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## Supplementary Text S1

## Literature Review

To assess the extent of awareness of trait repeatability as an important source of bias in estimates of selection, and the type of estimates that might often be biased, we surveyed the literature for papers presenting estimates of selection. We decided to take a sample of all such estimates by focusing on papers published within the journal Evolution in the years 2010-2019 inclusive. Our strategy was first to identify all papers published in that time period that cited Lande \& Arnold (1983). These were then pruned by skimming abstracts to assess if selection gradients of empirical data were likely to be presented. We then retrieved each paper and read the methods and results to confirm that gradients were indeed estimated. If so, we assessed the following variables: the trait(s) that were analysed, labelled as the authors chose and scored as to type (morphological, life history, physiological, performance, or behavioural) because repeatability varies considerably among these classes of traits. We used information in the methods to assess whether traits were mean-centred prior to analysis and whether repeated measures of the trait were taken (and if so, how many repeats). We further scored whether the authors used individual values, the mean, or some other technique such as principal components analysis that combines individual data points (and mean-centres as well), and whether trait correlations were presented in analyses of correlational selection. We also noted if the author(s) mentioned measurement error and repeatability in the paper, and if so, if they specified the trait repeatability. Finally, we noted what type of selection was estimated (directional, quadratic, or correlational) and any unusual elements of the analysis beyond the standard regression approach described by Lande \& Arnold (1983), such as use of path analysis, linear mixed models, aster analysis, or bivariate mixed-effects models.

Our survey resulted in 68 papers producing 311 trait estimates (we did not count replicate populations or years). Most estimates were on morphological traits ( $195 ; 63 \%$ ), but $38(12 \%)$ were of behavioural traits, $26(8 \%)$ of physiological, 31 ( $10 \%$ ) were of life history characters, and $21(7 \%)$ of performance traits. All traits were used to estimate directional selection; quadratic selection was also measured for $178(57 \%)$, and correlational selection was assessed among 107 (34\%). Table 1 (Main Text) provides summary statistics over all papers and Table S1 provides information extracted per paper.

Table S1. Studies publishing estimates of linear and nonlinear selection in Evolution from 2010 -2019, with species, trait studied, category of trait (MO=morphological, BEH = Behavioral, LH = Life history, PHY = Physiological, PER = Performance), fitness measure (L = lifetime, typically survival; $\mathrm{E}=$ one measure of an episode of fitness; $\mathrm{E} 2=$ at least two measures of episodic fitness), number of measures taken, whether the mean was used if more than 1 measure (or if $\geq 2$ traits were combined with PCA), whether repeatability was mentioned and its magnitude if known, type of selection measured ( $\mathrm{D}=$ directional, $\mathrm{Q}=$ quadratic, $\mathrm{C}=$ correlational), whether multivariate models were used, if traits were mean-centred before analysis (? = either authors did not say or simply stated they "standardized" without defining; residuals and PCA were counted as mean-centred) and if among-trait correlations were provided in cases of non-linear selection. Entries left blank if non-applicable.

| Authors | Year | Citation | Species | Trait | Category | Fitness | Measures | Used mean | Mentioned repeatability | Type of selection measured | Used multivariate | Traits mean-centred | Trait correlations estimated |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Reynolds et al. | 2010 | 64(2): 358-369 | Silene virginica | Petal length | MO | L | $2+$ | Yes | No | D,Q,C | No | ? | No |
|  |  |  |  | Petal width | MO | L | $2+$ | Yes | No | D,Q,C | No | ? | No |
|  |  |  |  | Flower height | MO | L | $2+$ | Yes | No | D,Q,C | No | ? | No |
|  |  |  |  | Corolla length | MO | L | $2+$ | Yes | No | D,Q,C | No | ? | No |
|  |  |  |  | Corolla width | MO | L | $2+$ | Yes | No | D, Q, C | No | ? | No |
|  |  |  |  | Stigma exertion | MO | L | $2+$ | Yes | No | D, Q, C | No | ? | No |
| van de Pol et al. | 2010 | 64(3):836-851 | Haematopus ostralegus ostralegus | Bill shape | MO | E | 1 |  | Yes | D | No | No |  |
| Cox \& Calsbeek | 2010 | 64(3):798-809 | Anolis sagrei | Body size | MO | L | 1 |  | No | D, Q | No | ? | No |
| Siepelski \& Benkman | 2010 | $\begin{gathered} 64(4): 1120- \\ 1128 \end{gathered}$ | Pinus flexilis | PC1 | MO | E | 2 | Yes | Yes | D | No | PCA |  |
| Freeman-Gallant et al | 2010 | $\begin{gathered} 64(4): 1007- \\ 1017 \end{gathered}$ | Geothlypis trichas | UV brightness | MO | E | 4 | Yes | No | D | No | Yes |  |
|  |  |  |  | Mask area | mo | E | 4 | Yes | 0.9 | D | No | Yes |  |
|  |  |  |  | Bib area | мо | E | 1 |  | 0.9 | D | No | Yes |  |
|  |  |  |  | Carotenoid chroma | мо | E | 4 | Yes | No | D | No | Yes |  |
|  |  |  |  | Yellow brightness | мо | E | 4 | Yes | No | D | No | Yes |  |
| Weese et al. | 2010 | $\begin{gathered} 64(6): 1802- \\ 1815 \end{gathered}$ | Poecilia reticulata | Body size | MO | L | 1 |  | No | D | No | Yes |  |
|  |  |  |  | Black | mo | L | 1 |  | No | D | No | Yes |  |
|  |  |  |  | Green | мо | L | 1 |  | No | D | No | Yes |  |
|  |  |  |  | Carotenoid | мо | L | 1 |  | No | D | No | Yes |  |
|  |  |  |  | Structural | мо | L | 1 |  | No | D | No | Yes |  |
|  |  |  |  | Total Color | MO | L | 1 |  | No | D | No | Yes |  |
| Perez \& Munch | 2010 | $\begin{gathered} 64(8): 2450- \\ 2457 \end{gathered}$ | Fish sp. | Body size | MO | L | ? |  | No | D,Q,C | No | Yes | No |
|  |  |  |  |  |  | E |  |  |  |  | No | Yes | No |
|  |  |  |  | Bower base | BEH | E | 1 |  | No | D, Q, C | No | Yes | No |
|  |  |  |  | Bower platform | BEH | E | 1 |  | No | D, Q, C | No | Yes | No |
|  |  |  |  | Bower position | BEH | E | 1 |  | No | D,Q, ${ }^{\text {d, }}$ | No | Yes | No |
| Baythavong \& Stanton | 2010 | $\begin{gathered} 64(10): 2904- \\ 2920 \end{gathered}$ | Erodium cicutarium | Emergence timing MP | LH | L | 6 |  | No | D | No | ? | No |


|  |  |  |  | Emergence timing L | LH | L | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Emergence timing Q | LH | L | 6 |
|  |  |  |  | Cotyledon width MP | MO | L | 6 |
|  |  |  |  | Cotyledon width L | MO | L | 6 |
|  |  |  |  | Cotyledon width Q | MO | L | 6 |
|  |  |  |  | Early leaf number MP | MO | L | 6 |
|  |  |  |  | Early leaf number L | MO | L | 6 |
|  |  |  |  | Early leaf number Q | MO | L | 6 |
|  |  |  |  | Leaf turnover MP | MO | L | 6 |
|  |  |  |  | Leaf turnover L | MO | L | 6 |
|  |  |  |  | Leaf turnover Q | MO | L | 6 |
|  |  |  |  | FFdateMP | MO | L | 6 |
|  |  |  |  | Ffdate L | MO | L | 6 |
|  |  |  |  | Ffdate Q | MO | L | 6 |
|  |  |  |  | Leaves MP | MO | L | 6 |
|  |  |  |  | Leaves L | MO | L | 6 |
|  |  |  |  | Leaves Q | MO | L | 6 |
| Sullivan-Beckers \& Cocroft | 2010 | $\begin{gathered} 64(11): 3158- \\ 3171 \end{gathered}$ | Enchenopa binotata | Survival | LH | E | 1 |
|  |  |  |  | Weight | MO | E | 1 |
|  |  |  |  | Signals per bout | BEH | E | 1 |
|  |  |  |  | Period | BEH | E | 1 |
|  |  |  |  | Whine length | BEH | E | 1 |
|  |  |  |  | Pulse rate | BEH | E | 1 |
|  |  |  |  | Frequency | BEH | E | 1 |
| Rundle \& Chenowth | 2011 | 65(3):893-899 | Drosophila serrata | CHC1 | PHY | E | 1 |
|  |  |  |  | CHC2 | PHY | E | 1 |
|  |  |  |  | CHC3 | PHY | E | 1 |
|  |  |  |  | CHC4 | PHY | E | 1 |
|  |  |  |  | CHC5 | PHY | E | 1 |
|  |  |  |  | CHC6 | PHY | E | 1 |
|  |  |  |  | CHC7 | PHY | E | 1 |
|  |  |  |  | CHC8 | PHY | E | 1 |
|  |  |  |  | CHC9 | PHY | E |  |
| Sahli \& Conner | 2011 | $\begin{gathered} 65(5): 1457- \\ 1473 \end{gathered}$ | Raphanus raphanistrum | Flower number | MO | E2 |  |
|  |  |  |  | Flower size | мо | E2 |  |
|  |  |  |  | Anther exsertion | MO | E2 |  |
|  |  |  |  | Stamen dimorphism | мо | E2 | 1 |
| Postma et al. | 2011 | $\begin{gathered} 65(8): 2145- \\ 2156 \end{gathered}$ | Poecilia reticulata | Black patch size | MO | E |  |
|  |  |  |  | Fuzzy black size | мо | E |  |
|  |  |  |  | Orange size | мо | E |  |


