Simulations of toroidal Alfven eigenmode excited by fast ions on the Experimental Advanced Superconducting Tokamak

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Abstract

Kinetic-MagnetoHydroDynamic (MHD) hybrid simulations are carried out to study fast ion driven toroidal Alfvén eigenmodes (TAEs) on the Experimental Advanced Superconducting Tokamak (EAST). The first part of this article presents the linear benchmark between two kinetic-MHD codes, namely MEGA and M3D-K, based on a realistic EAST equilibrium. Parameter scans show that the frequency and growth rate of TAE given by the two codes agree with each other. The second part of this article discusses the resonance interaction between TAE and fast ions simulated by MEGA code. The results show that the TAE exchanges energy with the co-current passing particles with parallel velocity $\left|v_{\|}\right| \approx V_{A0}/3$ or $\left|v_{\|}\right| \approx V_{A0}/5$, where V_{A0} is the Alfvén speed on the magnetic axis. The TAE destabilized by the counter-current passing ions is also analyzed and found to have much smaller growth rate than the co-current ions driven TAE. The reason for this is found to be that the overlap region of the TAE spatial location and the counter-current ion orbits is narrow and thus the wave-particle energy exchange is not efficient.

I. INTRODUCTION

Fast ions in tokamaks produced by fusion reactions, neutral beam injection (NBI) and RF heating can excite toroidal Alfvén eigenmodes (TAEs), [1–8], which can in turn enhance the transport of the fast ions[9–16]. TAEs have been widely observed in experiments[17–19] and a great deal of numerical simulations have been performed to understand the interaction between TAEs and fast ions [20–24]. Several numerical models based on different physical models have been established: the gyro-fluid model [25], the gyro/drift-kinetic MagnetoHydroDynamic (MHD) hybrid model [26–29] and the fully gyrokinetic model [30–32]. In the kinetic-MHD hybrid model, the main plasmas are described by the MHD model and the fast ions by the gyro/drift-kinetic model. The MEGA [27] and M3D-K [33] codes are two of the many codes based on the kinetic-MHD hybrid model. Both of MEGA code [13, 34, 35] and M3D-K code [36–39] have been widely used to investigate Alfvén eigenmodes (AEs) and energetic particles modes (EPMs) in many tokamaks. Recently, both of the codes are used to investigate AEs and EPMs in the Experimental Advanced Superconducting Tokamak (EAST). Therefore, a benchmark study between the two codes based on the EAST equilibrium is desired. The first part of this article presents the linear benchmark between these two codes using a realistic equilibrium from the EAST discharge #38300@3900 ms. The fast ions generated by the deuterium NBI on EAST are described by an anisotropic slowing down distribution in both of the codes. In the typical parameter regime of EAST fast ions, the mode excited is found to be a TAE with $|n| = 1$ and $m = 1, 2$, where m and n are the poloidal and toroidal mode number, respectively. The two-dimensional mode structures on the poloidal plane calculated by MEGA code and M3D-K code are in agreement with each other. Parameter scans show that the frequency and growth rate of the TAE given by the two codes agree with each other. The parameter scans of the TAE growth rate over

the birth velocity and central pitch angle of the fast ions show a peak near a particular value. To better explain this, the second part of this article discusses the resonance condition between TAE and fast ions. The results show that the TAE exchanges energy with the co-current passing particles with parallel velocity $\left|v_{\|}\right| \approx V_{A0}/3$ or $\left|v_{\|}\right| \approx V_{A0}/5$, where V_{A0} is the Alfvén speed on the magnetic axis. The resonant particles with $\left|v_{\|}\right| \approx V_{A0}/3$ are dominant. To further verify the role of $\left|v_{\|}\right| \approx V_{A0}/3$ co-current passing particles in exciting the TAE, we compare the TAE excited by fast ions with different birth velocities and injection angles but with approximately the same parallel velocity $\left|v_{\|}\right| \approx V_{A0}/3$. The results indicate that the growth rate of the excited TAE remains the same, which shows the dominant role of the $\left|v_{\|}\right| \approx V_{A0}/3$ resonant particles. This also explains why there is a peak in the dependence of the growth rate on the fast ions birth velocity and central pitch angle. The TAE destabilized by the counter-current passing ions is also analyzed and found to have much smaller growth rate than the co-current ions driven TAE. One of the reasons for this is found to be that the overlap region of the spatial location of the TAE and the counter-current ion orbits is narrow and thus the wave-particle energy exchange is not efficient.

The remainder of this article is organized as follows: Sec. II briefly reviews the physical models of MEGA and M3D-K codes. The thermal plasma parameters used in this work are described in Sec. III. The fast ion distribution function is described in Sec. IV. The comparison of the results given by the two codes is presented in Sec. V. Sec. VI discusses the resonance interaction between TAE and fast ions simulated by MEGA code. Sec. VII is a brief summary.

