized power-law sediment rating curve by
75 which to describe the daily water discharge–sediment relationship, and linear functions
76 for annual and monthly discharge–sediment relationships. Using a daily Q and SSC
77 dataset for the Beiluo River basin, Zhang et al. (2017) demonstrated that the streamflow
78 and the discharge–sediment relationship both changed due to recent ecological
79 restoration measures. In the context of climate change (Gou et al., 2019; Sun et al.,
80 2019), extremely intense hydrological events have always been a major concern
81 regarding sediment flux. Previous researchers reported that the decrease in SSL is
82 mainly caused by the changing discharge–sediment relationship during flood events,
83 whereas the relationship for relatively small values of Q involves only limited change
84 (Liao et al., 2008; Rustomji et al., 2008; Xu, 2002). However, Zheng et al. (2007)
85 reported that the SSC in certain small watersheds in gullied-hilly areas remained
86 relatively stable under heavy storms and changes in area of vegetation cover did not
87 alter the discharge–sediment relationship. The foregoing leads us to speculate about the
88 change in discharge–sediment relationship that occurs between extreme and ordinary Q
89 events, separate from the degree of change in Q and SSC .

90 In this study, we analyze changes in the SSC – Q relationship for the major

91 sediment-producing area of the Loess Plateau. Specifically, we determine the change in
92 extremely high *SSL*, compare the degree of change in both *Q* and *SSC*, devise
93 expressions for the patterns of change in *SSC–Q* relationships, and examine the leading
94 reasons behind these changes. An understanding of the change characteristics inherent
95 to the *SSC–Q* relationship for the Loess Plateau would provide a foundation for
96 optimizing the production and transportation processes affecting streamflow and
97 sediment and for evaluating and hence prioritizing different soil and water conservation
98 measures.

99

100 **2 Data and Methods**

101 **2.1 Study area and dataset**

102 The Loess Plateau of China, a cradle of ancient Chinese civilization, possesses the
103 most concentrated and largest area of loess in the world. It is highly prone to soil
104 erosion, with the most severe areas situated along the Helong section of the Yellow
105 River basin (hereafter, ‘the Helong section’), the Beiluo River, and the Jing River. Taken
106 together, these areas account for about 92% of the total *SSL* on the Loess Plateau during
107 1956–2000 (Ran, 2006), even though their total area accounts for just 29% of the total
108 area of the plateau. Changes in *SSC–Q* in these regions have long been of great concern.
109 Moreover, these regions have a characteristic landscape that produces sediment, called
110 the loess gully area (which includes the loess gullied-hilly areas and the loess *Yuan*
111 areas depicted in Fig. 1). The mean annual sediment yield of the loess gully area reached
112 10,000 t/km² before 1970 (Gong and Jiang, 1978). In recent years however, soil erosion

113 in most regions has been successfully controlled through soil management measures
114 (Xin et al, 2009), whereas the discharge–sediment relationship has become more
115 complicated due to human activities.

116

117 < Figure 1 >

118

119 In the present study, our dataset comprises daily records of Q (m^3/s) and SSC
120 (kg/m^3) acquired at 47 hydrological stations located on the Helong section, the Beiluo
121 River, and the Jing River (Fig. 1) for two periods spanning 1971–1987 (P1 period) and
122 2008–2016 (P2 period). The data were obtained from the Hydrological Yearbooks of
123 the People’s Republic of China, compiled by the Yellow River Conservancy
124 Commission (<http://www.yellowriver.gov.cn/>). Basic information for the three basins is
125 presented in Fig. S1. The wet season is the most important period for sediment
126 generation and transport in the Yellow River, with nearly 95% of sediment transported
127 from May to October (Zheng et al., 2019). Taking the integrity of the dataset into
128 account, also, we only use wet-season data (which is quite complete) to analyze changes
129 in the SSC – Q relationship.

130

131 **2.2 Methods**

132 **2.2.1 Quantifying the contribution of SSC to changes in SSL**

133 It is of interest to know whether Q or SSC plays the bigger role in the observed
134 sediment load changes between periods P1 and P2. To determine this, we use a simple

135 method that first divides the daily SSC by the daily Q to give the daily SSC/Q ratio.
 136 Then, we calculate the mean value and the standard deviation (std) of SSC/Q sequence
 137 values in P1 and in P2 and compare them. We pretreat the data by removing daily Q
 138 values that are less than $0.01 \text{ m}^3/\text{s}$ and the corresponding SSC values, because for $Q <$
 139 $0.01 \text{ m}^3/\text{s}$, the resulting value of SSC/Q would be very large and disproportionately
 140 influence the mean and std of the SSC/Q values. The number of instances where $Q <$
 141 $0.01 \text{ m}^3/\text{s}$ accounts for less than 10% of the data for all stations except for two stations
 142 in P1 and four stations in P2.

143 To quantify the contribution of SSC to the change in SSL , we perform an additional
 144 set of calculations through matching the probability density function (PDF) curves for
 145 discharge. The steps are as follows:

146 (i) First compress the PDF curves for discharge during the P1 period according to
 147 those during P2; that is, reconstruct the Q sequence in P1 (i.e., $Q_{P1,sim}$). Next, calculate
 148 the 1st, 2nd, ..., 99th, and 100th percentiles of the Q sequence in P1 and P2, respectively,
 149 and then scale these percentile values in P1 according to the corresponding percentiles
 150 in P2. Then, 100 scaling factors are obtained as follows:

$$\begin{aligned}
 k_1 &= per^{1st,P2} / per^{1st,P1} \\
 k_2 &= per^{2nd,P2} / per^{2nd,P1} \\
 &\dots \\
 k_{99} &= per^{99th,P2} / per^{99th,P1} \\
 k_{100} &= per^{100th,P2} / per^{100th,P1}
 \end{aligned} \tag{1}$$

151 where $per^{xth,P1}$ and $per^{xth,P2}$ are the x^{th} percentile of the Q sequence in P1 and P2, and x

152 = 1, 2, ..., 99, 100. Next, the Q values are scaled between 0 and $per^{1st,P1}$ by k_1 , between
 153 $per^{1st,P1}$ and $per^{2nd,P1}$ by k_2 , ..., and between $per^{99th,P1}$ and $per^{100th,P1}$ by k_{100} . This
 154 provides a simulated Q sequence for P1 ($Q_{P1,sim}$).

155 (ii) The portion of change in SSL solely due to SSC change (SSL_{SSC}) is calculated
 156 from:

$$SSL_{SSC} = \sum Q_{P1,sim} \cdot SSC_{P1,mat} - \sum Q_{P2} \cdot SSC_{P2} \quad (2)$$

157 Here, the PDF curve of $Q_{P1,sim}$ is nearly the same as that of Q_{P2} , and SSC_{P2} and Q_{P2} are
 158 the observed SSC and corresponding Q during P2. The $SSC_{P1,mat}$ is the matched value
 159 of SSC for each interval (step length set to 3) of observation Q in P1 and, for a specific
 160 interval, is calculated from:

$$SSC_{P1,mat} = \sum (Q_i \cdot SSC_i) / \sum Q_i \quad (3)$$

161 where Q_i and SSC_i are the Q and related SSC values in the specific interval, respectively.

162 (iii) The contribution of SSC to the change in SSL from P1 to P2 is

$$\text{Contribution of } SSC = \frac{SSL_{SSC}}{SSL_{SSC} + SSL_{not}} \quad (4)$$

163 where SSL_{not} is the SSL under the hypothetical condition that the PDF curves of SSC
 164 and Q in P1 are both the same as in P2 (which is equal to the observed SSL during P2).
 165 More details about the PDF-matching method and its uncertainty discussion can be
 166 found in the supplementary materials.

167

168 **2.2.2 Estimating the boundaries of numerous scatter plots**

169 From the observed dataset, we find that scatter plots of SSC against Q exhibit
 170 distinct areas of concentration for most watersheds. Taking Station 31 as an example

171 (Fig. 2), we plot lines to fit the upper and lower boundaries of the data to delineate these
172 areas of concentration. The lines show that SSC varies greatly when Q is small, whereas
173 SSC tends to be relatively stable for large Q events (Fig. 2a and b). Next, we consider
174 the change in position of boundary lines between the two periods as reflecting the
175 change in the discharge–sediment relationship (Fig. 2c). We then carry out a logarithmic
176 transformation (using the natural logarithm) on both SSC and Q to further study the
177 changing features of the relationship. We find that a linear equation gives a satisfactory
178 fit to the lower boundary of the logarithmically transformed data points (Fig. 2d and e).
179 Details for estimating the boundaries of the numerous scatter plots follow.

180 First, the reordered Q sequence is divided into a large number of intervals of fixed
181 step length. Then, the points with smallest or largest SSC are identified in each interval
182 (i.e., the prepared points) and used to fit the boundary using a nonlinear equation (Fig.
183 2a and b),

$$y = a \cdot \exp^{-\frac{x}{b}} + c \cdot \exp^{-\frac{x}{d}} + e \quad (5)$$

184 where a , b , c , d , and e are fitting parameters (Fig. 2a and b), and using a linear equation
185 (Fig. 2d and e). To delineate the boundary, we use bootstrap sampling (with drop-back
186 sampling). Specifically, we first randomly pick 75% of the prepared points to fit the
187 boundary. Then we repeat the step 50 times to obtain 50 lower boundaries (Fig. 2d and
188 2e). To check the effect of sample size on boundary fitting, we also randomly pick 25%
189 and 50% of points to fit the boundary, again repeating 50 times. Fig. S4 presents the
190 results. We find the lower-boundary fitting equations to be robust. In addition,
191 considering that the distribution of observed SSC – Q points is extremely uneven, we fit

192 the lines using a few larger Q points, so that a single line appears in Fig. 2a and b. More
193 details about the uncertainty analysis and applicability of the method are given in the
194 supplementary material. We call this method ‘Boundary Estimation with Interval
195 Extremum’ (BEIE).