|  |  |  |  | Iridescent size | MO | E | 1 |  | No | D,Q,C | No | ? | Yes |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Tail size | MO | E | 1 |  | No | D,Q,C | No | ? | Yes |
|  |  |  |  | Body size | мо | E | 1 |  | No | D,Q,C | No | ? | Yes |
| Martin \& Pfennig | 2011 | $\begin{gathered} 65(10): 2946- \\ 2958 \end{gathered}$ | Spea multiplicata | Denticle rows | MO | E | 1 |  | No | D,Q,C | No | Yes(residuals) | No |
|  |  |  |  | Orbitohyoideus muscle width | MO | E | 1 |  | No | D,Q,C | No | Yes(residuals) | No |
|  |  |  |  | Interhyodieus muscle width | MO | E | 1 |  | No | D,Q,C | No | Yes(residuals) | No |
|  |  |  |  | Gut length | мо | E | 1 |  | No | D,Q,C | No | Yes(residuals) | No |
|  |  |  |  | Mouthpart shape | мо | E | 1 |  | No | D,Q,C | No | Yes(residuals) | No |
|  |  |  |  | Denticle rows | mo | E | 1 |  | No | D,Q,C | No | Yes(residuals) | No |
| Leinonen et al. | 2011 | $\begin{gathered} 65(10): 2916- \\ 2926 \end{gathered}$ | Gasterosteus aculeatus | Lateral plate number | MO | L | 1 |  | No | D | No | No | Yes |
|  |  |  |  | Spine triangle size | мо | L | 1 |  | No | D | No | No | Yes |
|  |  |  |  | Head depth | MO | L | 1 |  | No | D | No | No | Yes |
|  |  |  |  | Head length | MO | L | 1 |  | No | D | No | No | Yes |
|  |  |  |  | Body depth | MO | L | 1 |  | No | D | No | No | Yes |
|  |  |  |  | Pelvic girdle length | MO | L | 1 |  | No | D | No | No | Yes |
|  |  |  |  | Caudal peduncle length | MO | L | 1 |  | No | D | No | No | Yes |
| Formica et al. | 2011 | $\begin{gathered} 65(10): 2771- \\ 2781 \end{gathered}$ | Bolitotherus cornutus | Body Size (PC1) | MO | L | 5 | PCA | No | D | No | PCA |  |
|  |  |  |  | Social Body Size | MO | L | 10+ | Yes | No | D | No | PCA |  |
|  |  |  |  | Body Size (PC1) | MO | E | 5 | PCA | No | D | No | PCA |  |
|  |  |  |  | Social Body Size | MO | E | $10+$ | Yes | No | D | No | PCA |  |
| Crean et al. | 2011 | $\begin{gathered} 65(11): 3079- \\ 3089 \end{gathered}$ | Styela plicata | Larval size | MO | L | 3 | Yes | No | D,Q,C | No | Yes | No |
|  |  |  |  | Hatch time | LH | L | 1 |  | No | D,Q,C | No | Yes | No |
|  |  |  |  | Settle time | BEH | L | 1 |  | No | D,Q,C | No | Yes | No |
|  |  |  |  | Larval size | MO | E | 3 | Yes | No | D,Q,C | No | Yes | No |
|  |  |  |  | Hatch time | LH | E | 1 |  | No | D,Q,C | No | Yes | No |
|  |  |  |  | Settle time | BEH | E | 1 |  | No | D, Q, C | No | Yes | No |
| Lorenzi \& Thompson | 2011 | $\begin{gathered} 65(12) \text { ):3527- } \\ 3542 \end{gathered}$ | Polistes biglumis | Head width | MO | L | 1 |  | No | D,Q | No | ? | Yes |
|  |  |  |  | Building effort | PER | L | 1 |  | No | D, Q | No | ? | Yes |
|  |  |  |  | Brood investment | PER | L | 1 |  | No | D, Q | No | ? | Yes |
|  |  |  |  | Protective effort | BEH | L | 1 |  | No | D, Q | No | ? | Yes |
| Egan et al. | 2011 | $\begin{gathered} \text { 65(12):3543- } \\ 3557 \end{gathered}$ | Belonocnema treatae | Gall size | MO | L | 1 |  | No | D, Q | No | Yes |  |
| Kulbaba et al. | 2012 | $\begin{gathered} 66(5): 1344- \\ 1359 \end{gathered}$ | Polemonium brandegeei | Herkegomy | MO | E | 1 |  | No | D,Q,C | No | ? | No |
|  |  |  |  | Corolla tube length | мо | E | 1 |  | No | D,Q,C | No | ? | No |
|  |  |  |  | Corolla tube width | MO | E | 1 |  | No | D,Q,C | No | ? | No |
|  |  |  |  | Sex organ height | MO | E | 1 |  | No | D,Q,C | No | ? | No |
|  |  |  |  | Flower mass | MO | E | 1 |  | No | D, Q, C | No | ? | No |
|  |  |  |  |  |  |  | 4 |  |  |  |  |  |  |


|  |  |  |  | Nectar volume Sugar content | $\begin{aligned} & \text { PHY } \\ & \text { PHY } \end{aligned}$ | E | 1 2 | Yes | $\begin{aligned} & \text { No } \\ & \text { No } \end{aligned}$ | $\begin{aligned} & \mathrm{D}, \mathrm{Q}, \mathrm{C} \\ & \mathrm{D}, \mathrm{Q}, \mathrm{C} \end{aligned}$ | No No | $\begin{aligned} & ? \\ & ? \end{aligned}$ | No No |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Godsen et al. | 2012 | $\begin{gathered} 66(7): 2106- \\ 2116 \end{gathered}$ | Drosophila melanogaster | CHC1 | PHY | E | 1 |  | No | D | No | Yes | No |
|  |  |  |  | CHC2 | PHY | E | 1 |  | No | D | No | Yes | No |
|  |  |  |  | СНС3 | PHY | E | 1 |  | No | D | No | Yes | No |
|  |  |  |  | CHC4 | PHY | E | 1 |  | No | D | No | Yes | No |
|  |  |  |  | CHC5 | PHY | E | 1 |  | No | D | No | Yes | No |
|  |  |  |  | CHC6 | PHY | E | 1 |  | No | D | No | Yes | No |
|  |  |  |  | CHC7 | PHY | E | 1 |  | No | D | No | Yes | No |
| Fitzpatrick et al. | 2012 | $\begin{gathered} 66(8): 2451- \\ 2460 \end{gathered}$ | Mytilus galloprovincialis | Sperm density | PER | E | 2 | Yes |  | D,Q,C | No | ? | No |
|  |  |  |  | Sperm head volume | MO | E | 30 | Yes |  | D, Q, C | No | ? | No |
|  |  |  |  | Sperm flagellum length | MO | E | 30 | Yes |  | D, Q, C | No | ? | No |
|  |  |  |  | Sperm motility PC1 | PER | E | 2 | Yes | Yes | D, Q, C | No | PCA | No |
|  |  |  |  | Sperm motility PC2 | PER | E | 2 | Yes | Yes | D, Q, C | No | PCA | No |
|  |  |  |  | Sperm age | PER | E | 1 |  | No | D, Q, C | No | ? | No |
|  |  |  |  | Egg age | PER | E | 1 |  | No | D, Q, C | No | ? | No |
| Guerreiro et al | 2012 | $\begin{gathered} 66(11): 3615- \\ 3623 \end{gathered}$ | Mus musculus | IL-6 | PHY | L | 1 |  | No | D,Q,C | No | Yes | No |
|  |  |  |  | $11-10$ | PHY | L | 1 |  | No | D, Q, C | No | Yes | No |
| Benkman et al | 2013 | 67(1):157-169 | Pinus contorta latifolia | Cone width/length | MO | E | 3 | Yes | Yes | D, Q | No | No | Yes |
|  |  |  |  | Cone mass | MO | E | 3 | Yes | Yes | D, Q | No | No | Yes |
|  |  |  |  | Distal scale | MO | E | 6 | Yes | Yes | D, Q | No | No | Yes |
|  |  |  |  | Scale length | MO | E | 6 | Yes | Yes | D,Q | No | No | Yes |
|  |  |  |  | Full seeds | PER | E | 3 | Yes | Yes | D,Q | No | No | Yes |
|  |  |  |  | Empty seeds | PER | E | 3 | Yes | Yes | D, Q | No | No | Yes |
|  |  |  |  | Seed mass | MO | E | 5 | Yes | Yes | D,Q | No | No | Yes |
| Marshall \& Monro | 2013 | 67(2):328-337 | Watersipora subtorquata | Offspring size | MO | E | 1 |  | No | D, Q | No | ? | No |
|  |  |  |  | Zoiod size | MO | E | 1+ | Yes | No | D, Q | No | ? | No |
|  |  |  |  | Senescence size | MO | E | 1 |  | No | D,Q | No | ? | No |
| Wacker et al. | 2013 | $\begin{gathered} 67(7): 1937- \\ 1949 \end{gathered}$ | Gobiusculus flavescens | Length | MO | E | 3 | Yes | Yes | D | No | Yes |  |
|  |  |  |  | Torso area | MO | E | 3 | Yes | Yes | D | No | Yes |  |
|  |  |  |  | Blue spots | MO | E | 3 | Yes | Yes | D | No | Yes |  |
|  |  |  |  | Tail length | MO | E | 3 | Yes | Yes | D | No | Yes |  |
| Fritzsche \& Arnqvist | 2013 | $\begin{gathered} 67(7): 1926- \\ 1936 \end{gathered}$ | Callosobruchus maculatus | Male body size | MO | E | 2 | Yes | No | D | No | Yes |  |
|  |  |  |  | Male body size | MO | E | 2 | Yes | No | D | No | Yes |  |
|  |  |  |  | Male body size | MO | E | 2 | Yes | No | D | No | Yes |  |
|  |  |  |  | Male body size | MO | E | 2 | Yes | No | D | No | Yes |  |
|  |  |  |  | Female body size | MO | E | 2 | Yes | No | D | No | Yes |  |
|  |  |  |  | Female body size | MO | E | 2 | Yes | No | D | No | Yes |  |
|  |  |  |  | Female body size | MO | E | 2 | Yes | No | D | No | Yes |  |
|  |  |  |  | Female body size | MO | E | 2 | Yes | No | D | No | Yes |  |
|  |  |  |  |  |  |  | 5 |  |  |  |  |  |  |


| Morrissey \& Sakrejda | 2013 | $\begin{gathered} \text { 67(7): } 2094- \\ 2100 \end{gathered}$ | Homo sapiens | Birth mass | MO | E | 1 |  | No | D, Q, C | No | ? | No |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Gestation length | LH | E | 1 |  | No | D,Q,C | No | ? | No |
| Kulbaba\&Worley | 2013 | $\begin{gathered} 67(8): 2194- \\ 2206 \end{gathered}$ | Polemonium brandegeei | Nectar conc | PER | E | 2 | Yes | No | D,Q | No | Yes | No |
|  |  |  |  | Tube length | MO | E | 2 | Yes | No | D,Q | No | Yes | No |
|  |  |  |  | Tube diameter | MO | E | 2 | Yes | No | D, Q | No | Yes | No |
|  |  |  |  | Herkogamy | MO | E | 2 | Yes | No | D, Q | No | Yes | No |
|  |  |  |  | Bird visits | PER | E | 2 | Yes | No | D, Q | No | Yes | No |
|  |  |  |  | Pollen in anthers | PER | E | 2 | Yes | No | D, Q | No | Yes | No |
|  |  |  |  | Pollen on stigma | PER | E | 2 | Yes | No | D,Q | No | Yes | No |
|  |  |  |  | Seeds set | PER | E | 2 | Yes | No | D, Q | No | Yes | No |
|  |  |  |  | Seeds sired | PER | E | 2 | Yes | No | D,Q | No | Yes | No |
| Mezquida \& Benkman | 2014 | $\begin{gathered} 68(6): 1710- \\ 1721 \end{gathered}$ | Pinus uncinata | Cone mass | MO | E | 4 | Yes | No | D | No | Yes |  |
|  |  |  |  | Full seeds | PER | E | 4 | Yes | No | D | No | Yes |  |
|  |  |  |  | Empty seeds | PER | E | 4 | Yes | No | D | No | Yes |  |
|  |  |  |  | Seed mass | MO | E | 4 | Yes | No | D | No | Yes |  |
| Sletvold \& Agren | 2014 | $\begin{gathered} 68(7): 1907-1918 \\ 1918 \end{gathered}$ | Dactylorhiza lapponica | Height | MO | E | 1 |  | No | D | No | ? |  |
|  |  |  |  | Num Flowers | MO | E | 1 |  | No | D | No | ? |  |
|  |  |  |  | Corolla size | мо | E | 1 |  | No | D | No | ? |  |
|  |  |  |  | Spur length | мо | E | 1 |  | No | D | No | ? |  |
|  |  |  |  | Flowering day | LH | E | 1 |  | No | D | No | ? |  |
| Gillespie et al | 2014 | $\begin{gathered} 68(12): 3421- \\ 3432 \end{gathered}$ | Narnia femorata | Male body size (PC) | MO | E | 7 | PCA | No | D | No | PCA |  |
|  |  |  |  | Female body size (PC) | мо | E | 7 | PCA | No | D | No | PCA |  |
| Ercit \& Gwynne | 2015 | 69(2):419-430 | Oecanthus nigricornis | Tegmen width | MO | L | 1 |  | No | D,Q,C | No | ? | No |
|  |  |  |  | Leg size (PC1) | мо | L | 3 | PCA | No | D,Q,C | No | PCA | No |
|  |  |  |  | Pronotum length | мо | L | 1 |  | No | D,Q,C | No | ? | No |
|  |  |  |  | Head width | мо | L | 1 |  | No | D,Q,C | No | ? | No |
|  |  |  |  | Tegmen width | мо | E | 1 |  | No | D,Q,C | No | ? | No |
|  |  |  |  | Leg size (PC1) | MO | E | 3 | PCA | No | D,Q,C | No | PCA | No |
|  |  |  |  | Pronotum length | мо | E | 1 |  | No | D,Q,C | No | ? | No |
|  |  |  |  | Head width | MO | E | 1 |  | No | D, Q, C | No | ? | No |
| Campobello et al. | 2015 | 69(4):916-925 | Falco naumanni | Individual attendance | BEH | E | 1 |  | No | D | No | Yes |  |
|  |  |  | Corvus Monedula | Individual attendance | BEH | E | 1 |  | No | D | No | Yes |  |
|  |  |  | Falco naumanni | Conspecific attendance | BEH | E | >2 | Yes | No | D | No | Yes |  |
|  |  |  | Corvus Monedula | Conspecific attendance | BEH | E | >2 | Yes | No | D | No | Yes |  |
|  |  |  | Falco naumanni | Heterospecific attendance | BEH | E | >2 | Yes | No | D | No | Yes |  |
|  |  |  | Corvus Monedula | Heterospecific attendance | BEH | E | >2 | Yes | No | D | No | Yes |  |
| Weis et al. | 2015 | $\begin{gathered} 69(6): 1361- \\ 1374 \end{gathered}$ | Brassica rapa | Emergence time | LH | L | 1 |  | No | D | No | Yes |  |
|  |  |  |  |  |  |  | 6 |  |  |  |  |  |  |