II. PHYSICAL MODELS

Both of MEGA code [27] and M3D-K code [33] describe the thermal plasma as a single fluid by using the nonlinear full MHD equations. The energetic particles (EPs) are described by drift-kinetic or gyrokinetic equations (in this work, drift kinetic model is chosen for both the codes). In MEGA code, the EP effects are included in the MHD momentum equation via the EP current (usually called current coupling scheme). In M3D-K code, the EP effects are included in the momentum equation via the EP pressure (called pressure coupling scheme).

III. THERMAL PLASMA PARAMETERS

The equilibrium used in MEGA is reconstructed by the EFIT code [40] based on the experimental diagnostic data of EAST discharge #38300@3900 ms. The flux surface configuration and the simulation box used by MEGA are plotted in Fig. 1(a). The profiles of electron number density n_e, plasma pressure P, and the safety factor q are plotted in Fig. 1(b). The equilibrium used by M3D-K code is generated from the VMEC code [41] by using the pressure and safety factor profiles reconstructed by EFIT. The equilibrium generated by VMEC is up-down symmetric.

IV. FAST ION DISTRIBUTION

The fast ions in both the codes are described by the following anisotropic slowing down distribution:

$$f_{\mathrm{eq}}\left(\overline{\psi}_p, v, \Lambda, \sigma\right) = C \exp\left(-\frac{\overline{\psi}_p}{\psi_{\mathrm{scale}}}\right) \frac{1}{v^3 + v_{\mathrm{crit}}^3} \frac{1}{2} \operatorname{erfc}\left(\frac{v - v_{\mathrm{birth}}}{\Delta v}\right) \exp\left(-\frac{(\Lambda - \Lambda_0)^2}{(\Delta\Lambda)^2}\right) \cdot H\left(-\sigma\right), \tag{1}$$

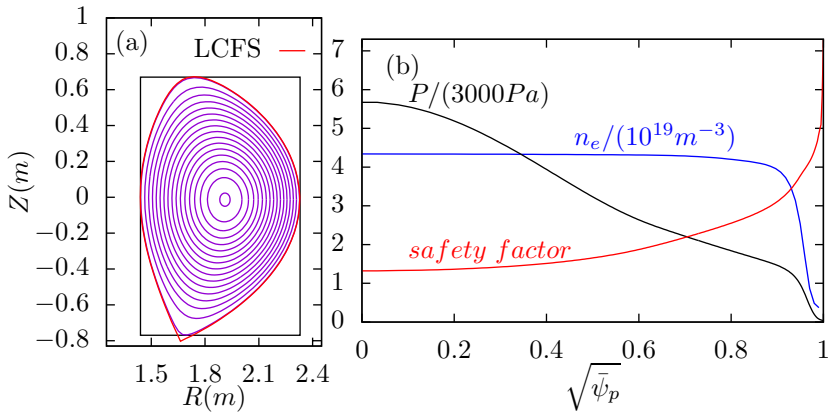

Figure 1. (a) Magnetic surface shape of EAST discharge 38300@3900 ms. The Last-Closed-Flux-Surface (LCFS) is indicated. The simulation box used in MEGA code on the poloidal plane is also indicated, which is a rectangle with $R_{\min} < R < R_{\max}$ and $Z_{\min} < Z < Z_{\max}$, where $R_{\min}$, $R_{\max}$, $Z_{\min}$, and $Z_{\max}$ are the extreme points on the flux surface with $\sqrt{\overline{\psi}_p} = 99\%$, where $\bar{\psi}_p$ is the normalized poloidal magnetic flux. (b) Radial profiles of the thermal plasma pressure, safety factor, and electron number density. The safety factor and electron number density at the magnetic axis are $q_0 = 1.32$ and $n_{e0} = 4.2 \times 10^{19} m^{-3}$, respectively. The toroidal magnetic field at the magnetic axis is $B_{\phi 0} = +1.64T$. The toroidal plasma current is $I_{p\phi} = -398\,\mathrm{kA}$. Here (R, ϕ, Z) is the right-handed cylindrical coordinates with R being the major radius, ϕ being the usual toroidal angel, and Z being the vertical coordinate.

where C is a constant determining the stored energy of fast ions; $\overline{\psi}_p$ is the normalized poloidal magnetic flux; ψ_{scale} is a quantity characterizing the radial gradient of fast ions; v is the velocity of fast ions; v_{crit} is the critical velocity for the collisional friction of fast ions with thermal electrons and ions being equal [19]; v_{birth} is the neutral beam injection velocity; Δv is a small velocity (compared with v_{birth}), which is used to set the cutoff width near v_{birth}; $\Lambda = \mu B_0/\varepsilon$ is the normalized magnetic moment with

μ and ε being the magnetic moment and kinetic energy of fast ions and B_0 being the magnetic filed strength at the magnetic axis; Λ_0 and $\Delta\Lambda$ characterize the peak location and the width of the distribution over the pitch angle, respectively; $H(\sigma)$ is the Heaviside step function ($H(\sigma) = 0$ for $\sigma < 0$ and $H(\sigma) = 1$ for $\sigma > 0$), $v_\parallel = \boldsymbol{v} \cdot \boldsymbol{b}$ is the parallel velocity of fast ions, where, $\boldsymbol{b} = \boldsymbol{B}/|\boldsymbol{B}|$ with $\boldsymbol{B}$ being the magnetic field, $\sigma = \text{sign}\left(v_\parallel\right)$ with $\sigma = -1$ and $+1$ corresponding to the co-current and counter-current injection, respectively (the toroidal magnetic field and the plasma current are in the opposite direction for the equilibrium used in this work).