196

197

< Figure 2 >

198

199 **3 Results**

200 **3.1 Change in contributions of extremely high SSL events to total SSL**

201 In this paper, extremely high *SSL* events refer to maximum- n -day-per-year *SSL*
202 events during period P1 or period P2 ($n = 1, 2, \dots, 6$). Fig. 3c shows that contributions
203 of maximum-3-day *SSL* generally exceeded 50% in both P1 and P2. However,
204 compared with P1, most contributions became larger in P2 (the majority of points are
205 above the 1:1 dashed lines), which illustrates that extremely high *SSL* events have
206 played a more important role in recent years and suggests that the effect of soil
207 management measures on extremely high *SSL* events was not as strong as on ordinary
208 *SSL* events. Fig. 4 shows the relationship between the percentage contributions of
209 extreme *SSL* events (occurrence ranging from 1 to 6 days per annum) with the control
210 area of the hydrological stations. Other than for the maximum-1-day *SSL* event (Fig. 4a
211 and g), the contributions of extremely high *SSL* events generally dominate (exceeding
212 50%) when the watershed area is less than 10,000 km² (see points in the top left
213 quadrant of each graph), and this relationship with watershed area has little to do with

214 change in land cover conditions. We speculate that when the basin area is larger than a
215 specific threshold value (such as the 10,000 km² value identified in this study),
216 underlying conditions rather than topography might play a more critical role in the
217 sediment load at the outlet of a basin; conversely, the topography determines the
218 extremes for relatively small basins.

219

220 < **Figure 3** >

221 < **Figure 4** >

222

223 **3.2 Contribution of *SSC* to the change in *SSL***

224 Both *SSC* and *Q* decreased in P2 relative to P1. Fig. 5a shows that the average
225 value of *SSC/Q* was almost invariably smaller in P2 than in P1 (except for one outlier),
226 indicating that the reduction in *SSC* was effectively much larger than the reduction in
227 *Q*. Fig. 5b shows that the variability in *SSC/Q* was also much smaller in P2 than in P1
228 (except for two outliers). Fig. 5 shows that the expected value and variability of *SSC*
229 decreased relative to that of *Q* between periods P1 and P2; this resulted in a significant
230 increase in *SSL*. For example, Generally speaking, sudden gravity erosion events,
231 such as landslide or hillslope collapse, could lead to small *Q* and large *SSC*. Increased
232 frequency of such events could raise the standard deviation of *SSC/Q*.

233 Then, through quantifying the contribution of *SSC* to the change in *SSL*, we found
234 that the contribution of *SSC* is generally more than 50% for watersheds in the Helong
235 section, whereas the contribution of *SSC* in the Jing River basin is generally less than

236 50%; this implies that the factor driving the drop in *SSL* is the decline in *SSC* in Helong
237 and the decline in *Q* in the Jing River. This is basically consistent with the results
238 produced using double mass curves (Figs S7 and S8). In addition, Fig. 6 shows that
239 many contribution values are concentrated around 76%. So, in brief, even though both
240 *Q* and *SSC* decreased on the central plateau, the decline in *SSC* is more important than
241 the decrease in *Q*.

242

243 < **Figure 5** >

244 < **Figure 6** >

245

246 **3.3 Changes in upper and lower boundaries of *SSC* vs. *Q* scatter plots**

247 Just as at Station 31 (discussed in Section 2.2.2), the *SSC*–*Q* distributions during
248 the P1 period have distinct areas of concentration for watersheds where gully landforms
249 dominate the control area (Fig. 7). However, this distribution pattern is not common in
250 the more complicated geomorphologic regions (Fig. S6), demonstrating that the pattern
251 correlates closely with geomorphic characteristics. For watersheds dominated by gully
252 landforms, the general trend in the upper boundary line for *SSC* is to decline slightly at
253 first and then stabilize with increasing discharge. By comparison, the trend in the lower
254 boundary is first to increase and then to reach a stable value with greater *Q* values. In
255 other words, *SSC* in larger *Q* events (flood events) remains relatively stable in these
256 watersheds. However, the boundaries of about half of these watersheds are indistinct
257 (*SSC*–*Q* distribution is irregular) in P2. For the other half of these watersheds, we found

258 that both boundaries tended to move downward between P1 and P2, except for the Jing
259 River basin.

260

261

< **Figure 7** >

262

263 With respect to the lower boundary, it is obvious that its fit is not very precise
264 because most Q data are concentrated at smaller values, and there is an enormous
265 difference between the smallest and largest values. Given that the lower boundary
266 relates to streamflow erosivity, we carried out log transformations of $SSC-Q$ and then
267 focused on middle and large Q values. With these transformed values, we found that a
268 linear equation can describe the mapped lower boundary well for almost all watersheds
269 (Fig. 8). The lower boundary, corresponding to the smallest SSC in the streamflow,
270 relates to the sediment carrying capacity of the river channels. As Q increases, the
271 scouring capacity of the streamflow is enhanced, and so SSC becomes greater. This
272 process continues until reaching dynamic equilibrium between erosion and deposition,
273 and after that, SSC tends to be stable.

274

275

< **Figure 8** >

276

277 In fact, the upper and lower boundaries are both extreme cases — that is, cases
278 where the SSC on slopes is extremely high or close to zero (i.e., clear runoff). More
279 often, the observed SSC at the watershed outlet lies somewhere between the two

280 boundaries. And at daily scale, the raw $SSC-Q$ relationship cannot be described by a
281 statistical regression equation for most watersheds.

282

283 **4 Discussion**

284 **4.1 Upper and lower boundaries and stable SSC in the loess gully area**

285 The surface of the loess gullied-hilly area is severely incised due to water erosion,
286 sometimes in combination with wind erosion (Fig. 9). Ravine density can reflect the
287 surface degree of crushing. According to Tian et al. (2013), gully density in the central
288 area of the Helong section is up to 10 km/km^2 , and the density in the central area of the
289 Loess Plateau is generally more than 3.5 km/km^2 . Dense gullies provide key transport
290 and storage conditions for sediment, and so slopes and gullies (or channels) become the
291 two main sources of sediment in such watersheds. The type of soil erosion is mainly
292 raindrop splash erosion and sheet erosion on the tops of slopes, rill erosion on the
293 middle and upper parts of slopes, and gully erosion and gravity erosion on the lower
294 slopes (Zheng et al., 2007). Gravity erosion (such as landslides and avalanches) is one
295 of the most important forms of sediment production on the Loess Plateau, and the
296 sediment from gravity erosion is about 20%–25% of the total sediment production of a
297 watershed (Yang et al., 2011). Gravity erosion provides a large quantity of loose
298 material for water flow, resulting in a generally higher SSC during heavy storms on the
299 central Loess Plateau.

300

301

< **Figure 9** >

302

303 Research by Xu (2004) has revealed that slope–channel systems (i.e., those with
304 vertically differentiated landforms) in the loess gully area have an important influence
305 on the formation of high-concentration flows. Xu suggested a storage–release
306 mechanism through which relatively coarse fractions of sediment are more likely to be
307 temporarily deposited and stored in gully channels when slope runoff is relatively low
308 (for example, as a result of small precipitation events), and the deposited sediments
309 might be then carried away later by the high-concentration runoff when heavy
310 precipitation occurs. Wang et al. (1982) reported that many channels have been cut into
311 bedrock in the gullied-hilly area, and so deposition and erosion occur alternately at
312 different times. In short, severe soil erosion on slopes along with a certain level of
313 sediment storage in channels have together ensured a high sediment yield in the loess
314 gully area.

315 The sediment carrying capacity of streamflow refers to the amount of sediment
316 transported by the streamflow when the riverbed is in an equilibrium state of erosion
317 and deposition (Xu, 1999). Many factors determine sediment carrying capacity, most
318 notably, drainage characteristics (slope, river length and shape, etc.) and sediment
319 properties. When the sediment transport rate reaches the sediment carrying capacity of
320 the streamflow, the riverbed is in a state of dynamic equilibrium whereby the rate of
321 deposition equals the rate of erosion. Fig. 7 shows that *SSC* in flood discharges tends to
322 be relatively high and stable in these areas. But why does *SSC* remain stable? Fig. 9
323 provides an illustrative explanation of the stability mechanism for *SSC* change during

324 storm events in the wet season. For high *SSC* of slope flood runoff, sediment is
325 deposited in channels; whereas for lower *SSC* of slope flood runoff, material previously
326 deposited after erosion in the lower slopes or channels is carried away, thus increasing
327 *SSC* in the channels. Hence, the actual streamflow sediment load always approaches
328 the sediment carrying capacity provided the land surface cover remains essentially
329 unchanged. In other words, the stable *SSC* of slope flood runoff may be considered a
330 proxy for sediment carrying capacity. Given the stable, high values of *SSC* during flood
331 events, the contribution of extremely high *SSL* events to the total *SSL* is usually
332 dominant (i.e., more than 50%) for relatively small, gullied watersheds (Figs. 3 and 4).
333 In general, the value of *SSC* observed at the hydrological station will be above the lower
334 boundary since that the lower boundary represents the fitting relationship between the
335 lowest *SSC* and the corresponding *Q*.

336

337 **4.2 Effect of land cover on the change in upper and lower boundaries in the loess** 338 **gully area**

339 Check dams are among the most important types of engineering measures on the
340 Loess Plateau (Li et al., 2019). Check dams are usually small and have limited life span.
341 Their main function is to intercept sediment to create farmland. Check dams promote
342 sediment deposition by intercepting and slowing the discharge (Liu et al., 2018), and
343 thus alter the relationship between water discharge and sediment flux (Zhang et al.,
344 2019). Li and Liu (2018) report that 50,935 check dams had been built in the upper
345 reaches of the Yellow River, above Tongguan station (at the mainstream of the Yellow

346 River) by 2012 when the average amount of intercepting sediment reached 204 million
347 tons per year. *SSC* reduction is the major reason for the decrease in *SSL* in the Helong
348 section, whereas *Q* reduction drove decreasing *SSL* in the Jing River; this may be due
349 to the much larger number of check dams in the Helong section than in the Jing River
350 (Li and Liu, 2018).

