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Kinematics and Kinetics of Capacitated and Non-Capacitated Mouse Sperm

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Washington University in St. Louis

JAMES MCKELVEY SCHOOL OF ENGINEERING

Fall 2021 Independent Study

Independent Study Research: Kinematics and Kinetics of Capacitated and Non-Capacitated Mouse
Sperm

Lab Instructor: Dr. Philip Bayly

Experiment Date: Fall 2021

Report Submission Date: Tuesday, December 21, 2021

I hereby certify that the lab report herein is my original academic work, completed in accordance with the McKelvey School of Engineering and Undergraduate Student academic integrity policies, and submitted to fulfill the requirements of this assignment:

Alicia Gupte

ABSTRACT: *The differences in kinetic measurements of force, work, power, and torque are quantitatively observed between non-capacitated and capacitated sperm. Isomap, a nonlinear dimensionality reduction technique, is used to get higher resolution imaging data of the sperm videos. This allowed accurate calculations of spatial and temporal derivatives to calculate the kinetics of the flagella. The results showed no statistical significance between the kinetic measurements of non-capacitated and capacitated mouse sperm.*

1 INTRODUCTION

Infertility affects approximately 8-12% of couples worldwide, 50% of which are caused by male infertility [1]. Male infertility is usually a result of deficiencies in semen; one of the most common deficiencies being poor sperm motility. Sperm motility describes the ability of the sperm to move through the female reproductive tract to reach and fertilize an egg. Sperm motility directly depends on the function of its flagellum; therefore, it is important to look at the mechanics of the flagellum.

1.1 Sperm Flagella Mechanics. The flagellum is a long appendage of the sperm cell that moves in a whiplike motion to propel the cell forward. Just as living cells are continuously exposed to forces from their environment and must develop specific mechanisms to accommodate these forces, sperm cells have developed a specific motion where their flagellum moves in an oscillation. Although it is uncertain how the cell modulates these oscillations, it has been observed that eukaryotic flagella exhibit a planar sinusoidal wave motion that propagates from the base to the tip of the cell [2]. The waveform can be estimated as Eq. 1 below,

$$y(s, t) = A \sin(ks - wt - \phi) \quad (1)$$

where A is the amplitude [μm], k is the spatial frequency [$\text{rad}/\mu\text{m}$], w is the temporal frequency [rad/s], t is time [s], and is ϕ the phase shift [rad]. This wave equation gives the position of y as a function of space and time (s and t).

1.2 Sperm Flagella Kinetics. At each moment in time, a flagellum's direction of motion can be described by normal and tangential vectors, which can be rotated to reference a cartesian coordinate system. Figure 1 below shows a flagellum's free body diagram along with its normal and tangential

components in relation to the cartesian coordinate system by an arbitrary angle θ [3].

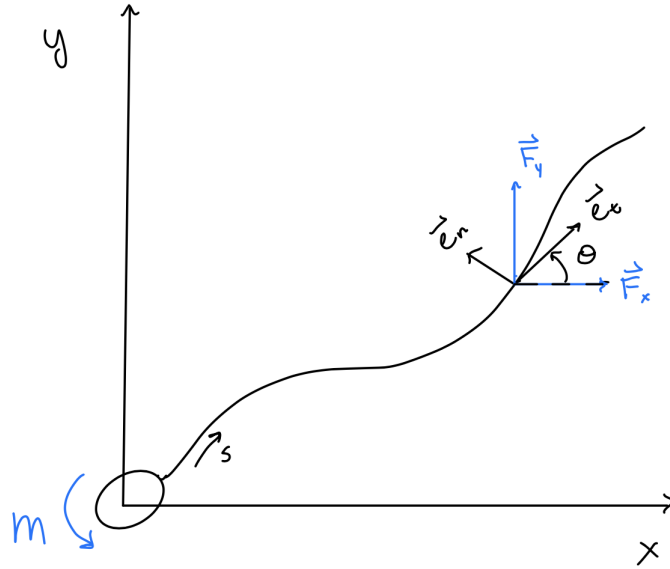


Figure 1 Free body diagram and normal and tangential components of flagellum

The cartesian coordinates of a flagellum can be found using Eq. 2 and Eq. 3.

$$x(s, t) = \int_0^s \cos(\theta)(s, t) ds \quad (2)$$

$$y(s, t) = \int_0^s \sin(\theta)(s, t) ds \quad (3)$$

where s is the length along the flagellum [μm], and t is time [s].

The forces in the normal and tangential directions can be found using resistive force theory [3]. As the sperm migrates through the female reproductive tract it experiences resistive forces due to the fluid's viscosity. Discovered by Gray and Hancock, resistive force theory neglects long-range hydrodynamic interactions and focuses on anisotropic local hydrodynamic friction between the sperm surface and the adjacent fluid [4]. Using resistive force theory, where frictional forces dominate inertial forces, the forces along the flagellum can be found using Eq. 4 and Eq.5.

$$F_n = -c_n * v_n \quad (4)$$

$$F_t = -c_t * v_t \quad (5)$$

where v_n and v_t are the velocity components in the normal and tangential direction, and c_n and c_t are the resistive friction coefficients in the normal and tangential directions. In this paper, the values of c_n and c_t are $3.4 \cdot 10^{-3}$ and $1.7 \cdot 10^{-3}$ [5]. These normal and tangential forces can be used to calculate the forces in the cartesian coordinate system as shown in Eq. 6 and Eq. 7.

$$F_x = F_n * -\sin(\theta) + F_t * \cos(\theta) \quad (6)$$

$$F_y = F_n * \cos(\theta) + F_t * \sin(\theta) \quad (7)$$

Using these forces, additional kinetic measurements such as the work, power, and torque exerted by the flagellum can be calculated as shown in Eq. 8, Eq. 9, and Eq. 10.

$$Power = F_n * v_n + F_t * v_t = F_x * v_x + F_y * v_y \quad (8)$$

$$Work = \int (Power) dt \quad (9)$$

$$Torque = F_y * X - F_x * Y \quad (10)$$

1.3 Reconstructing the waveform. In order to get accurate measurements for the kinematics of the flagellum motion, the motion has to be smooth as that of a sinusoidal wave. The imaging of flagellar motion is not always at high enough resolution to take accurate spatial and time derivatives so there is a need to sort the flagellar beat. Sorting the beat will make higher resolution images of the wave form. One way this can be done is by isometric mapping or isomap for short. Isomap is a nonlinear dimensionality reduction method which preserves local structures [6]. Isomap works by taking a data set with high dimensionality and computing the data points geodesic distance to reduce it into a lower dimension. A common example used to explain isomap is the swiss roll shown in Fig.2.

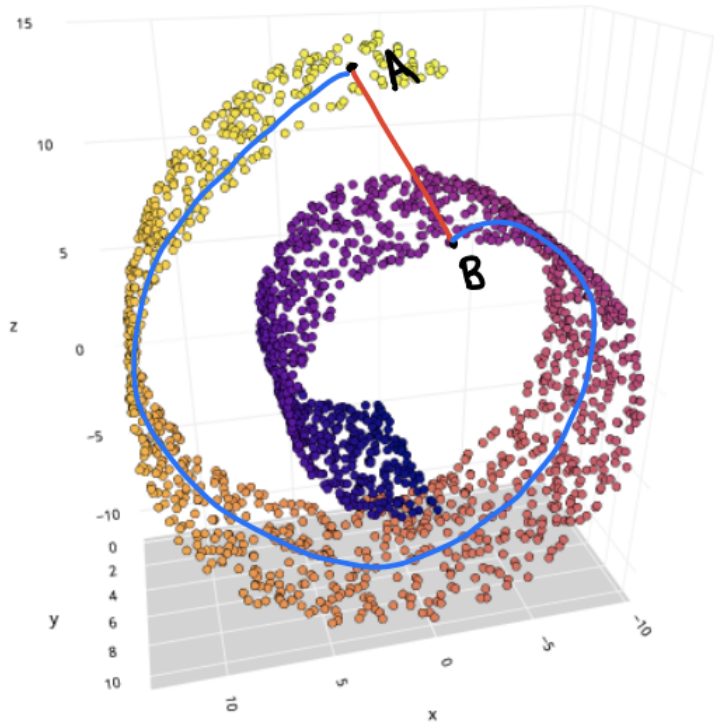


Figure 2 Swiss roll 3D data points [6]

The red line between arbitrary points A and B shows the euclidean distance, commonly used in linear reduction methods, while the blue line shows the geodesic distance. The geodesic distance can be found by specifying parameters of either neighbors, or epsilon. A numeric value for neighbors will connect data points to as many of its neighboring data points as specified by that value. Epsilon will connect data points based on whether its neighboring points fall within an imaginary ball of radius epsilon around that point.

In relation to flagella motion, since flagella are assumed to move in a periodic motion the expected isomap embedding should result in a circle because of the repeating pattern. The values obtained from isomap can be used to sort the flagellar beat such that similar motions are grouped together. This will result in a smoother reconstructed waveform which can be used to calculate time derivatives to get accurate results of kinetic measurements [3].

1.4 Capacitiation. The waveforms of mouse sperm with conditions A and B, non capacitated and capacitated sperm, are analyzed in this paper. Sperm are unable to fertilize an egg immediately after ejaculation and must go through a physiological maturation process known as capacitiation [7].

As the sperm swims through the female reproductive tract, capacitation is triggered by the uterine wall secretions. During this process, the sperm head and flagellum both undergo physical changes. The membranes of the sperm head become more fluid while the flagellum becomes hyperactive. Hyperactivation allows the sperm to generate greater propulsive forces to be able to move through the viscous fluids of the fallopian tubes to fertilize the egg [1].

2 METHODS

2.1 Tracing and Isomap. The flagellar waveform of the mouse sperm was traced using `autotrace_fun3.m`, a MATLAB program created by Professor Louis Woodhams at Washington University in St. Louis. This program recorded qualitative measurements such as the frequency, period, wavelength, curvature, and amplitude as well as the θ values as a function of time and space. The euclidean distance between the θ values was calculated using MATLAB function `L2_Distance.m` created by Roland Bunschoten at University of Amsterdam. The euclidean distance was then used as an input argument in MATLAB program `Isomap.m` created by Josh Tenenbaum at Stanford University. The additional input arguments, k , neighbors, or E , epsilon, were selected by trial and error for each video depending on which gave the most clear isomap embedding result. Once the output from `Isomap.m` was obtained, the waveform was sorted.

2.2 Sorting and reconstructing the waveform. `Isomap.m` outputs a vector each for the x and y coordinates from the isomap transformation. These values were used to calculate the new θ values using trigonometry. Using MATLAB's sort function, the new θ value indices were found. Using the indices, the polynomial coefficients of the waveform (`Out.PP.pArray` from `autotrace_fun3.m`) were sorted. A fast fourier transform (FFT) was taken of the sorted polynomial coefficients in order to get rid of higher harmonics. Next, the inverse FFT was taken to go back to the time domain. Finally, the waveform was reconstructed using the polynomial coefficients and space vector `Out.PP.s2` from `autotrace_fun3.m`.

2.3 Kinetics. The derivatives of the reconstructed wave form with respect to the time step of the reconstructed beat (found from the beat frequency and number of frames) were taken in order to find the velocity components of the flagellum. These values were then used to find the forces, power,

torque, and work produced by the flagellum using Eq. 6 through Eq. 10.

This procedure was repeated for each mouse sperm video for conditions A and B.

3 RESULTS

3.1 Autotrace Results. Autotrace_fun3.m provides the input data to plot the flagellum's trace with respect to time and space. Figure 3 shows the trace for video 3b.

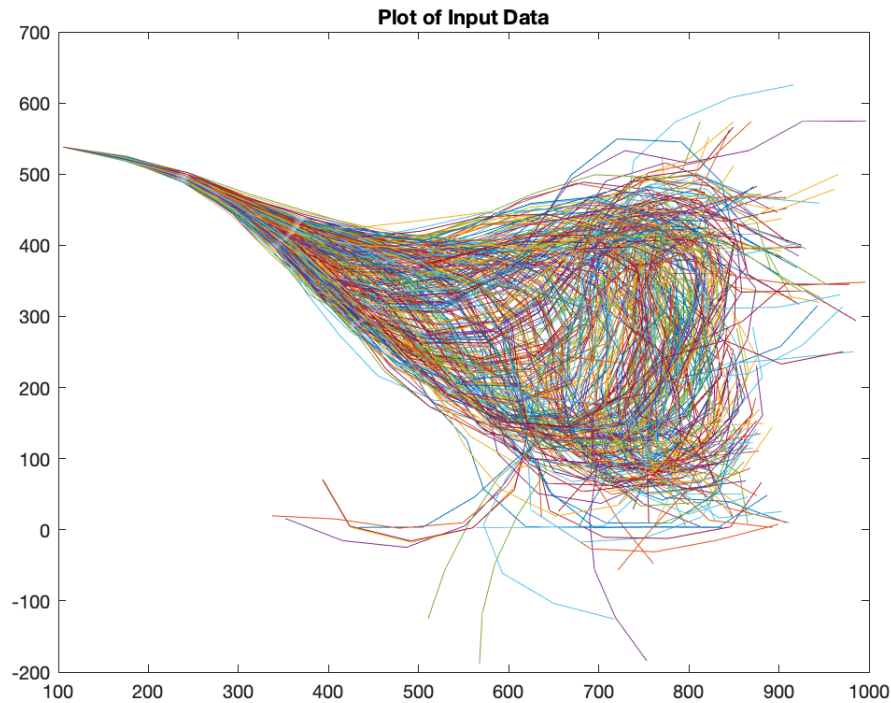


Figure 3 Video 3b trace

3.2 Isomap Results. The output from Isomap.m is a two dimensional isomap embedding shown in Fig 4. Figure 5 is the corresponding residual variance graph, which shows the error of the isomap transformation for each dimension.

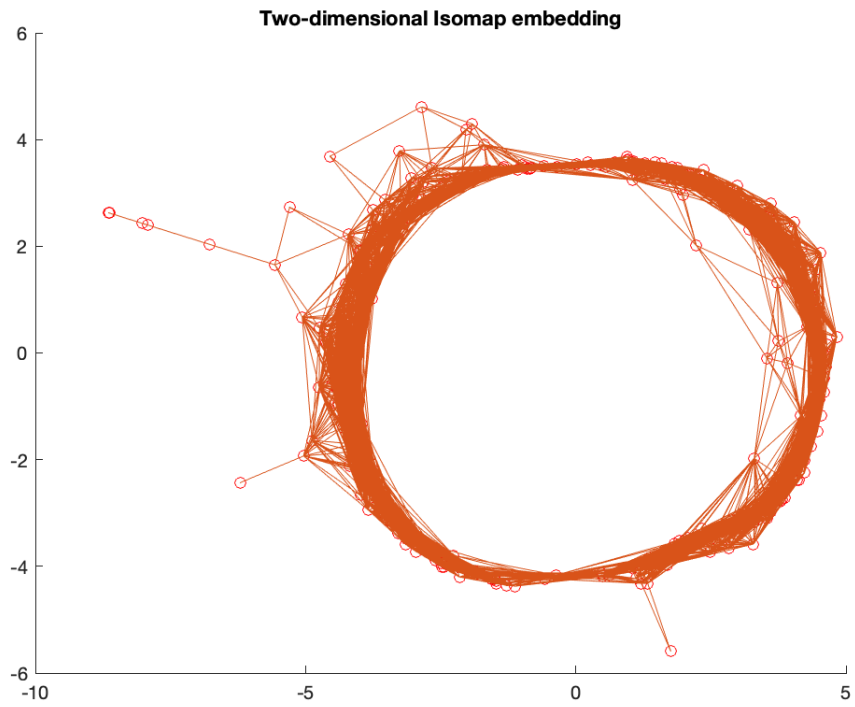


Figure 4 Video 3b isomap embedding

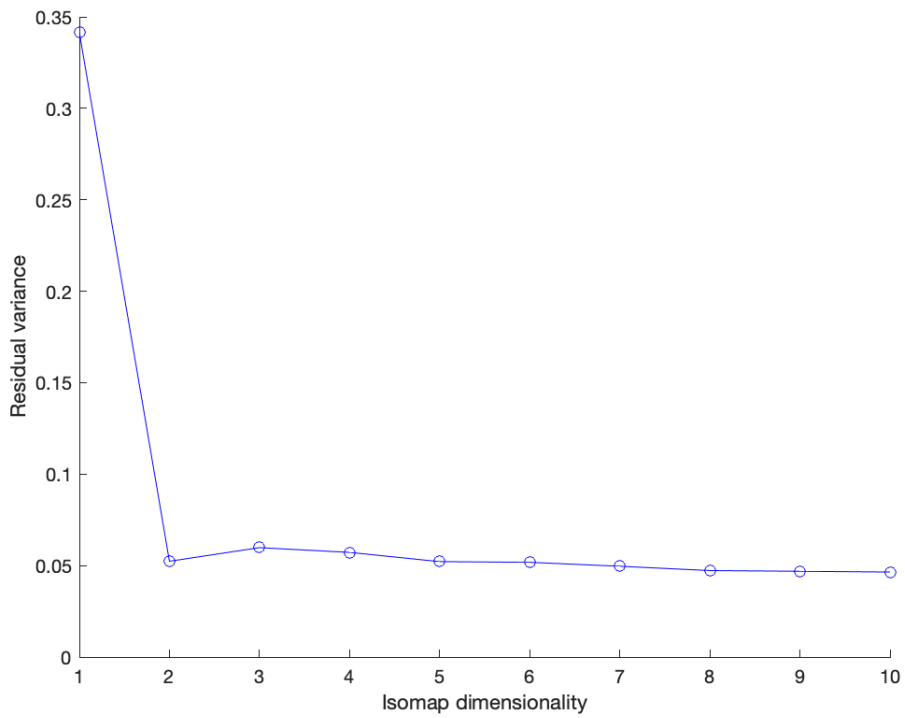


Figure 5 Video 3b residual variance for isomap embedding

3.3 Reconstructed Waveform. Figure 6 shows the process of reconstructing the waveform.

The result is a smooth curve of the waveform.

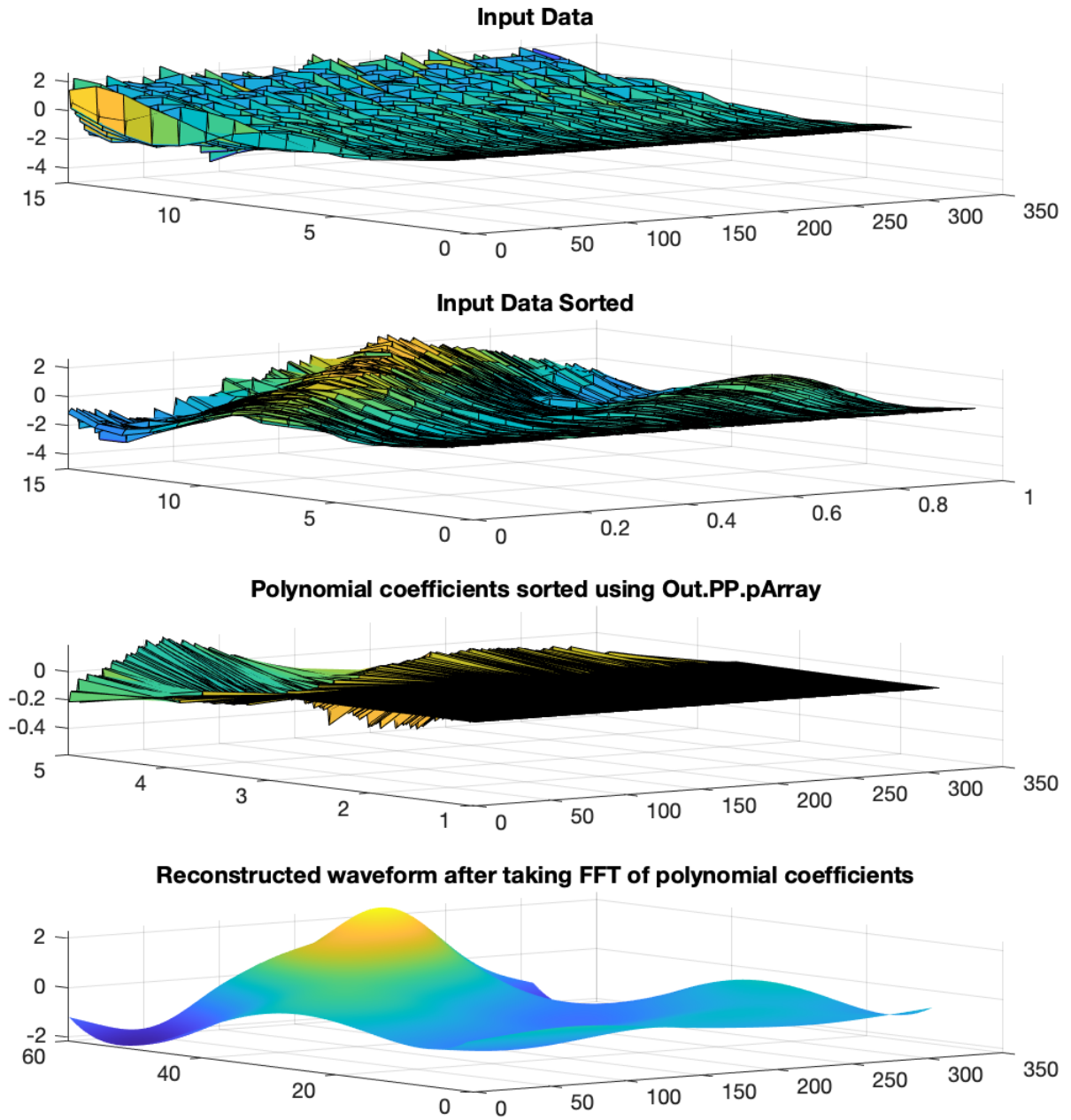


Figure 6 Video 3b smooth reconstructed waveform

3.4 Kinematics. The forces (x and y direction), work, power, and torque are plotted over the time of the flagellum's beat in Fig. 7, 8, 9, 10, and 11.

