FORMATION OF METALLIC GLASSES NEAR INTERMETALLICS IN ZR-CU AND ZR-CU-TI SYSTEMS

WANG YINXIAO

(B.Eng., BUAA)

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DECLARATION

I hereby declare that the thesis is my original work and it has been written by me in its entirety. I have duly acknowledged all the sources of information which have been used in the thesis.

This thesis has also not been submitted for any degree in any university previously.

Wang Yinxiao 6 August, 2012

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Table of Contents

Acknowledgements	i
Table of Contents	iii
Summary	vi
List of Tables	ix
List of Figures	x
List of Publications	xv
Chapter 1 Introduction	1
1.1 Introduction to Bulk Metallic Glasses (BMGs)	1
1.1.1 The history of the development of BMGs	1
1.1.2 Properties and applications of BMGs	5
1.2 Formation of BMGs	6
1.2.1 Thermodynamic consideration on glass formation	7
1.2.2 Kinetics consideration on glass formation	
1.3 Evaluation of glass forming ability	
1.3.1 T_{ro} criterion	
1.3.2 Three empirical rules proposed by Inoue	
1.4 Pinpoint strategy to locate the best glass forming range	
1.5 Glass formation in Zr-Cu and Zr-Cu-Ti allov systems	
1.5.1 Glass formation in Zr-Cu binary alloy system	
1.5.2 Glass formation in Zr-Cu-Ti tenary alloy system	
1.6 Motivation and outline of this thesis	29
Chapter 2 Experimental procedures	31
2.1 Preparation of master alloys	31
2.2 Casting procedures	32
2.2.1 Melt-spinning	32
2.2.2 Wedge casting method	33
2.2.3 Suction casting method	34
2.2.4 Copper mold casting	36

2.3 Microstructure characterization
2.3.1 X-ray diffraction (XRD)
2.3.2 Optical microscopy (OM) and scanning election microscopy
(SEM)
2.4 Thermal analysis

Chapter 3 The formation of intermetallic glasses in Zr–Cu system40

3.1 Introduction	40
3.2 Results	43
3.2.1 Glass formation near CuZr2 intermetallic	44
3.2.2 Glass formation near Cu10Zr7 intermetallic	47
3.2.3 Glass formation near Cu51Zr14 intermetallic	50
3.2.4 Glass formation near Cu ₈ Zr ₃ intermetallic	52
3.3 Discussion	59
3.3.1 Calculation of Gibbs free energy of liquid and intermeta	allic
phases as a function of composition by CALPHAD method	59
3.3.2 The thermodynamic explanation for the formation	of
intermetallic glasses	68
3.3.3 Kinetic influence on the formation of intermetallic glasses	74
3.4 Conclusion	88

Chapter 4 The formation of intermetallic glasses in Zr–Cu-Ti system90

4.1 Introduction90
4.2 Glass formation of compositions Cu_{100-x} (ZrTi) _x (Ti=5 at% and x=47.5-53)94
4.2.1 Glass formation of 3 mm rods of alloy Cu100-x(ZrTi)x (Ti=5 at%
and x=47.5-53)95
4.2.2 Glass formation of 5 mm rods of alloy Cu _{100-x} (ZrTi) _x (x=47.5-53)
4.3 Glass formation of compositions near Cu2ZrTi intermetallic phase .109
4.3.1 Glass formation of compositions Cu50ZrxTi50-x, CuyZr77-yTi23 and
Cu _y Zr ₂₇ Ti _{73-y}
4.3.2 XRD and melting studies of the composition in line 1, 2 and 3
4.4 Calculation of the glass forming range in Zr-Cu-Ti ternary system .123
4.5 Conclusion
hapter 5 Conclusion138
5.1 Summary of results138

5.2	Future work	142
Bibliogra	aphy	144

Summary

Two typical methods have been used to form metallic glass since 1960s: liquid quenching and solid-state reaction. The glass formation range obtained by liquid quenching method is believed near eutectic points, especially deep eutectic points. Metallic glass is formed in the centre of phase diagram by solid-state reaction. However, the discovery of so called "intermetallic glass" provides a wider perspective of formation of metallic glass.

Intermetallic glass is a pair of optimum glass formers, which is formed near but separated by the intermetallic composition. This dissertation is to investigate the underlying mechanism of the formation of the intermetallic glass. Two alloy systems are selected: Zr-Cu binary system and Zr-Cu-Ti ternary system.

In Zr-Cu system, there are six intermetallic phases (i.e. Cu₉Zr₂, Cu₅₁Zr₁₄, Cu₈Zr₃, Cu₁₀Zr₇, CuZr and CuZr₂), and we have studied the glass formation near Cu₅₁Zr₁₄, Cu₈Zr₃, Cu₁₀Zr₇ and CuZr₂ intermetallics. A pair of intermetallic glass is located near Cu₅₁Zr₁₄, Cu₁₀Zr₇ and CuZr₂ intermetallics respectively. The phenomenon of formation of the intermetallic glass has been confirmed. Based on the assumption that intermetallic has Gibbs free energy in a sharp

profile, we proposed that two thermodynamically favored glass formation ranges are present under quenching. Kinetically, the temperature dependent viscosities of certain alloys were measured and the TTT curves of these alloys were constructed. It is surprisingly found that the intermetallic compound has a higher critical cooling rate than those of the optimum glass formers. Therefore, both the thermodynamic and kinetic perspectives contribute to the formation of intermetallic glass.

In the Zr-Cu-Ti ternary systems, based on the experimental results obtained in binary system, 5 at% Ti was added into compositions Cu_{52.5}Zr_{47.5} to Cu₄₇Zr₅₃ to replace Zr to study the glass formation. It is demonstrated that the phenomenon of formation of intermetallic glass still can be observed in the resulting composition range (Cu_{100-x}(ZrTi)_x, where Ti=5% and x=47.5-53). The compositions of optimum intermetallic glass formers in ternary are as similar as those in binary system. Ti element is believed to stabilize the Cu₁₀Zr₇ phase during the precipitation.

However, in the composition range near Cu₂ZrTi intermetallic phase, the phenomenon of formation of intermetallic glass is not clear enough. Unlike the intermetallic in the previous study, Cu₂ZrTi intermetallic is not a line compound but has a wide homogeneity composition range. Furthermore, in this composition range, it is believed that the Gibbs free energy and liquidus temperature varies slightly with the changing of composition. This may makes that the changing of critical thickness is insensitive to that of composition.

List of Tables

Table 1.1 Summary of BMG compositions with their critical sizes
Table 1.2 Relationship between properties of BMGs and the potential applications
Table 1.3 Summary of glass forming ability in Zr-Cu binary system22
Table 3.1 Summary of the critical sizes of both eutectic glass formers and intermetallic glass formers 57
Table 3.2 Temperautre of T_g and T_x of Cu ₅₁ Zr ₁₄ , Cu ₁₀ Zr ₇ , CuZr and CuZr ₂ intermetallics63
Table 3.3 Gibbs free energies of liquid and intermetallic phases. 64
Table 3.4 List of the values of T_m and ΔH_m
Table 3.5 List of points were taken to calculate the values of <i>A</i> , <i>B</i> and <i>T</i> ₀ 77
Table 3.6 T_g and T_p of selected compositions at different heating rates78
Table 3.7 List of the values of A, B and To. 80
Table 3.8 the critical cooling rate, <i>R_c</i> , for the selected alloys
Table 4.1 Values of parameters needed to calculate the enthalpy of formation
Table 4.2 The calculated chemical enthalpies and elastic enthalpies

List of Figures

Figure 1.1 Schematic diagram of 'gun' technique of Duwez for rapid cooling (adapted from Ref. [2])2
Figure 1.2 Schematic plot shows glass will be formed (as shown in dash line 2) from liquid by avoiding crystallization (as shown in solid line 1)
Figure 1.3 The crystallization driving forces and the corresponding critical cooling rate for selected glass forming alloys (reproduced from Ref. [43])9
Figure 1.4 Angell plot comparing viscosities of some selected glass forming liquids (adapted from Ref. [51])11
Figure 1.5 Relationship between homogeneous nucleation rate I and the reduced temperature T_r (adapted from Ref. [54])13
Figure 1.6 Schematic variation of the T_g , T_l and T_{rg} in a typical binary eutectic system, which indicates T_{rg} reaches the highest value at the eutectic composition
Figure 1.7 Phase-formation diagrams which show the glass and composite forming range of (a) a regular eutectic system and (b) an irregular eutectic system
Figure 1.8 An schematic illustration of the glass forming ranges of the general metallic glass obtained by applying different theories and methods.
Figure 1.9 Calculated phase diagram of Zr-Cu binary system24
Figure 1.10 The calculated surface of the crystallization driving force for Zr- Cu system at 800K as well as the optimum glass formers (adapted from Ref. [96])25
Figure 1.11 Pseudo-ternary phase diagram of Ti-Zr-Cu-Ni system with two glass forming ranges (adapted from Ref. [97])26
Figure 1.12 The liquid projection of the ternary phase diagram of Cu-Zr-Ti system. Three eutectic points marked as blue square were given by Woychik [99]; and five eutectic points marked as red circles were given by Arroyave [100] (adapted from Ref. [51])

Figure 1.13 Summary of different glass forming ranges in Zr-Cu-Ti system. The red line, blue circle and the green dot represent glass formers from

different references [97, 101-103]28
Figure 2.1 A schematic diagram of the melt-spinning equipment
Figure 2.2 A schematic diagram of the wedge casting method
Figure 2.3 A schematic diagram of the suction casting equipment35
Figure 2.4 A photo of the LSG-400 arc melting system with copper mold in it.
Figure 2.5 A schematic diagram of the measurement of critical size of wedge sample.
Figure 3.1 Part of Zr-Cu phase diagram and the corresponding hypothetical free energy curves. The red lines represent glass forming regions and two solid circles are two intermetallic glass formers. The eutectic glasses are marked as open circles (adapted from Ref. [81])
Figure 3.2 SEM photos of wedge cast samples with compositions from Cu _{36.33} Zr _{63.67} to Cu _{30.33} Zr _{69.67} . The arrows all point to the critical thicknesses (boundary between crystalline phase and amorphous phase) and the red line represents the cutting edge for the DSC test
Figure 3.3 Summary of critical sizes and the enthalpy of crystallization of wedge cast samples46
Figure 3.4 DSC curves of the tip parts of wedge cast samples
Figure 3.5 OM photos of wedge cast samples with compositions from Cu _{60.32} Zr _{39.68} to Cu _{57.32} Zr _{42.68} . The arrows all point to the critical thicknesses48
Figure 3.6 Summary of critical sizes and the enthalpy of crystallization of wedge cast samples
Figure 3.7 DSC curves of the tip parts of wedge cast samples
Figure 3.8 DSC curves of 15 μm ribbons of compositions near Cu ₅₁ Zr ₁₄ intermetallic
Figure 3.9 XRD patterns of the chill-side of the ribbons with compositions near Cu ₅₁ Zr ₁₄ intermetallic
Figure 3.10 DSC curves of 20 μm ribbons of compositions near Cu ₈ Zr ₃ intermetallic
Figure 3.11 XRD patterns of the chill-side of the ribbons with compositions near Cu ₈ Zr ₃ intermetallic
Figure 3.12 Partial Cu-Zr binary phase diagram55
Figure 3.13 Partial of Cu-Zr binary phase diagram and summary of the

critical sizes of both eutectic glass formers and intermetallic glass formers.58

Figure 3.15 The crystallization driving force of CuZr₂, CuZr, Cu₁₀Zr₇ and Cu₅₁Zr₁₄ intermetallics under their corresponding T_g or T_x temperatures.....67

Figure 3.18 The crystallization driving force of Cu₅₁Zr₁₄, Cu₁₀Zr₇, CuZr and CuZr₂ intermetallic compounds in the whole composition range.70

Figure 3.22 Calculated TTT curves of selected composition......83

Figure 4.1 Part of Ti-Cu binary phase diagram......92

Figure 4.2 The composition ranges studied in this chapter (marked by the red line and the red circle) and the composition ranges studied before (marked by the purple line and the pruple circle) [97, 101-103]......94

Figure 4.3 SEM photos of the longitudinal view of 3 mm rods with composition from Cu_{52.5}(ZrTi)_{47.5} to Cu₄₇(ZrTi)₅₃......97

Figure 4.4 SEM photos of two kinds of crystalline phases detected in the 3

mm rods with composition from Cu52.5(ZrTi)47.5 to Cu47(ZrTi)53: (a) CuZr phase and (b) Cu10Zr7 phase98
Figure 4.5 XRD patterns of 3 mm rods with composition from Cu _{52.5} (ZrTi) _{47.5} to Cu ₄₇ (ZrTi) ₅₃ .
Figure 4.6 DSC curves of 3 mm rods with composition from Cu _{52.5} (ZrTi) _{47.5} to Cu ₄₇ (ZrTi) ₅₃
Figure 4.7 Calculated enthalpies of crystallization and percentage ofamorphous phase of all 3 mm rods
Figure 4.8 SEM photos of longitudinal view of 5 mm rods with composition from Cu _{52.5} (ZrTi) _{47.5} to Cu ₄₇ (ZrTi) ₅₃ 106
Figure 4.9 DSC curves of 3 mm rods with composition from Cu _{52.5} (ZrTi) _{47.5} to Cu ₄₇ (ZrTi) ₅₃
Figure 4.10 The studied compositions near Cu2ZrTi (Cu50Zr25Ti25), marked by the red dot
Figure 4.11 OM photos of the longitudinal view of the wedge cast samples of Cu ₅₀ Zr _x Ti _{50-x} (x=22-30)111
Figure 4.12 The critical sizes of the wedge cast samples of Cu ₅₀ Zr _x Ti _{50-x} (x=22-30).
Figure 4.13 OM photos of the longitudinal view of the wedge cast samples of $Cu_yZr_{77-y}Ti_{23}$ (y=48-52)
Figure 4.14 The critical sizes of the wedge cast samples of Cu _y Zr _{77-y} Ti ₂₃ (y=48-52)
Figure 4.15 OM photos of the longitudinal view of the wedge cast samples of $Cu_yZr_{27}Ti_{73-y}$ (y=48-52)
Figure 4.16 The critical sizes of the wedge cast samples of Cu _y Zr ₂₇ Ti _{73-y} (y=48-52). 115
Figure 4.17 Summary of the critical sizes of compositions along line 1, 2 and 3. A "ring" of the peaks in the critical thickness is marked by the red circle. The red values represent the "peak" values of critical size and the blue value represents the critical thickness of composition Cu ₅₀ Zr ₂₇ Ti ₂₃ 116
Figure 4.18 XRD patterns of the crystallization part of wedge cast samples of line 1, 2 and 3
Figure 4.19 Melting curves of compositions in line 1, 2 and 3. The dash dot lines indicate the liquid temperature119
Figure 4.20 Melting curves of composition line 4121 xiii

Figure 4.21 Critical size	es of compositions	around Cu ₄₂ Zr ₃₁ Ti ₂₇	121
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Figure 4.22 Color map of the calculated enthalpy of formation of solid solution phase in Zr-Cu-Ti ternary system. The unit is KJ/mol......130

Figure 4.23 Color map of the calculated enthalpy of formation of amorphous phase in Zr-Cu-Ti ternary system. The unit is KJ/mol......131

Figure 4.24 Color map of the approximated driving force of formation of amorphous phase for the Zr-Cu-Ti ternary system. The unit is KJ/mol.....132

Figure 4.25 The	e calculated gla	ss forming range	e in Zr-Cu-Ti	ternary system.

List of Publications

- <u>Wang Y.X.</u>, Yang H., Lim G., Li Y., Glass formation enhanced by oxygen in binary Zr-Cu system, *Scripta Materialia*, 2010,62:682-685
- <u>Wang Y. X.</u>, Li Y., Formation of metallic glasses near intermetallics in Cu-Zr binary system (submission in progress)

Chapter 1

Introduction

1.1 Introduction to Bulk Metallic Glasses (BMGs)

1.1.1 The history of the development of BMGs

Metallic glasses (MGs) can be defined as metals or metal alloys without crystalline structure. They can be prepared by rapid solidification from liquid phase. The crystallization can be avoided when the cooling rate is high enough, so the atoms can be frozen in their liquid configuration when the solidification occurs. The first metallic glass, Au₇₅Si₂₅, was discovered in 1960



by Duwez by applying a so called 'gun technique' [1].

Figure 1.1 Schematic diagram of 'gun' technique of Duwez for rapid cooling (adapted from Ref. [2]).

The Au₇₅Si₂₅ alloy was melt and then ejected by high pressure gas on copper substrate strip to obtain a high cooling rate of 10⁶K/s, as illustrated in **Figure 1.1** [2]. Since then, metallic glasses have attracted great attention and much research had been carried out to discover new metallic glasses in different alloy systems. However, the critical size of metallic glasses remained in micron-meter scale by the requirement of high cooling rate, which limited their commercial application.