| Kalvnes et al. | 2017 | $\begin{gathered} \text { 71(8): } 2062- \\ 2079 \end{gathered}$ | Passer domesticus | Tarsus | MO | L | 1 |  | No | D | No | Yes | Yes |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Wing | мо | L | 1 |  | No | D | No | Yes | Yes |
|  |  |  |  | Bill length | мо | L | 1 |  | No | D | No | Yes | Yes |
|  |  |  |  | Bill depth | мо | L | 1 |  | No | D | No | Yes | Yes |
|  |  |  |  | Condition | мо | L | 1 |  | No | D | No | Yes | Yes |
| O'Brien et al. | 2017 | $\begin{gathered} 71(11): 2584- \\ 2598 \end{gathered}$ | Sagra femorata | Hind leg length | MO | E | 1 |  | No | D,Q,C | No | ? | Yes |
|  |  |  |  | Elytra length | MO | E | 1 |  | No | D,Q,C | No | ? | Yes |
|  |  |  |  | Residual leg length to elytra | MO | E | 1 |  | No | D,Q,C | No | Yes | NA |
| McCollough et al | 2018 | 72(4):893-905 | Onthophagus taurus | Testes mass | MO | E | 1 |  | No | D,Q,C | No | Yes | No |
|  |  |  |  | Horn length | MO | E | 1 |  | No | D, Q, C | No | Yes | No |
|  |  |  |  | Soma mass | MO | E | 1 |  | No | D, Q, C | No | Yes | No |
| Hunter et al. | 2018 | 72(4):851-855 | Ovis aries | Mass | MO | E | 1 |  | Yes | D | No | No |  |
| Ferris \& Willis | 2018 | $\begin{gathered} 72(6): 1225- \\ 1241 \end{gathered}$ | M. lacinatus $\times M$. guttatus hybrids | Flowering time | LH | L | 1 |  | No | D, Q | No | Yes | No |
|  |  |  |  | Leaf area | мо | L | 1 |  | No | D, Q | No | Yes | No |
|  |  |  |  | Leaf lobes | MO | L | 1 |  | No | D, Q | No | Yes | No |
| Hamala et al | 2018 | $\begin{gathered} 72(7): 1373- \\ 1386 \end{gathered}$ | Arabidopsis lyrata | Flowering time | PER | L | 1 |  | No | D, Q | No | Yes | No |
|  |  |  |  | Shoot length | MO | L | 1 |  | No | D, Q | No | Yes | No |
|  |  |  |  | Inflorescence Num | мо | L | 1 |  | No | D, Q | No | Yes | No |
|  |  |  |  | Fruit maturation | LH | L | 1 |  | No | D, Q | No | Yes | No |
|  |  |  |  | Flowering cessation | LH | L | 1 |  | No | D, Q | No | Yes | No |
| Exposito-Alonzo et al. | 2018 | $\begin{gathered} 72(8): 1570- \\ 1586 \end{gathered}$ | Arabidopsis thaliana | Max Recruitment | PER | L | 1 |  | No | D, Q | No | Yes | Yes |
|  |  |  |  | Flowering time | LH | L | 1 |  | No | D, Q | No | Yes | Yes |
| Taylor et al | 2018 | $\begin{gathered} \text { 72(10): :2090- } \\ 2099 \end{gathered}$ | Urosaurus ornatus | Snout-vent length | MO | L | 1 |  | No | D, Q | No | Yes | No |
|  |  |  |  | Hind-limb length | MO | L | 1 |  | No | D, Q | No | Yes | No |
|  |  |  |  | Mass | MO | L | 1 |  | No | D, Q | No | Yes | No |
|  |  |  |  | MaxSprint | PER | L | 2 |  | No | D, Q | No | Yes | No |
| Hamann et al. | 2018 | $\begin{gathered} 72(12): 2682- \\ 2696 \end{gathered}$ | Brassica rapa | Flowering time | LH | L | 2 | Yes | No | D, Q | No | ? | No |
|  |  |  |  | Stem diameter | MO | L | 2 | Yes | No | D, Q | No | ? | No |
| Wang \& Althoff | 2019 | 73(2):303-316 | Drosophila melanogaster | ADH activity | PHY | L | 2 | Yes | No | D, Q | No | Yes | No |
|  |  |  |  | ADH_P010 | PHY | L | 2 | Yes | No | D, Q | No | Yes | No |
|  |  |  |  | ADH_P016 | PHY | L | 2 | Yes | No | D, Q | No | Yes | No |
|  |  |  |  | ADH_P1016 | PHY | L | 2 | Yes | No | D, Q | No | Yes | No |
| Ramakers et al. | 2019 | 73(2): 175-187 | Parus major | First-egg date Intercept first egg date | LH | L | 2 | Yes | No | D | Yes | Yes | Yes |


|  |  |  |  | Slope in FED with temperature | LH | L | 2 | Yes | No | D | Yes | Yes | Yes |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| LeGrice et al.. | 2019 | 73(4):762-776 | Lasiorhynchus barbicornis | Body length | MO | E | 1 |  | No | D, Q | No | ? | No |
| Keith \& MitchellOlds | 2019 | 73(5):947-960 | Boechera stricta | ConGS-R | MO | E | 1 |  | No | D | No | Yes |  |
|  |  |  |  | BC-ratio-R | MO | E | 1 |  | No | D | No | Yes |  |
|  |  |  |  | ConGS-C | MO | E | 1 |  | No | D | No | Yes |  |
|  |  |  |  | BC-ratio-C | мо | E | 1 |  | No | D | No | Yes |  |
|  |  |  |  | Congs-F | мо | E | 1 |  | No | D | No | Yes |  |
|  |  |  |  | BC-ratio-F | мо | E | 1 |  | No | D | No | Yes |  |
| Tonnabel et al. | 2019 | 73(5): 897-912 | Murcurialis annua | Height | MO | E | 1 |  | No | D, Q, C | No | Yes | Yes |
|  |  |  |  | Diameter | MO | E | 1 |  | No | D,Q,C | No | Yes | Yes |
|  |  |  |  | Mean branch length | мо | E | 2 | Yes | No | D, Q, C | No | Yes | Yes |
|  |  |  |  | Ped inflorescences | мо | E | 1 |  | No | D, Q, C | No | Yes | Yes |
|  |  |  |  | Peduncle length | мо | E | 5 | Yes | No | D, Q, C | No | Yes | Yes |
|  |  |  |  | Seeds | мо | E | 1 |  | No | D, Q, C | No | Yes | Yes |
|  |  |  |  | Vegetative weight | мо | E | 1 |  | No | D, Q, C | No | Yes | Yes |
|  |  |  |  | Germination rate | мо | E | 1 |  | No | D, Q, C | No | Yes | Yes |
| Watts et al | 2019 | $\begin{gathered} 73(9): 1927-1940 \\ 1940 \end{gathered}$ | Schizocosa crassipes | Mass | MO | E | 1 |  | No | D | No | Yes | Yes |
|  |  |  |  | Thorax width | MO | E | 3 | Yes | No | D | No | Yes | Yes |
|  |  |  |  | Brush area | мо | E | 1 |  | Yes | D | No | Yes | Yes |
|  |  |  |  | Tibial darkness | мо | E | 3 | Yes | No | D | No | Yes | Yes |
|  |  |  |  | Latency to Signal | BEH | E | 1 |  | No | D | No | Yes | Yes |
|  |  |  |  | Latency to Bounce | BEH | E | 1 |  | No | D | No | Yes | Yes |
|  |  |  |  | Bounce Rate | BEH | E | 1 |  | No | D | No | Yes | Yes |
|  |  |  |  | Bounce Interval | BEH | E | >1 | Yes | No | D | No | Yes | Yes |
|  |  |  |  | Number Wave Bouts | BEH | E | 1 |  | No | D | No | Yes | Yes |
|  |  |  |  | Total Wave Duration | BEH | E | 1 |  | No | D | No | Yes | Yes |
|  |  |  |  | Mean Wave Duration | BEH | E | >1 | Yes | No | D | No | Yes | Yes |
|  |  |  |  | Prop. Variance | BEH | E | 1 |  | No | D | No | Yes | Yes |
|  |  |  |  | Cummulative Variance | BEH | E | 1 |  | No | D | No | Yes | Yes |
|  |  |  |  | Courtship Effort (PC1) | BEH | E | 12 | PCA | No | D | No | Yes | Yes |
|  |  |  |  | Size-ornament (PC2) | мо | E | 12 | PCA | No | D | No | Yes | Yes |
|  |  |  |  | Leg-Wave duration (PC3) | BEH | E | 12 | PCA | No | D | No | Yes | Yes |

## Supplementary Text S2

Calculating bias in directional selection gradients that ignore effects of trait repeatability
We derive here Eqn. 5 (Main Text). We start with reprinting the mathematical relationship between $b_{1}^{*}$, the unstandardized linear selection gradient that ignores effects of withinindividual variance, the trait's repeatability $\left(R_{t}\right)$, and the true unstandardized linear selection gradient ( $b_{1}$ ) (Eqn. 4, Main Text):

$$
\begin{equation*}
b_{1}^{*}=b_{1} R_{t} \tag{S2.1}
\end{equation*}
$$

Standardized linear selection gradients $(\beta)$ measure the change in relative fitness per standard deviation unit trait (Lande and Arnold 1983), calculable by dividing the unstandardized linear selection gradient by mean fitness $(\bar{W})$ and by multiplying it by the square-root of the variance in trait value at the focal level of analysis, thus:
$\beta_{1}^{*}=b_{1}^{*} \frac{\sqrt{V_{p_{t}}}}{\overline{\mathrm{~W}}}$
The true standardized linear selection gradient $\left(\beta_{1}\right)$ represents the multiplication of $b_{1}$ with $\frac{\sqrt{V_{i_{i}}}}{\bar{W}}$, where $V_{i_{t}}$ represents the true individual variance in trait values:
$\beta_{1}=b_{1} \frac{\sqrt{V_{i_{t}}}}{\bar{W}}$
Eqn. S2.2 may therefore be rephrased as:
$\beta_{1}^{*}=\frac{\beta_{1}}{\sqrt{V_{i_{t}}}} R_{t} \sqrt{V_{p_{t}}}$
Expressing $R_{t}$ in its underlying variance components gives:
$\beta_{1}^{*}=\frac{\beta_{1}}{\sqrt{V_{i_{t}}}} \frac{V_{i_{t}}}{V_{i_{t}}+V_{e_{t}}} \sqrt{V_{i_{t}}+V_{e_{t}}}=\beta_{1} \frac{\sqrt{V_{i_{t}}}}{\sqrt{V_{i_{t}}+V_{e_{t}}}} \frac{\sqrt{V_{i_{t}}}}{\sqrt{V_{i_{t}}+V_{e_{t}}}} \frac{\sqrt{V_{i_{t}}+V_{e_{t}}}}{\sqrt{V_{i_{t}}}}=\beta_{1} \frac{\sqrt{V_{i_{t}}}}{\sqrt{V_{i_{t}}+V_{e_{t}}}}$
Re-expressing variance components in terms of repeatability, leads to Eqn. 5 (Main Text):
$\beta_{1}=\beta_{1}^{*} / \sqrt{R_{t}}$