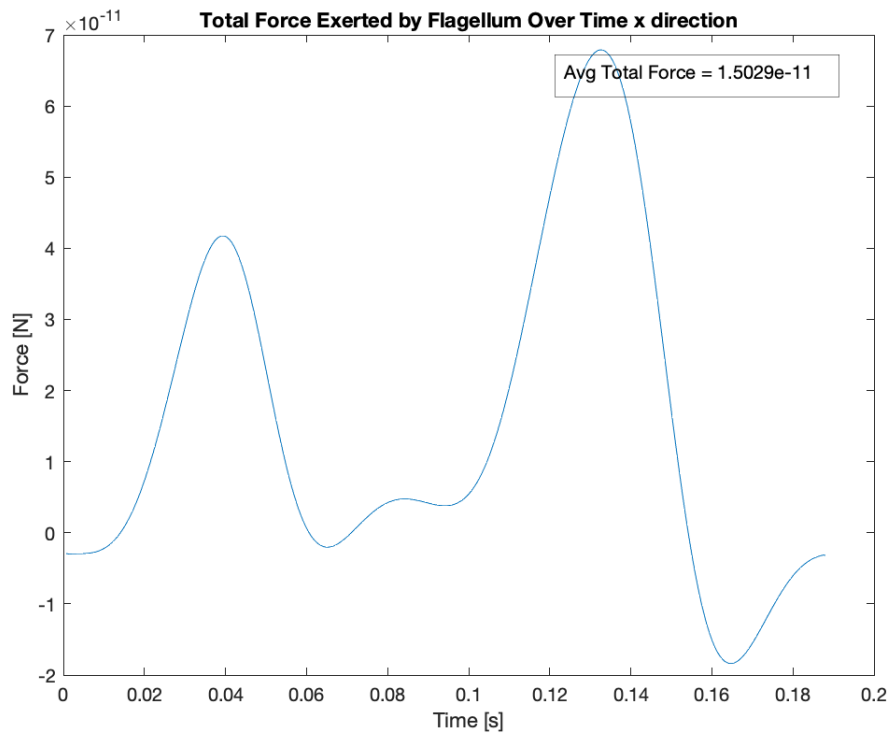


Figure 7 Video 3b force in the x-direction plotted as a function of time

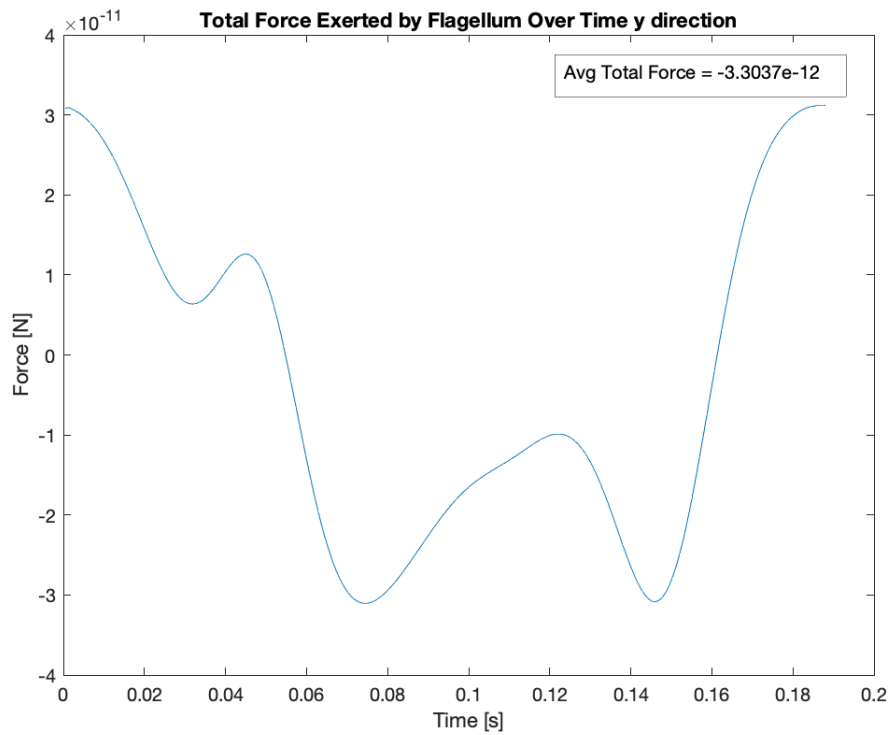


Figure 8 Video 3b force in the y-direction plotted as a function of time

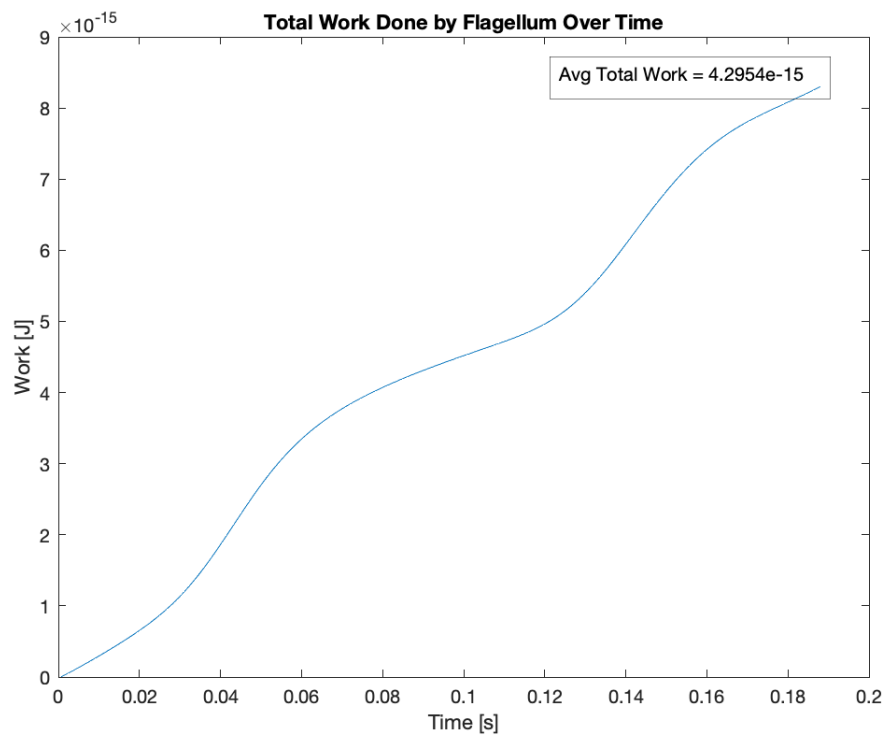


Figure 9 Video 3b work plotted as a function of time

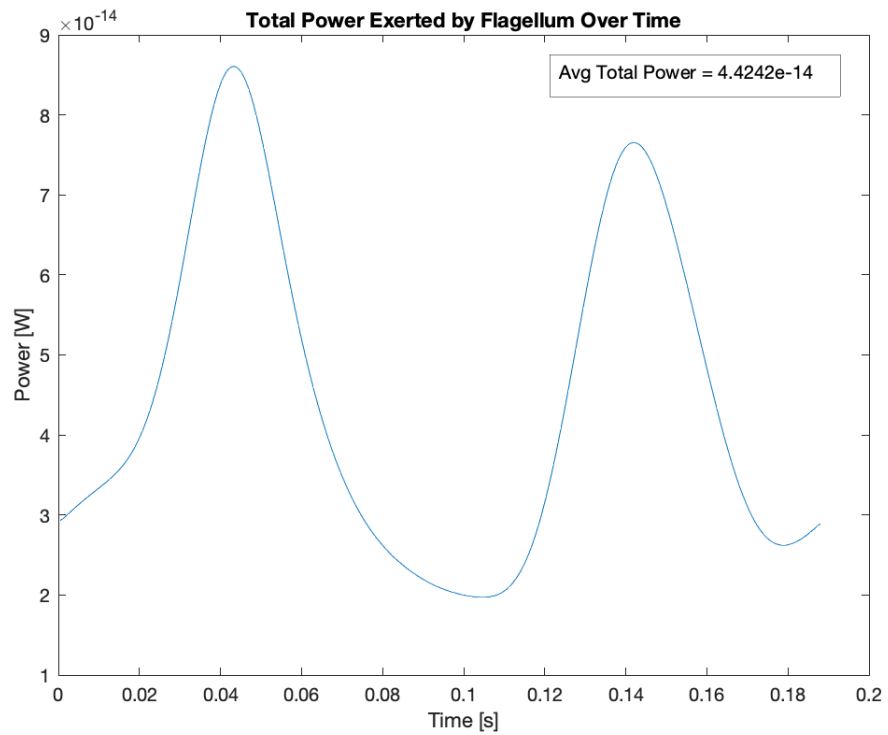


Figure 10 Video 3b power plotted as a function of time

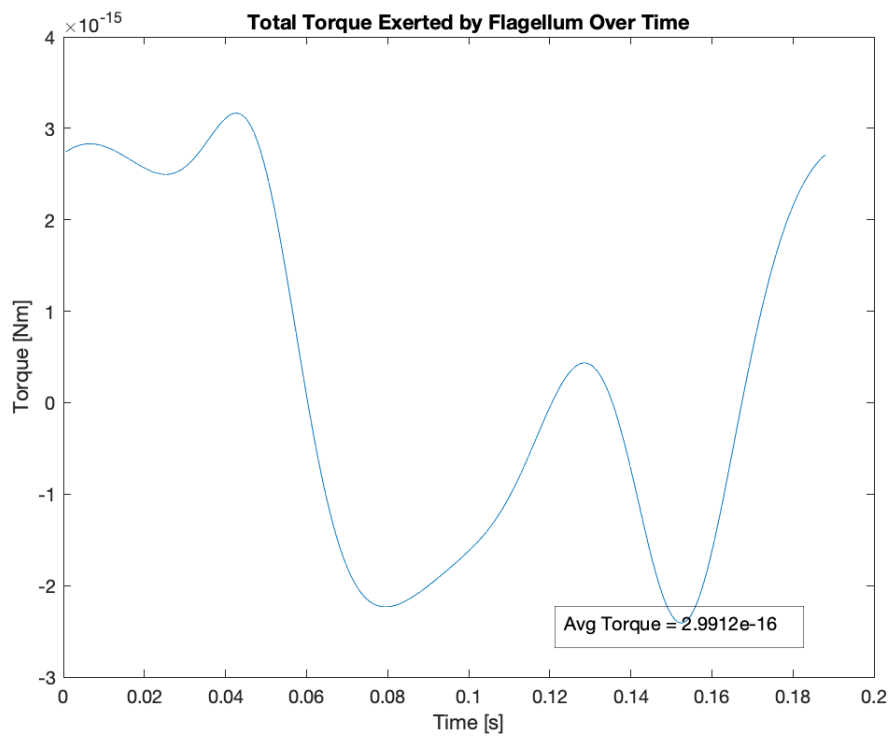


Figure 11 Video 3b torque plotted as a function of time

3.5 Comparing conditions A and B. The kinetic graphs were made for each video, shown in appendix, and a statistical analysis was done comparing the average work, average force magnitude, average power, and average torque between conditions A and B. The results are plotted in Fig. 12.

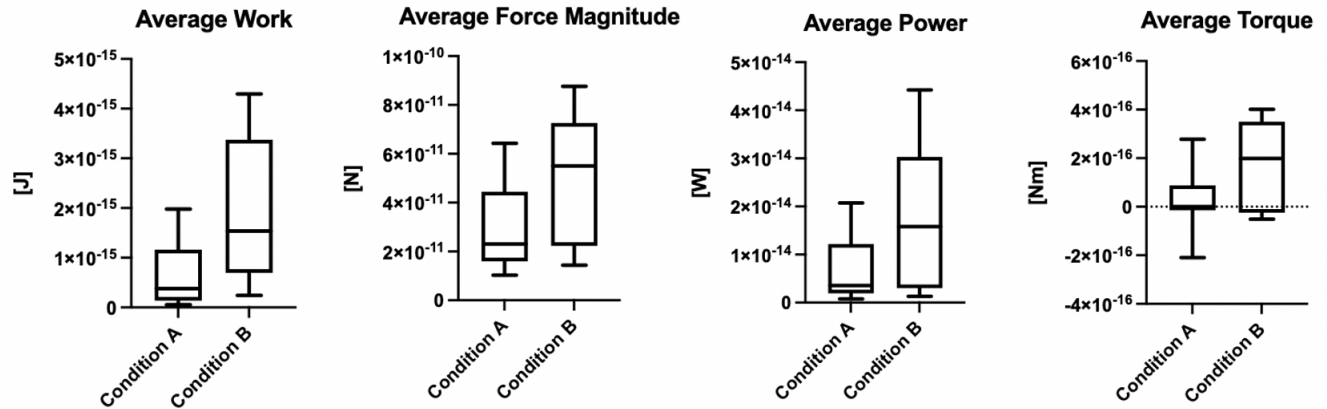


Figure 12 Box plots made for comparing conditions A, non-capacitated sperm, and condition B, capacitated sperm. 8/9 videos worked using Isomap.m for condition A and 5/7 videos worked for condition B.

A two-tailed T-test assuming unequal variances was performed for each of the kinetic measurements and the resulting p values is shown in Table 1.

Table 1 Video 3a Isomap Output data and reconstructed waveform

Output Data	P-value	Statistically Significant? ($P < 0.05$)
Average Work	0.2185	No
Average Force Magnitude	0.2762	No
Average Power	0.1459	No
Average Torque	0.2808	No

DISCUSSION

The circular shape of the isomap embedding in Fig. 4 shows that the motion of the flagella is periodic. Figure 5 shows that the residual variance is low, 0.05, for dimensions 2 and higher

which means the isomap transformation is reliable. In Fig. 6 the input data produces a rough curve and becomes smoother as the data is sorted and even smoother after the FFT is taken. The result is a smooth manifold which gives more accurate time derivatives. Even though the videos taken are of a flagellum with a fixed head, the reconstructed waveform shows slight movement at the head of the flagellum which suggests that there is some rotation at the head. The force for both the x and y directions shown in Fig 7 and 8 are in the range of tens of pico-newtons. This is a similar range to other mammalian sperm compared in papers by Kathleen A. Shmidtz et al. [8], and Wesley W Hsiao et al. [9]. The work, power, and torque are also found to be in the expected range. The plots of Fig. 12 show that condition B does have a higher average work, force, power, and torque than condition A. However, the results show that there is no statistical significance between the two conditions. This is unexpected since capacitated sperm are thought to produce more force in order to be able to penetrate the egg.

CONCLUSION

The motion of flagella can be analyzed from tracing the flagellum, using isomap reduction techniques to reconstruct the wave form, and then taking time derivatives to compute kinetic measurements such as forces, work, power, and torque produced by the flagellum. The analysis on mouse sperm showed there was no statistical significance of the kinetic measurements between non-capacitated and capacitated sperm. This was not expected since capacitation cause the sperm to undergo hyperactivation which is believed to increase the flagellum's propulsive forces. The small sample size of videos traced and analyzed could be a reason for maintaining the null hypothesis that there is no statistical significanc between conditions A and B. Researching the capacitation effects on the motion of flagella are important in understanding sperm motility and its role in male fertility.

References

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A Appendix

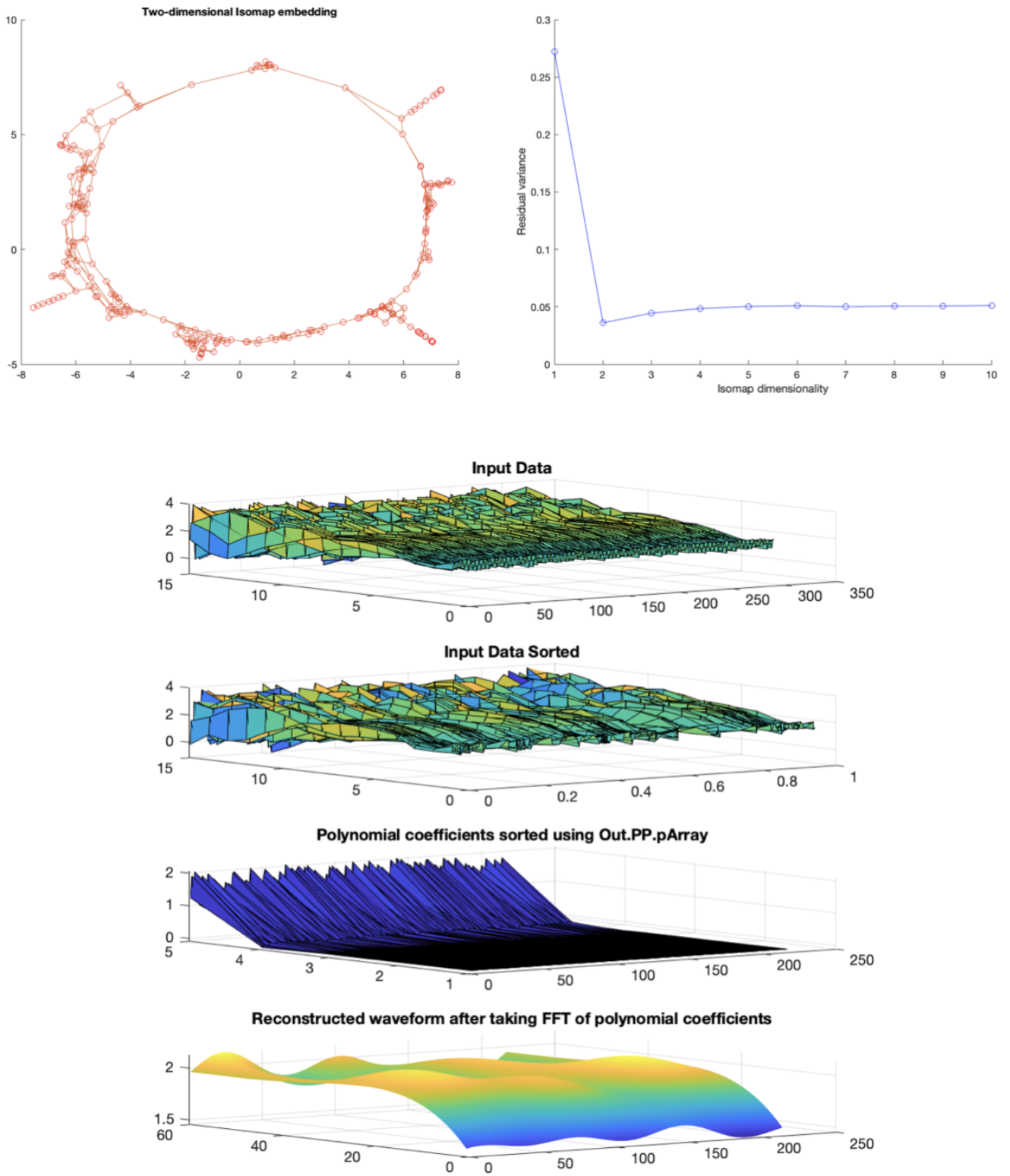


Figure A.1 Video 2a Isomap Output data and reconstructed waveform

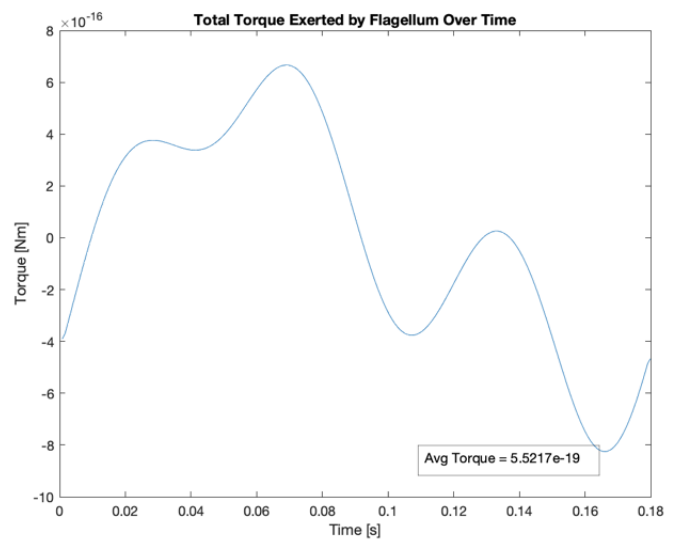
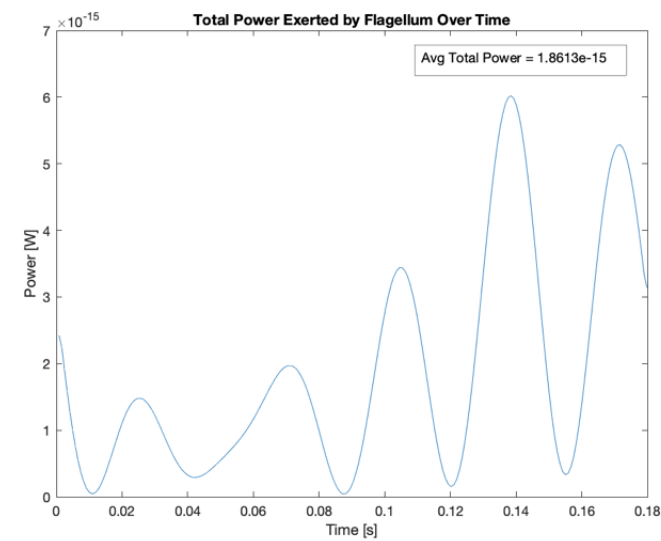
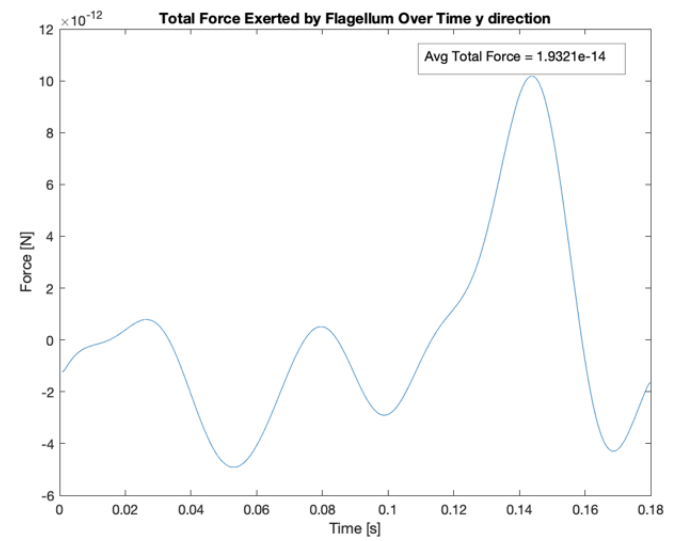
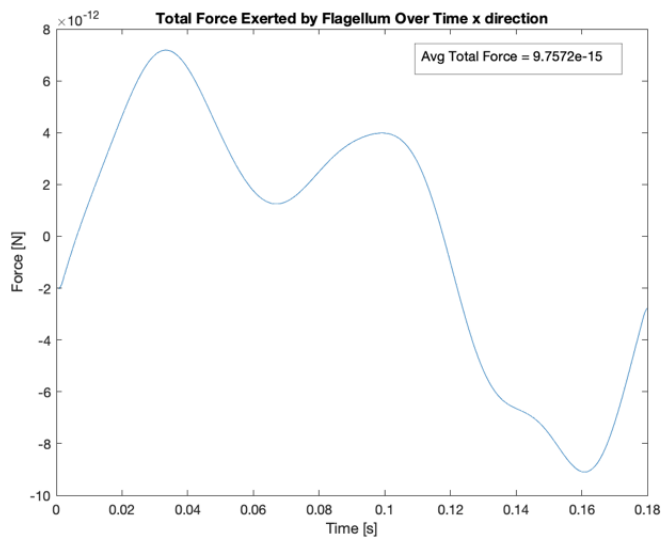
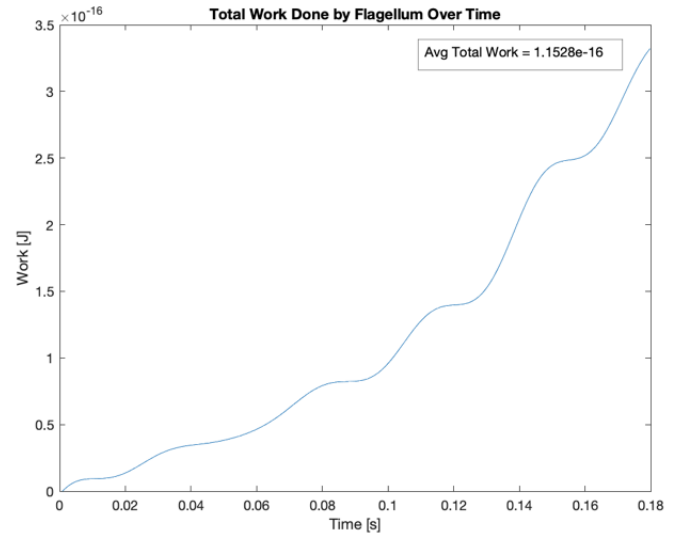
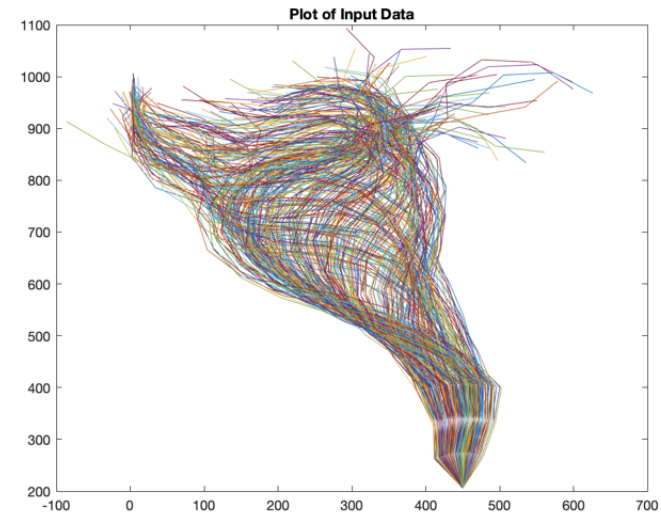


