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Improved Automated CASH Optimization with Tree Parzen Estimators for Class Imbalance Problems

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Abstract—The imbalanced classification problem is very relevant in both academic and industrial applications. The task of finding the best machine learning model to use for a specific imbalanced dataset is complicated due to a large number of existing algorithms, each with its own hyperparameters. The Combined Algorithm Selection and Hyperparameter optimization (CASH) has been introduced to tackle both aspects at the same time. However, CASH has not been studied in detail in the class imbalance domain, where the best combination of resampling technique and classification algorithm is searched for, together with their optimized hyperparameters. Thus, we target the CASH problem for imbalanced classification. We experiment with a search space of 5 classification algorithms, 21 resampling approaches and 64 relevant hyperparameters in total. Moreover, we investigate performance of 2 well-known optimization approaches: Random search and Tree Parzen Estimators approach which is a kind of Bayesian optimization. For comparison, we also perform grid search on all combinations of resampling techniques and classification algorithms with their default hyperparameters. Our experimental results show that a Bayesian optimization approach outperforms the other approaches for CASH in this application domain.

Keywords—hyperparameter optimization, algorithm selection, imbalanced classification, CASH optimization

I. INTRODUCTION

The imbalanced classification problem has caught growing attention from both academic and industrial fields. Technically, any dataset with an unequal class distribution is imbalanced. However, only datasets with a significantly skewed distribution are traditionally regarded as imbalanced in the imbalanced learning domain [1]. Academic researchers aim to propose novel algorithms to handle imbalanced classification problems in different scenarios, e.g., resampling techniques and algorithm-level approaches, while industrial researchers focus on improving imbalanced classification performances for specific real-life applications, e.g., fault diagnosis or anomaly detection [2], [3].

The combination of resampling techniques and classification algorithms is the most commonly used approach for handling imbalanced data [4]. However, the No Free Lunch (NFL) theorem [5] prescribes that there is no universally best algorithm for all problems. This leads to a challenge for an imbalanced classification problem on how to choose the best model (i.e., a combination of a resampling method) and a classifier (the so-called model selection problem or algorithm selection problem [6]). Besides, both the resampling techniques and classification algorithms have their hyperparameters that need to be tuned in order to achieve better performance [7].

Therefore, two tasks have to be taken into account in this paper: model selection (MS) and hyperparameter optimization (HPO). Usually, these tasks are addressed separately and sequentially [8], [9], where the practitioner can choose to handle either task first. Commonly, practitioners proceed by tuning the hyperparameters for each modeling algorithm separately and then choosing the best model. However, this approach is considerably more expensive due to a high number of combinations operations. Alternatively, the practitioner can select a suitable model, by training all models with their default hyperparameters or based on some experience, and then tune the hyperparameters only for the best model. This approach might get stuck in a local optimum of the model that has been initially chosen, based on the default hyperparameter setting. On the other hand, instead of sequentially solving these problems, they can be combined into a single problem and solved at the same time. Such approach is commonly referred to as the Combined Algorithm Selection and Hyperparameter optimization (CASH) or Full Model Selection (FMS) [10] approach.

Approaches for tackling the CASH problem have been widely proposed in the machine learning domain, especially in the context of automated machine learning (AutoML), e.g., Auto-Weka [10], [11] and Auto-Sklearn [11], [12], TPOT [13], HyperOpt-Sklearn [14]. In addition, [8] demonstrated that the CASH approach is competitive with the sequential approach and requires less computational effort. However, the CASH approach has not been studied yet in detail in the context of learning from imbalanced data.

Hence, in this work, we introduce CASH in the context of optimizing the machine learning pipeline of combined classification algorithms and resampling techniques for the class imbalance problem. We are particularly interested in studying which optimization approach for handling the CASH problem yields the best classification performance. We experiment with two well-known approaches, Random search and Tree Parzen Estimators approach (TPE) which is a kind of Bayesian optimization, on a search space of 64 hyperparameters¹ of 5 classification algorithms (Support Vector Machines (SVM), Random Forest (RF), K-Nearest Neighbors (KNN), Decision Tree (DT) and Logistic Regression (LR)) and 21 choices of resampling techniques on a range of 44 imbalanced datasets.

Furthermore, we experiment with dropping the hyperparameter tuning and carrying out only the MS part, as sometimes done by practitioners. Our results suggest the inferiority of such approach and demonstrate that applying CASH optimization gives better performance, for all test cases considered. Moreover, we observe that the Bayesian optimization approach produces better results than Random search. Hence, we recommend using this approach for handling the CASH problem for the class-imbalanced classification problem.