## Supplementary Text S3

Calculating bias in quadratic selection gradients ignoring effects of trait repeatability
To derive the bias in quadratic selection gradients caused by ignoring within-individual variation, we provide the mathematical relationship between the unstandardized quadratic selection gradient that ignores the effects of within-individual error ( $b_{11}^{*}$ ), the true unstandardized quadratic selection gradient $\left(b_{11}\right)$, and the repeatability of the squared value of the focal trait $t\left(R_{t^{2}}\right)$, i.e., we apply Eqn. 4 to an unstandardized quadratic selection gradient:
$b_{11}^{*}=b_{11} R_{t^{2}}$
where $R_{t^{2}}$ represents the repeatability of the square of trait $t$. Estimating standardized selection gradients requires expressing trait values in standard deviation units (Lande and Arnold 1983). As we have seen above, the standardized trait value $(z)$ equals the raw trait value $(t)$ divided by the square root of the variance in trait values $\left(\sqrt{V_{t}}\right)$, where $z=t / \sqrt{V_{t}}$. Z-transforming the raw trait value ( $t$ ) thus results in $z^{2}=t^{2} / \sqrt{V_{t^{2}}}$. As we show above (Supplementary Text S2), the bias in the standardized linear gradient represents the square root of the bias in unstandardized gradients. Applied to quadratic selection gradients:
$\gamma_{11}=\gamma_{11}^{*} / \sqrt{R_{t^{2}}}$
As above, the repeatability of the squared term of trait $t$ is attributable to within- and amongindividual variance components:

$$
\begin{equation*}
R_{t^{2}}=\frac{V_{i_{t^{2}}}}{V_{i_{t^{2}}}+V_{e_{t^{2}}}} \tag{S3.3}
\end{equation*}
$$

where $V_{i_{t^{2}}}+V_{e_{t^{2}}}$ equals the total phenotypic variance in squared trait values $\left(V_{p_{t^{2}}}\right)$. The phenotypic variance in squared trait values $\left(V_{p_{t^{2}}}\right)$ represents the variance of a product (i.e., $V_{p_{t^{2}}}=V_{p_{x \cdot y}}$; where $x=y=t$ ); this variance can be broken down into the following components (e.g., Mood et al. 1973; Cacoullos 1989):
$V_{p_{x, y}}=C_{p_{x^{2}, y^{2}}}+\mu_{x^{2}} \mu_{y^{2}}-\left(C_{p_{x, y}}+\mu_{x} \mu_{y}\right)^{2}$
Variance of products thus vary as a function of mean trait values ( $\mu_{x}, \mu_{y}$ ), means of squared trait values $\left(\mu_{x^{2}}, \mu_{y^{2}}\right)$, as well as trait covariances $\left(C_{p_{x^{2}, y^{2}}}, C_{p_{x, y}}\right)$. Assuming multivariate normality, we can apply the following transformation:
$C_{p_{x^{2}, y^{2}}}=\left(C_{p_{x, y}}^{2}+2 \mu_{x} \mu_{y} \sqrt{V_{p_{x}} V_{p_{y}}}\right)$
Substituting Eqn. S3.5 into S3.4 gives:
$V_{p_{x \cdot y}}=\left(C_{p_{x, y}}^{2}+2 \mu_{x} \mu_{y} \sqrt{V_{p_{x}} V_{p_{y}}}\right)+\mu_{x^{2}} \mu_{y^{2}}-\left(C_{p_{x, y}}+\mu_{x} \mu_{y}\right)^{2}$
Re-expressing S 3.6 in terms of trait values rather than squared trait values gives:
$V_{p_{x \cdot y}}=\left(C_{p_{x, y}}^{2}+2 \mu_{x} \mu_{y} \sqrt{V_{p_{x}} V_{p_{y}}}\right)+\left(\mu_{x}^{2}+V_{p_{x}}\right)\left(\mu_{y}^{2}+V_{p_{y}}\right)-\left(C_{p_{x, y}}+\mu_{x} \mu_{y}\right)^{2}$
Because $x=y=t, C_{p_{x, y}}=V_{p_{x}}=V_{p_{y}}=V_{p_{t}}$, we can substitute $V_{p_{t}}$ for $C_{p_{x, y}}$ :
$V_{p_{t^{2}}}=2\left(V_{p_{t}}^{2}+2 \mu_{t} \mu_{t} \sqrt{V_{p_{t}} V_{p_{t}}}\right)+\left(\mu_{t}^{2}+V_{p_{t}}\right)\left(\mu_{t}^{2}+V_{p_{t}}\right)-\left(V_{p_{t}}+\mu_{t} \mu_{t}\right)^{2}$
This then simplifies to:
$V_{p_{t^{2}}}=2 V_{p_{t}}^{2}+4 V_{p_{t}} \mu_{t}^{2}$
Applying Eqn. S3.9 to the among-individual $\left(V_{i_{t^{2}}}\right)$ instead of total phenotypic variance in squared trait values $\left(V_{t^{2}}\right)$ gives:
$V_{i_{t^{2}}}=2 V_{i_{t}}^{2}+4 V_{i_{t}} \mu_{t}^{2}$
We can now express the factor causing bias in quadratic selection gradients ( $\sqrt{R_{t^{2}}}$; Eqn. S3.2) in terms of variances in trait values rather than squared trait values:
$\sqrt{R_{t^{2}}}=\sqrt{\frac{2 V_{i_{t}}^{2}+4 V_{i_{t}} \mu_{t}^{2}}{2 V_{p_{t}}^{2}+4 V_{p_{t}} \mu_{t}^{2}}}=\sqrt{\frac{V_{i_{t}}^{2}+2 V_{i_{t}} \mu_{t}^{2}}{V_{p_{t}}^{2}+2 V_{p_{t}} \mu_{t}^{2}}}$
This formula shows that bias is much more complex for quadratic versus linear gradients. Bias in standardized linear selection gradients varies solely as a function of the relative magnitudes of among- $\left(V_{i_{t}}\right)$ and within-individual $\left(V_{e_{t}}\right)$ variances and equals the trait's square-root repeatability ( $\sqrt{R_{t}}$; Eqn. S2.6). By contrast, bias in quadratic selection gradients varies as a function of the among- $\left(V_{i_{t}}\right)$ and within-individual $\left(V_{e_{t}}\right)$ variances, and the square of the mean trait value $\left(\mu_{t}^{2}\right)$. Importantly, Eqn. S3.11 implies that bias in quadratic selection gradients is lowest when the trait mean $\left(\mu_{t}\right)$ equals zero. We show this by comparing bias $\left(\sqrt{R_{t^{2}}}\right)$ when the trait mean is zero versus infinite. When $\mu_{t}=0$, Eqn. S.3.11 simplifies into:
$\sqrt{R_{t^{2}}}=\sqrt{\frac{v_{i_{t}}^{2}}{V_{p_{t}}^{2}}}=\sqrt{R_{t}^{2}}=R_{t}$
By contrast, when $\left|\mu_{t}\right|$ approaches infinity, $\sqrt{R_{t^{2}}}$ (Eqn. S3.11) becomes:
$\lim _{\left|\mu_{t}\right| \rightarrow \infty} \sqrt{R_{t^{2}}} \approx \sqrt{\frac{V_{i_{t}}}{V_{p_{t}}}}=\sqrt{R_{t}}$

The magnitude of attenuation bias in quadratic selection gradient analyses $\left(\sqrt{R_{t^{2}}}\right.$; Eqn. S3.11) thus varies between $R_{t}$ (when $\mu_{t}=0$; Eqn. S3.12) and $\sqrt{R_{t}}$ (when $\left|\mu_{t}\right| \rightarrow \infty$; Eqn. S3.13). Because $R_{t}$ is always smaller than $\sqrt{R_{t}}$, attenuation bias therefore increases with decreasing value of $\left|\mu_{t}\right|$, and is, in fact, smallest when $\mu_{t}=0$. This insight is important as our literature review (TextS1) implies that many studies (Table 1) mean-centre traits prior to analysis as part of trait standardization (i.e., $z=\left(t-\mu_{t}\right) / \sqrt{V_{p_{t}}}$ ). This transformation effectively replaces $\mu_{t}$ for $\mu_{z}=0$ in Eqn. S3.11 and thereby (accidentally) minimizes attenuation bias.

Mean-centring traits minimizes attenuation bias but also affects the interpretation of the linear component of a quadratic selection gradient analyses. In a quadratic regression model, the linear effect $\left(b_{1}\right)$ of the trait $(t)$ on absolute fitness $(W)$ represents the slope of the tangent line where the trait has the value zero as illustrated by the orange dot in Figure S3a, where the arrow represents $b_{1}$ for $t=0$. A biologically meaningful zero-point represents the populationmean trait value ( $\bar{t}$; dotted line in Fig. S3), because the linear effect of the trait on fitness then provides information on whether the fitness peak/valley (white star in Fig. S3) is above or below the population mean trait value $(\bar{t})$. Said differently, it provides information on the expected strength of directional selection on the trait. The arrow in Fig. S3b represents the tangent line at this population-mean value (blue dot), and is calculated by adding $2 b_{11} \bar{t}$ to $b_{1}$ (as defined in Eqn. 14). Applying this transformation to the scenario presented in Fig S3, would result in $\beta_{1}>$ 0 at the population-mean trait value (Fig. S3b), implying that the population mean is below the optimal trait value, as illustrated.


Figure S3. Illustration of a parabolic relationship between trait $(t)$ on absolute fitness $(W)$, where the dotted line represents the population-mean trait value, the star represents the optimal trait value; (a) the orange dot represents the tangent line where the trait value has the value zero. (b) the blue dot represents the tangent line at the population-mean trait value.