Figure A.2 Video 2a Out put trace and kinematic data graphed

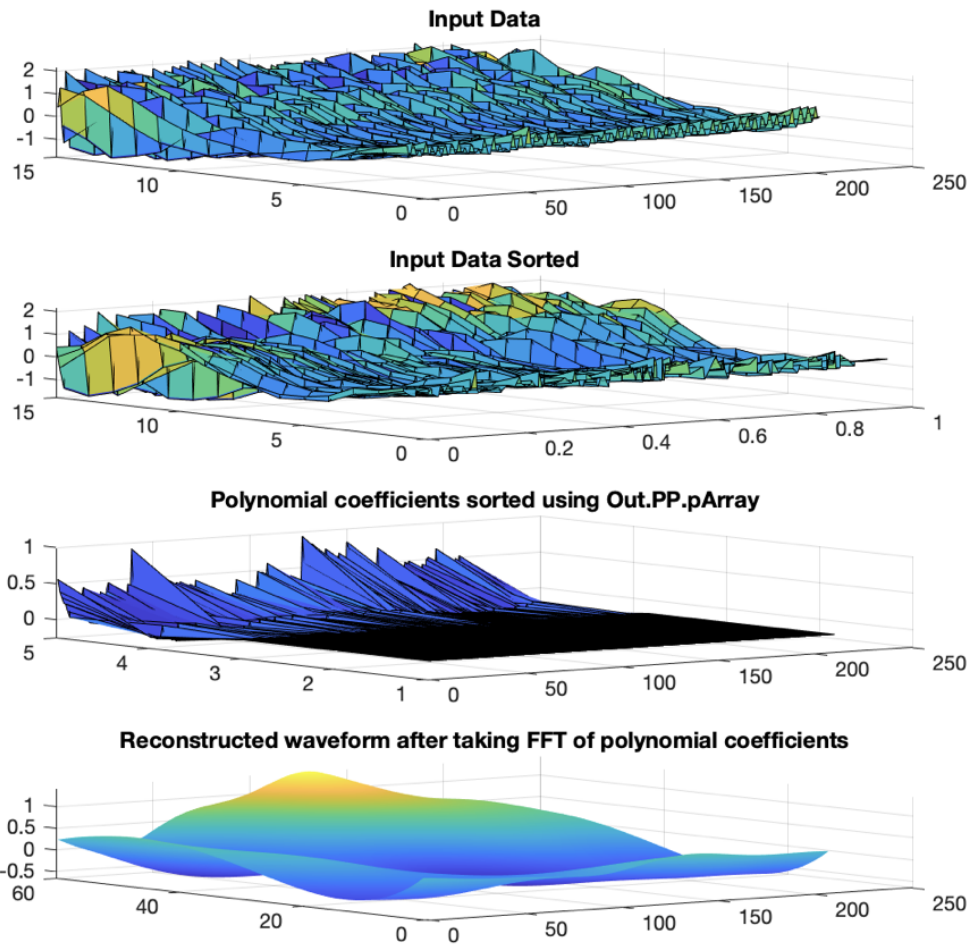
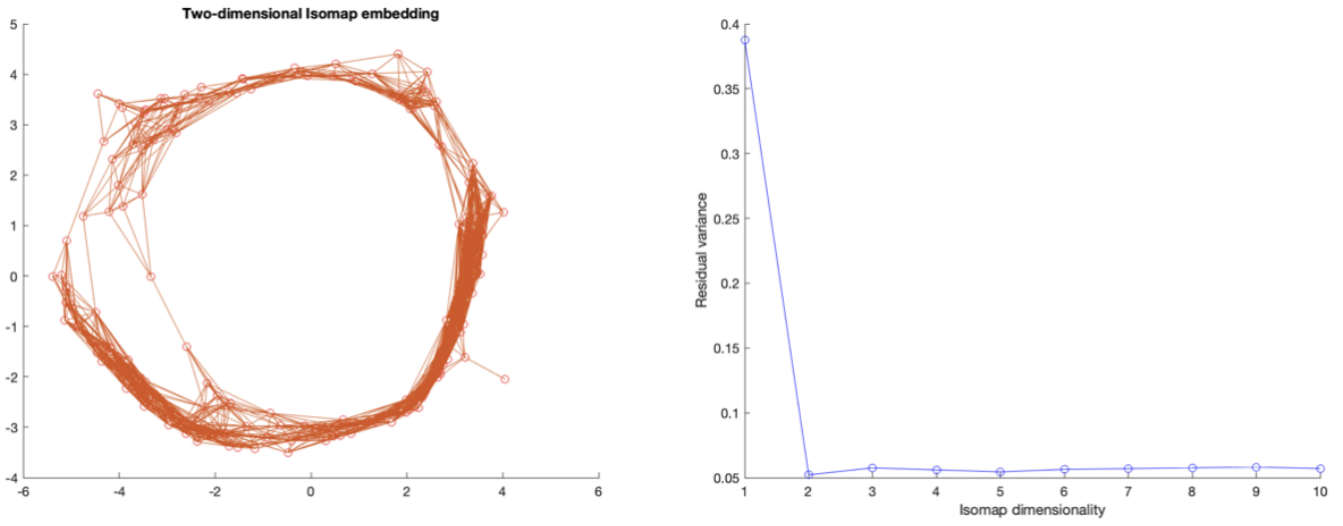


Figure A.3 Video 3a Isomap Output data and reconstructed waveform

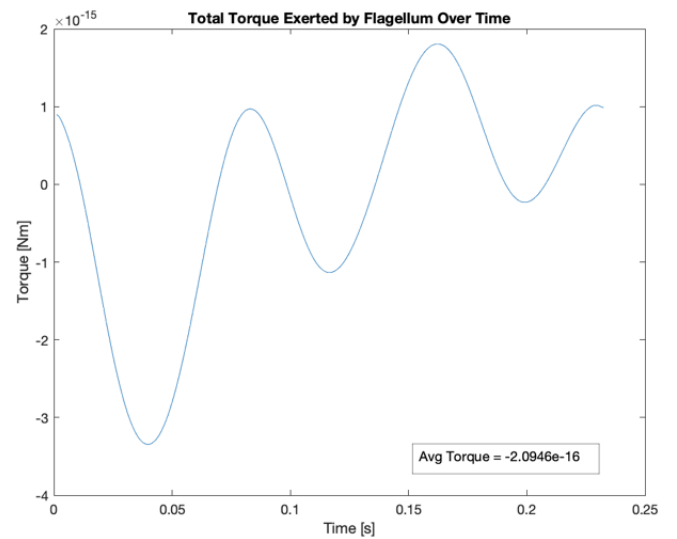
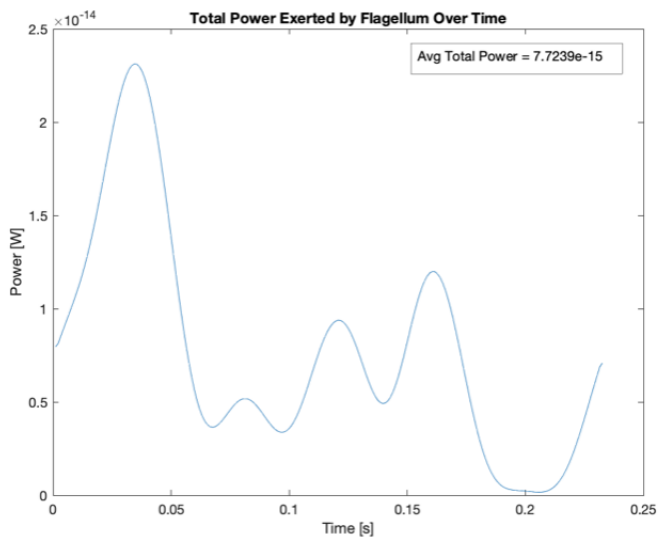
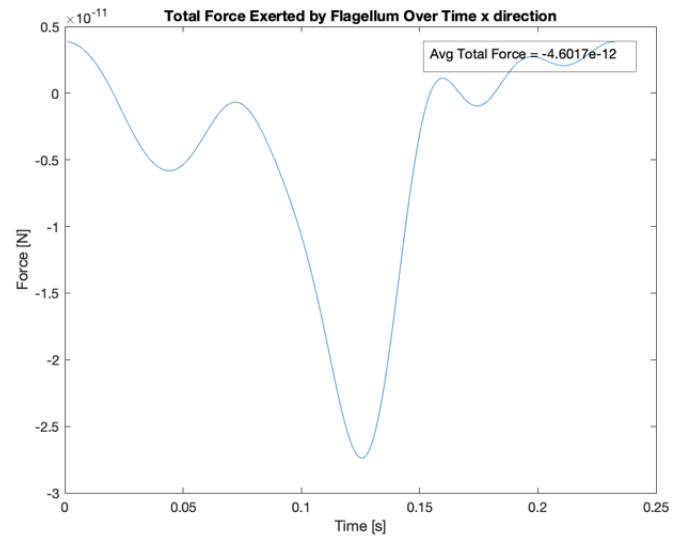
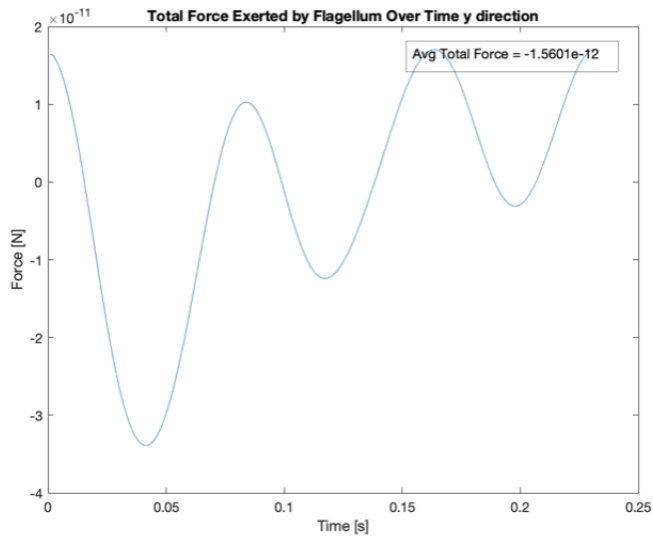
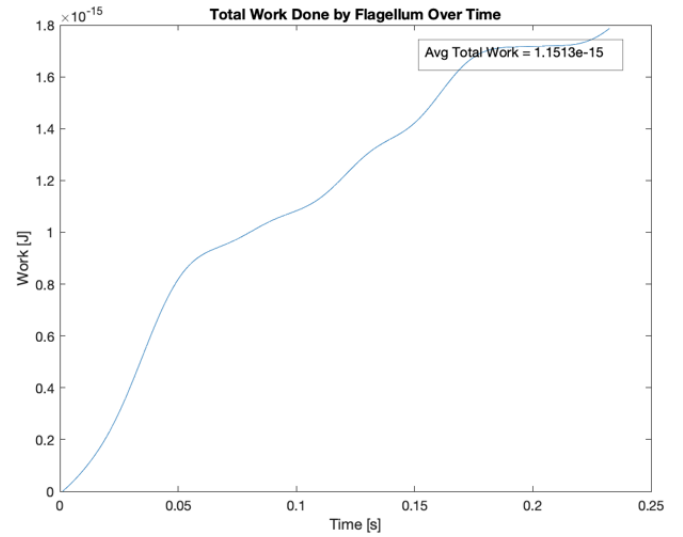
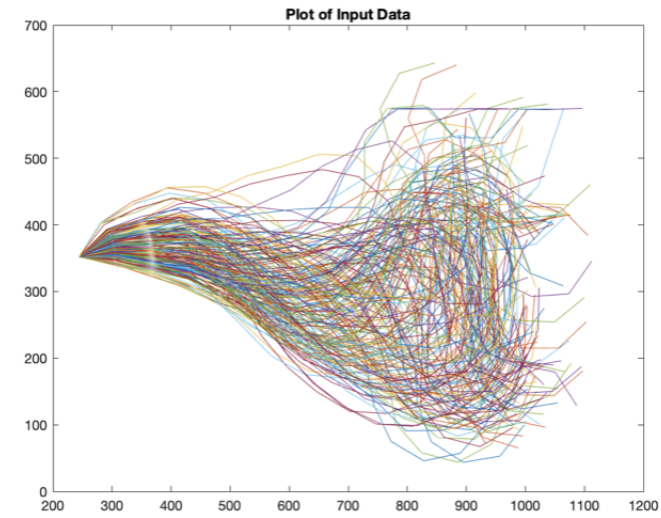


Figure A.4 Sample schematic diagram of test setup.

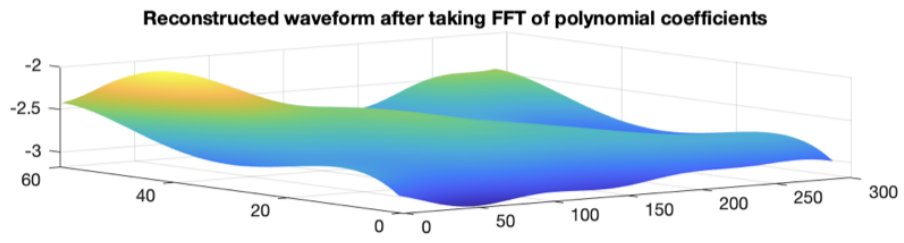
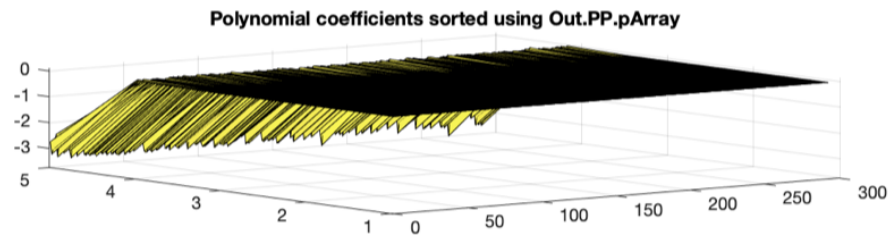
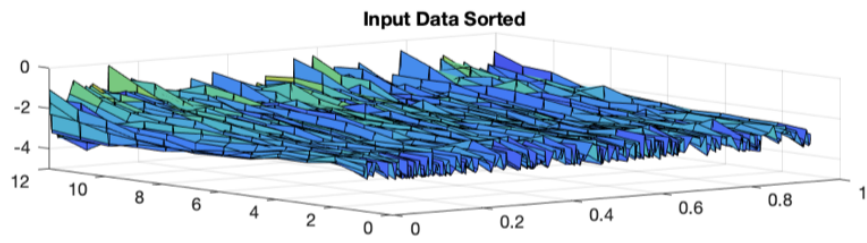
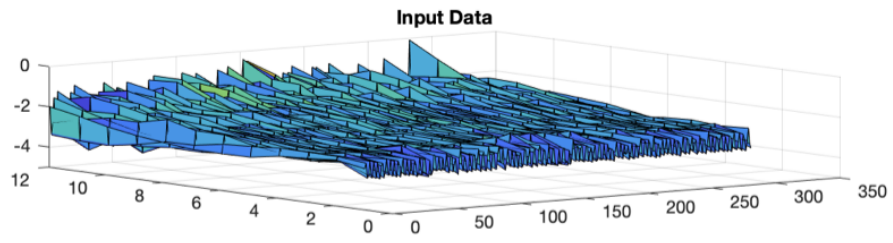
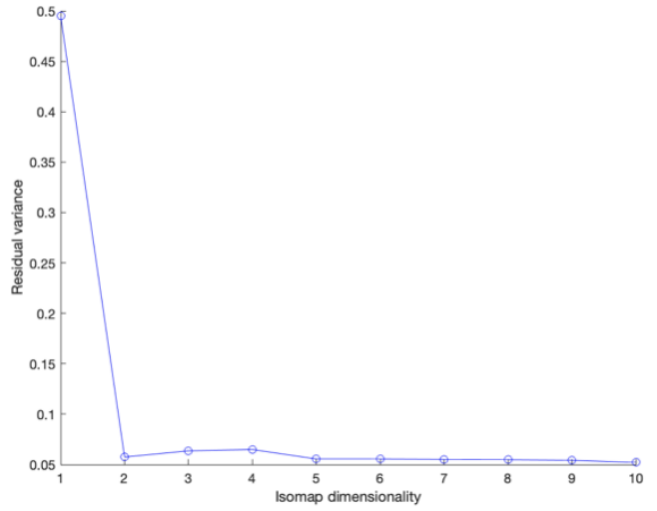
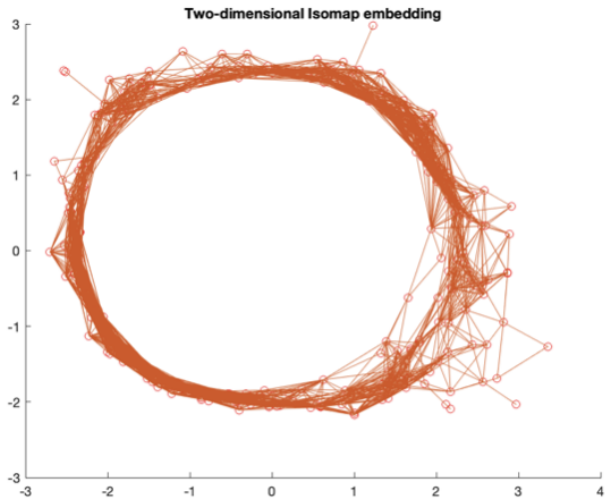


Figure A.5 Video 4a Isomap Output data and reconstructed waveform

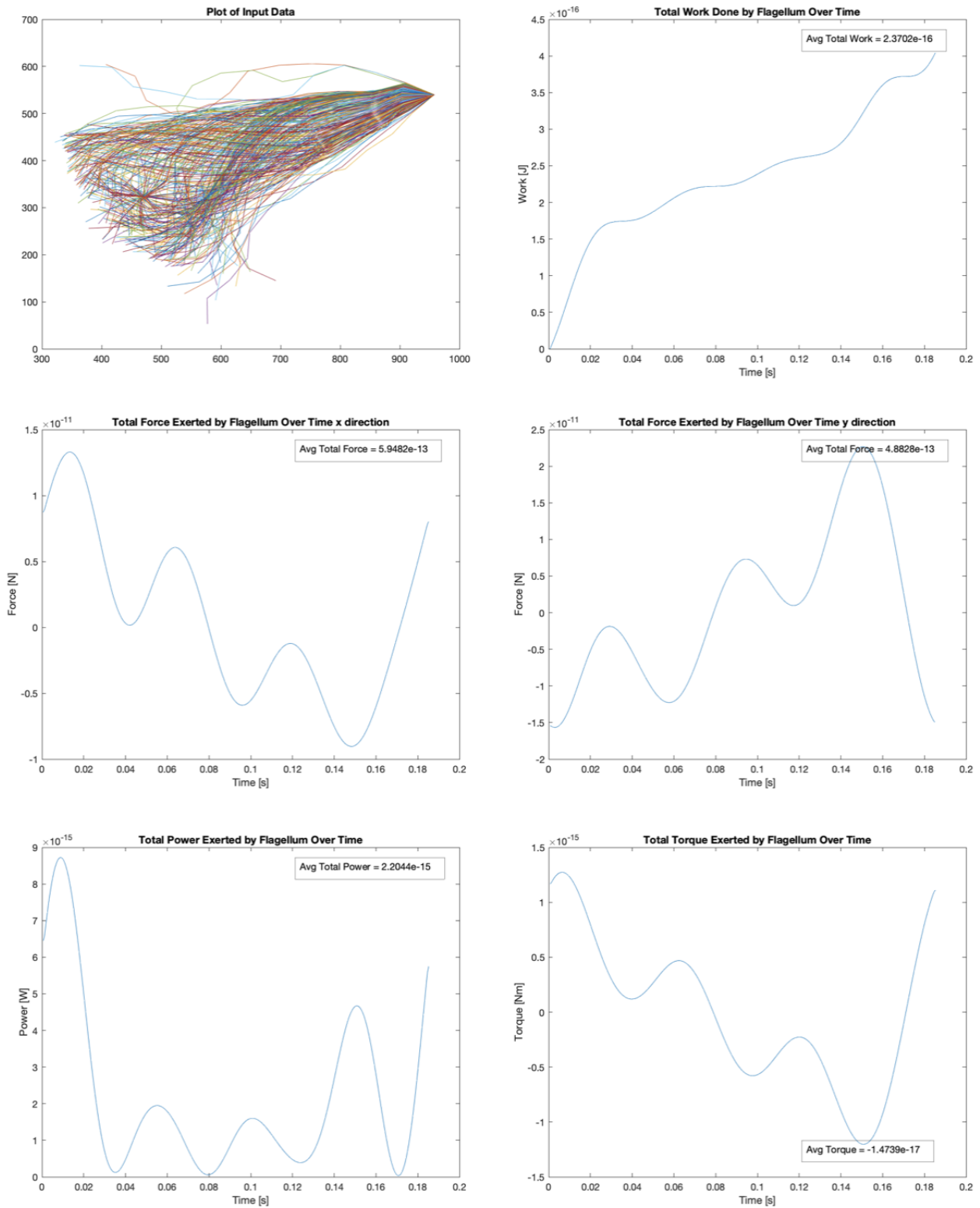


Figure A.6 Sample schematic diagram of test setup.