In 1974, Chen discovered metallic glass in Pd-Cu-Si ternary alloy system with critical thickness larger than 1 mm by water quenching, which had an estimated cooling rate less than 10³K/s [3]. If one arbitrarily defines 1 mm is the minimum thickness of the alloy as "bulk", then these Pd-Cu-Si ternary glasses should be the first bulk metallic glasses (BMGs) reported. After this, in 1984, another well-known Pd40Ni40P20 ternary metallic glass was discovered by Kui and other co-workers using boron oxide fluxing method to purify the melt and eliminate heterogeneous nucleation [4]. The cooling rate of this boron oxide fluxing method was significantly lower, which was estimated as 10K/s level. In the late 1980s, Inoue and his collaborators discovered bulk metallic glasses without noble metals in La-Al-Ni ternary alloy system for the first time [5]. Since then, a new era of the research of bulk metallic glasses has begun. Building on this work, a family of glasses with rare earth elements was discovered, for example, in the La-Al-Cu, La-Al-Cu-Ni and La-Al-Cu-Ni-Co systems [6-8]. Subsequently, more and more bulk metallic glasses have been discovered in other multi-component systems such as Zr-, Mg-, Y-, Ca-, Au-, Fe-, Ni-, Co-, Ti- and Cu-based alloy systems [9-29].

	Alloy system	Critical size	Year	Ref.
		(mm)		
Zr-based	Zr41.2Ti13.8Cu12.5Ni10Be22.5	25	1993	[17]
	Zr65Al17.5Ni10Cu17.5	16	1993	[18]
	Zr55Al10Ni5Cu30	30	1996	[30]
Ni-based	$Ni_{40}Cu_5Ti_{16.5}Zr_{28.5}Al_{10}$	5	2004	[31]
Pd-based	$Pd_{40}Cu_{30}Ni_{10}P_{20}$	72	1997	[32]
Cu-based	$Cu_{46}Zr_{42}Al_7Y_5$	10	2004	[33]
	Cu44.25Ag14.75Zr36Ti5	10	2006	[15]
Fe-based	$Fe_{48}Cr_{15}Mo_{14}Er_2C_{15}B_6$	12	2004	[34]
	$Fe_{41}Co_7Cr_{15}Mo_{14}C_{15}B_6Y_2$	16	2005	[16]
Mg-based	$Mg_{54}Cu_{26.5}Ag_{8.5}Gd_{11}$	25	2005	[35]
RE-based	Nd70Al10Fe20	15	1997	[24]
	Y36Sc20Al24Co20	25	2003	[10]
Ca-based	$Ca_{60}Mg_{25}Ni_{15}$	13	2005	[11]
Au-based	Au49Ag5.5Pd2.3Cu26.9Si16.3	5	2005	[12]
Al-based	Al85.5Ni9.5La5	1	2009	[36]
	Als6Si0.5Ni4.06Co2.94Y6Sc0.5	1	2009	[37]

Table 1.1 Summary of BMG compositions with their critical sizes

Table 1.1 summarizes some BMG compositions in different alloy systems with their critical sizes and their discovery years. Among all these BMGs, alloy Zr_{41.2}Ti_{13.8}Cu_{12.5}Ni₁₀Be_{22.5} was the first commercial alloy, which was called Vitreloy 1(Vit 1) [17]. And Pd₄₀Cu₃₀Ni₁₀P₂₀ alloy still holds the record of the largest critical size, which reaches 72 mm [32].

Table 1.2 Relationship between properties of BMGs and the potential applications.

Properties	Application field
High strength	Engineering structural materials
High hardness	Cutting materials
High fracture toughness	Die materials
High impact fracture energy	Tool materials
High elastic energy	Sporting goods materials
High corrosion resistance	Corrosion resistance materials
Good soft magnetism	Soft magnetic materials
Self-sharpening	Penetrator

1.1.2 Properties and applications of BMGs

Unlike conventional metallic materials, metallic glasses have no long-range atomic order, which provides some unique and interesting properties, such as high strength, high elastic limit, high toughness, high corrosion resistance and good soft magnetic properties. To date, BMGs have been used as hand phone casing, golf club head, scalpel, and also in many other areas [38, 39]. **Table 1.2** listed the relationship between the superior properties of BMGs and the possible variety applications. Furthermore, with the increasing number of BMGs and larger critical sizes of BMGs discovered, the future of BMGs is widely expanded both as potential engineering materials and as advanced research topics.

1.2 Formation of BMGs

Usually, metallic glasses are prepared by rapid quenching to avoid the nucleation and growth of crystalline phase, like shown in Figure 1.2. The melt should be quenched along line 2 to avoid "touching" the time-temperature-transformation (TTT) curve. Although a number of BMGs in various alloy systems have been discovered and even been commercially used in the past decades, understanding glass formation is still a basic but long-stand question, which is far from being solved. Generally, both thermodynamic and kinetic consideration are contributed to the glass formation; so it would be great help to predict glass forming ability (GFA) and glass forming range (GFR) by understanding how these two perspectives influence the glass formation.



Figure 1.2 Schematic plot shows glass will be formed (as shown in dash line 2) from liquid by avoiding crystallization (as shown in solid line 1).

1.2.1 Thermodynamic consideration on glass formation

Basically, glass formation is a process of competition between crystallization and vitrification. It is commonly believed that a low driving force for crystallization lead to low nucleation rate, which results in a high GFA. The crystallization driving force or the Gibbs free energy difference between the liquid phase and the crystalline phase ΔG_{l-s} can be calculated as [40]:

$$\Delta G_{l-s}(T) = \Delta H_f \Delta S_f T_0 - \int_T^{T_0} \Delta C_p^{l-s}(T) dT + \int_T^{T_0} \frac{\Delta C_p^{l-s}(T)}{T} dT$$
(1.1)

where ΔH_f and ΔS_f are the enthalpy and entropy of fusion, respectively and T_0 is the temperature which Gibbs free energy of liquid phase and crystal phase equals to each other; ΔC_p is the specific heat capacity. A low ΔG_{l-s} can be obtained by low ΔH_f value, high ΔS_f value and low ΔC_p value. According to the "confusion theory" [41] and "three empirical rules" [9], the increasing alloy components leads to a higher ΔS_f value, which causes the increasing degree of dense random packing. That is favorable for the decreasing ΔH_f value [42].

Figure 1.3 shows the driving force for crystallization as a function of supercooling of some glass forming systems [40, 43, 44]. The temperature is normalized to the melting temperatures of the corresponding alloys. It shows clearly that the glass forming ability decreases with the increasing critical cooling rate changes from 1K/s for Zr_{41.2}Ti_{13.8}Cu_{12.5}Ni₁₀Be_{22.5} alloy to 10⁴K/s for Zr₆₂Ni₃₈ alloy, which is directly related to the increasing crystallization driving forces.



Figure 1.3 The crystallization driving forces and the corresponding critical cooling rate for selected glass forming alloys (reproduced from Ref. [43]).

1.2.2 Kinetics consideration on glass formation

Besides thermodynamic considerations, kinetic considerations about the undercooled liquid and the nucleation and growth of crystals also play important roles to glass formation of BMGs, which are determined by viscosity of undercooled liquid. A lot of effort has been done to measure the viscosity of a liquid from the temperature above the melting point down to the temperature near the glass transition temperature T_g [43, 45-49]. The viscosity can be expressed in the form of Vogel-Fulcher-Tamman (VFT)

equation:

$$\eta(T) = \eta_0 exp\left(\frac{D^* \cdot T_0}{T - T_0}\right) \tag{1.2}$$

where D^* is the fragility parameter, η_0 is a constant and T_0 is the VFT temperature, where the barrier to flow would go to infinity.

The value of D^* can be considered as the degree of how the system obey the Arrhenius law; the value of T_0 is related to T_s and changes with the value of D^* [50]. The bigger the value of D^* is, the stronger glass former the system should be. **Figure 1.4** compares the viscosities of some selected different glass formers, which include BMGs and non-metallic glass formers [51]. According to **Figure 1.4**, SiO₂ has a D^* value of about 100, and it is the strongest glass former; O-terphenyl is a fragile glass former with a D^* value of 5. The viscosities of BMGs lie between these two strongest and the most fragile glass formers, but are closer to strong glasses. A strong liquid can help glass formation in the undercooled liquid. Liquid with high viscosity can impede the formation of nuclei, which makes the nucleation and growth of crystal much more difficult and thus the glass formation would be easier [52, 53].



Figure 1.4 Angell plot comparing viscosities of some selected glass forming liquids (adapted from Ref. [51]).

1.3 Evaluation of glass forming ability

Scientific efforts have been made to look for a parameter or criterion to evaluate or predict glass forming ability of metallic glasses since the first metallic glasses in Au-Si system was discovered [1]. To date, several parameters or criteria have been provided to explain why some composition ranges, such as compositions near eutectic points, may be easier to form glasses.

12

1.3.1 T_{rg} criterion

Among all the criteria, the reduced glass transition temperature criterion is the most famous one, it was first proposed by Turnbull [54], which is based on classic nucleation theory. When a liquid is cooled down below to a certain temperature, the melt can solidification bypass the crystallization but into glass; then this temperature can be defined as glass transition temperature T_g . The reduced glass transition temperature or T_{rg} is the ratio of the glass transition temperature T_g and the melting temperature T_m . Turnbull suggested that when $T_{rg} \ge 2/3$, the homogeneous nucleation of the crystalline phase in the melt should be suppressed to a low level that glass can be formed (as shown in **Figure 1.5**). This criterion was further modified by Lu et al. in 2000 [55]. They suggested using the liquidus temperature T_l to replace the melting temperature.

This criterion implies that compositions near eutectic points may be good glass formers, especially near "deep" eutectic. It is understandable because the glass transition temperature does not change too much with the changing of composition; however, the liquidus temperature usually changes more steeply. Furthermore, in the case of "deep" eutectic, the liquidus temperature may change sharply with the composition, which makes the value of T_{rg} strongly depends on the composition. Thus the value of T_{rg} should reach the highest point at the eutectic point (as shown in **Figure 1.6**), therefore the

formation of glass is easier at the eutectic composition. Although Turnbull's theory explains eutectic glasses very well, it still fails in many systems which glass formers are observed at off-eutectic compositions [34, 56]. For example, in Zr-Cu binary alloy system, the best glass former Cu_{64.5}Zr_{35.5} in the Cu₈Zr₃-Cu₁₀Zr₇ eutectic composition range did not correspond to the highest T_{rg} value [57].



Figure 1.5 Relationship between homogeneous nucleation rate I and the reduced temperature T_r (adapted from Ref. [54]).



Figure 1.6 Schematic variation of the T_g , T_l and T_{rg} in a typical binary eutectic system, which indicates T_{rg} reaches the highest value at the eutectic composition.

1.3.2 Three empirical rules proposed by Inoue

Based on the significant work of the synthesis of BMGs in various alloy systems [5, 18, 30, 58-62], Inoue summarized three basic empirical rules which may make the system favored to glass formation [9, 63]:

(1) The system should be a multi-component system which contains at least

three components. The formation of metallic glasses should become easier with the increasing number of the components. It can be easily understood because multi-components can increase the degree of the random packing of the atoms in the system, which leads to the increasing entropy of fusion thus the decreasing Gibbs free energy. This criterion is also consistent with the "confuse principle" proposed by Greer [41].

- (2) The atomic sizes of the components should be different. It is proposed that the atomic size difference should be at least 12%. This criterion is based on the structure and packing of atoms. The elements in the periodic table were divided into three groups by different atoms sizes [64]. By combination of atoms with significant differences in atom sizes could increase the density of random packing atoms, which increase the viscosity of the alloy liquid and makes the atomic diffusion sluggish in the undercooled liquid therefore the glass formation should be enhanced.
- (3) The heat of mixing of the components should be negative. The negative mixing heat could help to stabilize of the undercooled liquid and form a homogeneous glass state. This criterion also contributes to glass formation as efficient of random packing of atoms.

1.4 Pinpoint strategy to locate the best glass forming range

All the criteria mentioned above are all about how to find an alloy system that can form glass. But none of them provide an effective way to find the best glass former or the best glass forming range in a given alloy system. Ma et al. proposed a practical strategy to locate the best glass former or the best glass forming range [65] in 2005 and then this strategy was widely used [56, 57, 66-68]. By applying the competitive-growth principle, this strategy treats the glass phase as a competing phase, thus the process of glass formation should be a competition between the formation of glass phase and the crystalline phase, which involves nucleation and growth. It was suggested that the glass phase could form even the heterogeneous nucleation occurs, as long as the temperature of the glass transition is higher than the temperatures of all the other crystalline phases, due to the phase with the highest growth temperature is kinetically favored. During the cooling, the growth of all the crystalline phases are suppressed as the glass transition temperature is higher than the temperatures of all the crystalline phases, and this can be observed by investigation of the microstructure of alloys with continuous changing compositions.

Figure 1.7 summarizes the changing of microstructure of two different

eutectic systems with the changing of cooling rate and composition. With the glass formation, the microstructure of alloys with continuous changing compositions would change from a composite structure (a primary phase label as α plus amorphous phase) to fully amorphous to another composite structure (another primary phase label as β plus amorphous phase). The difference is, in a regular eutectic system, the best glass forming range includes the eutectic composition; but in an irregular eutectic system, the best glass forming range glass forming range would be away from the eutectic composition.



Figure 1.7 Phase-formation diagrams which show the glass and composite forming range of (a) a regular eutectic system and (b) an irregular eutectic system.

1.5 Glass formation in Zr-Cu and Zr-Cu-Ti alloy systems

Zr- based BMGs have been attracted much attention because their high glass forming ability and the superior mechanical properties such as high strength, high ductility and high elastic limit [69]. Until now, many BMG alloy systems have been developed in Zr- based alloys, for instance, Zr-Ti-Cu-Ni-Be [17], Zr-Al-Ni-Cu [18, 30, 70], Zr-Cu-Al [67, 71, 72]. In this section, a brief introduction will be given to the glass formation of Zr-Cu binary alloy system and Zr-Cu-Ti ternary alloy system.

1.5.1 Glass formation in Zr-Cu binary alloy system

Among all the metal-metal binary system, the Zr-Cu binary system has an outstanding glass forming ability. The studies about Zr-Cu system have been carried out for almost 30 years, including the calculation of phase diagram, glass formation, mechanical property [73-75], modeling and so on.

Zr-Cu system is an easy glass formation system; the glass formation range is wide and can be formed by different methods. In 1984, Atzmon et al. formed amorphous in Zr-Cu system by solid-state reaction [76], the amorphous had a composition of Cu₆₀Zr₄₀. In 2004, Wang et al. reported that Cu_{64.5}Zr_{35.5} alloy can be formed 2 mm amorphous rod by liquid quenching [57], which was the off-eutectic composition in Cu₈Zr₃-Cu₁₀Zr₇ eutectic range. At the meanwhile, Xu et al. also discovered a 2 mm metallic glass with a similar composition of Cu₆₄Zr₃₆ [77], this 0.5% atomic difference of composition can be contributed to the composition accuracy. Inoue reported that alloy Cu₄₅Zr₅₅, located near the eutectic point of Cu₁₀Zr₇-CuZr eutectic range, had a 1.5 mm glass forming ability [78]. Tang et al. reported Cu₅₀Zr₅₀ alloy also had a 2 mm glass forming ability [79], unusually, this composition is a line compound.

In 2008, by combining the sputter-deposited technique and micro-cantilever, Li et al. discovered three localized best glass formers by studying the density change of continuously changing compositions [80]. The critical sizes of these three compositions were: 1.14 ± 0.04 mm for Cu₆₄Zr₃₆, 1.14 ± 0.04 mm for Cu₅₀Zr₅₀ and 1.02 ± 0.04 mm for Cu₅₆Zr₄₄, respectively. The first two compositions were consistent with that in Ref. [57, 77] and that Ref. [79]; and the difference in the critical size should be understandable due to the wedge-casting method used in Ref. [80] had a lower cooling rate. However, the third composition, Cu₅₆Zr₄₄ was the first time reported.

In 2009, a new family of metallic glass, so called "intermetallic glass", was first reported by Wu and Li [81]. In their work, two optimized compositions, Cu_{51.5}Zr_{48.5} and Cu₄₉Zr₅₁, with 2 mm glass forming ability were obtained

19
through liquid quenching, meanwhile, the 2 mm rod of alloy Cu₅₁Zr₄₉ showed fully crystalline structure. In another word, two glass forming ranges near but separated by the CuZr intermetallic compound have been demonstrated. This phenomenon was quite different from all the research results mentioned above: these two glass forming ranges cannot be contributed to the T_{rg} theory as the compositions were far from eutectic points and their corresponding eutectic glasses (Cu₅₆Zr₄₄ [80]and Cu₄₅Zr₅₅ [78]) but near intermetallic phase; in addition, unlike amorphous obtained through solid-state reaction, the glass forming ranges did not cover the whole center part of the phase diagram [82-85]. The different glass forming ranges by apply different theories and methods are summarized in **Figure 1.8**.

The formation of the intermetallic glass was interpreted by the hypothetic free energy curves of liquid and intermetallic phases. Generally, the free energy of the liquid (amorphous) phase varies gradually along with the composition, while that of the CuZr intermetallic phase varies sharply around the stoichiometric composition. Since the amorphous phase has a lower free energy in the vicinity of the CuZr intermetallic, it is favored thermodynamically to form glass if the kinetic constraint can suppress the solidification of the primary crystalline phases. It is believed that this work provides a new perspective to find new metallic glasses.



Figure 1.8 An schematic illustration of the glass forming ranges of the general metallic glass obtained by applying different theories and methods.

To summarize the glass forming ability in Zr-Cu binary system, **Table 1.3** lists the glass forming compositions with their corresponding critical sizes and the method used. It is clearly that Zr-Cu binary system is easy for glass formation through both liquid quenching and solid-state reaction. The glass forming range of Zr-Cu system is wide and also being studied carefully, which will be introduced in the following section.