In this work, we fix the following parameters in both the codes: $\psi_{\text{scale}} = 0.3$; $v_{\text{crit}} = 0.62V_{A0}$, which corresponds to the critical velocity with electron temperature $T_e = 2k\,\text{eV}$, $V_{A0} = 3.837 \times 10^6 m/s$ is the Alfvén velocity at magnetic axis; the cutoff width near the beam velocity is chosen as $\Delta v = 0.15V_{A0}$. Except for the parameters scanning sections, typical EAST NBI fast ion parameters are used: the injected beam velocity is chosen as $v_{\text{birth}} = 0.72V_{A0}$, corresponding to a deuteron with kinetic energy of 80 keV, which is the maximum energy of a deuteron generated from the NBI on EAST; the central pitch angle variable Λ_0 is chosen as $\Lambda_0 = 0.68$; the expansion width of the distribution over Λ is chosen as $\Delta\Lambda = 0.1$; $\beta_{h0} = 0.5\%$.

In both MEGA and M3D-K simulations, the electrical resistivity η is set to be zero. In MEGA simulations, the artificial viscosity ν is chosen as $\nu = 10^{-6}R_0V_{A0} = 7.23m^2/s$, here R_0 is the major radius of the geometrical center of the simulation box. In M3D-K simulations, ν is chosen as $\nu = 10^{-5}aV_{A0} = 16.89m^2/s$, where a is the minor radius ($a = 0.44m$). The value of the viscosity is chosen to make the growth rate given by the two codes approximately agree with each other for the fast ions distribution with $\beta_{h0} = 0.5\%$, $\Lambda_0 = 0.68$ and $E_{\text{birth}} = 80\,\text{keV}$.

The numbers of grid points used in MEGA code are $(128 \times 16 \times 128)$ for cylindrical coordinates (R, ϕ, Z), and 5.2×10^5 markers are used in the linear parameter scans in Sec. V and Sec. VI B, while 4×10^6 particles are used in analyzing the

resonance condition between TAE and fast ions in Sec. VI A to reduce the numerical noise. The convergence over the marker number used in the simulation has been verified. The numbers of grid points used in M3D-K are $(101 \times 12 \times 101)$ for cylindrical coordinates (R, ϕ, Z), and 4×10^6 particles are used in the simulations.

V. BENCHMARK BETWEEN MEGA CODE AND M3D-K CODE

A. Identification of TAE

To analyze the MEGA simulation results, we use magnetic flux coordinates (ψ, θ, ϕ), where ψ is magnetic surface label (in this article, ψ is chosen as $\psi = \sqrt{\overline{\psi}_p}$, where $\overline{\psi}_p$ is the normalized poloidal magnetic flux), ϕ is the usual toroidal angle, and θ is chosen to make magnetic field lines straight on (θ, ϕ) plane. The perturbations are expanded in terms of the basis function $\exp\left[i\left(n\phi + m\theta - \omega t\right)\right]$. The results show that the dominant toroidal harmonic is $n = -1$. The mode propagates toroidally in the co-current direction, which is consistent with the general rules for the propagation direction of the ion-driven AEs in tokamaks [42]. Figures 2(a) and (b) plot the radial profiles of the sine and cosine parts of various poloidal harmonics of the $n = -1$ component of the perturbed poloidal magnetic field B_θ, which shows that the harmonics with $m = 1$ and $m = 2$ are dominant and the radial location of the dominant magnetic field perturbation is localized within $\psi = 0.4$. Figure 2(c) plots the time evolution of the frequency of $m/n = 1/-1$ component of B_θ in the linear stage, which shows that the mode frequency is about 96kHz. Figure 2(d) plots the $n = -1$ Alfvén continua calculated by a MHD eigenvalue code [43], which shows that the mode is within the TAE gap formed due to the coupling of the $m = 1, 2$ harmonics. Based on these observations, the mode destabilized in the simulation is identified as a TAE.