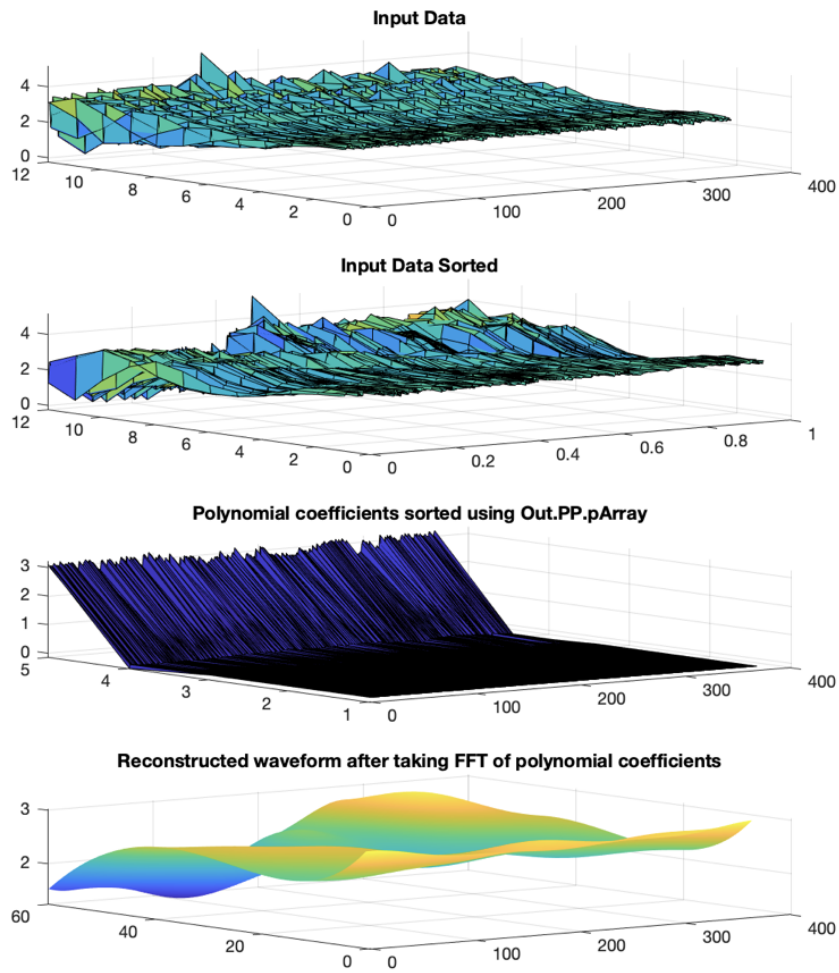
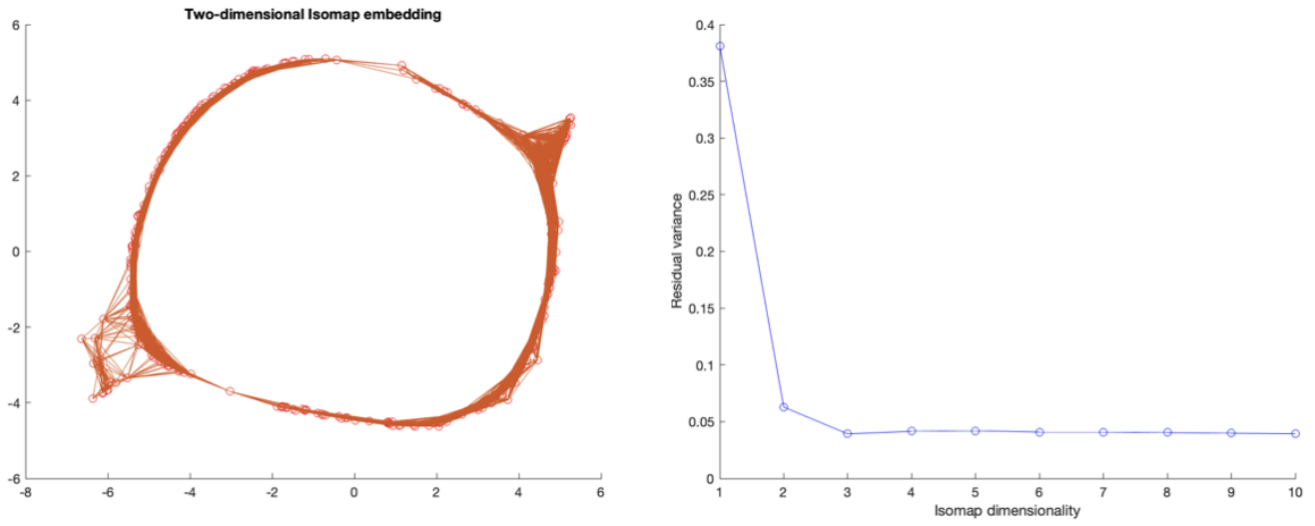


Figure A.7 Video 5a Isomap Output data and reconstructed waveform

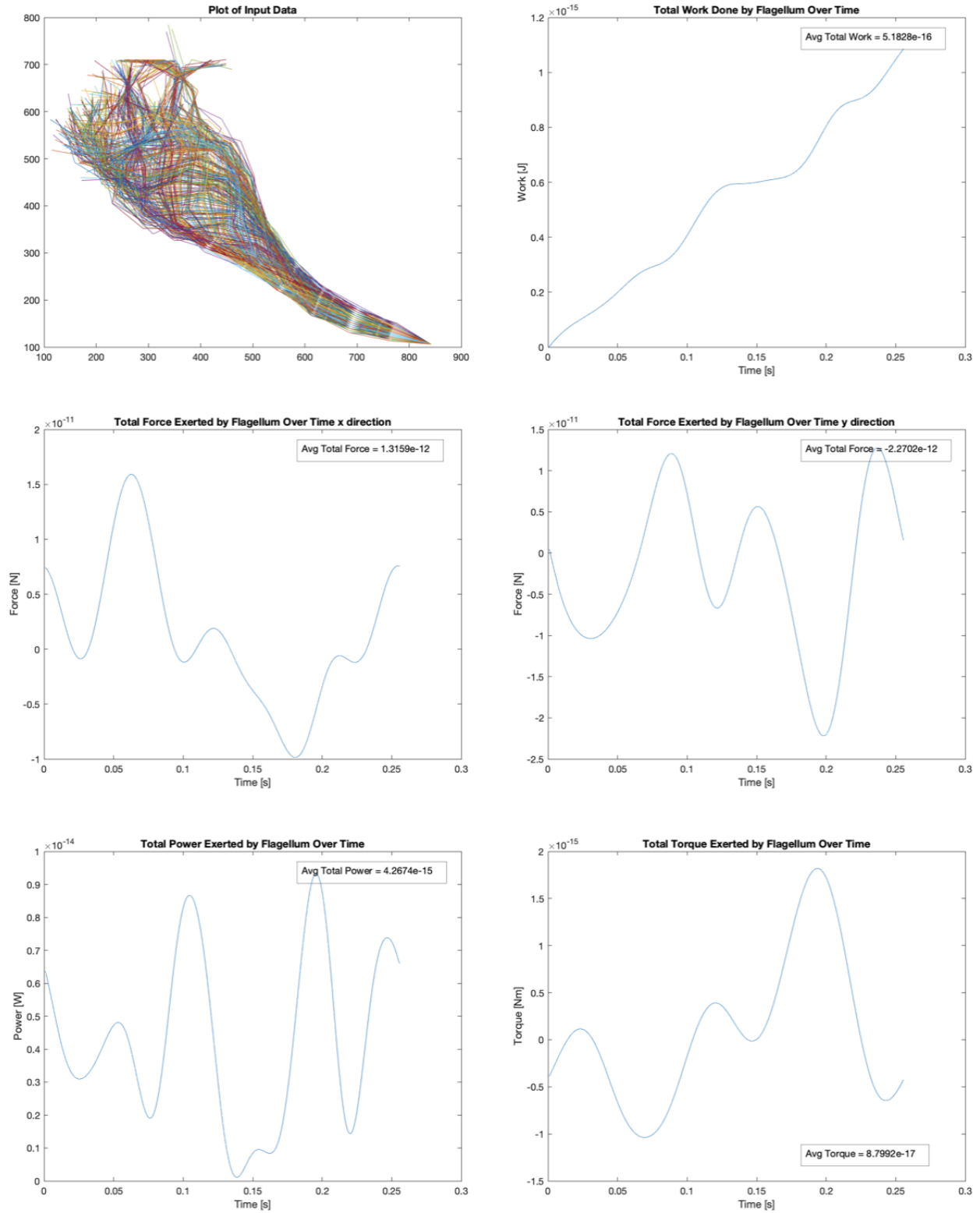


Figure A.8 Sample schematic diagram of test setup.

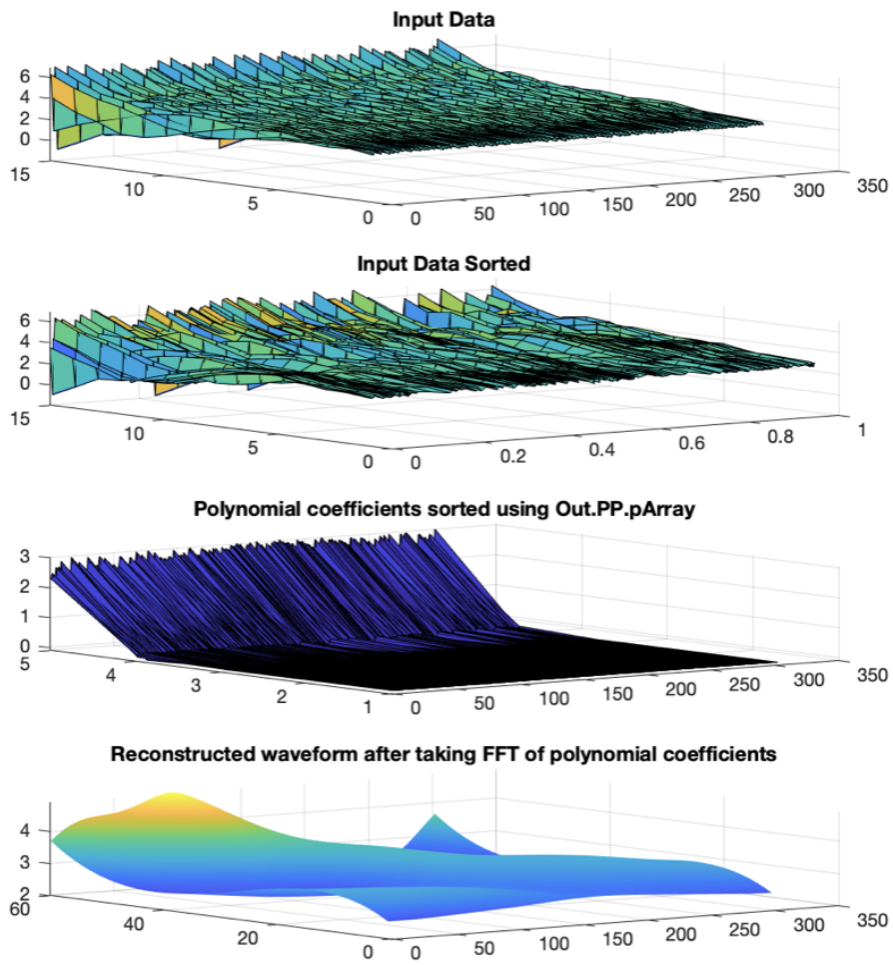
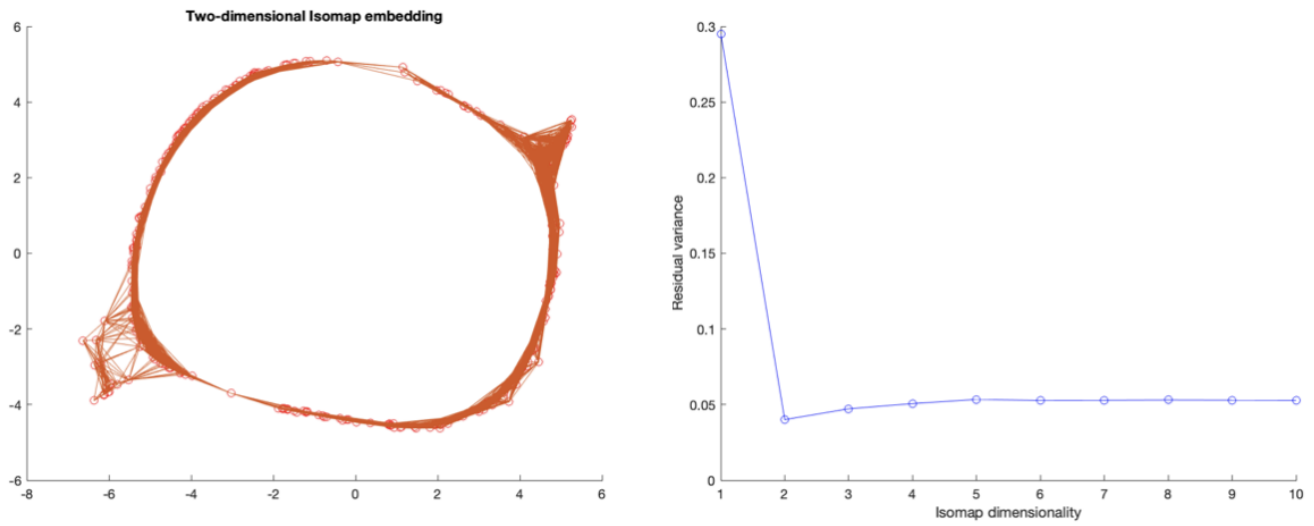


Figure A.9 Video 6a Isomap Output data and reconstructed waveform

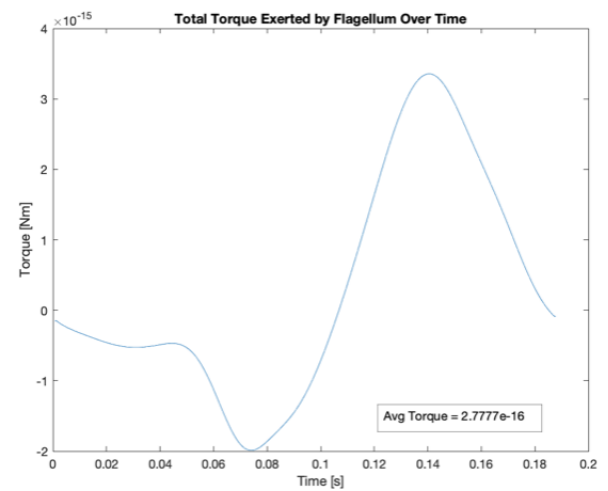
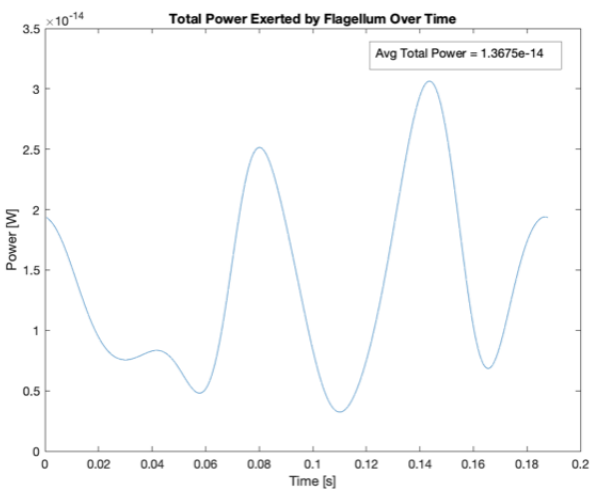
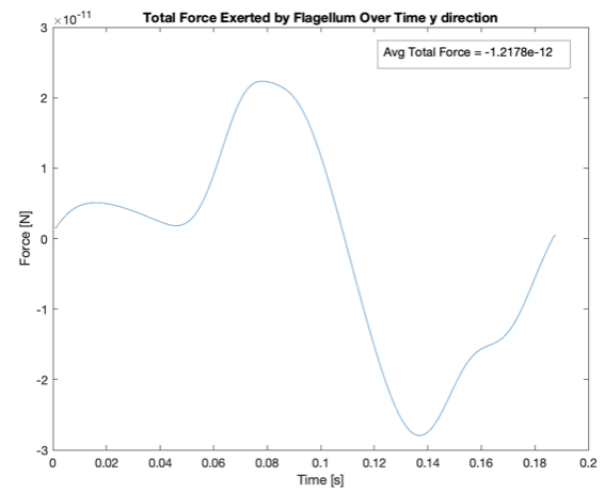
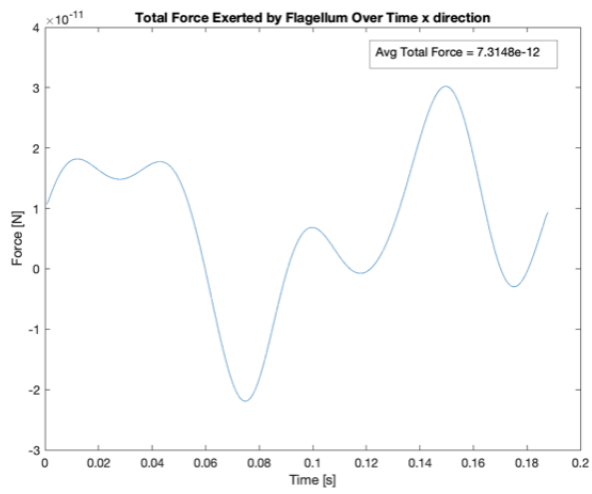
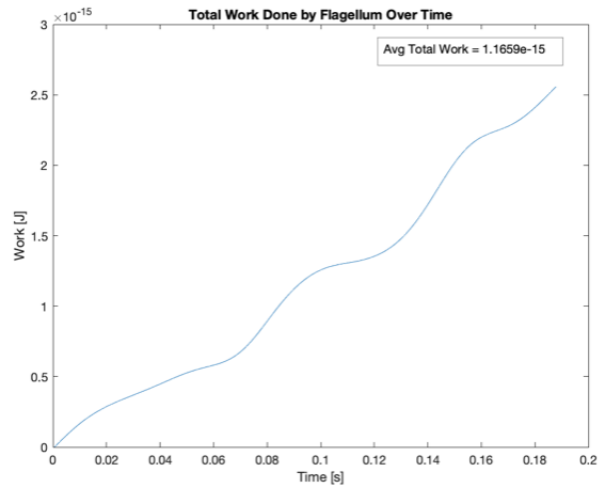
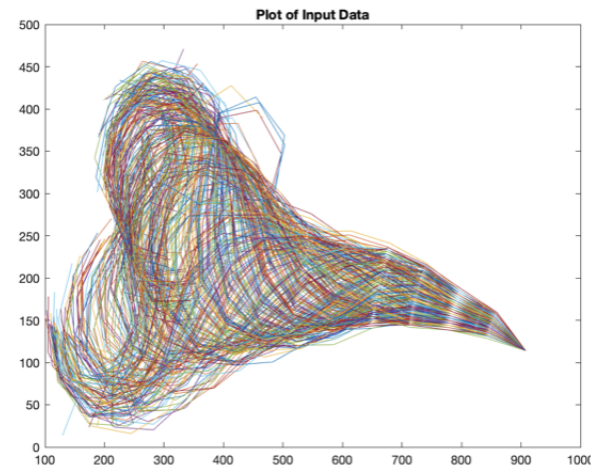


Figure A.10 Sample schematic diagram of test setup.

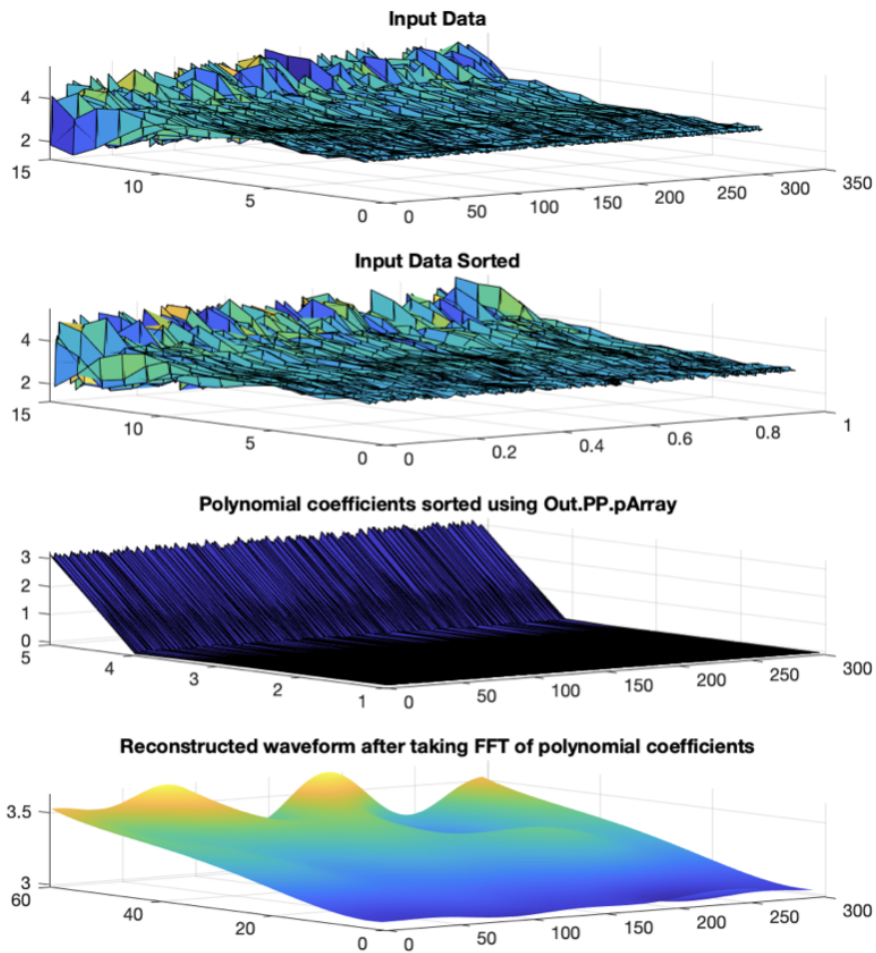
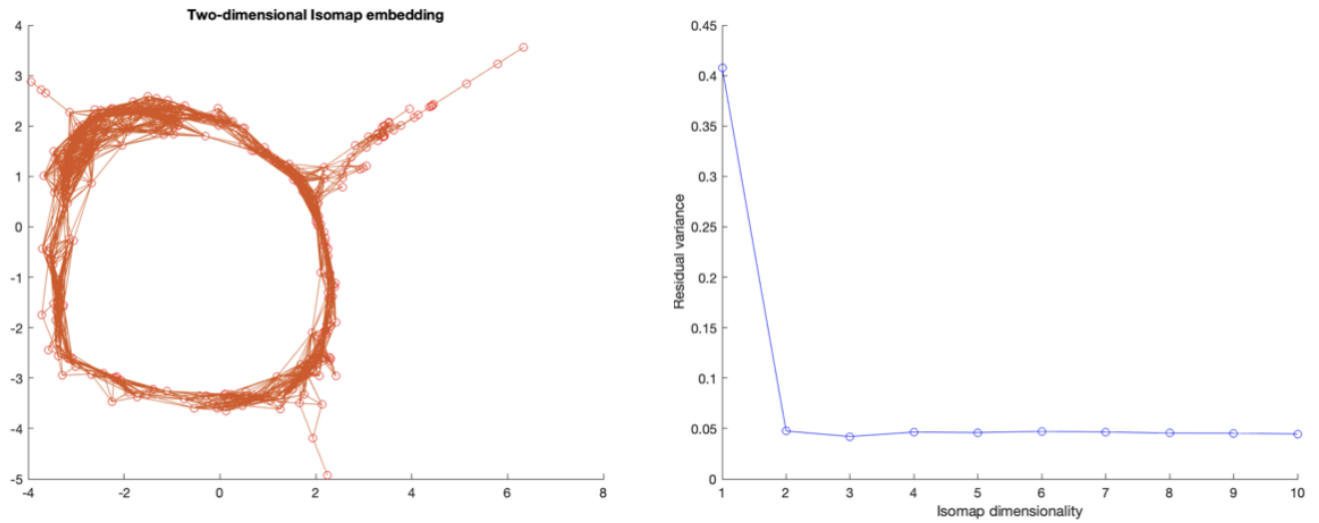