Composition	Critical size	Method	Ref.
	(mm)		
Cu ₆₀ Zr ₄₀	<1	Solid-State reaction	[76]
Cu64.5Zr35.5	2	Copper mold casting (rod)	[57]
Cu ₆₄ Zr ₃₆	2	Copper mold casting (rod)	[77]
Cu45Zr55	1.5	Copper mold casting (rod)	[78]
Cu50Zr50	2	Copper mold casting (rod)	[79]
Cu50Zr50	1.14 ± 0.04		
Cu ₅₆ Zr ₄₄	1.02 ± 0.04	Wedge casting (wedge shape)	[80]
Cu ₆₄ Zr ₃₆	1.14 ± 0.04		
Cu49Zr51	2	Conner mold casting (red)	[01]
Cu51.5Zr48.5	Z	Copper mole casting (rod)	[01]

Table 1.3 Summary of glass forming ability in Zr-Cu binary system.

Furthermore, there are also a plenty of work to calculate the phase diagram and the free energy curves of liquid, solid solution and intermetallic phases of Zr- Cu binary system, in order to predict glass forming range in this system [86-90]. **Figure 1.9** shows the calculated phase diagram of Zu- Cu binary system. In 1988, Saunders calculated the TTT curve of Zr- Cu system [91], and then the critical cooling rate was also calculated as 5×10^7 K/s. An assumption was made that the glass can be formed when the value of critical cooling rate for a certain composition is less than 5×10⁷ K/s. Due to the fact that the melt-spinning usually has a maximum cooling rate of ~1×10⁷ K/s, the calculated glass forming range should be comparable to the experimental results by melt-spinning . The glass forming range was predicted as from ~25 to ~70 atomic percent of Zr. Actually, this prediction was in good agreement to the experimental results. Altounian indicated a glass forming range from composition Cu₇₀Zr₃₀ to Cu₂₅Zr₇₅ by studying the crystallization behavior of alloys in this range [92]. Kneller also reported a similar glass forming range was reported by Buschow, which covered from composition Cu₃₀Zr₁₀ to Cu₂₅Zr₇₅ [94, 95]. It was noticed that all these results were produced by melt-spinning method, so the glass forming range should be wider than the results listed in **Table 1.3**.



Figure 1.9 Calculated phase diagram of Zr-Cu binary system.

Li et al. calculated the driving force of the crystallization in Zr- Cu system [96]. By the consideration that glass formation is the competition between the crystalline phase and the amorphous phase during the solidification, the optimized glass formers should locate at the compositions with the localize minima crystallization driving forces. As shown in **Figure 1.10**, there were four compositions had the localize minima crystallization driving forces; they all showed agreement in the reported glass formers listed above except composition with 0.068 mole fraction of Zr. This may be caused by the lack of consideration of kinetic point of view.



Figure 1.10 The calculated surface of the crystallization driving force for Zr- Cu system at 800K as well as the optimum glass formers (adapted from Ref. [96]).

In a word, the Zr-Cu system can form metallic glasses by both liquid quenching and solid-state reaction. It was reported that Zr-Cu showed a large negative heat of mixing [64], which may further help the glass formation [9]. Glass forming ranges are wide, which covers eutectic, off-eutectic and intermetallic compositions.

1.5.2 Glass formation in Zr-Cu-Ti tenary alloy system

According to Inoue [9, 64], the Zr-Cu-Ti ternary alloy system can be classified into glass forming group with elements from ETM and LTM, which represents early transition metal (elements belong to group IIIA-VIIA in the periodic table) and late transition metal (elements belong to group VIIIA-IIB in the periodic table) respectively. The glass forming ability of this ternary will be briefly introduced in the following.



Figure 1.11 Pseudo-ternary phase diagram of Ti-Zr-Cu-Ni system with two glass forming ranges (adapted from Ref. [97]).

In 1988, Massalski et al. reported a wide glass forming range in Zr-Cu-Ti system through melt-spinning method [98]. The resulting ribbons had a thickness about 50 μ m. The widest range reported was across the whole region of the phase diagram at about 50 atomic percent of Cu. In 1995, Lin et

al. discovered Ti₃₅Zr₁₀Cu₅₅ metallic glass with critical thickness of 500 μm; the critical cooling rate was estimated at a level of 2×10⁴K/s [97]. Meanwhile, a pseudo-ternary alloy system Ti-Zr-Cu-Ni was also reported. Two glass forming ranges, both Ti- rich region and Zr- rich region, were located with a maximum 4mm glass forming ability (as shown in **Figure 1.11**) [97].



Figure 1.12 The liquid projection of the ternary phase diagram of Cu-Zr-Ti system. Three eutectic points marked as blue square were given by Woychik [99]; and five eutectic points marked as red circles were given by Arroyave [100] (adapted from Ref. [51]).

Later, Inoue et al. studied the glass formation of compositions $Cu_{60}Zr_{40-x}Ti_x$, where x=0-40 at% [101, 102]. $Cu_{60}Zr_{30}Ti_{10}$ was the best glass former with 4mm glass forming ability. More recently, a series of metallic glasses were reported around the eutectic point E₃' with the composition of Cu₅₂Zr₄₀Ti₈ (as shown in **Figure 1.12**) with also have 4mm glass forming ability [103]. There were five compositions in this new glass forming range can form 4mm glass: Cu₅₂Zr₄₂Ti₆, Cu₅₁Zr₄₂Ti₇, Cu₅₁Zr₄₁Ti₈, Cu₅₂Zr₄₀Ti₈ and Cu₅₁Zr₄₀Ti₉. **Figure 1.13** summarizes the independent glass forming ranges from different references.



Figure 1.13 Summary of different glass forming ranges in Zr-Cu-Ti system. The red line, blue circle and the green dot represent glass formers from different references [97, 101-103].

1.6 Motivation and outline of this thesis

The underlying of the formation of intermetallic glass is still an unsolved question. The purpose of this thesis is to further investigate the mechanism of formation of intermetallic glass from both thermodynamic and kinetic points of view. Two alloy systems (Zr-Cu binary system and Zr-Cu-Ti ternary system) are selected to systematically study the glass forming ability first and then an interpretation is provided. There are five chapters in this thesis.

In Chapter 1 (this chapter), the development and general knowledge of BMGs was introduced. The glass formation of Zr-Cu and Zr-Cu-Ti systems was reviewed, followed by the motivation and the outline of this study.

In Chapter 2, schematic pictures of all equipments used in this thesis are provided. Furthermore, the experimental procedures and details are also provided.

In Chapter 3, the glass formation near intermetallic phases of Zr-Cu system is carefully studied. The underlying mechanism is provided in both thermodynamic and kinetic perspectives by studying the crystallization driving force, the viscosity of the liquid and the TTT curves of the selected compositions. In Chapter 4, the glass formation of two different composition zones in Zr-Cu-Ti ternary system is studied. And the glass forming range of Zr-Cu-Ti system was calculated by Miedema method.

Finally, the results of this thesis are summarized and topics for future research were suggested in Chapter 5.

Chapter 2 Experimental

procedures

2.1 Preparation of master alloys

The ingots of master alloy were prepared by arc melting a mixture of Zr with a purity of 99.98%, Cu with a purity of 99.9998% and Ti with a purity of 99.99%. The melting process was carried out under a high purity argon atmosphere in the Edmund Buhler LSG-400 arc melting system. Every ingot was re-melted at least six times to obtain chemical homogeneity. The weight loss during the melting was controlled within 0.3% to maintain the composition accuracy. The ingots were cut into pieces to cast into different shape.

2.2 Casting procedures

Different casting methods were used depending on the thickness or the shape required.

2.2.1 Melt-spinning

The melt-spinning method was used to produce ribbons; the cooling rate of melt-spinning can reach 10⁶K/s. The melt-spinning was carried out in the Edmund Buhler D-7400 single roller system, the diameter of the copper wheel is 20cm. The alloy was get from the master alloy and then placed into a quartz tube with a nozzle of ~0.4 mm in diameter. The quartz tube was placed into the center of the induction coil. The chamber was vacuumed first followed by backfilling argon gas to a certain pressure. The alloy was melted by the inducted current, and then the valve located at the top of the quartz tube was opened to let the high purity argon (with a higher pressure than the pressure in the chamber) gas in. The melt was ejected out by the input high pressure argon gas from the nozzle to cool down on the surface of a fast rolling copper wheel into a ribbon shape. **Figure 2.1** is a schematic diagram of the melt-spinning equipment and the procedure. The thickness of the ribbon can

be modified by changing the rolling speed of the copper wheel: the faster the rolling speed was, the thinner the ribbon would be. In this thesis, the rolling speed of the copper wheel changes from 35m/s to 45m/s.



Figure 2.1 A schematic diagram of the melt-spinning equipment.

2.2.2 Wedge casting method

The wedge casting method was widely used to study the critical thicknesses of the metallic glasses. The accurate critical size can be easily determined due to the wedge shape with gradually changed thickness. The experimental condition of wedge casting method was as similar as the melt-spinning method, except the melt was injected into copper mold with wedge shape instead of being ejected on the surface of a fast rolling copper wheel. **Figure 2.2** is a schematic diagram of the wedge casting method.



Figure 2.2 A schematic diagram of the wedge casting method.

2.2.3 Suction casting method

The suction casting method was used to produce rods with diameter of 3 mm or less. The equipment was modified from the Edmund Buhler D-7400 MAM-1 mini arc melting system: a cylindrical copper mold connecting to a container replaced the original copper crucible. The container was used to introduce a pressure difference between the chamber and the container so the melt can be sucked into the copper mold during the casting.



Figure 2.3 A schematic diagram of the suction casting equipment.

Figure 2.3 is a schematic diagram of this suction casting equipment. The container was pre-vacuumed to a certain pressure followed by the closing of the valve. After this, the chamber was backfilled with argon gas (to a higher pressure than that of container). The alloy was melt on the top of the copper mold and then the valve was opened so the pressure difference between the container and the chamber can suck the melt into the copper mold immediately. The diameter of the rod was 3 mm; the length of the rod was 30

mm, as long as the copper mold.

2.2.4 Copper mold casting

Copper mold casting was used to cast rods with diameter larger than 3 mm in this thesis. The casting procedure was carried out in the chamber of the Edmund Buhler LSG-400 arc melting system, the same system as the preparation of the master alloys. The master alloy was re-melted for several times to get the chemical homogeneity; and then the melt would be poured into the copper mold before the solidification occurred by rotating the copper crucible, with the electric storm on. Rods with different diameters were obtained by using different molds. **Figure 2.4** is an interior photo of the arc melting system with copper mold in it.



Figure 2.4 A photo of the LSG-400 arc melting system with copper mold in it.

2.3 Microstructure characterization

X-ray diffraction (XRD), optical microscopy (OM) and scanning election microscopy (SEM) were the general methods to characterize the samples.

2.3.1 X-ray diffraction (XRD)

The X-ray diffraction (XRD) was used to identify the amorphous phase or the crystalline phases if existed. The scanning was carried out in the Bruker D8 Advanced XRD machine with Cu-K α radiation (λ = 1.5402 Å). The current and the voltage were set as 40 mA and 40 kV, respectively. The step size is 0.005° and the time step is 0.25s. For the ribbon samples, the ribbons were fixed on a glass plate with double-side tape with the chill-side faced up. For the rod samples, they were mounted and then were polished to the central part of the rod longitudinally (the detail of the mounting and polishing would be mentioned in the next section).

2.3.2 Optical microscopy (OM) and scanning election microscopy (SEM)

The samples for OM and SEM were mounted into resin first, and then they were carefully grinded with 80 to 1200 grit silicon carbide papers to the central part of the rods or wedge samples longitudinally. Finally they were polished by 1 μm powder Al suspension. The samples were etched by a solution mixed by 65% HNO₃ and 50%HF at ratio 9:1. The etching time would be different for different alloy systems: for Zr-Cu system, it should be about 3 seconds and the time was about 60 seconds for the Zr-Cu-Ti system.

Optical microscopy was carried out by using an Olympus PME 3 optical microscope. The critical sizes of wedge sample were measure under OM by using a lens with ruler. The critical size of wedge sample was defined as the width of the wedge at the boundary between the crystalline phase and the amorphous phase, as shown in **Figure 2.5**. Scanning election microscopy (SEM) was carried out by using Philips XL30 FEG SEM.



Figure 2.5 A schematic diagram of the measurement of critical size of wedge sample.

2.4 Thermal analysis

The differential scanning calorimetry (DSC) was carried out by using TA instruments DSC 2920 machine. The DSC was calibrated by pure In and Zn first, and then the samples were heated with different heating rates in argon atmosphere. The glass transition temperature T_g , the onset crystallization temperature T_x and the enthalpy of crystallization, which is the area covered by the crystallization peak, can be obtained by analyzing the resulting DSC curves. The Universal Analysis program is used to do the analyzing.

The measurements of the melting temperature T_m and the liquidus temperature T_l were carried out in the Netzsch 404 Pegasus DSC machine. The heating rate was set as 0.17 K/s. The resulting traces were analyzed by the Proteus Analysis program.

Chapter 3

The formation of intermetallic

glasses in Zr–Cu system

3.1 Introduction

Basically, there are two common methods to form metallic glasses, one is thought liquid quenching and the other one is solid-state reaction. (1) Liquid quenching: Turnbull's earlier paper indicated that a larger reduced glass transition temperature T_{rg} value ($T_{rg}=T_g/T_l$, where T_g and T_l are the glass transition temperature and liquidus temperature, respectively) may lead to a smaller nucleation rate and subsequently a better glass-forming ability [54]. This makes bulk metallic glasses (BMGs) through liquid quenching 40 commonly to be formed near the eutectic compositions, specifically deep-eutectic compositions [51, 91, 104, 105]. (2) Solid-state reaction method: film or powders of MGs can be formed through isothermal inter-diffusion or mechanical milling below glass transition temperature, respectively [82-84, 106-108]. Usually, the alloy system, which can form metallic glasses through this method, has a large negative heat of mixing. Unlike the glass forming ranges through liquid quenching, the glass forming ranges obtained by solid-state reaction can cover the whole central part of the phase diagrams, including the intermetallic compounds.

However, the recent discovery so called "interemtellic glass" by Wu and Li provided a new perspective for searching new metallic glasses [81]. In their work, a pair of bulk metallic glasses (Cu_{51.5}Zr_{48.5} and Cu₄₉Zr₅₁) with 2 mm critical size was obtained by liquid quenching in the Zr-Cu binary alloy system, next to the intermetallic formed fully crystalline phase. This phenomenon is quite different from that of all the BMGs obtained through liquid quenching as the glass formation ranges are around intermetallic phase instead of eutectic point. Also, it is also distinguished from the glass obtained from solid-reaction method as the glass formation range did not cover the whole central part of the phase diagram.



Figure 3.1 Part of Zr-Cu phase diagram and the corresponding hypothetical free energy curves. The red lines represent glass forming regions and two solid circles are two intermetallic glass formers. The eutectic glasses are marked as open circles (adapted from Ref. [81]).

An explanation had been provided as indicated in **Figure 3.1**. In the vicinity of stoichiometric composition, the CuZr intermetallic phase has the lowest Gibbs free energy as marked as blue line. When the composition shifts lightly

away from the CuZr intermetallic phase, the liquid phase (amorphous phase) has the lowest Gibbs free energy due to the different rising rates of the free energy between the liquid phase and the intermetallic phase. This makes two separated thermodynamically favored glasses formed close to the intermetallic phase, when the crystallization of intermetallic phase was suppressed during liquid quenching.

In this chapter, we systematically studied the glass formation near all the intermetallics in the Zr-Cu system. The same phenomenon (the formation of "intermetallic glass") was observed for these intermetallics: Cu₅₁Zr₁₄, Cu₈Zr₃, Cu₁₀Zr₇, and CuZr₂ intermetallics; and interpretation from both thermodynamic and kinetic aspects have also been provided.

3.2 Results

There are six intermetallics in the Cu-Zr system (i.e. Cu₉Zr₂, Cu₅₁Zr₁₄, Cu₈Zr₃, Cu₁₀Zr₇, CuZr and CuZr₂), and the glass formation near Cu₅₁Zr₁₄, Cu₈Zr₃, Cu₁₀Zr₇ and CuZr₂ intermetallics is studued.

3.2.1 Glass formation near CuZr₂ intermetallic

For alloys with compositions near CuZr₂ intermetallic, the alloys are cast into wedge shape to determine the critical sizes. Figure 3.2 shows the SEM cross-section photos for wedge cast samples with compositions changing from Cu_{36.33}Zr_{63.67} to Cu_{30.33}Zr_{69.67}, and the boundaries between crystallization phase and amorphous phase are pointed by arrows. The critical thicknesses were obtained by measuring the width of these wedges at arrows and summarized in Figure 3.3. It clearly shows that alloys CuZr₂ (Cu_{33,33}Zr_{66.67}), Cu32.83Zr67.17 and Cu32.33Zr67.67 are almost fully crystalline structure. The critical thickness reaches 470 µm at composition Cu34.33Zr65.67 and falls down to 360 µm at composition Cu_{36.33}Zr_{63.67} when Zr content decreases. On the other side, when more Zr is added, the critical thickness reaches maximum 400 µm at composition Cu31.33Zr68.67 and goes down to 300 µm at composition Cu30.33Zr69.67 by further addition of Zr. So in the studied composition range, there are two peaks in glass forming ability at compositions Cu34.33Zr65.67 and Cu31.33Zr68.67 respectively, which are located at different sides of CuZr₂ intermetallic. To confirm this result, all wedges were cut at the thickness about 500 µm for the DSC (indicated by the red line in Figure 3.2). The DSC results are shown in Figure 3.4. Enthalpies of crystallization of these wedges are plotted together with critical size in Figure 3.3.