351 Besides check dams, the main difference between periods P1 and P2 is in land use
352 through implementation of the Grain-for-Green Project on the Loess Plateau. Fig. 10
353 shows that the cultivated land area shrank notably but grassland and woodland area
354 exhibited large increases. Vegetation cover area on the central plateau, also reflected in
355 the Normalized Difference Vegetation Index (NDVI), increased significantly by P2
356 (Miao et al., 2012; Zheng et al., 2019). Sloping farmland in this region was largely
357 converted to grassland or shrubland (Yu et al., 2009), which led directly to a great
358 reduction in slope erosion (Dang, 2011; Sheng et al., 2016). The effect of natural
359 vegetation on runoff and sediment flux is profound (Jiao et al., 2012; Yu et al., 2012).
360 Interception of precipitation by vegetation leaves and trunks reduces the kinetic energy
361 of raindrops and weakens soil erosion. Vegetation litter increases surface roughness,
362 thus lowering runoff velocity and volume, increasing infiltration, and reducing
363 sediment lateral transport. Plant roots stabilize the soil structure, raise soil resistivity,
364 increase gully slope stability, and reduce the occurrence frequency of gravity erosion
365 events (Miao et al., 2020). Consequently, an increase in vegetation cover reduces not
366 only the volume and velocity of runoff but also the *SSC*, and it may change sediment
367 deposition in rivers. Given the weaker soil erosion of slopes and the stronger

368 interception ability of channels (check dams) in P2, the discharge–sediment relationship
369 connects more closely to channel than slope transport processes. A change in the
370 sediment transport processes in channels therefore alters the sediment carrying capacity
371 of the streamflow (Fig. 7).

372 **< Figure 10 >**

373

374 It is interesting to see a declining trend depicted by the upper boundaries. Even
375 when Q is quite small, the associated observed SSC can be extremely high. This is most
376 likely due to sudden gravity erosion. Furthermore, if antecedent soil moisture starts to
377 be saturated, the soil's resistance to rainfall erosion weakens greatly. Under these
378 conditions, surface soil is prone to gravity erosion (such as landslide or gully slope
379 collapse) during rainfall events and the phenomenon of 'small Q –high SSC ' may occur.

380 Compared with period P1, the range of variation in SSC is smaller and the SSC – Q
381 distribution seems more irregular in P2. However, the lower boundaries of log-
382 transformed SSC – Q again form distinct lines (Fig. 8) and the boundaries tend to move
383 downward, except for the Jing River. This is the overall consequence of land use change
384 and check dams. Q reduced greatly as grassland and woodland area increased
385 significantly (Zhang et al., 2000). Moreover, the reductions in both Q and SSC may
386 have led to the actual streamflow sediment load being insufficient to reach the sediment
387 carrying capacity. As a result, the phenomenon of unstable SSC was commonplace in
388 many watersheds during P2. Of course, the streamflow may reach a new equilibrium
389 state under changed sediment carrying capacity, reflected by a new stable value for SSC

390 during P2. Because of the weakening of soil erosion caused by land use and the
391 lowering of streamflow kinetic energy (via velocity and volume) caused by land use
392 and check dams, the upper and lower boundaries of *SSC* generally moved downward
393 (Fig. 7) for most watersheds. Moreover, when insufficient sediment was deposited in a
394 channel, then the *SSC*–*Q* distribution tended to be irregular. However, in the Jing River
395 basin, several stations displayed an upward shift of the linear lower boundaries between
396 P1 and P2 (Fig. 8), and the resulting reduction in *SSL* can be attributed to declining *Q*,
397 not *SSC* (Fig. 6). We may infer that slope erosion in the Jing River basin was still
398 considerable, and sediment deposition on the riverbed was likely to be greater in period
399 P2, because the reduced discharge could not carry away all the sediment from the gully
400 slopes.

401

402 **5 Conclusions**

403 Based on daily discharge (*Q*) and sediment concentration (*SSC*) data from 47
404 hydrological stations in the major sediment-producing areas on the Loess Plateau (the
405 Helong section of the Yellow River, the Beiluo River, and the Jing River), this paper
406 has explored joint changes in *Q* and *SSC* from period P1 (1971–1987) to P2 (2008–
407 2016). The results show that during both P1 and P2, the contributions of maximum-3-
408 day-per-year sediment load (*SSL*) to the total *SSL* generally exceeded 50% (dominant),
409 and in the majority of cases, these values become larger by P2. The contribution of
410 extremely high *SSL* events (maximum-*n*-day-per-year *SSL*, $n = 1, 2, \dots, 6$) is generally
411 dominant for watersheds whose area is $< 10,000 \text{ km}^2$; this relationship with watershed

412 area has little to do with change in land cover conditions. Moreover, to determine
413 whether the streamflow became more dilute (in terms of sediment concentration) or less
414 (in terms of water amount) by P2, we calculate and analyze the degrees of change in
415 both SSC and Q . We find that the degree of reduction in SSC is greater than that of Q
416 for most watersheds (28 out of 47), especially in the Helong section. However, the
417 driving factor behind SSC decline is the decrease in Q for the Jing River basin. Also, we
418 find that the range of variation in SSC for smaller values of Q is large, and SSC during
419 flood events tends to be relatively stable in the loess gullied-hilly and *Yuan* areas. In
420 addition, we investigate a linear equation that can describe quite well the lower
421 boundary of an SSC – Q distribution after logarithmic transformation of each variable;
422 this relationship is likely to be related to riverbed erosion. Given the weakening soil
423 erosion of slopes during P2 and the lower volume and slower streamflow in channels,
424 the boundary lines tended to move downward between the two periods.

425

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432 providing the precipitation data (<http://data.cma.cn/>).

433

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560 2032(07)60075-4

561 **Figure Captions**

562 Fig. 1 Locations of 47 hydrological stations in the middle of the Loess Plateau, China.

563 Stations 1–9 are located in the eastern Helong section (left side of the main stream)
564 of the Yellow River. Stations 10–30 are located in the western Helong section
565 (right side of the main stream) of the Yellow River. Stations 31–37 are located in
566 the Beiluo River basin, and Stations 38–47 are located in the Jing River basin.

567 Fig. 2 Example showing how the boundary lines at Station 31 are determined. Panels

568 (a) and (b) show the nonlinear upper and lower boundaries for Q in P1 and P2.

569 Panels (c) and (f) depict the movement of the boundaries between P1 and P2.

570 Panels (d) and (e) show the linear lower boundaries after logarithmic

571 transformation of Q and SSC in P1 and P2. Note that the nonlinear boundaries in

572 (a) and (b) indicate the stability of SSC with increasing Q , using relatively larger

573 Q values and the related SSC values for fitting; whereas the linear boundaries in

574 (d) and (e) emphasize the erosive ability of streamflow with low sediment loads,

575 and they use medium Q values and their related SSC for fitting. Here medium Q

576 values refer to those Q between two critical Q values, and the points with the

577 smallest SSC show an almost linear relationship when Q is above one of the critical

578 values; and SSC is relatively stable when Q is above another critical value.

579 Fig. 3 Contribution of total maximum- n -day-per-year SSL to total SSL during P1 and

580 P2 periods (contribution = \sum (sum of maximum- n -day-per-year SSL) / total SSL

581 in P1 or P2), $n = 1$ (a), 2(b), 3(c), 4(d), 5(e), and 6(f). Each red point represents a

582 value from a single station. Note that the maximum- n -days here are not necessarily

583 consecutive.

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586 upper panels) and P2 (red points, lower panels). Panels (a–f) show the
587 contributions of maximum-1-day to maximum-6-days *SSL* to total *SSL* with
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591 above and below 10,000 km² in each graph.

592 Fig. 5 (a) Mean and (b) standard deviation of SSC/Q values, where $Q \geq 0.01$ m³/s,
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594 single station).

595 Fig. 6 Changes in contributions of *SSC* to changes in *SSL* from P1 to P2. The box in the
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598 at Station ID 3, and the negative value means the *SSC* may increase from P1 to P2,
599 especially for small-to-medium discharges.

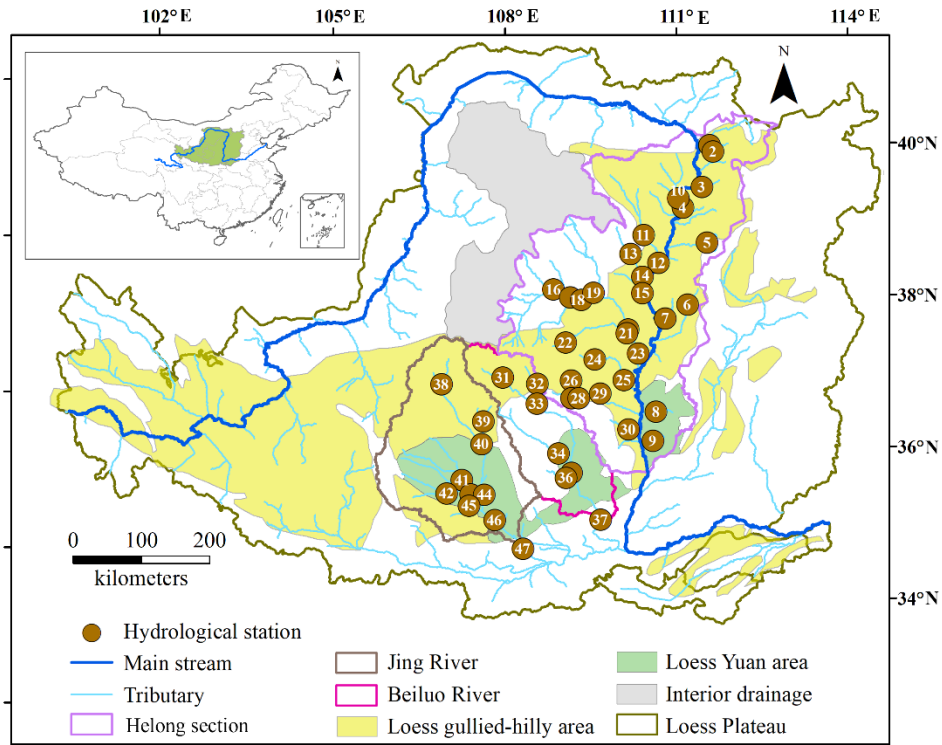
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601 dominate the control area. Pink and black curves delineate the upper and lower
602 boundaries of the data points. The captions correspond to station numbers in Fig.
603 1 and Table S1. The map at the bottom right summarizes how these boundary lines
604 in the $SSC-Q$ graphs changed between P1 and P2 for stations across the region.