The remainder of this paper is organized as follows. In Section II, the relevant background knowledge on imbalance classification and hyperparameter optimization are provided, and Section III lays out the experimental setup. Experimental results are discussed in Section IV. Finally, the paper is concluded, and further work is outlined in Section V.

II. BACKGROUND

In this section, we first provide a brief introduction to imbalanced classification (Section II-A), hyperparameter optimization approaches (Section II-B), and the CASH problem (Section II-C) studied in this paper.

A. Imbalanced Classification

The main problem in imbalanced classification is that the number of samples of one class is much lower than of the other classes [1]. Here, the one or more classes being underrepresented are called minority class(es) and the other class(es) are called majority classes.

It has been shown that both the data-level (resampling) approaches and algorithm-level approaches are efficient in handling class-imbalance problems [16]. The data-level approaches focus on producing balanced datasets based on the unbalanced original data, while the algorithmic-level approaches concentrate on adjusting classification algorithms to make them appropriate for imbalanced datasets. In the imbalanced learning domain, resampling techniques can be further divided into three groups: under-resampling, overresampling, and combine-resampling. Under-resampling balances the class distribution by removing majority samples, e.g., TomekLinks [17], while over-resampling balances the class distribution via producing synthetic minority samples, e.g., SMOTE [18]. The combine-resampling integrates both, removing the majority samples and creating synthetic minority samples in order to balance the class distribution, e.g., SMOTETomek [19].

Due to recent developments in data storage and management, it became possible for practitioners from industry and engineering to collect a large amount of data in order to extract knowledge and acquire hidden insights. An application example may be illustrated in the field of computational design optimization [20], where product parameters are modified to generate digital prototypes and the performances are usually evaluated through numerical simulations which often require minutes to hours of computation time. Here, some parameter variations (minority number of designs) would result in effective and producible geometric shapes, but the given constraints are violated in the final step of optimization. In this case, applying proper imbalanced classification algorithms to the design parameters could save computation time.

In the class imbalance domain, it is widely known that *accuracy* is a deceptive estimate of performance [7], [21]. Instead of *accuracy*, other metrics such as the area under the receiver operating characteristic (ROC) curve, F-measure, or geometric mean (GM) are commonly used to measure performance [22]. For comparison with previous studies [23], [24], we use GM as the performance evaluation metric, i.e.:

$$GM = \sqrt{TP_{rate} \cdot TN_{rate}} , \qquad (1)$$

where $TP_{rate} = \frac{TP}{TP+FN}$ and $TN_{rate} = \frac{TN}{FP+TN}$ are the true positive and true negative rate, respectively, with TP, TN, FN and FP denoting the number of true positive, true negative, false negative and false positive samples.

B. Hyperparameter Optimization

Hyperparameter optimization (HPO) has become increasingly important in the community of machine learning and optimization [25], [26]. In the context of optimization, HPO is generally viewed as a black-box optimization problem, which is aimed at finding the global optimum x^* of the hyperparameters, with respect to some real-valued loss function f, namely,

$$x^* = \arg\min_{x \in \chi} f(x) , \qquad (2)$$

where χ stands for the search space of hyperparameters. In the following paragraphs, we briefly introduce the HPO algorithms chosen in this study.

1) Grid search and Random search: Grid search is the most basic HPO algorithm. Given a set of hyperparameters, each of which has a (finite) set of values, we enumerate all combinations of these sets and create a list of all candidates. Grid search evaluates each of these candidates and chooses the best configuration among them – the number of function evaluations is precisely the number of configurations. However, practitioners are usually restricted by a limited computational budget, i.e., number of function evaluations, for HPO. Such limited budget is typically much smaller than the number of possible configurations to evaluate. Thus, limited budget restricts the applicability of grid search.

Unlike grid search which assesses all configurations, random search [27] evaluates only a subset of available candidate configurations at random until the given budget runs out and returns the best of the sampled configurations.

¹Detailed information on these hyperparameters are provided in [15] (Section I)

2) Bayesian Optimization: As the HPO task is typically time consuming, it is preferable to devise/choose an optimizer that would deliver a good hyperparameter setting with a relative small computational budget. Built upon surrogate models, Bayesian Optimization (BO) [28] is designed for such scenario. Generally speaking, BO iteratively updates a surrogate model M that aims to learn the probability distribution of the loss value conditioned on hyperparameter x, i.e. P(f|x), from the historical information, i.e, the evaluated hyperparameters and the corresponding loss function values. The new candidate hyperparameter is chosen by optimizing the so-called acquisition function [29], which is defined over the surrogate model M and often balances the exploration and exploitation of the search.