Figure 3.2 SEM photos of wedge cast samples with compositions from Cu_{36,33}Zr_{63,67} to Cu_{30,33}Zr_{69,67}. The arrows all point to the critical thicknesses (boundary between crystalline phase and amorphous phase) and the red line represents the cutting edge for the DSC test.



Figure 3.3 Summary of critical sizes and the enthalpy of crystallization of wedge cast samples.

The changing of the values of enthalpy of crystallization is in good agreement with the changing of corresponding critical thicknesses. CuZr₂ (Cu_{33,33}Zr_{66,67}), Cu_{32,83}Zr_{67,17} and Cu_{32,33}Zr_{67,67} have the lowest enthalpies of crystallization of 30.0 J/g, 8.6 J/g and 20.5 J/g, respectively, as same as they have the smallest critical thicknesses. Enthalpies of crystallization for compositions Cu_{34,33}Zr_{65,67} and Cu_{31,33}Zr_{68,67} (two optimum glass formers) are 91.3 J/g and 56.8 J/g respectively, which are the highest two values among their neighborhood compositions. This further confirms that there is a pair of optimum glass formers formed separated of CuZr₂ intermetallic.



Figure 3.4 DSC curves of the tip parts of wedge cast samples.

3.2.2 Glass formation near Cu₁₀Zr₇ intermetallic

For alloys with compositions near Cu₁₀Zr⁷ intermetallic, the alloys are also cast into wedge shape to determine the critical sizes. **Figure 3.5** shows the cross-section optical photos of these wedge cast samples, with arrows point to the boundaries between crystallization phase and amorphous phase. The critical thicknesses can be obtained by measuring the width of the wedges where the arrows located, and the changing of critical thicknesses with compositions near Cu₁₀Zr₇ intermetallic is summarized in **Figure 3.6**.



Figure 3.5 OM photos of wedge cast samples with compositions from Cu_{60.32}Zr_{39.68} to Cu_{57.32}Zr_{42.68}. The arrows all point to the critical thicknesses.

It shows that the critical thickness increases from 320 μ m at Cu_{60.32}Zr_{39.68} to the highest point of 520 μ m at Cu_{59.32}Zr_{40.68}, and then decreases to 380 μ m at Cu₁₀Zr₇ (Cu_{58.82}Zr_{41.18}). The critical thickness reaches another peak point of 460 μ m at Cu_{58.32}Zr_{41.68} when the Zr content keeps increasing and finally falls down to 320 μ m again at Cu_{57.32}Zr_{42.68}. The minimum critical thicknesses of 320 μ m on both ends of this composition ranges and the critical thickness of 380 μ m at Cu₁₀Zr₇ suggest that there are two peaks in glass forming ability (520 and 460

μm respectively) among these compositions, which are located at different sides of Cu₁₀Zr₇ intermetallic. **Figure 3.7** shows all DSC curves for all wedge cast samples at width about 520 μm, and the trend of enthalpy of crystallization is almost consistent with that of critical thicknesses. The enthalpy of crystallization for all samples are calculated and summarized in **Figure 3.2**. Enthalpies of crystallization for compositions Cu_{59,32}Zr_{40.68} and Cu_{58,32}Zr_{41.68} are 53.2 J/g and 44.2 J/g respectively, which are the highest two values of among their neighborhood compositions. This further confirms that there is a pair of optimum glass formers formed separated of Cu₁₀Zr₇ intermetallic.



Figure 3.6 Summary of critical sizes and the enthalpy of crystallization of wedge cast samples.



Figure 3.7 DSC curves of the tip parts of wedge cast samples.

3.2.3 Glass formation near Cu₅₁Zr₁₄ intermetallic

The glass forming ability near Cu₅₁Zr₁₄ phase, which has the highest melting point among the studied intermetallics, is relatively poor. The glass formation of six compositions (Cu_{79.96}Zr_{20.04}, Cu_{79.46}Zr_{20.54}, Cu_{78.96}Zr_{21.04}, Cu_{78.46}Zr_{21.54}, Cu_{77.96}Zr_{22.04} and Cu_{78.46}Zr_{22.54}) was carefully studied and only ribbons with thickness about 15 µm were obtained. **Figure 3.8** shows the results of DSC studies of these ribbons. Although the enthalpies of crystallization are small, there are three compositions exhibiting the presence of amorphous phase: Cu₅₁Zr₁₄ (Cu_{78.46}Zr_{21.54}), Cu_{79.46}Zr_{20.54} and Cu_{79.96}Zr_{20.04}. In the middle of these

three alloys, the enthalpy of crystallization of Cu_{78.96}Zr_{21.04} is zero, indicating it has a fully crystalline structure. These DSC results are in good agreement with the corresponding XRD patterns of chill-side of these ribbons (as shown in **Figure 3.9**). Due to the small amount of amorphous, only tiny humps of amorphous phase with peaks of Cu₅₁Zr₁₄ crystalline phase can be seen in the patterns of Cu_{78.46}Zr_{21.54}, Cu_{79.46}Zr_{20.54} and Cu_{79.96}Zr_{20.04}. Both DSC and XRD results confirm two peaks of glass forming ability near Cu₅₁Zr₁₄ intermetallic.



Figure 3.8 DSC curves of 15 µm ribbons of compositions near Cu₅₁Zr₁₄ intermetallic.



Figure 3.9 XRD patterns of the chill-side of the ribbons with compositions near Cu₅₁Zr₁₄ intermetallic.

3.2.4 Glass formation near Cu₈Zr₃ intermetallic

Finally, glass forming ability near Cu₈Zr₃ intermetallic is also studied. **Figure 3.10** shows the DSC curves for ribbons with 20 μ m thickness of six compositions (from Cu_{74.23}Zr_{25.77} to Cu_{71.73}Zr_{28.27}). The enthalpies of crystallization are listed in **Figure 3.10**. The DSC results show that there are amorphous phase in compositions Cu₈Zr₃ (Cu_{72.73}Zr_{27.27}), Cu_{72.23}Zr_{27.77} and Cu_{71.73}Zr_{28.27}. The XRD patterns of the chill-side of these ribbons are shown in **Figure 3.11**. The XRD patterns of compositions Cu₈Zr₃, Cu_{72.23}Zr_{27.77} and Cu_{71.73}Zr_{28.27} clearly show that crystalline diffraction peaks are located on a broad amorphous hump. This is consistent with the DSC results.



Figure 3.10 DSC curves of 20 µm ribbons of compositions near Cu₈Zr₃ intermetallic.



Figure 3.11 XRD patterns of the chill-side of the ribbons with compositions near Cu₈Zr₃ intermetallic.

However, compositions Cu_{74.23}Zr_{25.77}, Cu_{73.73}Zr_{26.27} and Cu_{73.23}Zr_{26.77} show no evidence of amorphous phase in both DSC and XRD results. It can be explained that the liquidus line drops with the increasing Zr content (as showed in **Figure 3.12**) near Cu₈Zr₃ intermetallic, and compositions with lower liquidus temperatures can be quenched into amorphous phase much more easily. This may cause all the compositions with high Zr content (Cu₈Zr₃, Cu_{72.23}Zr_{27.77} and Cu_{71.73}Zr_{28.27}) can form amorphous in the ribbons with 20 µm thickness but compositions (Cu_{74.23}Zr_{25.77}, Cu_{73.73}Zr_{26.27} and Cu_{73.23}Zr_{26.77}) with low Zr content cannot. Therefore, according to the enthalpies of crystallization of the alloys, there is only one peak in glass forming ability near Cu₈Zr₃ intermetallic.



Zr at%

Figure 3.12 Partial Cu-Zr binary phase diagram.

In summary, glass formation near Cu₅₁Zr₁₄, Cu₈Zr₃, Cu₁₀Zr₇, and CuZr₂ intermetallics has been studied. Including the previous results on CuZr intermetallic, the formation of intermetallic glass, i.e. two peaks in glass 55
forming ability near but separated by the intermetallic phase, has been confirmed. Only Cu₈Zr₃ intermetallic is an exception, while there is only one peak in glass forming ability near it. This may be caused by the fact that Cu₈Zr₃ intermetallic is a peritectic phase. To compare the composition range of glass formation of eutectic glasses and intermetallic glasses, the critical sizes and the corresponding compositions of all the glass formers in Cu-Zr binary system summarized in **Table 3.1** and are also plotted in are Figure 3.13 [57, 78, 81, 109-111]. It clearly shows that the intermetallic glasses have different glass formation ranges from those of the eutectic glasses. Furthermore, despite the fact that the composition is very close to the intermetallic compound, the intermetallic glass is capable to form bulk size sample, e.g. the glass near CuZr intermetallic can form 2 mm rod, which equals to the critical size of eutectic glass formers [81]. Moreover, for compositions near each intermetallic, the only phase detected by XRD is the corresponding intermetallic phase.

Composition	Eutectic		Intermetallic	
range	Composition	Critical size	Composition	Critical size
			Cu79.46Zr20.54	<15 µm
Cu 51 Zr 14			Cu78.46Zr21.54	<15 µm
Cu51Zr14-				
Cu10Zr7	Cu64.5Zr35.5	2 mm		
			Cu59.32Zr40.68	520 μm
$Cu_{10}Zr_7$			Cu58.32Zr41.68	460 μm
Cu10Zr7-				
CuZr	Cu45Zr55	1.5 mm		
			Cu51.5Zr48.5	2 mm
CuZr			Cu49Zr51	2 mm
CuZr-				
CuZr ₂	Cu ₅₆ Zr ₄₄	1 mm		
			Cu34.33Zr65.67	470 um
CuZr ₂			$C_{1121,22} \overline{7} r_{c0,c7}$	400 um
			CU31.33Z108.0/	του μπ

 Table 3.1 Summary of the critical sizes of both eutectic glass formers and intermetallic glass formers



Figure 3.13 Partial of Cu-Zr binary phase diagram and summary of the critical sizes of both eutectic glass formers and intermetallic glass formers.

3.3 Discussion

3.3.1 Calculation of Gibbs free energy of liquid and intermetallic phases as a function of composition by CALPHAD method

It has been revealed that GFA is correlated with crystallization driving force whereas a smaller crystallization force often accompanies a better GFA [40, 43, 44, 112]. Generally, two methods are often used to calculate the free energy of liquid and intermetallics phases. One is the CALPHAD method (calculation of phase diagram) [113-119]. The other method is based on the Miedema model [120-123]. Here, CALPHAD method was used to calculate the Gibbs free energy as function of composition of liquid and interemetallic phases and the corresponding crystallization driving forces for the Cu₅₁Zr₁₄, Cu₁₀Zr₇, CuZr and CuZr₂ intermetallics.

3.3.1.1 Calculation of free energy of liquid phase

In this thesis, substitutional solution model in CALPHAD method [114] is employed to calculate the Gibbs free energy, *G*. The Gibbs free energy of the liquid phase can be described as [114]:

$$G = G^{ref} + G^{id} + G^{ex} \tag{3.1}$$

where G^{ref} is the contribution of the pure constituents, G^{id} is the contribution of ideal mixing, and G^{ex} is the non-ideal mixing contribution or the excess part:

$$G^{ref} = x_{Cu}{}^{0}G_{Cu}(T) + x_{Zr}{}^{0}G_{Zr}(T)$$
(3.2)

$$G^{id} = RT(x_{Cu} \ln(x_{Cu}) + x_{Zr} \ln(x_{Zr}))$$
(3.3)

$$G^{ex} = x_{Cu} x_{Zr} \sum_{m=0}^{m} L^{m}_{Cu,Zr} \left(x_{Cu} - x_{Zr} \right)^{m}$$
(3.4)

where x_{Cu} and x_{Zr} are the molar fraction of Cu and Zr. The Gibbs free energy of pure element in liquid phase as function of temperature, ${}^{o}G_{i}(T)$, can be described as:

$${}^{0}G_{i}(T) = a + bT + cT\ln(T) + dT^{2} + eT^{1} + fT^{3} + gT^{4} + hT^{7} + kT^{9}$$
(3.5)

where *a*, *b*, *c*, *d*, *e*, *f*, *g*, *h* and *k* are coefficients, and they may have different values under different temperatures; and here *i* represents Cu or Zr. In this chapter, the corresponding values of these coefficients for Cu and Zr were taken from the Ref. [124].

The parameter $L^m_{Cu,Zr}$ in equation (3.4) can be expressed as a function of

temperature, where m = 0 or 1 or 2 in liquid phase:

$$L_{Cu,Zr}^{m} = A + BT + CT \ln(T)$$
(3.6)

3.3.1.2 Calculation of free energy of intermetallic phases

All intermetallic compounds were treated as stoichiometric phases due to the fact that there were no homogeneity ranges for these intermetallic compounds. The Gibbs free energy of compound Cu_iZr_j can be expressed as [125]:

$$G^{Cu_{i}Zr_{j}}(T) = x_{Cu}^{0} G^{FCC}_{Cu} + x_{Zr}^{0} G^{HCP}_{Zr} + C + DT$$
(3.7)

where ${}^{0}G_{Cu}^{FCC}$ and ${}^{0}G_{Zr}^{HCP}$ are the free energies of pure Cu and Zr in stable solid state at 298.15K under 1 atm (the stable states are FCC_A1 for Cu and HCP_A3 for Zr), which can be obtained in Ref. [124]. The *C* + *DT* part is the Gibbs free energy of formation of intermetallic phase. Here, the values of *C* and *D* were taken from Ref. [125] to calculate the free energy of Cu₅₁Zr₁₄, Cu₁₀Zr₇, CuZr and CuZr₂ intermetallic compounds.

3.3.1.3 The resulting Gibbs free energy of liquid and intermetallic phases

By applying eqs (3.1) to (3.7), the Gibbs free energy of liquid phase as a function of composition and that of intermetallic compositions has been calculated, as shown in Figure 3.14. The temperatures used are the corresponding glass transition temperatures (as listed in **Table 3.2**). As the T_g of Cu₅₁Zr₁₄ intermetallic is not obvious, T_x is used instead. All the expressions of the Gibbs free energies of the liquid and intermetallic phases are listed in Table 3.3. The crystallization driving forces at compositions of Cu₅₁Zr₁₄, Cu10Zr7, CuZr and CuZr2 intermetallic compounds are plotted with the corresponding maximum critical thicknesses in Figure 3.15. It shows that CuZr intermetallic compound has the smallest crystallization driving force, followed by Cu₅₁Zr₁₄, Cu₁₀Zr₇, and then CuZr₂ intermetallic. On the other hand, the maximum critical thickness around CuZr intermetallic is 2 mm, which is the largest one, followed by Cu10Zr7 intermetallic (520 µm), CuZr2 intermetallic (470 μ m), and then Cu₅₁Zr₁₄ intermetallic (< 15 μ m). It reveals that a smaller crystallization driving force is correlated with a better glass forming ability. The only exception is Cu51Zr14 intermetallic, which has a smaller crystallization force than CuZr² intermetallic but worse glass forming ability. However, this can be explained that Cu₅₁Zr₁₄ intermetallic has the highest melting temperature among all these four intermetallics, which makes the glass formation more difficult. This may imply that thermodynamic may not

be the sole determining factor for the glass formation of intermetallic glass.

Figure 3.16 shows the changing of crystallization driving force of all these four intermetallics as a function of temperature. This result is in a good agreement with the results obtained in other multi-component systems [40, 43, 44, 112], where a smaller crystallization driving force implies a smaller critical cooling rate or a better glass forming ability.

Table 3.2 Temperature of T_g and T_x of Cu₅₁Zr₁₄, Cu₁₀Zr₇, CuZr and CuZr₂ intermetallics.

	T _g (K)	T _x (K)	T _m (K)	T_{rg}	Critical size
$Cu_{51}Zr_{14}$	_	760	1388	0.55	<15 µm
$Cu_{10}Zr_7$	711	761	1183	0.60	520 μm
CuZr	674	720	1220	0.55	2 mm
CuZr ₂	615	662	1294	0.48	470 μm

 Table 3.3 Gibbs free energies of liquid and intermetallic phases.