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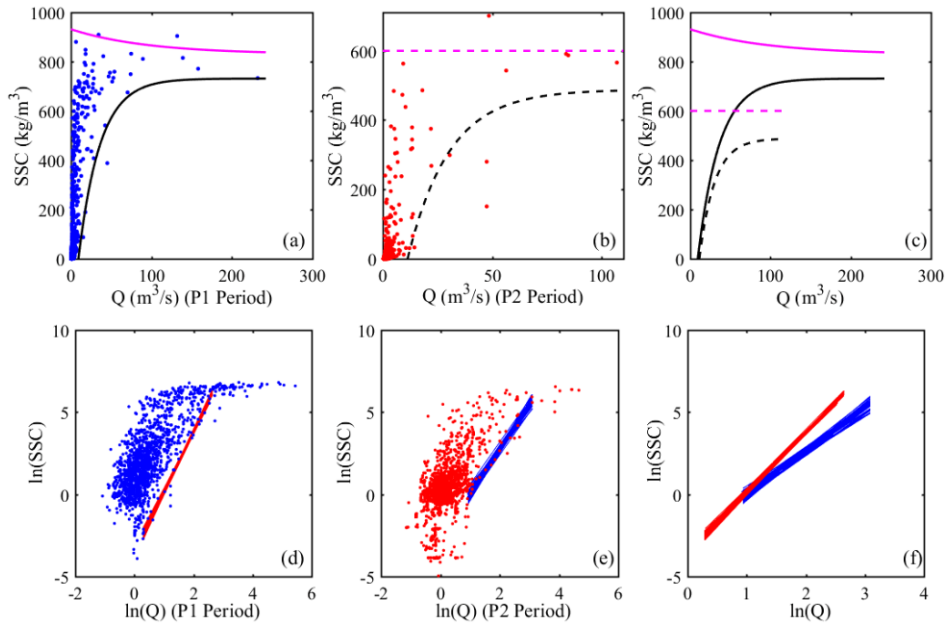
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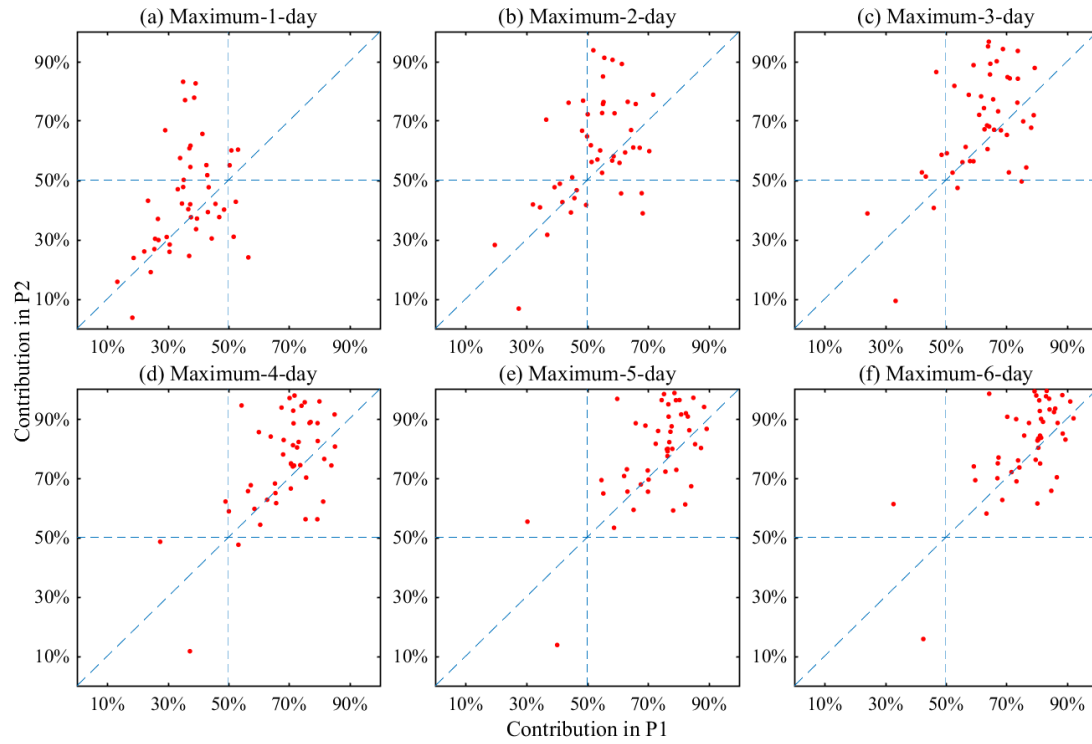
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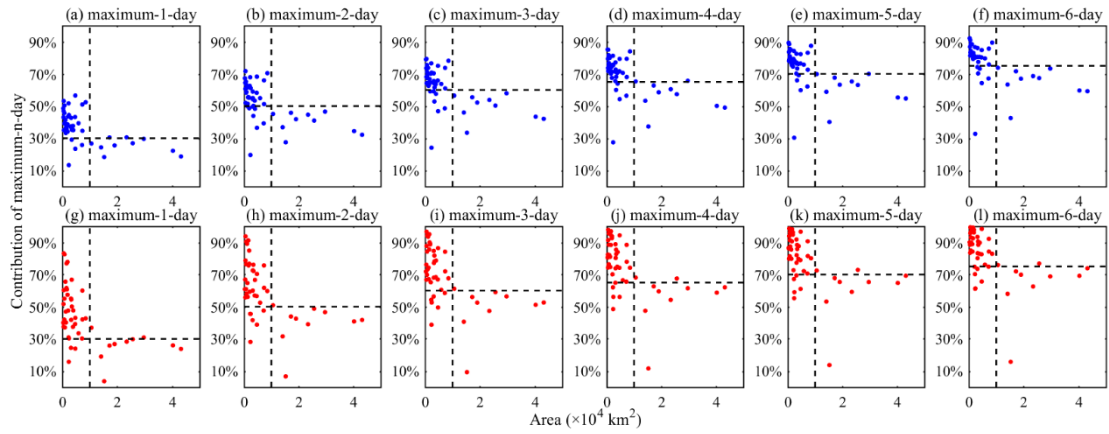
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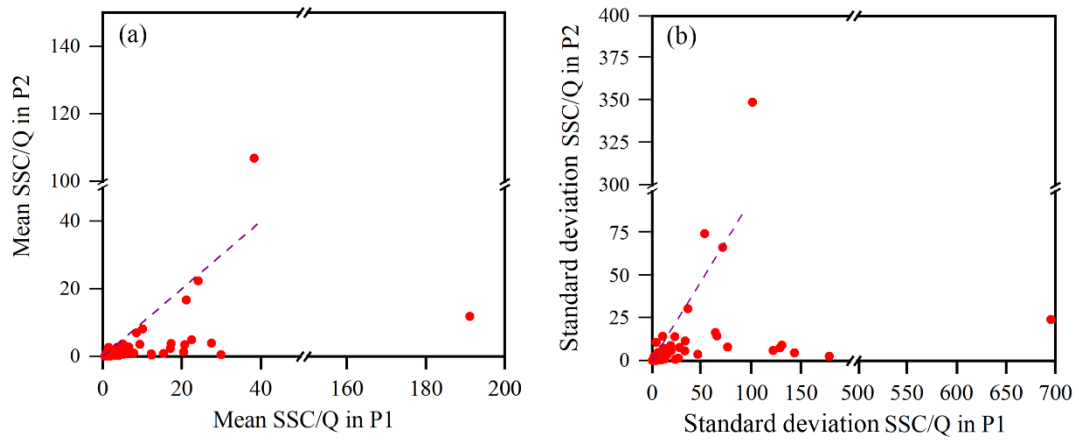
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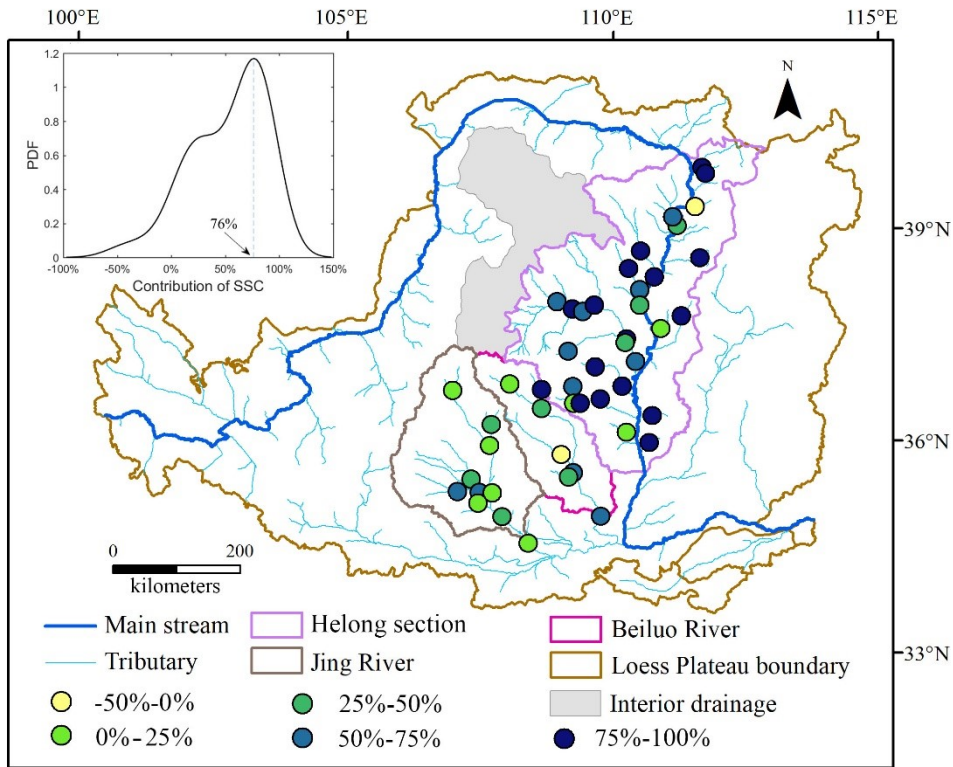