Many variants have been proposed for BO, including the Sequential Model-based Algorithm Configuration (SMAC) [30], Sequential Parameter Optimisation (SPO) [31], Mixed-Integer Parallel Efficient Global Optimization (MIPEGO) [32], and Tree-structured Parzen Estimator (TPE) [33], [34]. They differ mostly in the initial sampling method, the probabilistic model, and the acquisition function. Common choices for the probabilistic model are random forests (RF) [35], Gaussian process regression (GPR) [36], and TPE. As for the acquisition function, Expected Improvement (EI), Probability of Improvement (PI) [37], and Upper Confidence Bound (UCB) [38] are more frequently applied among many other alternatives. The initial sampling is also an essential consideration with conventional techniques including random, random sequences of low discrepancies, and Latin Hypercube Design (LHS) [39]. However, for current study we opted the random sampling. In this study, we use TPE as the BO approach and EI for the acquisition function.

C. The Combined Algorithm Selection and Hyperparameter Optimisation (CASH) Problem

The CASH problem [10] aims to identify the best machine learning model, e.g., preprocessing techniques, classification/regression algorithm and their hyperparameters, for minimizing the loss value of an arbitrary real-valued objective function f.

More formally, let $\mathcal{A} = \{A^{(1)}, \dots, A^{(n)}\}$ denote a set of algorithms, and $\chi = \{\chi^{(1)}, \dots, \chi^{(n)}\}$ their hyperparameter spaces. Let $\mathcal{D}_{train}^{(j)}$ and $\mathcal{D}_{valid}^{(j)}$, for $j = 1, \dots, K$, denote training and validation datasets, generated by applying *K*-fold cross-validation on dataset \mathcal{D} . Then the CASH problem is defined as follows:

$$A^{*}, x^{*} = \underset{A^{(i)} \in \mathcal{A}, x \in \chi^{(i)}}{\operatorname{arg\,min}} \frac{1}{K} \sum_{j=1}^{K} f(A_{x}^{(i)}, \mathcal{D}_{train}^{(j)}, \mathcal{D}_{valid}^{(j)}).$$
(3)

Here, $f(A_x^{(i)}, \mathcal{D}_{train}^{(j)}, \mathcal{D}_{valid}^{(j)})$ denotes the loss achieved by the learning algorithm $A^{(i)}$ and its corresponding hyperparameters $x \in \chi^{(i)}$ when trained and evaluated on $\mathcal{D}_{train}^{(j)}, \mathcal{D}_{valid}^{(j)}$.

Note that most HPO methods in practice can handle the CASH problem by modeling the choice of algorithms as a

categorical hyperparameter. Each algorithm is mapped to its locally dependent hyperparameters by the so-called conditional parameter.

III. EXPERIMENTAL SETUP

In this section, we briefly introduce the datasets (Section III-A), resampling techniques (Section III-B) and hyperoptimization approaches (Section III-C) chosen in this work. Finally, we specify the experimental procedure (Section III-D).

A. Datasets

For this study, 44 binary class imbalanced datasets from the KEEL repository [40] are used. Their *Imbalance Ratio* (IR), i.e., the ratio of the number of majority class instances to that of minority class instances, ranges here from 1.82 to 129.44. Figure 1 shows 44 examined datasets presenting the relation of the imbalance ratio (#IR) on the x-axis and the number of samples (#samples) on the y-axis; meanwhile colour of the symbols denotes the number of attributes for each dataset. The full list of datasets is given in [15] (Section II) of the supplementary materials file.



Fig. 1. Overview of the characteristics of the datasets. The scatter plot the Imbalance Ratio (#IR) and the number of samples (#samples) for all 44 datasets on a logarithmic scale. The color indicates the number of attributes.