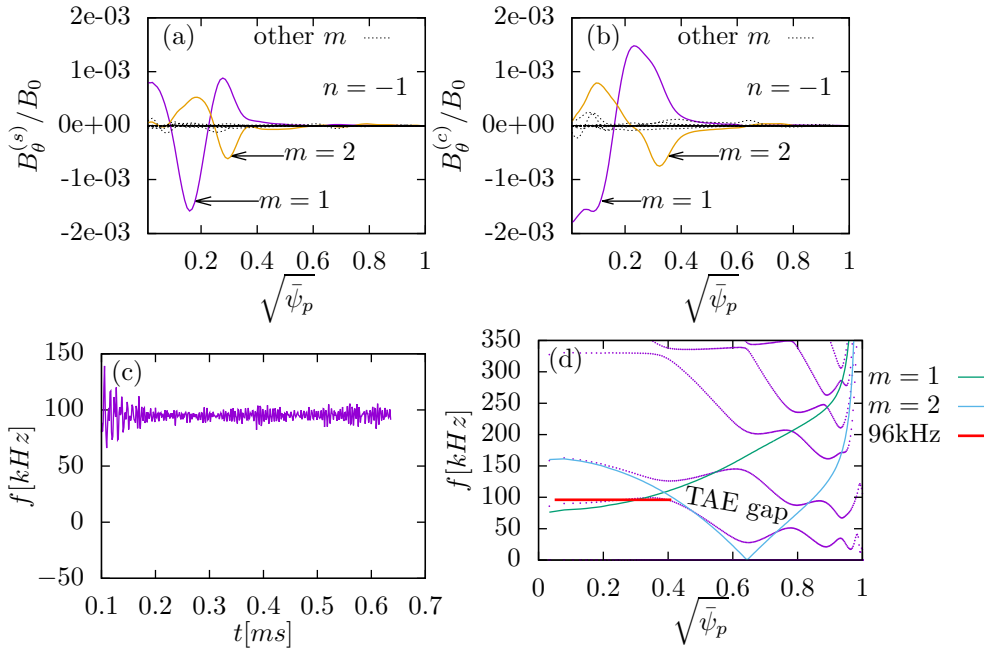

Figure 2. Radial profiles of the sine (a) and cosine (b) parts of various poloidal harmonics of the $n=-1$ component of the perturbed poloidal magnetic field B_θ in the linear stage. (c) Time evolution of the frequency of $m/n=1/-1$ harmonic of B_θ. (d) The frequency (96 kHz) and radial width of the TAE plotted on the $n=-1$ Alfvén continua. The $m=1$ and $m=2$ Alfven continua in the cylindrical limit are also plotted. The continua are computed by using an ideal MHD eigenvalue code GTAW[43].

B. Comparisons of two-dimensional mode structures in M3D-K code and MEGA code

Figures 3(a) and (b) plot the two-dimensional mode structures in poloidal plane calculated by M3D-K code and MEGA code, respectively. Agreement is found between these two codes as to the dominant poloidal mode numbers ($m=1,2$ are the dominant poloidal mode numbers with $m=1$ component larger than $m=2$

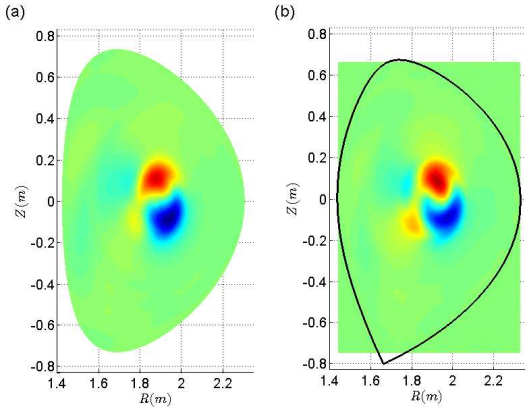

Figure 3. Contour of the toroidal electric field E_ϕ calculated by M3D-K code (a) and MEGA code (b) on the poloidal plane in the linear stage. Also plotted in figure (b) is the LCFS of the equilibrium used by MEGA code.

component, which is consistent with the results shown in Figs. 2(a) and (b)) and the spatial location of the mode on the poloidal plane.

C. Comparison of mode growth rate and frequency between MEGA and M3D-K code

Figures 4 plot the mode growth rate and frequency as functions of the fast ions on-axis beta value β_{h0}. The results indicate that the growth rate and frequency given by MEGA code and M3D-K code agree with each other for different values of β_{h0}. As is shown in Fig. 4(b), the mode frequency given by the two codes is a constant independent of the EP on-axis beta value. This is consistent with the previous conclusion that the mode is a TAE with frequency mainly determined by the main plasma.