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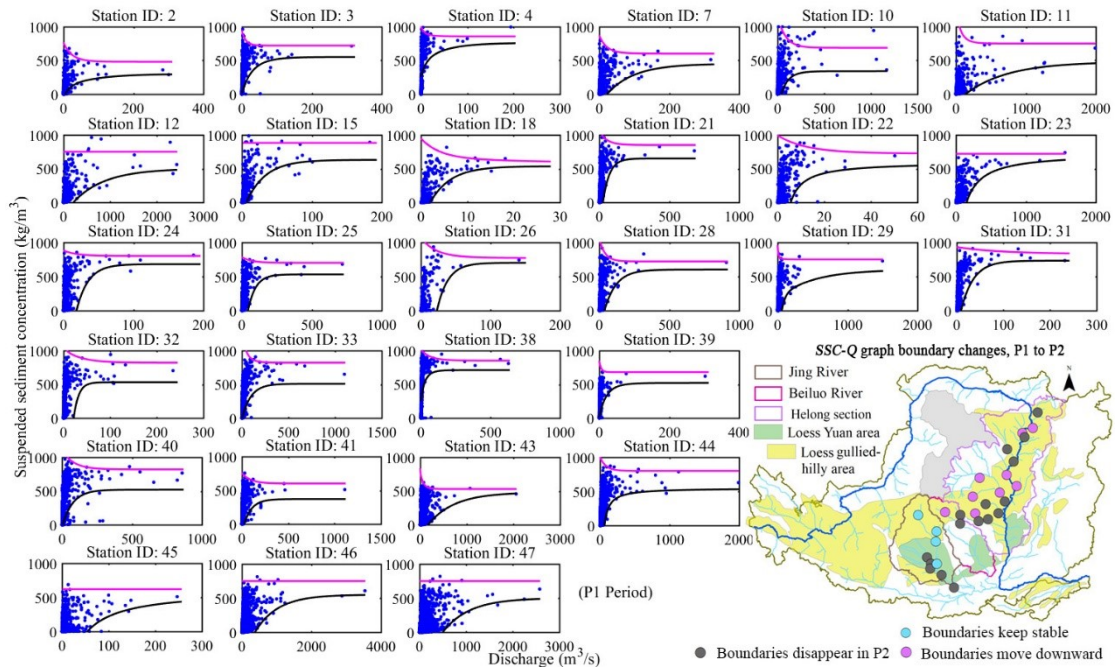


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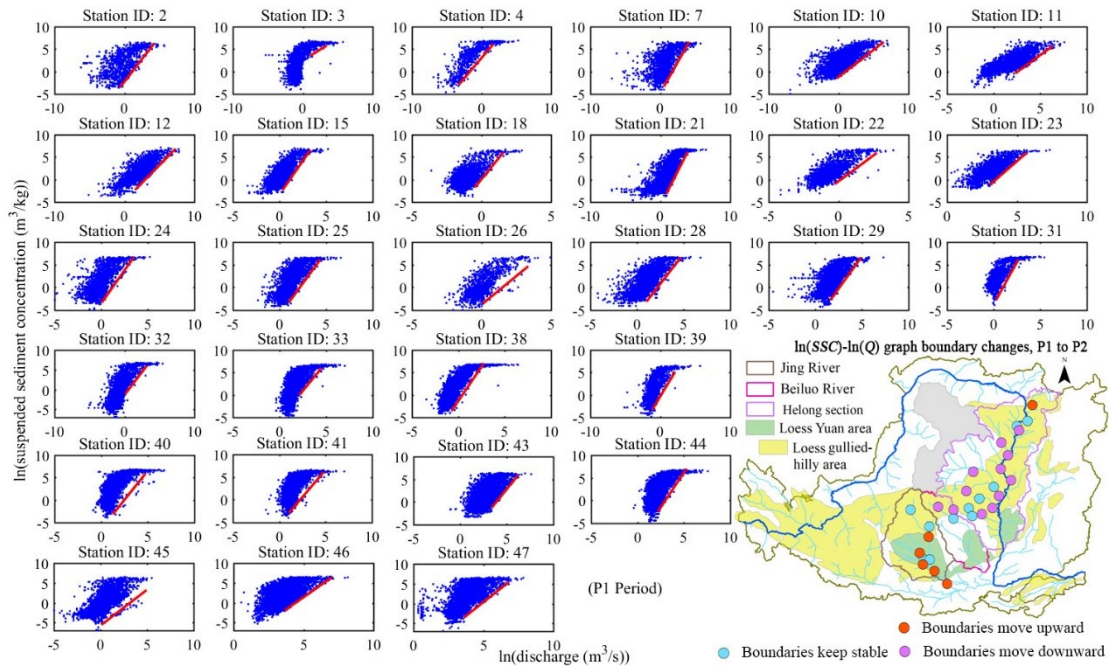
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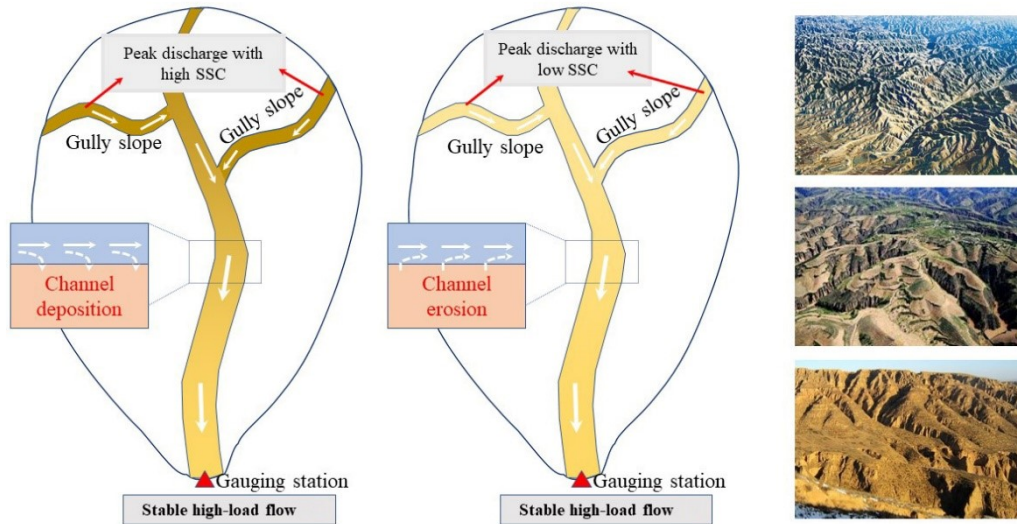
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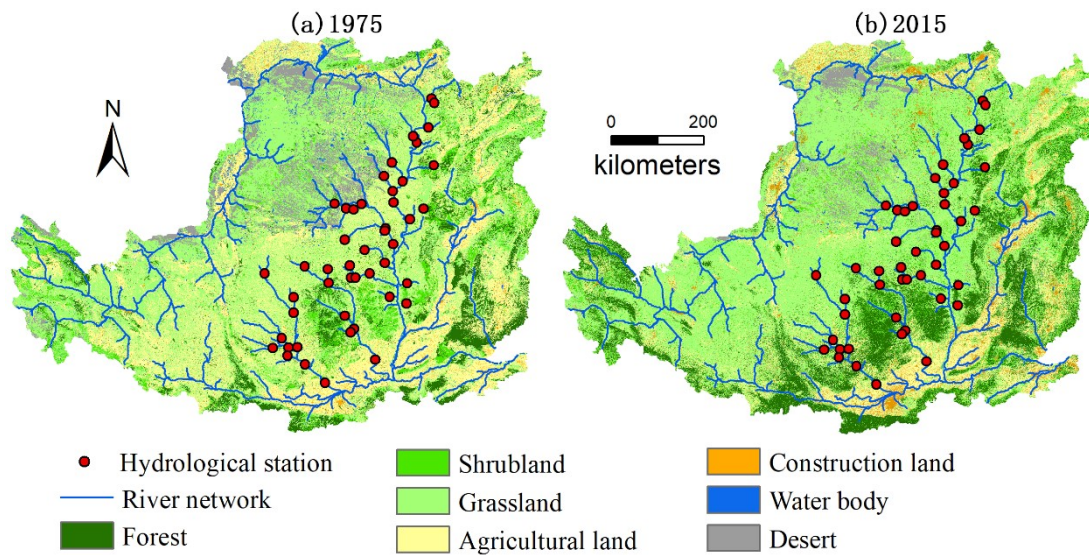
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685 *Supplementary Information for*

686 **Complex relationships between water discharge and sediment**

687 **concentrations across the Loess Plateau, China**

688

689

690 **Contents of this file**

691 **Table S1**

692 **Figs. S1-S8**

693

694 **Introduction**

695 This supplementary information section includes one table and eight figures that

696 support the results discussed in the main text.

Table S1. Locations of hydrological stations in Fig. 1.