Phase	Temperature range	Function
Liquid	298.15 <t<1357.77< th=""><th>${}^{0}G_{Cu}^{Liquid} = +5194.277 + 120.973331T - 24.112392T \times \ln(T) - 0.00265684T^{2}$</th></t<1357.77<>	${}^{0}G_{Cu}^{Liquid} = +5194.277 + 120.973331T - 24.112392T \times \ln(T) - 0.00265684T^{2}$
		+1.29223E-7×T ³ +52478T ⁻¹ -5.8489E-21×T ⁷
	1357.77 <t<3200.00< th=""><th>${}^{0}G_{Cu}^{Liquid} = -46.545 + 173.881484 \text{T} - 31.38 \text{T} \times \ln(\text{T})$</th></t<3200.00<>	${}^{0}G_{Cu}^{Liquid} = -46.545 + 173.881484 \text{T} - 31.38 \text{T} \times \ln(\text{T})$
	298.15 <t<2128.00< th=""><th>${}^{0}G_{Zr}^{Liquid} = +10320.095 + 116.568238 \text{T} - 24.1618 \text{T} \times \ln(\text{T}) - 0.00437791 \text{T}^{2} + 34971 \text{T}^{-1}$</th></t<2128.00<>	${}^{0}G_{Zr}^{Liquid} = +10320.095 + 116.568238 \text{T} - 24.1618 \text{T} \times \ln(\text{T}) - 0.00437791 \text{T}^{2} + 34971 \text{T}^{-1}$
		+1.6275E-22×T ⁷
	2128.00 <t<6000.00< th=""><th>${}^{0}G_{Zr}^{Liquid}$ =-8281.26+253.812609T-42.144T×ln(T)</th></t<6000.00<>	${}^{0}G_{Zr}^{Liquid}$ =-8281.26+253.812609T-42.144T×ln(T)
	298.15 <t<3000.00< th=""><th>${}^{0}L^{Liquid}_{C_{U:Zr}} = -140638.632 + 444.1606 \text{T} - 51.3121 \text{T} \times \ln(\text{T})$</th></t<3000.00<>	${}^{0}L^{Liquid}_{C_{U:Zr}} = -140638.632 + 444.1606 \text{T} - 51.3121 \text{T} \times \ln(\text{T})$
	298.15 <t<3000.00< th=""><th>$^{1}L_{Cu:Zr}^{Liquid}$ =-22066.212+84.9923T-9.6125T×ln(T)</th></t<3000.00<>	$^{1}L_{Cu:Zr}^{Liquid}$ =-22066.212+84.9923T-9.6125T×ln(T)
	298.15 <t<3000.00< th=""><th>$^{2}L_{Cu:Zr}^{Liquid}$ =56633.154-307.3817T+36.8512T×ln(T)</th></t<3000.00<>	$^{2}L_{Cu:Zr}^{Liquid}$ =56633.154-307.3817T+36.8512T×ln(T)
	298.15 <t<3000.00< th=""><th>$^{3}L_{Cu:Zr}^{Liquid} = -22368.721 + 119.5438T - 13.6488T \times \ln(T)$</th></t<3000.00<>	$^{3}L_{Cu:Zr}^{Liquid} = -22368.721 + 119.5438T - 13.6488T \times \ln(T)$

FCC_A1	298.15 <t<1357.77< th=""><th>${}^{0}G_{Cu}^{FCC-A1}$=-7770.458+130.485235T-24.112392T×ln(T)-0.00265684T²</th></t<1357.77<>	${}^{0}G_{Cu}^{FCC-A1}$ =-7770.458+130.485235T-24.112392T×ln(T)-0.00265684T ²
		+1.29223E-7×T ³ +52478T ⁻¹
	1357.77 <t<3200.00< th=""><th>${}^{0}G_{Cu}^{FCC-A1}$=-13542.026+183.803828T-31.38T×ln(T)-0.00265684T²+3.64167E</th></t<3200.00<>	${}^{0}G_{Cu}^{FCC-A1}$ =-13542.026+183.803828T-31.38T×ln(T)-0.00265684T ² +3.64167E
		+29×T ⁹
HCP_A3	130.00 <t<2128.00< th=""><th>${}^{0}G_{Zr}^{HCP_{-}A3} = -7827.595 + 125.64905T - 24.1618T \times \ln(T) - 0.00437791T^{2} + 34971T^{-1}$</th></t<2128.00<>	${}^{0}G_{Zr}^{HCP_{-}A3} = -7827.595 + 125.64905T - 24.1618T \times \ln(T) - 0.00437791T^{2} + 34971T^{-1}$
	2128.00 <t<6000.00< th=""><th>${}^{0}G_{Zr}^{HCP_{-}A3} = -26085.921 + 262.724183T - 42.144T \times \ln(T) - 0.00265684T^{2} + 1.342896E$</th></t<6000.00<>	${}^{0}G_{Zr}^{HCP_{-}A3} = -26085.921 + 262.724183T - 42.144T \times \ln(T) - 0.00265684T^{2} + 1.342896E$
		+31×T ⁹
Cu51Zr14	298.15 <t<3000.00< th=""><th>${}^{0}G_{Cu_{51}Zr_{14}}^{Cu_{51}Zr_{14}} = -10184.262 - 1.0260T + 0.785GHSERCU + 0.215GHSERZR$</th></t<3000.00<>	${}^{0}G_{Cu_{51}Zr_{14}}^{Cu_{51}Zr_{14}} = -10184.262 - 1.0260T + 0.785GHSERCU + 0.215GHSERZR$
Cu ₁₀ Zr ₇	298.15 <t<3000.00< th=""><th>${}^{0}G_{Cu_{10}Zr_{7}}^{Cu_{10}Zr_{7}}$ =-20463.114+5.8825T+0.588GHSERCU+0.412GHSERZR</th></t<3000.00<>	${}^{0}G_{Cu_{10}Zr_{7}}^{Cu_{10}Zr_{7}}$ =-20463.114+5.8825T+0.588GHSERCU+0.412GHSERZR
CuZr	298.15 <t<3000.00< th=""><th>${}^{0}G_{Cu:Zr}^{CuZr} = -14836.032 + 0.8587T + 0.5GHSERCU + 0.5GHSERZR$</th></t<3000.00<>	${}^{0}G_{Cu:Zr}^{CuZr} = -14836.032 + 0.8587T + 0.5GHSERCU + 0.5GHSERZR$
CuZr ₂	298.15 <t<3000.00< th=""><th>${}^{0}G_{Cu:Zr_{2}}^{CuZr_{2}} = -17045.108 + 4.2935T + 0.333GHSERCU + 0.667GHSERZR$</th></t<3000.00<>	${}^{0}G_{Cu:Zr_{2}}^{CuZr_{2}} = -17045.108 + 4.2935T + 0.333GHSERCU + 0.667GHSERZR$



Figure 3.14 Gibbs free energy curves of liquid phase and (a)CuZr₂, (b) CuZr, (c) Cu₁₀Zr₇ and (d) Cu₅₁Zr₁₄ phases under their corresponding T_g or T_x temperatures.



Figure 3.15 The crystallization driving force of CuZr₂, CuZr, Cu₁₀Zr₇ and Cu₅₁Zr₁₄ intermetallics under their corresponding T_8 or T_x temperatures.



Figure 3.16 The crystallization driving forces of CuZr₂, CuZr, Cu₁₀Zr₇ and Cu₅₁Zr₁₄ intermetallics, which are normalized to the corresponding melting temperature.

3.3.2 The thermodynamic explanation for the formation of intermetallic glasses

3.3.2.1 The relationship between the localize minimum crystallization driving force and the optimum glass formers

Generally, the compositions with local minimum crystallization driving forces in the whole composition range should be the optimum glass formers [87, 96, 126-129]. To locate the optimum glass formers, the crystallization driving force of each intermetallic as a function of composition needs to be obtained, by the method illustrated in **Figure 3.17** [91]. As shown in **Figure 3.17(a)**, the two solid curves represent the Gibbs free energy of liquid phase and α phase, respectively. The two paralleled dash lines are the tangent lines of the Gibbs free energy of these two phases. At a certain temperature, the crystallization driving force of α phase at composition X₀ is expressed by the arrow, or line Aa. **Figure 3.17(b)** shows the schematic diagram of the resulting crystallization driving force of α phase in the whole composition range.



Figure 3.17 (a) sketch diagram of the method to calculate the crystallization driving force of intermetallic from the liquid with composition X_0 ; (b) sketch diagram of the crystallization driving force of intermetallic phase in the whole composition range.

Figure 3.18 shows the crystallization driving forces of Cu₅₁Zr₁₄, Cu₁₀Zr₇, CuZr and CuZr₂ intermetallics as a function of the mole fraction of Zr. The local minimum crystallization driving forces located at around 0.321 and 0.536 mole fraction of Zr suggest that there are optimum glass formers, which match two eutectic glass formers as shown in **Figure 3.13**. Obviously, there is no local minimum crystallization driving forces near each intermetallic compound, where a pair of intermetallic glass formers is experimentally located. Thus, the method using local minimum in crystallization driving force to predict optimum glass formers failed to predict the intermetallic glass formers.



Figure 3.18 The crystallization driving force of Cu₅₁Zr₁₄, Cu₁₀Zr₇, CuZr and CuZr₂ intermetallic compounds in the whole composition range.

3.3.2.2 A new method to predict the formation of intermetallic glass

Due to the failure of the method mentioned in Figure 3.17 on the glass formation of intermetallic glass, a new method was proposed to predict intermetallic glass formers, as shown in Figure 3.19. Figure 3.19(a) shows a hypothetical binary system which has two intermetallic phases α and β . The solid curves were the free energy of liquid and intermetallic phases respectively. It is proposed that the Gibbs free energy curve of intermetallic phase rises sharply once composition shifts slightly away from the intermetallic compound. Moreover, this free energy curve covers a narrow composition range only as the intermetallic phase is treated as stoichiometric composition. It should be noticed that this sharp profile free energy curve is a hypothetical one and cannot be calculated by the CALPHAD method due to there is no solubility of the intermetallic phase. Therefore, the driving force of phase formation at any composition located between these two intermetallics should be the difference between the tangent line connecting α and β phases and the free energy curve of liquid phase. However, under quenching, it is suggested that the phase formation for compositions near α phase would not be influenced by β phase anymore, as shown in **Figure 3.19(b)**. Thus the dominant factor of the phase formation would be which phase has a lower Gibbs free energy. The new method to calculate the crystallization driving force of α phase as a function of composition under quenching was illustrated as Figure 3.19(c): (1) at the intermetallic composition, the intermetallic phase has the lowest Gibbs free energy thus it is favored to be formed thermodynamically. (2) When the composition shifted slightly away from the intermetallic compound, glass is favored to be formed thermodynamically due to the liquid phase has a lower Gibbs free energy at this composition range. Thus the crystallization driving force should be considered as zero. (3) When the composition shifted further away from the intermetallic compound, it reaches the composition range beyond where the Gibbs free energy curve of α phase covered. The crystallization driving force was calculated by the Figure 3.17. It should be noticed that even the method shown in composition in (3) was still far away from the eutectic composition, and the phase formation still would not be influenced by β phase. Figure 3.19(d) shows the resulting crystallization driving force of α phase. The two compositions ranges, near the intermetallic compound, with local minima crystallization driving forces were the glass formation ranges for intermetallic glass. Our proposed thermodynamic principle successfully interprets the phenomenon of formation of intermetallic glass.



Figure 3.19 (a) a hypothetical free energy curves of liquid and intermetallic phases and the corresponding driving force of phase formation; (b) the free energy curves of liquid and intermetallic phases under liquid quenching; (c) the suggested method to calculate the crystallization driving force of intermetallic phase under liquid quenching crystallization driving force from (c).

3.3.3 Kinetic influence on the formation of intermetallic glasses

Even though thermodynamic consideration can predict the formation of intermetallic glass successfully, the kinetic consideration is still valuable to help to understand the underlying mechanism of this phenomenon. The kinetic consideration can be represented by the critical cooling rate (R_c) for glass formation, as a lower R_c is related to a better glass forming ability. The R_c can be estimated through construction of the time-temperature-transition (TTT) curves. In order to compare their R_c , two optimum glass formers near Cu₁₀Zr₇, CuZr and CuZr₂ intermetallics respectively (Cu_{59,32}Zr_{40.68} and Cu_{58,32}Zr_{41.68}, Cu_{51,5}Zr_{48,5} and Cu₄₉Zr₅₁, Cu_{34,33}Zr_{65,67} and Cu_{31,33}Zr_{68,67}) and the three corresponding intermetallic compounds were selected to construct their TTT curves. According to the kinetic treatment of Uhlmann and Davies [130-133], the time needed for crystallization of volume fraction x can be estimated from:

$$t = \frac{9.32\eta}{kT} \left\{ \frac{a_0^9 x exp(1.024/T_r^3 \Delta T_r^2)}{N_v f^3 [1 - exp(-\Delta H_m^f \Delta T_r/RT)]^3} \right\}^{1/4}$$
(3.8)

where a_0 is the average atomic diameter, which equals to 0.28nm; k is the Boltzmann's constant; R is the universal gas constant; f is a structural constant 74

and $f = 0.2(T_m-T)/T_m$, where T_m is the melting temperature; N_v is the number of atoms per unit volume, here $N_v = 5 \times 10^{28} \text{atoms/m}^3$; $T_r = T/T_m$ and $\Delta T_r = (T_m-T)/T_m$; ΔH_m is the molar heat of fusion and all the values of T_m and ΔH_m are listed in **Table 3.4**; *x* was taken as 10⁻⁶ here [91]. The only unknown parameter is the temperature dependent viscosity η , which can be expressed by Vogel-Fulcher equation:

$$\eta(T) = Aexp(\frac{B}{T - T_0})$$
(3.9)

where *A*, *B* and *T*⁰ are constants. To determine *A*, *B* and *T*⁰, knowledge of η or $(d\eta)/(dT)$ at three temperature points is required. According to Ref. [134-136], the following three temperature points are taken to obtain a realistic estimation for the temperature dependent viscosity (as listed in **Table 3.5**): (1) the viscosity (=10¹³ Poise) at *T*=*T*₈, *T*₈ was measured at a heating rate of 0.667 K/s; (2) the viscosity (=3.5×10⁻² Poise) at melting temperature of pure Zr (*T*_m=2125K); (3) *E*(*T*₈) at *T*=*T*₈, where *E*(*T*₈) is the activation energy of glass transition and can be expressed as [137-139]:

$$E(T_g) = \frac{RBT_g^2}{(T_g - T_0)^2}$$
(3.10)

The value of $E(T_g)$ can be determined by Kissinger plot [137-139]:

75

$$\frac{E}{RT} = ln\left(\frac{T^2}{r}\right) + constant$$
(3.11)

Table 3.4 List of the values of T_m and ΔH_m .

	Cu59.32Zr40.68	Cu ₁₀ Zr ₇	Cu58.32Zr41.68
$T_m(\mathbf{K})$	1182	1183	1180
ΔH_m^f (J/Mol)	6.3×10 ³	6.7×10^3 6.2×10^3	
	Cu51.5Zr48.5	Cu51Zr49	Cu49Zr51
$T_m(\mathbf{K})$	1210	1213	1218
ΔH_m^f (J/Mol)	4.1×10 ³	3.6×10 ³	3.2×10 ³
	Cu34.33Zr65.67	CuZr ₂	Cu31.33Zr68.67
$T_m(\mathbf{K})$	1291	1294	1292
ΔH_m^f (J/Mol)	1.4×10 ³	3.0×10 ³	3.6×10 ³

Table 3.6 lists the T_g and T_p values of selected compositions under different heating rates. Typical Kissinger plots at T_g are shown in **Figure 3.20** for the selected alloys. The values of the corresponding *A*, *B* and T_0 are calculated and they are listed in **Table 3.7**.

	Cu59.32Zr40.68	Cu10Zr7	Cu58.32Zr41.68
Point 1	$\eta(T_g) = 10^{13}$ Poise	$\eta(T_g) = 10^{13}$ Poise	$\eta(T_g) = 10^{13}$ Poise
Point 2	E _g =681KJ/mol	E _g =772KJ/mol	E _g =672KJ/mol
	Where T _g =710.3K	Where T _g =711.6K	Where T _g =702.6K
Point 3	$\eta(T_{m} \text{ of } Zr=2125K)$	$\eta(T_{m} \text{ of } Zr=2125K)$	$\eta(T_{m} \text{ of } Zr=2125K)$
	=3.5x10 ⁻² Poise	=3.5x10 ⁻² Poise	=3.5x10 ⁻² Poise
	Cu51.5Zr48.5	Cu51Zr49	Cu49Zr51
Point 1	$\eta(T_g) = 10^{13}$ Poise	$\eta(T_g) = 10^{13}$ Poise	$\eta(T_g) = 10^{13}$ Poise
Point 2	E _g =681KJ/mol	E _g =805KJ/mol	E _g =649KJ/mol
	Where T _g =682.5K	Where T _g =681.5K	Where T _g =670.7K
Point 3	$\eta(T_{m} \text{ of } Zr=2125K)$	$\eta(T_{m} \text{ of } Zr=2125K)$	$\eta(T_{m} \text{ of } Zr=2125K)$
	=3.5x10 ⁻² Poise	=3.5x10 ⁻² Poise	=3.5x10 ⁻² Poise
	Cu34.33Zr65.67	CuZr ₂	Cu31.33Zr68.67
Point 1	$\eta(T_g) = 10^{13}$ Poise	$\eta(T_g) = 10^{13}$ Poise	$\eta(T_g) = 10^{13}$ Poise
Point 2	E _g =628KJ/mol	E _g =717KJ/mol	E _g =584KJ/mol
	Where T =621.0K	Where T =615.1.0K	Where T =606.5K
Point 3	$\eta(T_{m} \text{ of } Zr=2125K)$	$\eta(T_{m} \text{ of } Zr=2125K)$	$\eta(T_{m} \text{ of } Zr=2125K)$
	=3.5x10 ⁻² Poise	=3.5x10 ⁻² Poise	=3.5x10 ⁻² Poise

Table 3.5 List of points were taken to calculate the values of *A*, *B* and *T*₀.