Figures 5 compare the dependence of the TAE growth rate and real frequency on

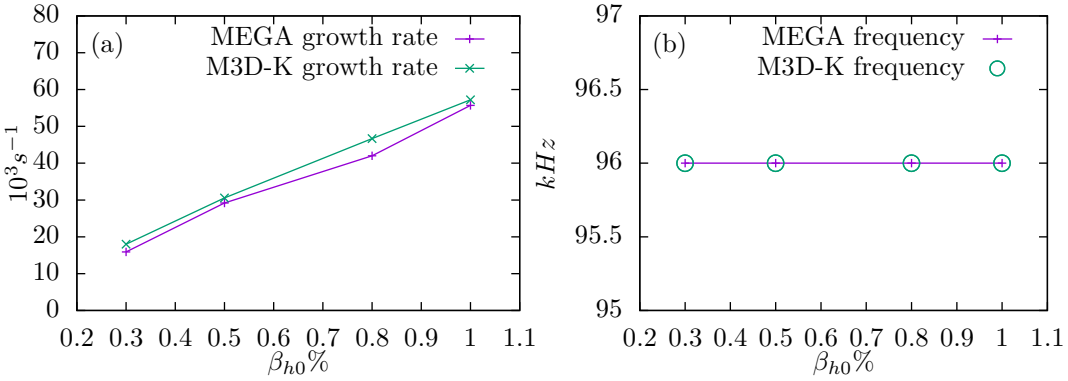

Figure 4. The TAE growth rate (a) and real frequency (b) as functions of fast ions on-axis beta value. Results from MEGA and M3D-K simulation are shown. The other fast ion parameters ($\Lambda_0 = 0.68$, $E_{\rm birth} = 80\,{\rm keV}$) are kept fixed in this parameter scan.

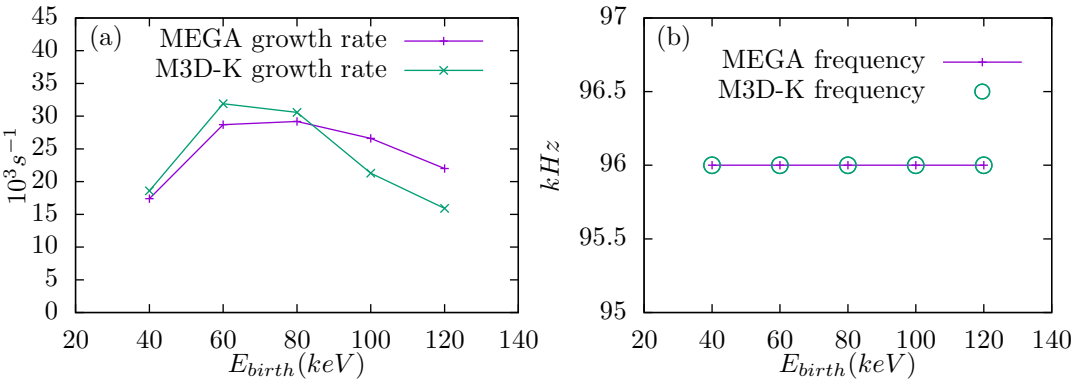

Figure 5. (a)The comparisons of the TAE growth rate (a) and frequency (b) calculated by MEGA code and M3D-K code for different beam injection energy $E_{\rm birth}$. The other parameters ($\Lambda_0 = 0.68$, $\beta_{h0} = 0.5\%$) are kept fixed in this parameter scan.

the beam injection energy $E_{\rm birth}$ calculated by the two codes. As is shown in Fig. 5(a), the dependence of the mode growth rate on $E_{\rm birth}$ calculated by these two codes shows qualitative agreement, with about 30% relative difference in the high injection energy region. Figure 5(b) shows, as expected, that the mode frequency calculated

by both the codes is a constant independent of $E_{\rm birth}$.

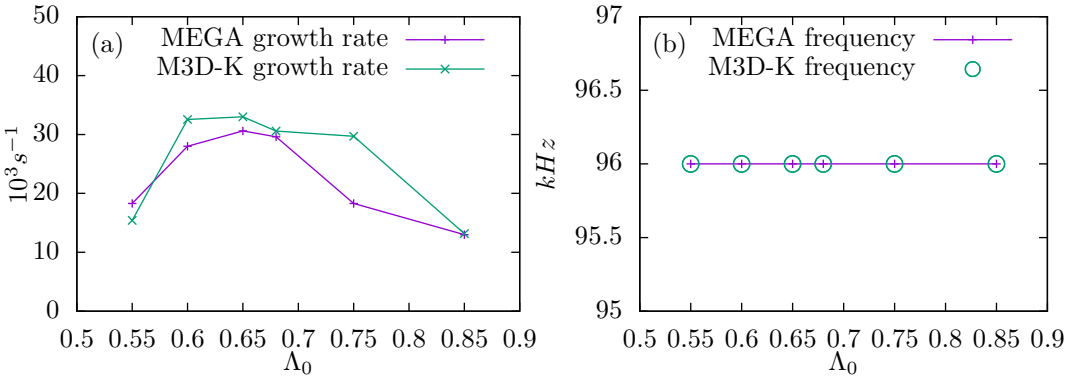

Figure 6. (a) The TAE growth rate (a) and frequency (b) as functions of the central pitch angle parameter Λ_0 calculated by MEGA code and M3D-K code. The other fast ion parameters ($\beta_{h0} = 0.5\%$, $E_{\rm birth} = 80\,{\rm keV}$) are kept fixed in this parameter scan.

Figures 6 plot the dependence of the mode growth rate and real frequency on the central pitch angle parameter Λ_0, which shows that the mode frequency and growth rate calculated by the two codes agree with each other.