B. Resampling Algorithms

The resampling algorithms are designed to handle the class imbalance scenario by producing balanced datasets. The resampling algorithms used in our experiments can be arranged into three groups:

- Over-resampling (7 algorithms): In the imbalanced learning domain, SMOTE is the most famous resampling technique and it generates synthetic samples based on the random interpolation between the chosen minority samples and their K-nearest neighbors. Various SMOTE-based extensions have been proposed to give further improvement on the SMOTE basis. For example, ADASYN [41] focuses on the harder-to-learn sample and BorderlineSMOTE [42] emphasizes the borderline samples. Other over-resampling approaches considered in this paper are KMeansSMOTE [43], SMOTENC [18], SVMSMOTE [44] and RandomOverSampler [45].
- 2) Under-resampling (11 algorithms): In a binary classification problem, a Tomek link is defined as a pair



Fig. 2. Flowchart of the experimental setup.

of samples from different classes which are the nearest neighbors for each other [17]. The undersampling method TomekLinks removes the Tomek links in the dataset in order to produce a clear decision boundary. OneSidedSelection [46] first removes noisy and borderline majority samples, then removes the safe majority samples which have limited contribution for building the decision boundary with the CondensedNearest-Neighbour Rule [47]. Other under-resampling methods considered in this paper are CondensedNearestNeighbour, EditedNearestNeighbours [48], RepeatedEdited-NearestNeighbours [49], AllKNN [49], InstanceHardnessThreshold [50], NearMiss [51], Neighbourhood-CleaningRule [52], ClusterCentroids [53], and RandomUnderSampler [54].

The family of evolutionary under-resampling techniques (EUS) have been proved powerful to handle instance reduction [55]. An EUS algorithm tries to optimize the selected samples in the majority class by performing a binary search guided by an evolutionary algorithm [56]. Results of the EUS and the most recent research studies in this family consist of EUS-Windowing (EUSW) [57], clustering-based surrogate model for EUS (EUSC) [23] and hybrid surrogate model for EUS (EUSHC) [24] are also compared with our approach in the followed section.

3) Combine-resampling (2 algorithms): SMOTETomek first oversamples the minority class using SMOTE, after which the Tomek links for the after-sampled samples are removed. Similar to SMOTETL, SMOTEENN first oversamples the minority class with SMOTE. After that, the Wilson's Edited Nearest Neighbors (ENN) is used to remove the sample which has a different class from at least two of its three nearest neighbors [58].

The setup also allows a "no resampling" option. The resampling algorithms are implemented in the Python package **imbalanced-learn**²

C. Hyperparameter Optimization

In this study, random search and TPE as implemented in the Python package $HyperOpt^3$ are used as HPO algorithms.

Based on the initial experiments, we set the number of iterations of HPO to 500, after which the algorithms have shown no significant improvements.

Moreover, to study the effectiveness of the HPO algorithms, we evaluated all possible combinations of classification and resampling algorithms with their default hyperparameter settings. On each dataset, we report the combination with the highest GM. As mentioned in Section I, an experimental study with 5 classification algorithms and 21 resampling techniques is conducted, thus making $5 \times 21 = 105$ combinations in total. Evaluating these combinations one by one is referred to as "Grid-Def" here (grid search HPO algorithm).

D. Implementation details

Algorithm 1: Experimental setup									
	Input: χ : Search space, r: Random seed, K: Number of								
	folds, m : Number of iterations, f : Objective								
	function (see Algorithm 2)								
	Output: x^* : the best configuration, y^* : GM achieved by x^*								
	Data: dataset D								
1	$\mathbf{D} \leftarrow \text{DataPreProcess}(\mathbf{D})$								
	<pre>/* DATAPREPROCESS includes LABELENCODER,</pre>								
	STANDARDSCALER	*/							
2	$\{\mathcal{D}_{train}, \mathcal{D}_{test}\}_{j=1}^{K} \leftarrow \text{StratifiedK-fold}(\mathbf{D}, K, r)$								
3	$\text{HPO} \leftarrow \text{HPO.INIT}(\chi, f, r, m, \{\mathcal{D}_{train}, \mathcal{D}_{test}\}_{j=1}^{K})$								
	/* initialize optimizer	*/							
4	$x^*, y^* \leftarrow \text{HPO.optimize}()$								

The overall structure of our implementation is summarized in Fig. 2. The process begins with data preprocessing on the input dataset. The 5-fold cross-validation is applied at this step to overcome the over-fitting problem. The outcome is fed into the second phase consisting of resampling and classification processes. Our contribution is emphasized at this phase, where the hyperparameters of the resampler and classifier are tuned. This block is highlighted in the blue rounded rectangle. The complete pseudo-code of this flowchart is elaborated in Algorithm 1.