An important question is whether estimates of optimal trait values in stabilising selection scenarios are also affected by failure to acknowledge biasing effects of withinindividual error. The optimal trait value represents the trait value at the vertex of the parabola, calculable as $\frac{-\beta_{1}}{2 \gamma_{11}}$ (Bronshtein et al. 2015). The trait value at the parabolic peak calculated while ignoring biasing effects of within-individual variance $\left(\frac{-\beta_{1}^{*}}{2 \gamma_{11}^{*}}\right)$ is mathematically related to the true
trait value at the parabolic peak $\left(\frac{-\beta_{1}}{2 \gamma_{11}}\right)$ because $\gamma_{11}=\gamma_{11}^{*} / \sqrt{R_{t^{2}}}($ Eqn. S3.2 $)$ and $\beta_{1}=\beta_{1}^{*} / \sqrt{R_{t}}$ (Eqn. S2.6), thus:
$\frac{-\beta_{1}}{2 \gamma_{11}}=\frac{-\beta_{1}^{*}}{2 \gamma_{11}^{*}} \frac{\sqrt{R_{t^{2}}}}{\sqrt{R_{t}}}$
where $\frac{\sqrt{R_{t^{2}}}}{\sqrt{R_{t}}}$ represents the bias in the trait value at the parabolic peak. Substituting $\sqrt{R_{t^{2}}}$ for Eqn. S3.11 gives:
$\frac{\sqrt{R_{t}{ }^{2}}}{\sqrt{R_{t}}}=\frac{\sqrt{\frac{V_{i_{t}}^{2}+2 V_{i_{t}} \mu_{t}^{2}}{V_{p_{t}}^{2}+2 V_{p} p_{t} \mu_{t}^{2}}}}{\sqrt{R_{t}}}$
Eqn. S3.15 simplifies for traits that were mean-centred (using Eqn. S3.12):
$\frac{\sqrt{R_{t^{2}}}}{\sqrt{R_{t}}}=\frac{R_{t}}{\sqrt{R_{t}}}=\sqrt{R_{t}}$
Eqn. S3.15 simplifies differently when the mean trait value approaches infinity (using Eqn. S3.13):
$\lim _{\left|\mu_{t}\right| \rightarrow \infty} \frac{\sqrt{R_{t^{2}}}}{\sqrt{R_{t}}} \approx \frac{\sqrt{R_{t}}}{\sqrt{R_{t}}}=1$
In other words, for variance-standardized traits that are also mean-centred, failure to control for within-individual error causes an overestimation of the optimal trait value by a factor equal $\sqrt{R_{t}}$ (Eqn. S3.16). Importantly, Eqn. S3.17 implies that bias in the placement of the parabolic peak is greatest when the trait mean $\left(\mu_{t}\right)$ equals zero. Moreover, Eqn. S 3.17 shows that bias in the placement of the parabolic peak $\left(\frac{\sqrt{R_{t}}}{\sqrt{R_{t}}}\right)$ disappears entirely when the mean trait value approximates infinity (and thus will not happen in practice). Mean-centring traits prior to analysis therefore decreases attenuation bias in standardized quadratic selection gradients (Eqn. S3.12) but simultaneously leads to an overestimation of the placement of the parabolic peak (Eqn. S3.16).

## Supplementary Text S4

## Calculating bias in correlational selection gradients ignoring effects of trait repeatability

To derive the bias in correlational selection gradients, we print the mathematical relationship between the unstandardized correlational selection gradient ignoring effects of trait repeatability $\left(b_{12}^{*}\right)$, the true unstandardized correlational selection gradient $\left(b_{12}\right)$, and the repeatability $\left(R_{t_{1} t_{2}}\right)$ of the interaction between two traits, trait $1\left(t_{1}\right)$ and trait $2\left(t_{2}\right)$, i.e., we apply Eqn. 4 to an unstandardized correlational selection gradient:
$b_{12}^{*}=b_{12} R_{t_{1} t_{2}}$
Estimating standardized selection gradients requires expressing trait values in standard deviation units (Lande and Arnold 1983). As we demonstrated above, the standardized trait value $(z)$ equals the raw trait value $(t)$ divided by the square root of the variance in trait values $\left(\sqrt{V_{t}}\right)$, where $z=t / \sqrt{V_{t}}$. Z-transforming $t_{1}$ and $t_{2}$ leads to $z_{1} z_{2}=t_{1} t_{2} / \sqrt{V_{t_{1} t_{2}}}$. We showed above (Supplementary Text S2) that the bias in the standardized linear gradient is equal to the square root of the bias in unstandardized gradients. Applying the same logic to correlational selection gradients, we obtain:
$\gamma_{12}=\gamma_{12}^{*} / \sqrt{R_{t_{1} t_{2}}}$

As above, the repeatability of the multiplication of the traits is attributable to within- and among-individual variance components:
$R_{t_{1} t_{2}}=\frac{V_{i_{t_{1}} t_{2}}}{V_{i_{t_{1} t_{2}}}+V_{e_{t_{1} t_{2}}}}$
We noted in Supplementary Text S3, the variance in the multiplication of the two traits ( $V_{t_{1} t_{2}}$ ) is equal to the variance of a product; this variance can be broken down into the following components (Eqn. S3.7):
$V_{t_{1} t_{2}}=\left(C_{t_{1} t_{2}}^{2}+2 \mu_{t_{1}} \mu_{t_{2}} \sqrt{V_{t_{1}} V_{t_{2}}}\right)+\left(\mu_{t_{1}}^{2}+V_{t_{1}}\right)\left(\mu_{t_{2}}^{2}+V_{t_{2}}\right)-\left(C_{t_{1} t_{2}}+\mu_{t_{1}} \mu_{t_{2}}\right)^{2}$
The among-individual variance in the multiplication of the two traits $\left(V_{i_{1} t_{2}}\right)$ thus equals:
$V_{i_{t_{1} t_{2}}}=C_{i_{t_{1} t_{2}}}^{2}+4 \mu_{t_{1}} \mu_{t_{2}} \sqrt{V_{i_{t_{1}}} V_{i_{t_{2}}}}+\left(\mu_{t_{1}}^{2}+V_{i_{t_{1}}}\right)\left(\mu_{t_{2}}^{2}+V_{i_{t_{2}}}\right)-\left(C_{i_{t_{1} t_{2}}}+\mu_{t_{1}} \mu_{t_{2}}\right)^{2}$
The total phenotypic variance in the multiplication of the two traits $\left(V_{p_{t_{1} t_{2}}}=V_{i_{t_{1} t_{2}}}+V_{e_{t_{1} t_{2}}}\right)$ instead equals:
$V_{p_{t_{1} t_{2}}}=C_{p_{t_{1} t_{2}}}^{2}+4 \mu_{t_{1}} \mu_{t_{2}} \sqrt{V_{p_{t_{1}}} V_{p_{t_{2}}}}+\left(\mu_{t_{1}}^{2}+V_{p_{t_{1}}}\right)\left(\mu_{t_{2}}^{2}+V_{p_{t_{2}}}\right)-\left(C_{p_{t_{1} t_{2}}}+\mu_{t_{1}} \mu_{t_{2}}\right)^{2}$
where $C_{p_{t_{1} t_{2}}}=C_{i_{t_{1} t_{2}}}+C_{e_{t_{1} t_{2}}}, V_{p_{t_{1}}}=V_{i_{t_{1}}}+V_{e_{t_{1}}}, V_{p_{t_{2}}}=V_{i_{t_{2}}}+V_{e_{t_{2}}}$. We express the bias in correlational selection gradients $\left(\sqrt{R_{t_{1} t_{2}}} ; \mathrm{S} 4.2\right)$ in terms of variances in trait values rather than trait products by substituting, obtaining:
$\sqrt{R_{t_{1} t_{2}}}=\sqrt{\frac{c_{i_{1} t_{2}}^{2}+4 \mu_{t_{1}} \mu_{t_{2}} \sqrt{V_{i_{1}} V_{i_{2}}}+\left(\mu_{t_{1}}^{2}+V_{i_{1}}\right)\left(\mu_{t_{2}}^{2}+V_{i_{t_{2}}}\right)-\left(c_{i_{1} t_{2}}+\mu_{t_{1}} \mu_{t_{2}}\right)^{2}}{c_{p_{t_{1} t_{2}}}^{2}+4 \mu_{t_{1}} \mu_{t_{2}} \sqrt{V_{p_{1}} V_{p_{t_{2}}}}+\left(\mu_{t_{1}}^{2}+V_{p_{t_{1}}}\right)\left(\mu_{t_{2}}+V_{p_{t_{2}}}\right)-\left(c_{p_{t_{1} t_{2}}}+\mu_{t_{1}} \mu_{t_{2}}\right)^{2}}}$
This formula shows that bias is much more complex for correlational versus quadratic gradients because bias in the former additionally varies as a function of covariances between the traits within and among individuals. When traits are mean-centred prior to analysis (i.e., $\mu_{t_{1}}=\mu_{t_{2}}=$ 0, Eqn. S4.7 can simplifies into:
$\sqrt{R_{t_{1} t_{2}}}=\sqrt{\frac{V_{i_{t_{1}}} V_{i_{t_{2}}}+C_{i_{t_{1}} t_{2}}}{V_{p_{t_{1}}} V_{p_{t_{2}}}+C_{p_{t_{1} t_{2}}}^{2}}}$
Expressing covariances in correlations gives $r_{i_{1} t_{2}}=\frac{C_{i_{t_{1} t_{2}}}}{\sqrt{V_{i_{1}} V_{i_{2}}}}$. Hence, $C_{i_{t_{1} t_{2}}}^{2}=r_{i_{t_{1} t_{2}}}^{2} V_{i_{t_{1}}} V_{i_{t_{2}}}$. Similarly, $r_{p_{t_{1} t_{2}}}=\frac{c_{p_{t_{1} t_{2}}}}{\sqrt{V_{p_{t_{1}}} V_{p_{t_{2}}}}}$. Eqn. S4.8 can thus be rephrased into:
$\sqrt{R_{t_{1} t_{2}}}=\sqrt{\frac{V_{i_{1}} V_{i_{t_{2}}}+c_{i_{1} t_{2}}}{2}} \frac{V_{p_{t_{1}}} V_{p_{t_{2}}}+C_{p_{t_{1} t_{2}}}^{2}}{2}=\sqrt{\frac{V_{i_{t_{1}}} V_{i_{t_{2}}}+r_{i_{1} t_{2}}^{2} V_{i_{t_{1}}} V_{i_{t_{2}}}}{V_{p_{t_{1}}} V_{p_{t_{2}}}+r_{p_{t_{1} t_{2}}}^{2} V_{p_{t_{1}}} V_{p_{t_{2}}}}}=\sqrt{\frac{V_{i_{t_{1}}} V_{i_{t_{2}}}\left(r_{i_{t_{1}} t_{2}}^{2}+1\right)}{V_{p_{t_{1}}} V_{p_{t_{2}}}\left(r_{p_{t_{1} t_{2}}}^{2}+1\right)}}=$
$\sqrt{R_{t_{1}} R_{t_{2}}} \sqrt{\frac{r_{t_{t_{1} t_{2}}+1}^{2}+1}{r_{p_{t_{1} t_{2}}^{2}}^{2}+1}}$
This shows that $\sqrt{R_{t_{1} t_{2}}}$ equals the geometric mean repeatability of the two traits $\left(\sqrt{R_{t_{1}} R_{t_{2}}}\right)$ when the correlations between the two traits do not differ between the levels (i.e., $r_{i_{1} t_{2}}=$ $\left.r_{e_{t_{1} t_{2}}}=r_{p_{t_{1} t_{2}}}\right)$ and traits are mean-centred prior to analyses. Therefore, when $\left|r_{i_{1} t_{2}}\right|>\left|r_{e_{t_{1} t_{2}}}\right|$
it follows that $\sqrt{R_{t_{1} t_{2}}}>\sqrt{R_{t_{1}} R_{t_{2}}}$; by contrast, when $\left|r_{i_{t_{1} t_{2}}}\right|<\left|r_{e_{t_{1} t_{2}}}\right|$, it follows that $\sqrt{R_{t_{1} t_{2}}}<$ $\sqrt{R_{t_{1}} R_{t_{2}}}$.