Hydrological Station ID	Station Name	Latitude (°N)	Longitude (°E)	Control Area (km ²)	Main Stream/ Subcatchment	Type of Geomorphology
1	Dangyangqiao	39.98	111.62	4,732	Helong section (left side of main stream)	II
2	Qingshuihe	39.90	111.68	541	Helong section (left side of main stream)	I
3	Pianguan	39.43	111.48	1,896	Helong section (left side of main stream)	I
4	Jiuxian	39.16	111.16	1,562	Helong section (left side of main stream)	I
5	Kelan	38.70	111.57	474	Helong section (left side of main stream)	II

6	Gedong	37.88	111.23	749	Helong section (left side of main stream)	II
7	Linjiaping	37.70	110.87	1,873	Helong section (left side of main stream)	I
8	Daning	36.47	110.72	3,992	Helong section (left side of main stream)	II
9	Jixian	36.08	110.67	436	Helong section (left side of main stream)	II
10	Huangfu	39.28	111.08	3,175	Helong section (Huangfu River)	I
11	Shenmu	38.80	110.50	7,298	Helong section (Kuye River)	I
12	Wenjiachuan	38.43	110.75	8,515	Helong section	I

					(Kuye River)	
13	Gaojiapu	38.55	110.28	2,095	Helong section (Tuwei River)	II
14	Gaojiachuan	38.25	110.48	3,253	Helong section (Tuwei River)	II
15	Shenjiawan	38.03	110.48	1,121	Helong section (right side of main stream)	I
16	Hanjiamao	38.07	109.00	2,348	Helong section (Wuding River)	II
17	Hengshan	37.97	109.28	2,415	Helong section (Wuding River)	II
18	Dianshi	37.93	109.47	327	Helong section (Wuding River)	I

19	Zhaoshiyao	38.03	109.67	15,253	Helong section (Wuding River)	II
20	Dingjiagou	37.55	110.25	23,422	Helong section (Wuding River)	II
21	Suide	37.50	110.23	3,893	Helong section (Wuding River)	I
22	Qingyangcha	37.37	109.22	1,260	Helong section (Wuding River)	I
23	Baijiachuan	37.23	110.42	29,662	Helong section (Wuding River)	I
24	Zichang	37.15	109.70	913	Helong section (Qingjian River)	I
25	Yanchuan	36.88	110.18	3,468	Helong section	I

					(Qingjian River)	
26	Ansai	36.87	109.32	1,334	Helong section (Yan River)	I
27	Zaoyuan	36.63	109.33	719	Helong section (Yan River)	II
28	Yanan	36.63	109.45	3,208	Helong section (Yan River)	I
29	Ganguyi	36.70	109.80	5,891	Helong section (Yan River)	I
30	Xinshihe	36.23	110.27	1,662	Helong section (right side of main stream)	II
31	Wuqi	36.88	108.20	3,408	Beiluo River	I
32	Zhidan	36.82	108.77	774	Beiluo River	I

33	Liujiahe	36.55	108.77	7,325	Beiluo River	I
34	Zhangcunyi	35.90	109.13	4,715	Beiluo River	II
35	Jiaokouhe	35.65	109.35	17,180	Beiluo River	II
36	Huangling	35.58	109.27	2,266	Beiluo River	II
37	Zhuangtou	35.03	109.83	25,645	Beiluo River	II
38	Hongde	36.77	107.20	4,640	Jing River	I
39	Yuele	36.30	107.90	528	Jing River	I
40	Qingyang	36.00	107.88	10,603	Jing River	I
41	Maojiahe	35.52	107.58	7,189	Jing River	I
42	Jingchuan	35.33	107.35	3,145	Jing River	II
43	Yangjiaping	35.33	107.73	14,124	Jing River	I
44	Yuluoping	35.33	107.95	19,019	Jing River	I
45	Zhanghe	35.18	107.72	1,506	Jing River	I

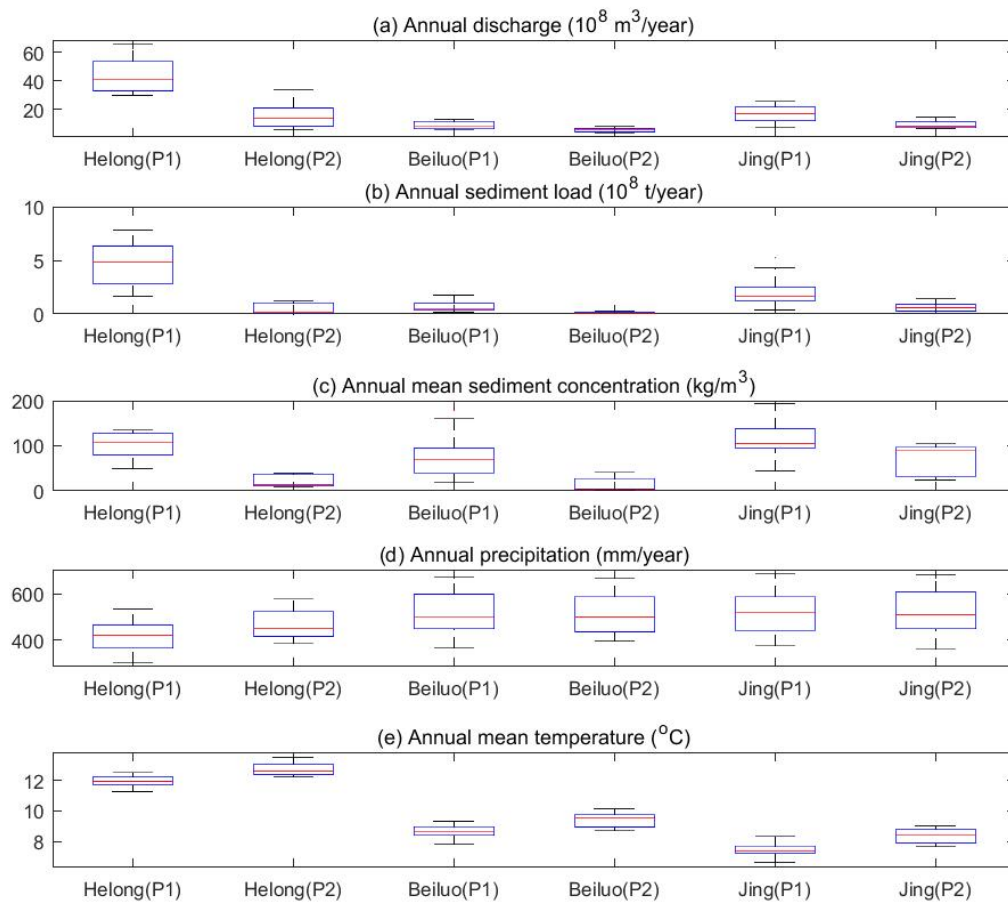
46	Jingcun	35.00	108.13	40,281	Jing River	I
47	Zhangjiashan	34.63	108.60	43,216	Jing River	I

698 Note: Stations marked as Type I in the last column (29 stations) represent watersheds where most of the area (> 80%) is covered by the loess gully
699 landscape; the exception is Baijiachuan station, where about half of the region is characterized by the loess gully landscape. Stations marked as
700 Type II (18 stations) represent watersheds with complex, heterogeneous landscapes (the control areas include a combination of the loess gully
701 landscape, desert, rocky mountain, etc.).

702 Table S2 Number of years in each station dataset for 47 stations along the Yellow River during P1 and P2

ID	P1	P2	ID	P1	P2	ID	P1	P2	ID	P1	P2	ID	P1	P2	ID	P1	P2
1	10	9	9	17	9	17	17	9	25	16	9	33	17	9	41	17	9
2	11	8	10	17	9	18	17	9	26	7	9	34	17	9	42	17	9
3	17	9	11	17	9	19	17	8	27	17	9	35	16	9	43	17	9
4	11	9	12	16	9	20	17	9	28	17	9	36	16	9	44	17	9
5	16	9	13	17	9	21	17	9	29	17	9	37	17	9	45	16	9
6	16	9	14	16	9	22	16	9	30	17	9	38	17	9	46	17	9
7	16	9	15	16	9	23	13	9	31	8	9	39	16	9	47	17	9
8	17	9	16	17	9	24	17	9	32	17	9	40	17	9			