Algorithm 1 consists of the following two steps:

- Preprocessing (line 1-2): We need to apply data preprocessing since machine learning models require input and output data to be numeric. Thus, we use Label encoder⁴ to encode any categorical data to a number for the input dataset. Then, we apply Standard Scaler⁴ on the encoded dataset to have zero mean and a standard deviation of one (line 1). Next, Stratified *K*-fold cross-validation⁴ using K = 5, commonly used in the literature, is used.
- Hyperparameter optimization (line 3-4): All parameters of HPO are initialized (line 3), taking values from the provided input including search space χ , random seed r, number of iterations m, objective function f and K folds of the examined dataset. Then, the algorithm optimizes the search space χ until the number of function evaluations reaches 500.

²https://github.com/scikit-learn-contrib/imbalanced-learn (version 0.7.0)

³https://github.com/hyperopt/hyperopt (version 0.2.5)

 $^{^4}$ Label encoder, Standard scaler and Stratified *K*-fold cross-validation are implemented in the python library scikit-learn (version 0.23.2).



Fig. 3. Illustration of the hyperparameter tuning process on dataset "abalone9-18". Scatter plots show the sequence of observed values vs the number of function evaluations, the red line shows the current best value, and the black vertical bars indicate the infeasible configurations where GM returns a zero if an invalid configuration is used. The stacked histogram plot next to the scatter plot shows the distribution of all observed values. Five last stacked histogram plots to the right indicate the distributions for each of the classification algorithms, namely SVM, RF, KNN, LR and DT.

Algorithm 2: Objective function								
Input: Hyperparameter configuration $x \in \chi$ generated by								
HPO; r : Random seed								
$/* x = \underbrace{x_{re_0}, x_{re_1}, \dots, x_{re_q}}_{* x_{cls_0}, x_{cls_1}, \dots, x_{cls_p}} * /$								
RESAMPLER CLASSIFIER								
Data: $\{\mathcal{D}_{train}, \mathcal{D}_{test}\}_{j=1}^{K}$								
1 foreach $\{\mathcal{D}_{train}^{(j)}, \mathcal{D}_{test}^{(j)}\} \in \{\mathcal{D}_{train}, \mathcal{D}_{test}\}_{j=1}^{K}$ do								
/* Build resampler and classifier models */								
2 RESAMPLER \leftarrow Build RESAMPLER x_{re_0} with the								
hyperparameters $\{x_{re_1}, \ldots, x_{re_q}\}$ and random seed r								
3 CLASSIFIER \leftarrow Build CLASSIFIER x_{cls_0} with the								
hyperparameters $x_{cls_1}, \ldots, x_{cls_p}$ and random seed r								
4 $\mathcal{D}_{train}^{(j)} \leftarrow \text{Resampler}(\mathcal{D}_{train}^{(j)})$								
5 $\lfloor y_j \leftarrow \text{Classifier.Learn}(\mathcal{D}_{train}^{(j)}).\text{Evaluate}(\mathcal{D}_{test}^{(j)})$								
6 return $y \leftarrow \frac{1}{K} \sum_{i=1}^{K} y_i$								

The computation of the objective function is presented in Algorithm 2. It elaborates further steps shown in the circle in Fig. 2. The input is a parameter setting generated by HPO consisting of random seed r and hyperparameter configuration x. The configuration x consists of two parts: the choice of resampler represented by x_{re_0} , and classifier denoted by x_{cls_0} , together with their corresponding hyperparameter settings

 $\{x_{re_1}, \ldots, x_{re_q}\}$ and $\{x_{cls_1}, \ldots, x_{cls_p}\}.$

For a fold of the examined dataset, the computation of an evaluation has the following steps:

- Step 1 (line 2-3): Resampler and classifier are initialized, using values of the configuration x and random seed r.
- Step 2 (line 4-5): The selected resampler is applied to the fold, followed by the classifier, which is applied to the balanced result from the resampler. Then, the GM on each validation fold is calculated.

The final value of the objective function is an average GM of K folds (line 6). Additionally, since the used algorithms, i.e., classifiers and resamplers, in the objective function are stochastic, we fixed 10 random seeds for HPO, classifiers and resamplers in 10 different runs to make the objective function *deterministic*, i.e., to assure the objective function always returns the same value for identical input values. The reported result of each dataset for an individual HPO approach is averaged over 10 executions.