Figure A.11 Video 7a Isomap Output data and reconstructed waveform

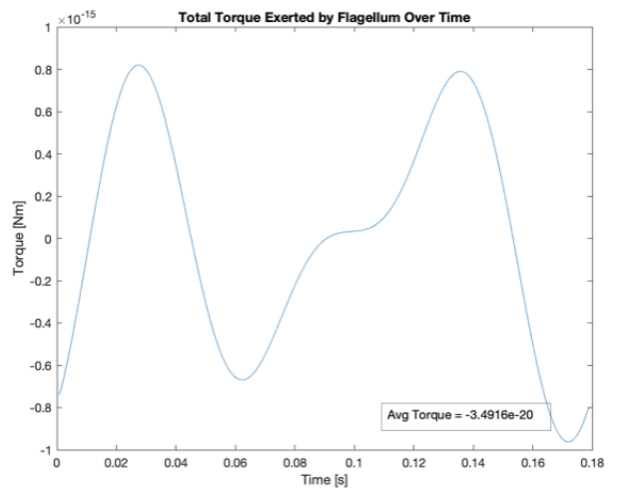
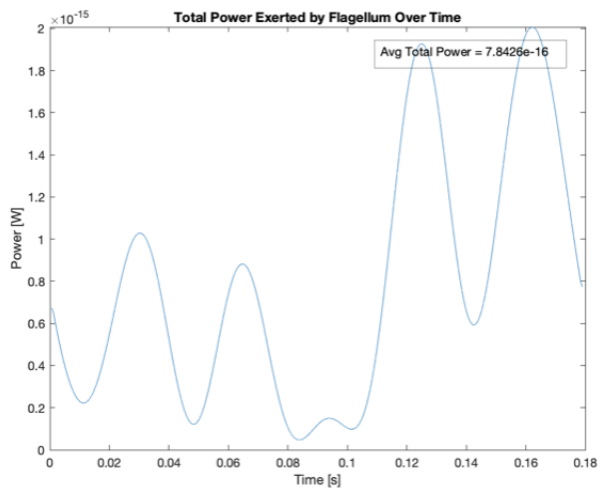
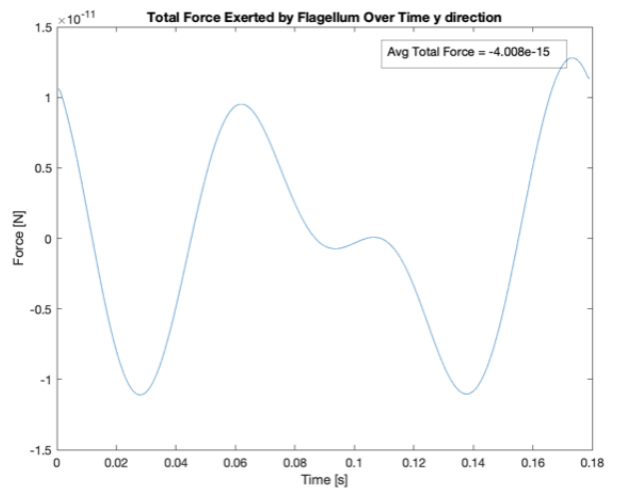
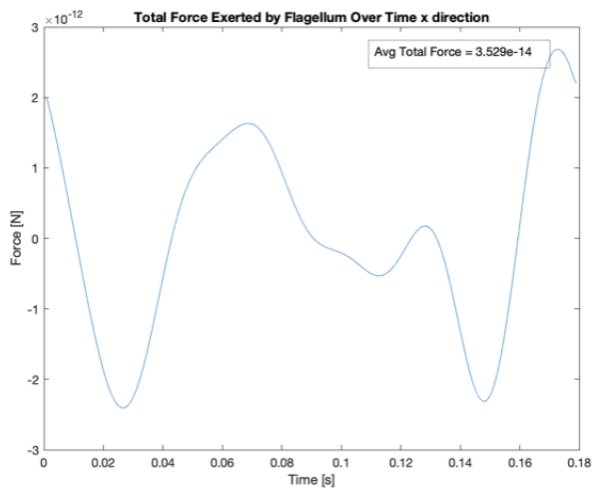
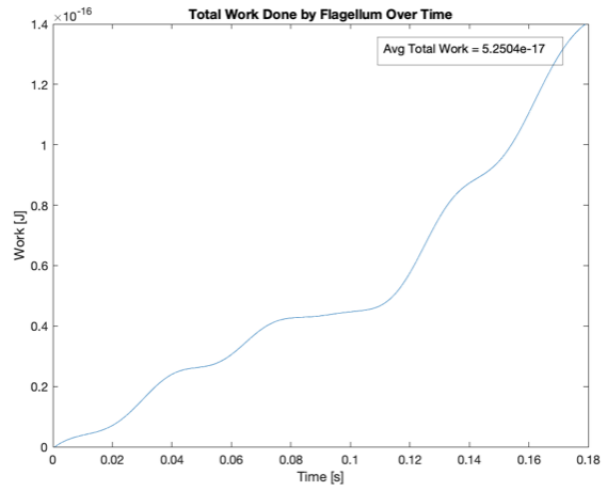
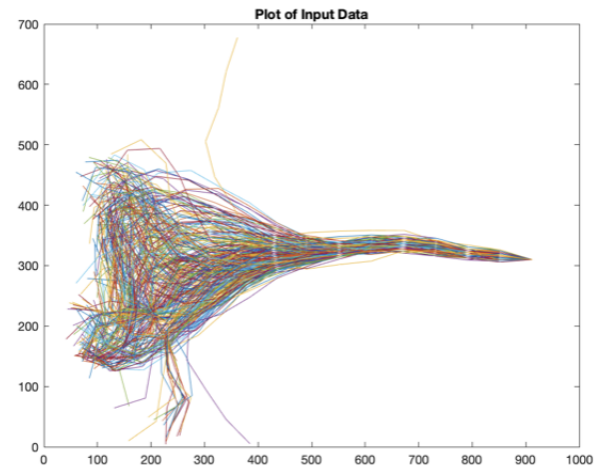


Figure A.12 Sample schematic diagram of test setup.

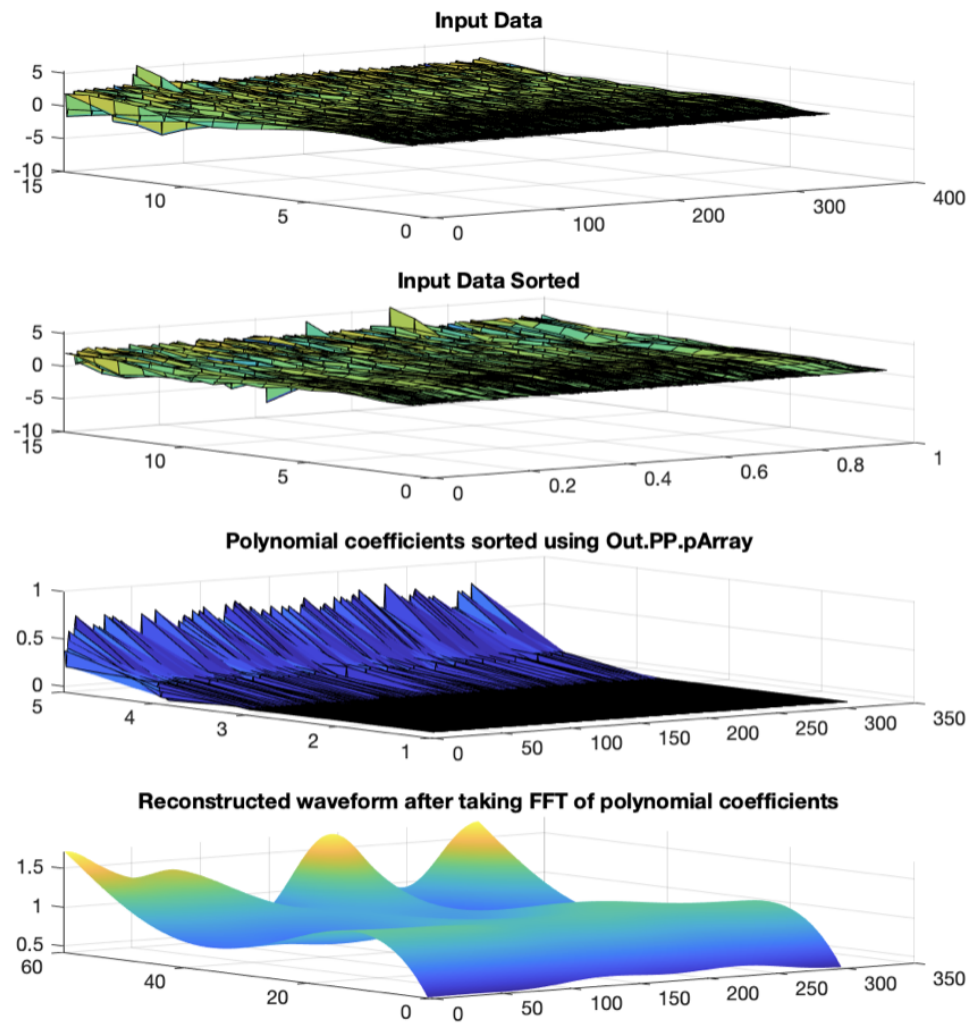
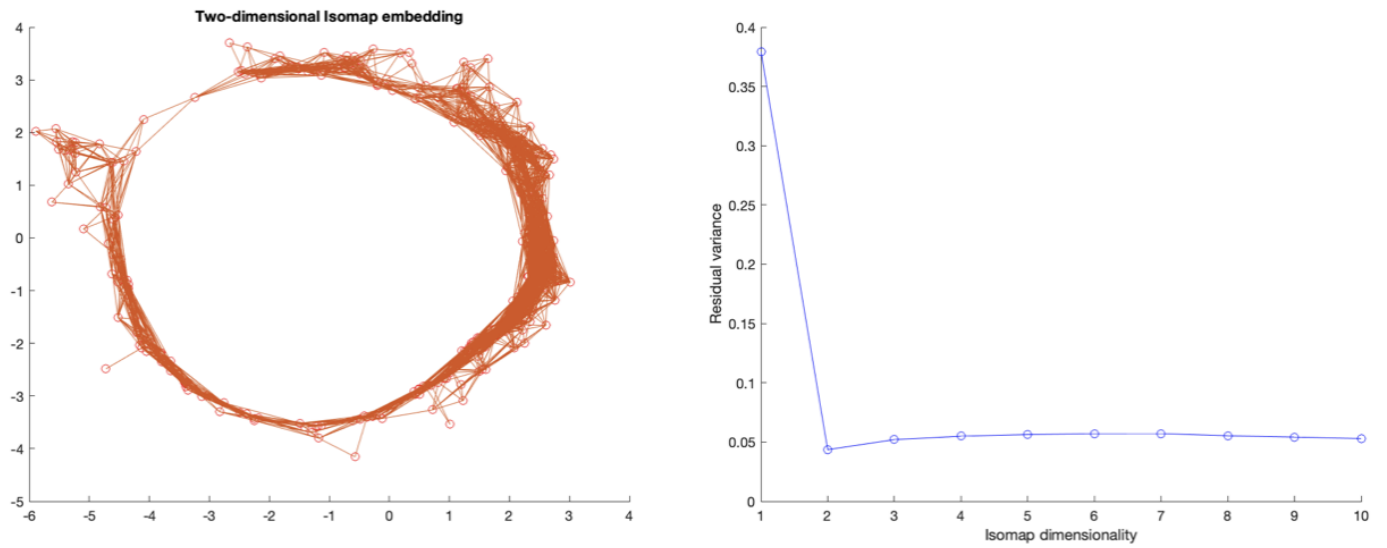


Figure A.13 Video 9a Isomap Output data and reconstructed waveform

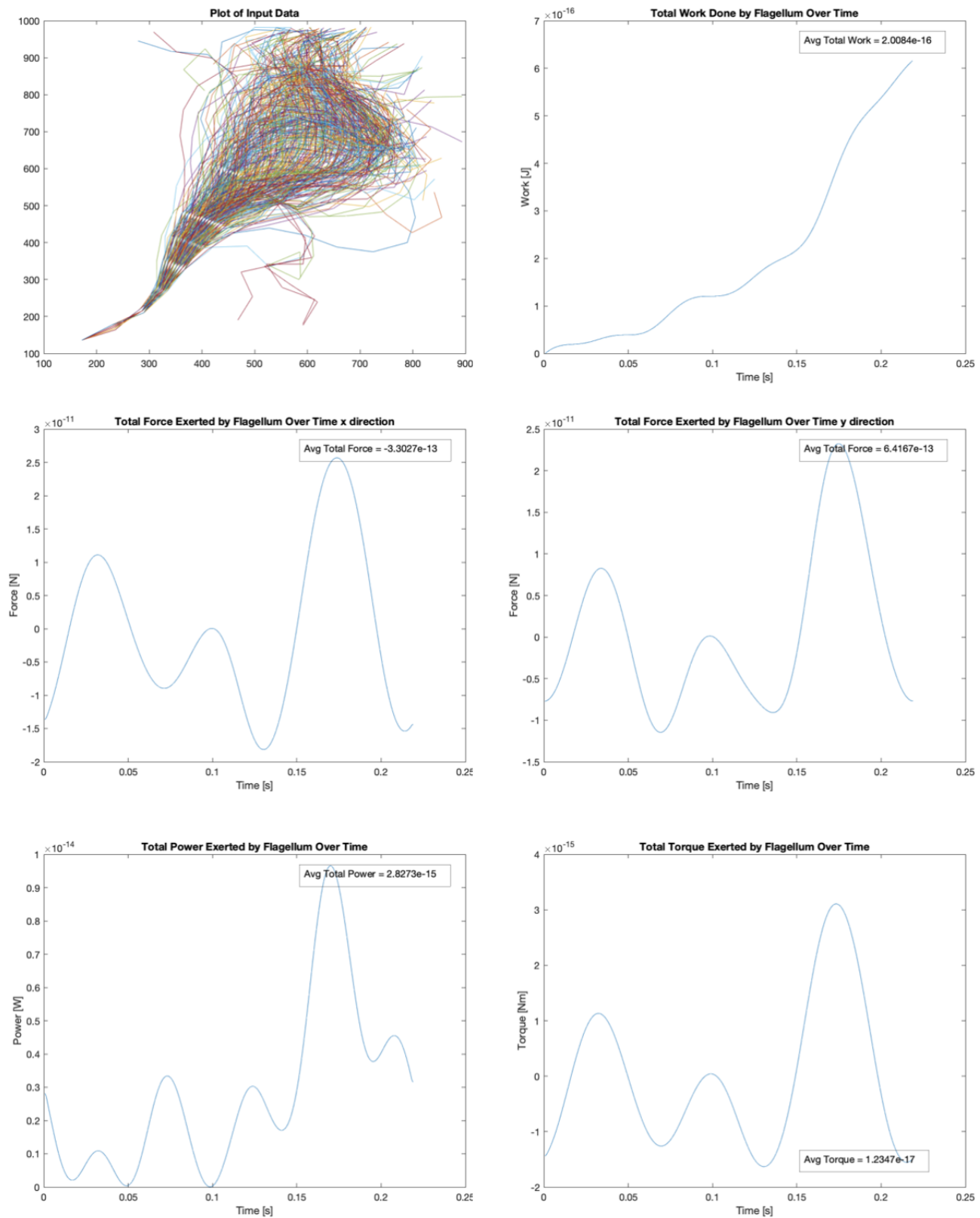


Figure A.14 Sample schematic diagram of test setup.

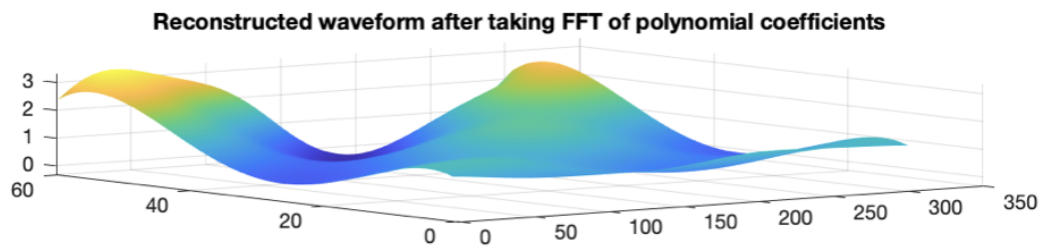
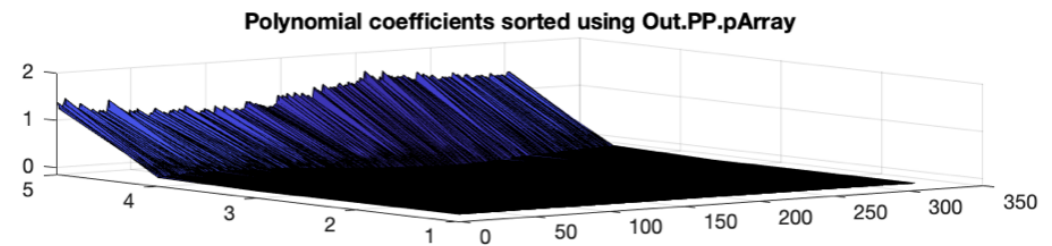
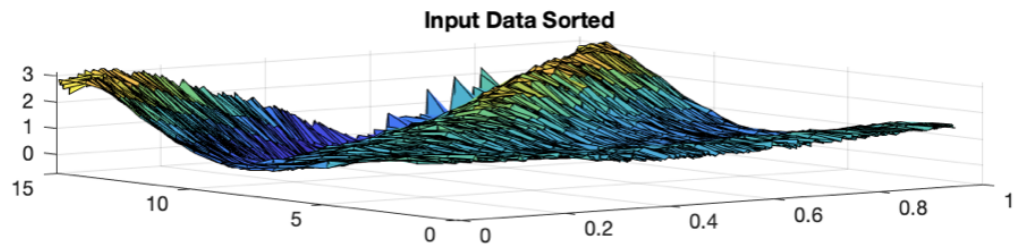
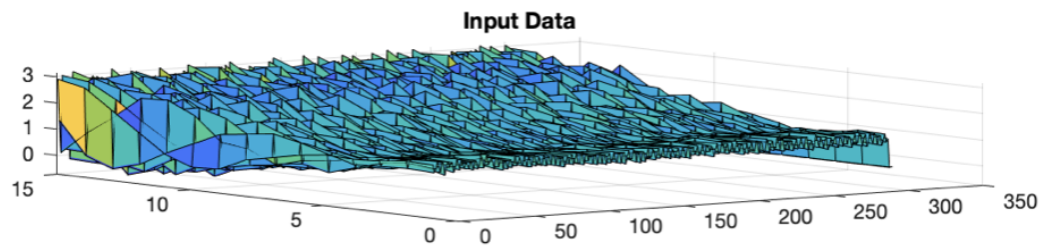
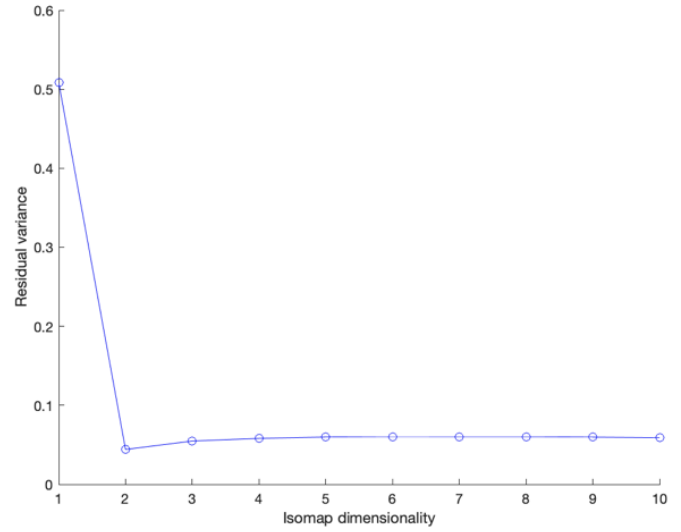
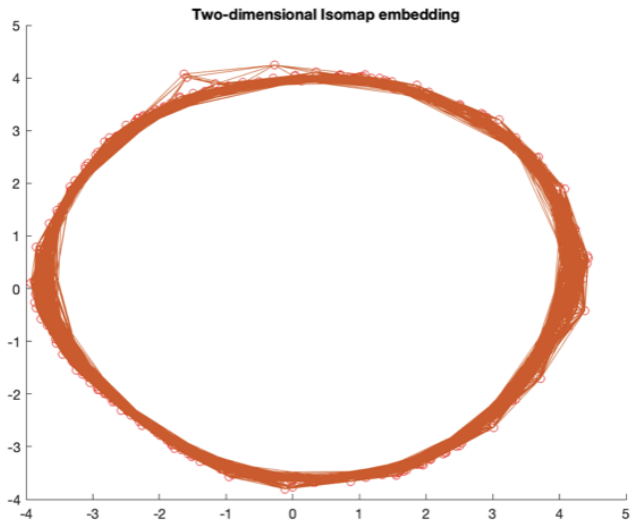


Figure A.15 Video 10a Isomap Output data and reconstructed waveform

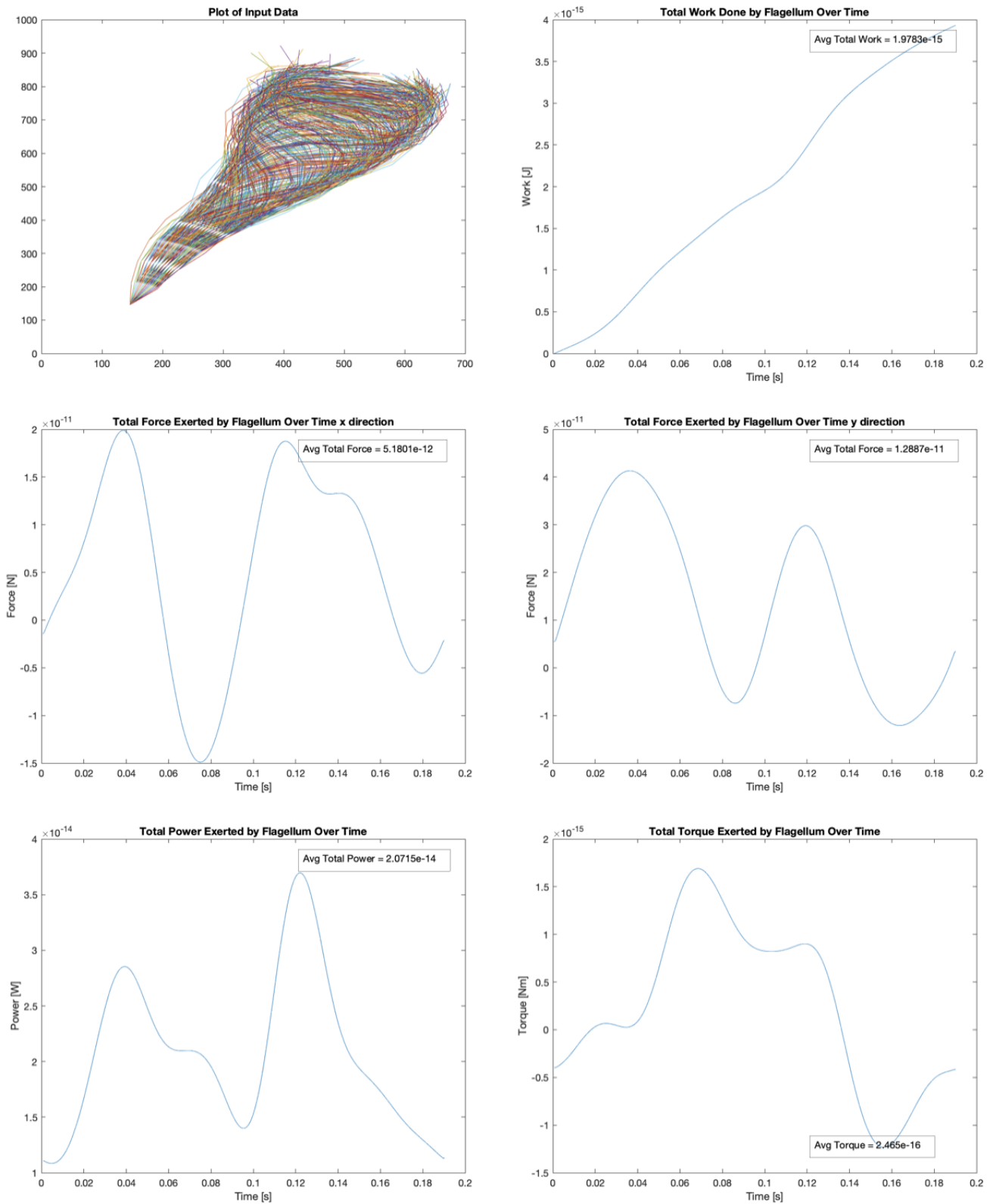


Figure A.16 Sample schematic diagram of test setup.

A.1 Output data for videos of mouse sperm with condition A.