703 The acronym ID corresponds to the hydrological station ID in Table S1.

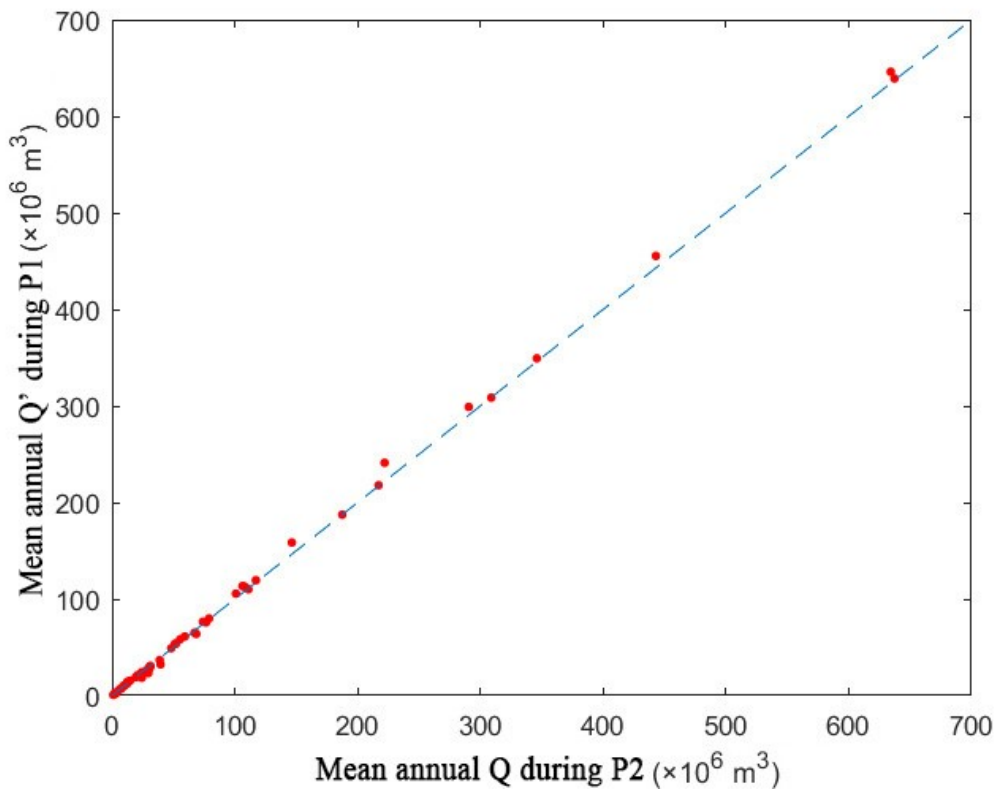


704

705 Fig. S1 Boxplots showing (a) discharge (Q), (b) sediment load (SSL), (c) annual mean
 706 sediment concentration (SSC), (d) annual precipitation (P), and (e) annual mean
 707 temperature (T) for the Helong section, Beiluo River, and Jing River during the P1 and
 708 P2 periods. The box plot is constructed from the minimum value, the first quartile, the
 709 median, the third quartile, and the maximum value. The P and T datasets are obtained
 710 from <http://data.cma.cn>. Note that the values of Q , SSL , and SSC for the Helong section
 711 are obtained as the difference between values at Longmen and Toudaoguai stations
 712 (both on the main stream of the Yellow River).

713 **Uncertainties of the PDF-matching method**

714 Step 1: Transformation of the PDF curves for Q during the P1 period to match the
715 PDF curves obtained during P2, in order for the matched PDF for Q in P1 (Q') to be
716 almost the same as the PDF for Q in P2. To check the effect of matching the PDF, we
717 compare the mean annual Q' during P1 with mean annual Q during P2. Fig. S2 shows
718 that the simulations are satisfactory at all the stations considered.



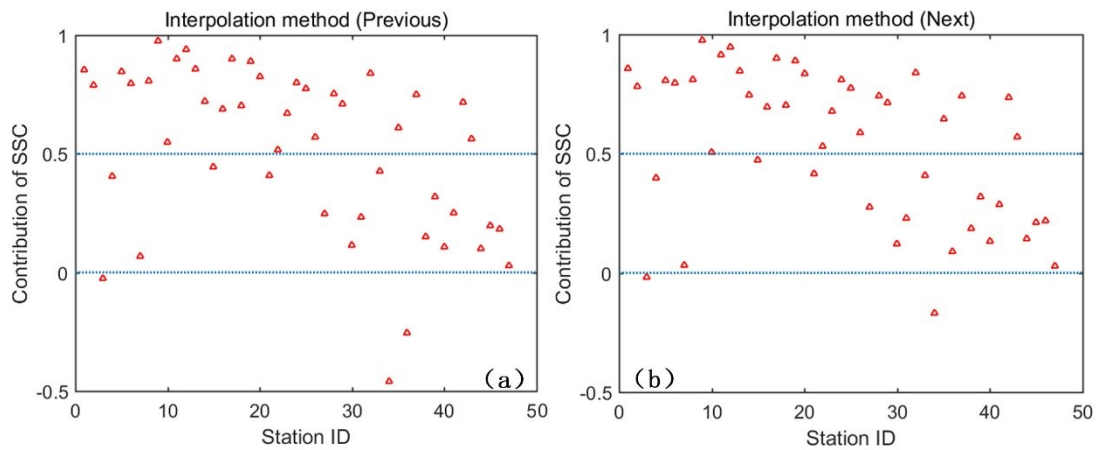
719

720 Fig. S2 Checking uncertainty in matching the PDF of Q to that of Q' .

721 Step 2: Calculation of the matched value of SSC for each interval (step length set
722 to 3) of the observed Q in P1. For the few intervals without observed points, we use
723 two interpolation procedures: 'Previous', where a null value is set equal to the value of
724 a preceding interval; and 'Next' where a null value is set equal to the value of the next
725 interval. Fig. S3 presents the results provided by these two methods, and it indicates

726 that there are hardly any differences evident for most stations, except at two stations
727 where the data are particularly uneven.

728 In short, the results display close correlation between the amount of data and the
729 uniformity of data distribution, with the ‘Next’ method better at handling very uneven
730 data. We therefore selected the ‘Next’ interpolation method.



731
732 Fig. S3 Contribution of *SSC* to changes in *SSL* obtained using (a) “Previous” and (b)
733 “Next” methods to fill null values.

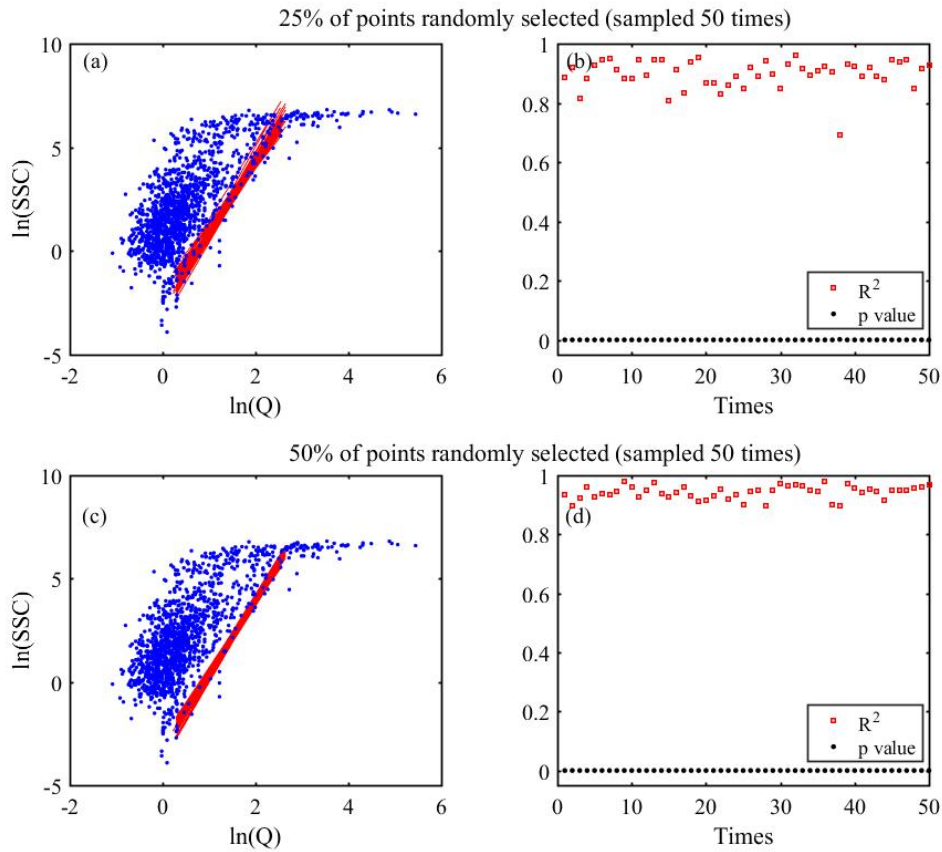
734
735

736 **Uncertainty analysis of ‘Boundary Estimation with Interval Extremum’ (BEIE)**

737 To check the effect of sample size, we use bootstrap sampling (with drop-back
738 sampling) to randomly pick 25, 50 and 75% of the prepared points to fit the boundary.
739 It is clear from Figs S4 and Fig. 2 that sample size has a very important effect on the
740 uncertainty of boundary fitting. It shows a thinner band of boundaries when picking 75%
741 of the sample points than when picking 25% and 50% of the points. In addition, the
742 distribution uniformity of points may also affect the fitting effect. For example, the
743 method is not well suited for the observed $SSC-Q$ distribution because the majority of
744 points are concentrated at small values and there is a huge difference between these
745 points and the few points with large values. We use the method simply to obtain a rough
746 boundary from the minority of points with larger values (Fig. 2a and b). But, as for log-
747 transformed $SSC-Q$, the fitting boundaries are much improved, especially during P1.

748 In conclusion, attaining a higher degree of accuracy depends on having larger
749 sample points and higher uniformity. In this study, the time series of the P2 data is not
750 as long as that of the P1 data, which may lead to poorer boundary fitting in P2 than in
751 P1. In practice, choice of step length (length = 0.2 in this study) has a great impact on
752 the effectiveness of the fit. When the step size has a large value, the boundary can better
753 encompass all data points; and when the step size has a small value, the influence of
754 certain outliers can be eliminated.