Heating rate		0.083K/s	0.167K/s	0.333K/s	0.667K/s	1.333K/s
Cu59.32Zr40.68	T _g (K)	704.2	707.7	710.3	715.8	720.9
	$T_p(K)$	743.9	752.7	765.0	776.1	786.2
Cu10Zr7	$T_g(K)$	707.3	709.5	711.6	716.3	721.8
	$T_p(K)$	744.4	757.9	769.5	781.3	791.9
Cu58.32Zr41.68	$T_g(K)$	700.6	701.1	702.6	710.1	714.7
	$T_{p}(K)$	735.6	745.3	755.4	766.1	775.7
Cu51.5Zr48.5	T _g (K)	675.7	677.5	682.5	686.4	690.4
	$T_{p}(K)$	714.0	723.4	733.8	742.1	752.8
Cu51Zr49	$T_g(K)$	675.0	678.5	681.5	686.4	686.8
	$T_{P}(K)$	714.4	724.3	732.0	742.5	751.6
Cu49Zr51	$T_g(K)$	664.7	668.7	670.7	676.7	680.1
	$T_p(K)$	705.5	713.9	723.0	734.0	743.4
Cu34.33Zr65.67	T _g (K)	614.1	616.5	621.0	622.9	628.0
	$T_p(K)$	657.0	668.5	678.6	689.8	699.3
CuZr ₂	$T_g(K)$	610.5	612.2	615.1	618.4	622.2
	$T_p(K)$	652.4	664.8	675.4	691.7	696.0
Cu31.33Zr68.67	$T_g(K)$	599.3	604.0	606.5	609.1	614.3
	T _p (K)	640.5	650.1	663.2	675.1	691.8

Table 3.6 T_g and T_p of selected compositions at different heating rates.



Figure 3.20 $\ln(T^2/r)$ versus 1000/T for T_g and T_p of (a) compositions near Cu₁₀Zr₇ intermetallic compound; (b) compositions near CuZr intermetallic compound; (c) compositions near CuZr₂ intermetallic compound; the lines are the best fit lines.

The resulting viscosities as a function of temperature of the selected alloys are shown in **Figure 3.21**. It clearly shows that the viscosity curves of the two intermetallic glass formers (e.g. Cu_{59,32}Zr_{40.68} and Cu_{58,32}Zr_{41.68}) near each intermetallic (e.g. Cu₁₀Zr₇ intermetallic) have a similar trend. However, the viscosity curve of the corresponding interemetallic composition (e.g. Cu₁₀Zr₇ (Cu_{58,82}Zr_{41.18})) has a lower viscosity at high temperature but rises more quickly than that of the nearby intermetallic glass formers when temperature decreases.

Table 3.7 List of the values of *A*, *B* and *T*₀.

	Α	В	T ₀
Cu59.32Zr40.68	5.118x10 ⁻⁵	10928.762	450.810
Cu ₁₀ Zr ₇	1.218x10 ⁻⁴	9273.487	486.785
Cu58.32Zr41.68	5.709x10 ⁻⁵	10776.071	446.070
Cu51.5Zr48.5	1.047x10 ⁻⁴	9752.947	446.925
Cu51Zr49	2.965x10 ⁻⁴	7810.424	487.980
Cu49Zr51	1.015x10 ⁻⁴	9893.202	431.918
Cu34.33Zr65.67	2.631x10 ⁻⁴	8368.582	414.262
CuZr ₂	5.791x10 ⁻⁴	6907.203	440.972
Cu31.33Zr68.67	2.373x10 ⁻⁴	8644.413	393.991



Figure 3.21 The viscosity curves of (a) compositions near Cu₁₀Zr⁷ interemtallic compound; (b) compositions near CuZr interemtallic compound; (c) compositions near CuZr² interemtallic compound.

Based on equation (3.8), the TTT curves of the selected alloys were calculated, and **Figure 3.22** shows the results. Based on these TTT curves, the critical cooling rates are approximated by:

$$R_c = \frac{T_m - T_n}{t_n} \tag{3.12}$$

where T_n and t_n are the temperature and time of the nose of the corresponding TTT curves, respectively. **Table 3.8** lists the values of *R*^c for the selected alloys. Some of them are unrealistically low down to ~10⁻⁶K/s, this may be caused by the fact that some values of the parameters are estimated during the construction of TTT curves. However, qualitatively, it still surprisingly clearly shows that the trend of values of R_c matches that of critical thicknesses. Among the selected alloys near Cu10Zr7, CuZr and CuZr2 intermetallics respectively, the intermetallic compound, which has the smallest experimental critical thickness, always has a higher critical cooling rate than the two optimum glass formers near it. For instance, CuZr₂ (Cu_{33,33}Zr_{66,67}) has the highest critical cooling rate at 1.4 K/s, and then followed by Cu_{31,33}Zr_{68.67} at 0.4 K/s and Cu_{34,33}Zr_{65,67} at 0.1 K/s. This matches with the experimental critical thicknesses as 180 µm, 400 µm and 470 µm, respectively. This match provides a direct confirmation that kinetic consideration plays an important role in the determination of the glass forming ability of intermetallic glass.



Figure 3.22 Calculated TTT curves of selected composition.

Composition	Critical cool rate(K/s)
Cu59.32Zr40.68	1.0E-6
Cu10Zr7	2.5E-6
Cu58.32Zr41.68	1.9E-6
Cu51.5Zr48.5	7.5E-5
Cu51Zr49	3.6E-4
Cu49Zr51	2.0E-4
Cu34.33Zr65.67	0.1
CuZr ₂	1.4
Cu31.33Zr68.67	0.4

Table 3.8 the critical cooling rate, *R*_c, for the selected alloys.

The glass formation near Cu₅₁Zr₁₄, Cu₈Zr₃, Cu₁₀Zr₇ and CuZr₂ intermetallics is systematically studied. The so called intermetallic glass phenomenon of two optimum glass formers formed near but separated by the intermetallic phase was confirmed, as similar to the previous results of the formation of intermetallic glass near CuZr intermetallic. Furthermore, a new method was proposed to predict the glass formation ranges of intermetallic glasses. A pair of intermetallic glass formation ranges with local minimum crystallization driving force was located. Kinetically, through construction of the TTT curves, it reveals that the intermetallic glass formers always have lower critical cooling rate than the corresponding intermetallic compound. Based on both thermodynamic and kinetic consideration, some unique characters of intermetallic glasses were summarized as following:

- (1) The intermetallic glasses present in pair but separated by intermetallic compounds. This was explained by our hypothetical Gibbs free energy curves: due to the different rising rates of the Gibbs free energy of liquid and intermetallic phases at compositions near intermetallic compound, the liquid phase has a lower Gibbs free energy. Thus two separated thermodynamically favored glass formation ranges can be located when the formation of primary phases next to the corresponding intermetallic would be kinetic suppressed under quenching.
- (2) Furthermore, the intermetallic glasses are sharply composition dependent, which are close to the intermetallic compounds. Thermodynamically, this is consistent with the narrow composition ranges covered by the Gibbs free energy curve of intermetallic phase. Moreover, if the compositions are too far away from the intermetallic compound, the formation of the neighbor primary phases become

85

kinetically feasible thus the two thermodynamically favored composition ranges would not exist.

- (3) Due to the kinetic constraint, the only crystalline phase competing with the amorphous phase during the precipitation is the corresponding intermetallic phase. For example, the glass formation of compositions close enough to CuZr² interemtallic would not be influenced by the nearby phases CuZr interemetallic and pure Zr under quenching. Thus no other primary phase would be precipitation during the cooling. This has been proved by the results of XRD and the observation optical microscope.
- (4) Surprisingly, the phenomenon that the critical cooling rates were also sharply composition dependant near intermetallic compound is discovered. The optimum intermetallic glass formers show different temperature dependent viscosity and R_c from those of the corresponding intermetallic compound. This may provide a kinetic evidence of formation of intermetallic glass.

There is no question that the intermetallic glass is a new family of glass and it provides a new perspective for the future research. There are still some questions needed to be investigated. Firstly, the structure of intermetallic glass is still a mystery. There are several atomic model had been proposed about the structure of metallic glass, however, none of these models can explain the phenomenon of intermetallic glass [140-144]. The challenge is a pair of optimum glass formers located near but separated by the intermetallic compound, the glass forming ability changes a lot in such narrow composition range. Secondly, it is proved that the intermetallic glass can be located not only near the equiatomic intermtallic like CuZr intermetallic but also near non-equiatomic intermtallics, which indicates that intermetallic glass can be located in a wide composition range in the phase diagram. However, all the intermetallics studied so far are so called line compounds, which have no solubility at all. It is open to question that whether the phenomenon of interemtallic glass exists in the intermetallic with solubility or not. Thirdly, as demonstrated above, the temperature dependent viscosities of the intermetallic glass formers and the intermetallic compounds show different trends, and it causes that the critical cooling rate changes quickly in a narrow composition range near interemtallic compound. The underlying mechanism of the sharply changing critical cooling rate needs further investigation.

3.4 Conclusion

Glass formation around the Cu₅₁Zr₁₄, Cu₈Zr₃, Cu₁₀Zr₇ and CuZr₂ intermetallic compounds has been carefully studied. The formation of interemetallic glass has been explained from both thermodynamic and kinetic perspectives. Here are the conclusions:

(1) Two optimum intermetallic glass formers can be easily located near but separated by almost every intermetallic compound in the Cu-Zr binary system. The result shows that maximum critical thickness of intermetallic glass formed near Cu₁₀Zr₇ intermetallic is 520 μm, followed by 470 μm near CuZr₂ intermetallic and less than 15 μm near Cu₅₁Zr₁₄ intermetallic. However, due to Cu₈Zr₃ intermetallic is a peritectic phase, there is only one optimum glass forming range near Cu₈Zr₃ intermetallic.

(2) The Gibbs free energy as a function of composition of liquid and intermetallic phases is calculated by CALPHAD method at different temperatures. An explanation has been provided that two thermodynamically favored glass forming ranges are present due to the liquid phase has a lower Gibbs free energy under quenching. (3) The temperature dependent viscosities of the selected compositions are studied. Furthermore, the TTT curves and the critical cooling rates of these selected compositions are calculated, and they are related to the experimental determined critical sizes: two optimum glass formers show lower critical cooling rates or larger critical thickness than those of the corresponding intermetallic compound.

Chapter 4

The formation of intermetallic glasses in Zr–Cu-Ti system

4.1 Introduction

The Zr-Cu-Ti ternary alloy system has attracted increasing interest due to the good glass forming ability and the superior mechanical property [99, 145-151]. Lin et al. indicated that Ti₃₅Zr₁₀Cu₅₅ can form metallic glass with critical thickness of 500 μ m; and the critical cooling rate was calculated as 2×10⁴ K/s [97]. Inoue et al. studied the glass formation of Cu₆₀Zr_{40-x}Ti_x, where x= 0-40 at% [101]. Cu₆₀Zr₃₀Ti₁₀ was the best glass former with 4 mm glass forming ability. More recently, a new glass forming range was reported

around composition $Cu_{52}Zr_{40}Ti_8$, the critical size was determined as 4 mm [103]. In this chapter, two new composition ranges ((1) $Cu_{100-x}(ZrTi)_x$, where Ti=5% and x=47.5-53; (2) compositions around Cu_2ZrTi intermetellic) are selected to study the phenomenon of formation of intermetallic glass and the glass forming ability.

It is commonly believed that when more elements are involved in the alloy system, the alloy should become too confused to have chance of crystallization under quenching [41]: elements with different radiuses can lead to dense packing structure in the liquid state, therefore glass formation should be favored than crystallization kinetically. Therefore, element addition is a very effective way to improve the glass forming ability or to develop new BMGs systems [66, 152-158]. In the first composition range studied in this chapter (Cu_{100-x}(ZrTi)_x, where Ti=5% and x=47.5-53), titanium can be considered as a third additional element. Although Zr-Cu binary system is the one of best glass formation binary systems, 2 mm critical size is still too small for the engineering application. Ti has an atomic radius between Zr and Cu, which may increase the dense packing in the liquid state. Also, the heat of mixing between Ti and Cu is negative as -9 kJ/mol, which may help to the glass formation [9, 64, 159]. Furthermore, from the Cu-Ti binary phase diagram, it shows TiCu phase is also an intermetallic phase (as shown in Figure 4.1). Therefore, the Zr-Ti-Cu system would be a good choice to obtain a
good glass forming ability and also to further study the formation of intermetallic glass in ternary system.



Figure 4.1 Part of Ti-Cu binary phase diagram.

The second composition range to be studied is around the Cu₂ZrTi intermetallic, which is a Laves phase. It has been reported that this Cu₂ZrTi phase covered a wide composition range at high temperature (more than 10 at%) [119, 160, 161]. The wide Laves phase homogeneity range suggests that the Gibbs free energy varies slowly with the changing of composition and the liquidus lines are relatively flat with respect to compositions. In this sense, the Laves phase is "forgiving" of composition variation. Moreover, it is believed

that when the composition of the liquid phase is very different from that of the competing crystalline phase, the nucleation would be difficult for the crystalline phase due to the fact that composition required may not be satisfied through diffusion in the undercooling liquid. All of these suggest that crystallization of the Laves phase may occur more easily than the formation of amorphous phase in this Laves phase composition range [97]. Therefore, all the reported investigations about glass forming ability in this Zr-Ti-Cu ternary system focus on the compositions away from Laves phase, and there is no report about the glass forming ability in the Laves phase composition range before. At the meantime, there was also some work treated Cu₂ZrTi phase as a stoichiometric compound, because there was no solubility of the Cu₂ZrTi phase at low temperature reported [100]. In this chapter, the glass forming ability around the Cu2ZrTi ternary intermetallic phase would be studied.

Figure 4.2 shows the composition ranges studied in this chapter. For the first composition range, 5 at% Ti would be added into Zr-Cu system. Ti was demonstrated to stabilize the Cu₁₀Zr₇ phase but there are still two optimum glass formers separated by the center composition. Cu₂ZrTi phase was found cover a wide composition range, and the phenomenon of formation of intermetallic glass was not clear in this area.



Figure 4.2 The composition ranges studied in this chapter (marked by the red line and the red circle) and the composition ranges studied before (marked by the purple line and the pruple circle) [97, 101-103].

4.2 Glass formation of compositions Cu_{100-x}(ZrTi)_x (Ti=5 at% and x=47.5-53)

CuZr intermetallic was selected to investigate the influence of Ti addition on the formation of intermetallic glass. Based on the fact that a pair of optimum glass formers (Cu_{51.5}Zr_{48.5} and Cu₄₉Zr₅₁) are located near but separated by CuZr intermetallic [81], 5 at% Ti was added to replace Zr from composition 94 Cu_{52.5}Zr_{47.5} to Cu₄₇Zr₅₃. Two kinds of rods were cast with diameter in 3 mm and 5 mm, respectively.

4.2.1 Glass formation of 3 mm rods of alloy Cu_{100-x}(ZrTi)_x (Ti=5 at% and x=47.5-53)

Figure 4.3 shows the SEM photos of the longitudinal view of 3 mm rods with compositions from Cu_{52.5}(ZrTi)_{47.5} to Cu₄₇(ZrTi)₅₃. The dark contras parts are amorphous phase and the light contrast parts are the crystalline phase. Two crystalline phases can be observed in these 3 mm rods: CuZr phase and Cu₁₀Zr₇ phase, whose morphologies are shown in Figure 4.4, respectively. The CuZr phase can be easily observed even under low magnification, while the Cu10Zr7 phase is much "smaller" in the size and only can be observed under high magnification. According to the (ZrTi) content, the whole composition range can be divided into five regions with different amount of crystalline phase: (1) For the starting composition Cu_{52.5}(ZrTi)_{47.5}, there is clearly large amount of crystalline phase scattered in the amorphous matrix. Although the light contrast parts are not obvious in the SEM photos of Cu₅₂(ZrTi)₄₈, large amount of Cu₁₀Zr₇ phase (as shown in Figure 4.4(b)) can be observed under high magnification. (2) When the composition reaches Cu_{51.5}(ZrTi)_{48.5}, the 3 mm rod shows as-cast structure with > 90% amount of amorphous phase.





Figure 4.3 SEM photos of the longitudinal view of 3 mm rods with composition from $Cu_{52.5}(ZrTi)_{47.5}$ to $Cu_{47}(ZrTi)_{53}$.

(3) The amount of amorphous phase decreases with the further increase (ZrTi) content to Cu_{51,25}(ZrTi)_{48,75} and Cu₅₁(ZrTi)₄₉. (4) Within the composition range from Cu₄₉(ZrTi)₅₁ to Cu_{47,75}(ZrTi)_{52,25}, all the 3 mm rods contain large amount of amorphous phase, while Cu₄₈(ZrTi)₅₂ show fully amorphous structure. (5) The amount of crystalline phase becomes more (than the previous region) when the composition reaches Cu_{47,5}(ZrTi)_{52,5} and Cu₄₇(ZrTi)₅₃. It shows that two optimum glass forming ranges (regions (2) and (4)) are located near but separated by region (3). This result is in good agreement with the glass forming ranges near CuZr intermetallic: two optimum glass formers Cu_{51,5}Zr_{48,5} and Cu₄₉Zr₅₁ were separated by CuZr intermetallic.



Figure 4.4 SEM photos of two kinds of crystalline phases detected in the 3 mm rods with composition from Cu_{52.5}(ZrTi)_{47.5} to Cu₄₇(ZrTi)₅₃: (a) CuZr phase and (b) Cu₁₀Zr7 phase.



Figure 4.5 XRD patterns of 3 mm rods with composition from Cu_{52.5}(ZrTi)_{47.5} to Cu₄₇(ZrTi)₅₃.