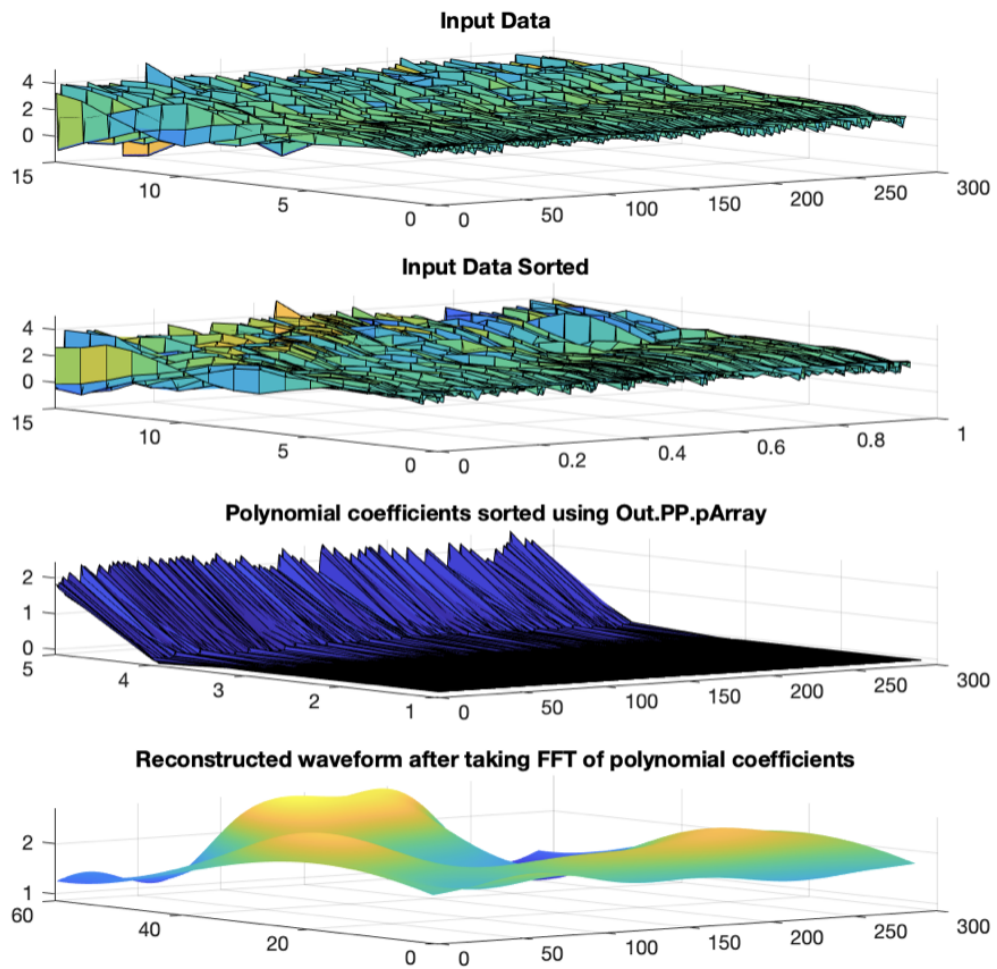
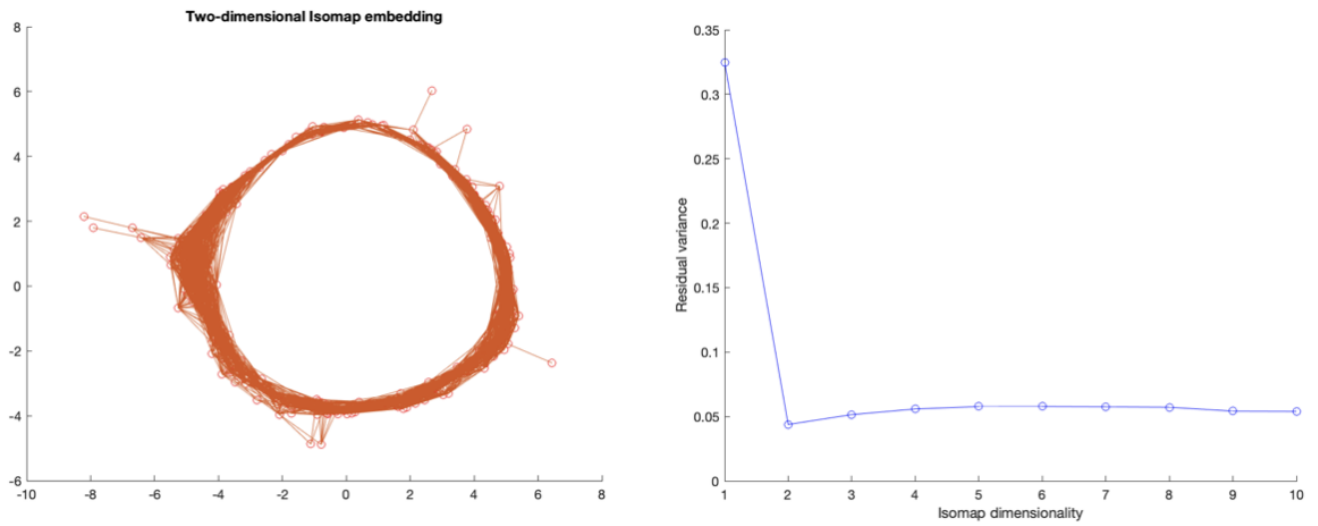


Figure A.17 Video 2b Isomap Output data and reconstructed waveform

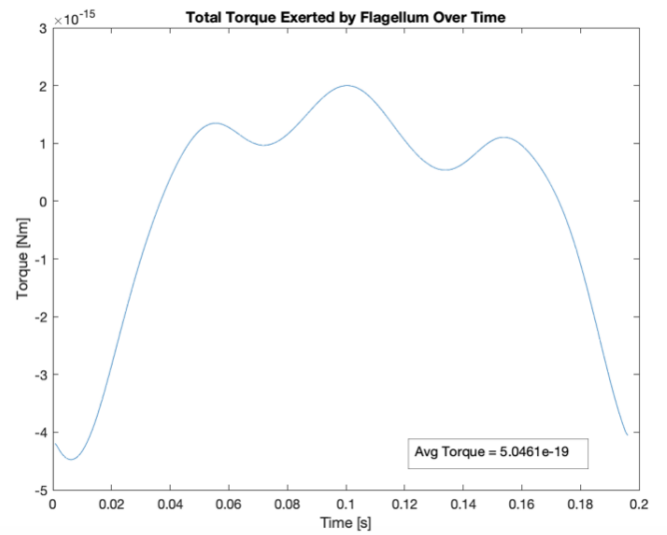
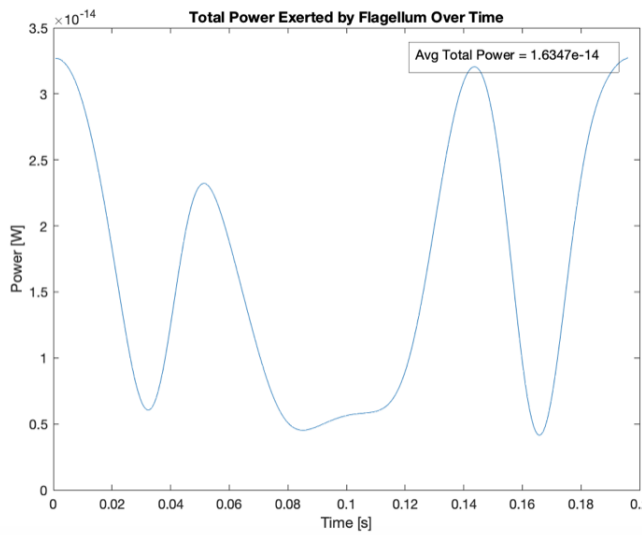
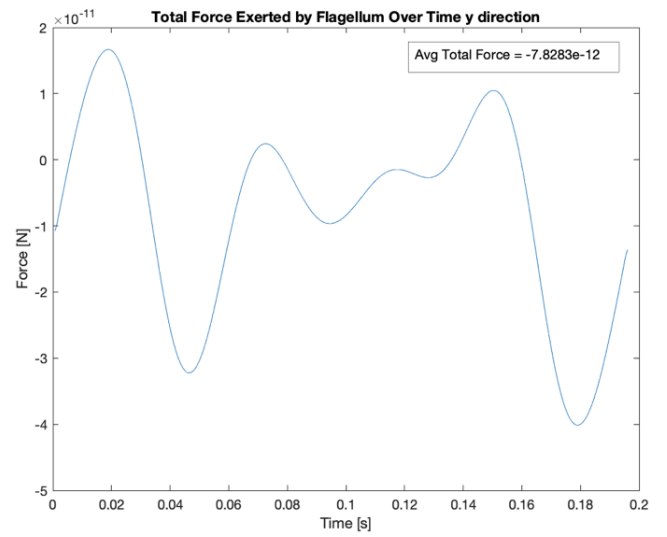
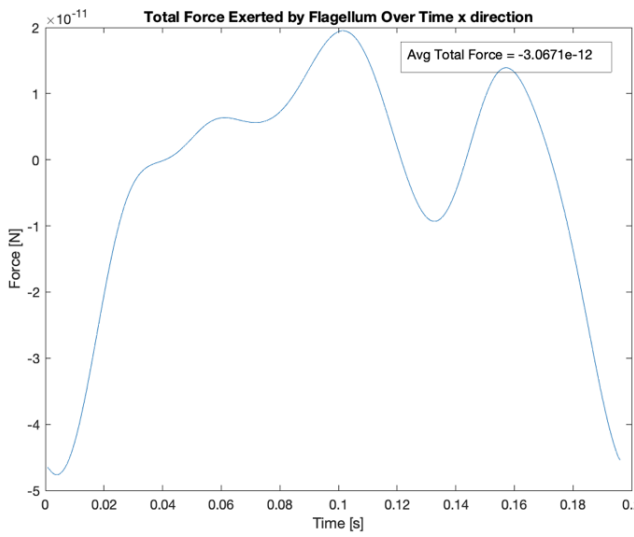
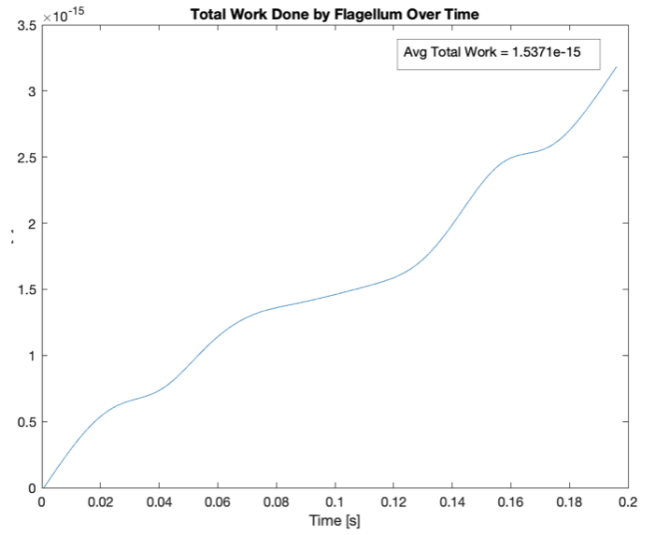
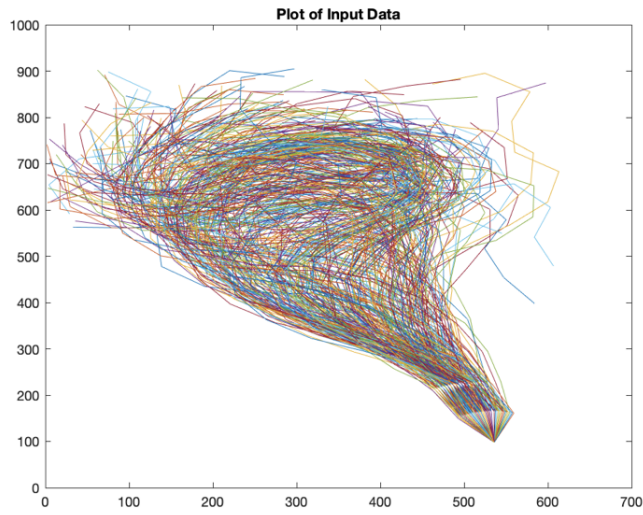


Figure A.18 Sample schematic diagram of test setup.

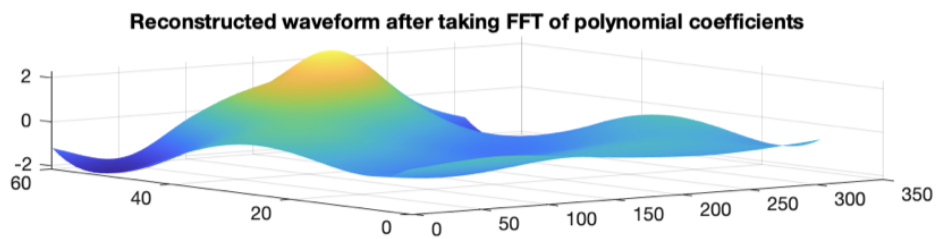
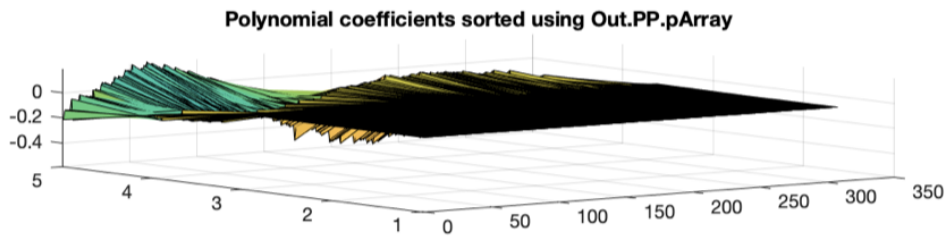
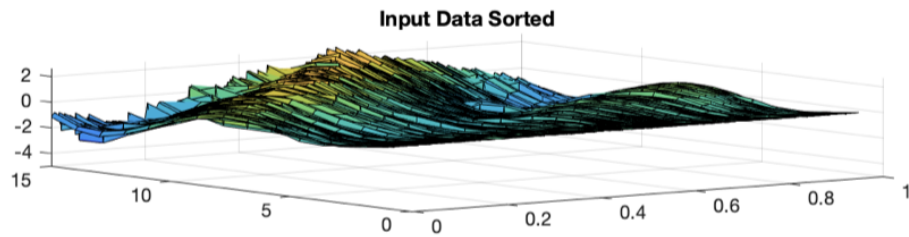
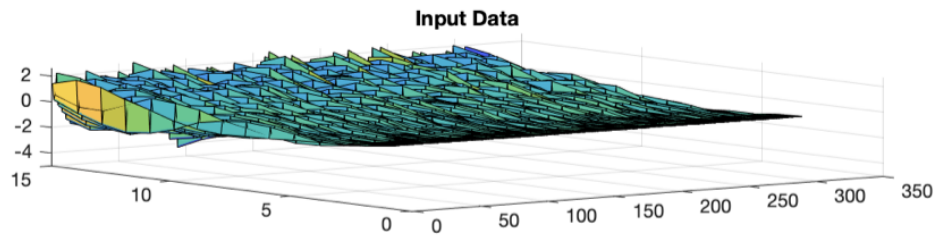
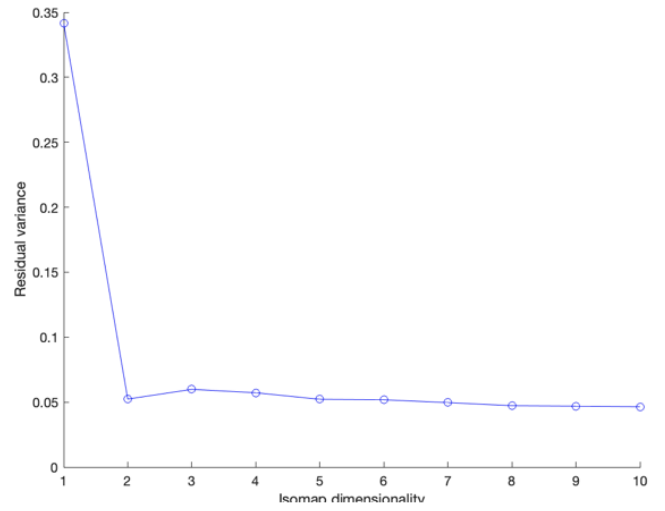
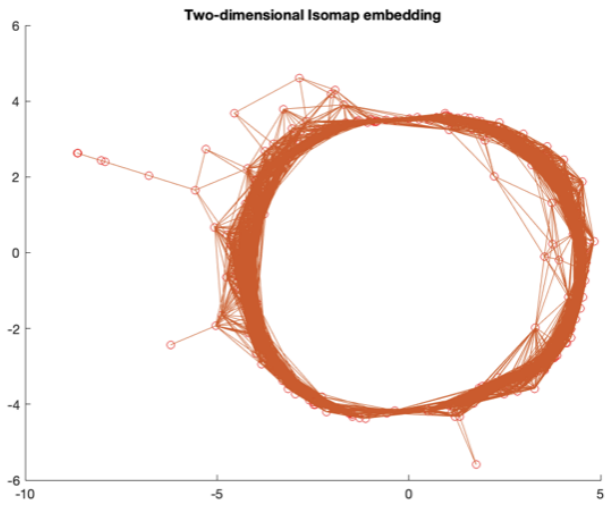


Figure A.19 Video 3b Isomap Output data and reconstructed waveform

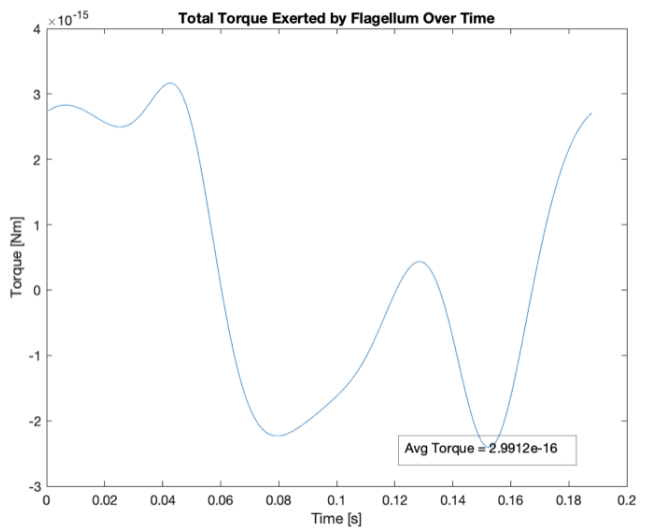
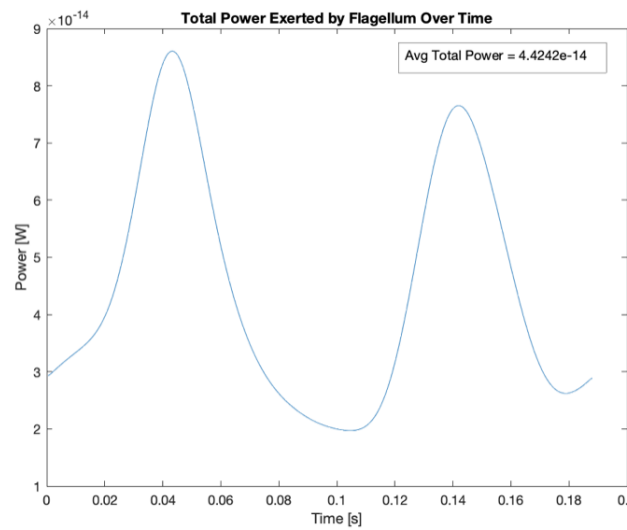
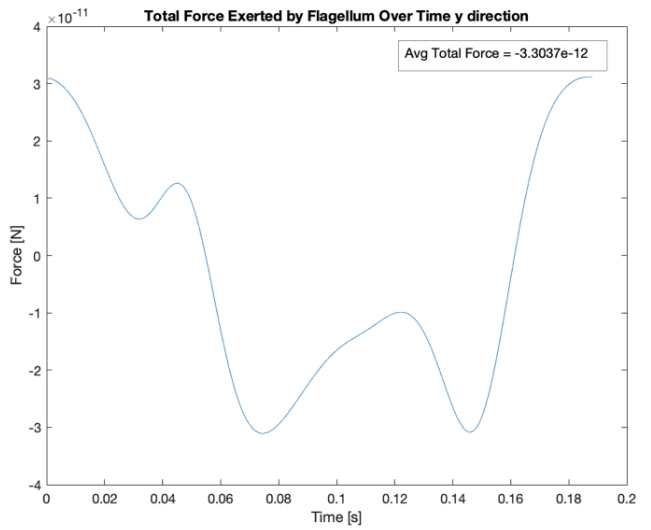
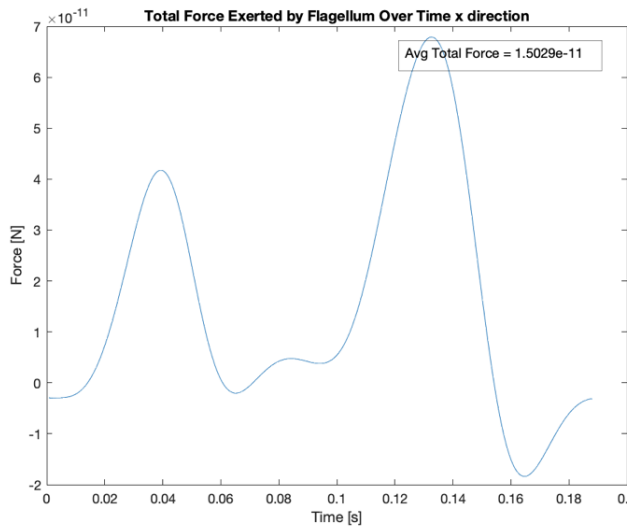
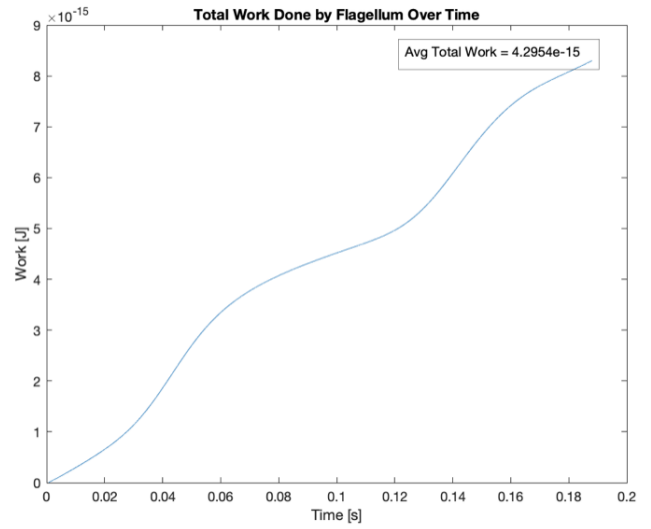
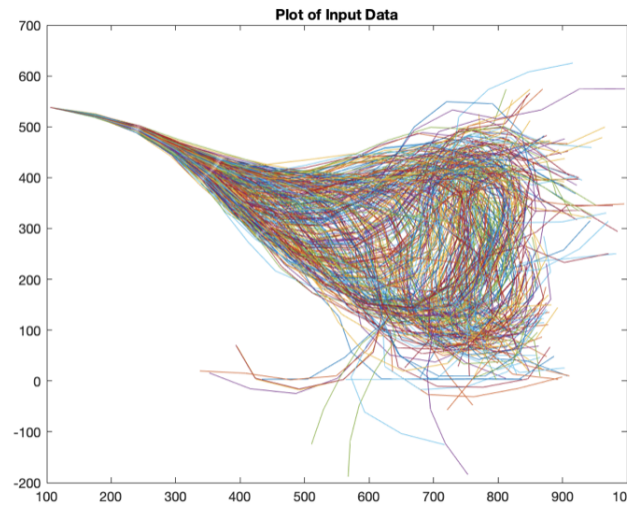