In the parameter scans shown in both Fig. 5(a) and Fig. 6(a), there is a peak of the growth rate. The peak in Fig. 5(a) appears at $E_{\rm birth} = 80\,{\rm keV}$ with $\Lambda_0 = 0.68$ while the peak in Fig 6(a) appears at $\Lambda_0 = 0.65$ with $E_{\rm birth} = 80\,{\rm keV}$. Using the relation $\left|v_\parallel\right| = \sqrt{2\varepsilon\left(1 - \Lambda B/B_0\right)/m_D}$, where m_D is the mass of the fast ion, we find that the two peaks both correspond to $\left|v_\parallel\right| \approx V_{A0}/3$.

VI. MEGA SIMULATION RESULTS

A. Resonance interaction between TAE and fast ions

This section discusses the resonance interaction between TAE and fast ions simulated by MEGA code. In the δf particle simulation, large value of $|\delta f|$ in the phase

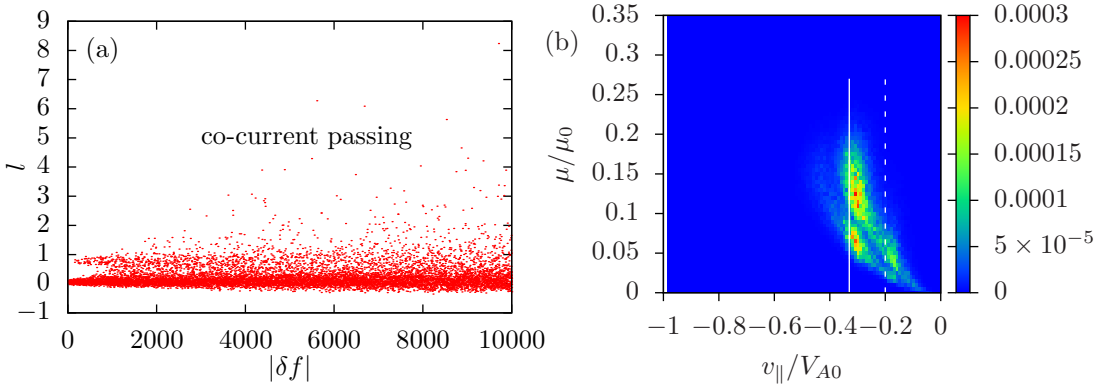

Figure 7. (a) The values of the resonance order l of the top 10000 markers with large value of $|\delta f|$. (b) Contour of averaged $|\delta f|$ on $(v_\parallel, \mu)$ plane in the linear stage of the mode evolution, where the solid white line indicates the region with $v_\parallel = -V_{A0}/3$ and white dot line indicates $v_\parallel = -V_{A0}/5$. Here $\mu_0 = m_D v_{A0}^2/(2B_0)$.

space usually indicates that the particles in that phase space region are having strong interaction with the wave. Therefore, to identify the particles that are resonant with the TAE, a simple method is to pick out those particles that have large value of $|\delta f|$. We pick out top 10000 particles with large value of $|\delta f|$ in the linear stage. To confirm that these particles are indeed resonant with the TAE, we calculate the toroidal and poloidal frequency ω_ϕ and ω_θ, of these markers and then examine how well the resonance condition is satisfied. The resonance condition of fast ions with a coherent mode is given by [44]

$$l = \frac{\omega - n\omega_\phi}{\omega_\theta} \tag{2}$$

where ω is the frequency of the coherent mode, n is the toroidal mode number, and l is called the resonance order in this paper and should be close to an integer if the particle is resonant with the mode. The values of the resonance order l for the top 10000 particles chosen above are plotted in Fig. 7(a), which shows that l is close to zero for most of the particles chosen above. This confirms that the resonance

condition is well satisfied by these particles, i.e. they are indeed resonant with the TAE.

We found 99% of the top 10000 particles are strongly passing particles. In this case, the resonance condition (2) can be further simplified. For a strongly circulating particle (i.e. the change of $v_\parallel$ during one poloidal period is small), neglecting the guiding-center orbit width, the poloidal period is approximated by $T_\theta = 2\pi R q/v_\parallel$, where R is the major radius and q is the safety factor. Thus the poloidal frequency ω_θ is written $\omega_\theta = 2\pi/T_\theta = v_\parallel/(qR)$. Similarly, the toroidal angular frequency is written as $\omega_\phi = v_\parallel/R$. Using these, the resonance condition (2) is written as

$$v_\parallel \left(n + \frac{l}{q}\right) = \omega R \tag{3}$$

On the other hand, the frequency and radial location of the TAE are approximately given by

$$\omega = \frac{V_{A0}}{2qR}, \tag{4}$$

and

$$q = \left|\frac{2m+1}{2n}\right|, \tag{5}$$

respectively. Substituting Eqs. (4) and (5) into Eq. 3 and using $n = -1$, we obtain