One key question is whether the shape of the selection surface is also affected by failure to acknowledge biasing effects of within-individual variation. Surface shape is a function of the ratio of the product of the quadratic selection gradients of two focal traits over the square of their correlational selection gradient (i.e., $\frac{\gamma_{11} \gamma_{22}}{\gamma_{12}^{2}}$ ), which describes a saddle-shaped fitness surface when below one (assuming $\gamma_{11}$ and $\gamma_{22}$ are both negative) but a fitness peak when above one (Phillips and Arnold 1989). For mean-centred traits, the shape of the selection surface calculated while ignoring biasing effects of within-individual variance $\left(\frac{\gamma_{11}^{*} \gamma_{22}^{*}}{\gamma_{12}^{*}}\right)$ is mathematically related to true surface $\left(\frac{\gamma_{11} \gamma_{22}}{\gamma_{12}^{2}}\right)$ in the following way:
$\frac{\gamma_{11} \gamma_{22}}{\gamma_{12}^{2}}=\frac{\gamma_{11}^{*}}{\sqrt{R_{t_{1}^{2}}}} \frac{\gamma_{22}^{*}}{\sqrt{R_{t_{2}^{2}}}} \frac{R_{t_{1} t_{2}}}{\gamma_{12}^{*}{ }^{2}}=\frac{\gamma_{11}^{*} \gamma_{22}^{*}}{\gamma_{12}^{*}{ }^{2}} \frac{R_{t_{1} t_{2}}}{\sqrt{R_{t_{1}^{2} R_{2}^{2}}}}$
The shape of the selection surface is not affected when $\frac{R_{t_{1} t_{2}}}{\sqrt{R_{t_{1}^{2}} R_{2}^{2}}}=1$. For mean-centred traits, $\sqrt{R_{t^{2}}}=R_{t}($ Eqn. S3.12 $), \sqrt{R_{t_{1} t_{2}}}=\sqrt{R_{t_{1}} R_{t_{2}}} \sqrt{\frac{r_{i_{t_{1} t_{2}}+1}^{2}}{r_{p_{t_{1} t_{2}}}^{2}+1}}$ (Eqn. S4.9), therefore bias in the selection surface is described as:
$\frac{R_{t_{1} t_{2}}}{\sqrt{R_{t_{1}^{2}}^{2} t_{t_{2}}^{2}}}=\frac{R_{t_{1}} R_{t_{2}}\left(\frac{r_{i_{t_{1} t_{2}}}^{2}}{r_{p_{t_{1} t_{2}}+1}^{2}}\right)}{R_{t_{1}} R_{t_{2}}}=\frac{r_{i_{t_{1} t_{2}}}^{2}+1}{r_{p_{t_{1} t_{2}}^{2}}^{2}+1}$
This demonstrates that the bias in the fitness surface is not a function of (geometric mean) repeatability of the traits for mean-centred traits. Eqn. S 4.11 shows instead that the fitness surface is unbiased when the correlations between the two traits do not differ between the levels (i.e., $r_{i_{1} t_{2}}=r_{e_{t_{1} t_{2}}}=r_{p_{t_{1} t_{2}}}$ ). However, when correlations among individuals are tighter than those within individuals (i.e., $\left|r_{i_{1} t_{2}}\right|>\left|r_{e_{1} t_{2}}\right|$, failure to acknowledge within-individual variance can cause bias in the shape of the selection surface because it makes the fitness surface appear more saddle-shaped. Along the same lines, when correlations within individuals are tighter than those among individuals (i.e., $\left|r_{i_{t_{1} t_{2}}}\right|<\left|r_{e_{t_{1} t_{2}}}\right|$ ), failure to acknowledge withinindividual variance can cause bias in the shape of the selection surface because it makes the fitness surface appear more peaked. Such simple rules, notably, do not apply when correlational selection gradient analyses were based on traits that were not mean-centred prior to analyses because bias in the correlational selection gradient $\left(\sqrt{R_{t_{1} t_{2}}}\right)$ is then much more complex (Eqn. S4.7) thus also any effects on fitness surfaces.

## Supplementary Text S5

Bias in selection gradients used on mean trait values
Researchers commonly calculate individual-mean trait values prior to conducting phenotypic selection analyses (Table 1). In what follows, we logically assume that researchers working with individual-mean trait values would apply trait standardization after rather than before calculating individual-mean trait values. We note that none of the papers using individualmeans in phenotypic selection analyses in our review (Text S1) clarified when standardization
was applied. However, this would be the only sensible decision when one views the variance in individual-mean trait values as the best proxy of the among-individual variance.

In previous sections, we derived the equations for bias in linear (Text S2), quadratic (Text S3), and correlational (Text S4) selection gradients resulting from failure to acknowledge residual within-individual variance. Based on few additional assumptions, we can readily modify these equations to be applied to analyses using individual-mean trait values. Specifically, following Snijders \& Bosker (1999), we assumed that the total phenotypic variance among individual-mean trait values $\left(V_{p_{\bar{t}}}\right)$ can be approximated as:

$$
\begin{equation*}
V_{p_{\bar{t}}}=V_{i_{t}}+\frac{V_{e_{t}}}{n} \tag{S5.1}
\end{equation*}
$$

where $V_{i_{t}}$ and $V_{e_{t}}$ represent the among-individual and residual within-individual variance in trait values, respectively, and $n$ represents the number of replicate samples collected per individual (assuming equal replication among all individuals). We further assumed that the phenotypic covariance between mean traits $\left(C_{p_{\bar{t}_{1} \bar{t}_{2}}}\right)$ can then be approximated as (Snijders and Bosker 1999):
$\operatorname{Cov}_{p_{\bar{t}_{1} \bar{t}_{2}}}=\operatorname{Cov}_{i_{t_{1} t_{2}}}+\frac{\operatorname{Cov}_{e_{t_{1} t_{2}}}}{n}$
where $\operatorname{Cov}_{i_{t_{1} t_{2}}}$ and $\operatorname{Cov}_{e_{t_{1} t_{2}}}$ represent the among-individual and residual within-individual covariances between traits. The associated formula for the phenotypic correlation between individual-mean trait values ( $r_{\bar{t}_{1} \bar{t}_{2}}$ ) is therefore (Dingemanse et al. 2012):
$r_{p_{\bar{t}_{1} t_{2}}}=\frac{\operatorname{Cov}_{i_{t_{1} t_{2}}}+\frac{\operatorname{Cov}_{e_{t_{1}} t_{2}}}{n}}{\sqrt{\left(V_{i_{t_{1}}}+\frac{V_{e_{t_{1}}}}{n}\right)\left(v_{i_{t_{2}}}+\frac{V_{e_{e_{2}}}}{n}\right)}}$
In brief, any equation printed in Texts S2-S4 can therefore be modified to derive bias for phenotypic selection analyses that used individual-mean trait values, which may be achieved by replacing (i) $V_{e_{t}}$ for $\frac{V_{e_{t}}}{n}$, (ii) $V_{p_{t}}$ for $V_{p_{\vec{t}}}$, (iii) $R_{t}$ for $\frac{V_{i_{t}}}{V_{i_{t}}+\frac{v_{e_{t}}}{n}}$, (iv) $C_{e_{t_{1} t_{2}}}$ for $\frac{C_{e_{t_{1} t_{2}}}}{n}$ and (v) $r_{p_{t}}$ for $r_{p_{\bar{t}}}$. When applied to individual-mean trait values, main formulae for bias in standardized selection gradients owing to failure to acknowledge within-individual variation consequently become:
(i) For linear selection gradients: $\sqrt{\frac{V_{i_{t}}}{V_{i_{t}}+\frac{V_{e}}{n}}}$ instead of $\sqrt{R_{t}}$ (Eqn. S2.6).
(ii) For quadratic selection gradients (general formula): $\sqrt{\frac{V_{t_{t}}^{2}+2 V_{i_{t}} \mu_{t}^{2}}{V_{p_{\bar{t}}}^{2}+2 V_{p_{\bar{t}}} \mu_{t}^{2}}}$ instead of Eqn. S3.11.
(iii) For quadratic selection gradients (mean-centred traits): $\frac{V_{i_{t}}}{V_{i_{t}}+\frac{v_{t}}{n}}$ instead of Eqn. S3.12.
(iv) For correlational selection gradients (general formula): $\left.\left.\sqrt{\frac{2 c_{i_{t_{1}} t_{2}}^{2}}{2}+4 \mu_{t_{1}} \mu_{t_{2}} \sqrt{V_{i_{t_{1}}}^{2} V_{\bar{t}_{1} \bar{t}_{2}}}+4 \mu_{t_{1}} \mu_{t_{2}}}+\left(\mu_{t_{1}}^{2}+V_{i_{t_{1}}}\right)\left(\mu_{\bar{t}_{\bar{t}_{1}}}^{2}+V_{i_{t_{t_{2}}}}\right)-\left(c_{i_{t_{1} t_{2}}}+\mu_{t_{1}} \mu_{t_{2}}\right)^{2}{ }_{t_{1}}^{2}+V_{p_{\bar{t}_{1}}}\right)\left(\mu_{t_{2}}^{2}+V_{p_{\bar{t}_{2}}}\right)-\left(c_{p_{\bar{t}_{1} \bar{t}_{2}}}+\mu_{t_{1}} \mu_{t_{2}}\right)^{2}\right) ~ i n s t e a d ~ o f ~ E q n . ~ S 4.7 . ~$
(v) For correlational selection gradients (mean-centred traits): $\sqrt{\frac{v_{t_{t_{1}}} V_{i_{t_{2}}}}{V_{\bar{t}_{1}}} V_{p_{\bar{t}_{2}}}} \sqrt{\frac{r_{t_{t_{1}} t_{2}}^{2}+1}{r_{p_{\bar{t}_{1} \bar{t}_{2}}}^{2}+1}}$ instead of Eqn. S4.9.

## Supplementary Text S6

## Estimating quadratic selection gradients with multivariate mixed-effects models

To estimate quadratic selection using a multivariate mixed-effects model, we expand the bivariate model used to estimate linear selection (Eqn. 9, 10). This introduces a general solution applicable to further extensions. Quadratic selection gradients calculated using analyses ignoring within-individual variance $\left(\gamma_{11}^{*}\right)$ would normally be modelled by expanding Eqn. 1 into (Stinchcombe et al. 2008):
$\omega=\alpha+\beta_{1}^{*} z+\frac{1}{2} \gamma_{11}^{*} z^{2}+\varepsilon$
This model is applied when each individual's trait (e.g., tarsus) is measured only once, but would suffer the problem of attenuation. Unattenuated quadratic selection gradients $\left(\gamma_{11}\right)$ may be acquired by expanding the bivariate into a trivariate mixed-effects model; again, this requires repeated measures. We propose here to estimate quadratic selection gradients by fitting the squared term of the trait $\left(t_{h i}^{2}\right)$ as a third response. We note an apparent problem: our aim is estimating the effect of the square of individual-mean trait values $\left(\bar{t}_{i}^{2}\right)$ on fitness rather than the effect of individual-means of squared trait values $\left(\overline{t_{l}^{2}}\right.$; note the subtle difference in the coverage of the bar to distinguish the two values). The mixed-model would estimate effects of $\bar{t}{ }_{l}^{2}$ not $\bar{t}_{i}^{2}$; fitting the squared value of each observation $\left(t_{h i}^{2}\right)$ thus seems inappropriate. To assess if this is indeed a problem, we ran simulations with normally distributed data, for different levels of trait repeatability, and compared the two metrics. We found that mixed-model estimates of amongindividual variance in mean-of-squares accurately approximate simulated variances of the square of individual-specific values (see Section "Mean-of-squares vs. Square-of-means" below). The proposed trivariate model has the following phenotypic equation and random effects structure:

$$
\left[\begin{array}{c}
t_{h i} \\
t_{h i}^{2} \\
\mathrm{~W}_{i}
\end{array}\right]=\boldsymbol{\beta}_{\mathbf{0}}+\boldsymbol{I}_{\boldsymbol{i}}+\boldsymbol{e}_{\boldsymbol{h i}}
$$

$$
\left[\begin{array}{c}
I_{t} \\
I_{t^{2}} \\
I_{\mathrm{W}}
\end{array}\right] \sim M V N\left(0, \Omega_{I}\right):\left[\begin{array}{ccc}
V_{i_{t}} & C_{i_{t, t^{2}}} & C_{i_{t, \mathrm{~W}}} \\
C_{i_{t, t^{2}}} & V_{i_{t^{2}}} & C_{i_{t^{2}, \mathrm{~W}}} \\
C_{i_{t, \mathrm{~W}}} & C_{i_{t^{2}, \mathrm{~W}}} & V_{i_{\mathrm{W}}}
\end{array}\right]
$$

$$
\left[\begin{array}{c}
e_{t}  \tag{S6.2}\\
e_{t^{2}} \\
e_{\mathrm{W}}
\end{array}\right] \sim M V N\left(0, \Omega_{e}\right):\left[\begin{array}{ccc}
V_{e_{t}} & C_{e_{t, t^{2}}} & C_{e_{t, \mathrm{~W}}} \\
C_{e_{t, t^{2}}} & V_{e_{t^{2}}} & C_{e_{t^{2}, \mathrm{~W}}} \\
C_{e_{t, \mathrm{~W}}} & C_{e_{t^{2}, \mathrm{~W}}} & V_{e_{\mathrm{W}}}
\end{array}\right]
$$