Figure A.20 Video 2b Isomap Output data and reconstructed waveform

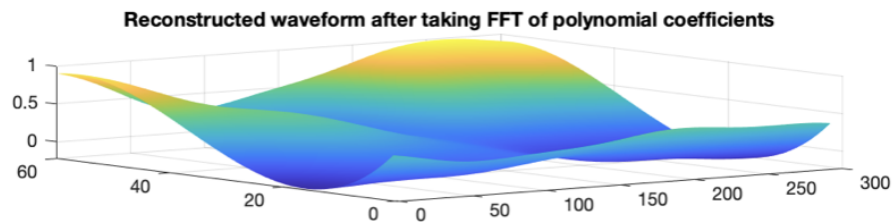
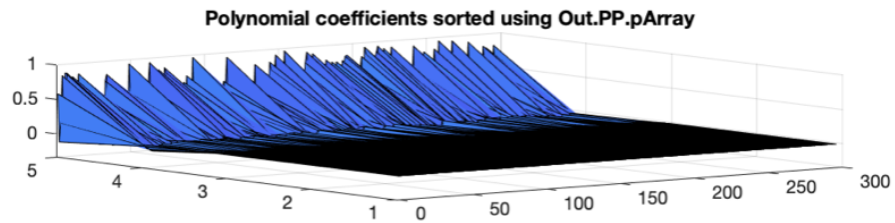
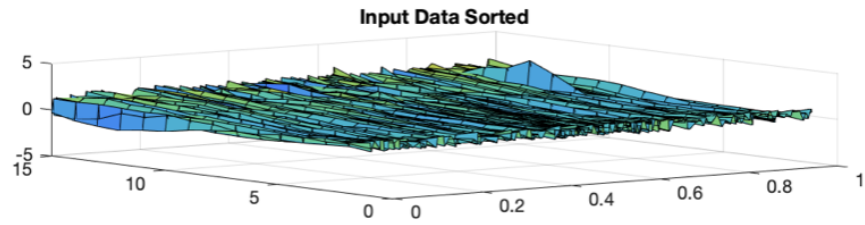
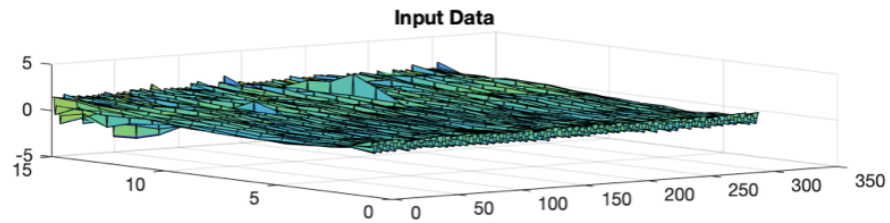
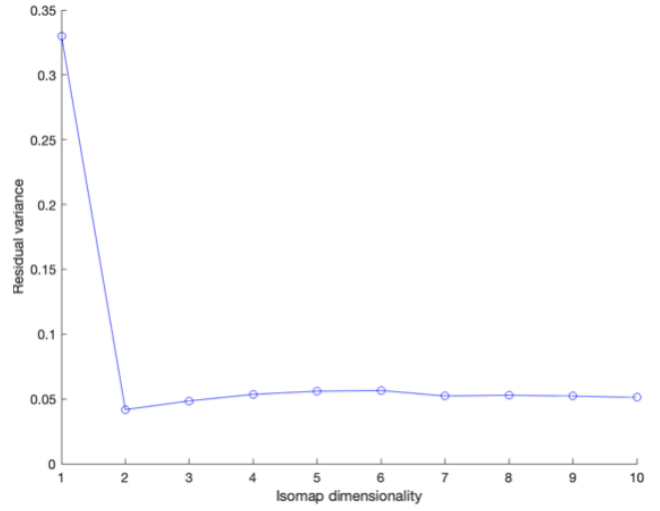
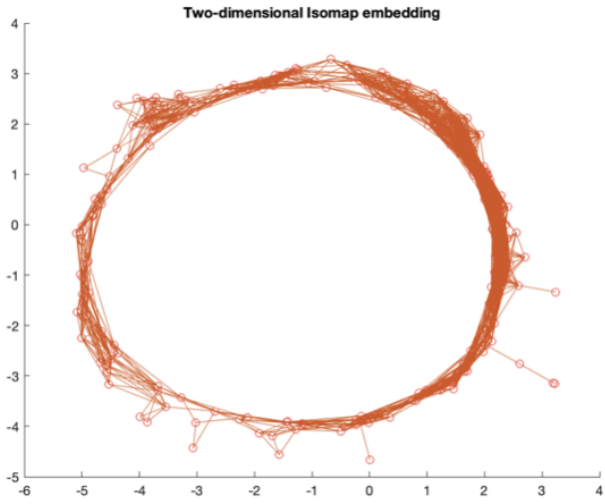


Figure A.21 Video 6b Isomap Output data and reconstructed waveform

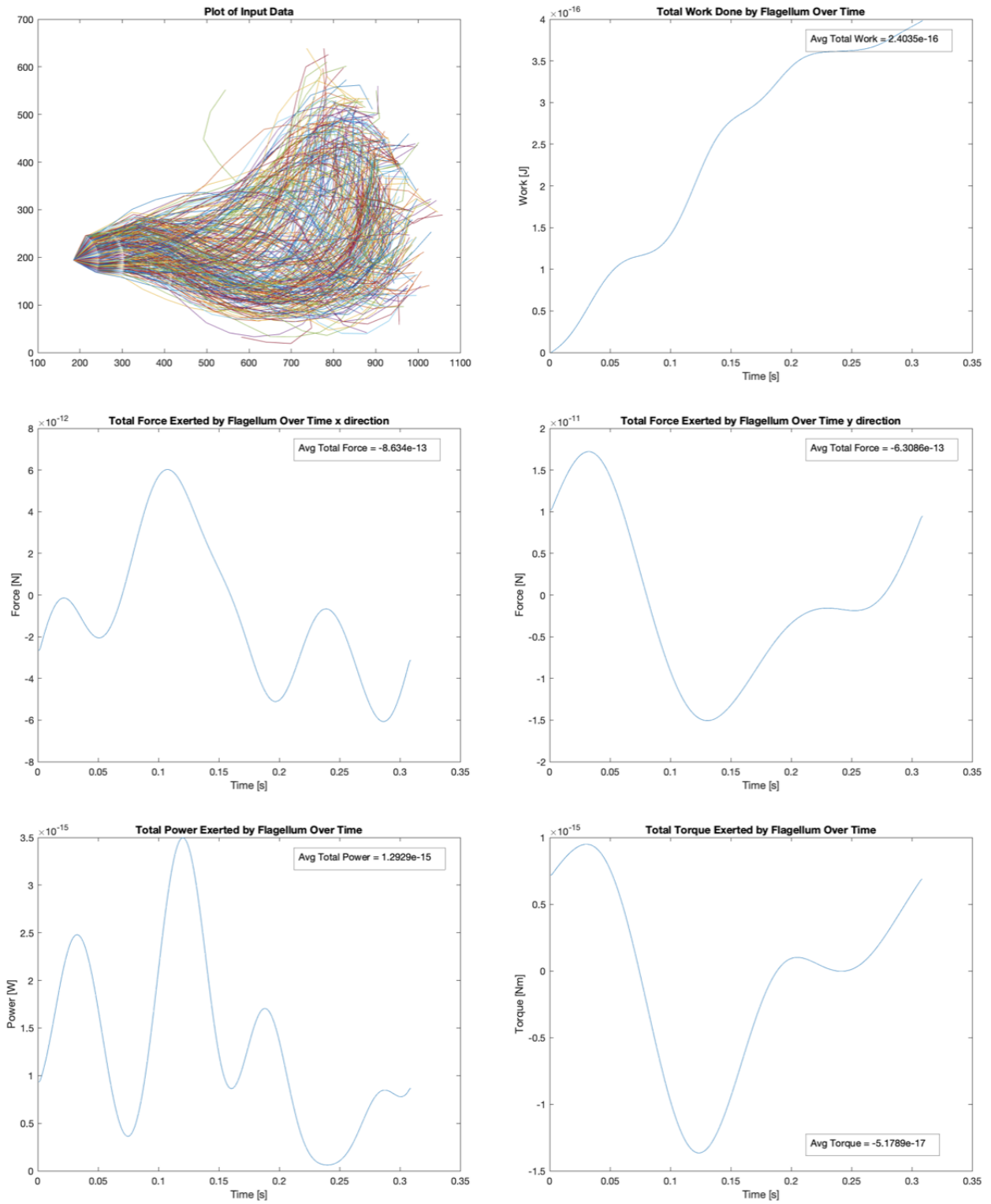


Figure A.22 Sample schematic diagram of test setup.

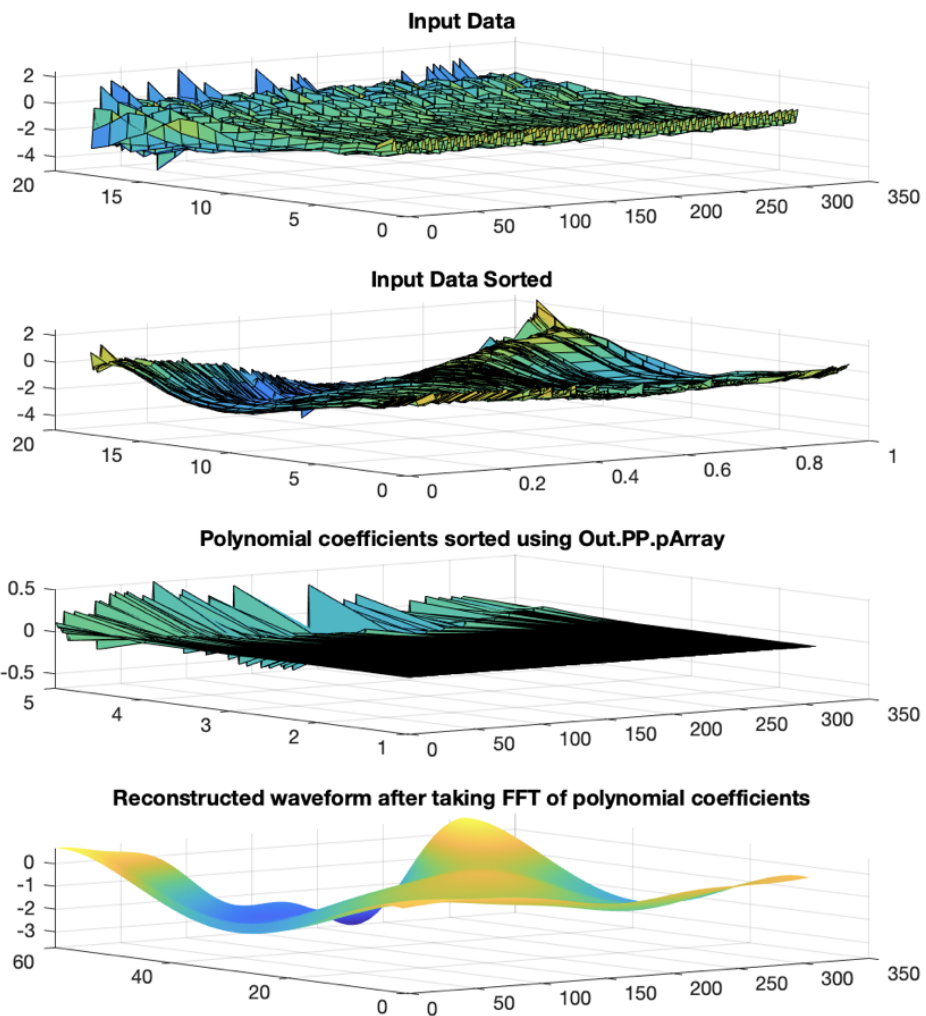
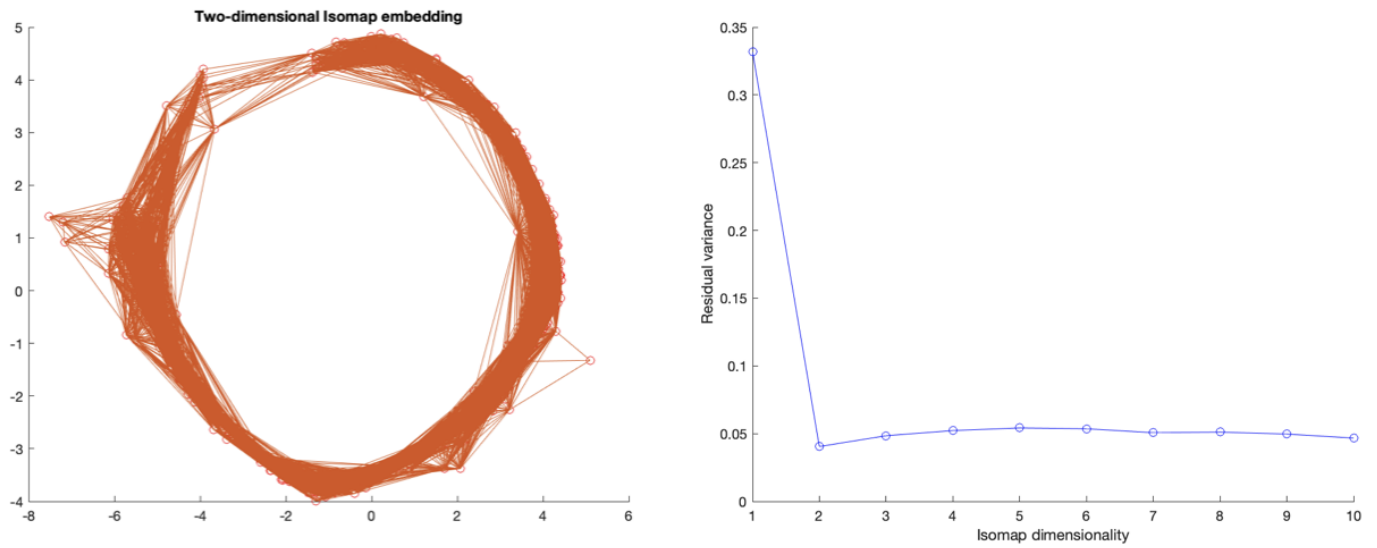


Figure A.23 Video 9b Isomap Output data and reconstructed waveform

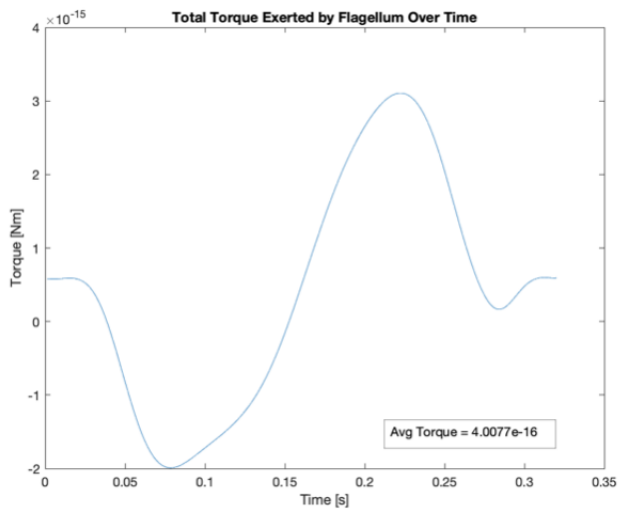
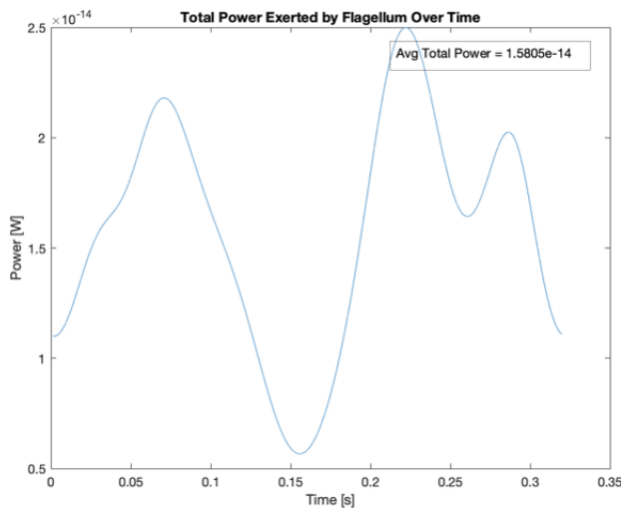
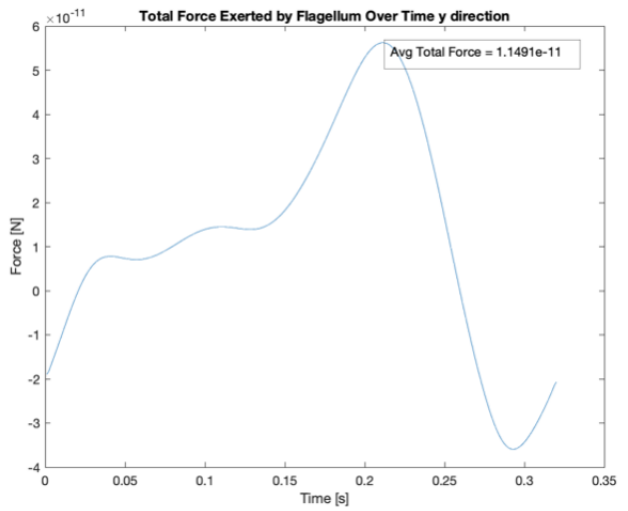
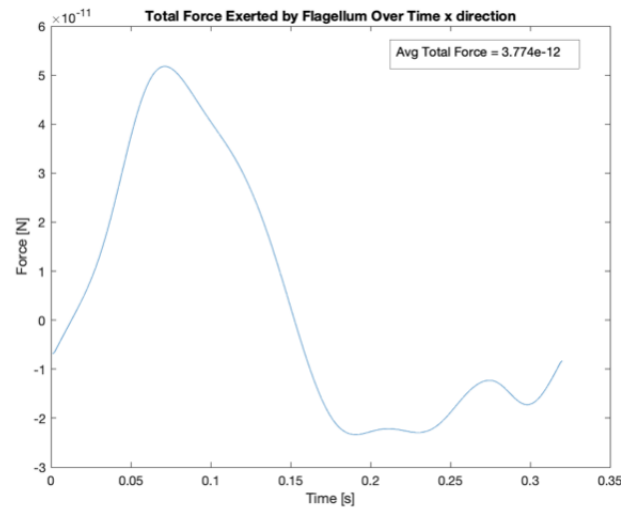
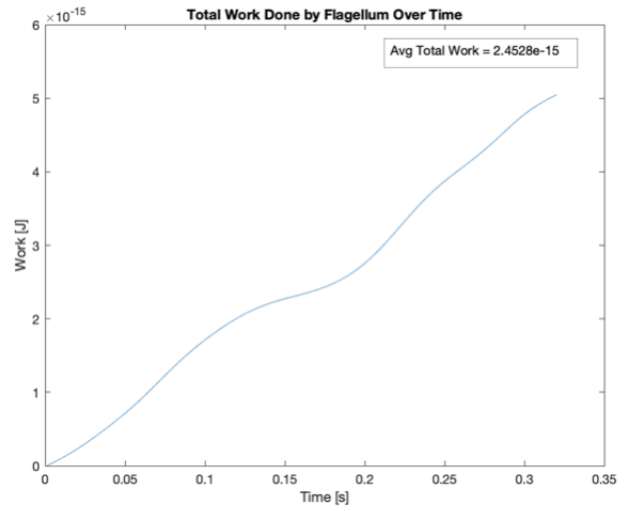
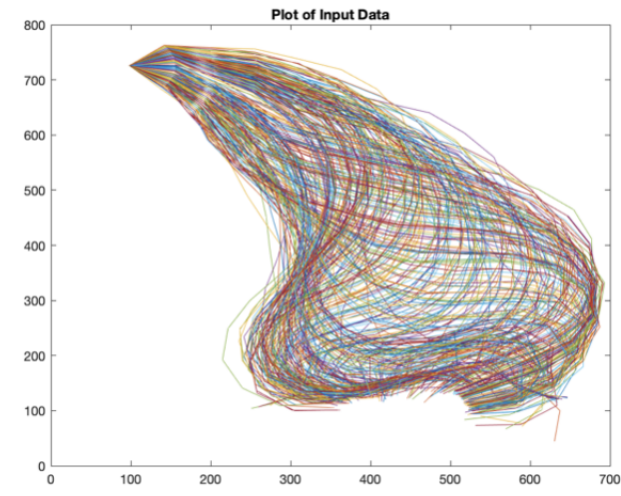


Figure A.24 Sample schematic diagram of test setup.