$$v_\parallel = \frac{V_{A0}}{2l - 2m - 1}. \tag{6}$$

For the present case with the resonance order $l = 0$ and dominant poloidal mode numbers $m = 1, 2$, equation (6) gives $v_\parallel = -V_{A0}/3$ and $v_\parallel = -V_{A0}/5$. This means that the particles with $v_\parallel = -V_{A0}/3$ or $v_\parallel = -V_{A0}/5$ are resonant with the TAE. This conclusion can be verified by examining the phase-space structure of δf. Figure 7(b) plots the contour (color-map) of the averaged $|\delta f|$ on the $(v_\parallel, \mu)$ plane, which shows that the region with $v_\parallel \approx -V_{A0}/3$ or $v_\parallel \approx -V_{A0}/5$ has larger value of δf, indicating that these particles are resonant with the TAE. Figure 7(b) also shows

that the resonant particles with $v_\parallel \approx -V_{A0}/3$ are dominant compared with those with $v_\parallel \approx -V_{A0}/5$. This is consistent with the fact that the amplitude of the $m = 1$ harmonic is larger than that of the $m = 2$ harmonic.

The above resonant condition can partially explain the dependence of the TAE growth rate on the fast ion parameters shown in Figs. 5(a) and 6(a). Both figures 5(a) and 6(a) show that the TAE growth rates reach a peak value near $\left|v_\parallel\right| \approx V_{A0}/3$, which is consistent with the conclusion that the TAE is mainly resonant with the particles with $\left|v_\parallel\right| \approx V_{A0}/3$. The parallel velocity of most passing fast ions in the distribution (1) is given by $v_\parallel \propto \sqrt{\varepsilon} \cdot \sqrt{1-\Lambda}$. With ε or Λ changing away from the value that corresponds to $\left|v_\parallel\right| \approx V_{A0}/3$, the fraction of the resonant particles is reduced. Then the TAE growth rate decreases correspondingly. To further verify this, three simulations with different values of Λ_0 and $E_{\rm birth}$ but with the same value of $v_\parallel$ are carried out. The results are shown in Fig. 8, which indicates that the TAE growth rate remains nearly unchanged in the three cases.

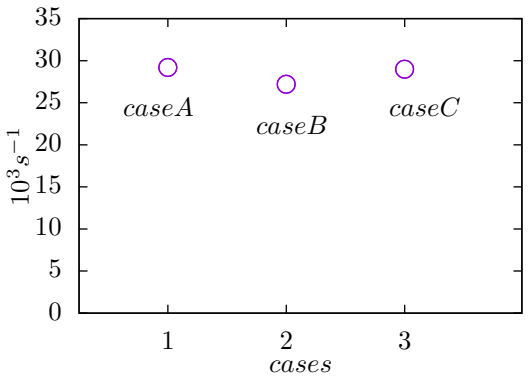

Figure 8. The TAE growth rate in three cases with different fast ion parameters calculated by MEGA code. Case A: $\Lambda_0 = 0.68$, $E_{\rm birht} = 80\,{\rm keV}$; Case B: $\Lambda_0 = 0.56$, $E_{\rm birth} = 56\,{\rm keV}$; case C: $\Lambda_0 = 0.37$, $E_{\rm birth} = 41\,{\rm keV}$. The parallel velocity $v_\parallel$ is approximately the same in the three cases.

B. Destabilization of TAE by counter-current passing fast ions

In the above, the TAE is excited by co-current passing fast ions. We also investigate the case with counter-current passing fast ions. We found the same TAE as above is also excited but the growth rate is much smaller compared with the case with co-current passing fast ions. The TAE growth rates of the two cases are compared in Fig. 9(b) at different values of fast ions beta, which shows that the growth rate of the TAE excited by counter-current fast ions is always smaller than that excited by the co-current fast ions. Figure 9(a) plots the typical orbits of co-current passing particle and counter-current passing particle on the poloidal plane. From Fig. 9(a), we can observe that the overlap region between the TAE and co-current passing fast ions is larger than the counter-current passing fast ions. Thus the interaction between the TAE and co-current passing fast ions can be stronger than the counter-current passing fast ions. This partially explains why the co-current fast ions driven TAE has larger growth rate that that of the counter-current fast ions.

Similar resonance condition analysis as above can be performed for the counter-current passing fast ions. Figure 10(a) plots the values of the resonance order l calculated by Eq. 2 for counter-current passing fast ions, which shows that $l \approx 3$ for most of the particles with large value of $|\delta f|$. The contour of the averaged $|\delta f|$ on $\left(v_{\parallel}, \mu\right)$ plane is plotted in Fig. 10(b), which shows that the fast ions with parallel velocity $v_{\parallel} \approx V_{A0}/3$ exchange energy with the TAE. This parallel velocity is consistent with the results calculated by Eq. 6 with $m = 1$ and $l \approx 3$.