Importantly, the standardized quadratic selection gradient ( $\gamma_{11}$ ) to be calculated represents a partial regression coefficient (Lande and Arnold 1983). The linear ( $b_{1}$ ) and quadratic $\left(b_{11}\right)$ slopes of the regression of the unstandardized trait on absolute fitness are partial regression coefficients; their calculation requires information embedded in the among-individual variancecovariance matrix $\left(\Omega_{I}\right)$ :
$b_{1}=\frac{C_{i_{t, \mathrm{~W}} V_{i^{2}}}-C_{i_{t}, \mathrm{~W}} C_{i_{t, t}}}{V_{i_{t}} V_{i_{t^{2}}}-\left[C_{i_{t, t^{2}}}\right]^{2}}$
$b_{11}=\frac{C_{i_{t^{2}, \mathrm{~W}}} V_{i_{t}}-C_{i_{t, \mathrm{~W}}} C_{i_{t, t^{2}}}}{V_{i_{t}} V_{i_{t^{2}}}-\left[C_{i_{t, t^{2}}}\right]^{2}}$

Mathematically, partial regression coefficients may directly be derived by inverting the among-individual covariance matrix ( $\Omega_{A}$ ). Briefly, matrix $\Omega_{I}$ (Eqn. S6.2) may be "split" into a matrix of predictors ( $\Omega_{A}$ ) and a matrix of covariances between predictors (traits) and response (fitness) $\left(\Omega_{B}\right)$, here taking the form of:

$$
\begin{align*}
& \Omega_{A}:\left[\begin{array}{cc}
V_{i_{t}} & C_{i_{t, t^{2}}} \\
C_{i_{t, t^{2}}} & V_{i_{t^{2}}}
\end{array}\right] \\
& \Omega_{B}:\left[\begin{array}{ll}
C_{i_{t, \mathrm{~W}}} & C_{i_{t^{2}, \mathrm{~W}}}
\end{array}\right] \tag{S6.4}
\end{align*}
$$

Partial regression coefficients (here, the unstandardized selection gradients) are then derived by multiplying $\boldsymbol{A}^{-1} \boldsymbol{B}$ (Bernstein 2005). In Supplementary Text S 8 and on Github (https://github.com/YimenAraya-Ajoy/SelectionBias), we provide R-code to estimate and invert $\Omega_{I}$ and calculate partial regression coefficients. The standardized quadratic selection gradient ( $\gamma_{11}$ ) then represents the multiplication of the unstandardized quadratic selection gradient ( $b_{11}$; Eqn. S6.3) with $\frac{\sqrt{V_{i_{t^{2}}}}}{\beta_{0_{\mathrm{W}}}}$ :
$\gamma_{11}=2 b_{11} \frac{\sqrt{V_{i_{t^{2}}}}}{\beta_{0_{\mathrm{W}}}}$
A similar procedure can be applied to transform the unstandardized linear component in the quadratic selection model ( $b_{1}$; Eqn. 6.3) into an interpretable standardized linear gradient $\left(\beta_{1}\right)$. Adding a quadratic term, importantly, changes the meaning of this parameter, now representing the slope of the tangent where the trait has the value zero. A biologically meaningful zero-point represents the population-mean trait value, estimated as $\beta_{0_{t}}$ in formulations like Eqn. S6.2 (illustrated in Fig. S3). Expressing $\beta_{1}$ relative to the populationmean trait value is insightful, for example, when $\gamma_{11}<0$, the finding that $\beta_{1}=0$ implies stabilising selection with the optimal phenotype matching the population-mean trait value. $\beta_{1} \neq$ 0 instead implies the adaptive peak is shifted away from the population-mean (see Fig. S3b), indicative of directional selection. The unstandardized linear gradient at the population-mean is the value of $b_{1}$ (as defined in Eqn. S6.3) plus $2 b_{11} \beta_{0_{t}}$. An insightful standardized value of $\beta_{1}$ is thus calculated by multiplying this sum with, $\frac{\sqrt{V_{i_{t}}}}{\beta_{0_{\mathrm{W}}}}$ (as in Eqn. 11, Main Text):

$$
\begin{equation*}
\beta_{1}=\left(b_{1}+2 b_{11} \beta_{0_{t}}\right) \frac{\sqrt{V_{i_{t}}}}{\beta_{0_{W}}} \tag{S6.6}
\end{equation*}
$$

The above assumes the trait was not mean-centred prior to analysis (see Discussion); the correction $+2 b_{11} \beta_{0_{t}}$ would be unnecessary if it was.

## Estimating correlational selection gradients with multivariate mixed-effects models

Expanding the model to estimate correlational selection gradients requires modifying Eqn. S6.2 to instead fit two traits $\left(t_{1}, t_{2}\right)$ and their product $\left(t_{1} t_{2}\right)$ as response variables. In many cases, researchers fit both the linear and quadratic of both traits in such models, in which case the multivariate mixed-model solution would fit six response variables. Unstandardized partial regression coefficients (here, $b_{1}, b_{2}, b_{11}, b_{22}$, and $b_{12}$ ) are again calculated by splitting $\Omega_{I}$ into $\Omega_{A}$ and $\Omega_{B}$, and multiplying $\boldsymbol{A}^{-1} \boldsymbol{B}$. Standardized linear ( $\beta_{1}, \beta_{2}$ ) and quadratic ( $\gamma_{11}, \gamma_{22}$ ) components are calculated as above (Eqn. S6.5, S6.6), while the standardized correlational selection gradient is calculated as:
$\gamma_{12}=b_{12} \frac{\sqrt{V_{i_{t_{1} t_{2}}}}}{\beta_{0_{\mathrm{W}}}}$

Where $V_{i_{t_{1} t_{2}}}$ equals (Eqn. S4.5):

$$
\begin{equation*}
V_{i_{t_{1} t_{2}}}=2 C_{i_{t_{1} t_{2}}}^{2}+4 \beta_{0_{t_{1}}} \beta_{0_{t_{2}}} \sqrt{V_{i_{t_{1}}} V_{i_{t_{2}}}}+\left(\beta_{0_{t_{1}}}^{2}+V_{i_{t_{1}}}\right)\left(\beta_{0_{t_{2}}}^{2}+V_{i_{t_{2}}}\right)-\left(C_{i_{t_{1} t_{2}}}+\beta_{0_{t_{1}}} \beta_{0_{t_{2}}}\right)^{2} \tag{S6.8}
\end{equation*}
$$

For mathematical derivation see Text S4. A simulated example is described in Supplementary Texts S7; we provide R-code in Supplementary Text S8 and (future updates) on Github (https://github.com/YimenAraya-Ajoy/SelectionBias).

## Mean-of-squares vs. Square-of-means

Above, we propose to estimate quadratic selection gradients by fitting the squared term of the focal trait $\left(t_{h i}^{2}\right)$ as a response variable. Doing so assumes that the variance among-individuals in means of their squared trait values $\left(\overline{t_{l}^{2}}\right)$ approximates the true among-individual variance in the square of individual-specific trait values ( $\bar{t}_{i}^{2}$ ) of actual interest. Statistical simulations validated this assumption by demonstrating that the proposed multivariate mixed-effect model formulation produced unbiased estimates of the among-individual variance in squared values of individual-specific trait values.

We used the following simulation approach. We started by drawing individual-specific trait values $\left(t_{i}\right)$ from a normal distribution with a mean $(\bar{t})$ equal to zero and $V_{i_{\mathrm{t}}}=3$. We then simulated 3 phenotypic observations for each of 800 individuals by adding an observationspecific error (drawn from a normal distribution with zero-mean and variance $V_{e_{\mathrm{t}}}$ ). Next, we estimated the among-individual variance in the squared values in three different ways. (1) We squared the values of each observation, then calculated a mean value for each individual using all its squared values $\left(\overline{t_{l}^{2}}\right)$, and finally, calculated the among-individual variance in this metric (among-individual variance in "mean-of-squared values"; Fig. S6). (2) We calculated the mean trait value over all observations per individual, squared this value $\left(\bar{t}_{i}^{2}\right)$, and then calculated the among-individual variance in this metric (among-individual variance in "square-of-mean value"; Fig. S6). (3) We squared the values of each observation and fitted this variable $\left(t_{h i}^{2}\right)$ as a response variable into a mixed-effects model with individual fitted as a random effects, and estimated the among-individual variance of this metric ("mixed-model estimate"; Fig. S7). We applied these simulations for two values of repeatability by setting $V_{e_{\mathrm{t}}}=\frac{\left(V_{i_{\mathrm{t}}}-R_{t}\right)}{R_{t}}$ using procedures detailed in Supplementary Texts S7 and S8. We repeated this procedure 100 times for both types of repeatability ( $R_{t}=0.3$ and $R_{t}=0.7$ ).


Fig. S6. The among-individual variance in squared values of a focal trait estimated in three different ways. The dashed line represents the true (simulated) among-individual variance in the square of individual-specific values.

Results show that the among-individual variance calculated using the mean of squares (white bars), as well as the among-individual variance calculated using the square of means (light-grey bars), overestimated the true among-individual variance in squared values of simulated individual-specific trait values (dotted line) for both levels of repeatability (Fig. S6). By contrast, the proposed mixed-effects model solution produced unbiased estimates of the true among-individual variance in trait values.

## Supplementary Text S7

Linear selection analysis
We used simulations to assess, first, whether classic approaches produced attenuated estimates of linear selection gradients, and second, whether the proposed solutions (the application of corrections (Table 1), multivariate mixed-models, or errors-in-variables models would address this problem (for Results, see Table S7). We first studied a scenario where the absolute fitness (W) of individual $i$ was a function $\left(b_{1}\right)$ of its true mean-centred trait value $\left(t_{i}\right)$ (in its natural scale; e.g., cm ) plus an individual-specific stochastic environmental effect $\left(e_{i}\right)$ with a variance of $1\left(V_{e_{\mathrm{W}}}=1\right)$.
$\mathrm{W}_{i}=b_{1} t_{i}+e_{i}$
The individual-specific values $\left(t_{i}\right)$ were drawn from a normal distribution with a mean $(\bar{t})$ equal to zero and among-individual variance $\left(V_{i_{\mathrm{t}}}\right)$ defined below. We then simulated 3 phenotypic observations for each of 800 individuals by adding an observation-specific error drawn from a normal distribution with zero-mean and residual variance $\left(V_{e_{\mathrm{t}}}=\frac{V_{i_{\mathrm{t}}}}{R_{t}}-V_{i_{\mathrm{t}}}\right)$ three separate times to each $t_{i}$ to produce the three measurements. As in the Main Text, the expected standardized selection gradient $\beta_{1}$ equalled $b_{1} \frac{\sqrt{V_{i_{t}}}}{\overline{\mathrm{~W}}}$, where $V_{i_{\mathrm{t}}}=3, b_{1}=0.346$, and $\overline{\mathrm{W}}=2$. Thus, $\beta_{1}=0.3$. We ran simulations with $\left(R_{t}\right)$ equal to 0.3 and 0.7 by varying $V_{e_{\mathrm{t}}}=\frac{V_{i_{\mathrm{t}}}}{R_{t}}-V_{i_{\mathrm{t}}}$. We used $\mathrm{n}=100$ replicate studies per level of repeatability. Following the generation of each full dataset (with $n$ $=2400$ data points per simulation), we generated two sub-sets of data. The first subset contained one randomly drawn trait value (of the three produced) per individual. The second subset contained one mean value per individual calculated using all three observations. Fitness was transformed into relative fitness and the trait transformed into standard deviation units for the two sub-sets, where the standardization was applied after calculating trait means for the second subset (for rational, see Text S5); no transformations were applied to the full dataset. Subsequently, we ran four analyses. First, we estimated the standardized linear selection gradient using a linear regression, fitting the standardized trait as a predictor of relative fitness, on the sub-set containing one random observation per individual. Second, we applied the latter approach using the mean value per individual. Third, we ran a bivariate mixed-model with random intercepts for individual identity on the full dataset, fitting the mean-centred trait and absolute fitness as the two response variables, and estimated the standardized linear selection gradient using Eqn. 11 (Main Text). We fitted the multivariate mixed-effects models in a Bayesian framework using MCMCglmm (Hadfield 2010) in the R environment ( R -Core-Team 2020). Finally, using RStan, we ran an errors-in-variables models. For all approaches, we calculated estimation bias as the difference between the observed standardized selection gradient minus the simulated standardized selection gradient divided by the simulated standardized selection gradient. We provide R-code in Supplementary Text S8 and (future updates) on Github (https://github.com/YimenAraya-Ajoy/SelectionBias).