IV. RESULTS AND DISCUSSION

In this section, we report the results and discuss our insights. The experimental results are summarised in Table I to illustrate

TABLE I

Average Geometric mean (rounded to 4 decimals) over 10 repetitions for the 44 datasets, ordered by increasing IR value. The left part shows our experimental results, i.e., TPE, Random search (rs), Grid-Def (grid), and the right part (grey shaded) those obtained by evolutionary algorithms according to [23], i.e., EUS, EUS-Windowing, EUSC, EUSHC, respectively. Boldface highlights the best performing method per dataset on each group and underline indicates results that are significantly different from the best method in that group according to a Wilcoxon signed-rank test (p < 0.05). A value labeled with * indicates that our experimental result outperforms the results from [23] for the corresponding dataset.

Dataset	#IR Our experimental results		Evolutionary algorithms [23]				Overall		
		TPE	RS	Grid	EUS	EUSW	EUSC	EUSHC	Winner
glass1	1.82	*0.7989	0.7763	0.7793	0.7773	0.7010	0.7941	0.7367	TPE
ecoli-0_vs_1	1.86	*0.9864	*0.9864	*0.9864	0.9583	0.9312	0.9581	0.9615	TPE RS Grid
wisconsin	1.86	*0.9814	*0.9807	*0.9788	0.9690	0.9652	0.9600	0.9590	TPE
pima	1.87	*0.7711	*0.7651	*0.7599	0.6943	0.6749	0.6957	0.7145	TPE
iris0	2.00	1	1	1	1	1	1	1	-
glass0	2.06	*0.8749	* <u>0.8588</u>	*0.8719	0.8009	0.6176	0.8047	0.6595	TPE
yeast1	2.46	*0.7324	*0.7304	*0.7183	0.6533	0.6501	0.6600	0.6600	TPE
haberman	2.78	*0.7025	* <u>0.6926</u>	* <u>0.6678</u>	0.5475	0.5635	0.5521	0.5497	TPE
vehicle2	2.88	*0.9915	*0.9874	*0.9895	0.9259	0.9175	0.9265	0.9173	TPE
vehicle1	2.90	*0.8658	*0.8429	*0.8333	0.6729	0.6624	0.6512	0.6926	TPE
vehicle3	2.99	*0.8482	*0.8231	*0.8108	0.7280	0.7142	0.7165	0.7204	TPE
glass-0-1-2-3_vs_4-5-6	3.20	0.9559	0.9505	0.9483	0.9525	0.9385	0.9647	0.9546	EUSC
vehicle0	3.25	*0.9863	*0.9809	*0.9766	0.9164	0.9027	0.9103	0.9016	TPE
ecoli1	3.36	*0.9047	*0.8966	*0.8999	0.8634	0.8306	0.8554	0.8424	TPE
new-thyroid1	5.14	*0.9969	*0.9966	*0.9944	0.9882	0.9809	0.9859	0.9653	TPE
new-thyroid2	5.14	*0.9978	*0.9966	*0.9910	0.9865	0.9773	0.9831	0.9746	TPE
ecoli2	5.46	*0.9361	*0.9337	*0.9361	0.9000	0.8663	0.9034	0.8772	TPE Grid
segment0	6.02	*0.9993	*0.9990	*0.9965	0.9881	0.9870	0.9876	0.9858	TPE
glass6	6.38	*0.9524	*0.9516	*0.9381	0.8889	0.9071	0.9156	0.9054	TPE
veast3	8.10	*0.9428	*0.9395	*0.9290	0.8728	0.8740	0.8752	0.8550	TPE
ecoli3	8.60	*0.9061	*0.9023	*0.9044	0.8348	0.8153	0.8500	0.8097	TPE
page-blocks0	8.79	*0.9456	*0.9422	*0.9401	0.9117	0.9038	0.9096	0.9085	TPE
veast-2 vs 4	9.08	*0.9559	*0.9474	*0.9401	0.9042	0.8774	0.9156	0.8930	TPE
veast-0-5-6-7-9 vs 4	9.35	*0.8212	*0.8063	*0.7938	0.7685	0.7663	0.7901	0.7535	TPE
vowel0	9.98	0.9581	0.9483	0.9427	0.9897	0.9719	0.9877	0.9831	EUS
glass-0-1-6 vs 2	10.29	*0.8498	*0.8216	*0.7904	0.6383	0.6164	0.6651	0.5815	TPE
glass2	11.59	*0.8516	*0.8271	*0.7903	0.7194	0.6525	0.7262	0.6173	TPE
shuttle-c0-vs-c4	13.87	*1	*1	*1	0.9960	0.9968	0.9960	0.9960	TPE RS Grid
yeast-1_vs_7	14.30	*0.8028	*0.7926	*0.7979	0.7176	0.7079	0.7068	0.6669	TPE
glass4	15.46	*0.9323	*0.9244	*0.9318	0.8700	0.8513	0.8613	0.8531	TPE
ecoli4	15.80	*0.9727	0.9551	0.9415	0.8984	0.9362	0.8857	0.9645	TPE
page-blocks-1-3_vs_4	15.86	*0.9925	*0.9877	*0.9884	0.9674	0.9399	0.9471	0.9294	TPE
abalone9-18	16.40	*0.8889	*0.8752	*0.8536	0.7269	0.6772	0.7224	0.6559	TPE
glass-0-1-6_vs_5	19.44	*0.9567	*0.9530	0.9304	0.9214	0.9151	0.9160	0.9501	TPE
shuttle-c2-vs-c4	20.50	*1	*1	*1	0.9577	0.6449	0.9414	0.7365	TPE RS Grid
yeast-1-4-5-8_vs_7	22.10	*0.7035	*0.6874	*0.6650	0.6569	0.6088	0.6604	0.6149	TPE
glass5	22.78	*0.9637	0.9555	0.9438	0.8105	0.9076	0.9600	0.9103	TPE
yeast-2 vs 8	23.10	*0.8231	*0.8031	*0.7945	0.7931	0.7496	0.7656	0.7668	TPE
veast4	28.10	*0.8803	*0.8664	*0.8585	0.8050	0.7799	0.8288	0.7970	TPE
veast-1-2-8-9 vs 7	30.57	*0.7459	*0.7402	*0.7289	0.6721	0.6078	0.6704	0.6500	TPE
veast5	32.73	*0.9803	*0.9790	*0.9788	0.9634	0.9494	0.9455	0.9653	TPE
ecoli-0-1-3-7 vs 2-6	39.14	*0.9095	*0.8770	*0.9091	0.6700	0.7048	0.6625	0.6865	TPE
veast6	41.40	*0.8972	*0.8905	*0.8840	0.8357	0.8080	0.8034	0.8031	TPE
abalone19	129.44	*0.7967	*0.7942	*0.7579	0.6258	0.6061	0.7214	0.6556	TPE