VII. SUMMARY

This article presents a linear benchmark between two kinetic-MHD hybrid codes, MEGA and M3D-K, for the fast ions driven toroidal Alfvén eigenmodes in a realistic

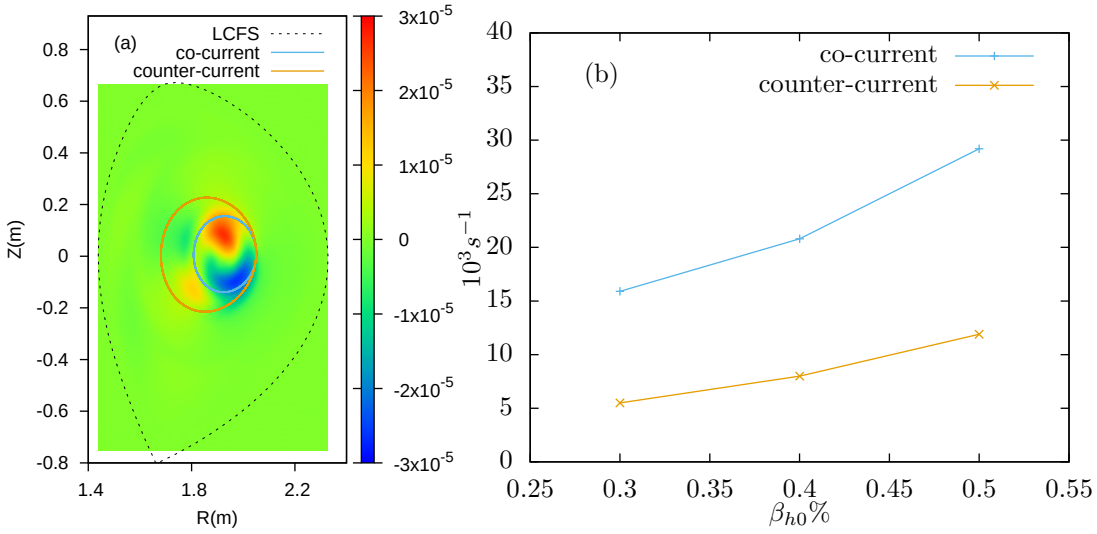

Figure 9. (a)The mode structure of the TAE calculated by MEGA code. Also plotted on (a) are typical orbits of co-current and counter-current passing particles with $E_{\rm birth} = 80\,{\rm keV}$, $\Lambda = 0.68$ and the birth location at $(R = 2.1m, Z = 0m)$ on the poloidal plane. (b) The dependence of the growth rate of the TAE destabilized by co-current and counter-current passing particles on fast ions on-axis beta value β_{h0}. The other parameters of the fast ion distribution are fixed ($E_{\rm birth} = 80\,{\rm keV}$, $\Lambda_0 = 0.68$).

EAST plasma. The results show good agreement between the two codes with respect to the dependence of the TAE growth rate and the real frequency on the fast ions on-axis beta β_{h0}, injection beam energy $E_{\rm birth}$ and central pitch angle parameter Λ_0. To better understand the details of the interaction between TAE and fast ions, a series of simulations are carried out by using MEGA code. The results show that the TAE are resonant with the co-current passing particles with parallel velocity $v_{\|} \approx -V_{A0}/3$ or $v_{\|} \approx -V_{A0}/5$. In addition, the TAE destabilized by the counter-current passing ions is also analyzed and found to have much smaller growth rate than that of the co-current fast ions driven TAE. One of the reasons for this is found to be that the

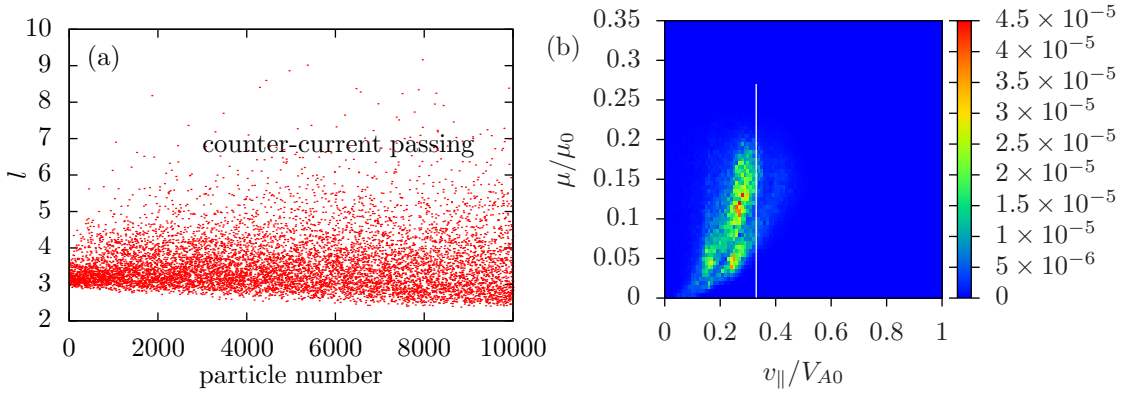

Figure 10. (a) The values of resonance order l of the top 10000 markers with a large value of $|\delta f|$. (b) Contour of averaged $|\delta f|$ on $\left(v_{\parallel}, \mu\right)$ plane in the linear stage of the mode evolution, where the white line indicates the location $v_{\parallel} = V_{A0}/3$.

counter-current passing fast ion orbits lie on the radial edge of the TAE and thus the wave-particle energy exchange is not efficient.

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