Estimates of standardized linear selection gradients based on the first subset, containing one randomly drawn trait value of the three produced per individual, were expected to be attenuated by $\sqrt{R_{t}}=\sqrt{\frac{V_{i_{t}}}{V_{i_{t}}+V_{e_{t}}}}$ (Eqn. S2.6). Estimates of standardized linear selection gradients based on the second subset, containing one mean value per individual calculated using all three observations, were instead expected to be attenuated by $\sqrt{\frac{V_{i_{t}}}{V_{i_{t}}+\frac{V_{e}}{}+}}$ (see Text S5), where $n$ represents the number of observations per individual equal to three. As a follow-up analysis, we fitted a univariate mixed-effects model with random intercepts for individual identity to estimate $V_{i_{t}}$ and $V_{e_{t}}$ from the full dataset. We then corrected the standardized linear selection gradient estimated for the first subset by dividing it by $\sqrt{R_{t}}$; the estimate for the second subset was instead divided by $\sqrt{\frac{V_{i_{t}}}{V_{i_{t}}+\frac{V_{e_{t}}}{n}}}$. This procedure enabled us to assess whether corrections applied to published data based on knowledge of trait repeatability could produce unbiased estimates.

## Quadratic selection analysis

We expanded our simulation to study how each approach (detailed above) performed when applied to estimate standardized quadratic selection gradients. We did so by expanding Eqn. S8.1 to include the effect of the quadratic component of the focal trait on absolute fitness $\left(b_{2}\right)$ :
$\mathrm{W}_{i}=b_{1} t_{i}+b_{2} t_{i}^{2}+e_{i}$
The expected value of $\beta_{1}$ equalled $b_{1} \frac{\sqrt{V_{i_{t}}}}{\overline{\mathrm{~W}}}$. We set $V_{i_{\mathrm{t}}}=3, b_{1}=2.19$, and $\overline{\mathrm{W}}=2$. Thus, $\beta_{1}=$ 1.90. As in Eqn. S6.5, the expected value of $\gamma_{11}$ equalled $2 b_{11} \frac{\sqrt{V_{i_{t^{2}}}}}{\overline{\mathrm{~W}}}$. As $V_{i_{t^{2}}}=2 V_{i_{t}}^{2}+4 V_{i_{t}} \mu_{t}^{2}$ (Eqn. S3.10), $\gamma_{11}$ thus equalled $2 b_{11} \frac{\sqrt{2 V_{i_{t}}^{2}+4 V_{i_{t}} \mu_{t}^{2}}}{\overline{\mathrm{~W}}}$. We set $b_{2}=-0.14$ and $\mu_{t}=0$, thus $\beta_{2}=-0.3$. As detailed above, we ran simulations with $\left(R_{t}\right)$ equal to 0.3 and 0.7 by varying $V_{e_{\mathrm{t}}}=\frac{V_{i_{\mathrm{t}}}}{R_{t}}-V_{i_{\mathrm{t}}}$. We provide R-code in Supplementary Text S 8 and (future updates) on Github (https://github.com/YimenAraya-Ajoy/SelectionBias).

Estimates of standardized quadratic selection gradients based on the first subset, containing one randomly drawn trait value of the three produced per individual, were expected to be attenuated by $\sqrt{R_{t^{2}}}=R_{t}$ (Eqn. S3.12) because we pragmatically mean-centred the trait prior to analysis. Estimates of standardized quadratic selection gradients based on the second subset, containing one mean value per individual calculated using all three observations, were instead expected to be attenuated by $\frac{V_{i_{t}}}{V_{i_{t}}+\frac{V_{e}}{}}$ (instead of $R_{t}$; see above). As a follow-up analysis, we fitted a univariate mixed-effects model that had as a response variable $t$ and random intercepts for individual identity. We then corrected the standardized quadratic selection gradient estimated for the first subset by dividing it by $R_{t}=\frac{V_{i_{t}}}{V_{i_{t}}+V_{e_{t}}}$; the estimate for the second
subset was instead divided by $\frac{V_{i_{t}}}{V_{i_{t}}+\frac{e_{e_{t}}}{n}}$. This procedure enabled us to assess whether corrections applied to published data based on knowledge of among- and within-individual variances and trait means could produce unbiased estimates.

## Correlational selection analysis

Finally, we expanded our simulation to study how each approach (detailed above) performed when applied to estimate standardized correlational selection gradients. We did so by expanding Eqn. S 8.2 to include the linear and quadratic effects of two focal traits $\left(t_{1}, t_{2}\right)$, as well as their interaction, on absolute fitness:
$\mathrm{W}_{i}=b_{1} t_{1_{i}}+b_{11} t_{1_{i}}^{2}+b_{2} t_{2_{i}}+b_{22} t_{2_{i}}^{2}+b_{12} t_{1_{i}} t_{2_{i}}+e_{i}$
For each trait $\left(t_{1}, t_{2}\right)$, expected values for standardized linear $\left(\beta_{1}, \beta_{2}\right)$ and quadratic ( $\beta_{11}, \beta_{22}$ ) selection gradients were set as detailed for the linear and quadratic selection examples above.
The expected value of the correlational selection gradient $\left(\gamma_{12}\right)$ equalled $b_{12} \frac{\sqrt{V_{i_{1} t_{2}}}}{\overline{\mathrm{~W}}}$ (Eqn. 18), where $V_{i_{t_{1} t_{2}}}=C_{i_{t_{1} t_{2}}}^{2}+2 \mu_{t_{1}} \mu_{t_{2}} \sqrt{V_{i_{t_{1}}} V_{i_{t_{2}}}}+\left(\mu_{t_{1}}^{2}+V_{i_{t_{1}}}\right)\left(\mu_{t_{2}}^{2}+V_{i_{t_{2}}}\right)-\left(C_{i_{t_{1} t_{2}}}+\mu_{t_{1}} \mu_{t_{2}}\right)^{2}$ (Eqn. S4.5). We provide R-code in Supplementary Text S 8 and (future updates) on Github (https://github.com/YimenAraya-Ajoy/SelectionBias).

Estimates of standardized correlational selection gradients based on the first subset (one randomly drawn trait value of the three produced per individual) were expected to be attenuated by $\sqrt{R_{t_{1} t_{2}}}$ (Eqn. S4.7). Estimates of standardized correlational selection gradients based on the second subset (containing one mean value per individual calculated using all three observations) were instead expected to be attenuated by $\sqrt{\frac{V_{i_{1}} V_{i_{t_{2}}}}{V_{p_{\overline{\bar{T}_{1}}} p_{\bar{t}_{2}}}} \sqrt{\frac{r_{i_{t_{1} t_{2}}}^{2}+1}{r_{\bar{t}_{\bar{t}_{1}} \bar{t}_{2}}^{2}}+1} \text { (Text S5). Our simulations }{ }^{2}}$ assumed a zero correlation between the traits such that the latter attenuation equated $\sqrt{\frac{v_{t_{t_{1}}} V_{i_{t_{2}}}}{V_{p_{\bar{t}_{1}}} V_{p_{\bar{t}_{2}}}}}$ while $\sqrt{R_{t_{1} t_{2}}}=\sqrt{R_{t_{1}} R_{t_{2}}}$ (S4.9). As a follow-up analysis, we therefore two univariate mixedeffects model, with the traits were fitted as response variables, with random intercepts for individual identity on the full simulated dataset. We then corrected the standardized correlational selection gradient estimated for the first subset by dividing it by $\sqrt{R_{t_{1}} R_{t_{2}}}$; the estimate for the second subset was instead divided by $\sqrt{\frac{v_{t_{t_{1}}} V_{i_{t_{2}}}}{V_{\bar{t}_{1}} V_{\bar{t}_{t_{2}}}}}$. This procedure enabled us to assess whether corrections applied to published data based on knowledge of trait means and among- and within-individual correlations between traits could produce unbiased estimates.

Table S7. Estimates of accuracy and precision in linear ( $\beta_{1}$ ), quadratic ( $\gamma_{11}$ ), and correlational $\left(\gamma_{12}\right)$ selection gradients derived from regression models fitting one observed trait value or a mean of three observed trait values, multivariate mixed-effects models, and errors-in-variables models. We also show accuracy and precision after applying corrections to regressions. We calculated bias (i.e., inaccuracy) as the difference between estimated minus true standardized gradients, divided by the true gradient. This produced a mean percentage (upward/downward) bias. The coefficient of variation (CV) among 100 datasets simulated for a given scenario was used to measure imprecision. Estimates are provided for two levels of trait repeatability (R).

| Model | R | \%Bias <br> $\beta_{1}$ | CV <br> $\beta_{1}$ | \%Bias <br> $\gamma_{11}$ | CV <br> $\gamma_{11}$ | \%Bias | CV |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0.3 | -45.04 | 0.07 | -70.21 | -0.64 | -74.63 |
| $\gamma_{12}$ |  |  |  |  |  |  |  |
| 1 obs | 0.7 | -16.02 | 0.05 | -33.13 | -0.25 | -31.05 | 0.23 |
| 1 obs | 0.3 | -24.93 | 0.05 | -42.58 | -0.30 | -49.35 | 0.36 |
| Mean of 3 obs | 0.7 | -5.97 | 0.04 | -15.03 | -0.14 | -14.87 | 0.15 |
| Mean of 3 obs | 0.3 | 0.85 | 0.06 | 1.32 | -0.65 | -1.92 | 0.86 |
| 1 obs corrected | 0.7 | 0.45 | 0.04 | -3.93 | -0.24 | 1.16 | 0.24 |
| 1 obs corrected | 0.3 | 0.46 | 0.04 | 2.78 | -0.31 | -4.88 | 0.36 |
| Mean of 3 corrected | 0.7 | 0.56 | 0.04 | -2.98 | -0.14 | -1.82 | 0.16 |
| Mean of 3 corrected | 0.3 | 2.22 | 0.06 | -1.10 | -0.77 | -7.02 | 1.61 |
| Multivariate mixed model | 0.6 |  |  |  |  |  |  |
| Multivariate mixed model | 0.7 | 0.66 | 0.04 | -2.75 | -0.20 | -2.61 | 0.21 |
| Errors-in-variables model | 0.3 | 0.30 | 0.05 | 0.87 | -0.13 | -0.07 | 0.27 |
| Errors-in-variables model | 0.7 | 0.42 | 0.04 | -0.25 | -0.10 | -1.58 | 0.15 |

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