the performance differences between the three integrated optimization approaches used, i.e., TPE, Random search (RS) and Grid-Def (Grid), and to compare them against the state-of-theart Evolutionary under-resampling (EUS) methods [23]. In this table, our results are presented in the corresponding columns on the left side (not shaded) and the results from [23] are presented on the right side (grey shaded) for EUS, EUSW, EUSC and EUSHC, respectively. In both groups, the highest performance for each dataset is highlighted in bold. In our experimental results, the methods performing significantly worse than the best according to the Wilcoxon signed-rank test with $\alpha = 0.05$ are underlined. A value labeled with * indicates that our result outperforms those from [23] for the corresponding dataset. Additionally, an extra column to the right summarizes the method that achieves the highest GM for the corresponding dataset.

The results allow the following insights:

• HPO approaches exhibit better performance compared



Fig. 4. Resulting combination of classifier and resampler choices for an optimization process using TPE across 10 repetitions on 44 datasets. Figure best viewed in color.

to the Grid-Def approach which uses static default hyperparameters. Moreover, according to the results of the Wilcoxon signed-rank test, TPE is always the best method found: it significantly outperforms the Grid-Def in 32/44 datasets, while it significantly outperforms RS in 26/44 tested cases⁵.

- Overall, TPE shows the highest GM for most of the datasets, 41/44. Other compared methods win on different datasets, e.g., EUSC and EUS achieve the highest GM on "glass-0-1-2-3_vs_4-5-6" and "vowel0", respectively. All approaches get the maximum GM on dataset "iris0".
- Furthermore, based on our experimental results, we conclude that TPE wins over the methods from [23] on 41/44 datasets, RS on 38/44 datasets and Grid-Def on 37/44 datasets. This is surprising since the number of function evaluations used in our experiment is much smaller than in [23]: 500 function evaluations for TPE and RS, 105 function evaluations for Grid-Def vs 10.000 function evaluations for each method in [23]. A possible explanation for this might be that [23] employs a simple KNN rule with k = 1 as the mere classifier, while more complicated classification algorithms are used in our study. More precisely, according to our experimental results, tuned KNN wins only in 11% (TPE), 13% (RS), and 9% (Grid-Def) of all cases.