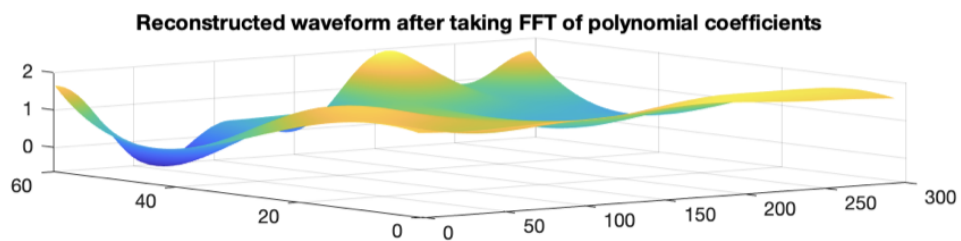
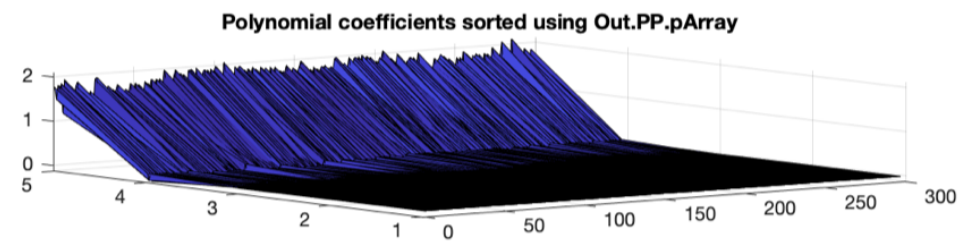
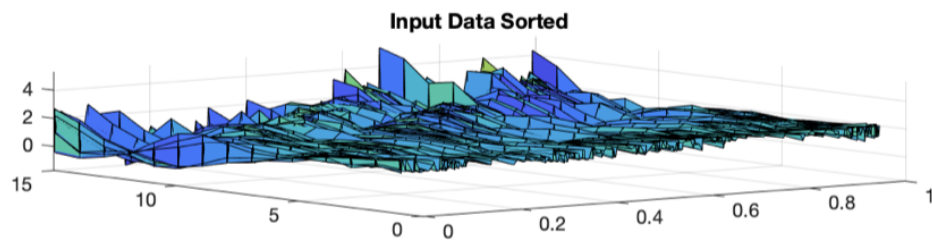
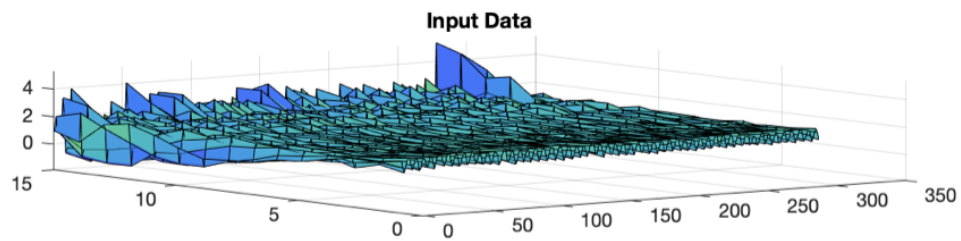
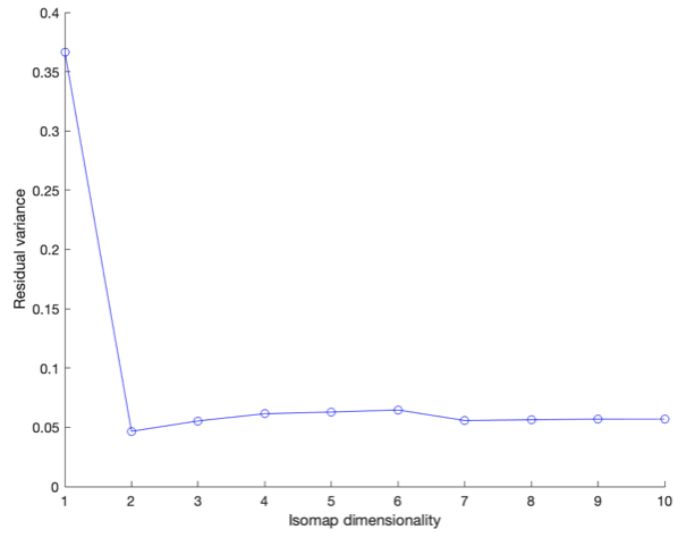
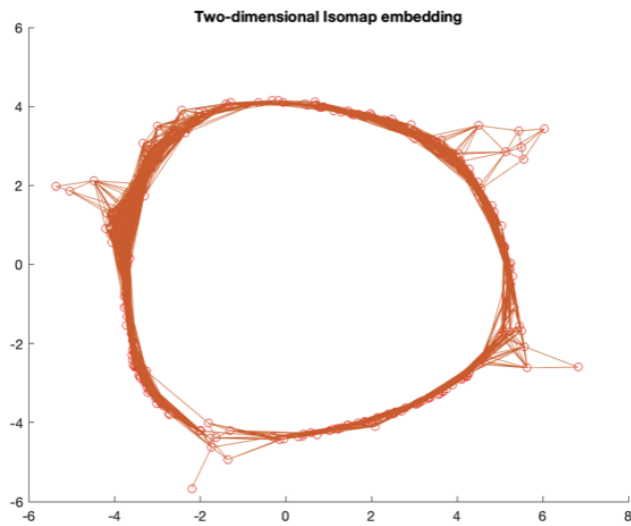


Figure A.25 Video 11b Isomap Output data and reconstructed waveform

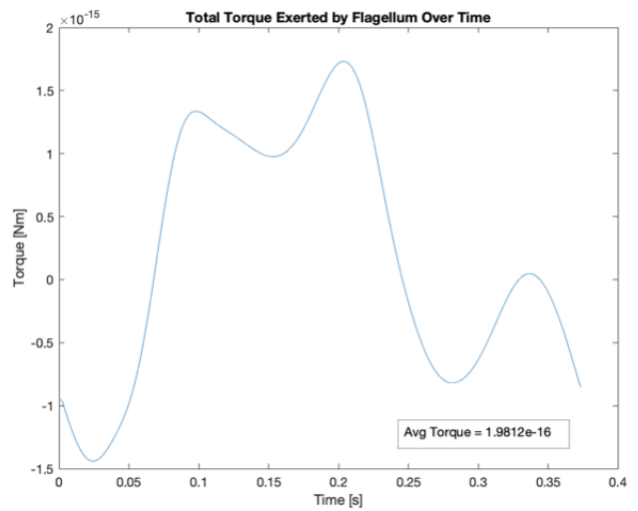
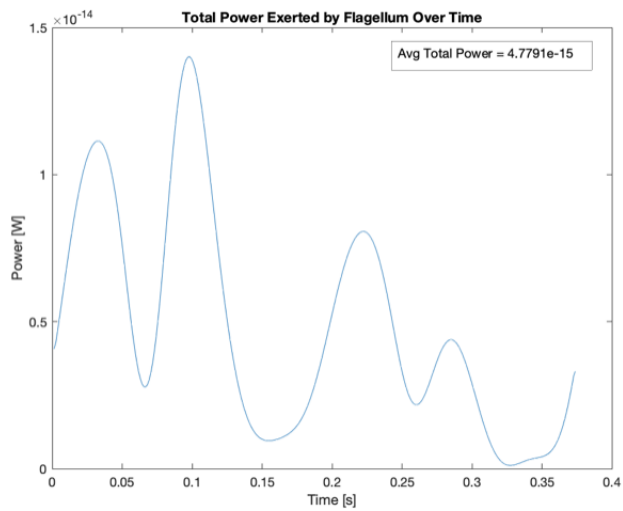
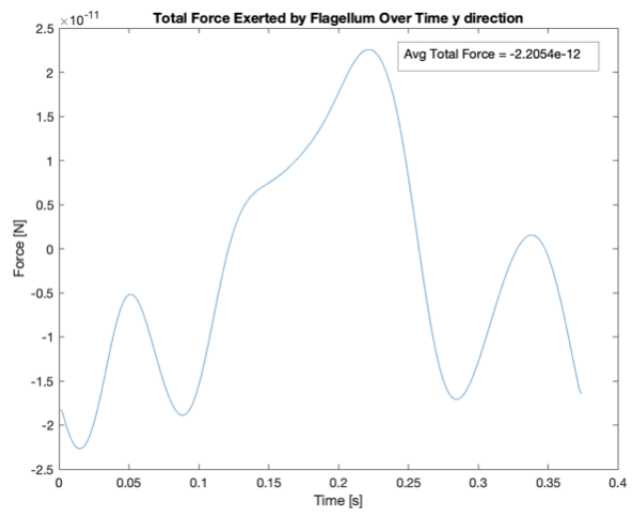
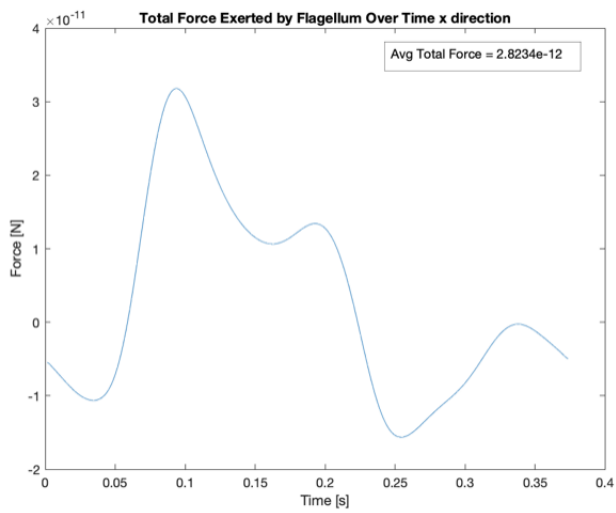
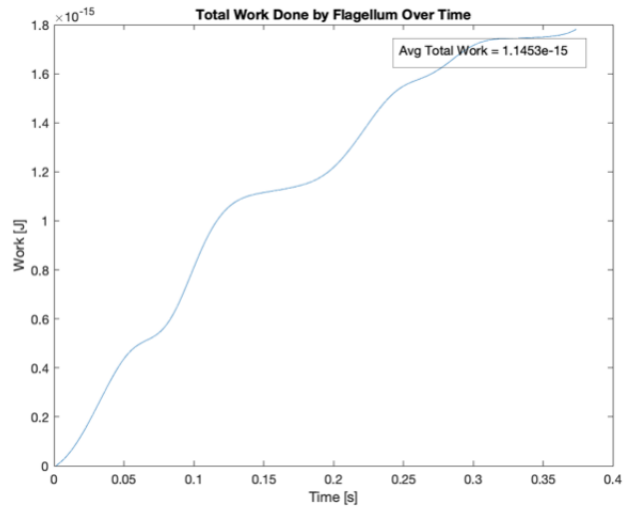
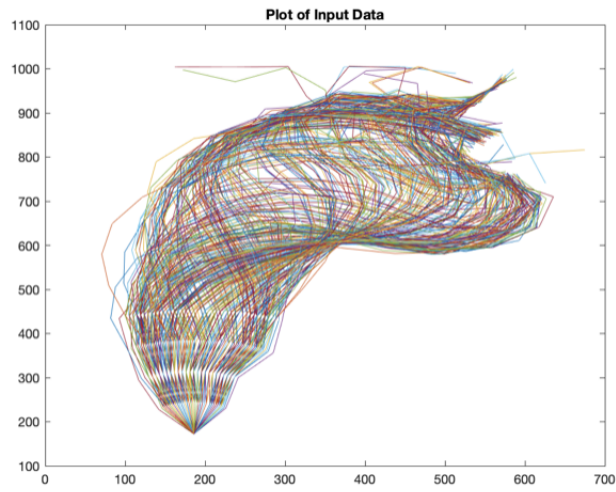


Figure A.26 Sample schematic diagram of test setup.

A.2 Output data for videos of mouse sperm with condition B.

B MATLAB Code

```
1 % Sort waveforms and compute forces
2 % A Gupte and PVB 2021 1207
3 MOVIEYES = 0; % set to 1 to show movies
4 % Get coordinates in low-dimensional projection
5 coords = Y.coords(2); % coordinates in embedding space
6 len = length(Y.index); % how many time steps
7
8 % % LGW Purge:
9 % twod = find(options.dims==2);
10 % nc = sum(E);
11 % outside = nc < 0;
12 % inside = ~outside;
13
14
15 % get each component
16 x = coords{1}(1,:);
17 y = coords{1}(2,:);
18 thetaRecon = Out.PP.thetaRecon;
19 % sort by phase angle in cycle
20 theta = atan2(y,x);
21 [thetas, inds] = sort(theta);
22
23
24 % % LGW
25 % elim = find(outside);
26 % for ii = elim
27 %     inds(inds == ii) = [];
28 % end
29 len = numel(inds);
30 tt = (theta(inds)+pi)/(2*pi);
31 % apply to sort your input
32 % PVB 2021 1207 check of sorting
33 % xi=x(inds);
```

```

34 % yi=y(inds);
35 % figure(100), plot(xi,yi)
36
37 inputsorted = input_data(:,inds);
38 % subplot(4,1,1)
39 % imagesc(input_data)
40 % subplot(4,1,2)
41 % imagesc(inputsorted)
42
43 % next, reconstruct waveform based on the sorted beat
44 % smooth the sorted beat
45 % fit a polynomial or sinusoid over time - NEXT
46 subplot(4,1,1)
47 surf(input_data)
48 title('Input Data')
49
50 subplot(4,1,2)
51 surf(tt, 1:num_theta, inputsorted)
52 title('Input Data Sorted')
53
54 % perform FFTs of polynomial coefficients
55 parraysorted = Out.PP.pArray(:,inds);
56 subplot(4,1,3)
57 surf(parraysorted)
58 title('Polynomial coefficients sorted using Out.PP.pArray')
59 fp = fft(parraysorted,[],2);
60 fp0 = fp;
61
62 % get rid of higher harmonics ( > nh/period)
63 nh = 3; % number of harmonics
64 fp0(:,nh+2:len-nh) = 0; % keep first and last elements of FFT
65 p0 = ifft(fp0,[],2); % should be purely real
66
67 % reconstruct waveforms
68 for n = 1:len
69     q(:,n) = polyval(p0(:,n),Out.PP.s2);
70 end
71

```

```

72 subplot(4,1,4)
73 surf(q)
74 title('Reconstructed waveform after taking FFT of polynomial coefficients')
75 shading interp
76
77 %% %%
78 % Analysis section
79
80 L = Out.length *10^-6;
81 numpoints = 60;
82 nframes = Out.Stats.numFrames;
83 h = ((0:60)./60)*Out.length*10)/Out.length;
84 h = round(h*100)/100;
85
86 % PVB 2021 1207 replace framespersec with freq
87 % prompt = 'number of frames per sec: ';
88 % framespersec = input(prompt);
89 % prompt = 'Beat frequency (Hz): ';
90 % beatfreq = input(prompt);
91 beatfreq = Out.PP.freq;
92
93 %orientation of hooke on sperm (CW or CCW)
94 prompt = 'Is it CW? Y/N [Y]: ';
95 str = input(prompt, 's');
96 if str == 'Y'
97     q = -1*q;
98     %     kappaRecon = -1*kappaRecon;
99 end
100 %get x and y coordinates of theta
101 sinVals = sin(q);
102 cosVals = cos(q);
103
104 % PVB 2021 1207 moved these lines up
105 numpoints = 60;
106 leachseg = L/numpoints;
107 xVals = cumtrapz(cosVals)*leachseg;
108 yVals = cumtrapz(sinVals)*leachseg;
109

```

```

110 % PVB 2021 1207 addition of Dt
111 %     [dxdt,-] = gradient(xVals);
112 %     [dydt,-] = gradient(yVals);
113 beatT = (1/beatfreq);           % period of "reconstructed" beat
114 Dt = beatT/nframes;           % Dt - time step of reconstructed beat (sec)
115 TT = Dt*(1:n);                 % time vector
116 [dxdt,-] = gradient(xVals,Dt); % units are now microns/sect
117 [dydt,-] = gradient(yVals,Dt);
118
119 Vx = dxdt;
120 Vy = dydt;
121
122 %normal and tangent vectors
123 Tx = cos(q);
124 Ty = sin(q);
125 Nx = -sin(q);
126 Ny = cos(q);
127
128 %finding normal and tangent velocity vectors
129 Vnormalx = Vx.*Nx;
130 Vnormaly = Vy.*Ny;
131 Vtanx = Vx.*Tx;
132 Vtany = Vy.*Ty;
133 Vn = Vnormalx+Vnormaly;
134 Vt = Vtanx+Vtany;
135
136 %coefficients
137 %friction coefficient normal = 3.4*10^-3
138 %parallel is half of normal
139 %finding force in normal and tangent directions
140 Cn = 0.0034;
141 Ct = Cn/2;
142 Fn = Vn*Cn;
143 Ft = Vt*Ct;
144
145 %Force
146 Fx = Fn.*Nx + Ft.*Tx;
147 Fy = Fn.*Ny + Ft.*Ty;

```

```

148
149 fmag = sqrt(Fx.^2+Fy.^2);%get x and y components and add them separately
150 avgfmag = mean(sum(fmag,1)*leachseg)
151 % PVB 2021 1207 added segment length (leachseg) to integral
152 % Forceateachtimex = sum(Fx,1);
153 Forceateachtimex = sum(Fx,1)*leachseg;
154 % Forceateachlengthx = sum(Fx,2);
155 % PVB 2021 1207 added segment length (leachseg) to integral
156 % Forceateachtimey = sum(Fy,1);
157 Forceateachtimey = sum(Fy,1)*leachseg;
158 % Forceateachlengthy = sum(Fy,2);
159
160 % Average force over time
161 avgTotalForcethrougtimex = mean(Forceateachtimex);
162 % avgTotalForceeachlength = mean(Forceateachlengthx);
163 avgTotalForcethrougtimey = mean(Forceateachtimey);
164 % avgTotalForceeachlengthy = mean(Forceateachlengthy);
165
166 figure(8)
167 plot(TT,Forceateachtimex);
168 title('Total Force Exerted by Flagellum Over Time x direction')
169 % newLim = get(gca,'XLim');
170 % newx = linspace(newLim(1), newLim(2),8);
171 % set(gca,'xticklabel', round(newx*(1/15)*100)/100);
172 xlabel('Time [s]')
173 ylabel('Force [N]')
174 annotation('textbox', [0.60, 0.8, 0.1, 0.1], 'String', "Avg Total Force = " + ...
    avgTotalForcethrougtimex)
175
176 % figure(7)
177 % plot(Forceateachlengthx);
178 % set(gca,'xticklabel',(h));
179 % title('Total Force Exerted Over Normalized Length of Flagellum x direction')
180 % xlabel('Normalized Length')
181 % ylabel('Force [N]')
182 % annotation('textbox', [0.60, 0.1, 0.1, 0.1], 'String', "Avg Total Force ...
    = " + avgTotalForceeachlengthx)
183

```

```

184 figure(9)
185 plot(TT,Forceateachtimey);
186 title('Total Force Exerted by Flagellum Over Time y direction')
187 % newLim = get(gca,'XLim');
188 % newx = linspace(newLim(1), newLim(2),8);
189 % set(gca,'xticklabel', round(newx*(1/15)*100)/100);
190 xlabel('Time [s]')
191 ylabel('Force [N]')
192 annotation('textbox', [0.60, 0.8, 0.1, 0.1], 'String', "Avg Total Force = " + ...
    avgTotalForcethrougtimey)
193
194 % figure(10)
195 % plot(Forceateachlengthy);
196 % set(gca,'xticklabel',(h));
197 % title('Total Force Exerted Over Normalized Length of Flagellum y direction')
198 % xlabel('Normalized Length')
199 % ylabel('Force [N]')
200 % annotation('textbox', [0.60, 0.1, 0.1, 0.1], 'String', "Avg Total Force ...
    = " + avgTotalForceeachlengthy)
201
202 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
203 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
204 % Power calculation
205 % PVB 2021 1207 added the lenght element (leachseg) to integral
206 POWER = (Fn.*Vn+Ft.*Vt); % Power per unit length at each segment
207 % Could also used POWER = Fx.*Vx + Fy.*Vy; % should be the same
208
209 powerateachtime = sum(POWER,1)*leachseg;
210 %powerateachlength = sum(POWER,2);
211 TotalavgPowertime = mean(powerateachtime);
212 % totalavgPowerlength = mean(powerateachlength);
213
214 figure(11)
215 plot(TT,powerateachtime);
216 %0.0640
217 title('Total Power Exerted by Flagellum Over Time');
218 % newLim = get(gca,'XLim');
219 % newx = linspace(newLim(1), newLim(2),8);

```



```

220 % % PVB 2021 1207 not sure but replacing framespersec with beatfreq
221 % % set(gca,'xticklabel', round(newx*(1/framespersec)*100)/100);
222 % set(gca,'xticklabel', round(newx*(1/beatfreq)*100)/100);
223
224 xlabel('Time [s]'); %frames per second 15.6131575
225 ylabel('Power [W]');
226 annotation('textbox', [0.60, 0.8, 0.1, 0.1], 'String', "Avg Total Power = " + ...
    TotalavgPowertime)
227
228 %     figure(12)
229 %     plot(powerateachlength);
230 %     set(gca,'xticklabel',(h));
231 %     title('Total Power Exerted Over Normalized Length of Flagellum');
232 %     xlabel('Normalized Length');
233 %     ylabel('Power [W]');
234 %     annotation('textbox', [0.60, 0.1, 0.1, 0.1], 'String', "Avg
235
236 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
237 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
238
239 % PVB 2021 1207 moved the length multiplier to integral
240 %TORQUE
241 Torque = (Fy.*xVals - Fx.*yVals);
242 %     avgTorquelength = sum(Torque,2)
243 %     avgavgtorquel = mean(avgTorquelength)
244 avgTorquetime = sum(Torque,1)*leachseg;
245 avgavgtorquet = mean(avgTorquetime);
246 %     figure(4)
247 %     plot(avgTorquelength)
248 %     set(gca,'xticklabel',(h));
249 %     title('Total Torque Exerted Over Normalized Length of Flagellum')
250 %     xlabel('Normalized Length');
251 %     ylabel('Torque [Nm]');
252 %     annotation('textbox', [0.60, 0.1, 0.1, 0.1], 'String', "Avg Torque = " + ...
    avgavgtorquel)
253 %
254 figure(13)
255 plot(TT, avgTorquetime)

```

```

256 % newLim = get(gca,'XLim');
257 % newx = linspace(newLim(1), newLim(2),8);
258 % % PVB 2021 1207 not sure but replacing framespersec with beatfreq
259 % % set(gca,'xticklabel', round(newx*(1/framespersec)*100)/100);
260 % set(gca,'xticklabel', round(newx*(1/beatfreq)*100)/100);
261 title('Total Torque Exerted by Flagellum Over Time')
262 xlabel('Time [s]');
263 ylabel('Torque [Nm]');
264 annotation('textbox', [0.60, 0.1, 0.1, 0.1], 'String', "Avg Torque = " + ...
    avgavgtorquet)
265
266 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
267 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
268 % % WORK
269 % % t = [1:nframes];
270 % TotalWork = trapz(TT,powerateachtime);
271 TotalWork = trapz(powerateachtime)*Dt;
272
273 intofpateachtime = cumtrapz(powerateachtime)*Dt;
274 %intofpateachlength = cumtrapz(powerateachlength);
275
276 avgWorkateachtime = mean(intofpateachtime);
277 %avgWorkateachlength = mean(intofpateachlength);
278
279 figure(2)
280 plot(TT,intofpateachtime)
281 title('Total Work Done by Flagellum Over Time')
282 % newLim = get(gca,'XLim');
283 % newx = linspace(newLim(1), newLim(2),8);
284 % % PVB 2021 1207 not sure but replacing framespersec with beatfreq
285 % % set(gca,'xticklabel', round(newx*(1/framespersec)*100)/100);
286 % set(gca,'xticklabel', round(newx*(1/beatfreq)*100)/100);
287
288 xlabel('Time [s]');
289 ylabel('Work [J]');
290 annotation('textbox', [0.60, 0.8, 0.1, 0.1], 'String', "Avg Total Work = " + ...
    avgWorkateachtime)
291 %

```

```

292 % figure(1)
293 % plot(intofpateachlength)
294 % set(gca,'xticklabel',(h));
295 % title('Total Work Done Over Normalized Length of Flagellum')
296 % xlabel('Normalized Length');
297 % ylabel('Work [J]');
298 % annotation('textbox', [0.60, 0.1, 0.1, 0.1], 'String', "Avg Total Work = " + ...
    avgWorkateachlength);
299
300 %%
301
302 if MOVIEYES,
303     loops = num_frames;
304     %loops = 30; %display first 30 frames
305     M(loops) = struct('cdata',[],'colormap',[]);
306
307     h = figure;
308     h.Visible = 'off';
309     for j = 1:loops
310         plot(Out.Data.xArray(:,j),Out.Data.yArray(:,j))
311         drawnow
312         M(j) = getframe;
313     end
314     h.Visible = 'on';
315
316     movie(M,1,3);
317     %%
318
319     loops = num_frames;
320     %loops = 30; %display first 30 frames
321     M(loops) = struct('cdata',[],'colormap',[]);
322
323     h = figure;
324     h.Visible = 'off';
325     for j = 1:loops
326         plot(xVals(:,j),yVals(:,j))
327         drawnow
328         M(j) = getframe;

```

```

329     end
330     h.Visible = 'on';
331
332     movie(M,1,3);
333
334 end;

1 % RUn isomap to organize data int a closed cycle
2 % A Gupte PVB 2021 1207
3 %
4 clear;
5 %load Out1b.mat
6 %load Out2a.mat
7 %load Out2b.mat
8 %load Out3a.mat
9 %load Out3b.mat
10 %load Out4a.mat
11 %load Out5a.mat
12 %load Out5b.mat
13 %load Out6a.mat
14 %load Out6b.mat
15 %load Out7a.mat
16 %load Out8a.mat
17 %load Out9a.mat
18 %load Out9b.mat
19 %load Out10a.mat
20 load Out11b.mat
21
22 options.dims = 1:10;
23 options.verbose = false;
24 options.overlay =true;
25 num_neighbors =3; % this is a hyper parameter and changing this gives ...
    different embedding result
26
27 [num_points, num_frames] = size(Out.Data.xArray)
28 [num_theta, num_theta_frames] = size(Out.Data.thetaArray)
29

```

```
30 % Using vector of theta
31
32 input_data = Out.Data.thetaArray(:, :);
33 D = L2_distance(input_data(:, :), input_data(:, :), 1);
34
35 % PVB 2021 1207
36 % use distance criterion
37 eps = 1.5;      % choose to make simple closed curve, if periodic beating
38 [Y,R] = Isomap(D, 'epsilon', eps, options);
39
40 %alternave us number criterion
41 %[Y,R] = Isomap(D, 'k', num_neighbors, options);
42
43
44 figure;
45 plot(Out.Data.xArray, Out.Data.yArray)
46 title("Plot of Input Data")
```