755

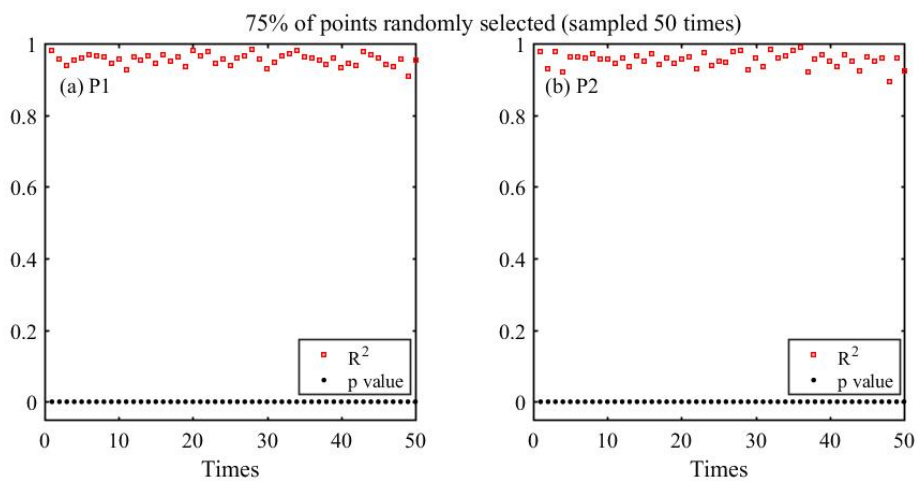


756

757 Fig. S4 The boundary fit obtained by randomly picking (a) 25% and (c) 50% of scatter-

758 plot data points 50 times. Panels (b) and (d) show the R^2 and p values of these fitting

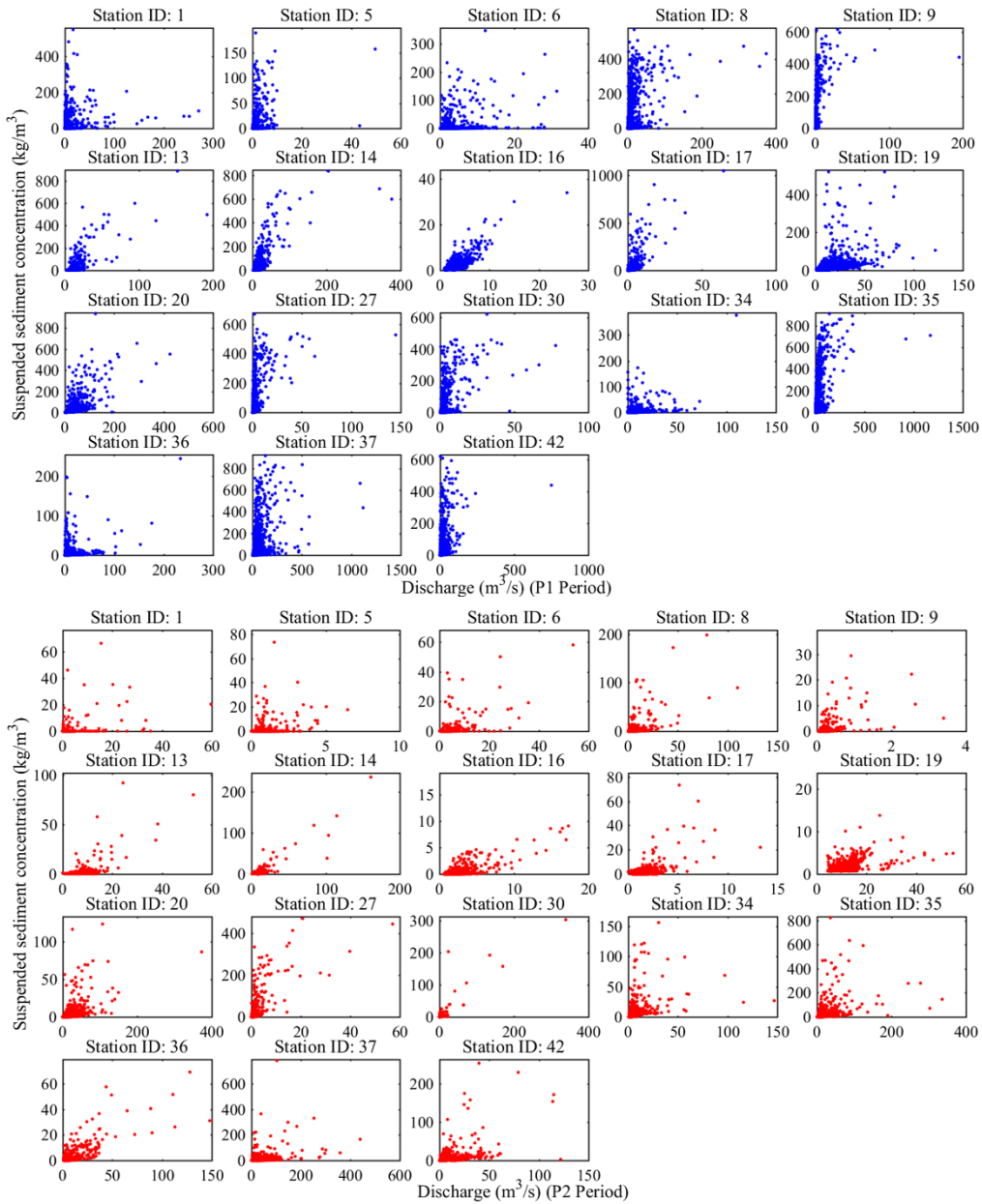
759 boundaries and all p values < 0.01 in the figures.



760

761 Fig. S5 R^2 and p values for line-fitting boundaries when randomly picking 75% of

762 scatter-plot points in (a) P1 and (b) P2.

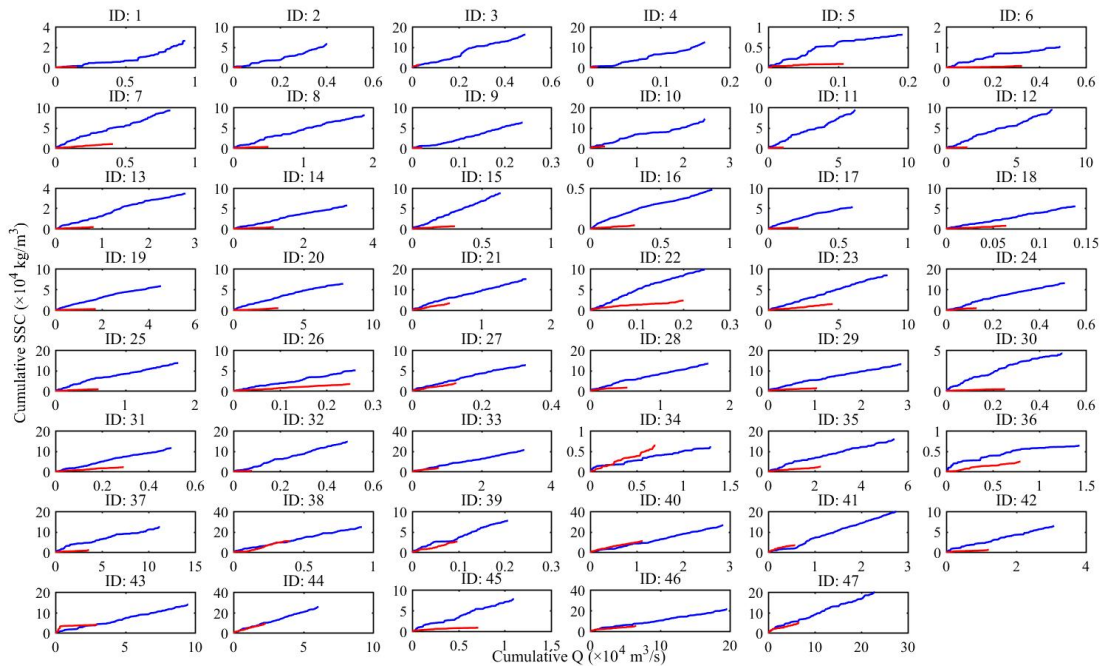


763

764 Fig. S6 SSC– Q distributions for watersheds with complex landscapes during P1 (blue

765 dots) and P2 (red dots) periods.

766



767

768 Fig. S7 Double mass curve relationships between cumulative Q and cumulative SSC

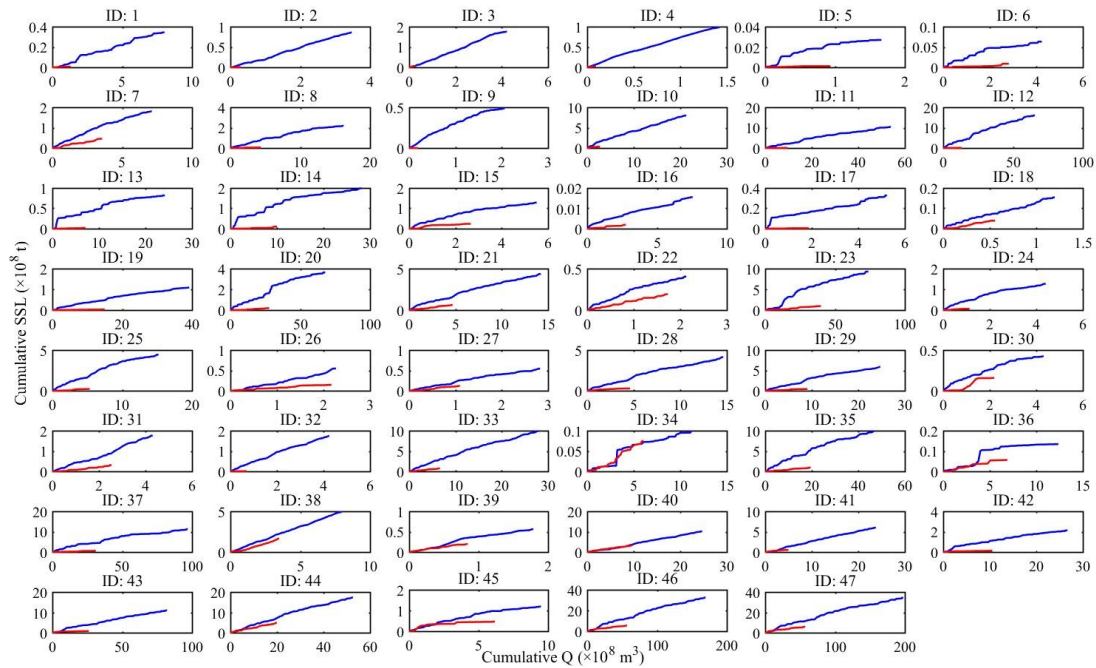
769 for 47 stations along the Yellow River. Blue lines represent the relationship during P1,

770 and red lines represent the relationship during P2. The number of years of available data

771 for P1 and P2 for these stations is presented in table S2 (the observed data have missing

772 values in certain years).

773



775

776 Fig. S8 Double mass curve relationships between cumulative Q and cumulative
 777 sediment load (SSL) for 47 stations along the Yellow River. Blue lines represent the
 778 relationship during P1, and red lines represent the relationship during P2. The number
 779 of years of available data for P1 and P2 for these stations is presented in table S2 (the
 780 observed data have missing values in certain years).