The XRD patterns of the cross-section of all the 3 mm rods are shown in **Figure 4.5**. Only Cu_{52.5}(ZrTi)_{47.5} shows clearly diffraction peaks of crystalline

phases. All the others show either a board amorphous hump or some tiny peaks of crystalline phase on it. This may be caused by that the amount of crystalline phases in these 3 mm rods is small (the morphology of Cu₁₀Zr⁷ phase is "small"). Therefore, the area covered by the crystalline phases is not big enough to be detected as only Cu_{52.5}(ZrTi)_{47.5} contains large amount of crystalline phase among all these compositions.

The corresponding DSC curves of these 3 mm rods are shown in Figure 4.6 to further confirm the observation of the SEM photos and the XRD results. The enthalpies of crystallization were used to estimate the amount of the amorphous phase, as plotted in Figure 4.7. Cu51.5(ZrTi)48.5 and Cu48(ZrTi)52 have 71.8 J/g and 79.3 J/g of enthalpies of crystallization respectively, which are the highest two values among their neighbor compositions. Composition Cu₄₈(ZrTi)₅₂ has the highest enthalpy of crystallization among all the composition, and moreover, there is no crystalline phase observed from both XRD and SEM results. Thus Cu₄₈(ZrTi)₅₂ is believed as a fully amorphous structure. According to the resulting enthalpies of crystallization, the percentage of the amorphous phase in each rod can be easily calculated and plotted in Figure 4.7. The DSC results confirm that there are two optimum glass formers separated by the composition of Cu51.25(ZrTi)48.75, which is consistent with the character of intermetallic glass. It is also noticed that the glass transition temperature T_g and the onset crystallization temperature T_x shift to lower temperature with the increasing (ZrTi) content. The crystallization peaks split from on peak into two peaks at high (ZrTi) composition side, which suggests that new crystalline phase precipitates. This indicates the end of the intermetallic glass formation zone, as it is proposed that the crystalline phases (competing with the amorphous) during cooling would not change in the intermetallic glass formation range.

Therefore, the SEM and DSC results show the phenomenon of formation of intermetallic glass in the studied composition range $(Cu_{100-x}(ZrTi)_x (x=47.5-53))$. However, the XRD results are not convincing enough as almost all compositions seem like "fully" amorphous.



Figure 4.6 DSC curves of 3 mm rods with composition from Cu52.5(ZrTi)47.5 to Cu47(ZrTi)53.



Figure 4.7 Calculated enthalpies of crystallization and percentage of amorphous phase of all 3 mm rods.

4.2.2 Glass formation of 5 mm rods of alloy Cu_{100-x}(ZrTi)_x (x=47.5-53)

In the same composition range as Cu_{100-x}(ZrTi)_x (x=47.5-53), 5 mm rods were cast to further investigate the glass forming ability and to confirm the phenomenon of formation of intermetallic glass obtained through 3 mm rods. **Figure 4.8** shows the SEM photos of the longitudinal view of the 5 mm rods. Unfortunately, there is no fully amorphous structure observed. Therefore, the optimum glass former is defined as the composition containing the largest amount of amorphous phase among the compositions around it. The studied composition range also can be divided into five regions: (1) Compositions Cu_{52.5}(ZrTi)_{47.5} and Cu₅₂(ZrTi)₄₈ show almost fully crystalline structure. (2) Cu_{51.5}(ZrTi)_{48.5} shows the largest area covered by amorphous phase among its neighbor composition, which suggests that it is an optimum glass former. (3) Composition Cu₅₁(ZrTi)₄₉ has structure of almost fully crystalline phase. (4) With the further increase (ZrTi) content, all compositions from Cu₄₉(ZrTi)₅₁ to Cu₄₈(ZrTi)₅₂ show structure of crystalline phases embedded in the amorphous matrix. Cu₄₈(ZrTi)₅₂ is considered as the optimum glass former among them as it has the largest amount of amorphous phase. (5) The amount of crystalline phase keeps increasing from Cu47.75(ZrTi)52.25 to Cu47(ZrTi)53 and finally ends with structure of fully crystalline phase. These five composition ranges are consistent with those obtained through 3 mm rods, and two optimum glass formers (Cu51.5(ZrTi)48.5 and Cu48(ZrTi)52) are located near but separated by the composition of Cu₅₁(ZrTi)49. There are also two kinds of phases can be observed in all the rods: CuZr phase and Cu10Zr7 phase.





Figure 4.8 SEM photos of longitudinal view of 5 mm rods with composition from Cu_{52.5}(ZrTi)_{47.5} to Cu₄₇(ZrTi)₅₃.

DSC studied is also carried out to confirm the observation obtained from the SEM photos and the results are shown in **Figure 4.9** along with the calculated enthalpies of crystallization. The enthalpies of crystallization of Cu_{51.5}(ZrTi)_{48.5} and Cu₄₈(ZrTi)₅₂ are 52.7 J/g and 69.1 J/g respectively, which are highest value among their neighbor compositions. Compositions from Cu₄₉(ZrTi)₅₁ to Cu_{48.25}(ZrTi)_{51.75} also have relatively high values of enthalpies of crystallization, which suggest the presence of quite amount of amorphous phase. The DSC results are almost consistent with the observation obtained from SEM photos and confirm the phenomenon of formation of intermetallic glass. The only exception is Cu_{48.25}(ZrTi)_{51.75}; its enthalpy of crystallization is much lower than those of compositions around it. However, it should be noticed that the value of enthalpy of crystallization would be highly dependent on the selected position (on the 5 mm rods) measured by DSC. Therefore, the DSC results can



only imply the amount of amorphous phase in this 5 mm case.

Figure 4.9 DSC curves of 3 mm rods with composition from Cu_{52.5}(ZrTi)_{47.5} to Cu₄₇(ZrTi)₅₃.

Based on the experimental results of both 3 mm and 5 mm rods with compositions from Cu_{52.5}(ZrTi)_{47.5} to Cu₄₇(ZrTi)₅₃, the glass formation of this composition range can be summarized as following:

- (1) The phenomenon of intermetallic glass, two optimum glass formers located near but separated by the intermetallic phase, can be confirmed. However, with the addition of 5 at% Ti, two kinds of intermetallic phases precipitated in both 3 mm and 5 mm rods instead of only one corresponding intermetallic phase can be detected in all the samples in binary system. It should be noticed that there is no crystalline phase containing Ti detected. The precipitated of Cu₁₀Zr₇ phase was unexpected due to the composition range was based on the compositions near CuZr intermetallic. More importantly, the Cu₁₀Zr₇ phase can still be detected when the composition reaches high (ZrTi) content ((ZrTi) > 50 at%), where should correspond to composition region between CuZr and CuZr₂ phases in binary system. Thus the role of Ti addition may not be simply replace Zr but also stabilize the Cu₁₀Zr₇ phase.
- (2) As mentioned before, two optimum glass formers were located at Cu_{51.5}Zr_{48.5} and Cu₄₉Zr₅₁, which are separated by Cu₅₁Zr₄₉ with fully crystalline structure in Zr-Cu binary system [81]. With the addition of Ti, the two optimum glass formers in the ternary system, separated by

Cu₅₁(ZrTi)₄₉, are located at Cu_{51.5}(ZrTi)_{48.5} and Cu₄₈(ZrTi)₅₂. Although composition Cu₄₈(ZrTi)₅₂ is slightly different from composition Cu₄₉Zr₅₁, the compositions of the two optimum glass formers in ternary system still can be considered as same as those in binary system.

4.3 Glass formation of compositions near Cu₂ZrTi intermetallic phase

Generally, it is believed that the glass formation range should be (1) close to eutectic points, where the value of T_{rg} should be high; (2) away from Laves phase, where the nucleation would occur easily [97]. Previously, the formation of glasses near intermetallic phases has been demonstrated. In this section, the glass formation near Laves phase would be studied.

4.3.1 Glass formation of compositions Cu₅₀Zr_xTi_{50-x}, Cu_yZr_{77-y}Ti₂₃ and Cu_yZr₂₇Ti_{73-y}

Starting with the composition of Cu₂ZrTi (Cu₅₀Zr₂₅Ti₂₅), the glass forming ability near it was investigated by studying the critical thickness of the wedge cast samples, and **Figure 4.10** shows the compositions studied.



Figure 4.10 The studied compositions near Cu2ZrTi (Cu50Zr25Ti25), marked by the red dot.

The OM photos of the longitudinal view of the wedge samples with the compositions $Cu_{50}Zr_xTi_{50-x}$ (x=22-30) are shown in **Figure 4.11**. The arrows are pointing to the boundaries between the crystalline phase and the amorphous phase, where the critical thicknesses are measured. The critical thicknesses of the wedge samples are plotted in **Figure 4.12**. The results show that the Cu_2ZrTi ($Cu_{50}Zr_{25}Ti_{25}$) has the maxmium critical thickness of 600 µm among these compositions. With the decreasing Zr content, the critical thickness decreases from 600 µm to 400 µm first and then rises to 480 µm, after that the critical thickness keeps decreasing to 300 µm. With the increasing Zr content, the critical thickness changes with no clear trend; the smallest critical

thickness presents at Cu₅₀Zr₂₇Ti₂₃ of 320 μ m, as pointed by the arrow in **Figure 4.12**. If Cu₅₀Zr₂₇Ti₂₃ is considered as the center composition, there are two peaks in critical thickness located at both sides of it although the critical thickness keeps fluctuating. Furthermore, Line 2 (Cu_yZr_{77-y}Ti₂₃) and line 3 (Cu_yZr₂₇Ti_{73-y}) are extended from Cu₅₀Zr₂₇Ti₂₃ since it has the smallest critical thickness.



Figure 4.11 OM photos of the longitudinal view of the wedge cast samples of Cu₅₀Zr_xTi_{50-x} (x=22-30).



Figure 4.12 The critical sizes of the wedge cast samples of Cu₅₀Zr_xTi_{50-x} (x=22-30).

Figure 4.13 shows the OM photos of the cross-section view of the wedge cast samples with compositions along line 2 (Cu_yZr_{77-y}Ti₂₃, y=48-52). The horizontal arrows are pointing to the critical thickness and the vertical arrow indicates the composition of Cu₅₀Zr₂₇Ti₂₃, which is the starting composition of line 2. **Figure 4.14** summarizes the critical thicknesses of compositions along line 2. Unlike the fluctuating of the critical thicknesses observed in line 1, it shows that two peaks in the critical thickness (480 μm at Cu_{51.5}Zr_{25.5}Ti₂₃ and 400 μm at Cu_{49.5}Zr_{27.5}Ti₂₃) are separated by the compositions of Cu_{50.5}Zr_{26.5}Ti₂₃ and Cu_{50.5}Zr_{27.7}Ti₂₃.

Chapter 4 The formation of intermetallic glasses in Zr-Cu-Ti system



Figure 4.13 OM photos of the longitudinal view of the wedge cast samples of $Cu_yZr_{77-y}Ti_{23}$ (y=48-52).



Figure 4.14 The critical sizes of the wedge cast samples of Cu_yZr_{77-y}Ti₂₃ (y=48-52).

Figure 4.15 shows the OM photos of the wedge samples with the compositions along line 3 and their critical thicknesses are summarized in **Figure 4.16**. The vertical arrows in both **Figure 4.15** and **Figure 4.16** indicate the composition of Cu₅₀Zr₂₇Ti₂₃. The changing of critical thickness has similar trend as that of line 2. Two peaks in critical thickness (480 μm at Cu_{51.5}Zr₂₇Ti_{21.5} and 440μm at Cu_{49.5}Zr₂₇Ti_{23.5}) are located at both sides of composition Cu₅₀Zr₂₇Ti₂₃.



Figure 4.15 OM photos of the longitudinal view of the wedge cast samples of $Cu_yZr_{27}Ti_{73-y}$ (y=48-52).



Figure 4.16 The critical sizes of the wedge cast samples of Cu_yZr₂₇Ti_{73-y} (y=48-52).

Figure 4.17 summaries the critical thicknesses of compositions along line 1, 2 and 3. It is assumed that Cu₅₀Zr₂₇Ti₂₃ is the composition with minimum critical thickness, just like the intermetallic compound has the smallest critical thickness among the compositions near it in binary system. **Figure 4.17** suggest that there is a "ring" of peaks in critical thickness around Cu₅₀Zr₂₇Ti₂₃, although line 1 shows weakly fluctuation in critical thickness. It is noticed that the difference between the maximum and minimum values of the critical thickness is small: for line 2, one of the maximum values is only 400 μm as only 80-100 μm difference to the minimum value. It may be caused by the wide homogeneity composition range covered by the Laves phase: the 115 insensitivity to the composition variation leads to slightly changing in critical thickness. XRD and melting studies were carried out to confirm that the compositions studied are all located in the range of Cu₂ZrTi intermetallic phase.



Figure 4.17 Summary of the critical sizes of compositions along line 1, 2 and 3. A "ring" of the peaks in the critical thickness is marked by the red circle. The red values represent the "peak" values of critical size and the blue value represents the critical thickness of composition Cu₅₀Zr₂₇Ti₂₃.

4.3.2 XRD and melting studies of the composition in line 1, 2 and 3

To identify the crystalline phase precipitated during the casting, the crystallization parts of all the wedge cast samples were investigated by XRD. **Figure 4.18** shows the resulting XRD patterns. In all these samples, only one phase can be detected, which is believed as Cu₂ZrTi phase. There is no other crystalline phase precipitated. It can be interpreted by the liquid project of the ternary phase diagram shown in **Figure 1.12**. It shows that the compositions studied in this section are away from any eutectic point reported. Therefore, the precipitation of other crystalline phases is kinetically suppressed under quenching. These XRD results prove that all the compositions studied are in the Laves phase range.

The melting temperatures and the liquidus temperatures were also measured for all the studied compositions. **Figure 4.19** shows the melting curves of these compositions. The liquidus temperatures of the alloys with compositions along line 1 do not change too much from each other, they all fluctuates around 1145K. For line 2, the liquidus temperature increases from 1143K at Cu₅₂Zr₂₅Ti₂₃ to 1154K at Cu₄₈Zr₂₉Ti₂₃. For line 3, liquid temperature increases from 1143K at Cu₅₂Zr₂₇Ti₂₁ to 1152K at Cu₄₈Zr₂₇Ti₂₅.



Figure 4.18 XRD patterns of the crystallization part of wedge cast samples of line 1, 2 and 3.



Figure 4.19 Melting curves of compositions in line 1, 2 and 3. The dash dot lines indicate the liquid temperature.

It indicates that the liquidus temperature increases with the decreasing Cu content in this Laves phase range. Moreover, there are two melting peaks in these melting curves and the first peak becomes smaller when the liquidus temperature is higher. It is believed that there should be only one melting peak if no other phase involved. In the binary system, like Zr-Cu system, the liquidus temperature of the intermetallic compound is higher than those of the compositions near it. It is assumed that the intermetallic glass may locate near the composition with the highest melting temperature. Therefore, further investigation need to be done to locate the composition with both the highest melting temperature and one melting peak.

According to **Figure 4.19**, the melting of a new composition line (line 4 and the compositions change from high Cu content to low Cu content) was studied, as shown in **Figure 4.20**. It clearly shows that the composition Cu₄₄Zr₃₀Ti₂₆ has the highest liquidus temperature, however, two melting peaks. Cu₄₂Zr₃₁Ti₂₇ shows only one melting peak, which means the Cu₂ZrTi phase is the only phase formed. Thus, the critical thicknesses of compositions around Cu₄₂Zr₃₁Ti₂₇ were studied and they were plotted in **Figure 4.21**. The critical thickness decreases from 420 µm at Cu₄₄Zr₃₀Ti₂₆ to 280 µm at Cu₄₀Zr₃₂Ti₂₈ except Cu₄₁Zr_{31.5}Ti_{27.5}. But Cu₄₁Zr_{31.5}Ti_{27.5} should not be considered as a peak in critical thickness as its 360 µm critical thickness is only 20 µm higher than that of Cu₄₂Zr₃₁Ti₂₇. Therefore, there is no a pair of optimum glass formers near 120

 $Cu_{42}Zr_{31}Ti_{27}.$



Figure 4.20 Melting curves of composition line 4.



Figure 4.21 Critical sizes of compositions around Cu₄₂Zr₃₁Ti₂₇.

According to the experimental results mentioned above, the glass formation in the composition range of Cu₂ZrTi Laves phase can be summarized as following:

- (1) Cu₅₀Zr₂₇Ti₂₃ has a relatively minimum critical thickness as 320 μm among the compositions around it, and there is a "ring" of peaks in critical thicknesses around it. However, the difference in critical thickness among all the compositions along line 1, 2 and 3 is not significant enough and the fluctuating of critical thickness in line 1 should not be ignored. Thus, the phenomenon of formation of intermetallic glasses may not be present in this Laves phase composition range.
- (2) By the investigation of melting behavior, a new composition Cu₄₂Zr₃₁Ti₂₇ with relatively high liquidus temperature and one step of melting was located. But there is no a pair of optimum glass formers located near it, which is the character of intermetallic glass.
- (3) It is unexpected that among all the compositions studied in this section, the composition with the maximum critical thickness is composition Cu₂ZrTi (Cu₅₀Zr₂₅Ti₂₅). The critical thickness of it reaches 600 μm, which is higher than that of Ti₃₅Zr₁₀Cu₅₅: 500 μm [97]. More importantly, Ti₃₅Zr₁₀Cu₅₅ is believed to be located near eutectic point and to be considered as a

eutectic glass former. This discovery is significant: usually, compositions in or near Laves phase region were considered as poor glass former; however, the critical thickness in Laves phase region in this section is higher than that of eutectic glass former.