To investigate the tuning behavior of the methods, we plot single runs of TPE and RS on the dataset "abalone9-18"⁶ in Fig. 3. The scatter plots on the left show the observed GM values over 500 function evaluations. The scatter plots on the left show the observed GM values over 500 function

evaluations. Six last stacked histogram plots describe the distribution of the observed values, in which the first plot shows all observed values, and the five last plots indicate the distributions for each of the classification algorithms, i.e. SVM, RF, KNN, LR and DT. We conclude that:

- Configurations generated by TPE can avoid area of infeasible parameters better than RS⁷. In this run, the number of errors occurring in the TPE and RS runs are 14 and 22, respectively. Based on all datasets and repetitions, the number of infeasible configurations encountered by TPE and RS are 4.4% and 5.9%, respectively.
- Apart from zero values, the GM values of TPE are mostly in the range from 0.8 to 0.9, while the GM of RS are distributed in the range from 0.6 to 0.7.

Based on the highest results obtained by TPE, Fig. 4 shows the final combination of choices of classification algorithms and resampling approaches once the optimization run is over. Clearly, no dominant algorithm exists over many datasets but different datasets benefit from different classification algorithms. For example, "glass0", "yeast1", "yeast3", "haberman", "vehicle2", "ecoli1" and "page-blocks0" achieve the best results with SVM, "vehicle0", "vehicle1", "vehicle3" with KNN, whereas "abalone9-18" always results in LR. Besides, 98% of runs yield the best performance by using some resampling technique. Particularly, over-resampling, under-resampling and combine-resampling obtain 182, 199, 50 wins over $44 \times 10 = 440$ runs. Additionally, there is no classifier/resampler combination providing the best classification performance over all datasets. Specifically, RF and SVM obtain 206 and 84 wins, while other algorithms (LR, KNN, DT) find the best performance in 73, 48 and 29 runs, respectively.

 $^{{}^{5}}$ Full details of our experimental results are provided in [15] (Section V) of the supplementary materials file

⁶Note that, due to the page limitation, the plots for this dataset over 10 repetitions can be found in Section IV of the supplementary material [15]

⁷Evaluations with infeasible combinations of parameters are marked on the figure as black dashes with GM = 0.

V. CONCLUSIONS AND FUTURE WORK

In this paper, we applied a special type of Bayesian Optimization approach, the Tree Parzen Estimators to optimize the combined algorithm selection and hyperparameter optimization problem to improve the performance of classification algorithms for the class imbalance problems. In other words, we proposed an automated CASH optimization approach for imbalanced classification problems. Our approach automatically chooses the best set of algorithms, i.e., resampling technique and classification algorithm, together with their optimized hyperparameter settings for an arbitrary imbalanced dataset. The numeric results show significantly improved performance with respect to the state-of-the-art techniques in the imbalanced classification domain over 44 examined datasets.

Four main conclusions can be drawn from our experimental results:

- 1) Use of HPO clearly improves classification performance compared to using static default parameters.
- TPE outperforms Random search on 91% of the tested datasets, while equal performance is found on the remaining cases.
- Overall, the TPE approach produces the best results among other competitors in various scenarios. Hence, we recommend using TPE for handling CASH optimization in imbalanced classification problems.
- 4) Another finding is that 98% of runs yield the best performance with the help of resampling techniques. Thus we recommend researchers to use resampling to deal with class imbalanced problems.

There are several interesting research directions for extending this work. Firstly, we intend to apply other Bayesian optimization variants such as SMAC, SPO, and MIPEGO, in order to study the performance between variants in this domain. Secondly, the scope of this study was limited in terms of classification problems; therefore, our future research might extend our research for regression problems. Thirdly, in addition to GM, other commonly used performance evaluation metrics in this domain will be investigated in our future work, including the Area Under the ROC Curve (AUC), Fmeasure, and recall. Fourthly, the penalty-based methods, e.g., penalized-SVM, themselves can efficiently handle imbalanced datasets in several cases. Thus, we plan to study their effectiveness in the context of CASH optimization. Additionally, instead of applying hyperparameter tuning on the level of an individual dataset, we are interested in studying the behavior of HPO approaches when tuning for a set of datasets. Finally, besides Bayesian optimization, we will extend our research with other state-of-the-art HPO approaches such as iRace [59] and Hyperband [60] for the class-imbalanced problem.

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