(4) This study proves that Cu₂ZrTi intermetallic phase has a wide composition range. It also proves the glass formation in this composition range is more complicated than that near intermetallics in binary system. Further work need to be done to investigate the underlying mechanism of the glass formation in Laves phase or intermetallic with solubility.

4.4 Calculation of the glass forming range in Zr-Cu-Ti ternary system

For Zr-Cu-Ti ternary system, unlike the binary system, the CALPHAD method is no longer appropriate due to the lack of thermodynamic information of the ternary intermetallic phase. Also, the wide composition range of the Laves phase makes it more complicated. Therefore, Miedema method is used to calculate the glass forming range [120]. This model is actually a semi-empirical model adopting a few parameters to predict the heat

of mixing (or the enthalpy of formation) two pure liquid metals, resulting a liquid solution, solid solution or intermetallic and it is applicable to a plenty of alloy systems. The amorphous phase can form if the enthalpy of formation of the amorphous is less than that of the solid solution phase.

The enthalpy of formation of a solid solution is comprised by three parts: interfacial (chemical) enthalpy, elastic enthalpy and structural enthalpy, and for a binary system it can be written as [162]:

$$\Delta H_{AB} = \Delta H_{AB}^c + \Delta H_{AB}^e + \Delta H_{AB}^s \tag{4.1}$$

The chemical enthalpy of enthalpy of mixing can be obtained from:

$$\Delta H^{c}_{AB} = X_{A} X_{B} (X_{A} \Delta H^{inter}_{B \ in \ A} + X_{B} \Delta H^{inter}_{A \ in \ B})$$

$$\tag{4.2}$$

where X_A and X_B are the mole fraction of element A and B, respectively; ΔH^{inter} is the interfacial enthalpy of solving one mole of element A in an excess of element B and have a expression as:

$$\Delta H_{A \text{ in } B}^{\text{inter}} = \frac{V_A^{2/3}}{\frac{1}{2} (\frac{1}{n_{ws A}^{1/3}} + \frac{1}{n_{ws B}^{1/3}})} \left\{ -P(\Delta \varphi)^2 + Q(\Delta n_{ws}^{1/3})^2 \right\}$$
(4.3)

where V_A is the mole volume of pure element A; n_{ws} is the electron density parameter; φ is the electronegativity or the work function of pure element; Pand Q are constants, and for a transition-transition binary metal alloys, P=14.1 and Q/P=9.4.

For the enthalpy of elastic part, which is caused by the mismatch during mixing, can be defined as:

$$\Delta H^{\boldsymbol{e}}_{AB} = X_A X_B (X_A \Delta H^{\boldsymbol{e}}_{B \ in \ A} + X_B \Delta H^{\boldsymbol{e}}_{A \ in \ B}) \tag{4.4}$$

where ΔH^e is the elastic enthalpy of per mole of element A in excess of element B and can be calculated based on the continuous elastic model (or the sphere and hole model) [163, 164]:

$$\Delta H_{A \text{ in } B}^{e} = \frac{2K_{A}G_{B}(W_{A} - W_{B})^{2}}{4G_{B}W_{A} + 3K_{A}W_{B}}$$
(4.5)

where *K* and *G* are the bulk modulus and shear modulus respectively; W_A and W_B are the modified volumes of sphere and hole as:

$$W_A = V_A + \alpha \frac{(\varphi_A - \varphi_B)}{n_{WS}^A} \tag{4.6}$$

$$W_B = V_B + \alpha \frac{(\varphi_A - \varphi_B)}{n_{WS}^B} \tag{4.7}$$

and

$$\alpha = 1.5 \frac{V_A^{2/3}}{n_{ws}^{A^{-1/3}} + n_{ws}^{B^{-1/3}}}$$
(4.8)

For the structural enthalpy, the contribution to the enthalpy of formation is so small that it is neglected in this section.

For the case of amorphous phase, the enthalpy of formation does not comprise the elastic and structural parts but a part of enthalpy difference between the amorphous and crystalline states of the pure element, and can be written as [165, 166]:

$$\Delta H^{am} = \Delta H^c + X_A H_A^{a-s} + X_B H_B^{a-s} \tag{4.9}$$

where ΔH^{a-s} is the enthalpy difference between the amorphous and crystalline states of the pure element or enthalpy of topological and the quantity is given by [167]:

$$\Delta H_i^{a-s} = \alpha T_{m,i} \tag{4.10}$$

126

where α = 3.5 Jmol⁻¹K⁻¹ and $T_{m,i}$ is the melting temperature of element *i*. Furthermore, due to the short-range order structure of amorphous phase, a factor *f* was multiplied to the right part of equation (4.2) and *f* is given as [168]:

$$f = l + 5(c_A^s c_B^s)^2 \tag{4.11}$$

where c^{s_A} and c^{s_B} are the surface fraction and can be defined as:

$$c_A^s = \frac{c_A V_A^{2/3}}{c_A V_A^{2/3} + c_B V_B^{2/3}} \tag{4.12}$$

$$c_B^{S} = \frac{c_B V_B^{2/3}}{c_A V_A^{2/3} + c_B V_B^{2/3}} \tag{4.13}$$

If extending the Miedema model to ternary systems, the enthalpy of formation of the solid solution have a similar form of that of the binary system and can be written as [162]:

$$\Delta H_{ABC} = \Delta H^c_{ABC} + \Delta H^e_{ABC} + \Delta H^s_{ABC}$$
(4.14)

$$\Delta H^c_{ABC} = \Delta H^c_{AB} + \Delta H^c_{AC} + \Delta H^c_{BC} \tag{4.15}$$

$$\Delta H^e_{ABC} = \Delta H^e_{AB} + \Delta H^e_{AC} + \Delta H^e_{BC} \tag{4.16}$$

and the enthalpy of formation of amorphous phase is:
$$\Delta H^{am}_{ABC} = \Delta H^c + X_A H^{a-s}_A + X_B H^{a-s}_B + X_C H^{a-s}_C \tag{4.17}$$

	0	7	
	Cu	Zr	11
φ(V)	4.45	3.45	3.80
n ws	3.18	2.80	3.51
V (×10-6m³/mol)	7.09	14.06	10.64
T_m (K)	1356	2125	1939
G (GPa)	45.13	34.14	39.34
K (GPa)	130.10	83.35	105.20

Table 4.1 Values of parameters needed to calculate the enthalpy of formation.

Table 4.2 The calculated chemical enthalpies and elastic enthalpies.

	∠H ^{chem} (KJ/mol)	∆H ^{elastic} (KJ/mol)
Cu in Zr	-78	62
Zr in Cu	-110	96
Cu in Ti	-33	21
Ti in Cu	-40	33
Zr in Ti	-1	15
Ti in Zr	-1	15

All the parameters used to calculate the enthalpy of formation are taken from Refs [162] and [169] and they are listed in **Table 4.1**. By applying equations (4.2) to (4.8), the chemical enthalpies and elastic enthalpies are calculated and listed in **Table 4.2**.

By applying equations (4.1) to (4.17), the enthalpies of formation of solid solution phase and amorphous phase of Zr-Cu-Ti ternary system are calculated and plotted in Figure 4.22 and Figure 4.23, respectively. Figure 4.24 shows the values of difference between Figure 4.22 and Figure 4.23. If the value of entropy of formation is considered as small enough to be ignored, the Gibbs free energy should equal to the enthalpy of formation. Thus the driving force of formation of amorphous phase should equal to the values of difference shown in Figure 4.24, where the influences from the binary or ternary intermetallics are ignored. It should be noticed that this result is only an approximated result; the modeling of the Gibbs free energy of Zr-Cu-Ti system is still an unsolved question. Therefore, the glass forming range in Zr-Cu-Ti ternary system is defined as where the value of the difference between the enthalpies of formation of solid solution phase and amorphous phase is positive [166]. The calculated glass forming range can be shown as Figure 4.25. It shows the glass forming range is quite wide, which covers from 15 at% to 95 at% of Cu, from 0 at% to 85 at% of Zr and from 0 at% to 70% of

Ti.

129



Figure 4.22 Color map of the calculated enthalpy of formation of solid solution phase in Zr-Cu-Ti ternary system. The unit is KJ/mol.



Figure 4.23 Color map of the calculated enthalpy of formation of amorphous phase in Zr-Cu-Ti ternary system. The unit is KJ/mol.



Figure 4.24 Color map of the approximated driving force of formation of amorphous phase for the Zr-Cu-Ti ternary system. The unit is KJ/mol.



Figure 4.25 The calculated glass forming range in Zr-Cu-Ti ternary system.

This resulting ternary glass forming range is much wider than the experimental determined one [98, 151, 170, 171]. For the binary Cu-Ti and Zr-Cu systems, the calculated glass forming range covers from 30 at% Cu to 80 at % Cu in Cu-Ti system and from 5 at% to 85 at% Zr in Zr-Cu system. These are in agreement to the reported glass forming range in these two systems: from 28 at% to 75 at% Cu in Cu-Ti system [172, 173] and from 10 at% to 75 at% of Zr in Zr-Cu system [94].

It is believed that the enthalpy of mixing, or the enthalpy of chemical, plays an important role in the glass formation [9, 64, 159, 174]. It suggests that a larger negative enthalpy of mixing among the elements can lead to a better glass forming ability. Therefore, the enthalpy of mixing for the Zr-Cu-Ti ternary system is also calculated and shown in **Figure 4.26**. It shows that the large negative enthalpy of mixing can be found at compositions with 30 at% to 60 at% of Zr, 50 at% to 70 at% of Cu and 0 at% to 10 at% of Ti. This composition range is consistent with the reported compositions which can form bulk metallic glass in this Zr-Cu-Ti system: Cu₆₀Zr_{40-x}Ti_x, where x=0-40 at% [101] and compositions near Cu₅₂Zr₄₀Ti₈ [103]. Moreover, among the corresponding binary systems, Zr-Cu system has the relatively largest negative enthalpy of mixing and the best glass forming ability, followed by Cu-Ti system. The Zr-Ti system has no glass forming ability at all.

It should be noticed that the Cu₂ZrTi phase is treated as solid solution during the calculation in this section, which is based on the experimental result that the Cu₂ZrTi phase covers a wide composition range.



Figure 4.26 Color map of the calculated enthalpy of mixing (enthalpy of chemical) for the Zr-Cu-Ti ternary system. The unit is KJ/mol.

4.5 Conclusion

In this chapter, the glass formation of two composition ranges in Zr-Cu-Ti system has been studied. Miedema model was used to calculate the enthalpy of mixing, enthalpy of elastic, enthalpy of formation and glass formation range. The followings are the conclusions:

- (1) For the compositions from Cu_{52.5}(ZrTi)_{47.5} to Cu₄₇(ZrTi)₅₃ (Ti = 5 at%), the phenomenon of intermetallic glass still can be observed as two optimum glass formers Cu_{51.5}(ZrTi)_{48.5} and Cu₄₈(ZrTi)₅₂ are separated by composition Cu₅₁(ZrTi)₄₉. The critical size reaches to 3 mm by the Ti addition. Cu₁₀Zr⁷ phase was stabilized by Ti and precipitated with CuZr phase during the cooling.
- (2) For the compositions nearby Cu₂ZrTi, the phenomenon of intermetallic glass is not clear enough. The critical sizes fluctuated from ~300 μm to 600 μm. The liquidus temperature changes slowly with the changing of composition. A wide composition range was proved to be covered by Cu₂ZrTi intermetallic.
- (3) The Miedema model was used to calculate the glass forming range for

Zr-Cu-Ti system. The resulting glass forming range covers from 15 at% to 95 at% of Cu, from 0 at% to 85 at% of Zr and from 0 at% to 70% of Ti. Also the enthalpy of mixing (chemical) was calculated and the possible composition range with good glass forming ability was suggested.

Chapter 5

Conclusion

5.1 Summary of results

This dissertation has explored the phenomenon of formation of intermetallic glass in binary and ternary systems, the relationship between the glass forming ability of intermetallic glass and the crystallization driving force or the temperature dependant viscosity. Also the possible glass forming range in ternary system has been studied. The major results are summarized as follows:

(1) The glass formation near Cu₅₁Zr₁₄, Cu₈Zr₃, Cu₁₀Zr₇ and CuZr₂ intermetallics

has been systemically studied. Intermetallic glasses can be easily located near almost all intermetallic compounds in the Cu-Zr binary system. Two optimum intermetallic glass formers were located near but separated by $(Cu_{51}Zr_{14},$ the corresponding intermetallic $Cu_{10}Zr_7$ and $CuZr_2$ intermetallics), respectively. The result shows that glass formed near Cu₁₀Zr₇ intermetallic has the a maximum critical thickness of 520 µm, followed by glass near CuZr₂ intermetallic with 470 µm critical thickness and glass near Cu₅₁Zr₁₄ intermetallic with less than 15 μ m critical thickness. Due to the fact that Cu₈Zr₃ intermetallic is a peritectic phase, only one optimum glass former was found near it.

- (2) The Gibbs free energy as a function of composition of liquid and intermetallic phases is calculated by CALPHAD method at different temperatures. All the crystallization driving forces at compositions $Cu_{51}Zr_{14}$, $Cu_{10}Zr_7$, CuZr and $CuZr_2$ are also calculated under their corresponding T_8 or T_x temperatures. According to the relationship between the maximum critical thickness of the intermetallic glass and the crystallization driving force of the corresponding intermetallic, a smaller crystallization driving force is related to a better glass forming ability.
- (3) The nature of formation of intermetallic glasses was explained from both thermodynamic and kinetic perspectives. Thermodynamically, it is 139

proposed that the Gibbs free energy of intermetallic rises sharply near intermetallic composition. The liquid phase has a lower Gibbs free energy when the composition shifts slightly from the intermetallic compound. Thus two thermodynamically favored glass forming ranges are present, when the formation of neighbor primary phases was kinetically suppressed under quenching. Kinetically, it is surprisingly found that the two optimum glass formers near intermetallic compound have lower critical cooling rates (which lead to a better glass forming ability) than that of the corresponding intermetallic compound. This provides a kinetic evidence of the formation of intermetallic glass. The changing of critical cooling rate in such a narrow composition range can be considered as an evidence of the sharp profile of the Gibbs free energy of the intermetallic phase.

(4) The formation of intermetallic glass was also studied in Zr-Cu-Ti ternary system. Based on the glass formation near CuZr intermetallic in binary system, the glass formation of the compositions from Cu_{52.5}(ZrTi)_{47.5} to Cu₄₇(ZrTi)₅₃ (Ti = 5 at%) was studied. The phenomenon of formation of intermetallic glass still can be observed as two optimum glass formers Cu_{51.5}(ZrTi)_{48.5} and Cu₄₈(ZrTi)₅₂ are located near but separated by composition Cu₅₁(ZrTi)₄₉ in both 3 mm and 5 mm rods. The critical size is improved to 3 mm by adding Ti element into Zr-Cu system. Cu₁₀Zr₇ phase 140

was stabilized by Ti and precipitated along with CuZr phase in this composition range.

- (5) Glass formation in the composition range of Cu₂ZrTi ternary intermetallic phsae, or Laves phase, was also studied. The phenomenon of intermetallic glass is not clear enough. The critical sizes of the wedge cast samples fluctuated from ~300 µm to 600 µm without consistently trend. Cu₂ZrTi (Cu₅₀Zr₂₅Ti₂₅) was discovered to have a critical thickness of 600 µm, which is larger than that of eutectic glass Ti₃₅Zr₁₀Cu₅₅. Furthermore, the liquidus temperature in this composition range changes slowly with the changing of composition. Along with the XRD results of the crystalline parts of all the samples, it reveals that Cu₂ZrTi intermetallic covers a wide composition range more than 10 at%.
- (6) The Miedema model was used to calculate the glass forming range in Zr-Cu-Ti ternary system. The resulting glass forming range covers from 15 at% to 95 at% of Cu, from 0 at% to 85 at% of Zr and from 0 at% to 70% of Ti, which is much wider than reported experimental glass forming range. Also the enthalpy of mixing (chemical) was calculated and the possible composition range with good glass forming ability (compositions with 30 at% to 60 at% of Zr, 50 at% to 70 at% of Cu and 0 at% to 10 at% of Ti) was suggested.

5.2 Future work

This thesis demonstrates the experimental phenomenon and underlying mechanism of formation of intermetallic glass. However, the intermetallic glass is a new family of metallic glasses, there are more work needed to do. Based on the current results and understanding, the following points are raised for future work:

- (1) In binary system, the intermetallic phases selected in this thesis are all line compounds with no solubility. Also, the investigation of glass formation in Cu₂ZrTi phase did not show convincing evidence of existence of intermetallic glass. Therefore, binary intermetallic phase with limited solubility would be a great choice to study whether the phenomenon of formation of intermetallic glass is present.
- (2) The phenomenon of formation of intermetallic glass makes a challenge for the modeling of the structure of metallic glass. The glass forming ability is sharply dependant on the composition in such a narrow composition range. There is no method to modeling the structure of intermetallic glass so far. Knowing the structure of intermetallic glass would help the further investigation.

(3) It would be interesting to study the mechanical property of intermetallic glass. Since intermetallic glass has different glass forming range from eutectic glasses, whether they show similar mechanical property is still open to question.

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